

# Competitive Accretion in Stellar Clusters

Ian Bonnell  
(St Andrews)

Matthew Bate, Paul Clark,  
Ralf Klessen, Jim Dale

# Origin of stellar masses

- **Turbulently driven fragmentation**
  - Structure in molecular clouds
  - Clump mass spectrum: IMF
- **Gravity driven fragmentation**
  - ~ thermal Jeans masses
  - Accretion in clusters produces higher masses
  - Low masses from gravity-produced dense gas
- SPH Simulations: **self-gravitating decaying turbulence**
  - $E_{\text{kin}} \geq |E_{\text{grav}}|$
  - No Magnetic fields
  - Some feedback!



# Origin of stellar masses: context

- Need to understand SF in context of forming full IMF

M. McCaughrean

- many/most stars form in clusters

- Full IMF

- ~ All higher mass stars

De Wit et al 2005

- Massive stars in centre

- Binaries

- Disks

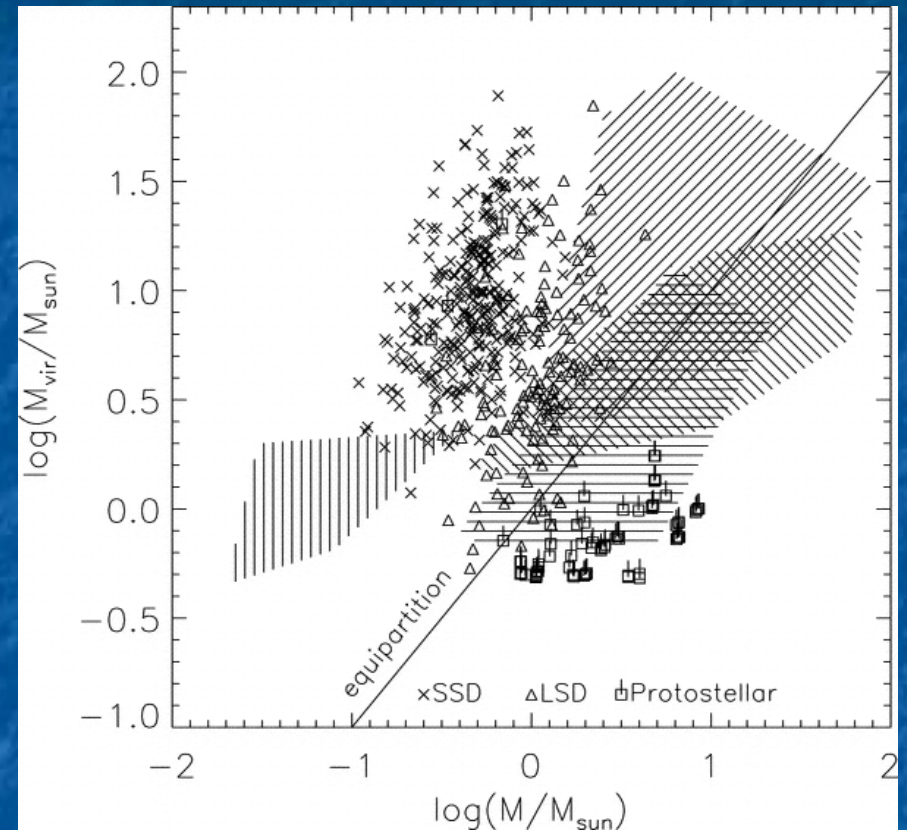
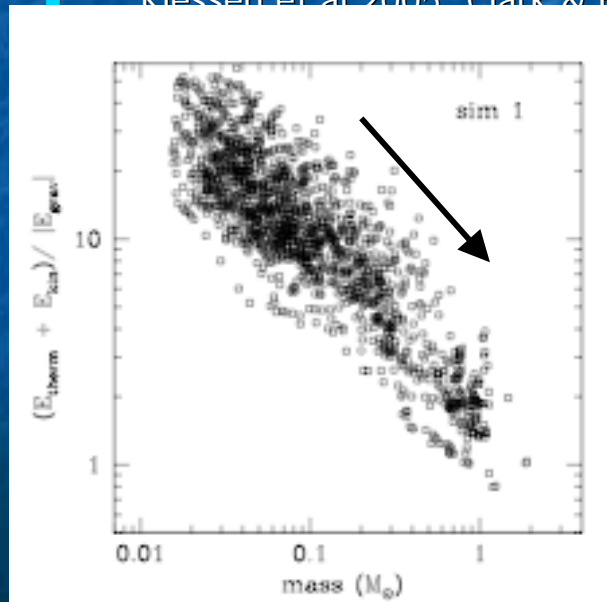


The Orion Nebula and Trapezium Cluster  
(VLT ANTU + ISAAC)

# Turbulent Fragmentation

- Produces full clump mass
- fn
- But low masses unbound
- High-mass clumps fragment
- Star formation occurs  $\sim$  Jeans Mass

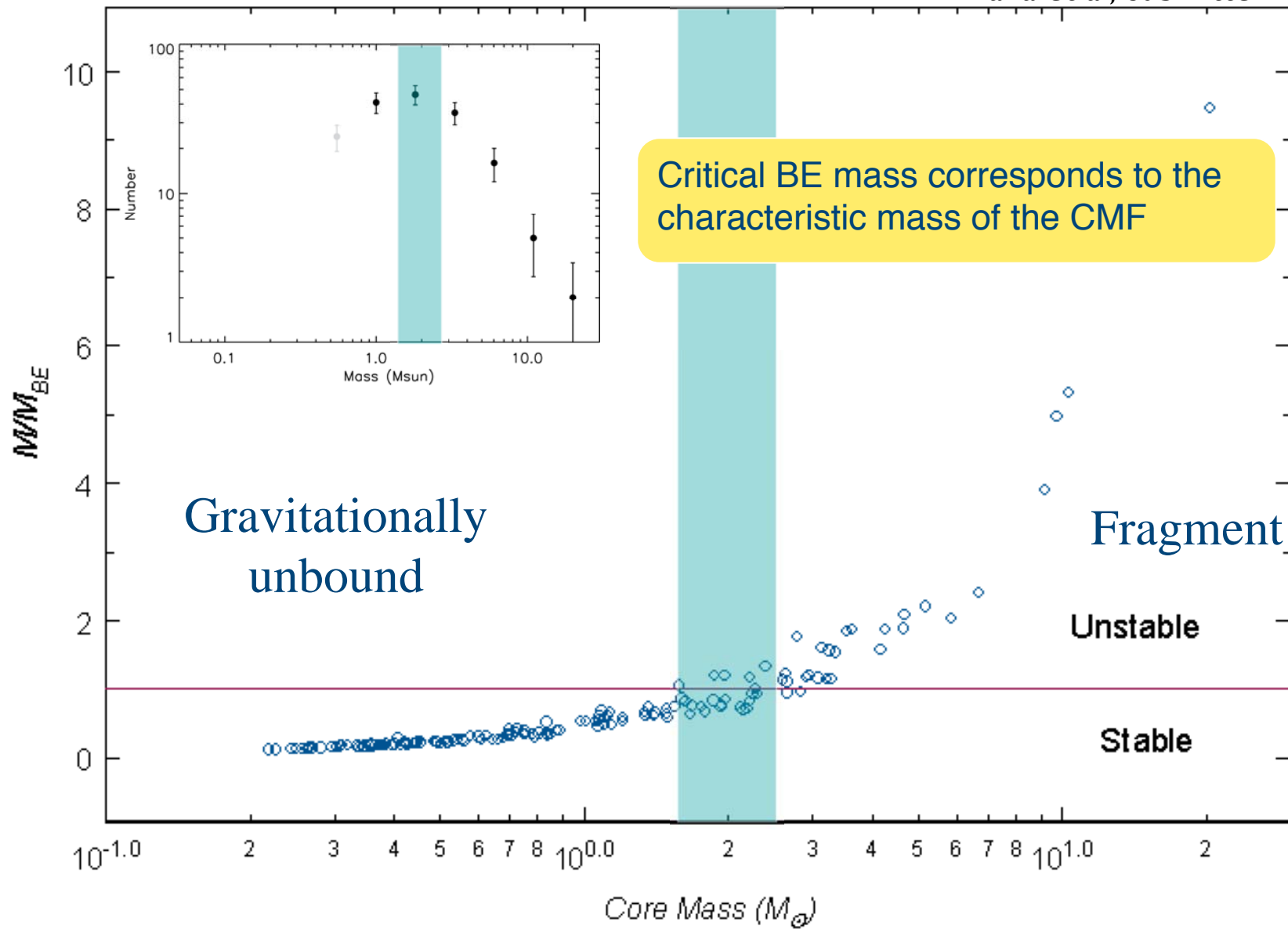
Klessen et al 2005; Clark & Bonnell



Klessen et al 2005

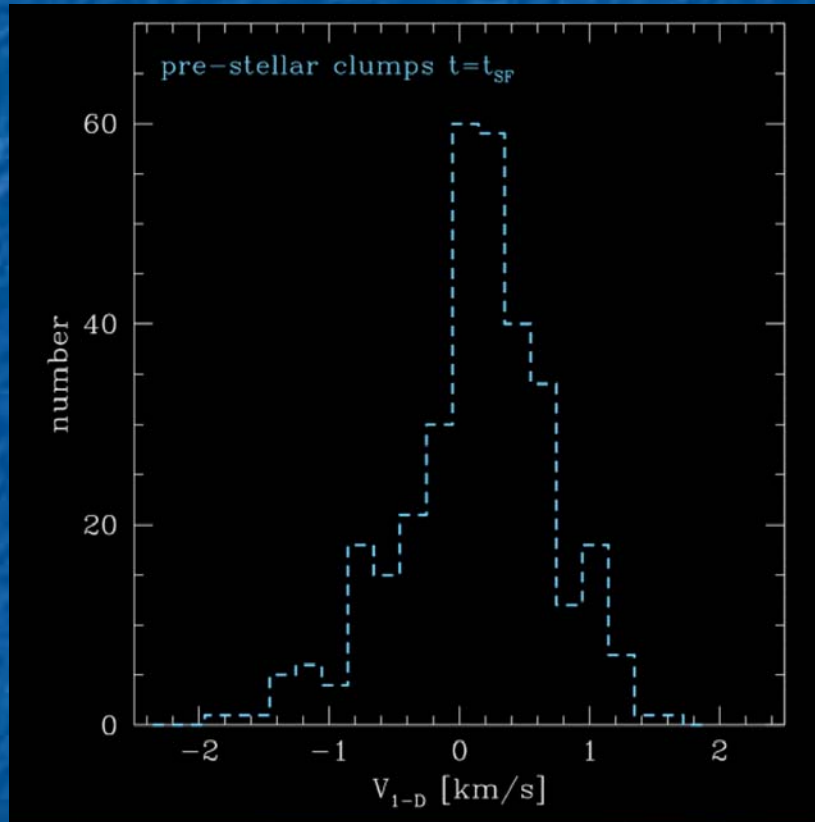
Evolution towards SF

Clark & Bonnell 2005

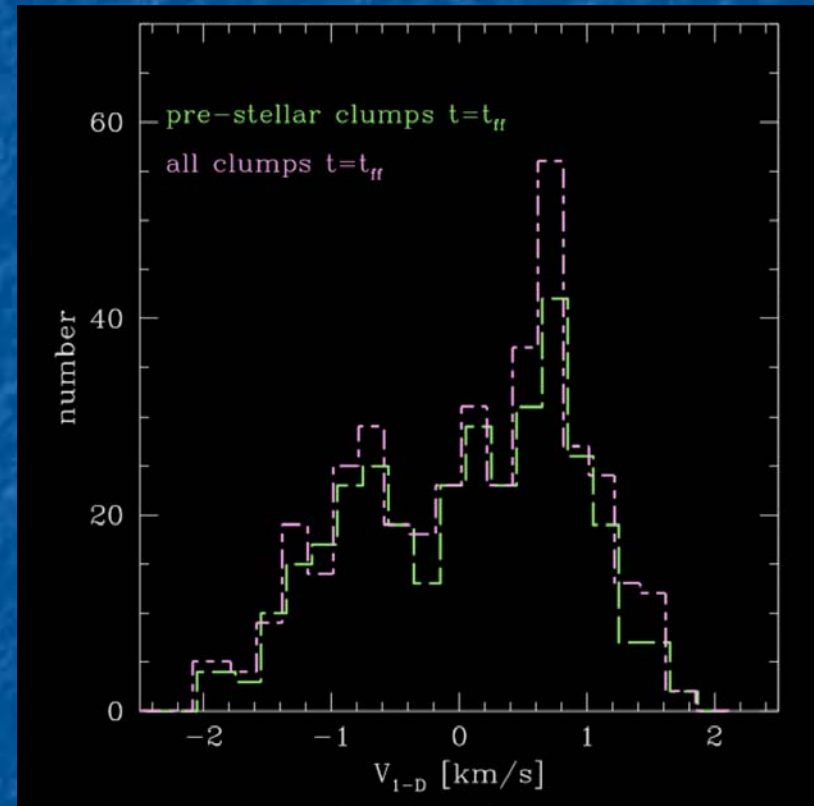


# Clump velocities

P. Clark



- At point of first SF
- Low clump-clump vels



- After free-fall time
- ~ higher clump-clump vels



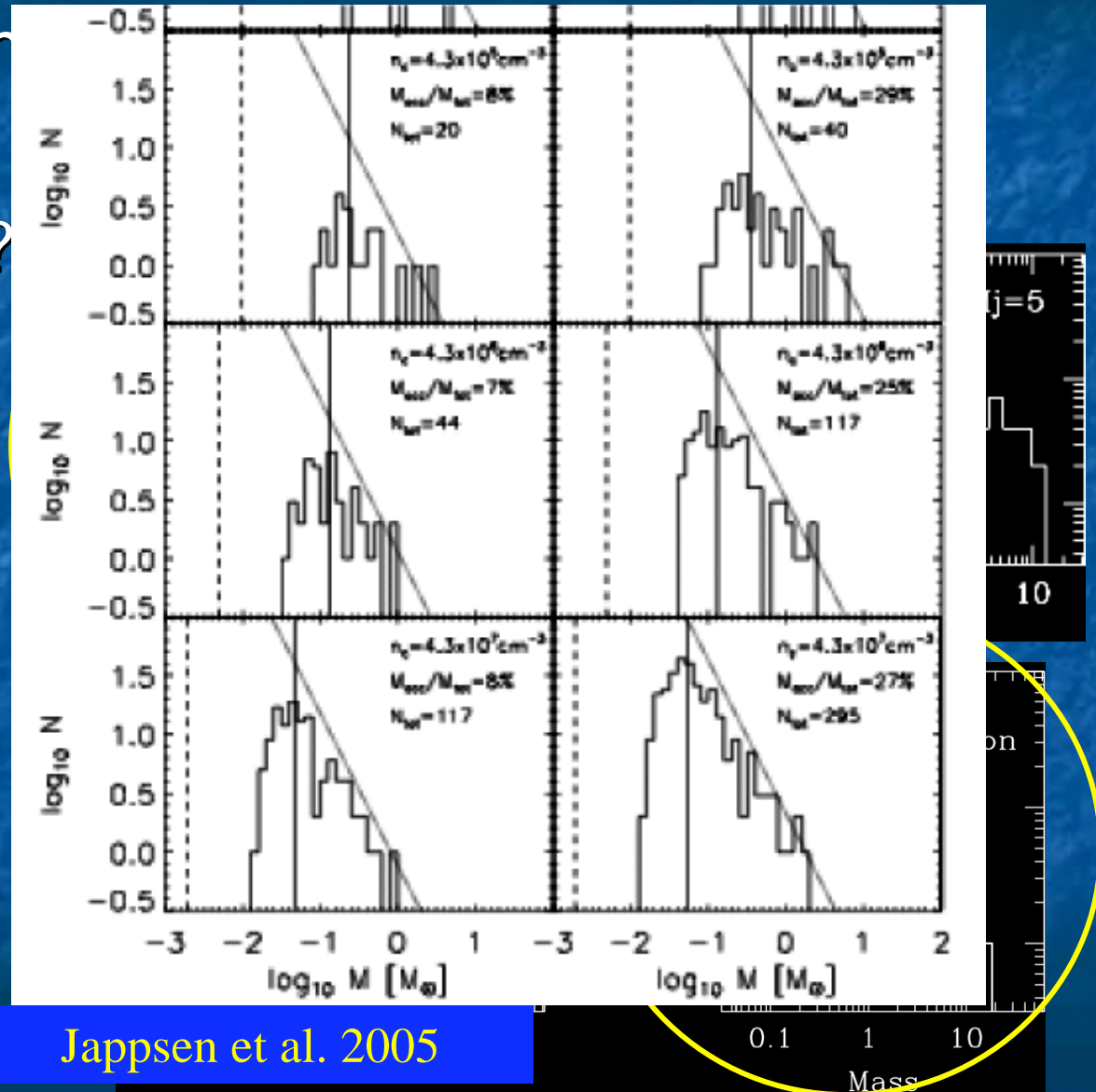
# Characteristic stellar mass

- Simulations show that the characteristic stellar mass is not constant
- What sets  $M_J$ ?

Thermal physics:



(Larson 2005, Spaans & Silk 2000)



Jappsen et al. 2005

Bonnell, Clarke & Bate 2006

# Competitive accretion

Bonnell et al 1997, 2001

- Fragmentation down to (thermal) Jeans Mass
  - Form as lower mass stars ( $\sim 0.5 M_{\text{sun}}$ )
  - Subsequent accretion forms high-mass stars

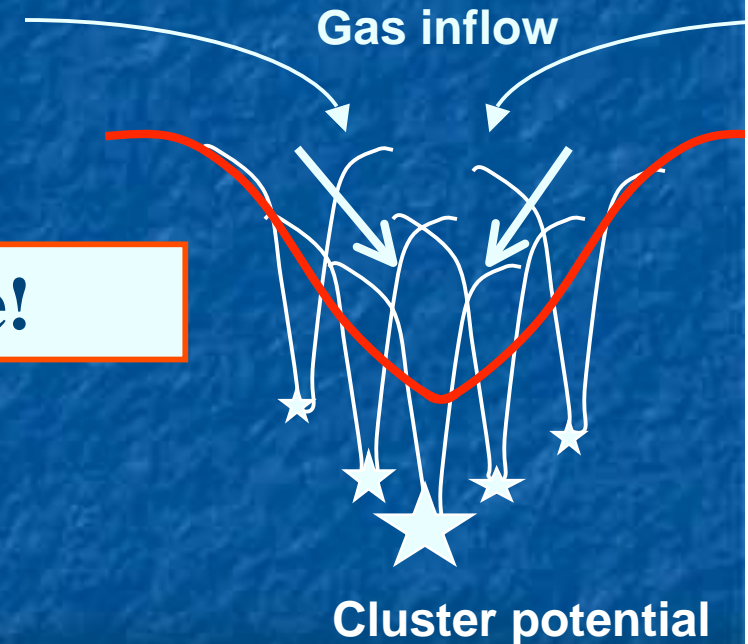
- Accretion limited by
  - Tidal effects
  - Gas velocities: Bondi-Hoyle

**Stars do not have to move!**

- Gas inflow due to cluster potential

- to cluster centre
- Higher gas density:
  - Higher accretion rates

- Requirements:
  - $N > 2$  fragments
- Common gas reservoir

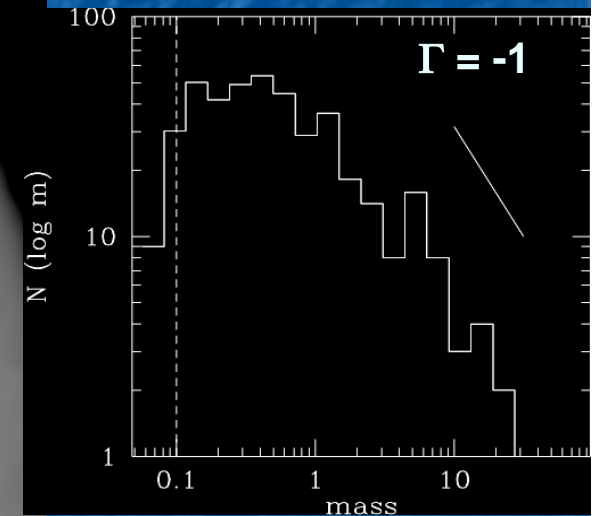




# The Formation of a stellar cluster

$10^3 M_{\text{sun}}$  in 1 pc

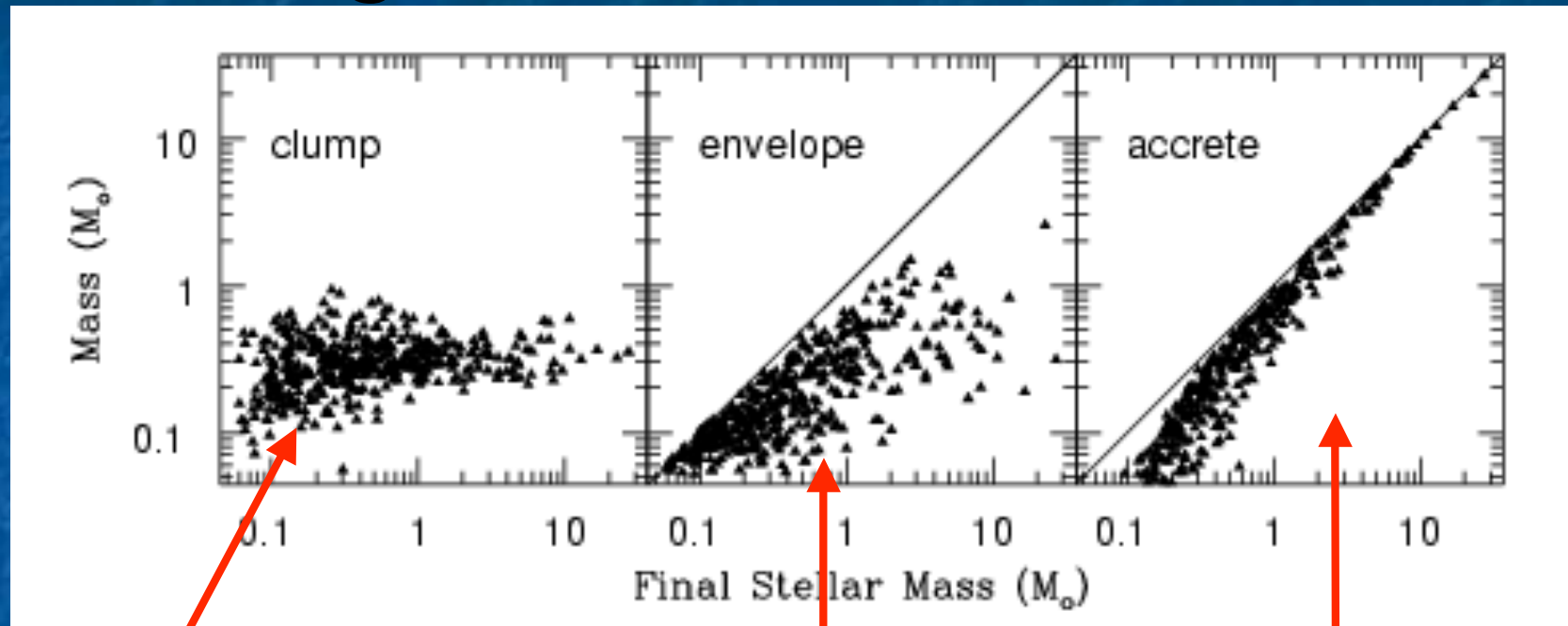
Stellar masses



Forms full IMF

Mass segregated  
clusters

# Origin of stellar masses



Fragmentation mass  
~ Jeans Mass

• Envelope mass

• Accretion from  
outside stellar cluster

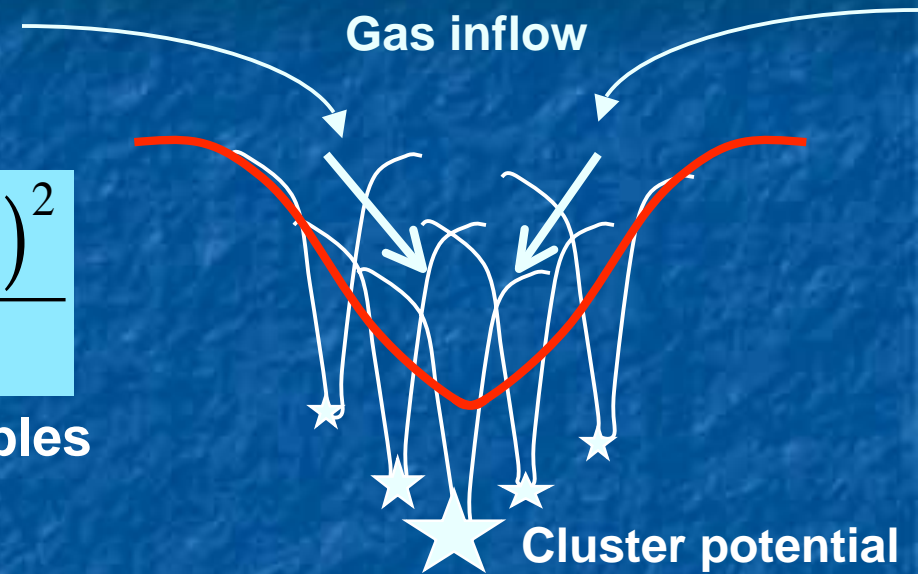
**• Massive stars form due to accretion  
from large-scale reservoir**

# Competitive accretion

- Accretion rates

$$\dot{M}_{acc} = \pi \rho v R_{acc}^2 \approx \pi \rho \frac{(GM_*)^2}{v^3}$$

All local variables



	Global Cloud
$\rho$	$2 \cdot 10^{-19} \text{ g/cm}^3$
$v$	2 km/s
$M_*$	$0.1 M_{\text{sun}}$
$\dot{M}_{acc}$	$10^{-9} M_{\text{sun}}/\text{yr}$



Competitive accretion  
doesn't work ?

Krumholz et al 2005

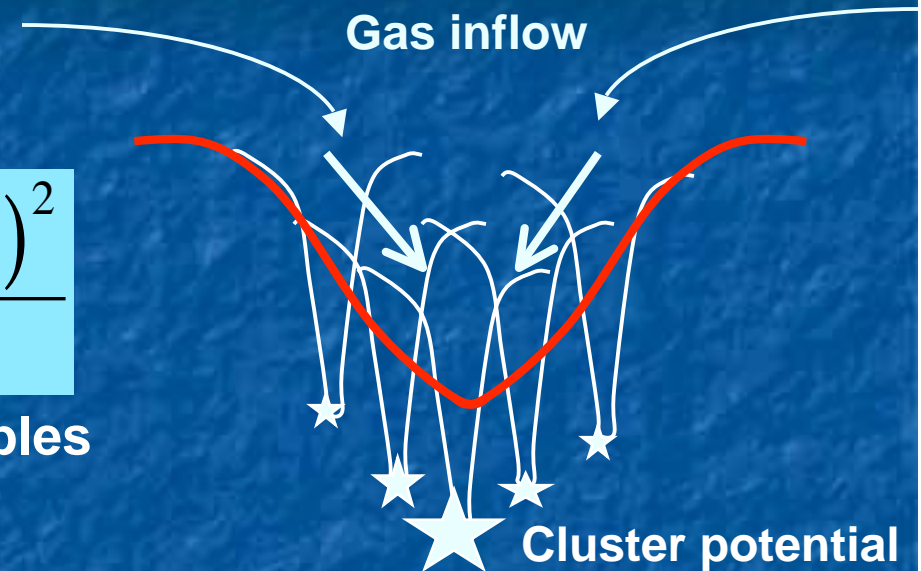


# Competitive accretion

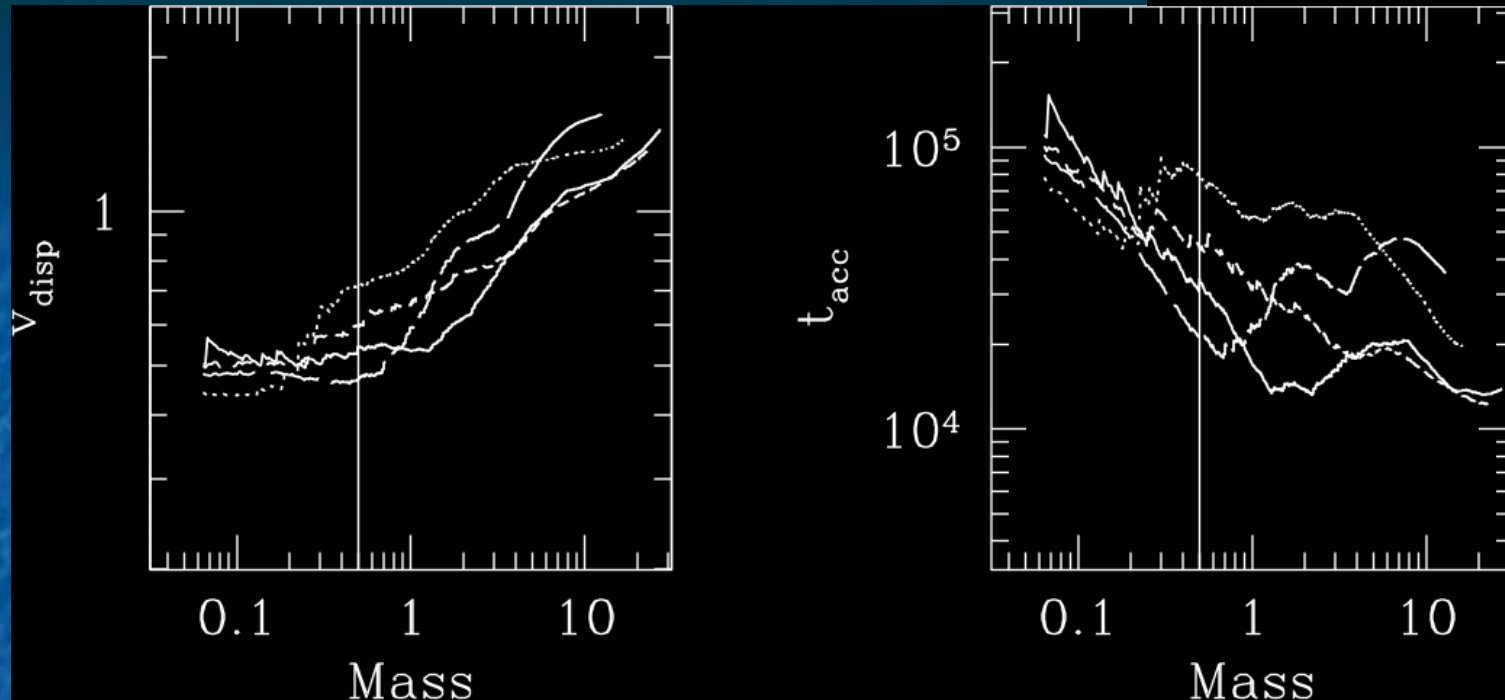
- Accretion rates

$$\dot{M}_{acc} = \pi \rho v R_{acc}^2 \approx \pi \rho \frac{(GM_*)^2}{v^3}$$

All local variables



	Global Cloud	Local Cluster Core	
$\rho$	$2 \cdot 10^{-19} \text{ g/cm}^3$	$10^{-17} \text{ g/cm}^3$	Large range in possible $\dot{M}_{acc}$
$v$	2 km/s	0.5 km/s	
$M_*$	$0.1 M_{sun}$	$0.5 M_{sun}$	
$\dot{M}_{acc}$	$10^{-9} M_{sun}/\text{yr}$	$10^{-4} M_{sun}/\text{yr}$	→ full IMF



- Accretion starts in small-N clusters
- Low velocity dispersion
  - Short accretion timescale
- Attain ~higher masses before  $v_{disp}$  high
- Form massive stars in few  $10^5$  years

$$t_{acc} = \frac{M_*}{\dot{M}_{acc}}$$

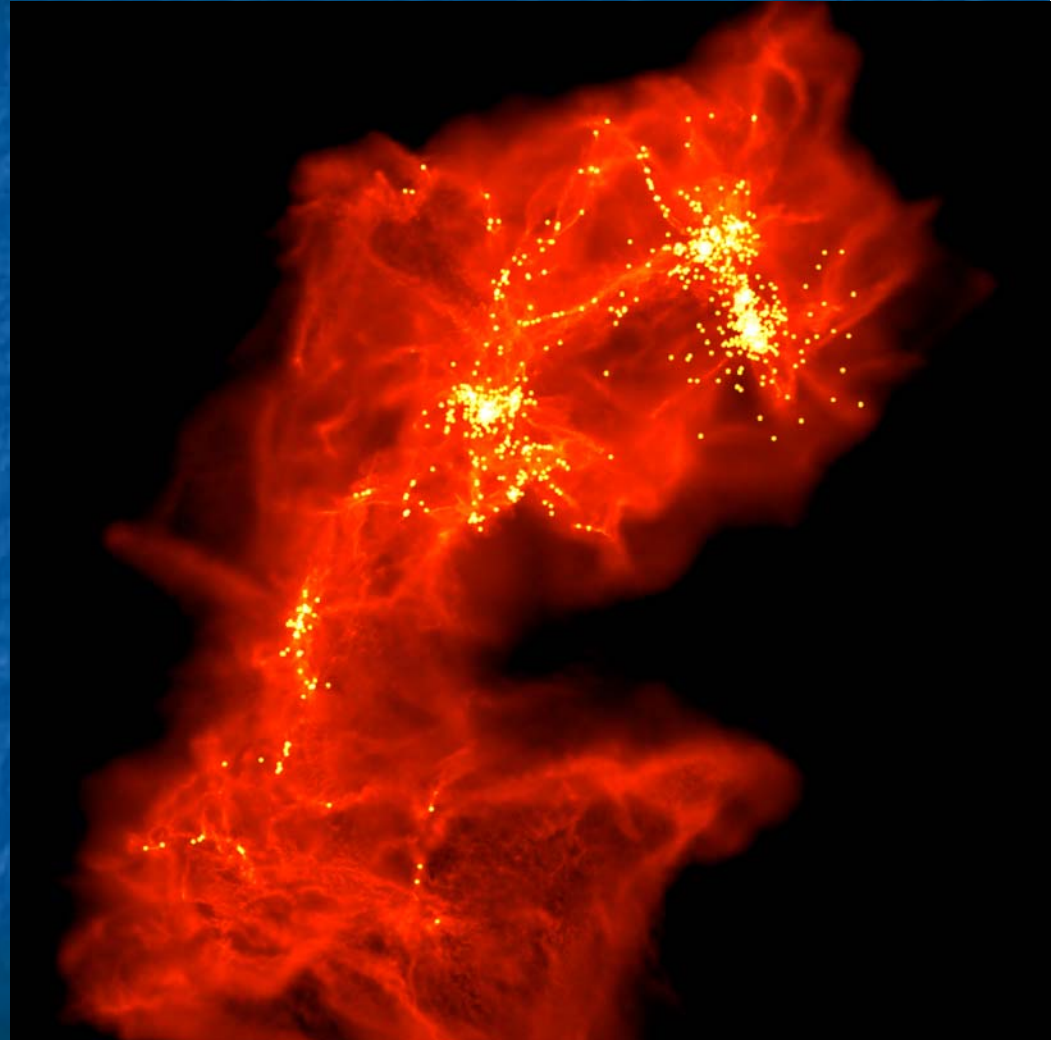
# GMC scale star formation

- $10^4 M_{\text{sun}}$  in 10 pc
- Forms  $> 2500$  stars
  - Over  $6 \times 10^5$  years
- Full IMF
- $1.5 \times 10^7$  SPH particles
  - On two levels

Mass resolution  $\sim 0.02 M_{\text{sun}}$

- Sink radii 200 AU

Bound (top) and unbound  
(bottom) initial conditions





# Full GMC

Bound (top) and  
unbound (bottom)  
initial conditions

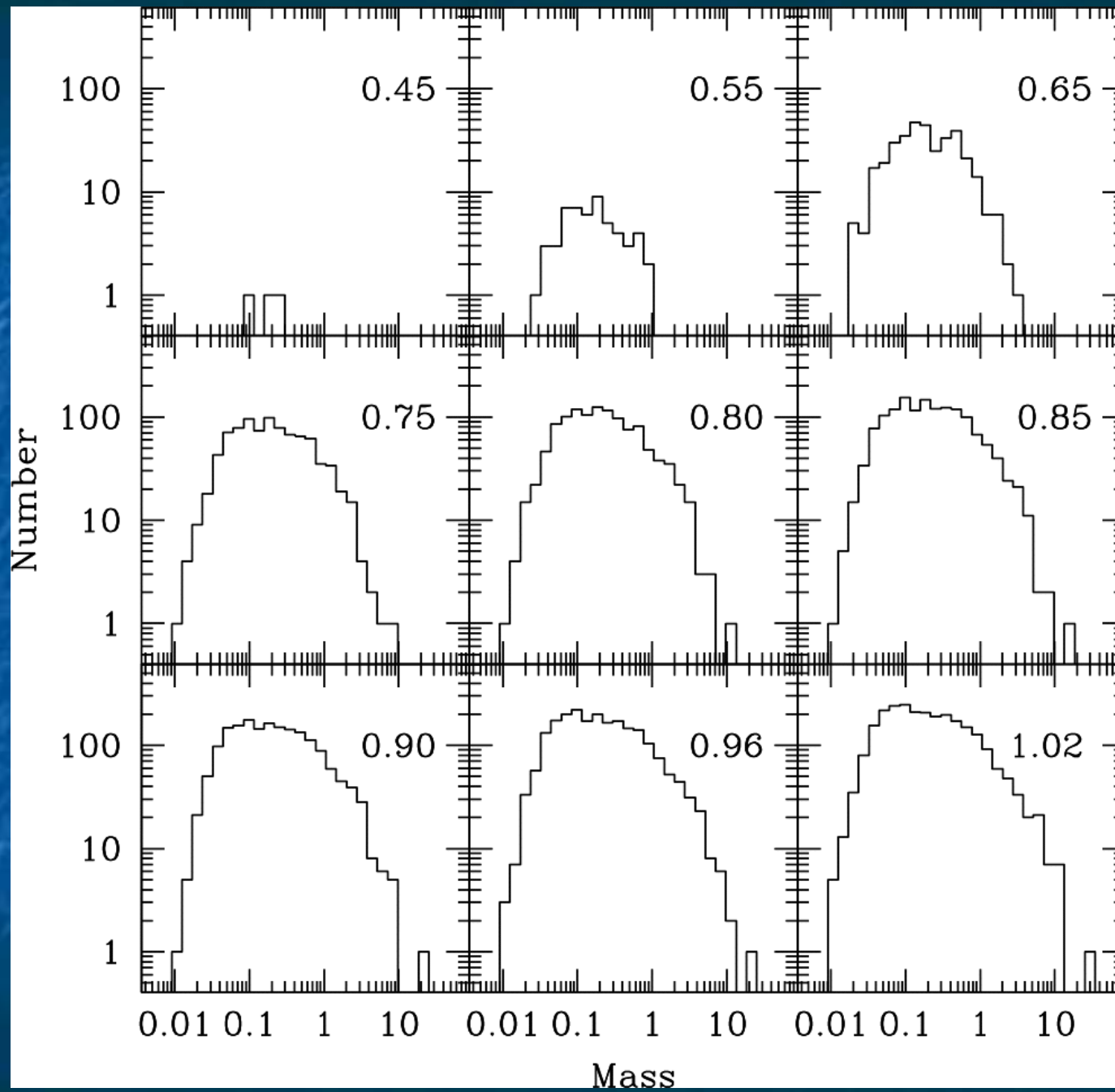
$10^4 M_{\text{sun}}$  in 10 pc

Clustered and  
distributed SF

Efficiency varies  
from  $< 1\%$  to  $20\%$

Universal IMF





# Fragmentation environment

Gas density

in 0.1 pc

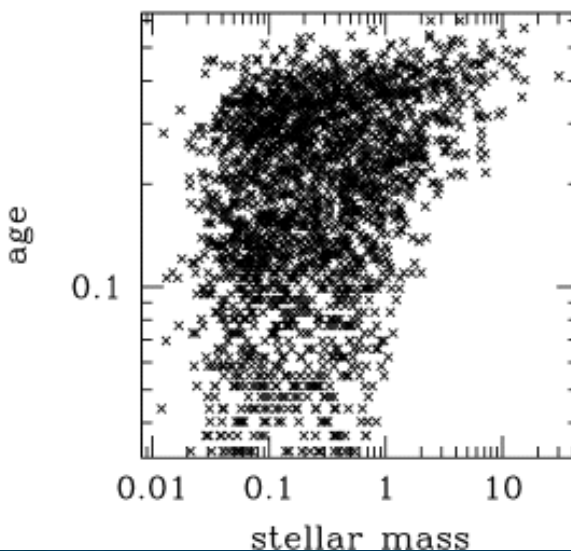
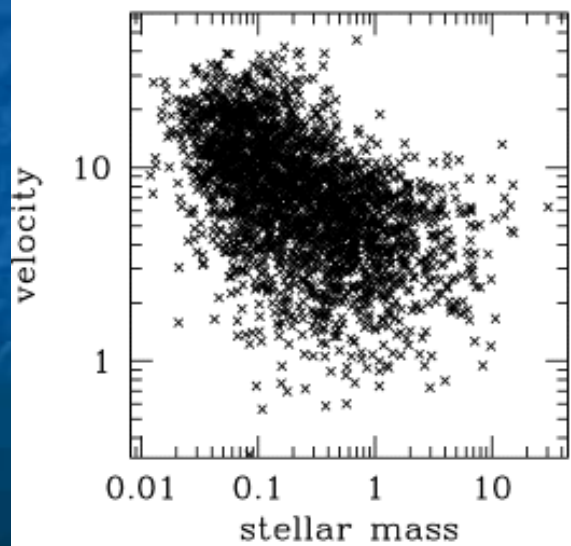
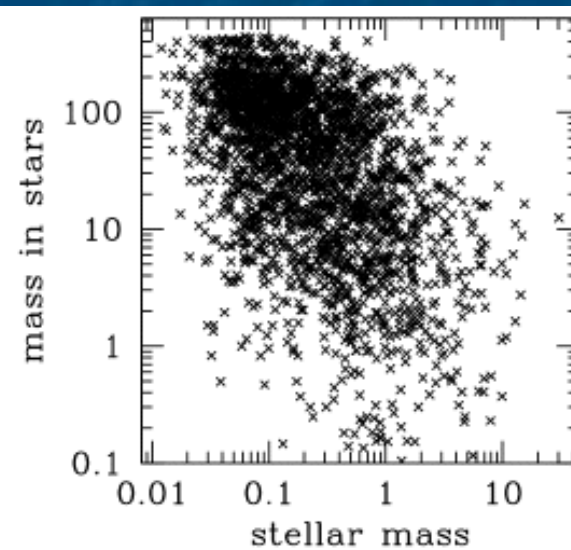
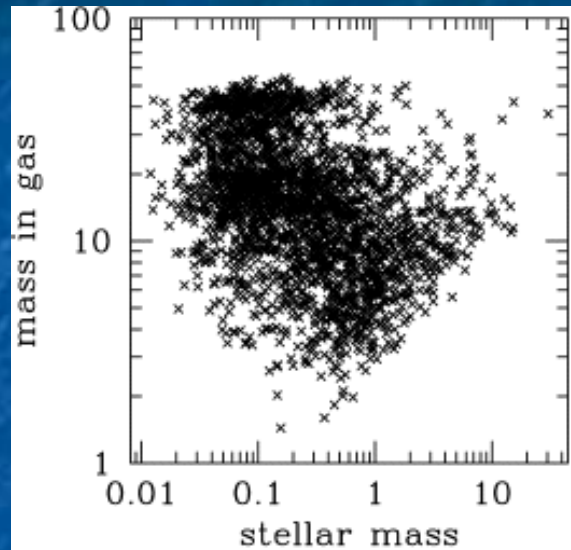
$$M_J \sim \rho^{-1/2}$$

Velocity

in (0.2 km/s)

relative to  
CoM

in 0.5 pc



Clusters

Stars in 0.5pc  
at point of  
fragmentation

When  
fragment  
formed

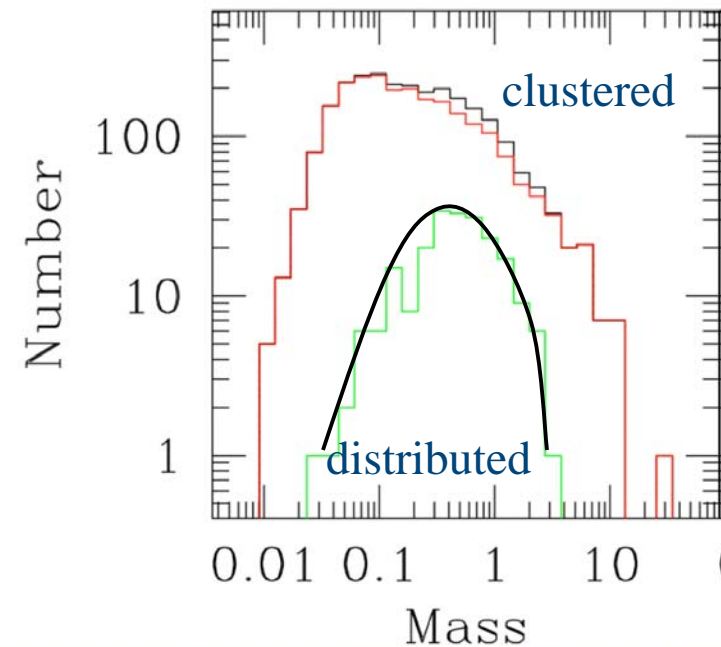
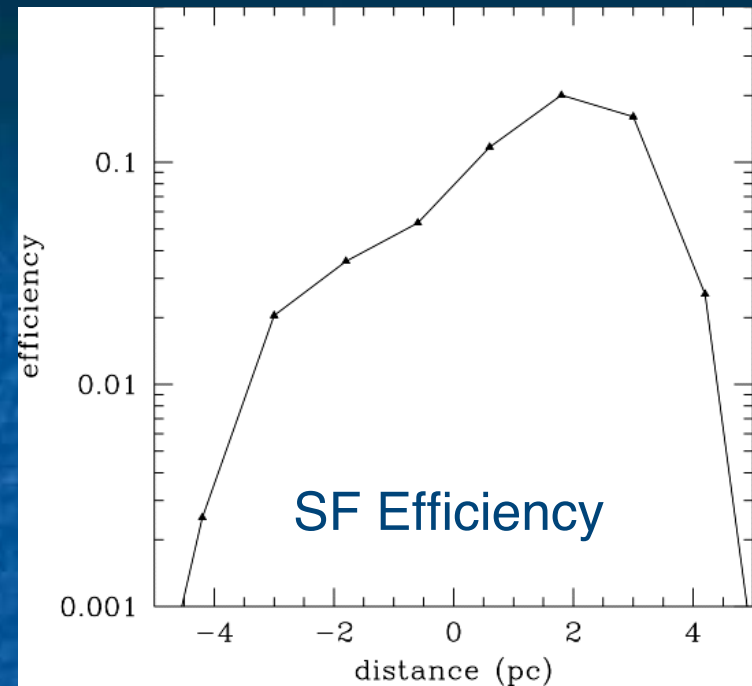


# Origin of stellar masses

- Massive stars
  - Form early at  $\sim M_J$ , sit in centre of cluster
  - High accretion rates
- Low-mass stars
  - Form later as gas falling into cluster potential
  - High relative velocity
  - Little subsequent accretion

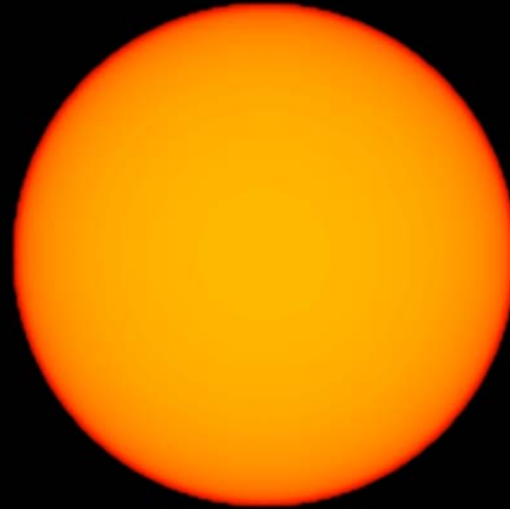
# SF efficiencies and clustered SF

- **Bound** conditions produce stellar clusters
  - Relatively high efficiencies
  - 20-50 %
  - Full IMF
- **Unbound** regions produce distributed SF
  - Low SF efficiencies
  - Few %
  - Flat/Peaked IMF
  - No high-mass, few low mass stars



# An unbound example...

KE = 2 × PE  
(initially)  
Isothermal  
EOS



Clark, Bonnell & Klessen (2007)

0.25pc

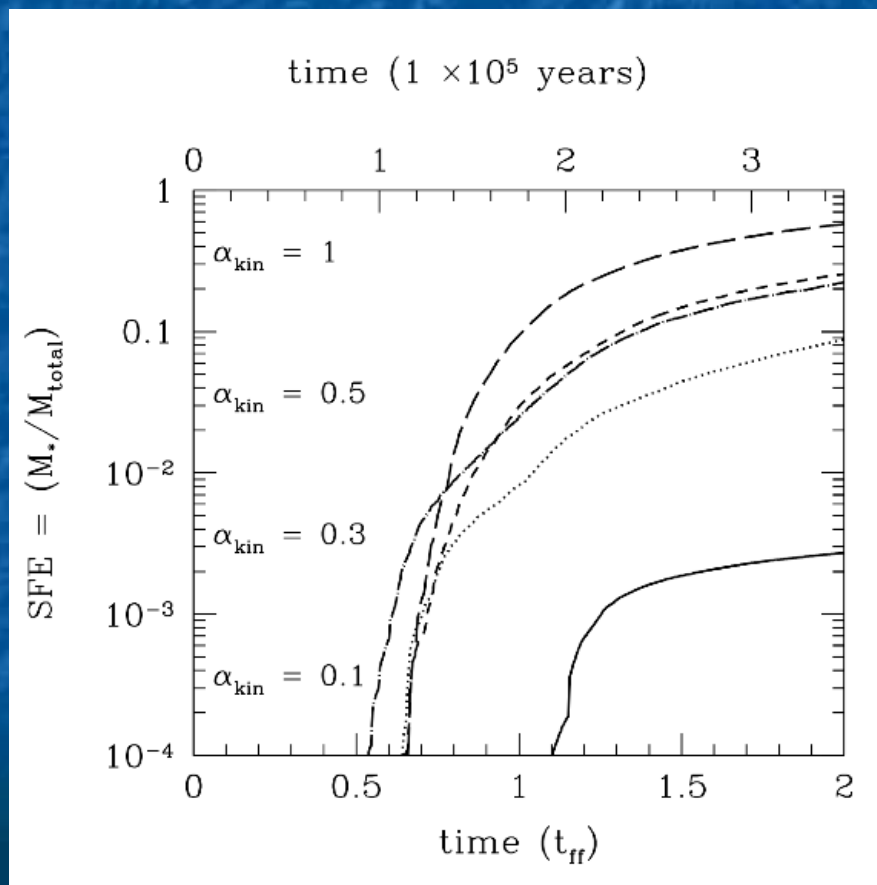


# Star formation efficiencies?

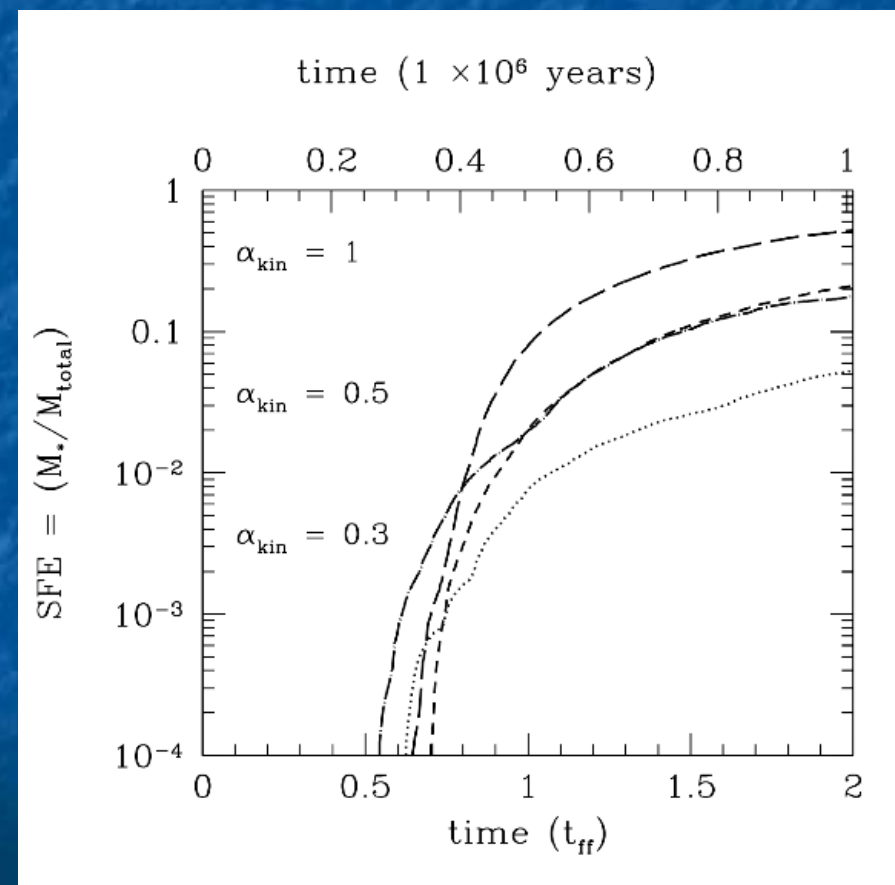
Naturally, more unbound clouds/regions have lower efficiencies...

$$\alpha_{\text{kin}} = \text{IPEI/KE}$$

Clark et al 2007



Isothermal EOS

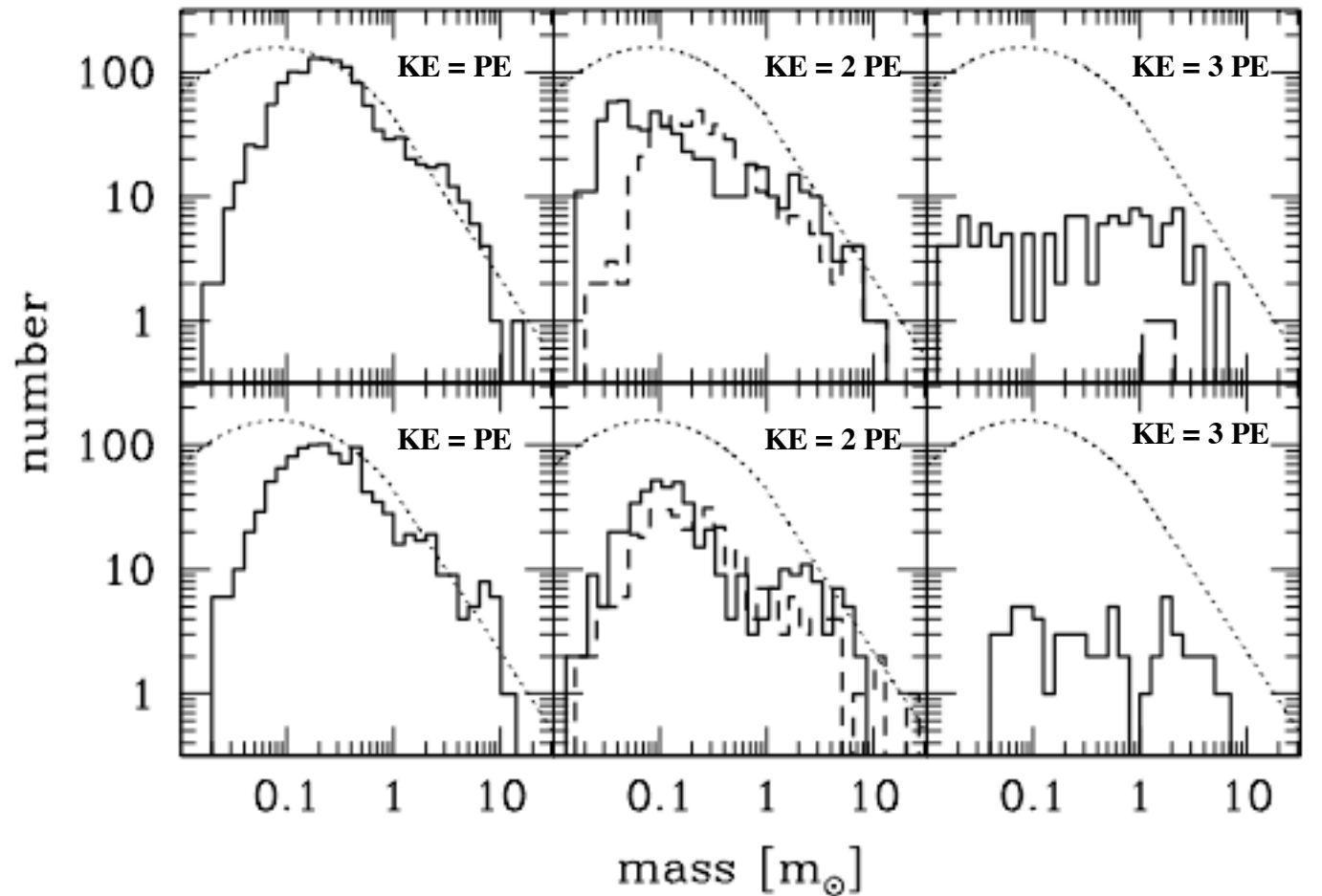


Barotropic EOS

# IMFs of unbound clouds

Isothermal EOS

Barotropic  
(Larson Style)  
EOS



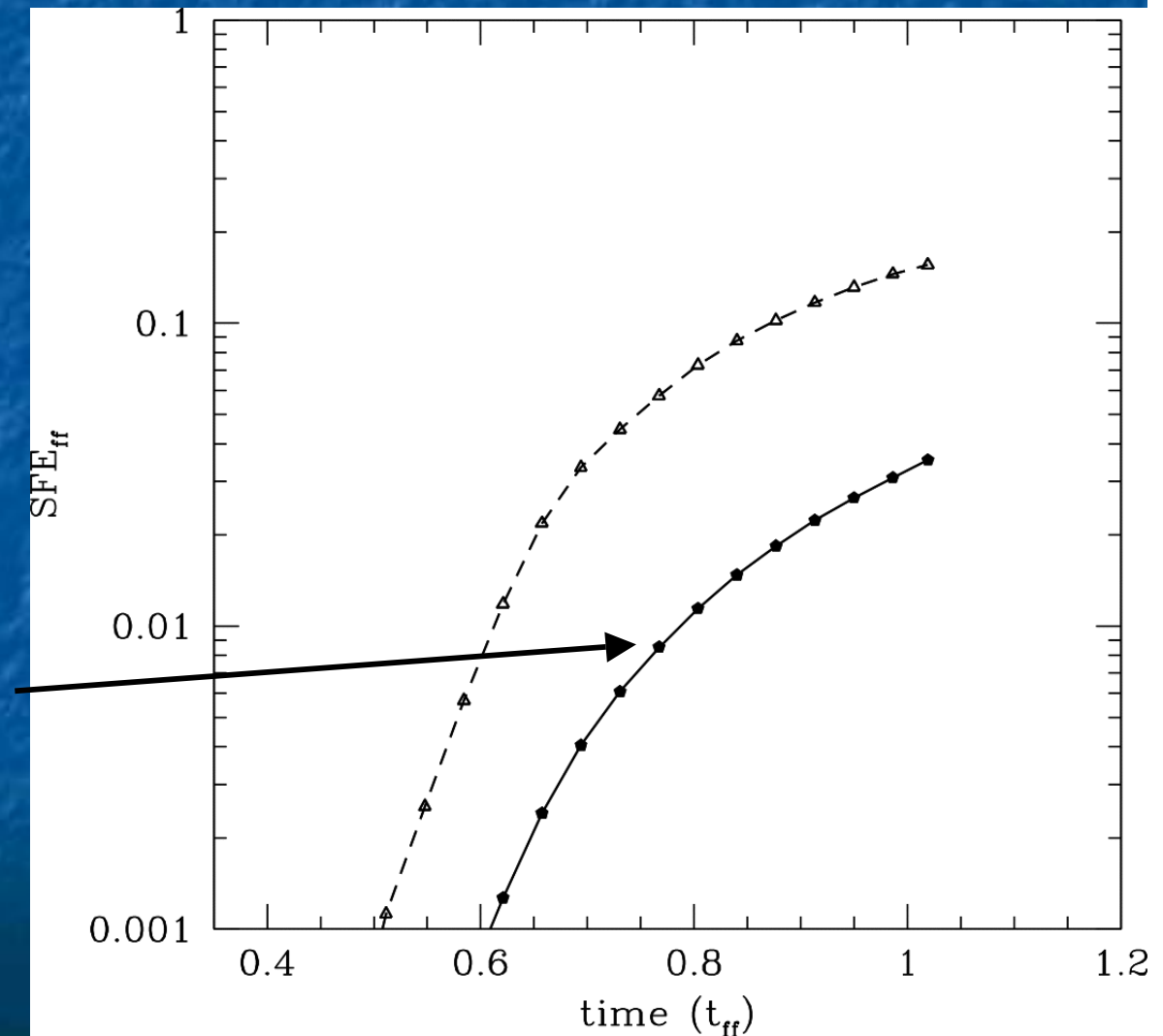
As clouds become  
more unbound



Competitive accretion is unable to  
create the 'correct' IMF

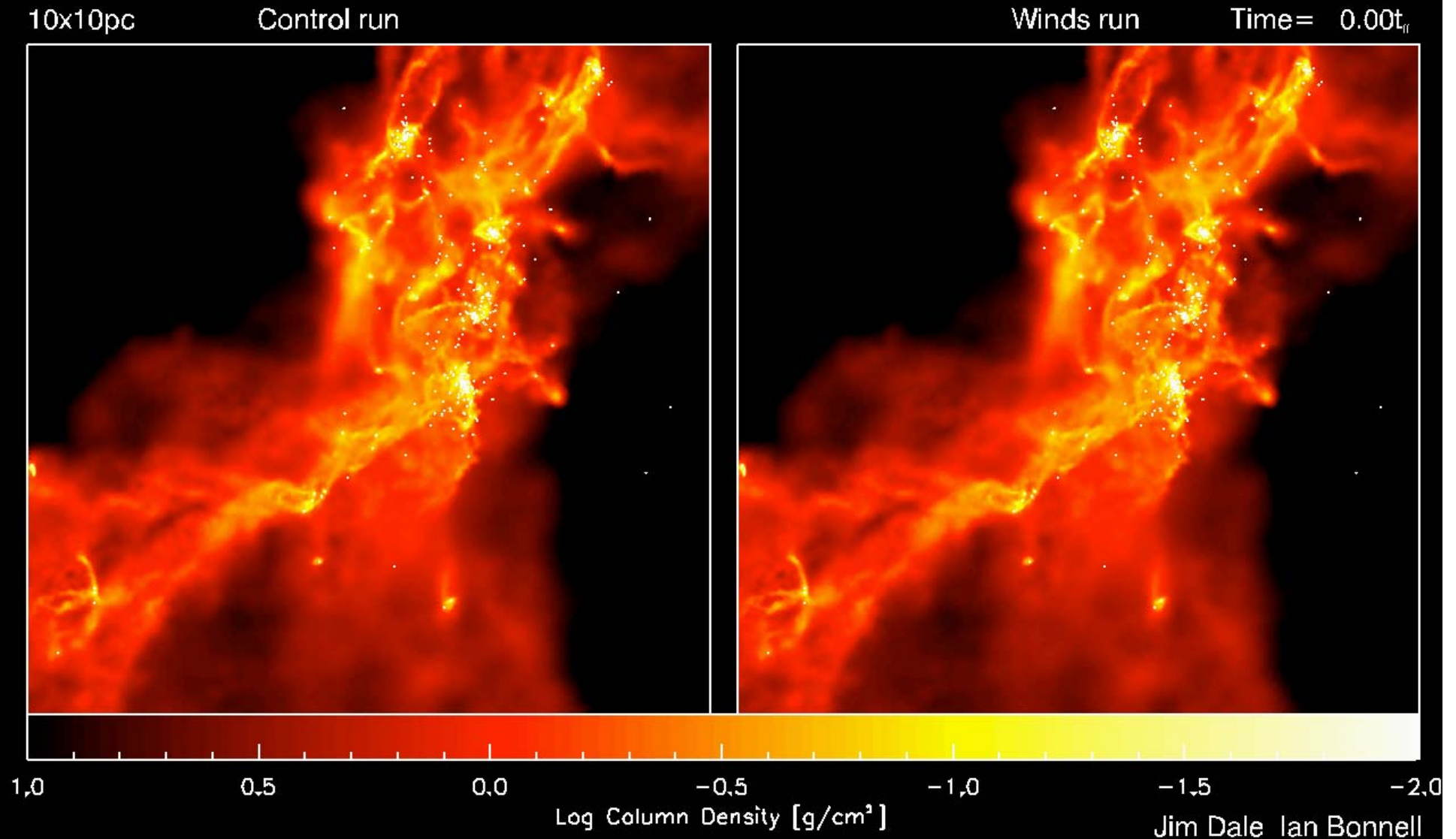
# Star formation efficiency per $t_{ff}$

- GMC simulation
- Final SFE  $\sim 15\%$
- BUT
- Equal probability of observing at all stages of evolution
- Average value of SFE is then much lower
- $\sim 3\% \text{ SFE}/t_{ff}$
- Even for short cloud lifetimes

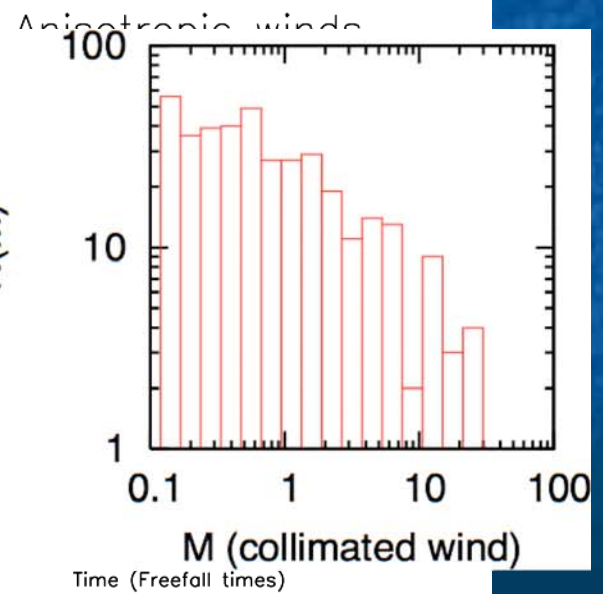
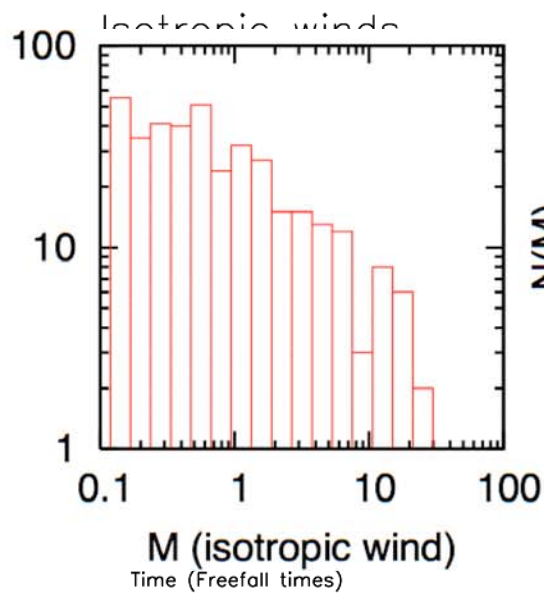
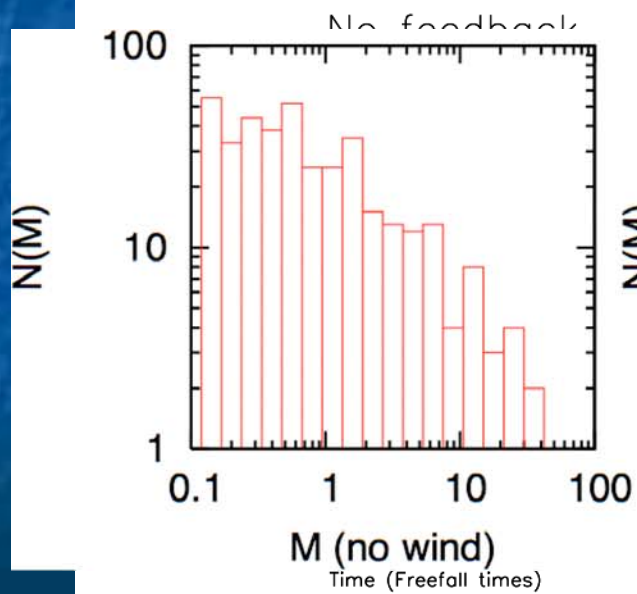
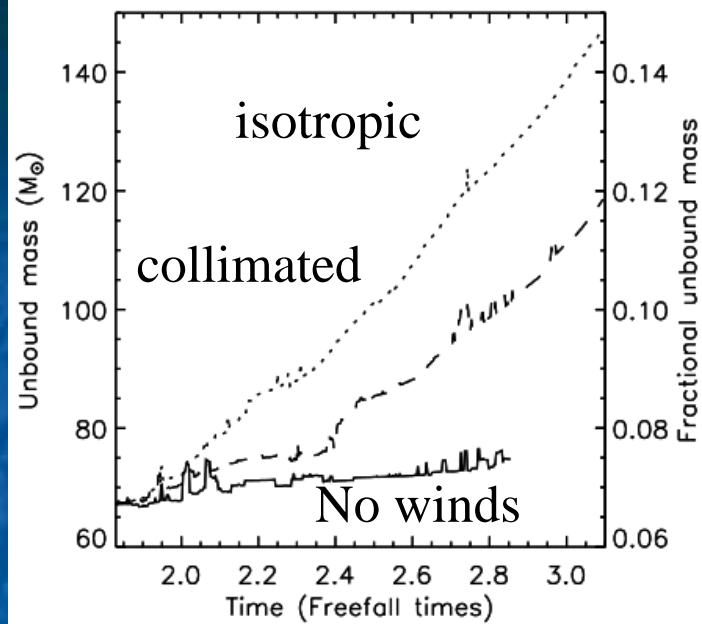
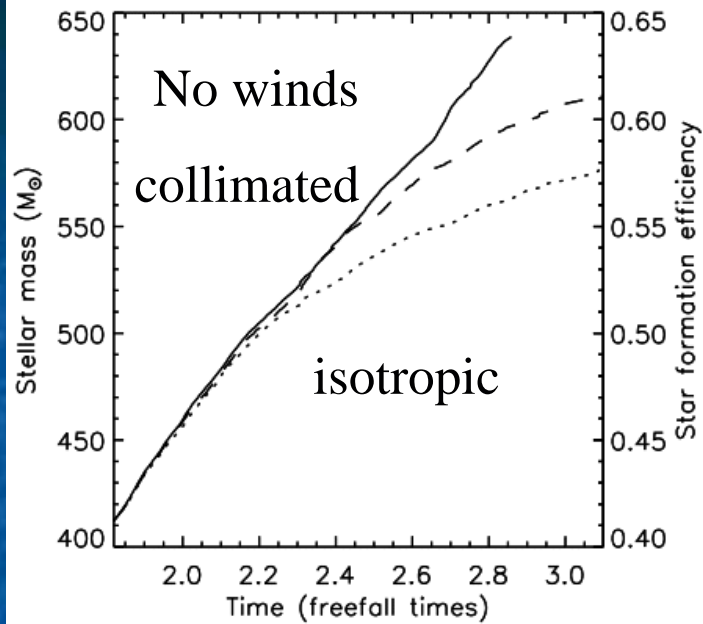




# Feedback from stellar winds



Winds have moderate effect on accretion rates



# Conclusions

- Gravity driven SF can explain IMF
  - Competitive accretion in cluster potential:
    - Higher mass stars due to high accretion rates in cluster centres
    - Low mass stars/BDs from infalling gas into cluster
  - Unbound clouds produce low SFEs
    - Distributed SF
    - Abnormal IMFs
  - Most stars must form in bound groups
  - Need to include all feedback processes



