



# Turbulent Control of the Star Formation Efficiency

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## I. INTRODUCTION

- The Star Formation Efficiency (SFE) can be defined as

the fraction of a molecular cloud's mass that ends up in stars during its lifetime.

- It is the integral of the SFR over the cloud's lifetime  $\Delta t$ :

$$\text{SFE} = \frac{1}{M_{\text{cl}}} \int_{\Delta t} \text{SFR} \, dt$$

- The SFE is known to be low:

- ~ a few % in global cloud complexes (e.g., Myers et al. 1986)

- ~ 10-30% in cluster-forming cores (e.g., Lada & Lada 2003)

- Why?

- low SFR? (“Slow”) (e.g., Mouschovias 1976; Shu et al. 1977; Klessen et al. 2000; Palla & Stahler 2002; Mouschovias & Tassis 2004; Vázquez-Semadeni et al. 2003, 2005; Krumholz, Tan & McKee 2006),

- or small  $\Delta t$ ? (“Brief”) (e.g., Ballesteros-Paredes et al. 1999; Elmegreen 2000; Hartmann et al. 2001; Hartmann 2003; Bate et al. 2003; Vázquez-Semadeni et al. 2007; Ballesteros-Paredes & Hartmann 2007; Elmegreen 2007),

- or something else? A combination of the above?

## II. MECHANISMS FOR A SLOW SFR

### 1. Magnetic support (Mouschovias 1976, 1991; Shu, Adams & Lizano 1987).

- Low-mass SF occurs in magnetically subcritical molecular clouds (MCs) mediated by ambipolar diffusion (AD).
  - **Low efficiency** because
    - Low filling factor of supercritical gas.
    - Long AD timescale ( $\tau_{AD}$ ) in quiescent, strongly subcritical conditions.
- High+low-mass SF occurs in supercritical clouds
  - **High efficiency.**

– However,

- GMCs are supersonically turbulent... (e.g., Zuckerman & Palmer 1974; Larson 1981; Heyer & Brunt 2004) :
  - Cores form in (short) crossing time (Ballesteros-Paredes et al. 1999; Elmegreen 2000).
  - $\tau_{AD}$  is comparable to dynamical time (Fatuzzo & Adams 2002 ; Heitsch et al. 2004).
- ... and marginally magnetically critical (e.g., McKee 1989; Bourke et al. 2001; Hartmann et al. 2001)
  - $\tau_{AD}$  is comparable to dynamical time in moderately subcritical clouds (Ciolek & Basu 2001).
- Most low-mass stars form in high-mass star forming regions (supercritical mode).
- So, probably cannot appeal to low-mass mode of magnetic support model to account for low SFE.

## 2. Turbulent regulation of the SFE in isolated clouds.

- Turbulence is a ***multiscale*** phenomenon, with largest velocities and timescales at largest spatial scales (Kolmogorov 1941; Larson 1981; Heyer & Brunt 2004).
- Dual role of supersonic turbulence:
  - Prevent monolithic cloud collapse.
  - Promote *nonlinear* (large amplitude) small-scale density fluctuations that
    - Shorter formation and free-fall times than parent cloud's.
    - Involve only a fraction of the total cloud mass (a different kind of filter than AD-mediated cores).
    - Only a fraction of which proceeds to collapse (Elmegreen 1993; Padoan 1995; Vázquez-Semadeni et al. 1996, 2003, 2005; Klessen, Heitsch & Mac Low 2000; Heitsch, Mac Low & Klessen 2001; Padoan & Nordlund 2002; Nakamura & Li 2005).

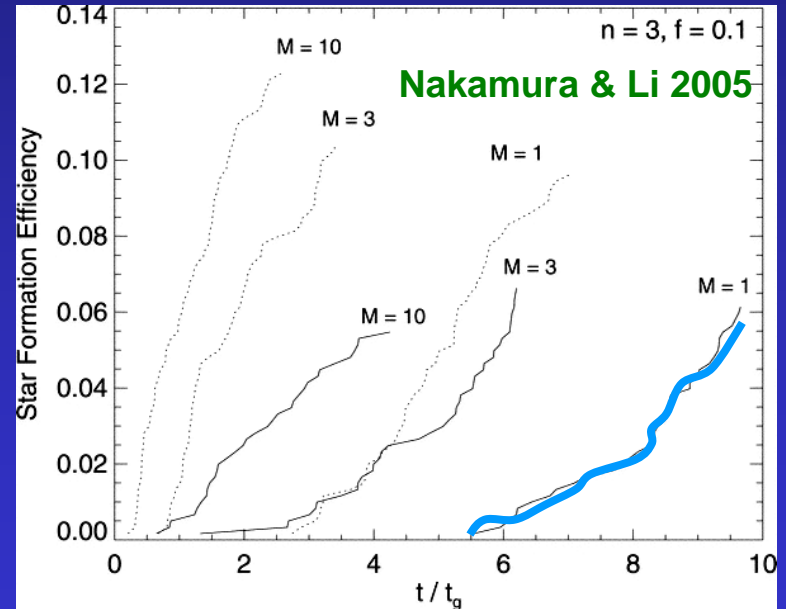
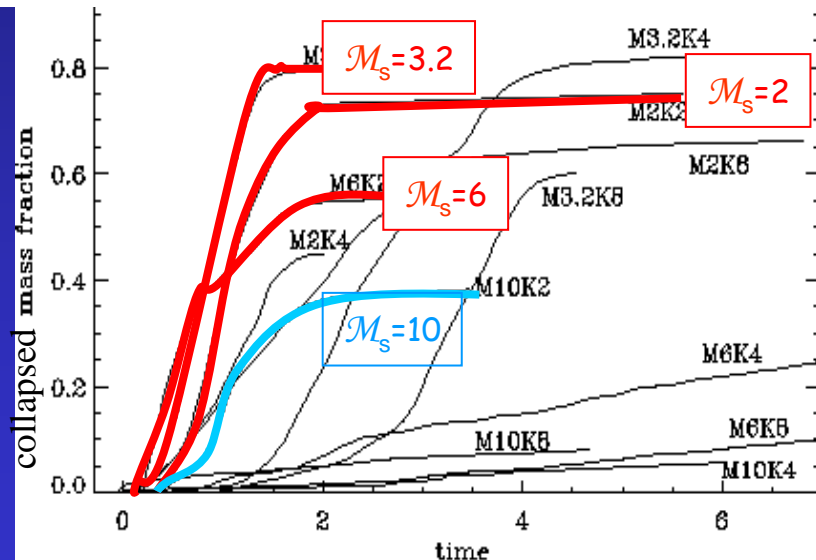
- Precise effect of turbulence strength depends on global cloud conditions:

a) *Smaller SFE* requires:

**Larger** turbulent rms Mach # in continually driven regimes.

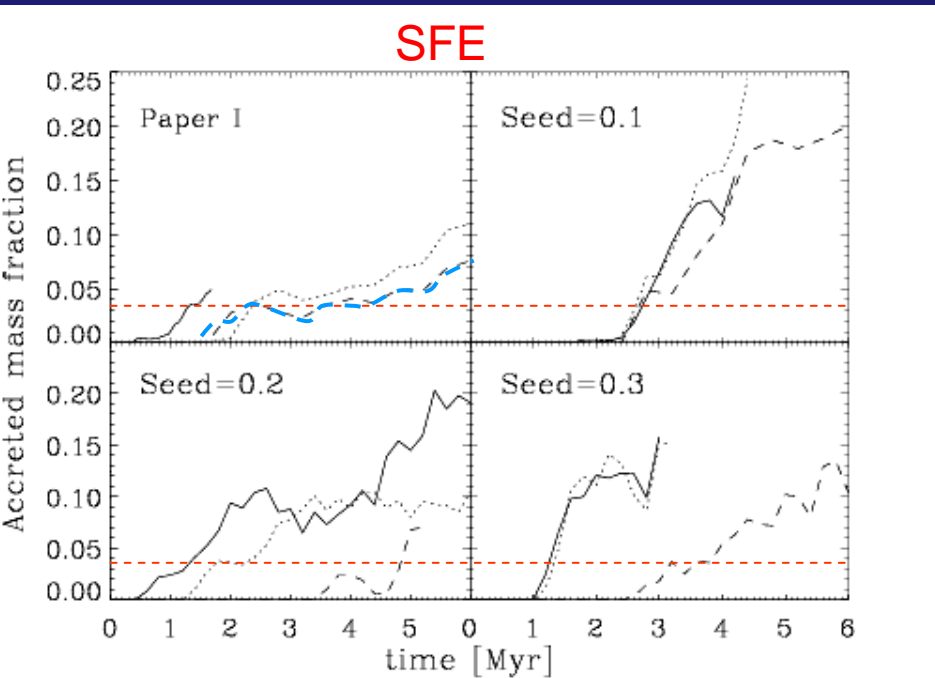
**Smaller** turbulent rms Mach # in decaying regimes.

Klessen et al. 2000; Vázquez-Semadeni et al. 2003





b) Same (2-5%) values of SFE over “reasonable” cloud lifetimes require moderately supercritical B in driven regimes, moderately subcritical B in decaying regimes,



Vázquez-Semadeni, Kim & Ballesteros-Paredes (2005). 3D, supercritical, no AD.

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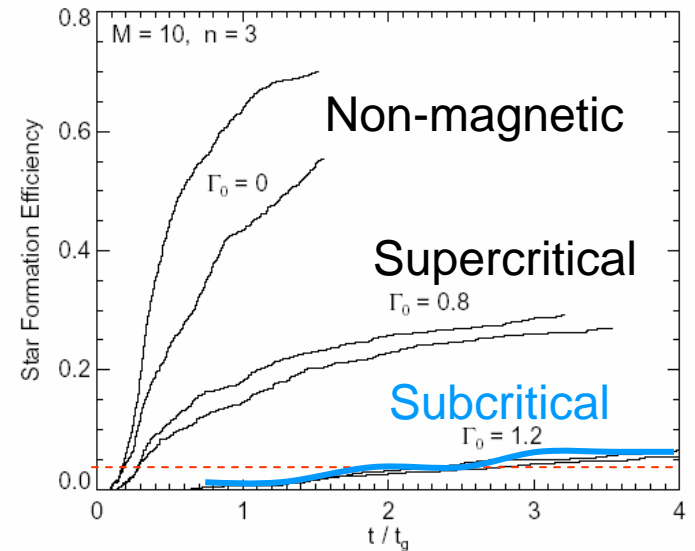


FIG. 6.— Efficiencies of star formation for clouds of the same initial turbulent velocity field but different degrees of magnetization, measured by the dimensionless flux-to-mass ratio  $\Gamma_{\text{ff}}$  labeled beside the curves. The heavy (thin) solid lines are for strong (weak) outflow cases with  $f = 0.1$  (0.01).

Nakamura & Li (2005), 2D, decaying, with AD.

- Non-magnetic
- ..... Strongly supercritical
- - - Moderately supercritical

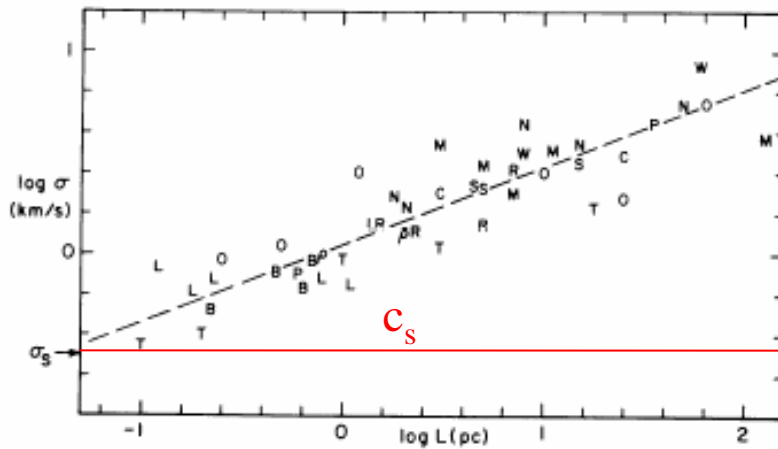
A model for the inhibitory effect of turbulence in stationary turbulent regimes (continuously driven), is based on the *sonic scale*  $\lambda_s$  (Padoan 1995; Vázquez-Semadeni et al. 2003; Krumholz & McKee 2005):

$\lambda_s$ : The scale across which the typical turbulent velocity difference equals the sound speed:

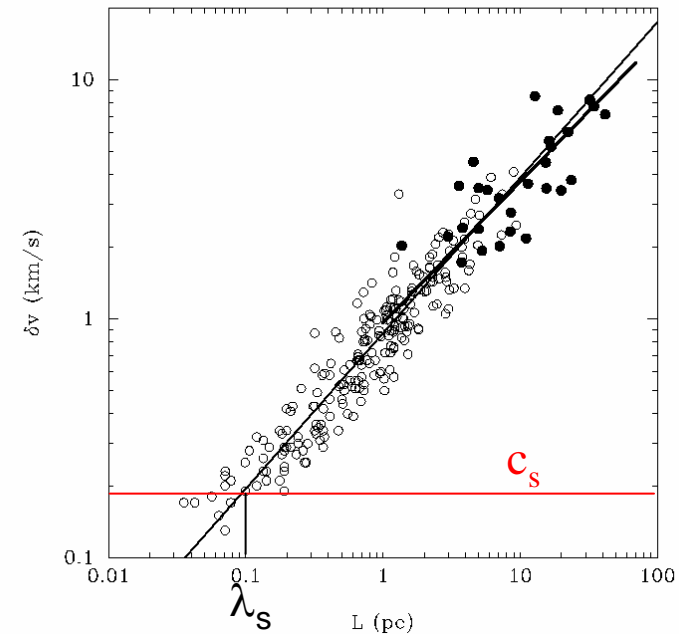
$$\Delta v \approx 0.8 \text{ km s}^{-1} \left( \frac{L}{1 \text{ pc}} \right)^\alpha$$

$\alpha \approx 1/2$

$$\lambda_s \sim 0.07 \text{ pc}$$



Larson 1981



Heyer & Brunt 2004

– Below  $\lambda_s$ :

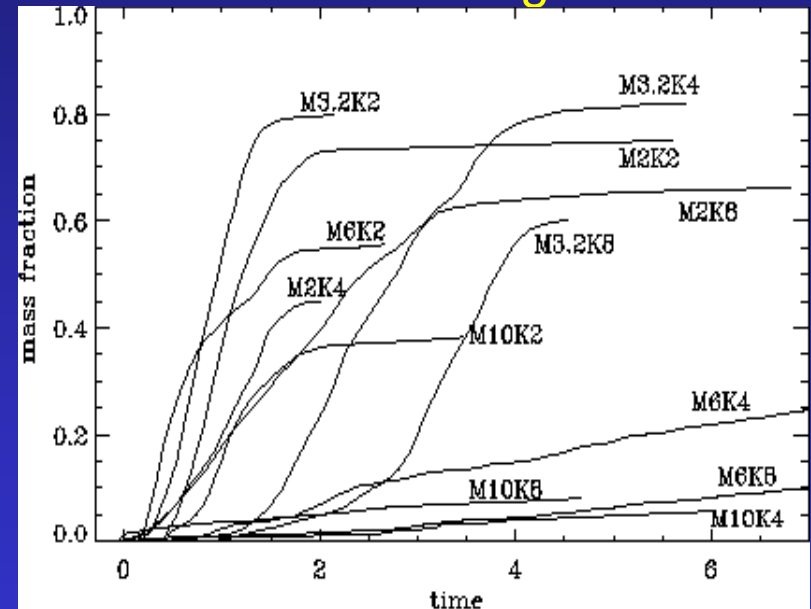
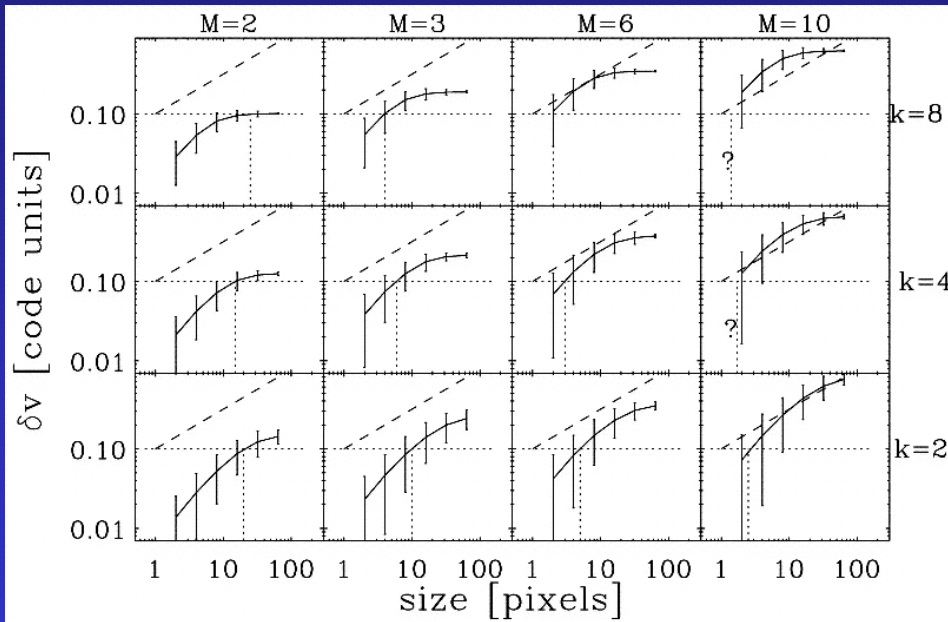
- Turbulent subfragmentation becomes weaker ( $\delta\rho/\rho \sim M_s^2 < 1$ ) (or  $\sim M_a$  for MHD turbulence – Padoan & Nordlund 2002)
- Turbulent support becomes subdominant ( $\delta u_{\text{turb}} < c_s$ ).

→ Maybe SFE related to fraction of mass in Jeans-unstable cores of size  $< \lambda_s$ ? (i.e., “super-Jeans”, subsonic cores).

- Supported by simulations of varying  $M_s$  and driving scale at constant  $J=L/L_J=4$  (Vázquez-Semadeni, Ballesteros-Paredes & Klessen 2003, ApJ 585, L131).

– Sonic scale and SFE measured in the simulations:

SFE measured as collapsed mass fraction after 2 crossing times.



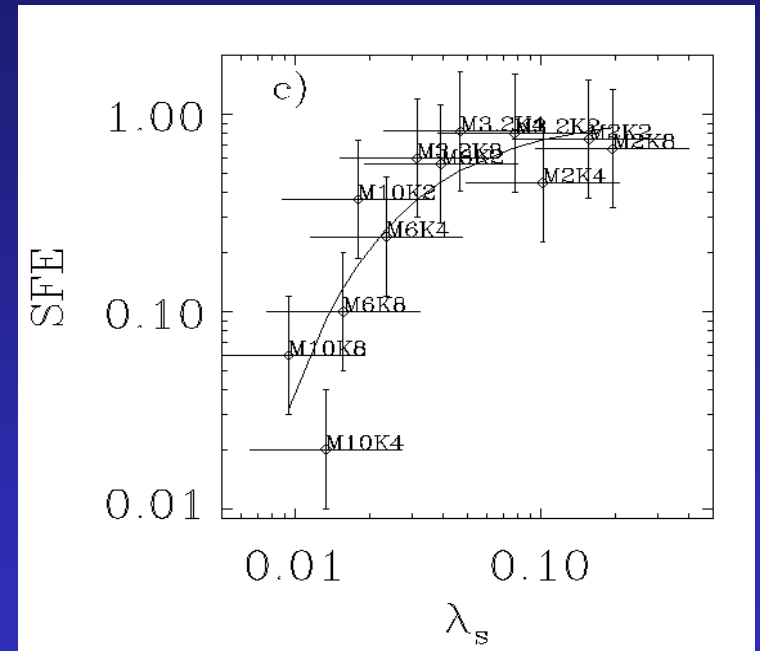
$\lambda_s$  decreases with increasing levels of turbulence at given T.

$M_s$	2	3.2	6	10
$2\tau_c/\tau_0$	12.5	10	6.7	2

$$\tau_0 \sim 2/3 \tau_{ff}$$

SFE depends monotonically on  $\lambda_s$   
(regardless of driving length)

$$\text{SFE}(\lambda_s) \propto \exp(-\lambda_0 / \lambda_s)$$



Vázquez-Semadeni et al. 2003

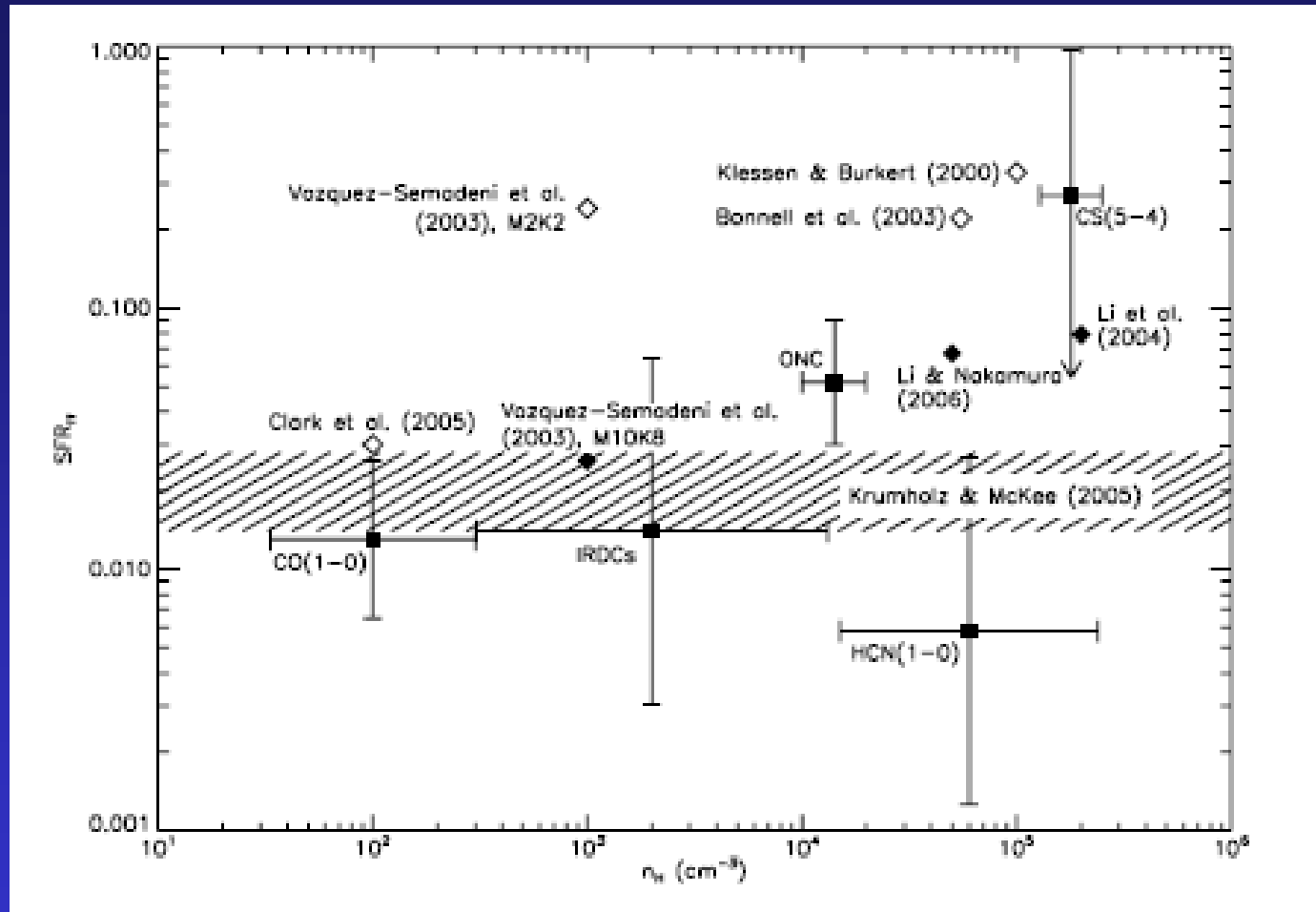
- The model has been extended by (Krumholz & McKee (2005) to use the ratio of  $\lambda_s$  to the Jeans length  $L_J$  as the condition for gravitational collapse,
- Select the regions from lognormal density PDF (Vázquez-Semadeni 1994; Padoan et al 1997; Padoan & Nordlund 2002)
- for obtaining the SFE after one free-fall time

$$\text{SFR}_{\text{ff}} \approx 0.014 \left( \frac{\alpha_{\text{vir}}}{1.3} \right)^{-0.68} \left( \frac{\mathcal{M}}{100} \right)^{-0.32}.$$

where

$$\alpha = \frac{E_{\text{kin}}}{|E_{\text{grav}}|} \propto \left( \frac{\mathcal{M}}{J} \right)^2$$

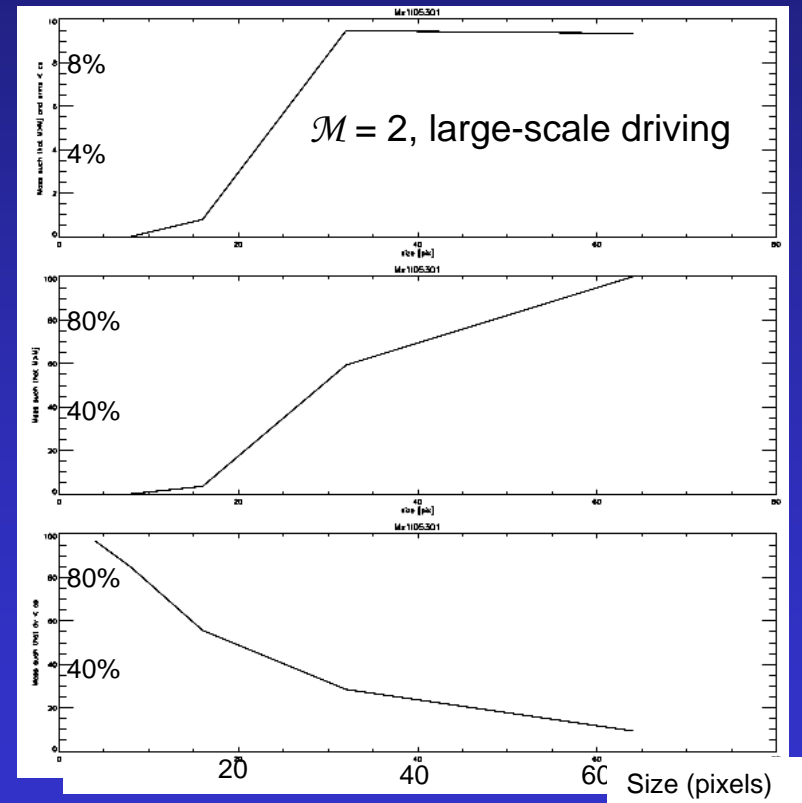
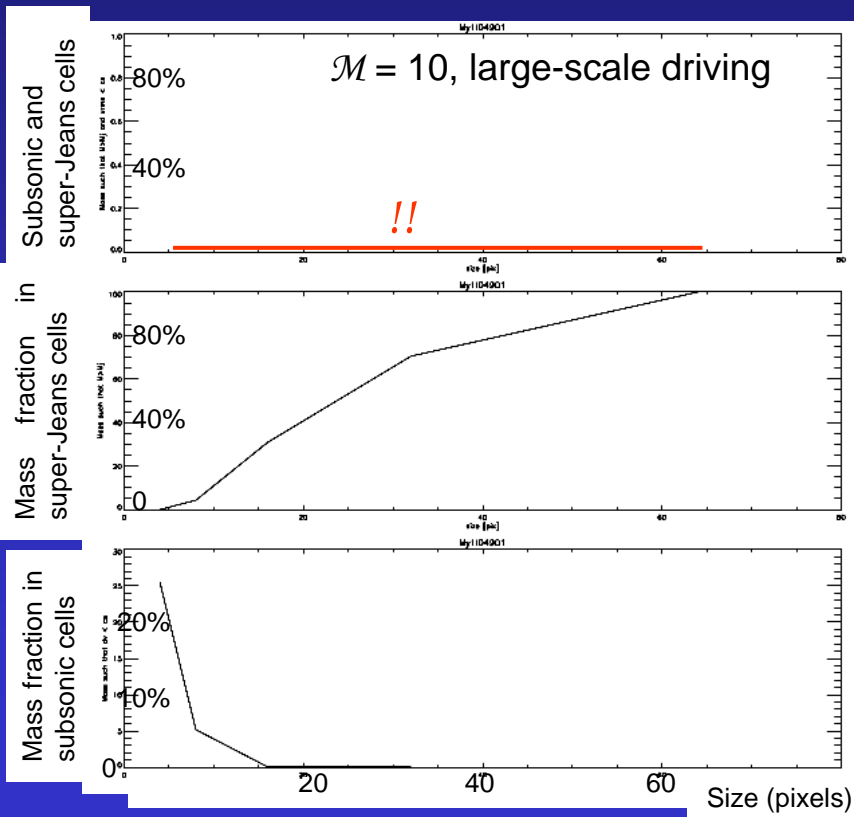
is the *virial parameter*.  $\mathcal{M}$  is the rms Mach number and  $J$  the Jeans number ( $L/L_J$ ).



Krumholz & Tan 2007

## However (#1)...

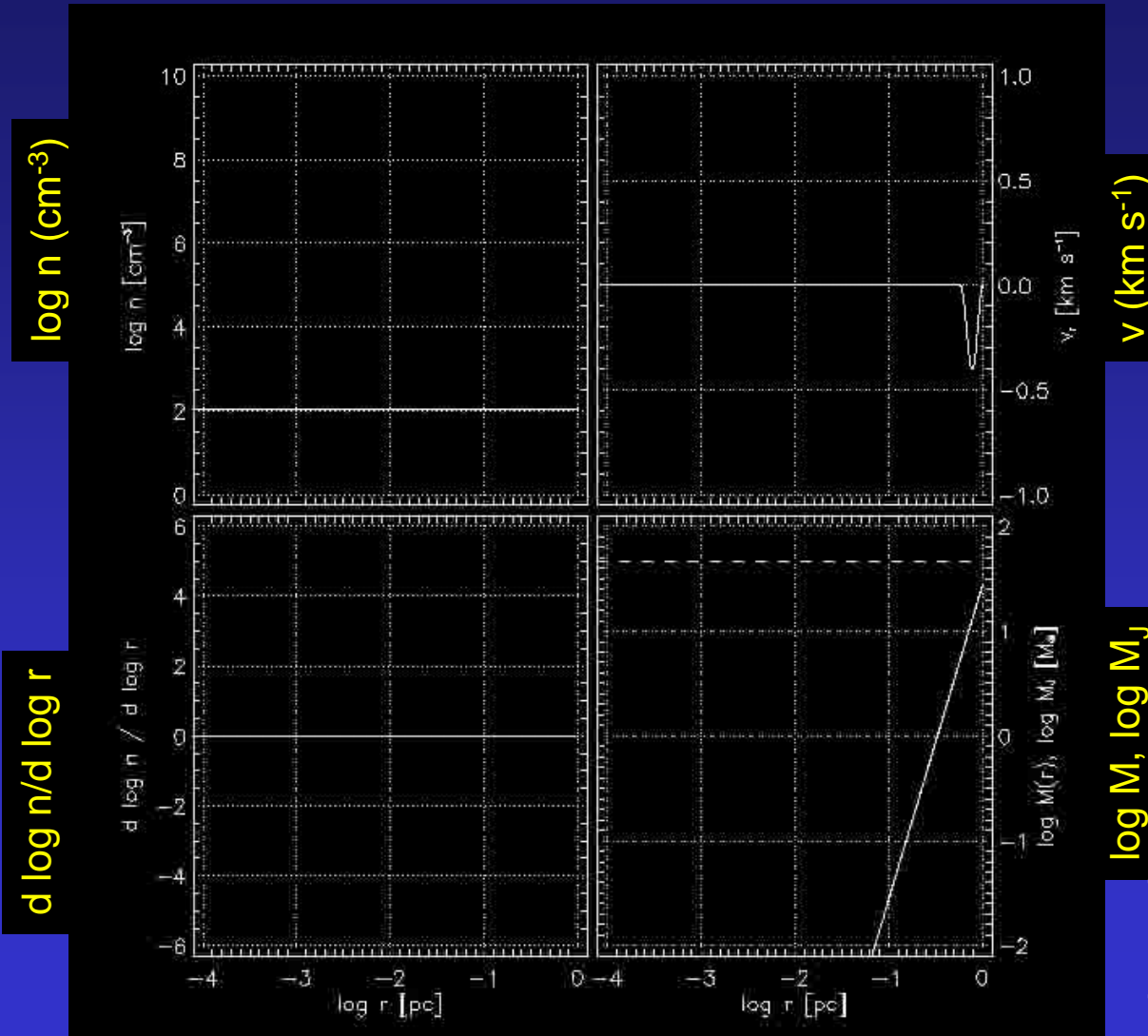
- Fraction of mass in subsonic, super-Jeans cells as function of cell size may be lower than mass in collapsed objects, even zero at large Mach numbers (Vázquez-Semadeni & Ballesteros-Paredes, in prep.)



Subcells in simulation, not clumps.



- There **must** be some subsonic, super-Jeans structures:
  - Quiescent starless cores.
  - Seen in idealized simulations...

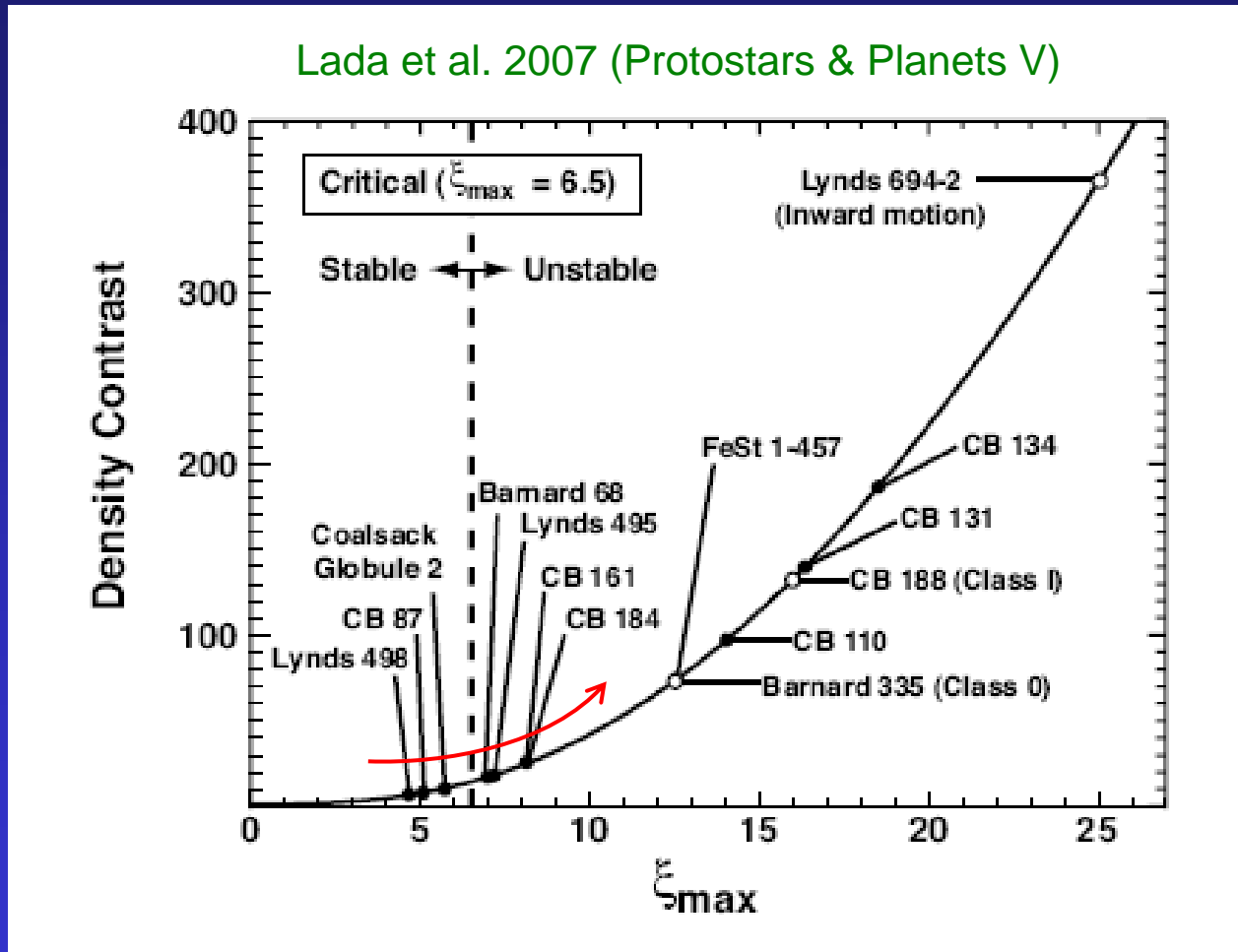


Growing, ram-pressure confined BE spheres.

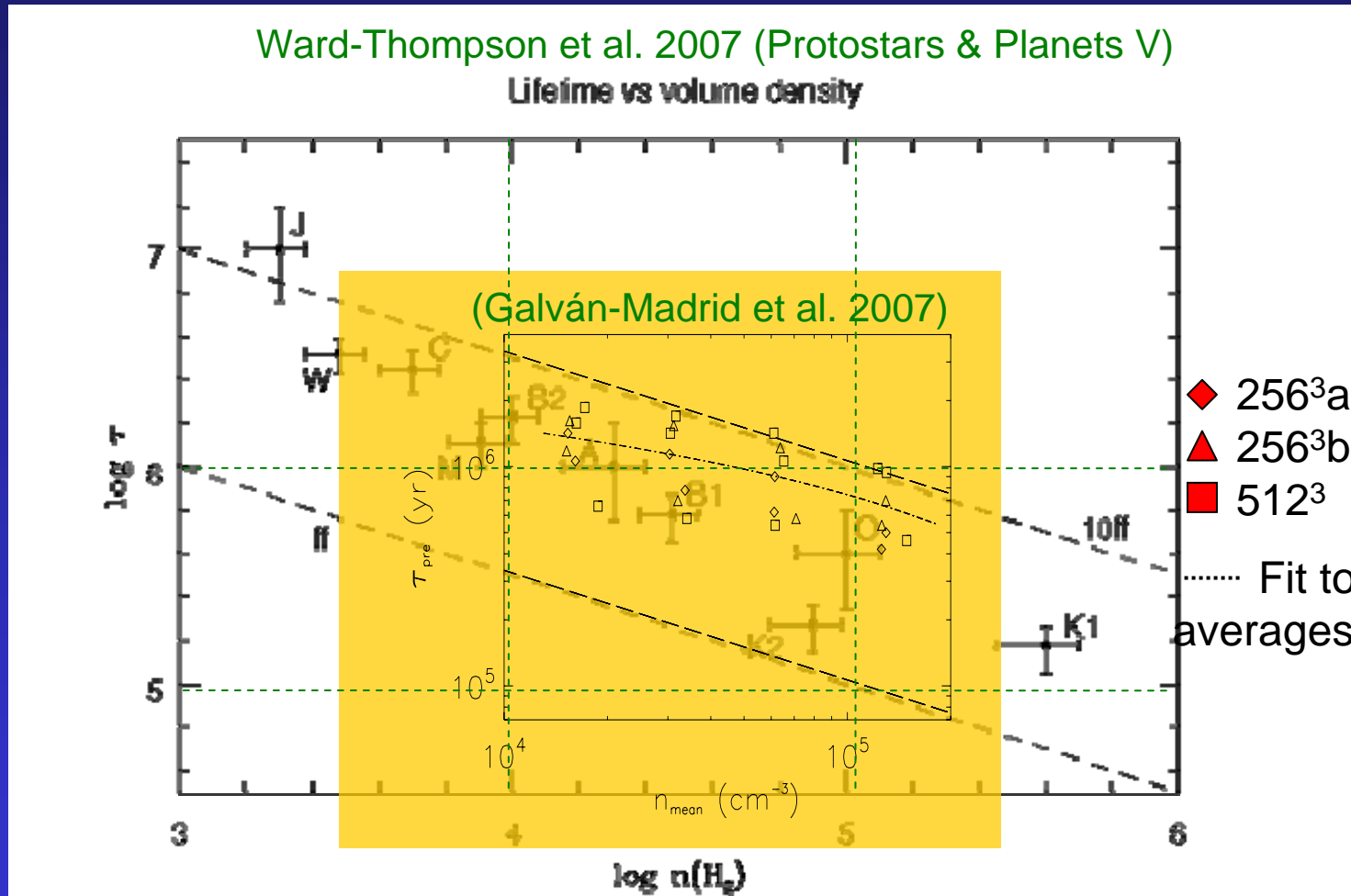
—  $M(r)$

----  $M_J(r)$

- ... which evolve along the stability sequence:

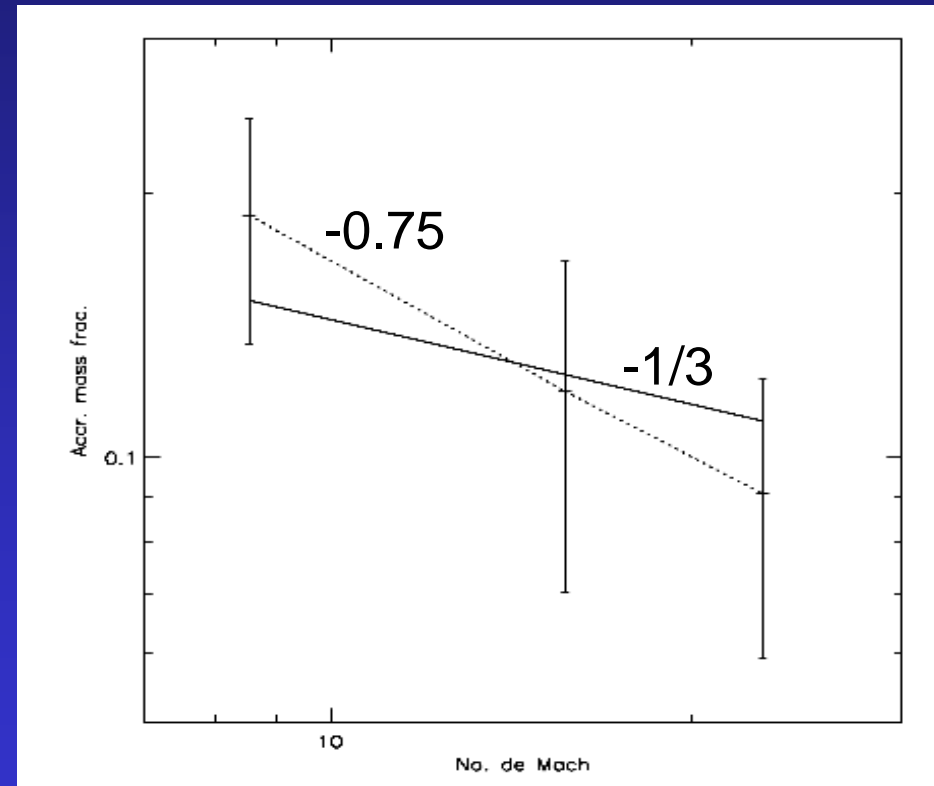
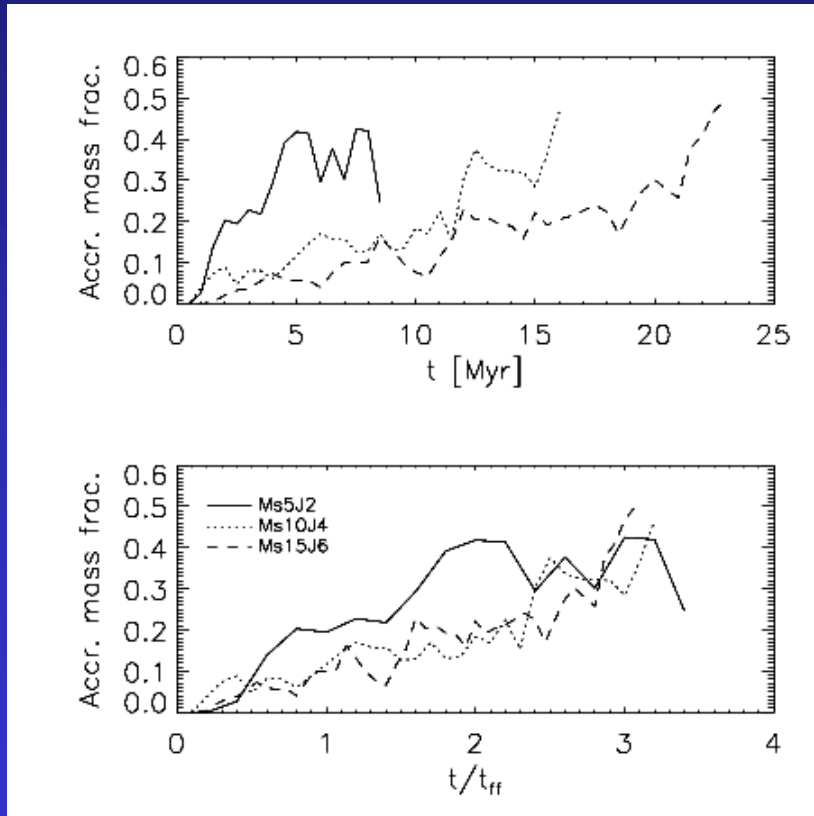


- Collapse times in moderately supercritical MHD isothermal, driven simulations (“prestellar lifetimes”): 2—10  $\tau_{\text{ff}}$ .
  - Consistent with observations.



(Galván-Madrid et al. 2007, ApJ in press, arXiv/0704.3587)

- **However #2:** Numerical simulations of turbulent clouds with various Mach numbers, keeping  $\alpha$  cst. are marginally consistent with the sonic-scale/ $L_J$  model.



Vázquez-Semadeni, González & Kim, 2007, in prep.

- Conclude:

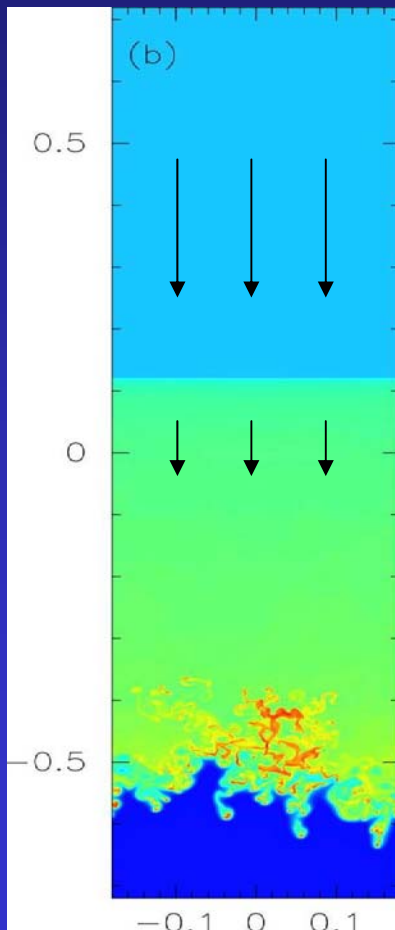
- Not all collapsing mass may come from subsonic, super-Jeans structures (Bate, Bonnell et al...)
  - Correlation between SFE and  $\lambda_s$  may be representative of disruptive effect of turbulence, but not exhaust mass reservoir for collapse.
  - Need full virial balance studies (e.g., Tilley & Pudritz 2004, 2005; Dib et al. 2007), but correlating with SFE.
- Moreover, all these studies have been in closed boxes. A certain lifetime for the clouds has to be *assumed*.
  - Cloud lifetimes need to be assessed to understand SFE.

→ Cloud evolution studies.

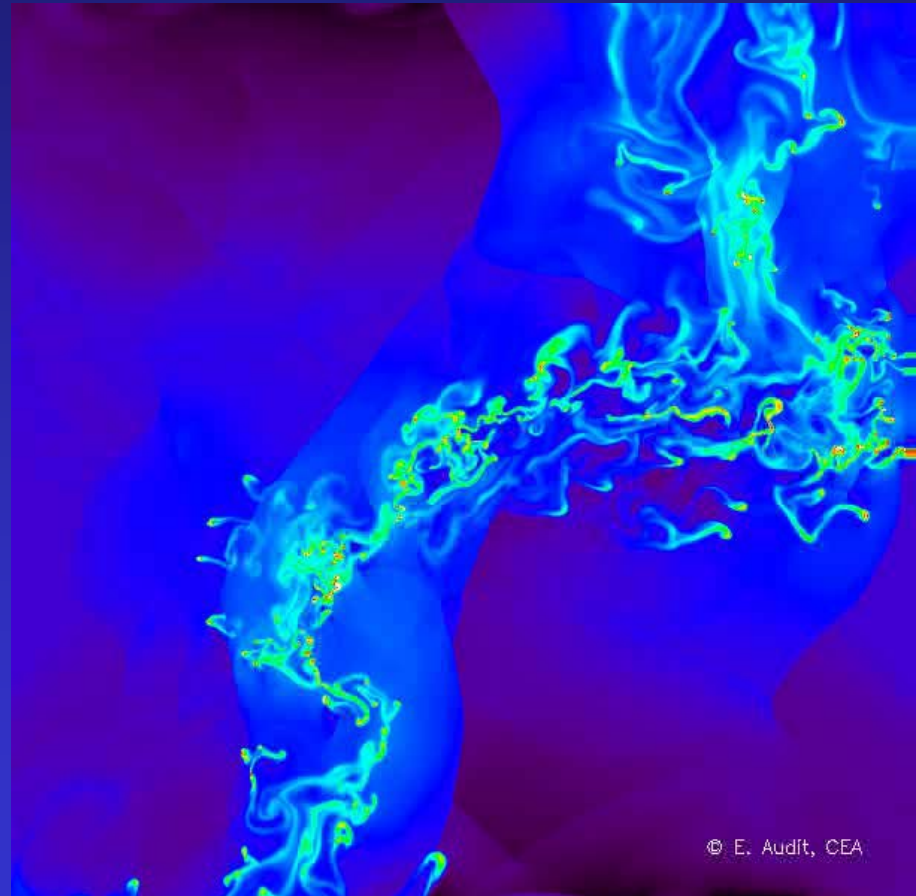
### III. MC FORMATION AND EVOLUTION (“BRIEF” SF?)

- Some key questions in MC evolution:
  - How do they form?
    - Large-scale instabilities mainly? (Mac Low and Ostriker talks)
    - Cooling and thermal instability are essential (Hennebelle & Pérault 1999, 2000; Koyama & Inutsuka 2000, 2002; Heitsch et al. 2005, 2006; Audit & Hennebelle 2005, 2007; Vázquez-Semadeni 2006, 2007).
      - Can trigger turbulence with transonic compressions.
  - How do they get their turbulence and how long is it driven?
  - How long do they live?

- Two kinds of models for driving/lifetime of GMCs:
  - 1) Turbulence “built in” from formation mechanism from diffuse atomic ISM (Vishniac 1994; Walder & Folini 2000; Koyama & Inutsuka 2002, 2004; Audit & Hennebelle 2005; VS et al. 2003, 2006; Heitsch et al. 2005, 2006).
    - **Natural** way of driving turbulence (including duration).

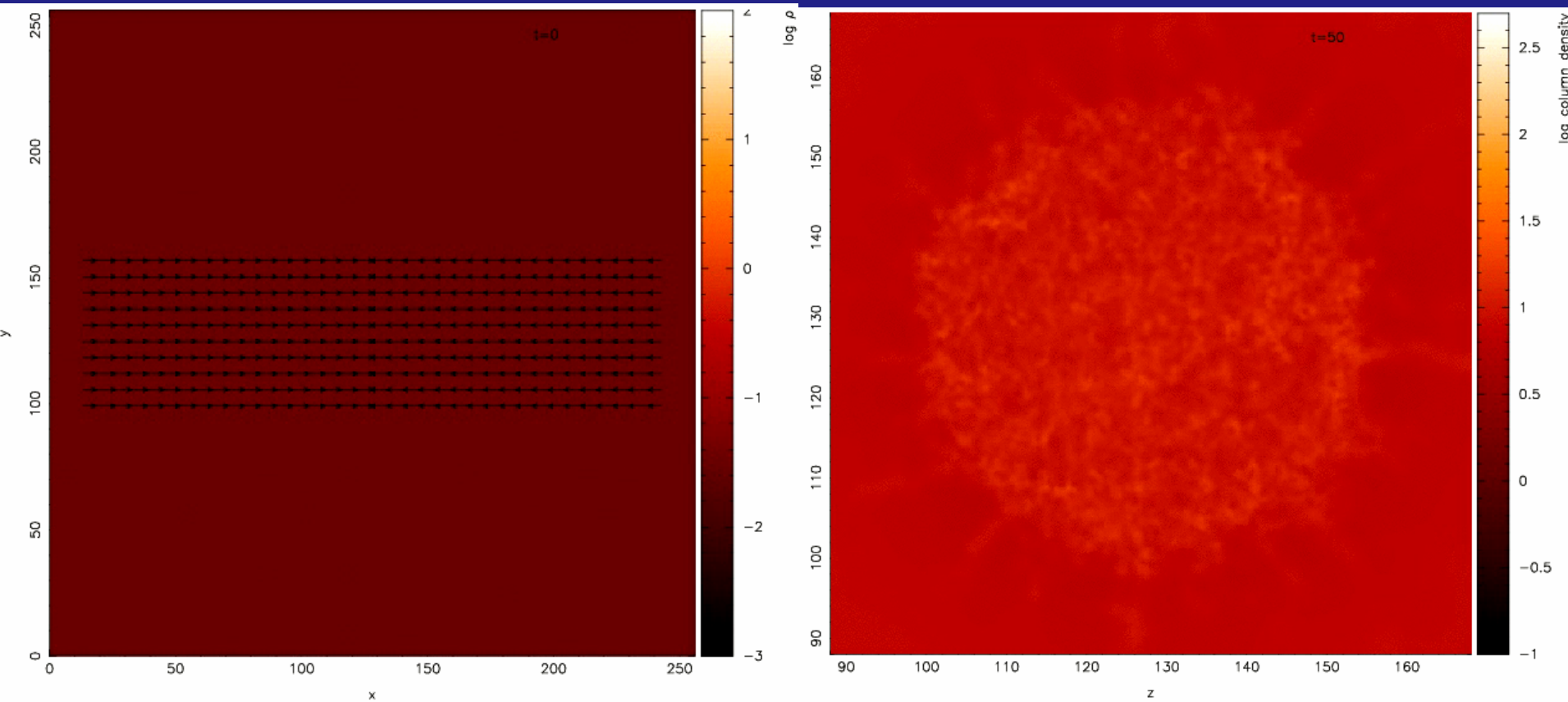


Koyama & Inutsuka 2002



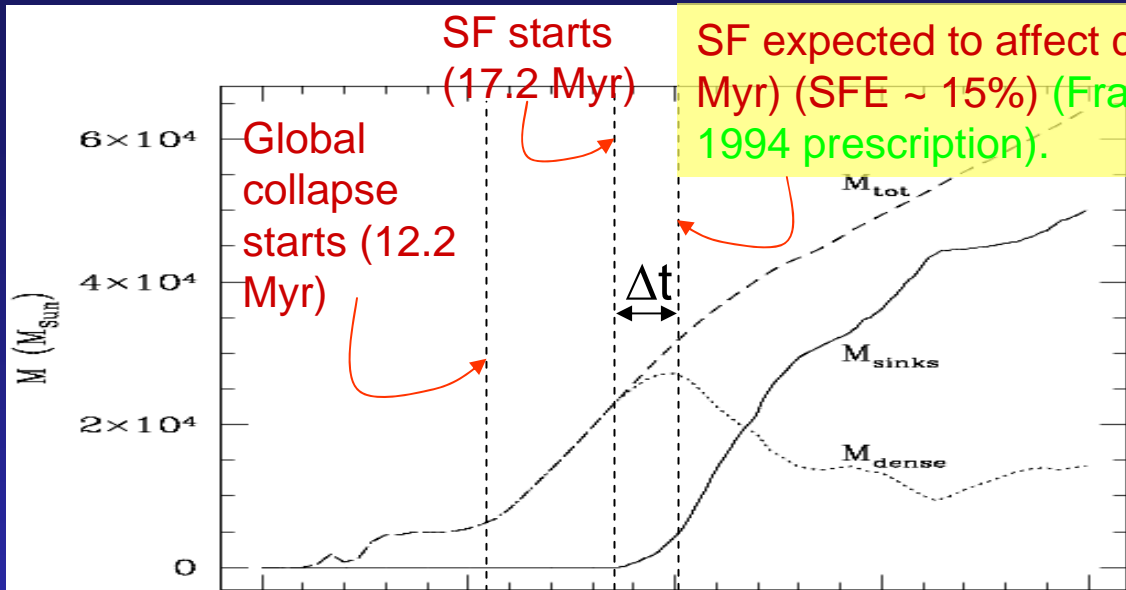
Audit & Hennebelle 2005

- SF proceeds rapidly and briefly (Ballesteros-Paredes et al. 1999; Elmegreen 2000; Hartmann et al. 2001).
- $E_{\text{kin}}$  at later times driven by gravity (Hartmann & Burkert 2007; VS et al. 2007).
- Clouds probably dispersed shortly after SF episode (e.g., Whitworth 1979; Franco et al. 1994; Hartmann et al. 2001; VS et al. 2007; Elmegreen 2007).



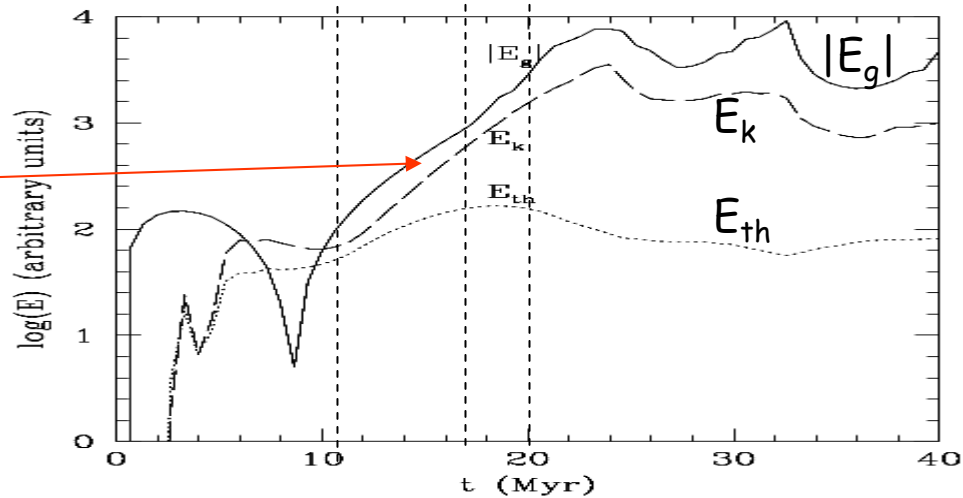
(Vázquez-Semadeni et al. 2007, ApJ 657, 870)





SF expected to affect cloud (20.3 Myr) (SFE  $\sim$  15%) (Franco et al.'s 1994 prescription).

SFR not small, but  $\Delta t$  may be small.



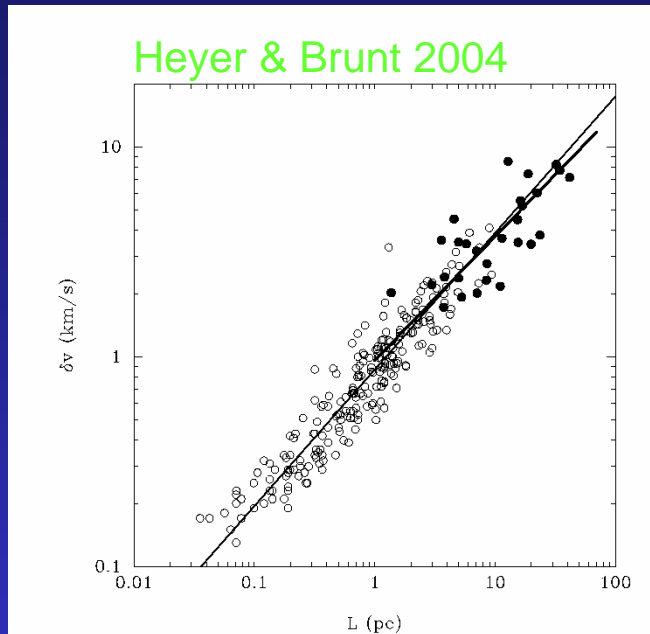
Turbulent  $E_{\text{kin}}$  fed by collision first, then by gravitational contraction.

Turbulent driving decays on time. Intermediate between driven and decaying.

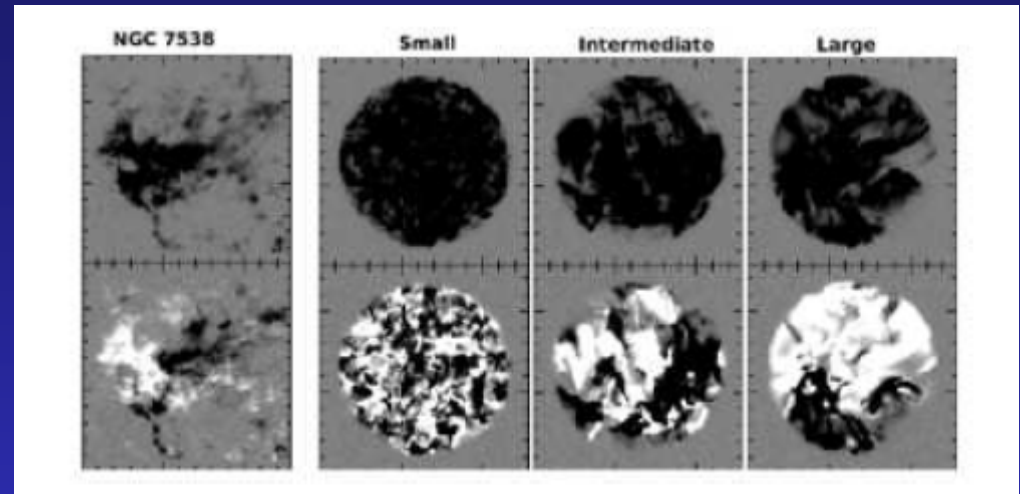
Run with:  
 $L_{\text{box}} = 256 \text{ pc}$ ,  
 $L_{\text{inf}} = 112 \text{ pc}$

(Vázquez-Semadeni et al. 2007)

– (Indirect) evidence in favor of externally-driven turbulence:



a) A universal scaling law, independent of SF activity.

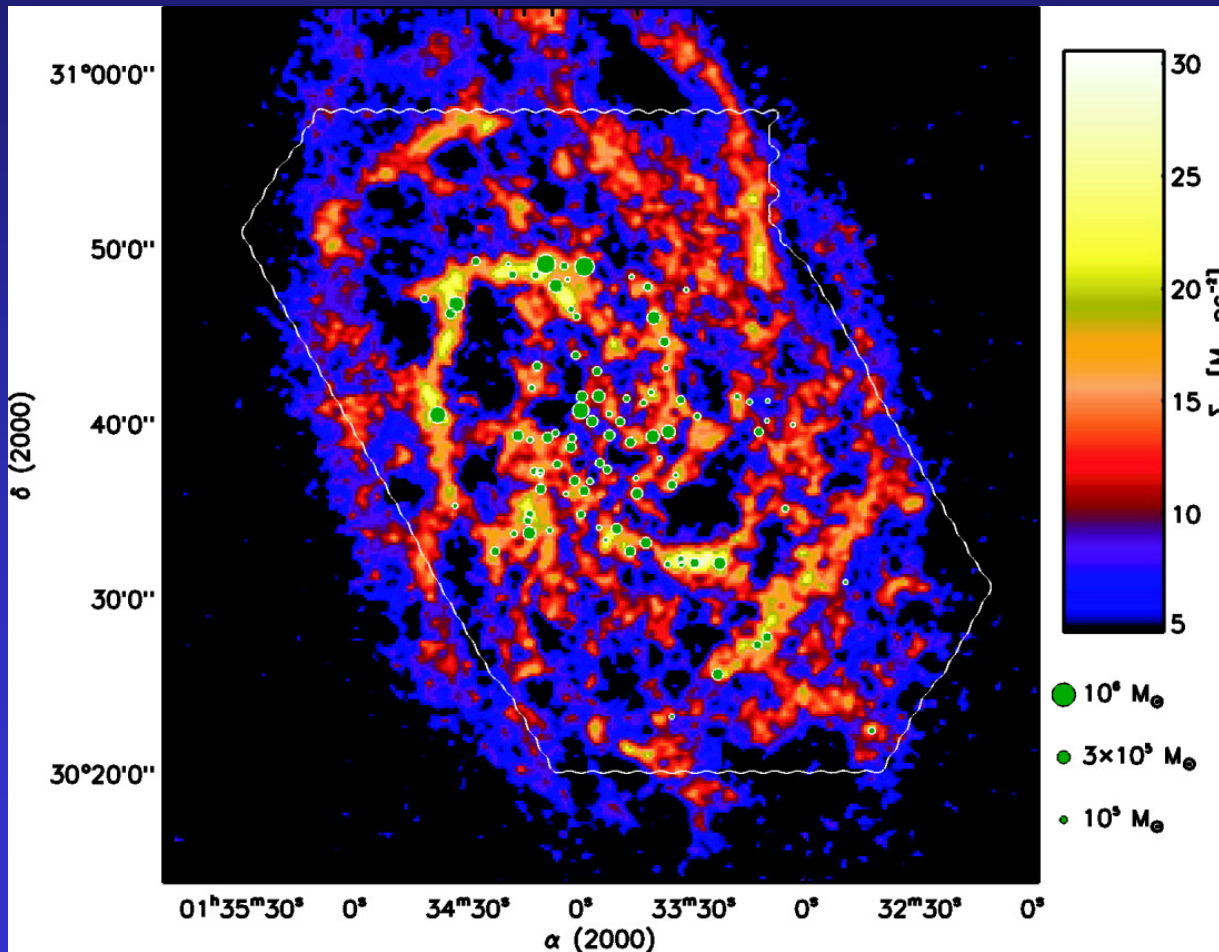


Heyer & Brunt 2007

b) A universal “dipole” large-scale mode. Consistent with “driving from the outside”.

- Suggest a (turbulent?) cascade from larger scales.
- No decay?

c) GMCs are not isolated, but rather the “tip of the iceberg” (or the “white caps”) of the galactic density distribution (e.g., Blitz et al. 2007, PPV).



Color image: HI distribution

Circles: CO

They conclude that GMCs *form* out of the HI.

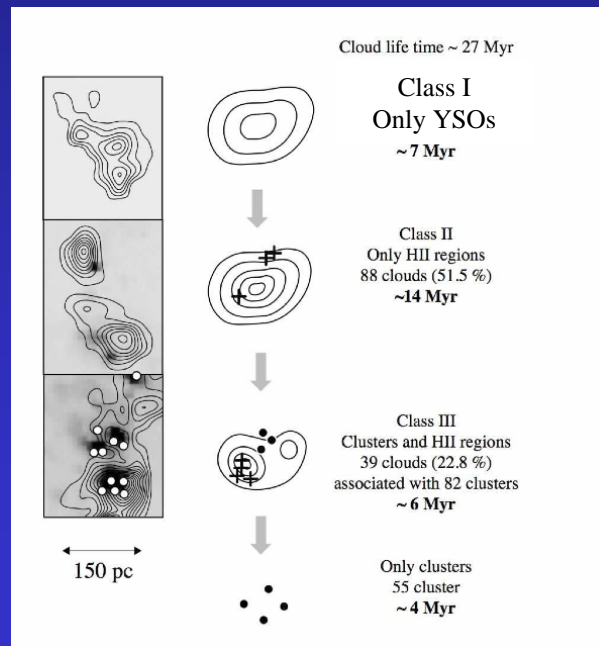
→ GMC dynamics are part of global ISM dynamics.

- Two kinds of models for driving/lifetime of GMCs (cont'd):

2) From stellar feedback (Whitworth 1979; McKee 1989; Matzner & McKee 1999; Matzner 2002; Krumholz et al. 2006; Nakamura & Li 2007; Nakamura's talk).

- SF may proceed slowly over relatively long times (Palla & Stahler 2000, 2002; Krumholz & Tan 2006).

- (Indirect) evidence in favor of internally-driven turbulence:



Apparently long lifetimes (25-30 Myr) of GMCs in external galaxies.

**BUT:** “GMCs are probably *not* in virial equilibrium”:

- highly filamentary
- not very centrally concentrated

- But are clouds supported or disrupted by stellar feedback?
  - Evidence in favor of quick cloud dispersal:
    - Clusters older than ~5-10 Myr are usually devoid of gas (Leisawitz et al. 1989; Fukui et al. 1999).

## Observed in simulations with HII-region like driving:

250

J. BALLESTEROS-PAREDES 2004

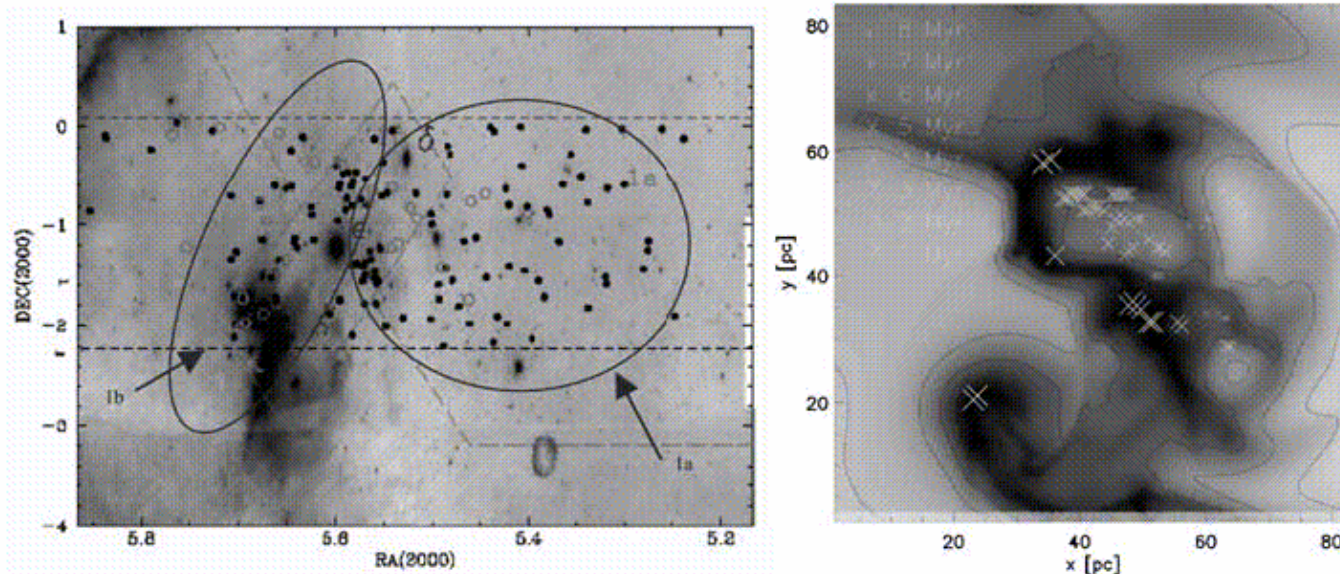
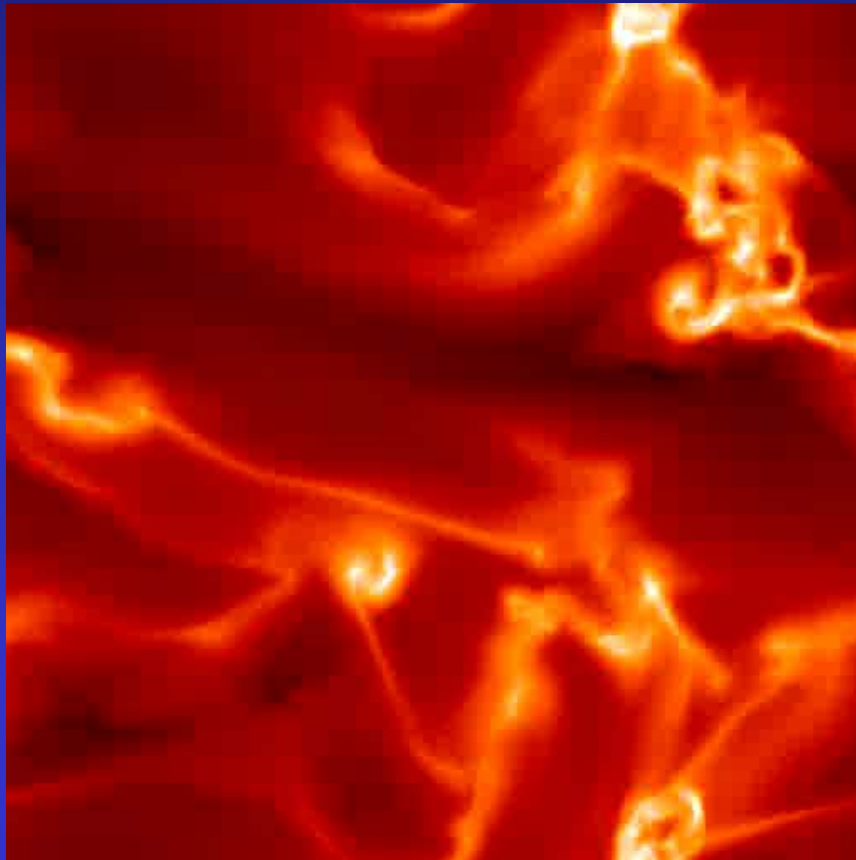


Figure 1. a. Orion OB1 association. b. Cloud in simulations from (Passot et al., 1995). Note that stars of more than 5 Myr old are 10 pc or more far from the dense gas. The simulation was not intended to reproduce the particular behavior of Orion.

Gas pushed sideways from SF regions.



- Stellar-driven “equilibrium GMC” concept may operate in an averaged sense over sufficiently large volumes.
- Locally clouds can be dispersed, but globally GMCs may “persist”.



$L = 1 \text{ kpc}$

$\Delta t = 50 \text{ Myr}$

Including: self-gravity,  
B, HII-like feedback.

A multi-timescale process  
(Elmegreen 2000).

Passot, et al. 1995

- CONCLUSIONS

- Turbulence provides an effective filter for the mass that can collapse in a MC.
- SFE levels below 10% over times  $\sim \tau_{\text{ff}}$  (“slow SFR”) can be obtained *in closed boxes* with either
  - Stationary supersonic turbulence in magnetically supercritical clouds.
  - Decaying turbulence in moderately magnetically subcritical clouds.
  - Perhaps reality in intermediate, gradual decay regime?
- Super Jeans-, subsonic-fraction model of “mass filtering” for collapse explains low SFE.

– However:

- Subsonic, super-Jeans model may possibly miss part of the total mass involved in collapse.
- Effect of turbulent Mach number and magnetic field strength depend on nature of turbulence (driven or decaying).
- Numerical models of cloud *and* star formation suggest
  - Turbulence from formation mechanism (at least initially).
  - *SFR may be not so small,*
    - » but *then need brief  $\Delta t$*  (due to SF feedback?)
- All models **assume** a cloud lifetime
  - Longish  $\Delta t$  for slow SFR.
- Observations suggest turbulence driven from the outside of clouds.
  - Rather than from stellar feedback?
  - Does stellar feedback then disrupt parent clouds?

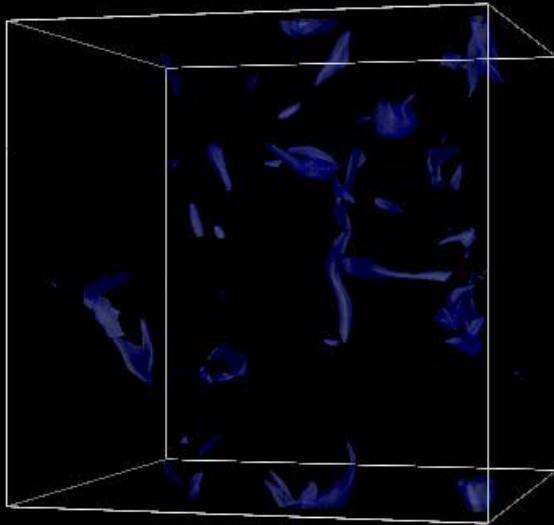


– Need:

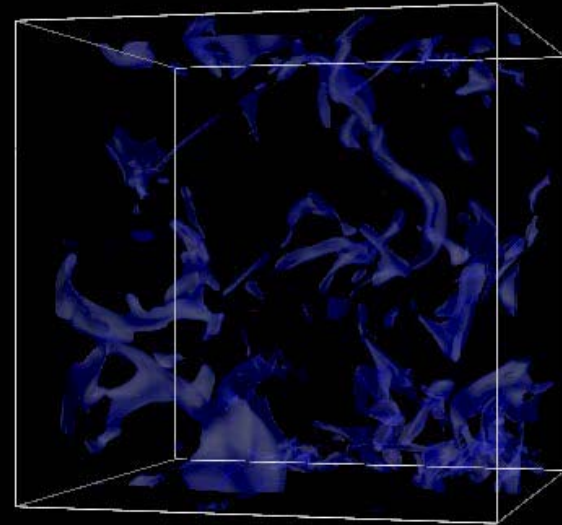
- Studies of cloud evolution+SFE including stellar feedback and magnetic fields in open boxes to determine:
  - Determination and evolution of clouds' physical parameters.
  - Mechanism and duration of turbulence driving.
  - Duration of SF episodes as a function of scale size.
  - Role of magnetic fields.

The End

- Additional result: Magnetically supercritical case produces fewer but more massive collapsed objects than non-magnetic case.

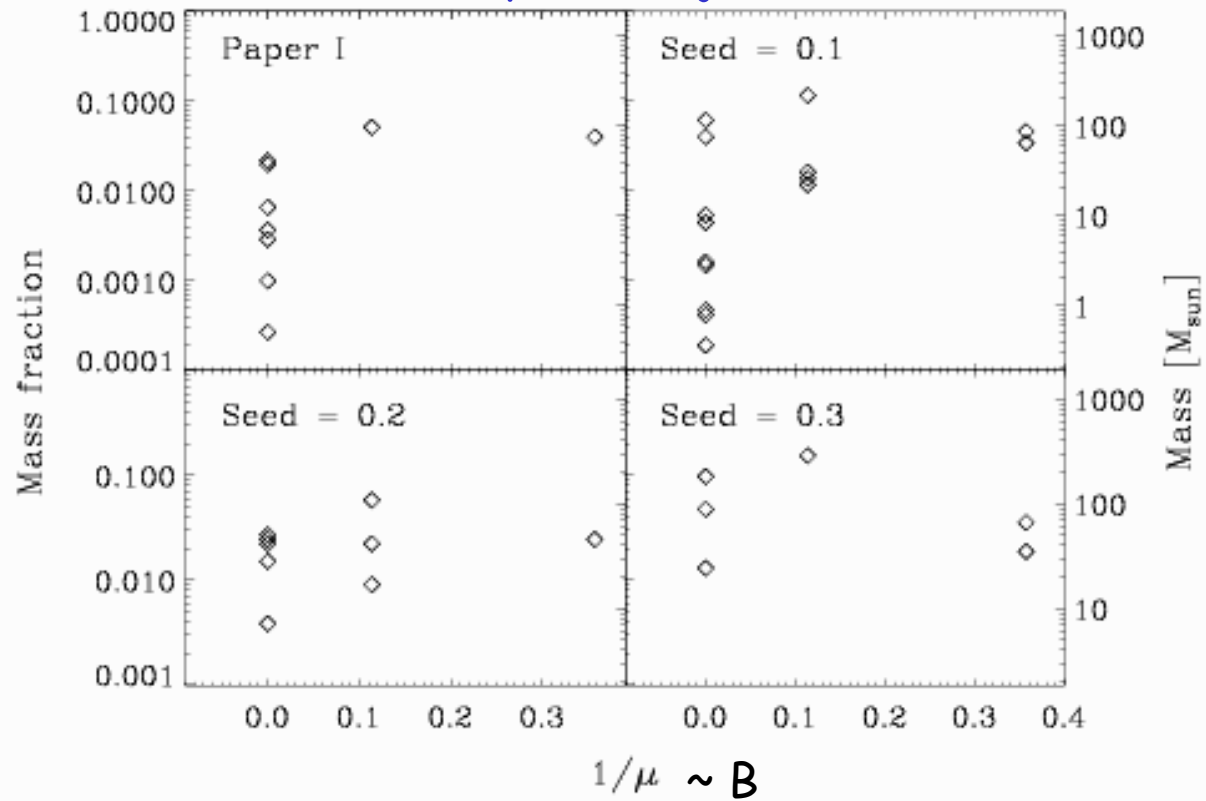


3D MHD, moderately supercritical,  $\mu = 2.8$



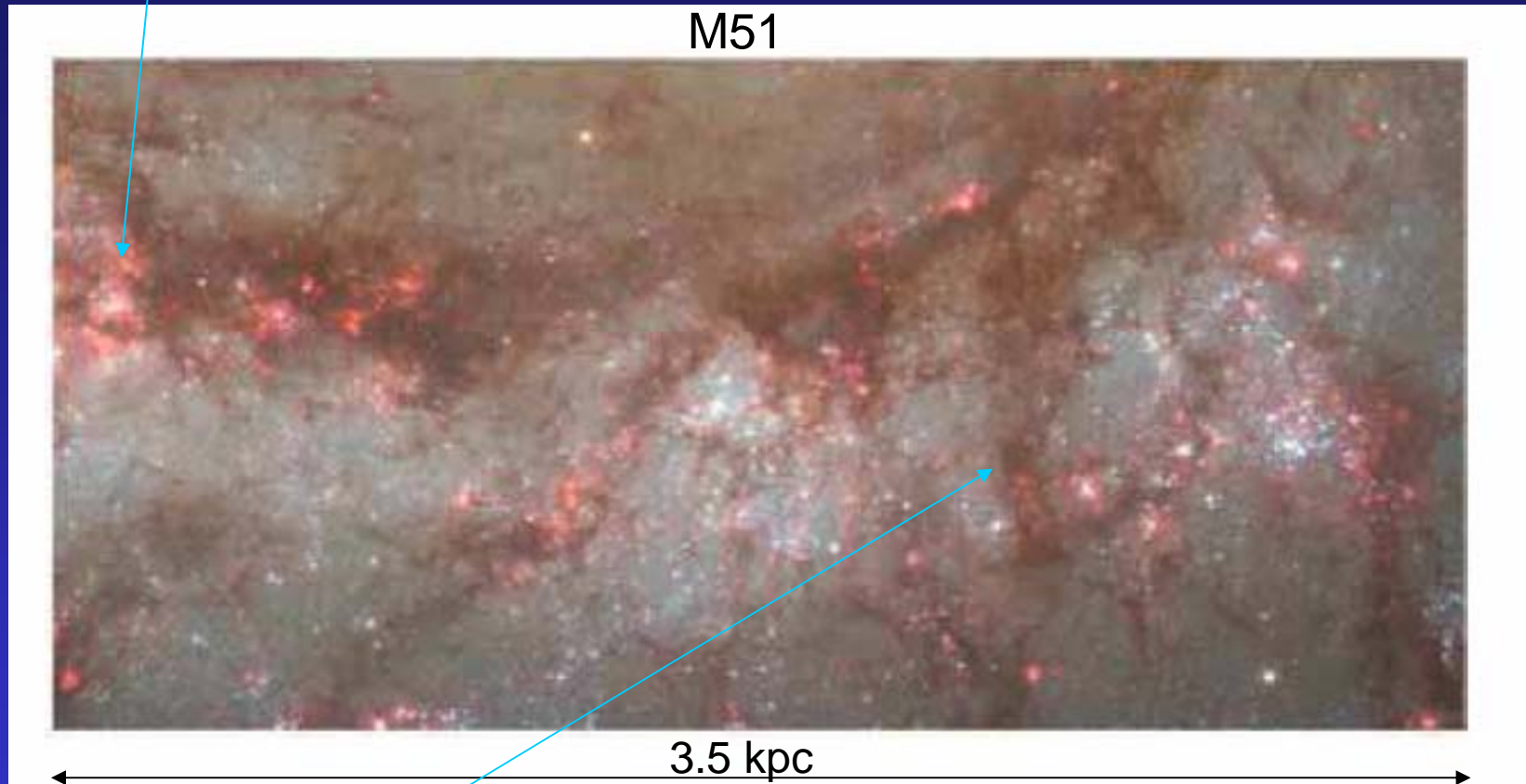
3D non-magnetic

## Masses of collapsed objects vs. $B \sim 1/\mu$



Vázquez-Semadeni, Kim & Ballesteros-Paredes (2005)

“Instantaneous” SF  
on the dust lane.



Shredded material  
and secondary SF  
behind arm.

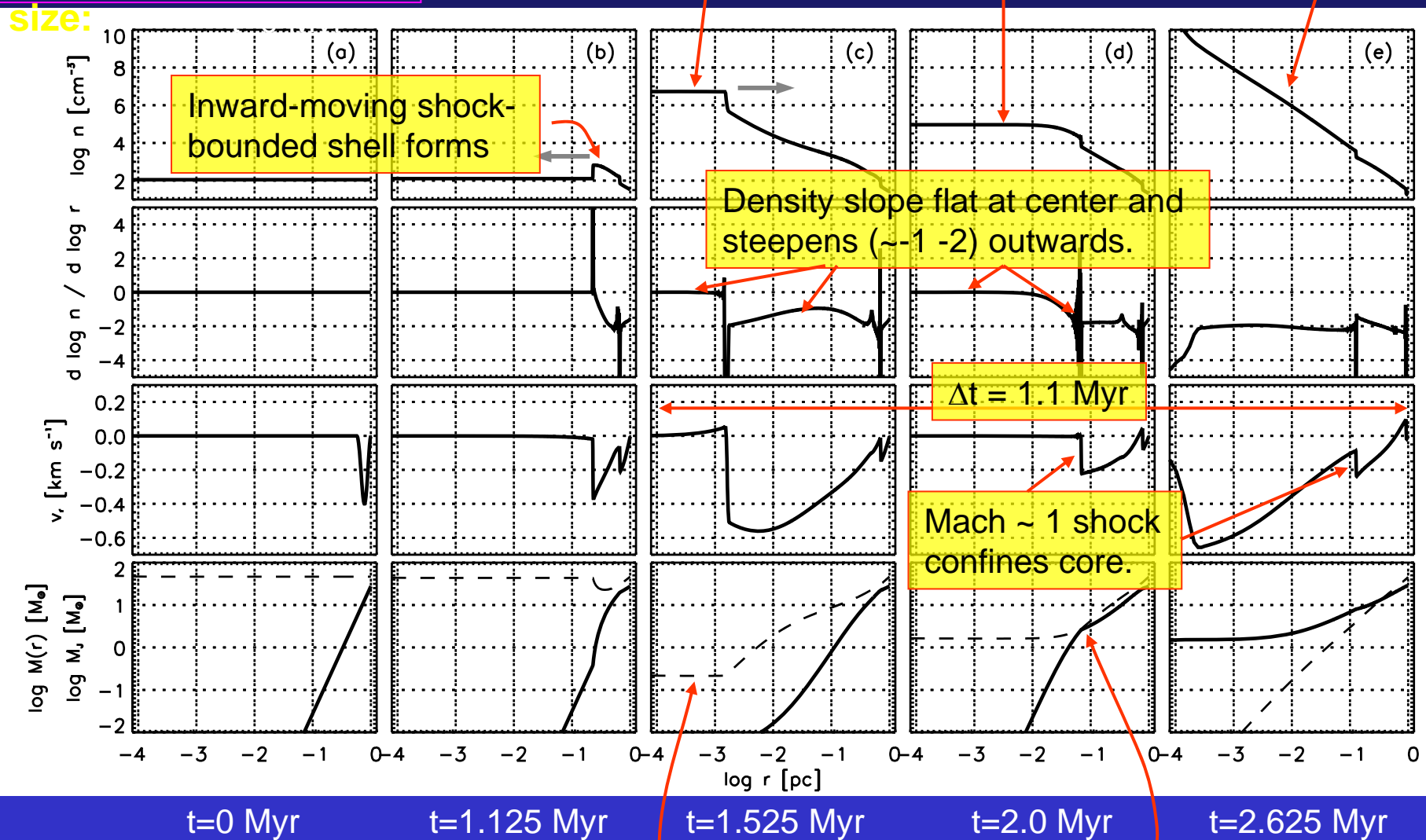
Elmegreen 2007.  
See also Ballesteros-Paredes  
& Hartmann 2007.

**Compression forms central core that grows in mass and size:**

Non-self-gravitating central core with high uniform density.

Self-gravitating central core with BE-like density profile.

Collapsed core, with SIS profile.



Gómez et al. 2007, ApJ in press, arXiv/0705.0559

Jeans mass decreases in central dense core.

Core's mass catches up with Jeans mass.