



Continuous magnetic spectra in absence of quasiparticle fractionalization

Martin Mourigal

School of Physics, Georgia Institute of Technology, Atlanta, USA



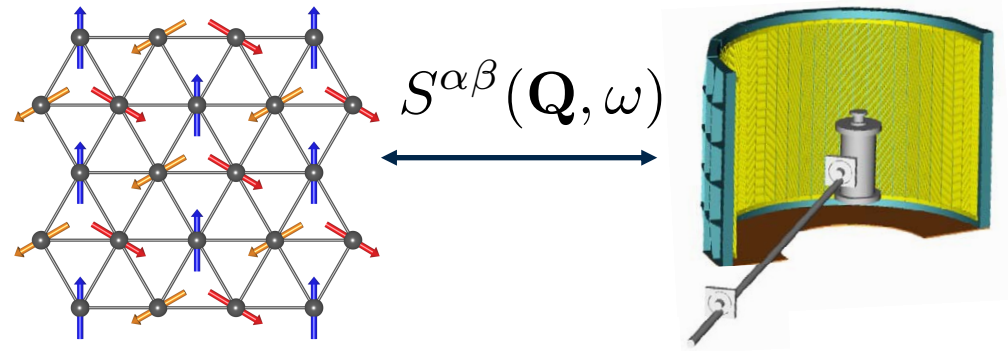
U.S. DEPARTMENT OF
ENERGY

Award DE-SC-0018660

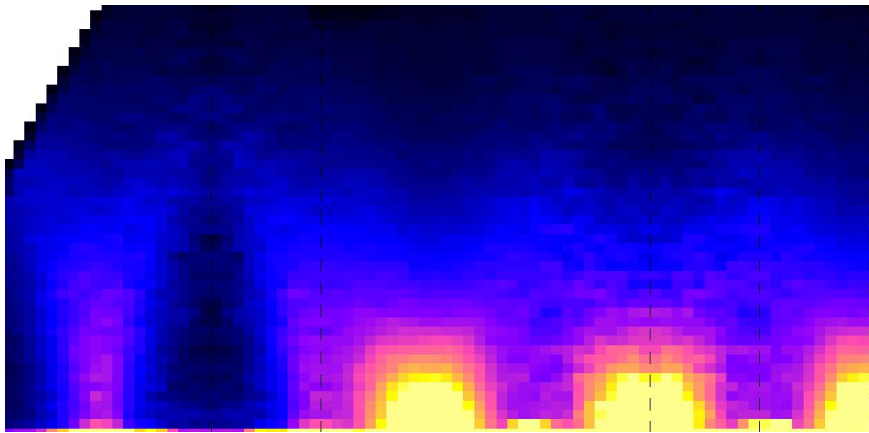
TOPOQUANT
KITP, Santa Barbara
October 14, 2019

Outline

1. Introduction and neutron scattering warm-up

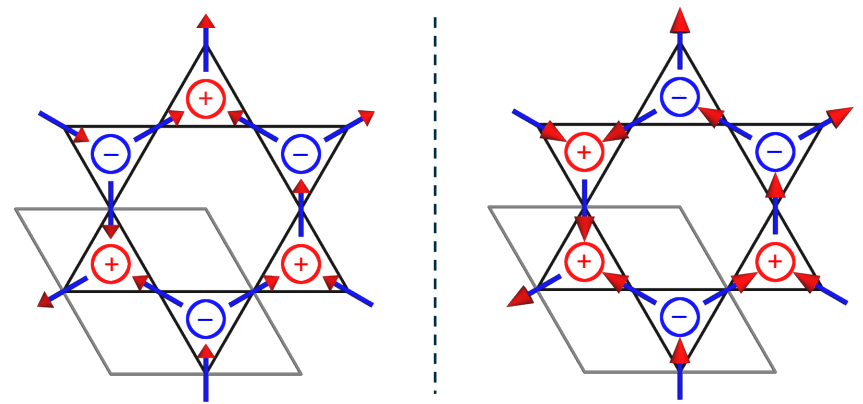


2. Nature of excitations in the classical pyrochlore Heisenberg AFM MgCr_2O_4



Bai *et al.* Phys. Rev. Lett. **122**, 097201 (2019)

2. Kagome spin-ice physics in the tripod compounds $\text{Ln}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$



Paddison *et al.*, Nat. Commun. **7**, 13842 (2016)
Dun *et al.*, arXiv:1806.04081 (2019) + in prep.

Magnetic quantum matter in Mott insulators

- The foundations of quantum magnetism:

$$\mathcal{H} = \sum_{(ij)} \hat{\mathbf{S}}_i J_{ij} \hat{\mathbf{S}}_j$$

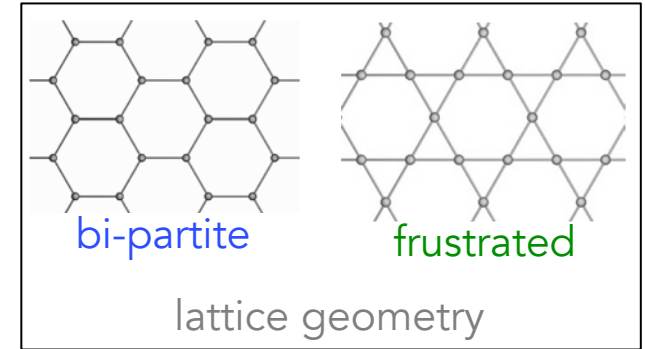
magnetic system

J_{ij}

lattice-space

spin-space

$\hat{\mathbf{S}}$

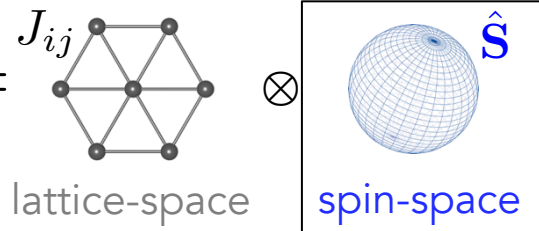


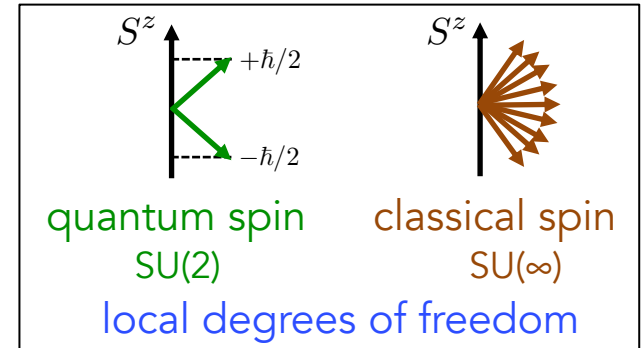
Magnetic quantum matter in Mott insulators

□ The foundations of quantum magnetism:

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magnetic system



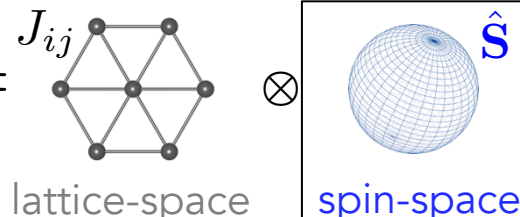


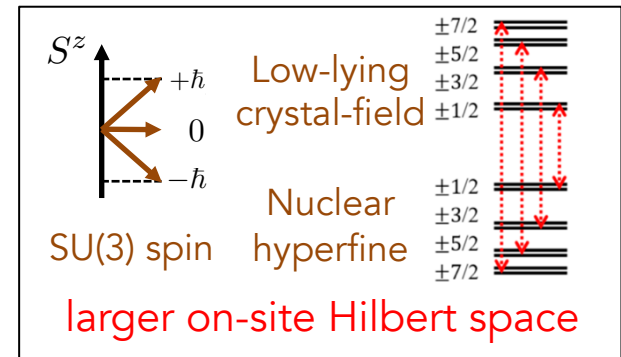
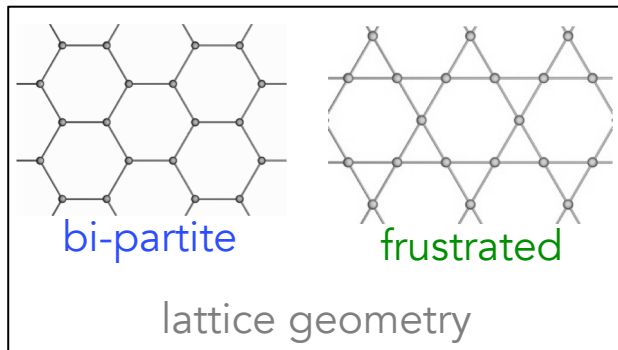
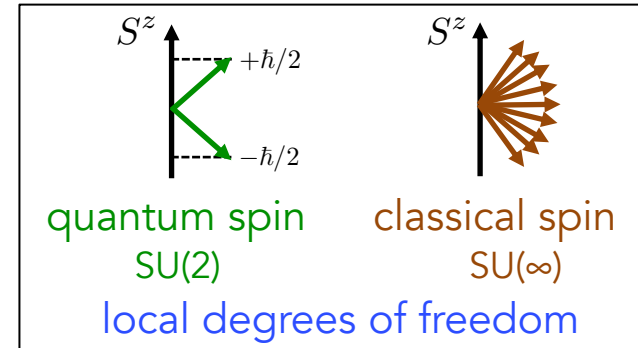
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magnetic system

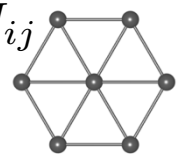
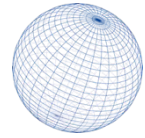




Magnetic quantum matter in Mott insulators

- The foundations of quantum magnetism:

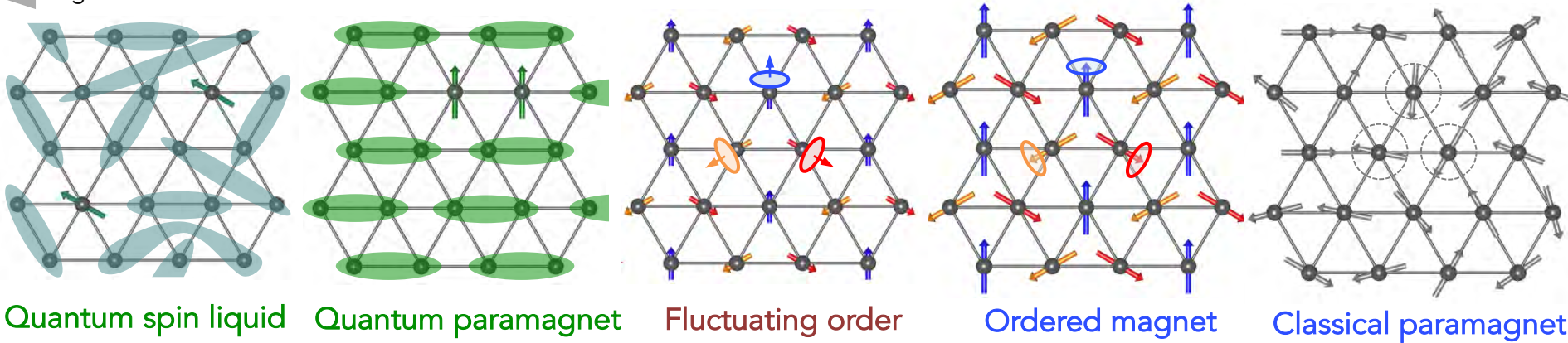
$$\mathcal{H} = \sum_{(ij)} \hat{\mathbf{S}}_i J_{ij} \hat{\mathbf{S}}_j = \text{magnetic system} \otimes \text{spin-space}$$

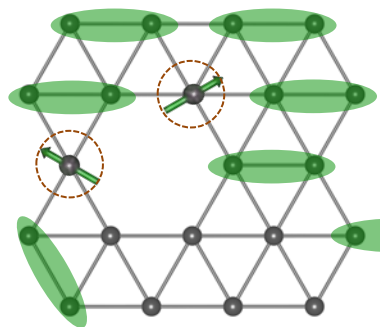
magnetic system
lattice-space
spin-space

- Clean magnetic phases and their excitations:

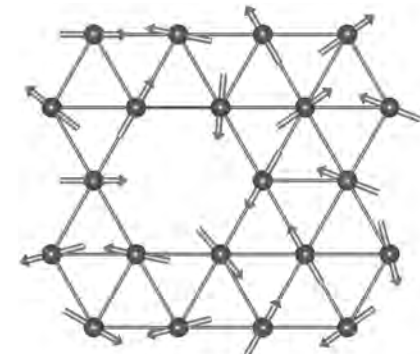
← Entanglement



- Extra challenge from chemical heterogeneities/disorder:



Valence Bond Glass



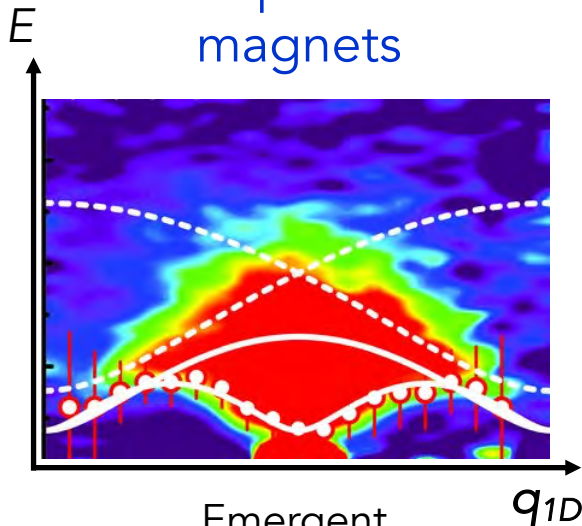
Spin Glass

The quest for a quantum spin-liquid

Experimentalist view:



1D quantum magnets

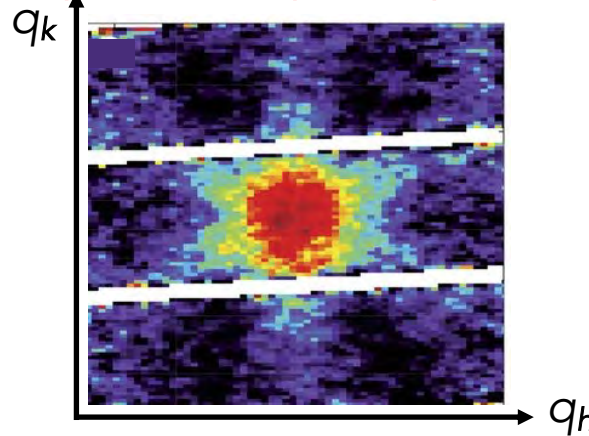


Emergent antiferromagnetic chains in metallic $\text{Yb}_2\text{Pt}_2\text{Pb}$

Wu *et al.*,
Science **352**, 1206 ('16)

Continuous in energy

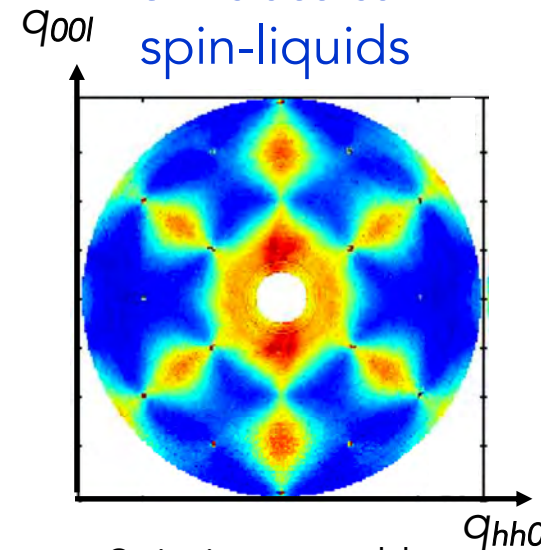
2D and 3D quantum spin-liquids



Kitaev honeycomb
Banerjee *et al.*, *Science* **356**, 1055 ('17)
Heisenberg kagome
Han *et al.*, *Nature* **492**, 406 ('12)
Distorted bilayer kagome
Balz *et al.*, *Nature Physics* **12**, 942 ('16)

Continuous response in both momentum & energy

3D classical spin-liquids



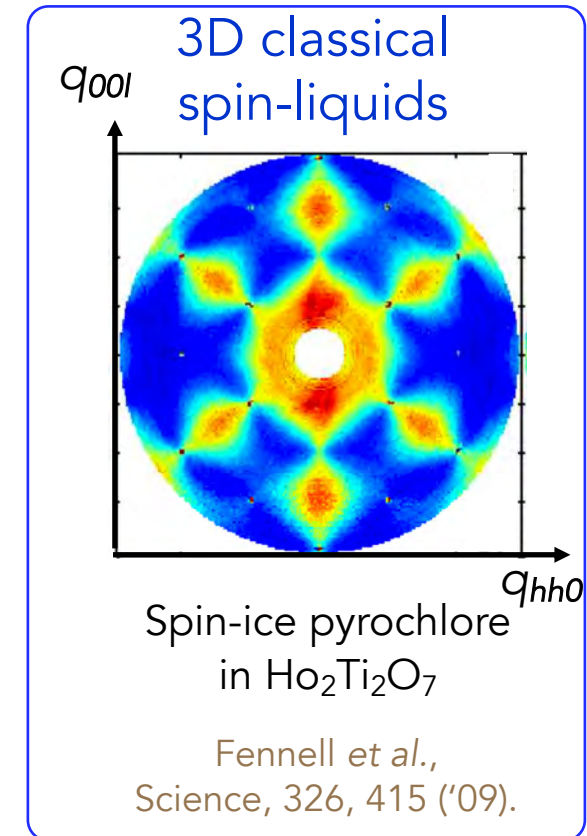
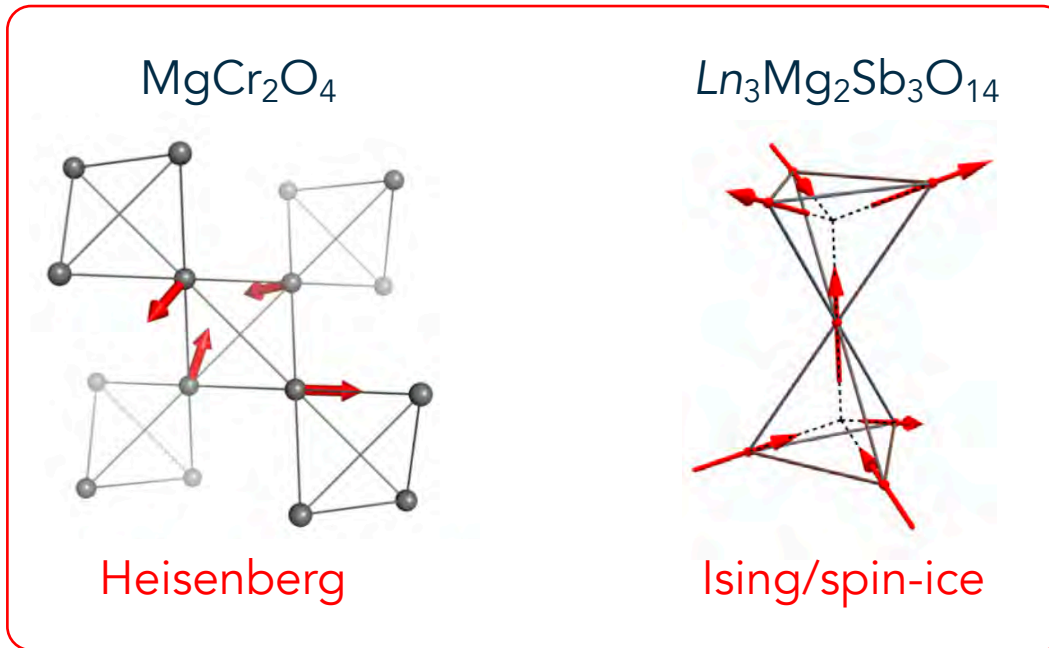
Spin-ice pyrochlore in $\text{Ho}_2\text{Ti}_2\text{O}_7$

Fennell *et al.*,
Science, **326**, 415 ('09).

Continuous in momentum

The quest for a quantum spin-liquid

Experimentalist view:

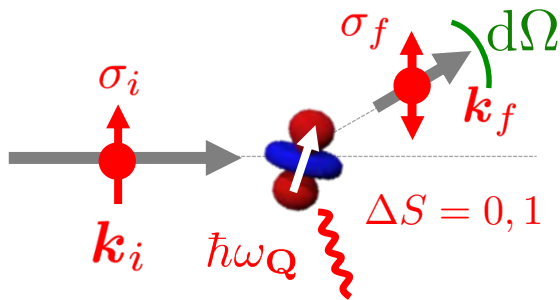


General question:

In general, a continuous excitation spectrum is not enough to conclude on fractional excitations. So how to discover a quantum spin-liquid?

Technique: Neutron Scattering

- Magnetic Scattering: ideal but weak thus requires "large" samples



$$\frac{d^2\sigma}{dE_f d\Omega} \Big|_{\text{mag}} = \frac{k_f}{k_i} r_0^2 \underbrace{|gf(\mathbf{Q})|^2}_{\text{magnetic form-factor}} \sum_{\alpha\beta} (\delta_{\alpha\beta} - \hat{Q}_\alpha \hat{Q}_\beta) \underbrace{\mathcal{S}^{\alpha\beta}(\mathbf{Q}, \omega)}_{\text{dynamic structure-factor}}$$

measured cross-section

$$\mathbf{Q} = \mathbf{k}_i - \mathbf{k}_f$$

$$\hbar\omega = \frac{\hbar^2(\mathbf{k}_i^2 - \mathbf{k}_f^2)}{2m_n}$$

$$\Delta S = \sigma_i - \sigma_f$$

Conservation laws

$$\underbrace{\mathcal{S}^{\alpha\beta}(\mathbf{Q}, \omega)}_{\text{dynamic s.f.}} = \frac{1}{2\pi\hbar} \int dt e^{-i\omega t} \frac{1}{N} \sum_{\mathbf{r}\mathbf{r}'} e^{-i\mathbf{Q}\cdot(\mathbf{r}-\mathbf{r}')} \underbrace{\langle S^\alpha(\mathbf{r}, t) S^\beta(\mathbf{r}', 0) \rangle}_{\text{dynamic pair correlations}}$$

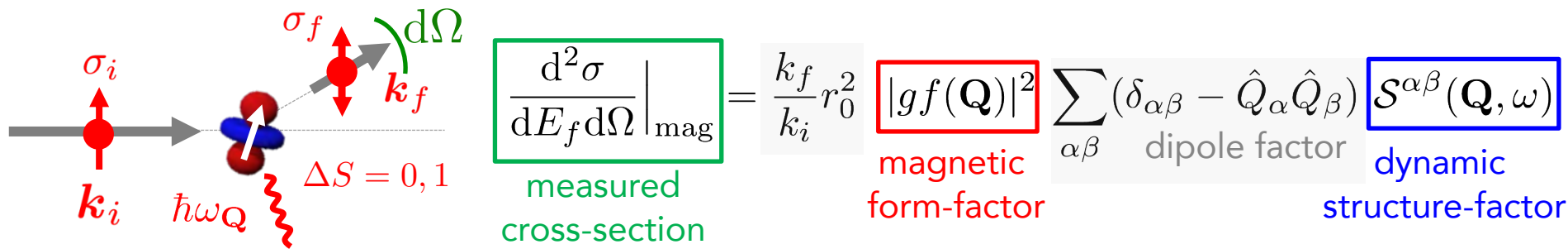
Fourier transform

$$\underbrace{\mathcal{S}^{\alpha\beta}(\mathbf{Q})}_{\text{instantaneous s.f.}} = \int \mathcal{S}^{\alpha\beta}(\mathbf{Q}, \omega) d\omega = \frac{1}{N} \sum_{\mathbf{r}\mathbf{r}'} e^{-i\mathbf{Q}\cdot(\mathbf{r}-\mathbf{r}')} \langle S^\alpha(\mathbf{r}) S^\beta(\mathbf{r}') \rangle$$

instantaneous pair correlations

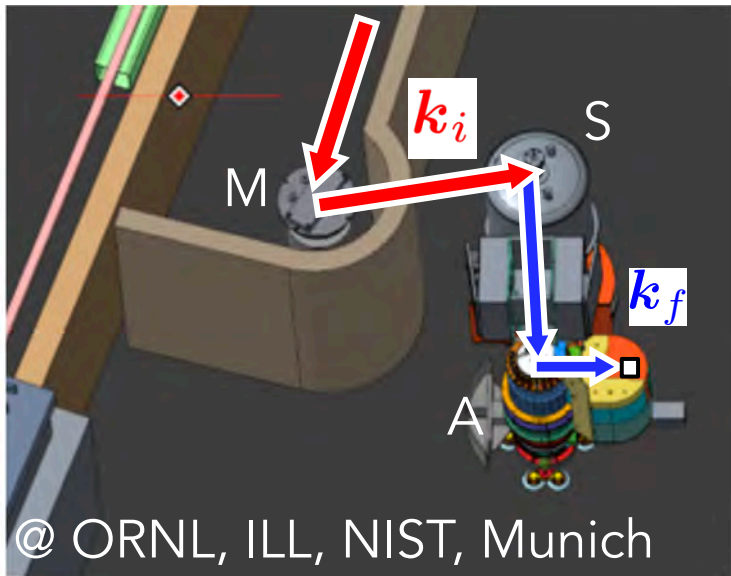
Technique: Neutron Scattering

- ❑ Magnetic Scattering: ideal but weak thus requires "large" samples



- ❑ Instrumentation: designed to detect a broad Q-E response

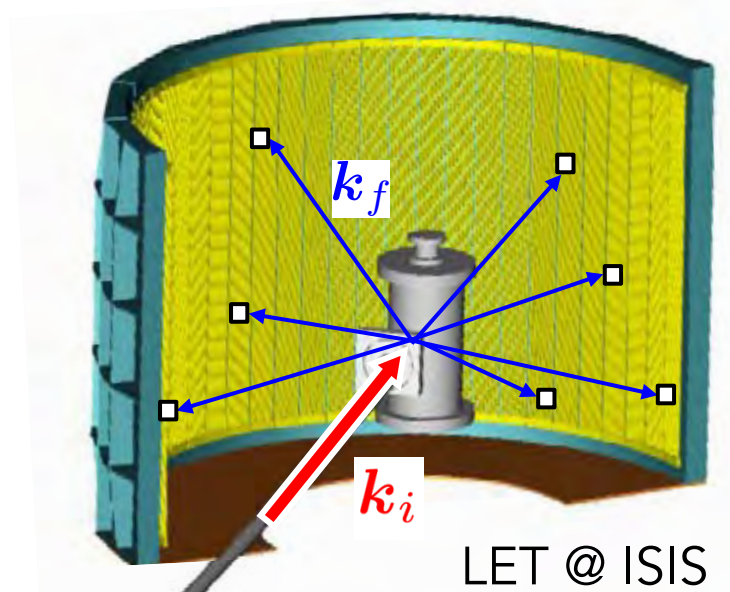
Triple-axis (TAS)



@ ORNL, ILL, NIST, Munich

Point by point detection

Time-of-flight (TOF)

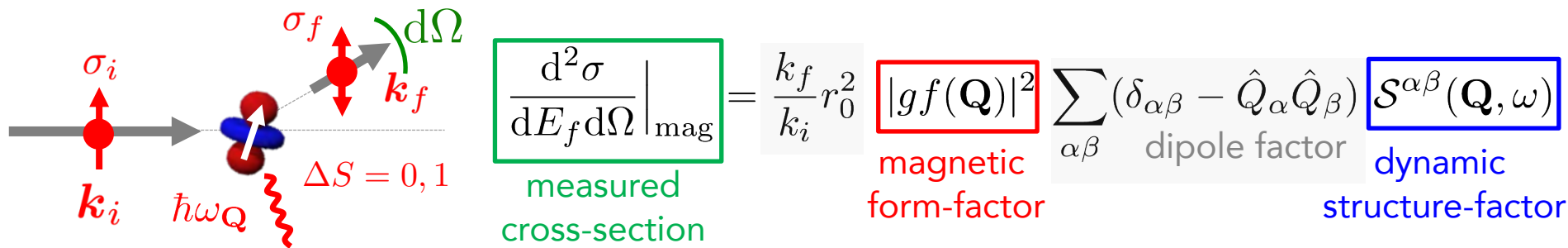


LET @ ISIS

Massively parallelized detection but lot of deadtime

Technique: Neutron Scattering

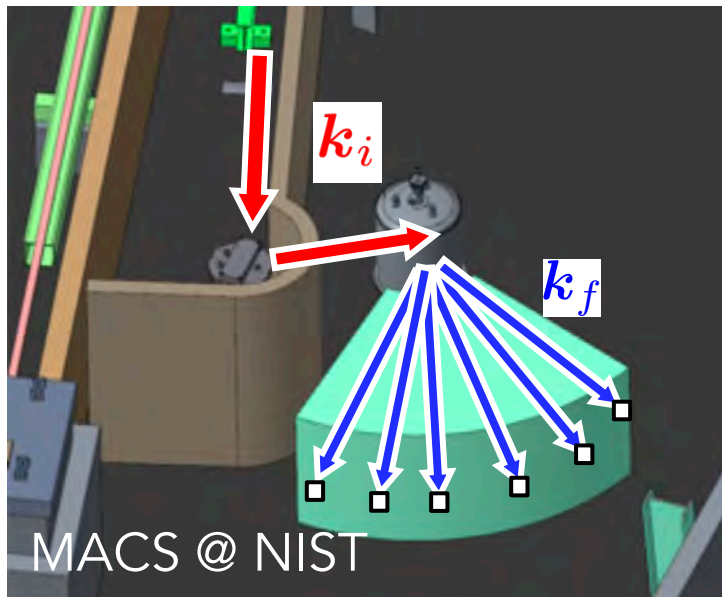
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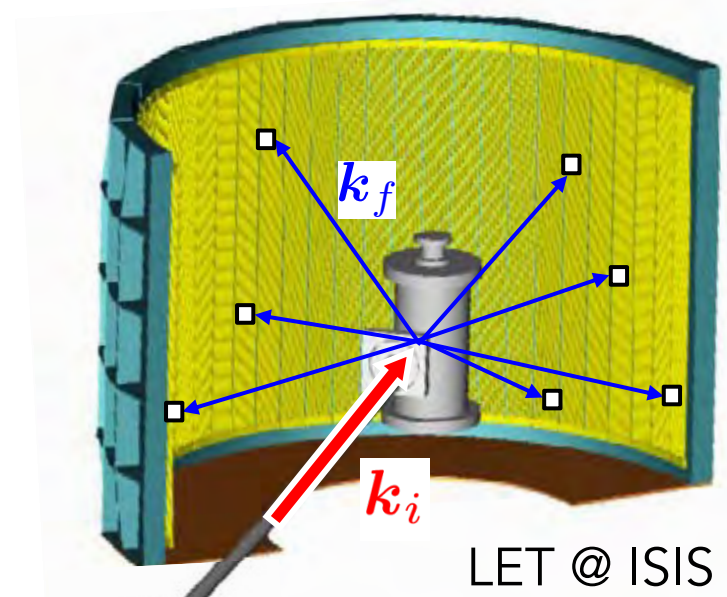
- ❑ Instrumentation: designed to detect a broad Q-E response

Multiplexed triple-axis (TAS)

Time-of-flight (TOF)



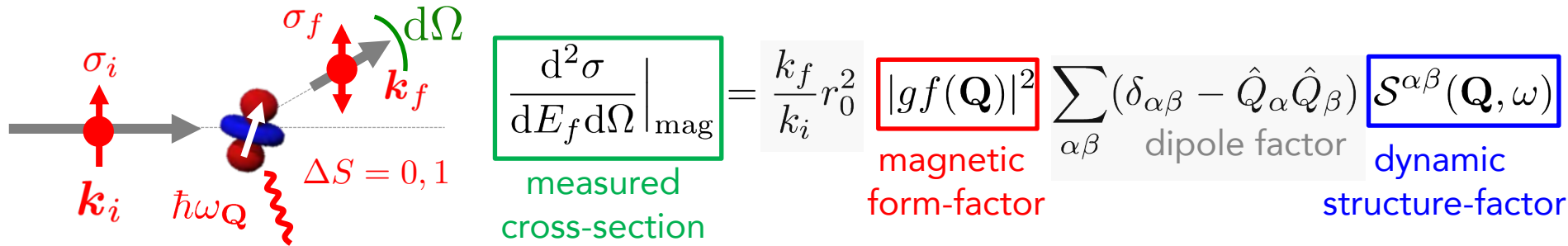
Plane by plane detection
Focusing optics



Massively parallelized detection
but lot of deadtime

Technique: Neutron Scattering

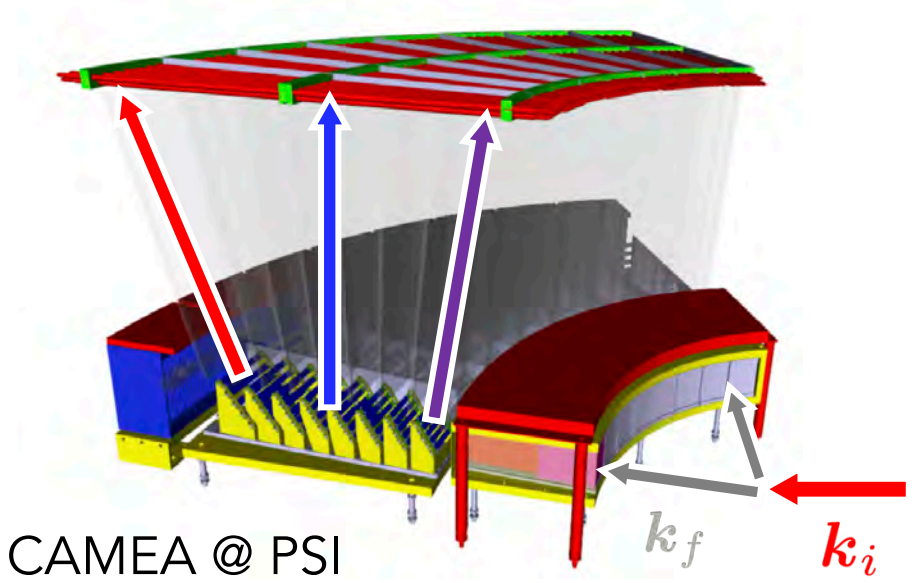
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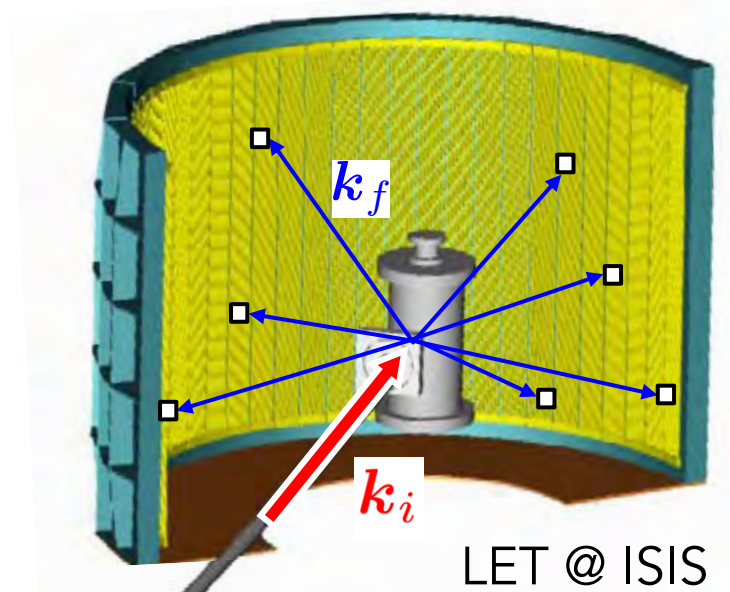
Multiplexed² triple-axis (TAS)

Time-of-flight (TOF)



CAMEA @ PSI

Prismatic detection
Focusing optics



LET @ ISIS

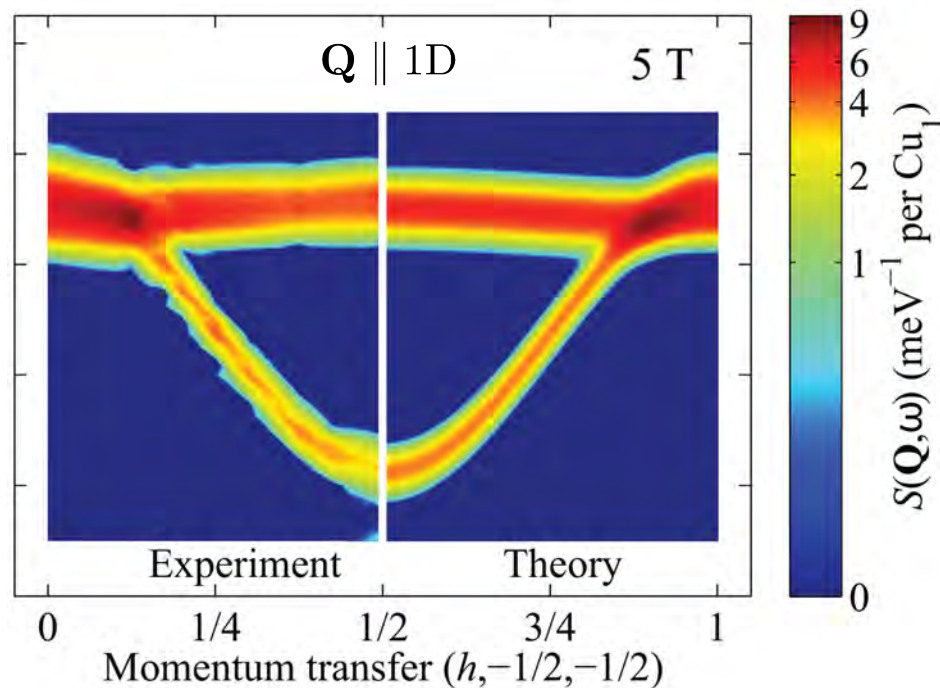
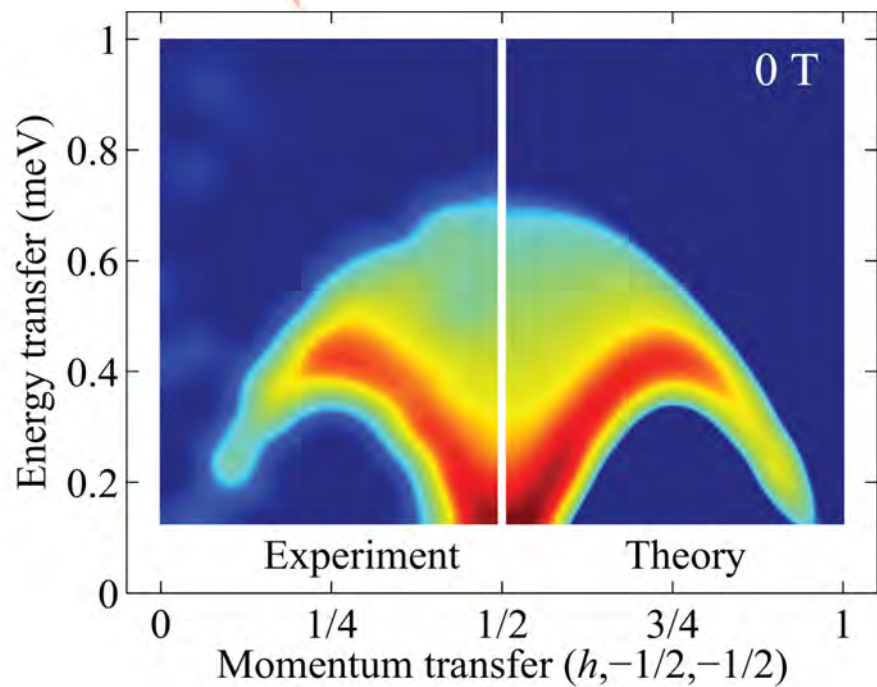
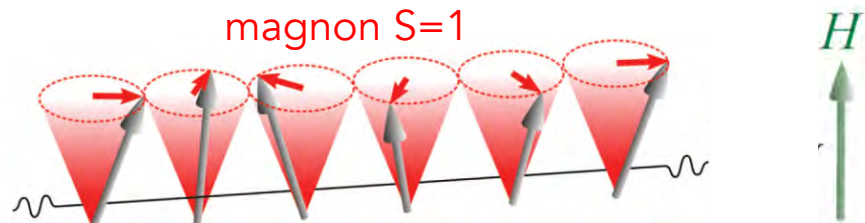
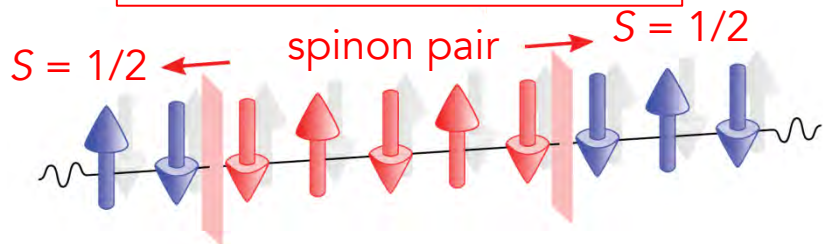
Massively parallelized detection
but lot of deadtime

Spin liquid vs Ordered magnet – What to expect

□ 1D chains in $\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$ ($H_s = 3.4\text{T}$)

Entangled ground-state
Fractional excitations
Continuous spectra

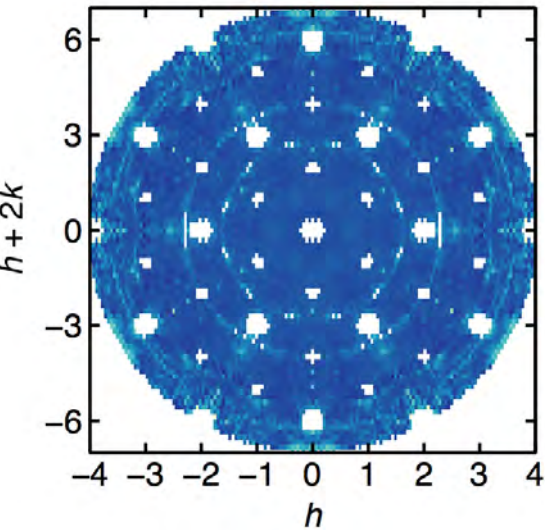
Ordered ground-state
Spin-wave excitations
Sharp spectra



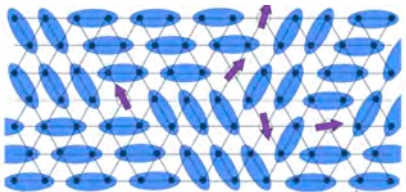
Spin liquid vs Random singlets – The unexpected

□ Rare-earth triangular in $\text{Yb}(\text{MgGa})\text{O}_4$ ($H_s \sim 5.0\text{T}$)

Continuous spectra
in both 0T and 7.8T

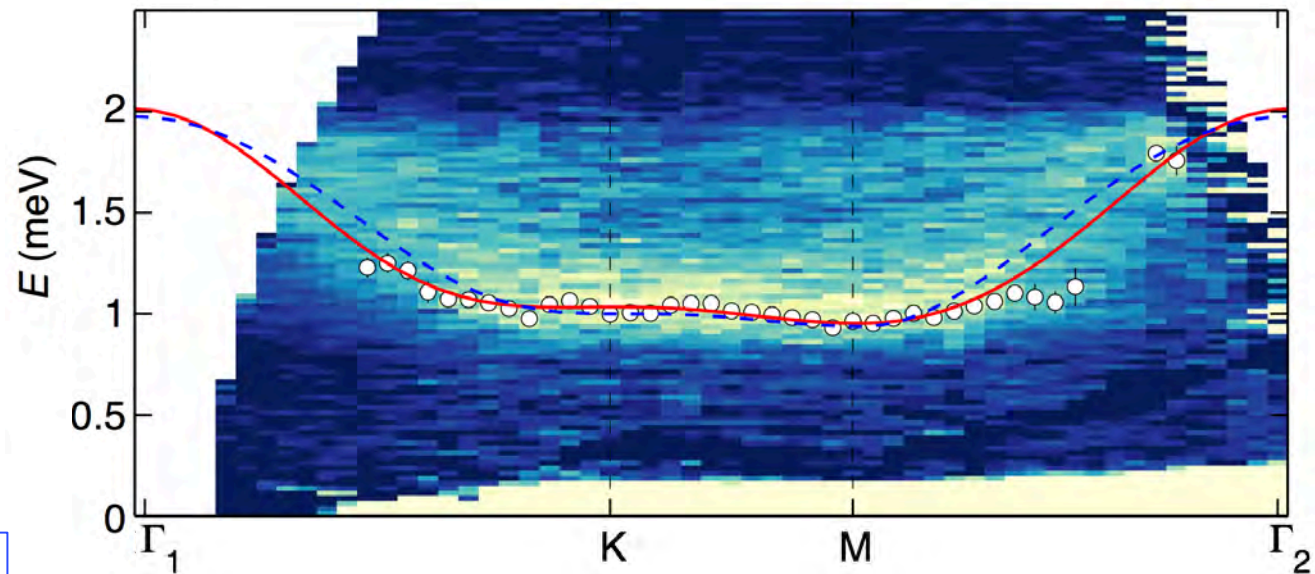
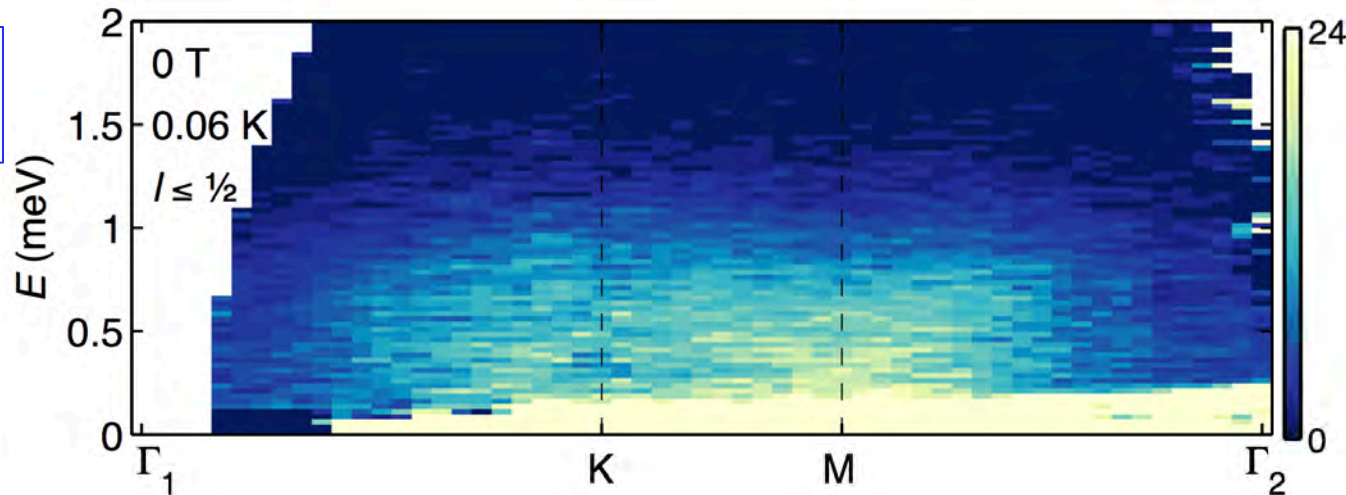


Structural Diffuse Scattering



Kimchi, Senthil PRX'18
Tsirlin, Gegenwart PRL'19

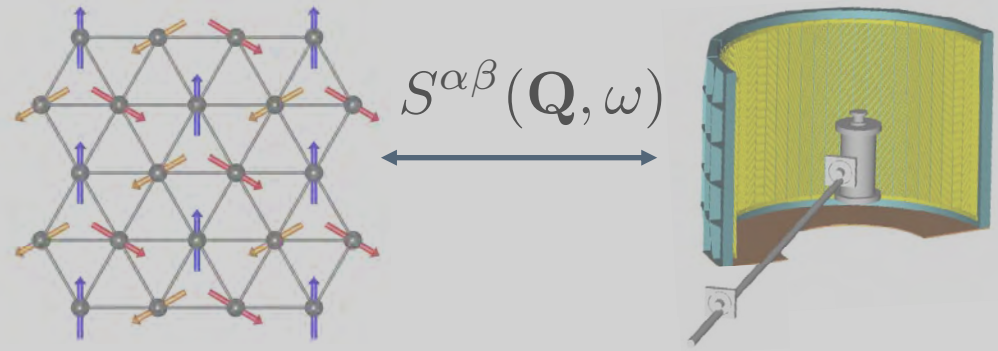
Correlated disorder
Random valence bonds?



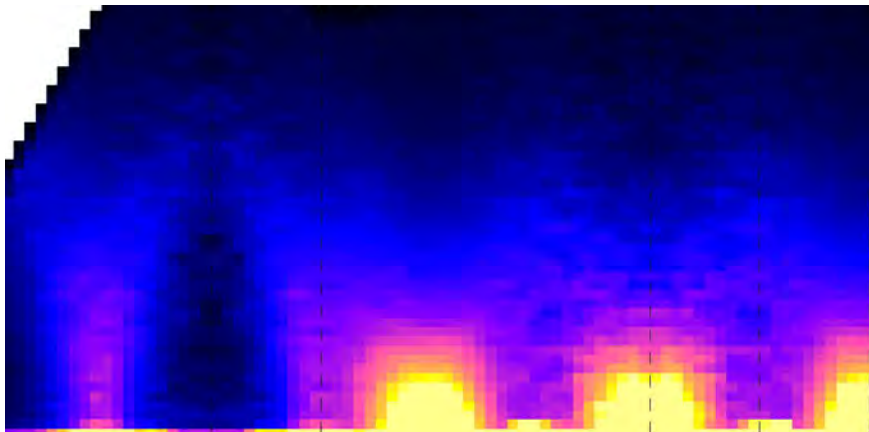
Paddison, Dun, Daum, Zhou, Mourigal, Nature Physics 13, 117 (2017)

Outline

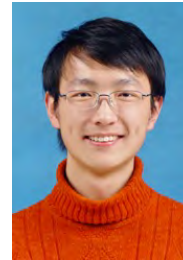
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2. Nature of excitations in the classical pyrochlore Heisenberg AFM MgCr_2O_4



Bai *et al.* *Phys. Rev. Lett.* **122**, 097201 (2019)



Xiaojian
Bai



Seyed
Koohpayeh



Eliot
Kapit



John
Chalker



Siân
Dutton



Joe
Paddison



Jiajia
Wen

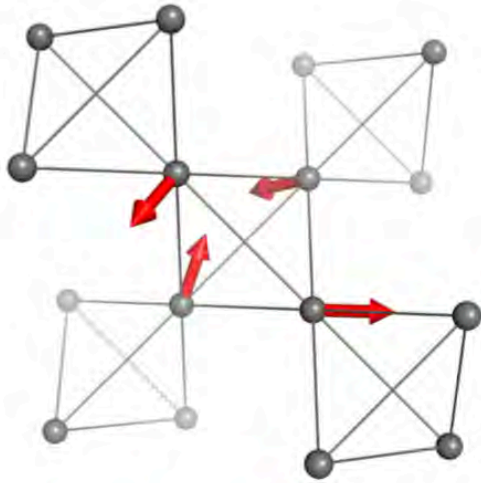


Collin
Broholm

Garrett Granroth (ORNL), Ovi Garlea (ORNL), Andrei Savici (ORNL), Sasha Kolesnikov (ORNL)

Large- S pyrochlore Heisenberg antiferro.

□ A paradigmatic classical spin-liquid model:



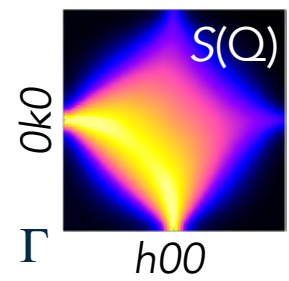
Large spins
($n \rightarrow \infty$ components)

$$H = J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j \equiv \frac{J}{2} \sum_{\alpha} |\mathbf{L}_{\alpha}|^2 + \text{cte} \quad \mathbf{L} = \sum_{i=1}^4 \mathbf{S}_i$$

nearest-neighbor interaction \nearrow \nwarrow spins are under-constrained!
 \nwarrow rewrite as sum over tetrahedra



extensive degeneracy

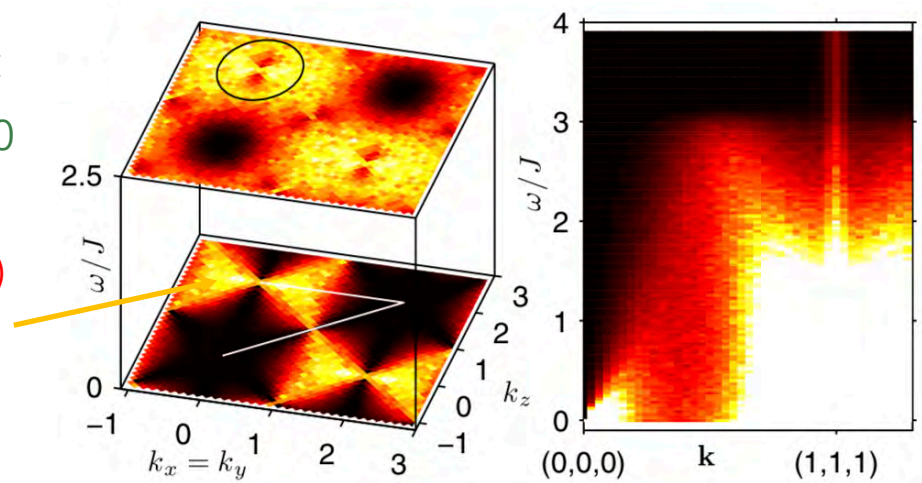


Correlations decay algebraically in real space such that sharp pinch-points appear in reciprocal space. An example of a Coulomb Phase.

Anderson 1956, Villain 1979, Reimers 1992, Moessner & Chalker 1998, Henley 2011

□ Dynamics is very rich:
molecular dynamics $T \sim J/500$

zero-energy (quasi-elastic) spectral weight

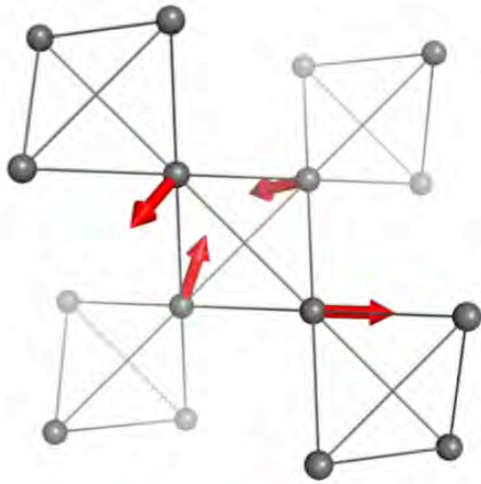


Relaxational
Precessional
Diffusive

Conlon and Chalker PRL 2009

Large- S pyrochlore Heisenberg antiferro.

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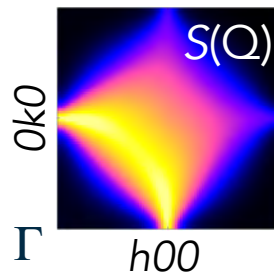
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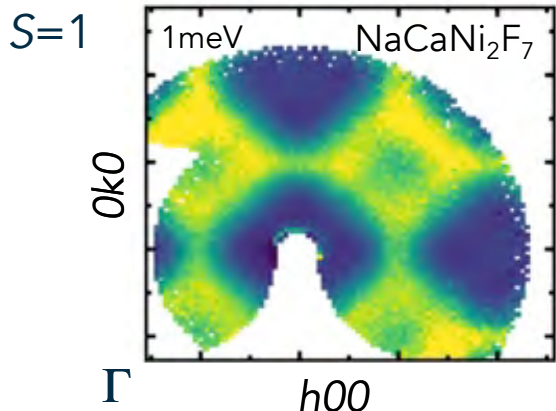
extensive degeneracy



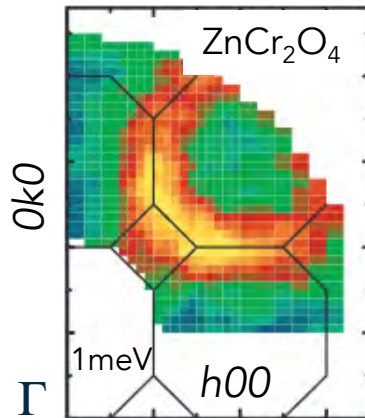
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Anderson 1956, Villain 1979, Reimers 1992, Moessner & Chalker 1998, Henley 2011

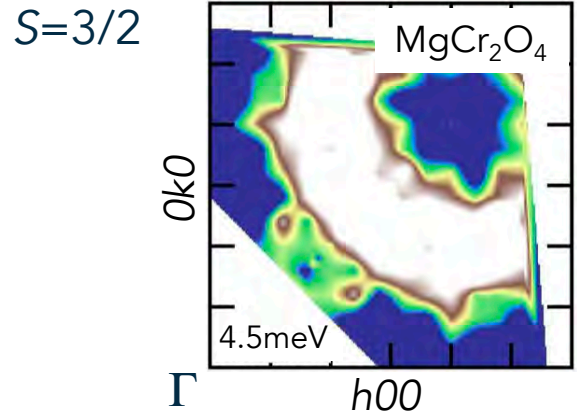
□ Approximated e.g. by $\text{NaA}'\text{B}_2\text{F}_7$ pyrochlore fluorides and cubic spinels AB_2O_4



Plumb et al. Nature Physics 2019



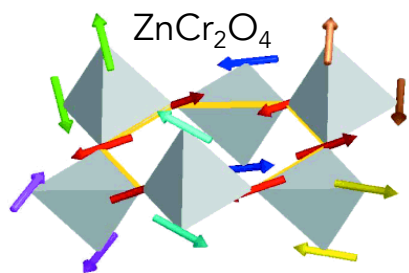
S.H. Lee et al. Nature 2002



Tomiyasu et al., PRL 2008 17

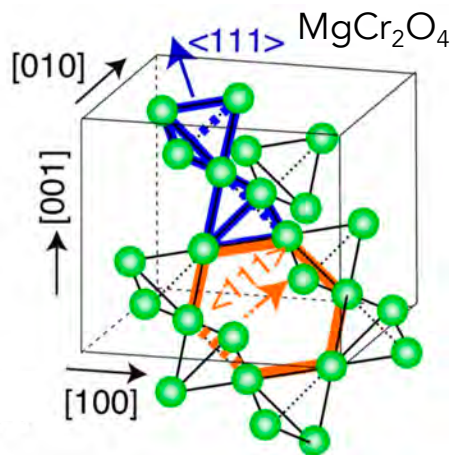
Loop Scattering in Spinel

□ Absent pinch-points & excitations in ordered phase: emergent spin clusters?



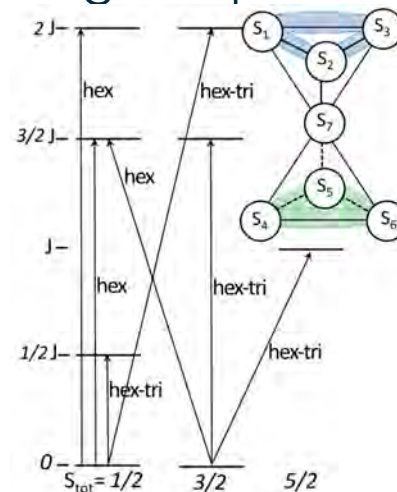
Hexamers

Tchernyshyov 2002
S.H. Lee *et al.* Nature 2002



Molecular spin resonances

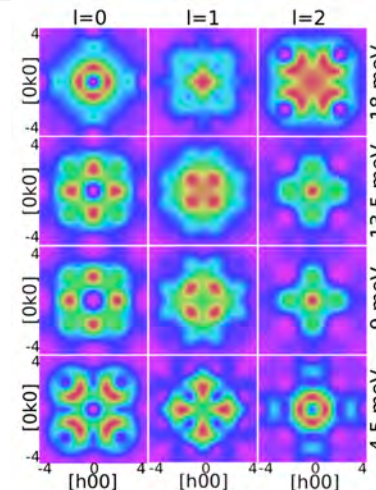
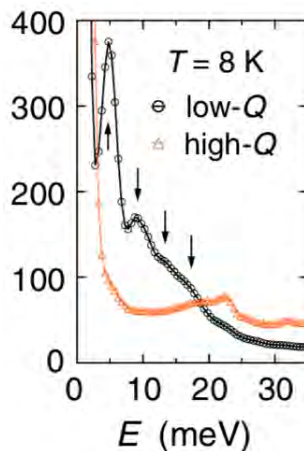
Tomiyasu PRL 2008
Tomiyasu PRL 2012



Heptamers

Gao PRB 2018
Haraldsen PRB 2018

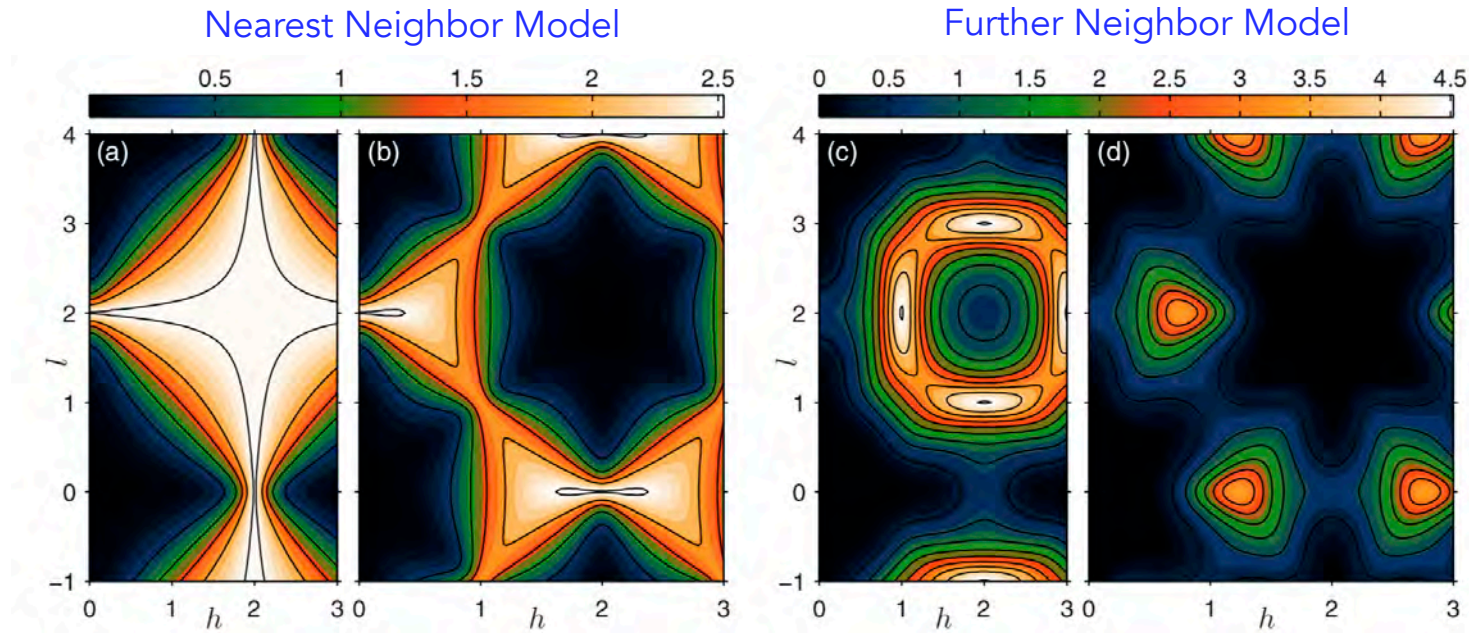
Loop inflation



Motivation: different clusters to explain magnetic resonances in the ordered phase and their momentum dependence

What is the origin of the loop scattering?

- Theoretical work by Conlon & Chalker attributing it to further-neighbor ex.



Conlon and Chalker, PRB 2010

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- ❑ Theoretical work by Conlon & Chalker attributing it to further-neighbor ex.
- ❑ MgCr_2O_4 : grew and co-aligned ~14 grams of single-crystals



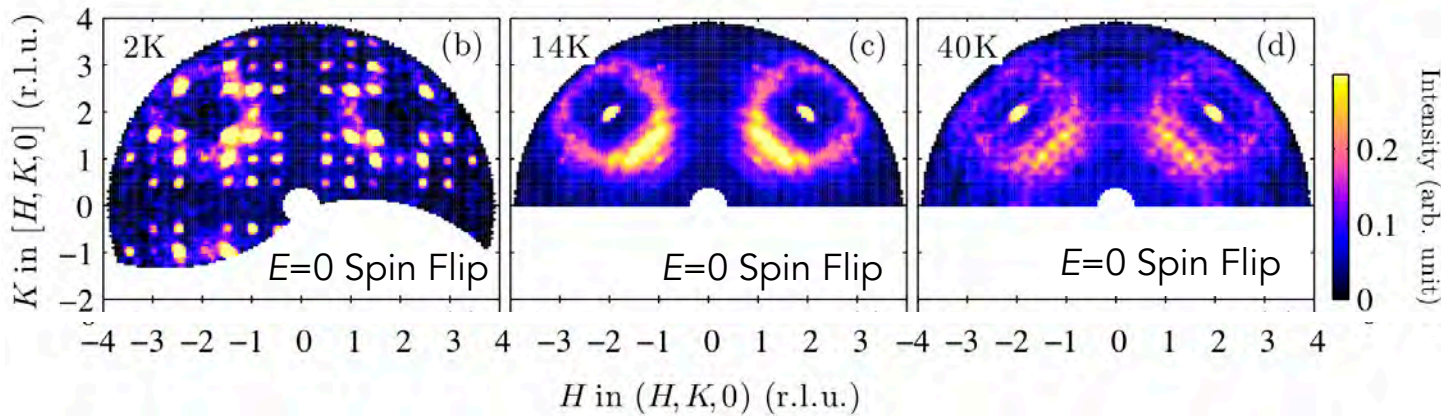
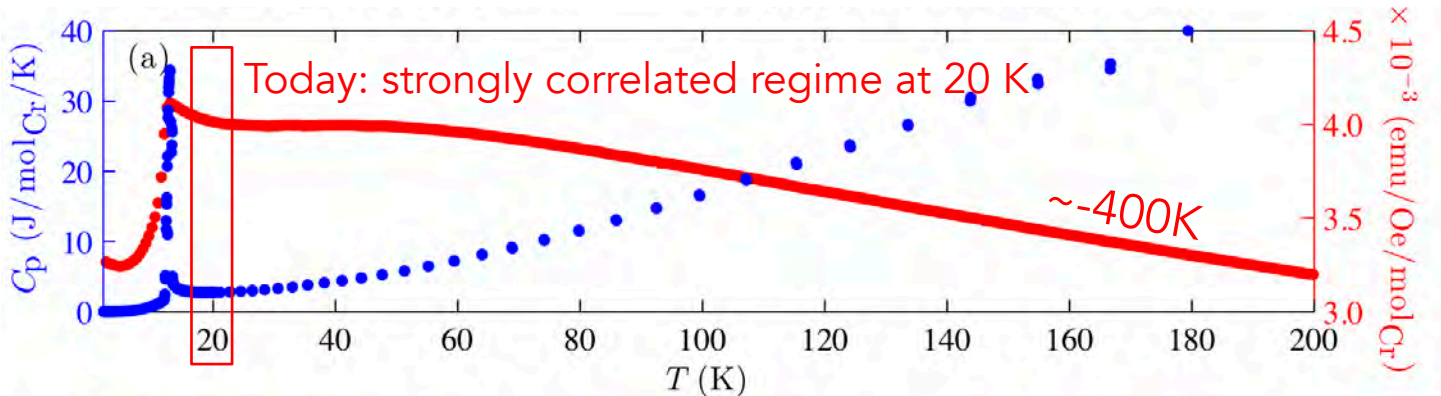
Koohpayeh, Wen *et al.*
J. Cryst. Growth 2011



Dutton *et al.*
PRB 2010

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- MgCr_2O_4 : grew and co-aligned ~ 14 grams of single-crystals



↑
magneto-
structural
ordering

↑
coexistence of
broad and
sharp features

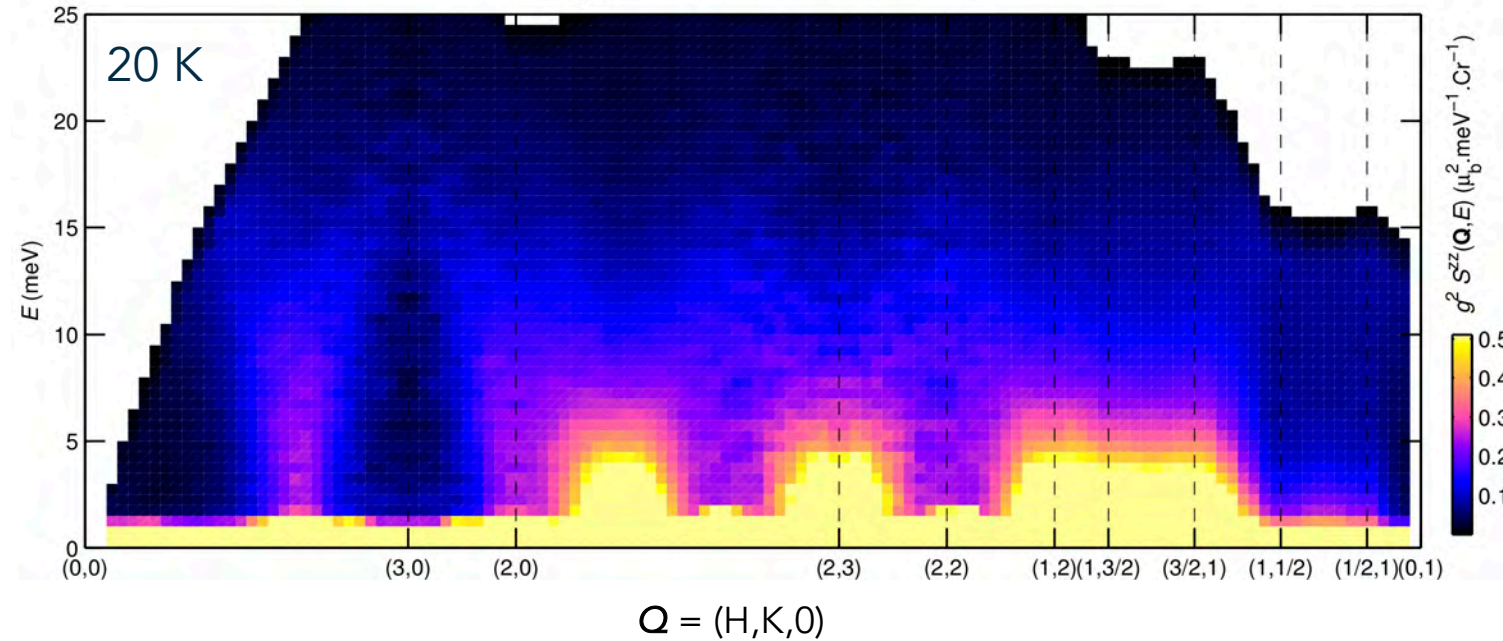
↑
highly structured
diffuse scattering



Polarized Elastic
Scattering

What is the origin of the loop scattering?

- ❑ Theoretical work by Conlon & Chalker attributing it to further-neighbor ex.
- ❑ MgCr₂O₄: grew and co-aligned ~14 grams of single-crystals



Complete map of the inelastic spectrum

All measurements are performed at 20 K which is 5% of the Weiss constant

How to analyze such a large and broad "4D" dataset?

Analysis of energy-integrated data

- For a spin-space isotropic magnet with Heisenberg exchange interactions:

Structure Factor

$$\begin{aligned} \mathcal{S}(\mathbf{Q}) &= \int_{-\infty}^{+\infty} dE \mathcal{S}(\mathbf{Q}, E) \\ &= \frac{2}{3N} \sum_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle \cos(\mathbf{Q} \cdot \mathbf{r}_{ij}) \end{aligned}$$

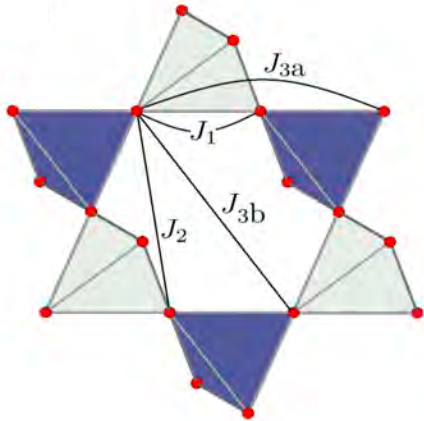
First Moment

$$\begin{aligned} \mathcal{K}(\mathbf{Q}) &= \int_{-\infty}^{+\infty} dE E \mathcal{S}(\mathbf{Q}, E) \\ &= -\frac{1}{3N} \sum_{ij} J_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle [1 - \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})] \end{aligned}$$

Hohenberg 1974
Broholm 2001

Fit then divide Fourier coefficients

- Further-neighbor interactions on the pyrochlore lattice:



J_{3a} and J_{3b} span the same length

Analysis of energy-integrated data

- For a spin-space isotropic magnet with Heisenberg exchange interactions:

Structure Factor

$$S(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE S(\mathbf{Q}, E)$$

$$= \frac{2}{3N} \sum_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})$$

First Moment

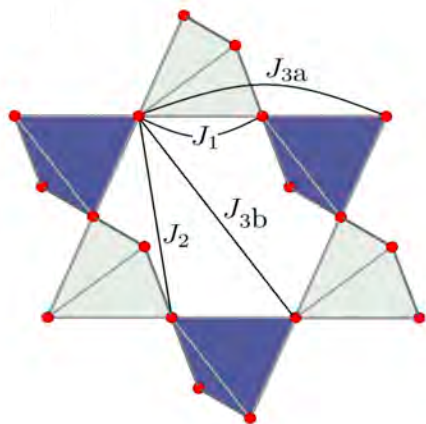
$$\mathcal{K}(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE E S(\mathbf{Q}, E)$$

$$= -\frac{1}{3N} \sum_{ij} J_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle [1 - \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})]$$

Hohenberg 1974
Broholm 2001

Fit then divide Fourier coefficients

- Further-neighbor interactions on the pyrochlore lattice: "microscopic" theory

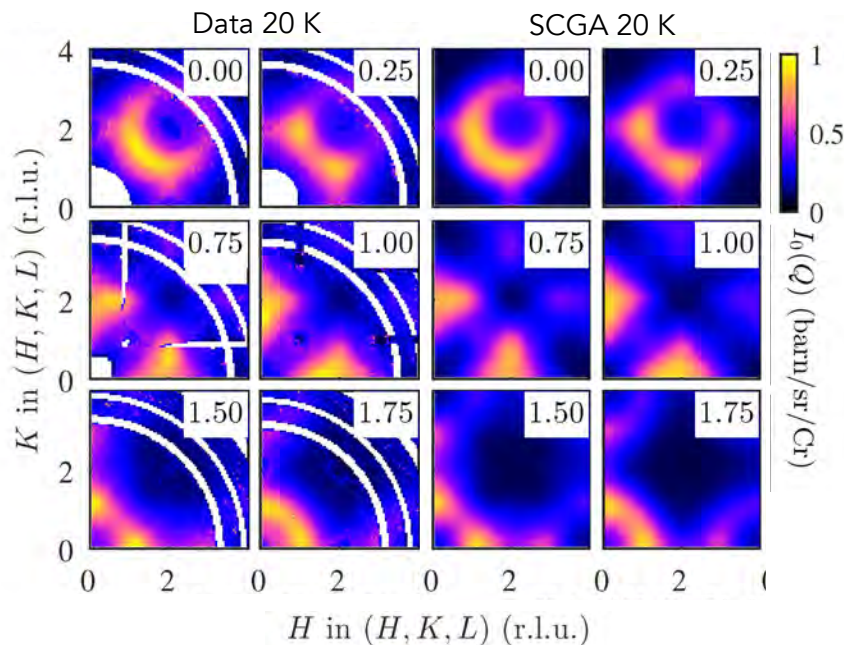


Self Consistent Gaussian Approx.

Soft spin constraint + Sum rule

Calculates $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_T$ given J_{ij}

Global Fit



Analysis of energy-integrated data

- For a spin-space isotropic magnet with Heisenberg exchange interactions:

Structure Factor

$$S(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE S(\mathbf{Q}, E)$$

$$= \frac{2}{3N} \sum_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})$$

First Moment

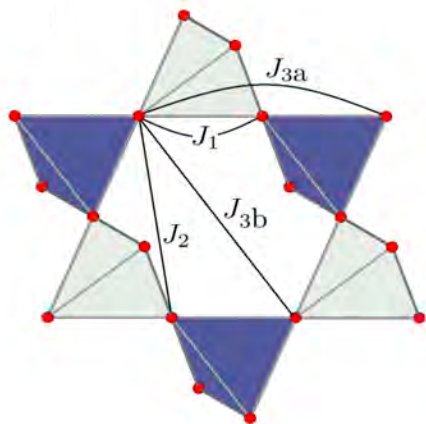
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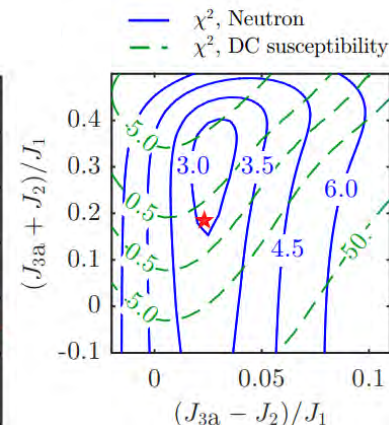
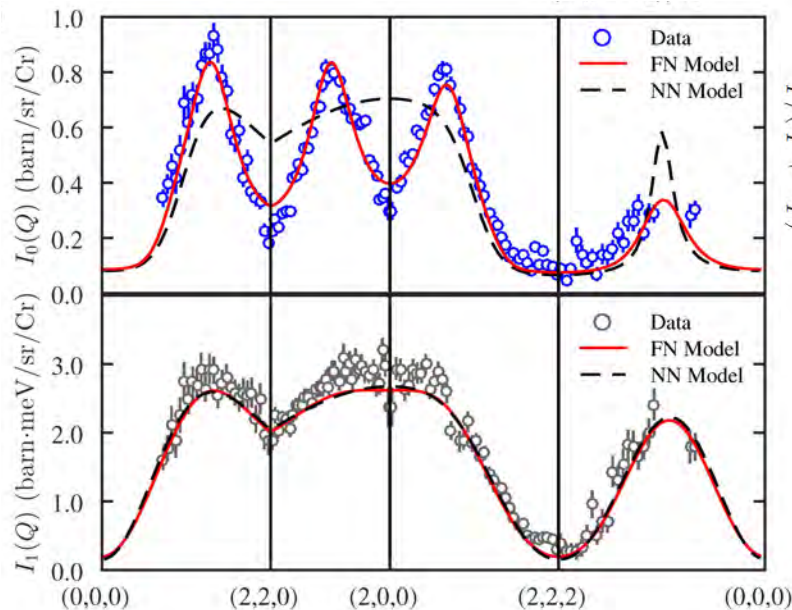


Self Consistent Gaussian Approx.

Soft spin constraint + Sum rule

Calculates $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_T$ given J_{ij}

Global Fit



$J_1 = 3.28(9) \text{ meV}$
 $J_2 = 0.081 J_1$
 $J_{3a} = 0.105 J_1$
 $J_{3b} = 0.009 J_1$
 $T = 20 \text{ K}$

Analysis of energy-integrated data

- For a spin-space isotropic magnet with Heisenberg exchange interactions:

Structure Factor

$$S(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE S(\mathbf{Q}, E)$$

$$= \frac{2}{3N} \sum_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})$$

First Moment

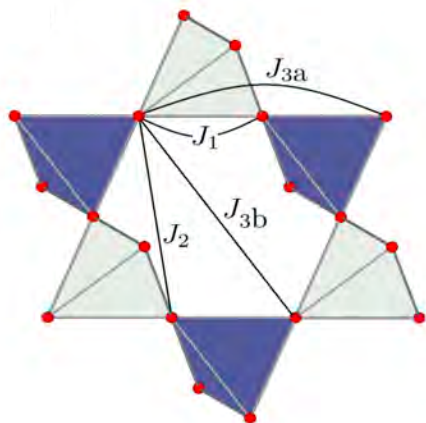
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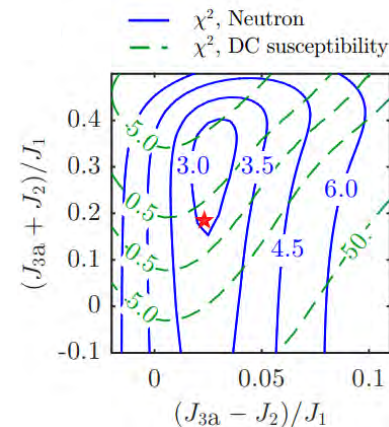
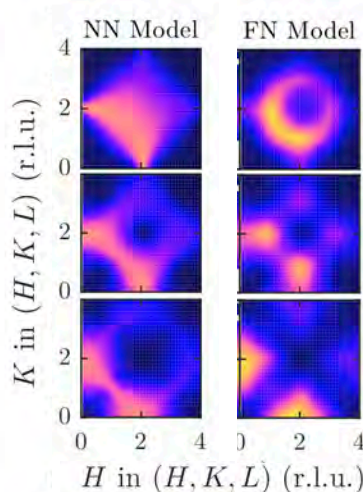
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Fit then divide Fourier coefficients

- Further-neighbor interactions on the pyrochlore lattice: "microscopic" theory



Global Fit



Self Consistent Gaussian Approx.

Soft spin constraint + Sum rule

Calculates $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_T$ given J_{ij}

FN interactions destroy the pinch point and produce the ring-like scattering pattern

$$J_1 = 3.28(9) \text{ meV}$$

$$J_2 = 0.081 J_1$$

$$J_{3a} = 0.105 J_1$$

$$J_{3b} = 0.009 J_1$$

$$T = 20 \text{ K}$$

Analysis of energy-integrated data

- For a spin-space isotropic magnet with Heisenberg exchange interactions:

Structure Factor

$$S(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE S(\mathbf{Q}, E)$$

$$= \frac{2}{3N} \sum_{ij} \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle \cos(\mathbf{Q} \cdot \mathbf{r}_{ij})$$

First Moment

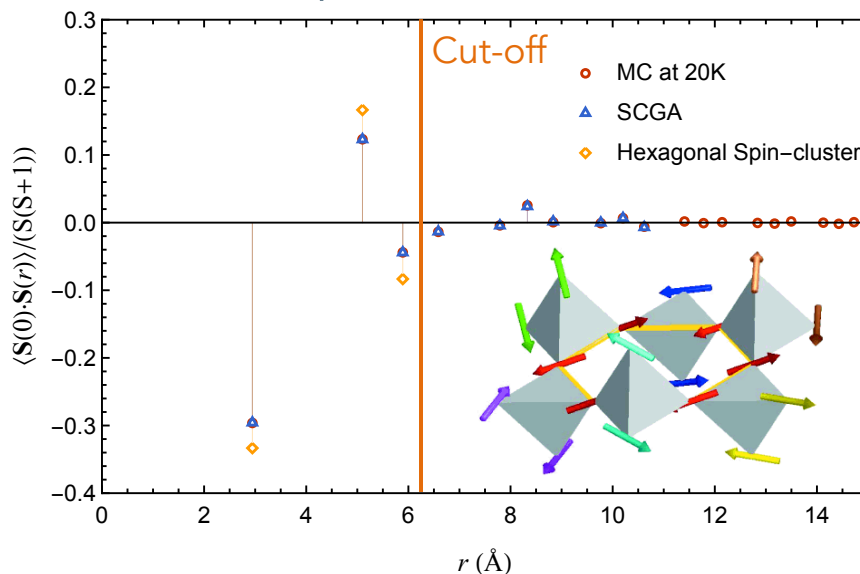
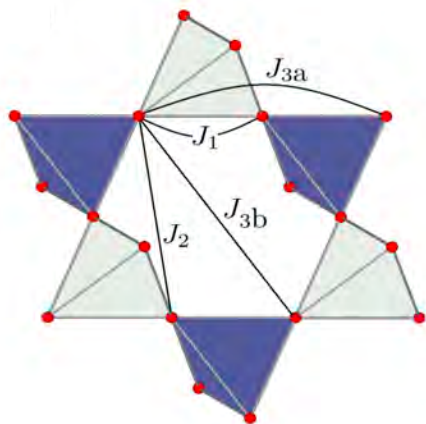
$$\mathcal{K}(\mathbf{Q}) = \int_{-\infty}^{+\infty} dE E S(\mathbf{Q}, E)$$

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Hohenberg 1974
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Fit then divide Fourier coefficients

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Self Consistent Gaussian Approx.

Soft spin constraint + Sum rule

Calculates $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_T$ given J_{ij}

Hexagonal spin-cluster produces similar spin-correlations up to third neighbor

$$J_1 = 3.28(9) \text{ meV}$$

$$J_2 = 0.081 J_1$$

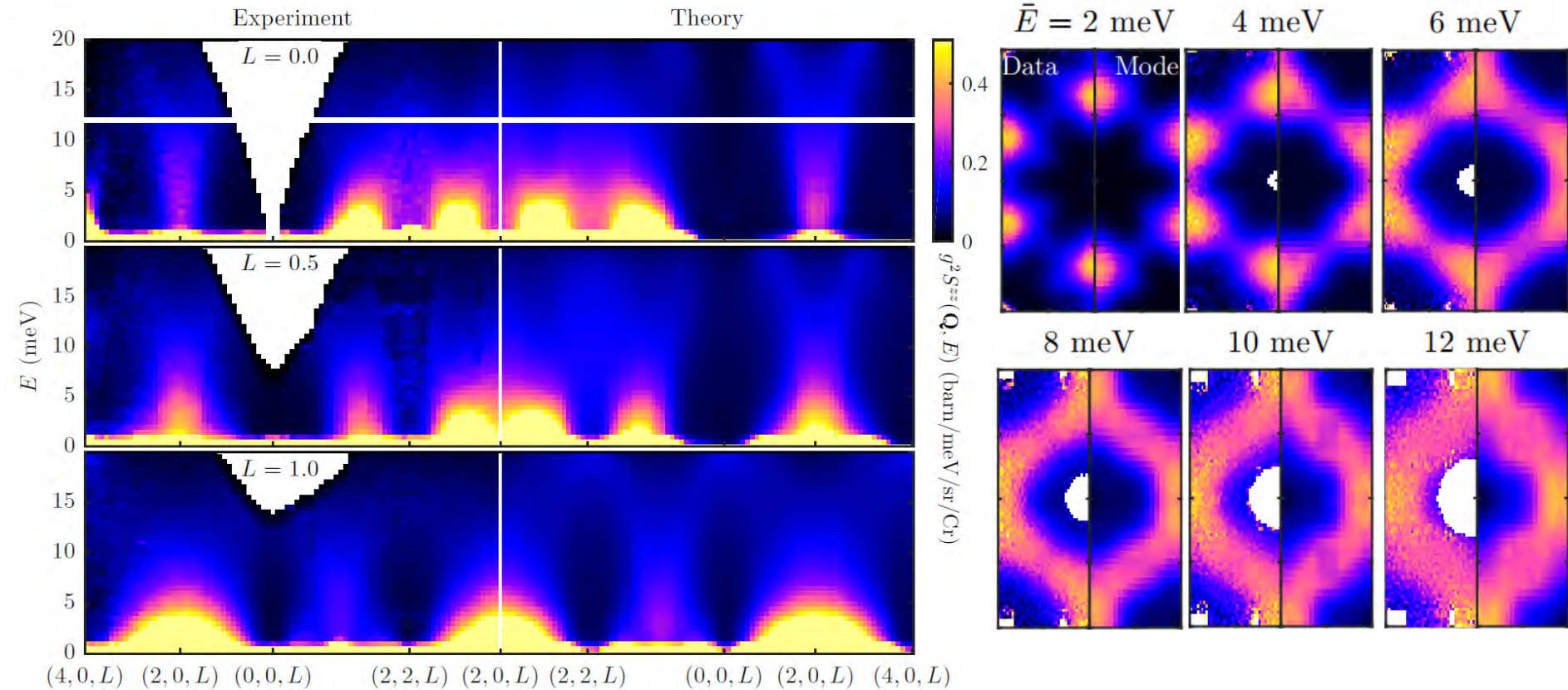
$$J_{3a} = 0.105 J_1$$

$$J_{3b} = 0.009 J_1$$

$$T = 20 \text{ K}$$

Back to the energy-resolved data

Can this FN Heisenberg model be used to model the excitations? **Yes!**



Our modeling strategy



Monte-Carlo cool down to 20 K for 6x6x6 super cell

Calculate harmonic fluctuations for resulting configuration

Kapit, Chalker Discard small fraction of imaginary modes, average samples

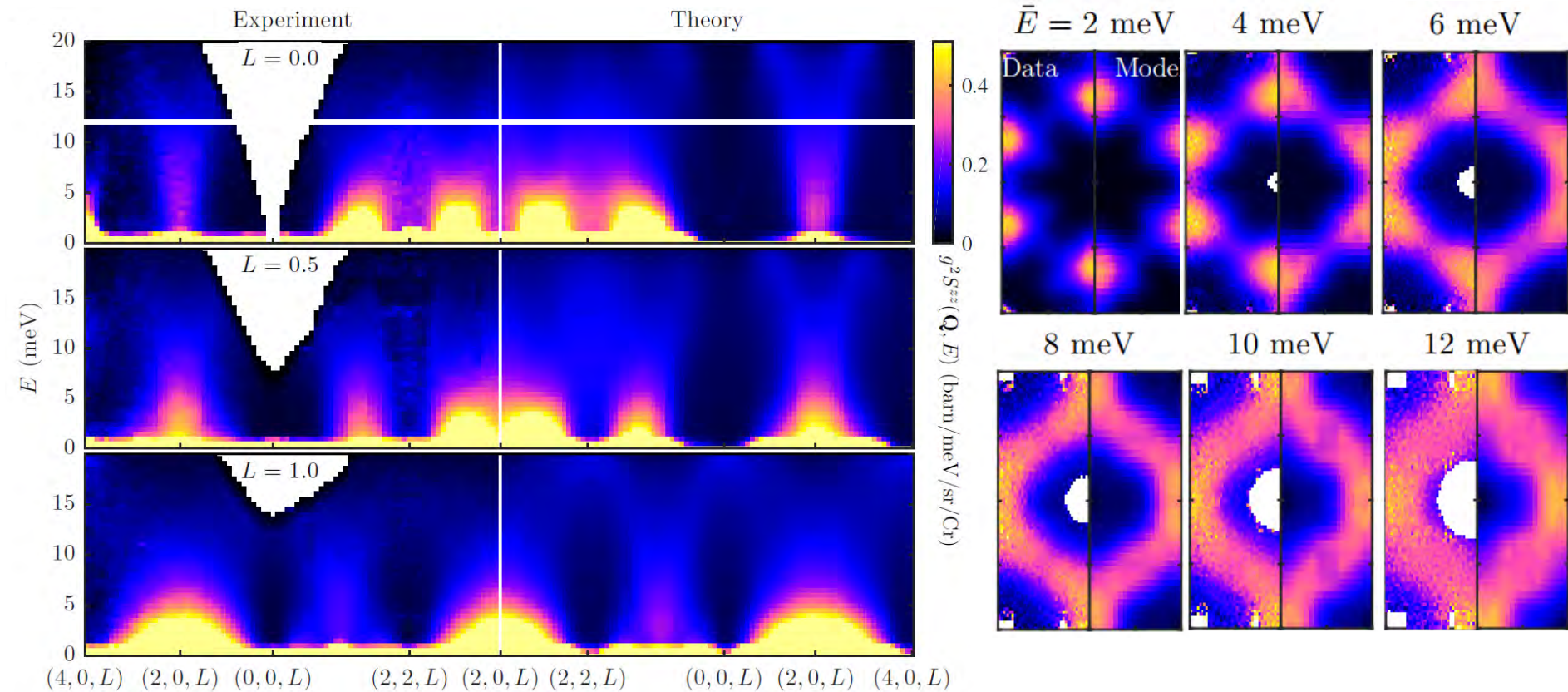
See also

Molecular Dynamics
vs Spin-Wave

Zhang, Changlani,
Tchernyshyov, Moessner
PRL 122, 167203 (2019)

Back to the energy-resolved data

Can this FN Heisenberg model be used to model the excitations? **Yes!**



Dynamics is broad because spins ride a disordered background

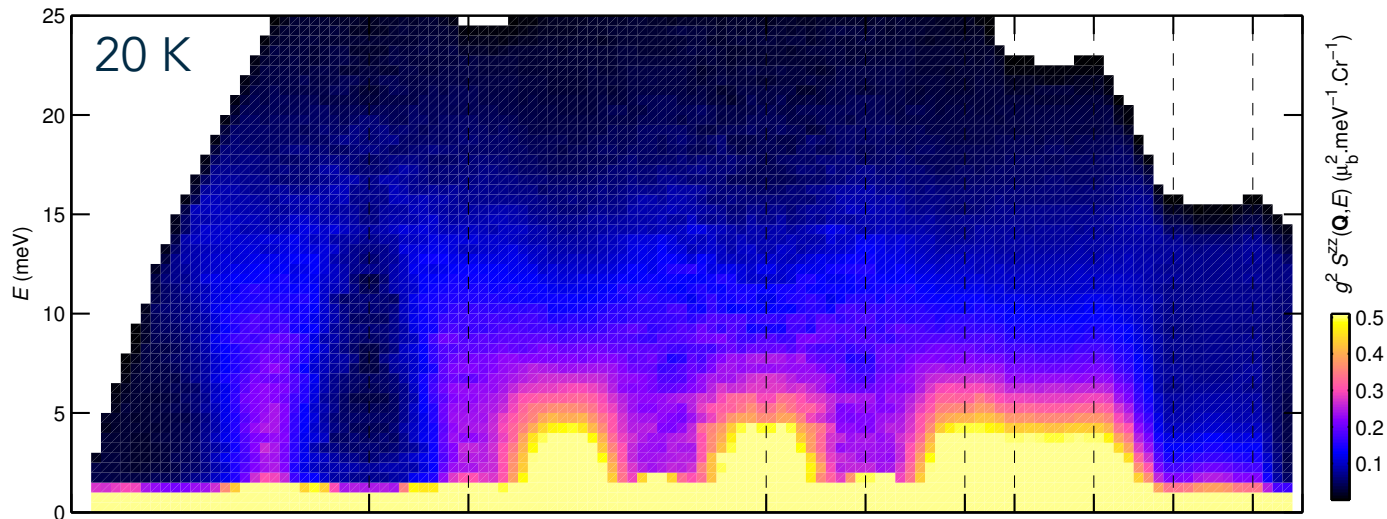
To first order: not because of fractionalization, not because of magnon decay

Time-scales of harmonic spin precessions and ground-state reconfigurations vastly differ

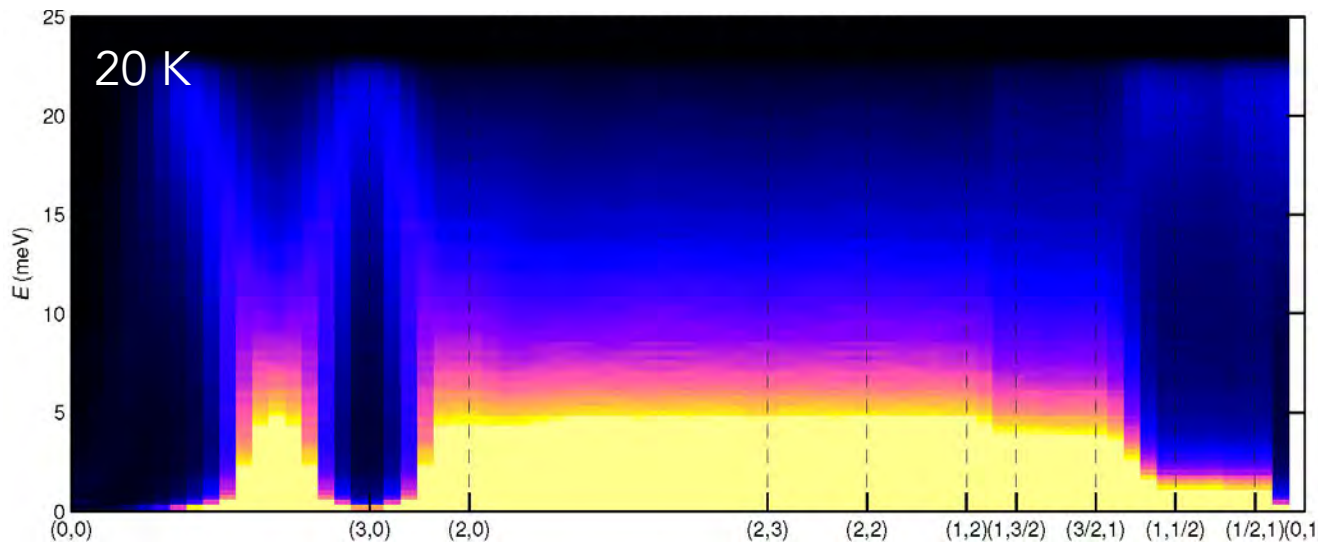
Final Remarks on MgCr_2O_4

- (1) Further neighbor interactions clearly modify the dynamics

Data



J_1 only

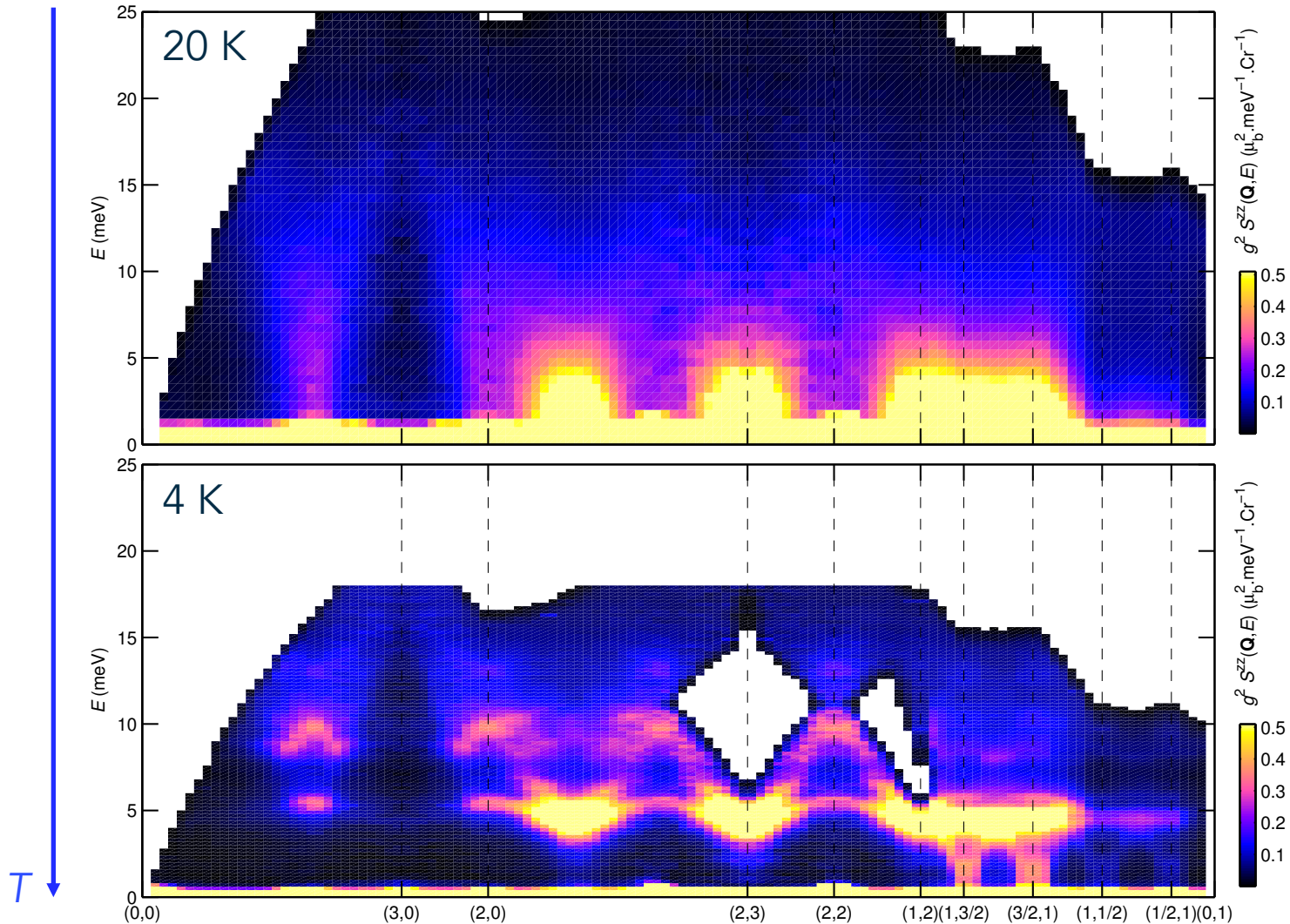


Clear mode vs wall of scattering

A continuum does not necessarily mean fractionalization

Final Remarks on MgCr_2O_4

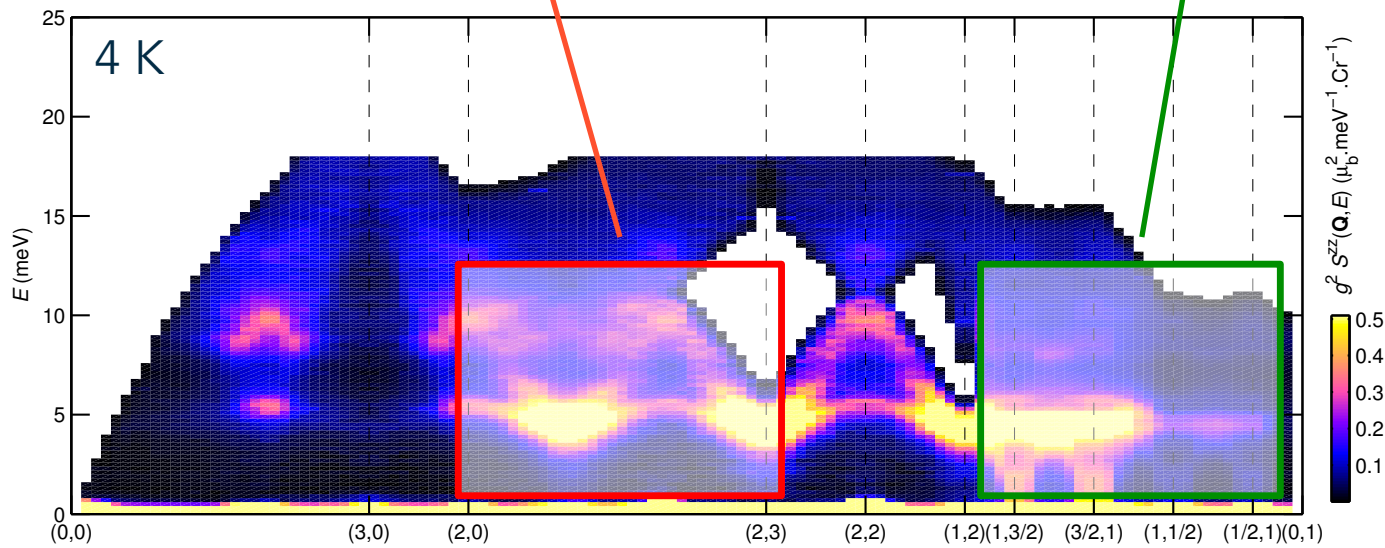
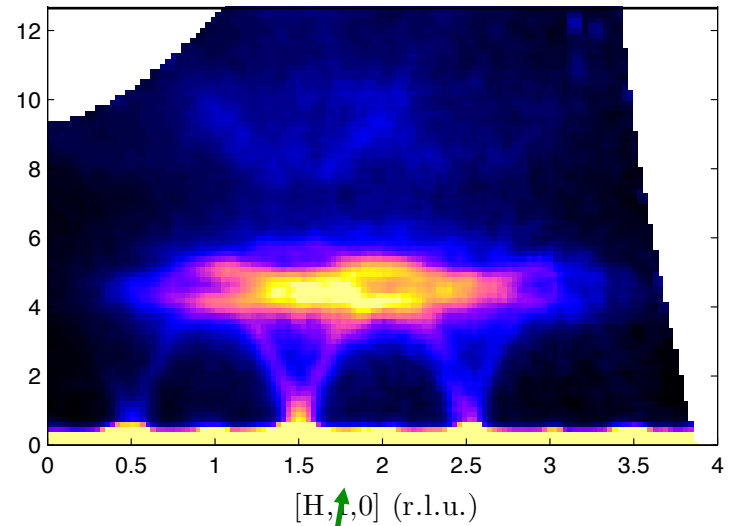
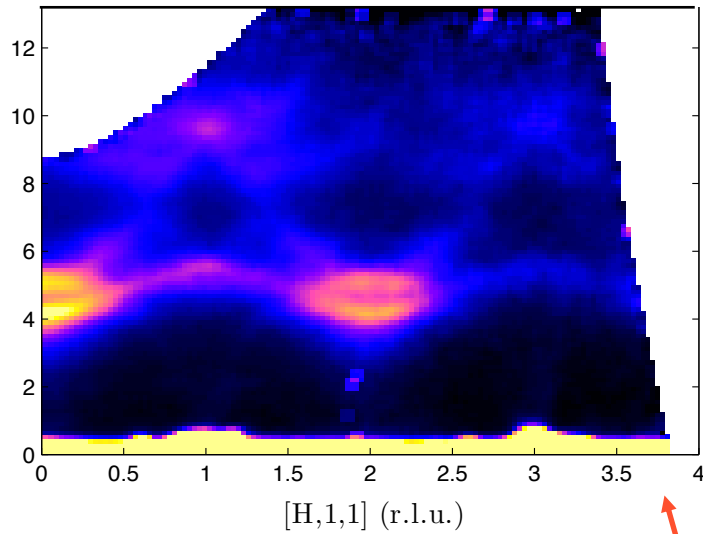
- (2) Excitations become sharp below the magneto-structural transition



See also Gao PRB 2018

Final Remarks on MgCr_2O_4

- (2) Excitations become sharp below the magneto-structural transition



Conclusion MgCr_2O_4

(3) Excitations become sharp below the magneto-structural transition

Loop scattering in chromium spinels: presence of further neighbor exchanges can explain all features of the paramagnetic data.

Excitations are broad primarily because the spins ride a spatially disordered background in a strongly correlated spin configuration.

Modeling works because in a classical spin-liquid there is a separation of time-scales between fast harmonic fluctuations and slow exploration of the ground-state manifold.

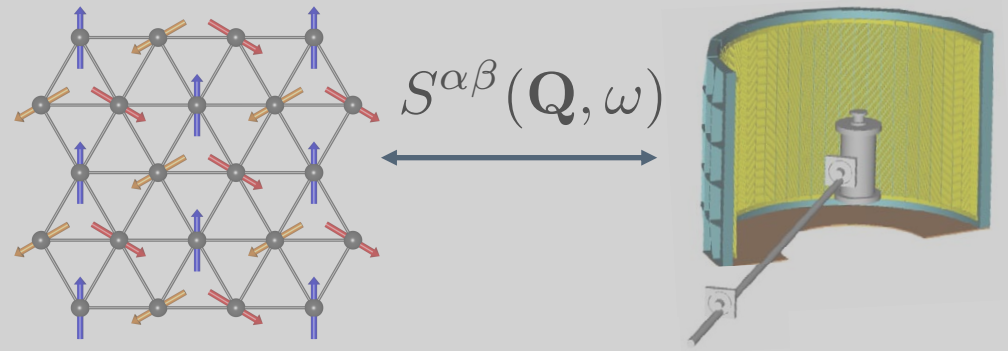
Can we explain the structure and excitations below 13K?

Classical vs quantum spin-liquids: how does the spectrum evolve with lowering S ?

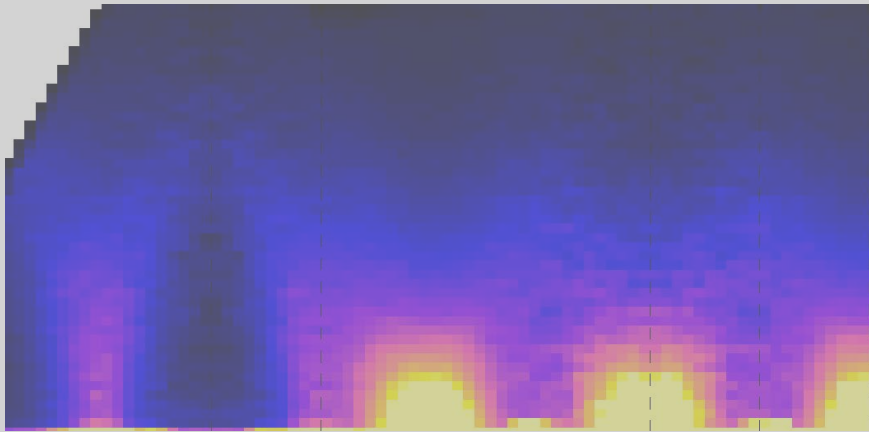
Idea: Using the spin waves to solve the magneto-structural transition?

Outline

1. Introduction and neutron scattering warm-up

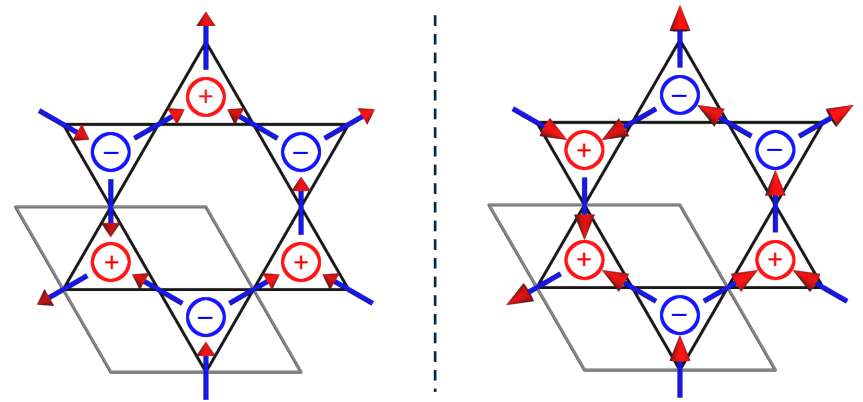


2. Nature of excitations in the classical pyrochlore Heisenberg AFM MgCr_2O_4



Bai *et al.* Phys. Rev. Lett. **122**, 097201 (2019)

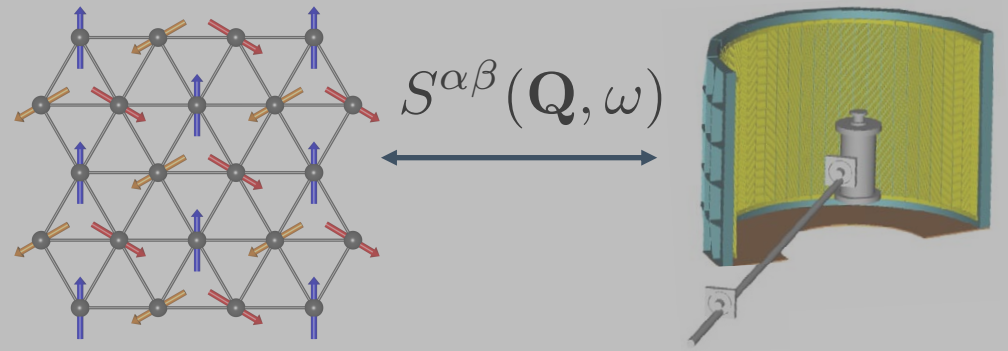
3. Kagome spin-ice physics in the tripod compounds $\text{Ln}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$



Paddison *et al.*, Nat. Commun. **7**, 13842 (2016)
Dun *et al.*, arXiv:1806.04081 (2019) + in prep.

Outline

1. Introduction and neutron scattering warm-up



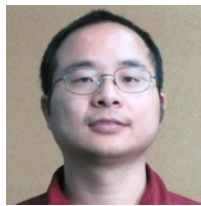
Zhiling
Dun



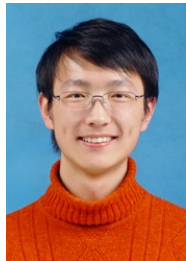
Joe
Paddison



Siân
Dutton



Haidong
Zhou



Xiaojian
Bai

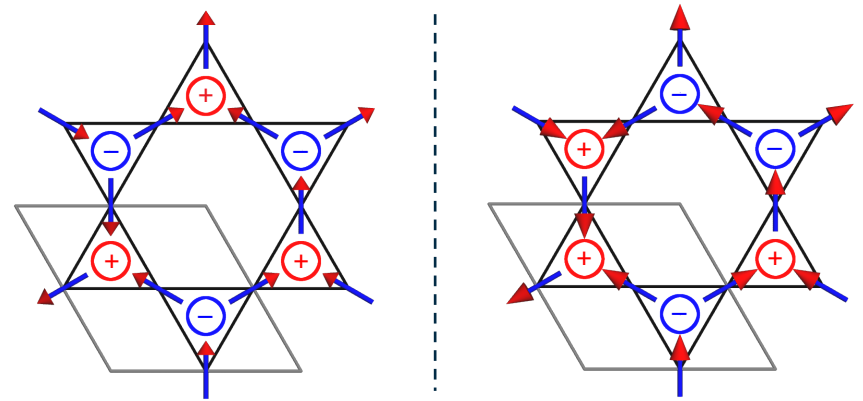


Emily
Hollingworth



Claudio
Castelnovo

3. Kagome spin-ice physics in the tripod compounds $Ln_3Mg_2Sb_3O_{14}$



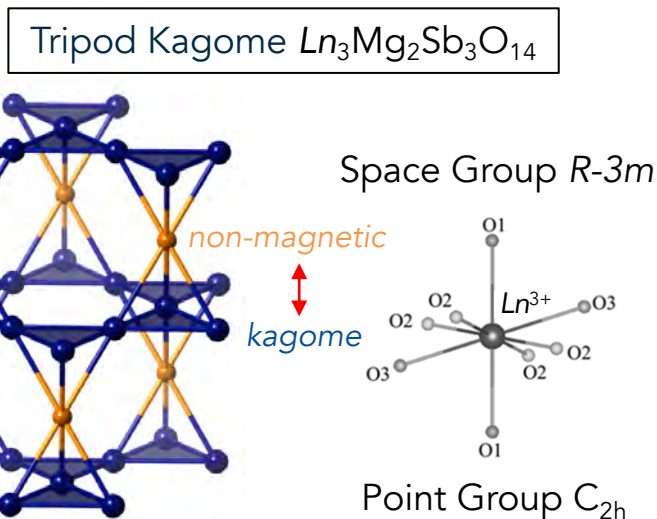
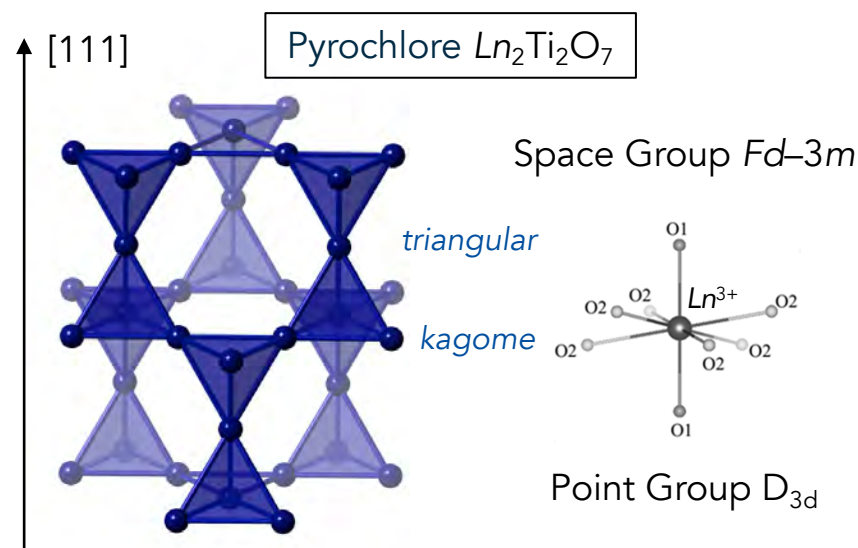
Paddison *et al.*, *Nat. Commun.* **7**, 13842 (2016)

Dun *et al.*, arXiv:1806.04081 (2019) + in prep.

Matt Stone (ORNL), Clarina de la Cruz (ORNL), Matt Tucker (ORNL/ISIS), Franz Demmel (ISIS), Nick Butch (NIST)

From pyrochlore spin-ice to kagome spin-ice

- Discovery of "tripod" systems:



site mixing possible, only powders

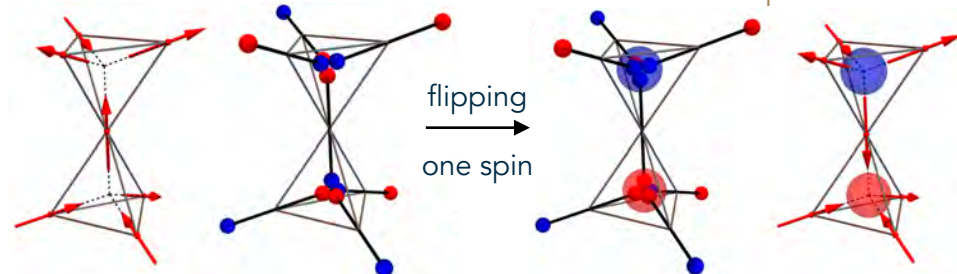
Dun et al., PRL 116, 157201 (2016); PRB 95, 104439 (2017).
Paddison, Dutton et al., Nat. Comm. 7, 13842 (2016)

- Spin-ice anisotropy is maintained

Dy Ho

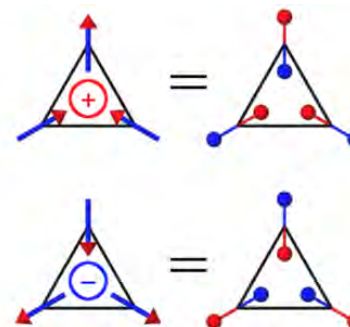
- Magnetic charges and monopoles

Illustrations James Hamp PhD Thesis

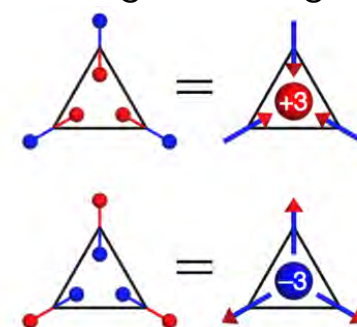


Monopole pairs interact via Coulomb's law

+/-1 magnetic charges



+/-3 magnetic charges



flipping
→
one spin

System is dense in interacting magnetic charges

Castelnovo, Moessner, and Sondhi, Nature 451, 42 (2008)
Moller & Moessner, PRB 80, 140409 (2009)

The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

☐ Predictions from classical MC:

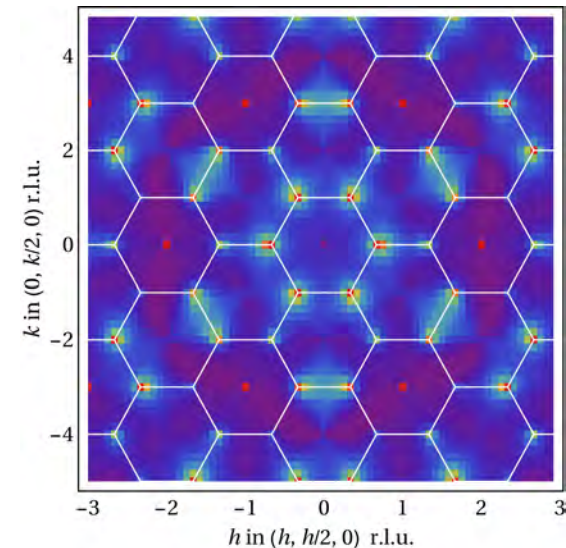
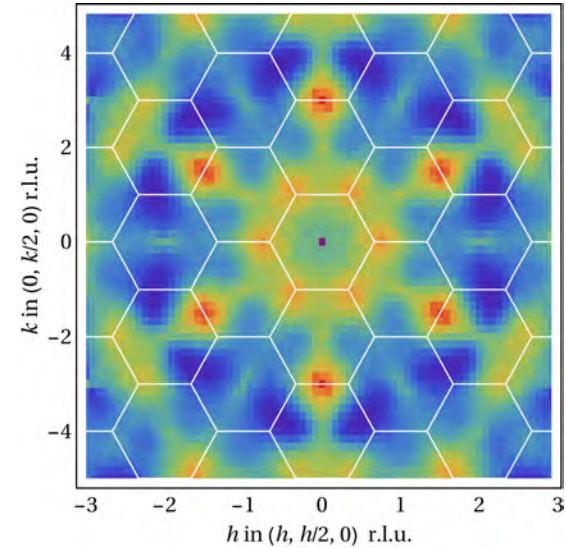
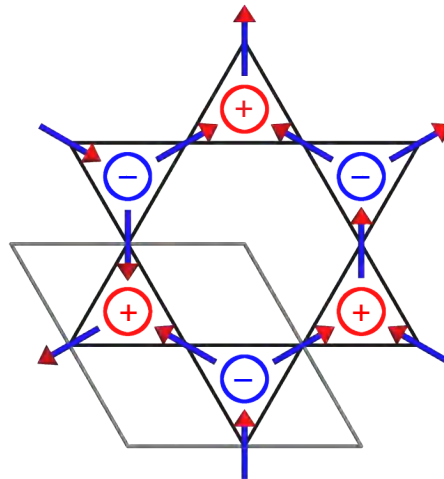
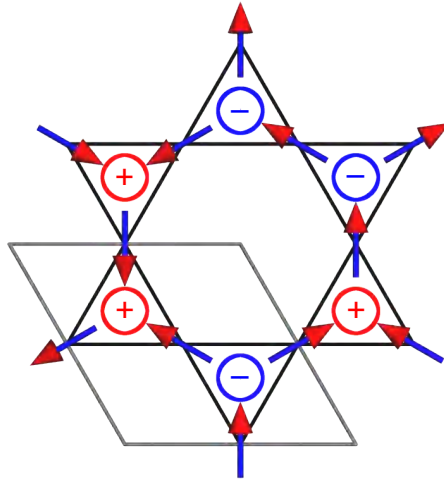
spins in plane, no disorder

Paramagnet
 ± 1 or ± 3

Kagome spin ice
 ± 1

Emergent-charge order
 ± 1

cooling



The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

☐ Predictions from classical MC:

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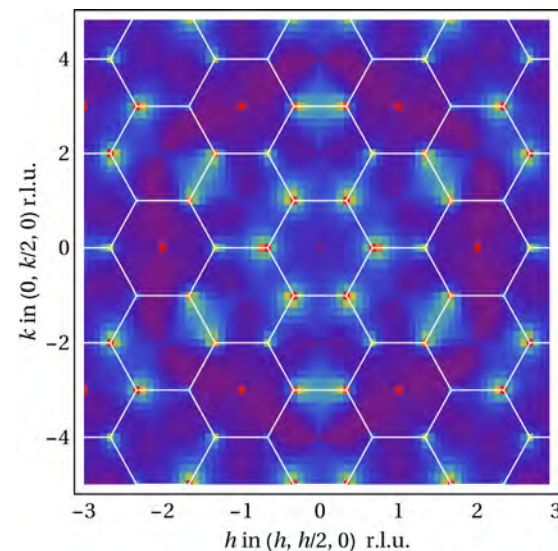
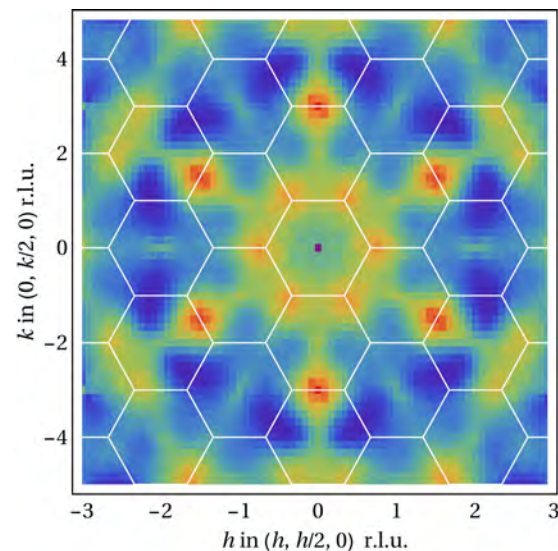
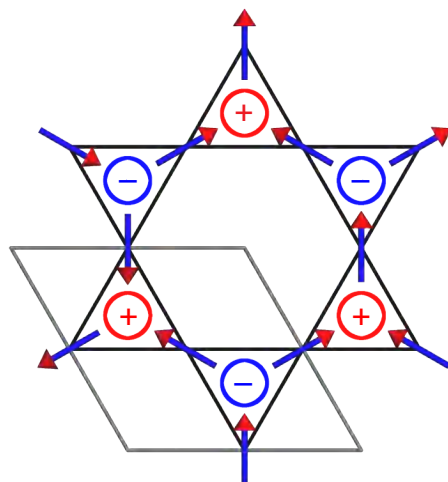
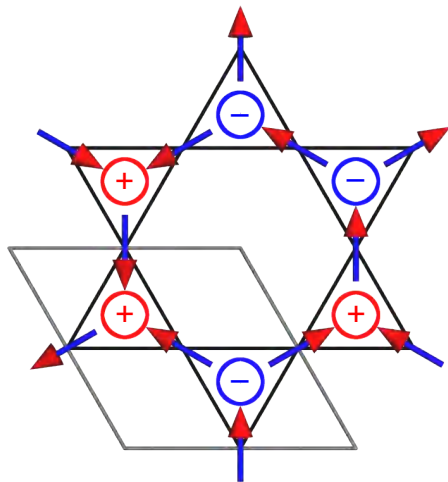
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The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

☐ Predictions from classical MC:

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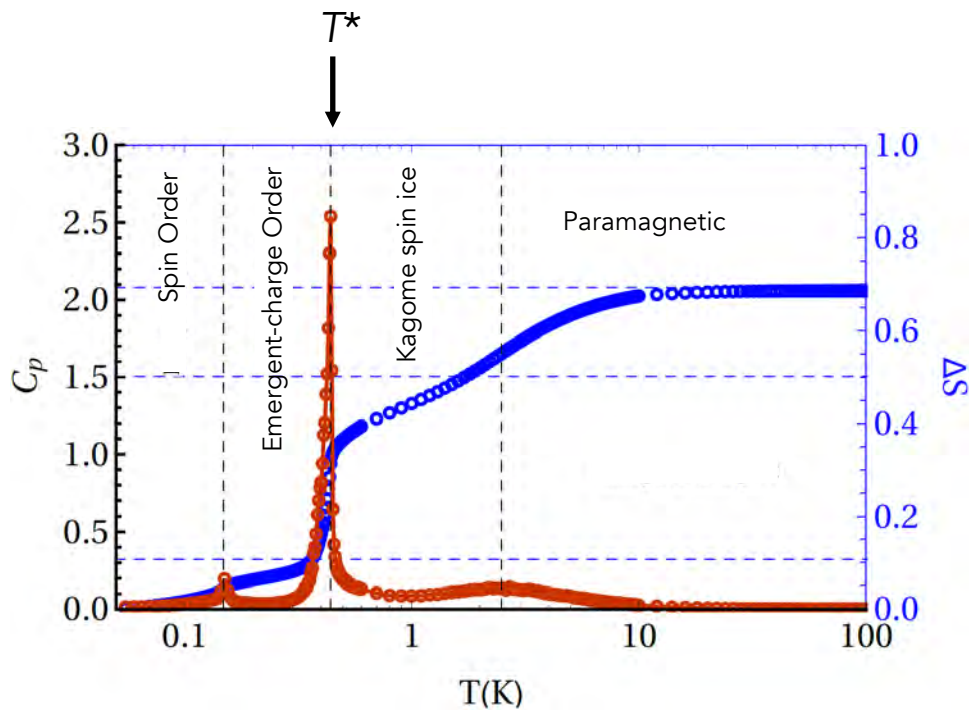
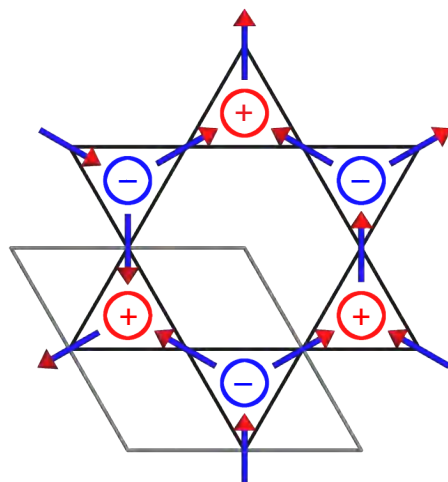
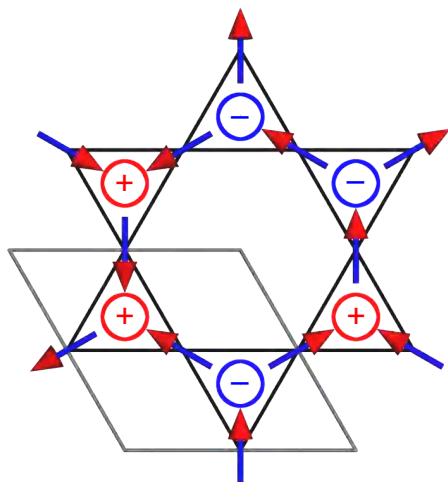
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The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

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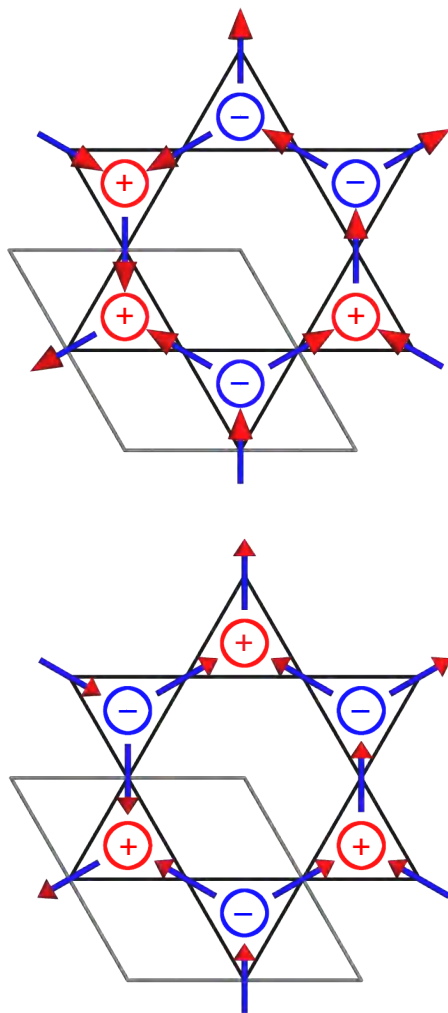
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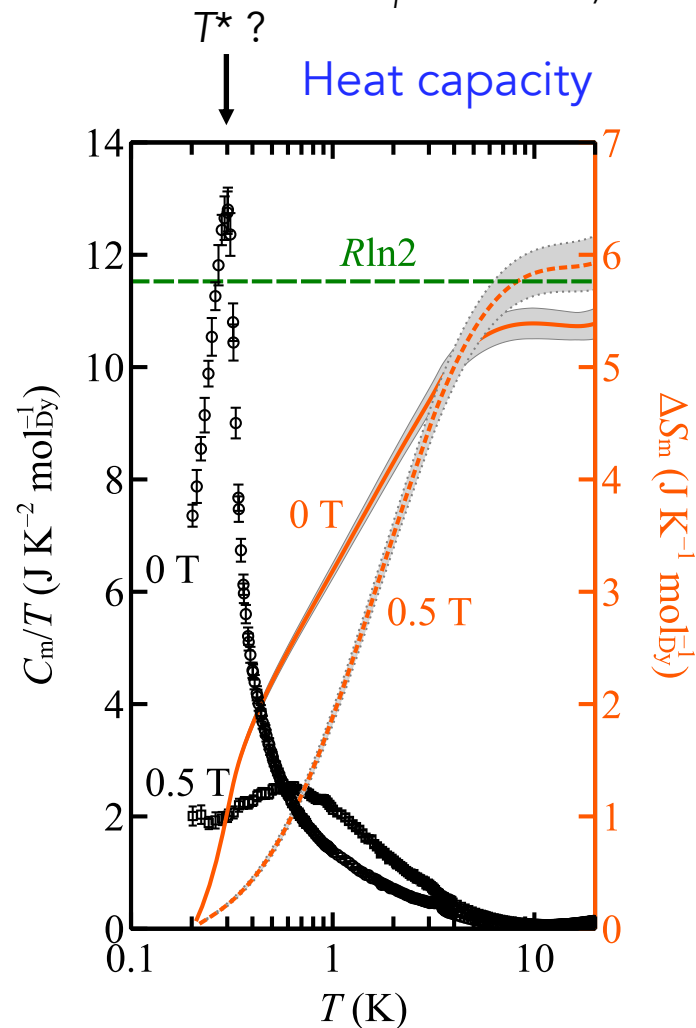
Spin order

cooling



☐ Experiments on powder samples:

spins titled 26°, disorder 6%



The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

☐ Predictions from classical MC:

spins in plane, no disorder

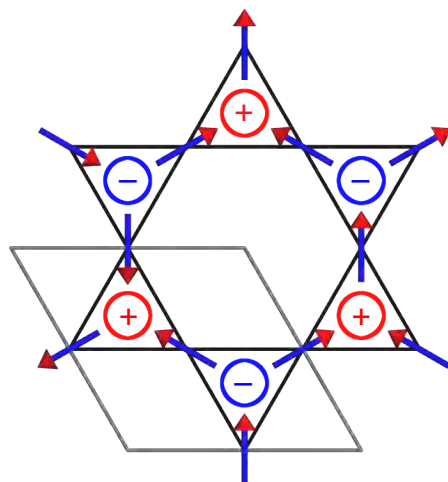
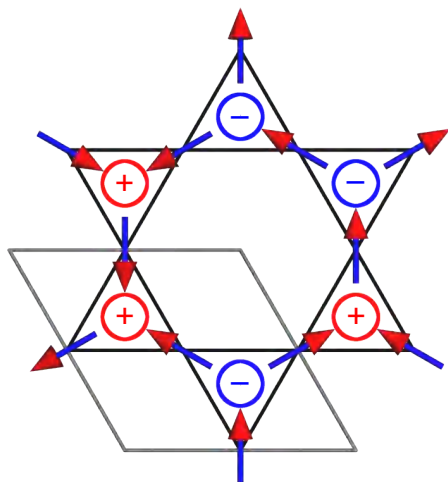
Paramagnet
 ± 1 or ± 3

Kagome spin ice
 ± 1

Emergent-charge order
 ± 1

Spin order

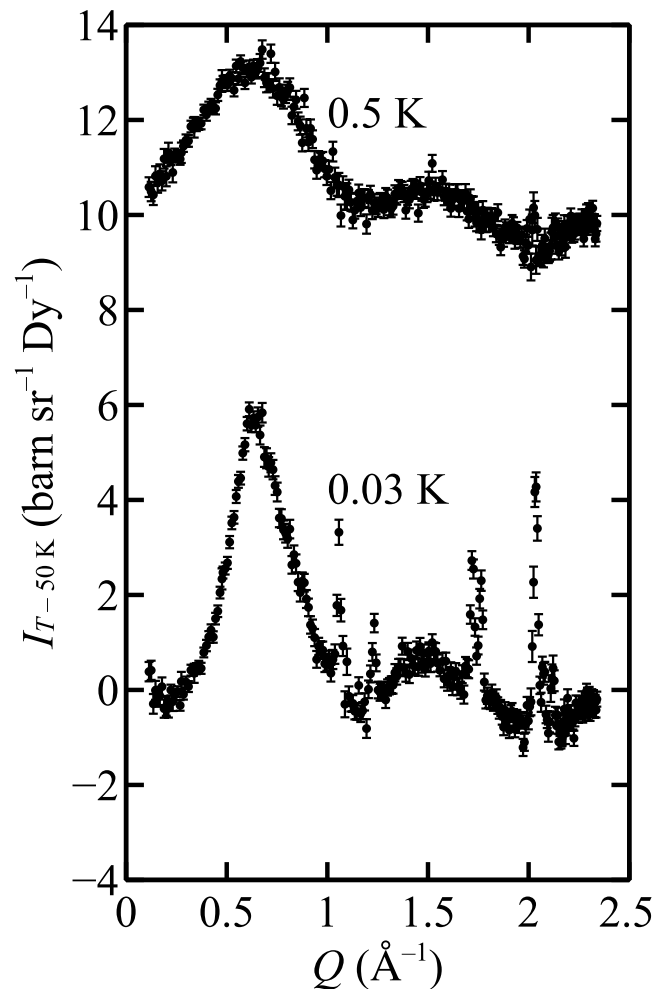
cooling



☐ Experiments on powder samples:

spins titled 26° , disorder 6%

Magnetic neutron scattering



The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

☐ Predictions from classical MC:

☐ Experiments on powder samples:

spins in plane, no disorder

spins titled 26°, disorder 6%

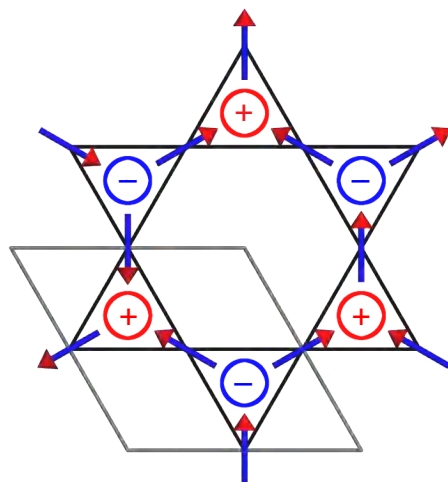
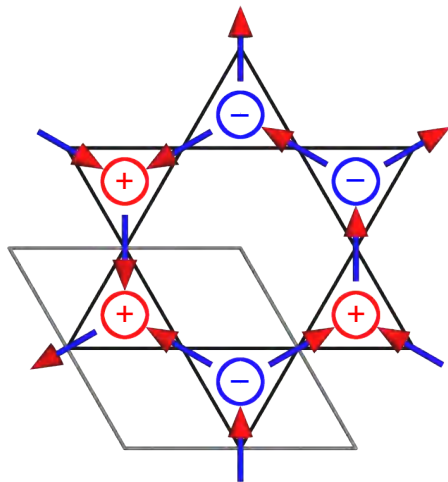
Paramagnet
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Kagome spin ice
 ± 1

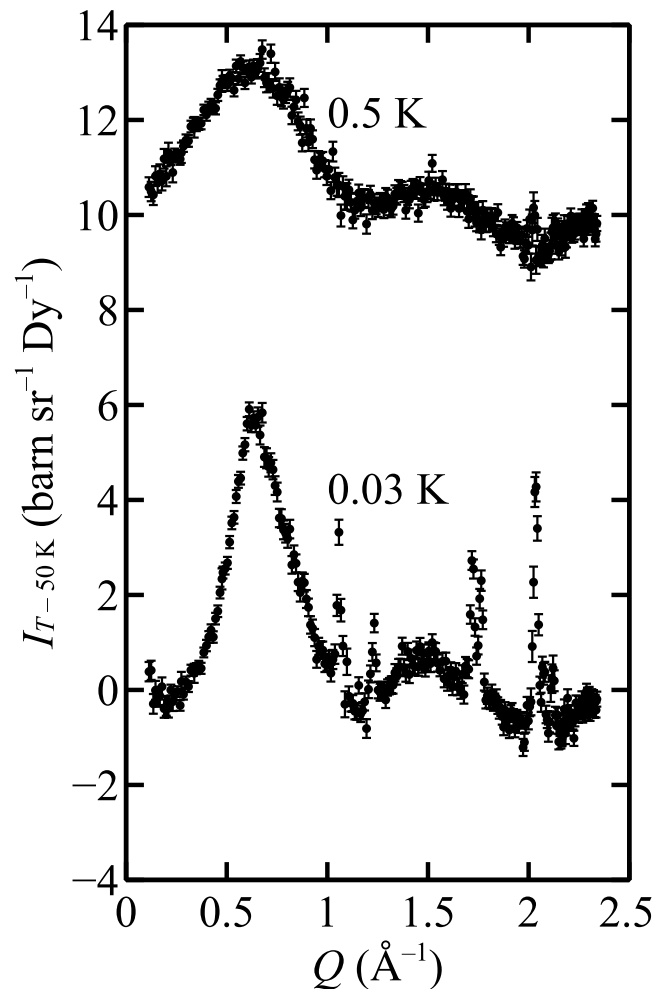
Emergent-charge order
 ± 1

Spin order

cooling



Magnetic neutron scattering



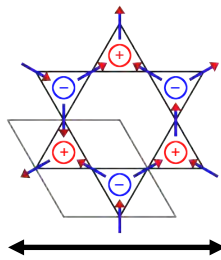
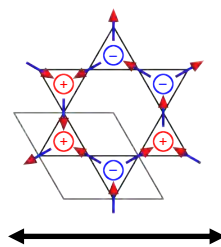
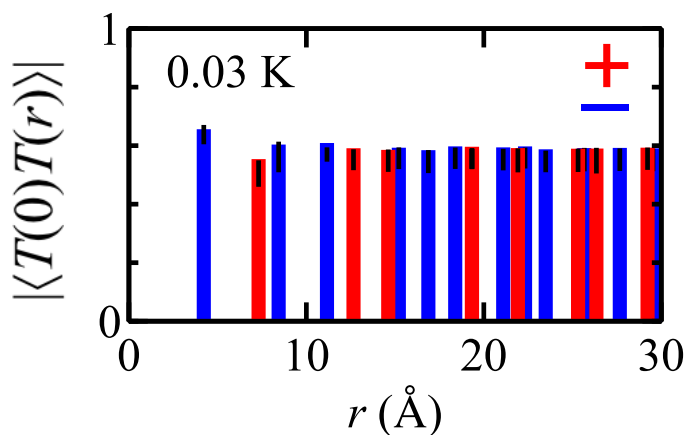
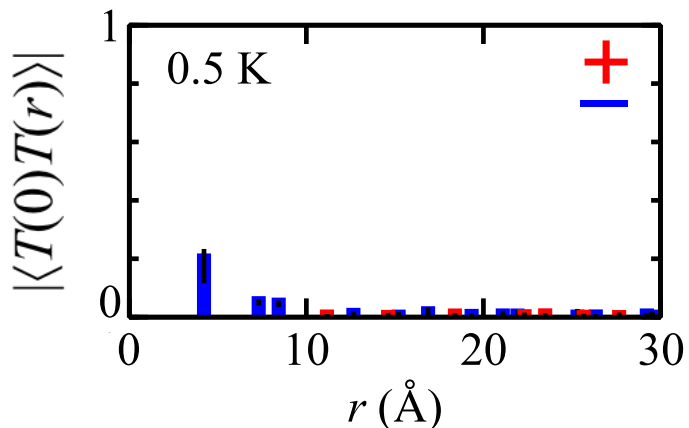
The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

Reverse Monte Carlo fits:

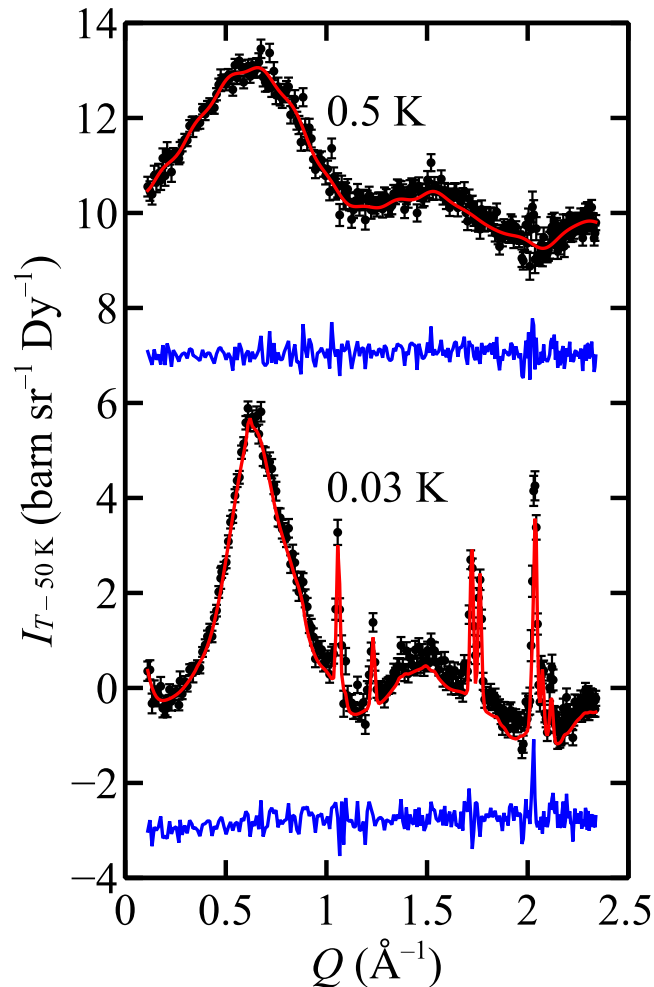
Experiments on powder samples:

spins titled 26°, disorder 6%

Charge-charge correlations

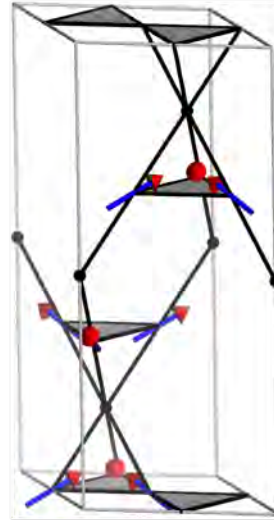
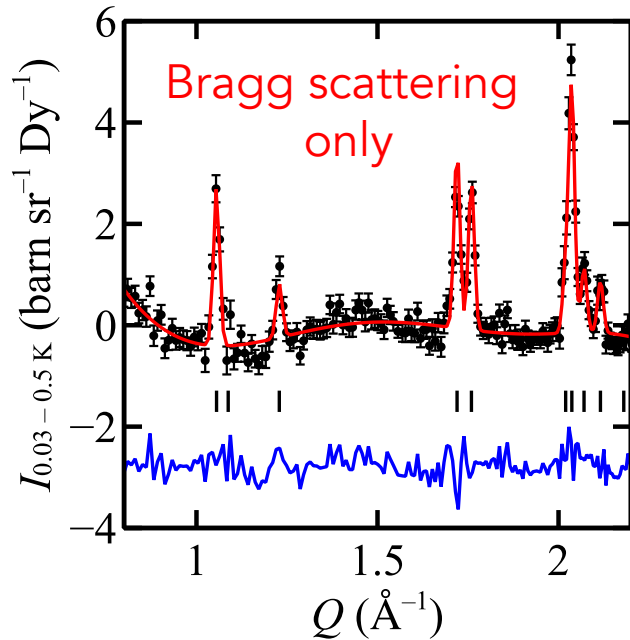


Magnetic neutron scattering



The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

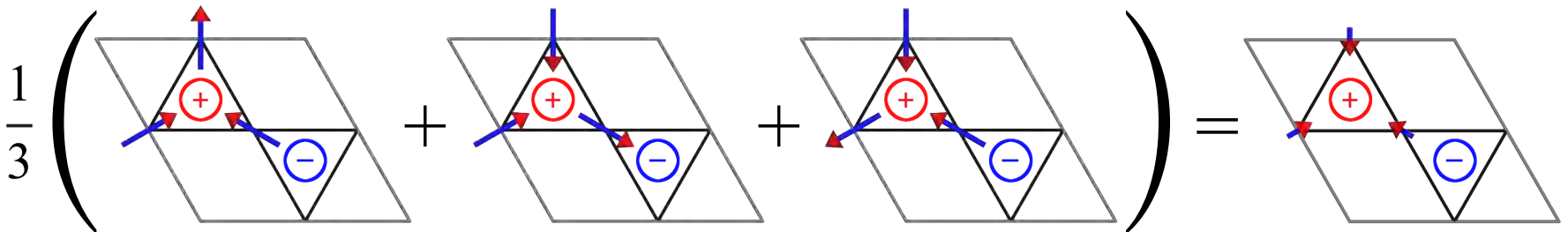
□ Coexistence of Bragg and diffuse scattering



$k = 0$ average magnetic structure
All-In All-Out (AIAO) state with $2.8 \mu_B$

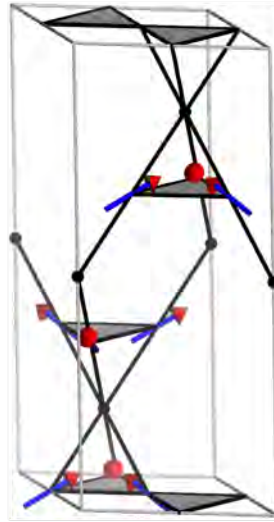
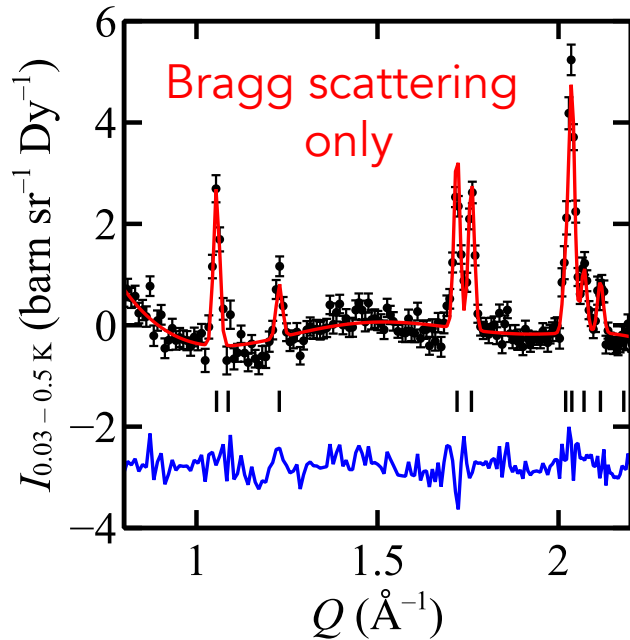
Only $\approx 1/3$ of the total moment is
found in the Bragg peaks

□ "Spin fragmentation"



The canonical behavior of $\text{Dy}_3\text{Mg}_2\text{Sb}_3\text{O}_{14}$

□ Coexistence of Bragg and diffuse scattering

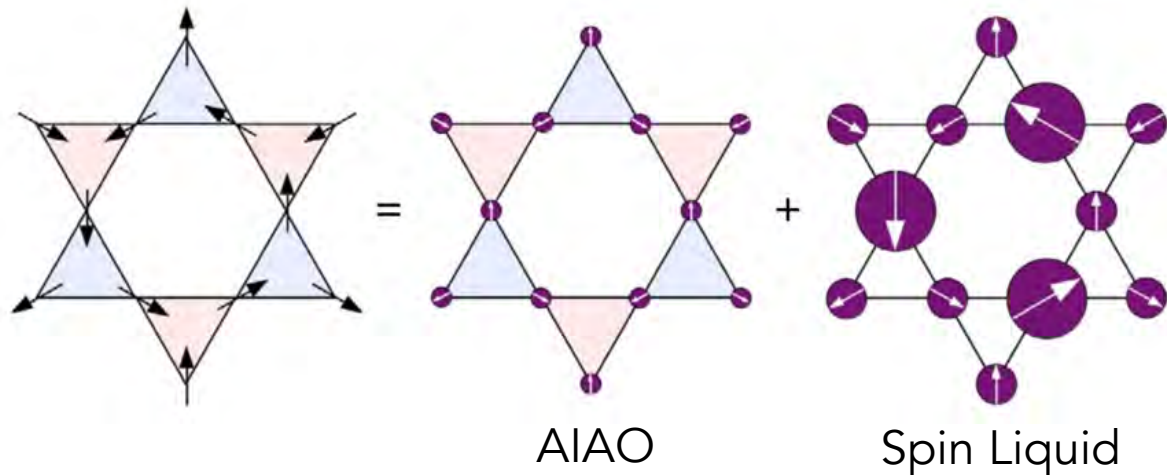


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Brooks-Bartlett et al., *PRX* **4**, 011007 (2014)
Canals et al., *Nature Commun.* **7**, 11446 (2016)
Petit et al., *Nature Physics* **12** 746-750 (2016)



Thank you for your attention!

