

# Observation of an oscillating magnetoresistance with gate voltage in carbon-nanotube based TMR devices

Spintronics

Kavli Institute for Theoretical Physics; UCSB, March 2006

## F - Carbon Nanotube - F

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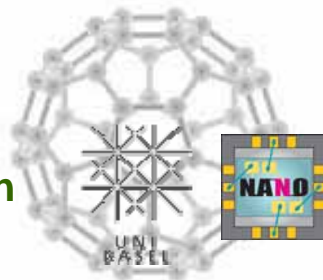
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Swiss National Science Foundation



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D. Loss (Basel)

J. Schliemann (Basel)

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**Reinhold Egger**

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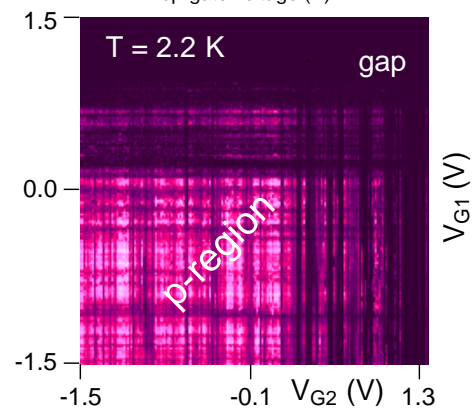
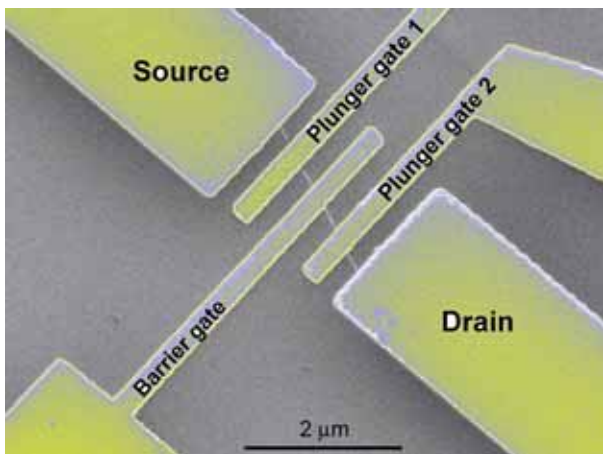
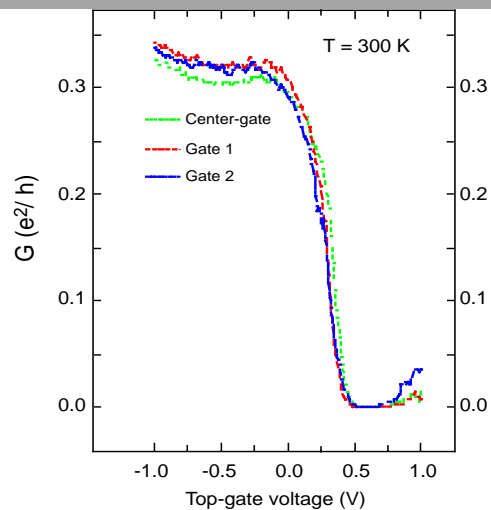
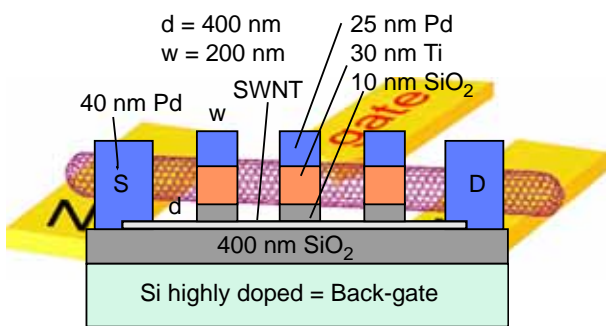
theoretische physik



# Carbon Nanotube Devices



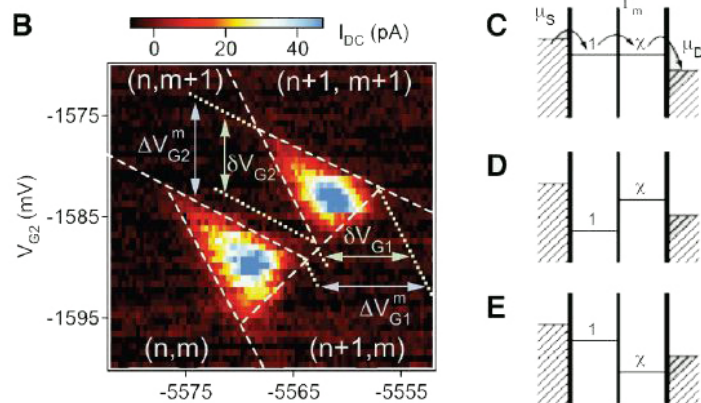
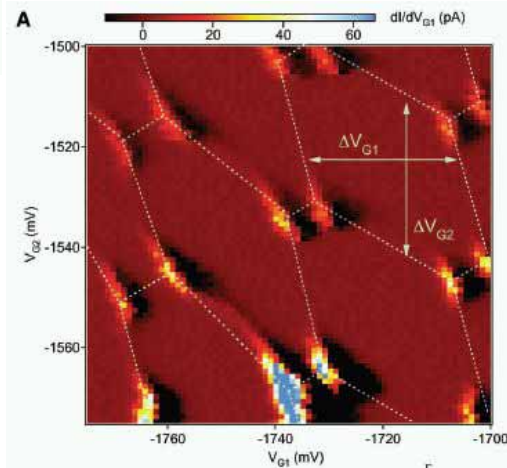
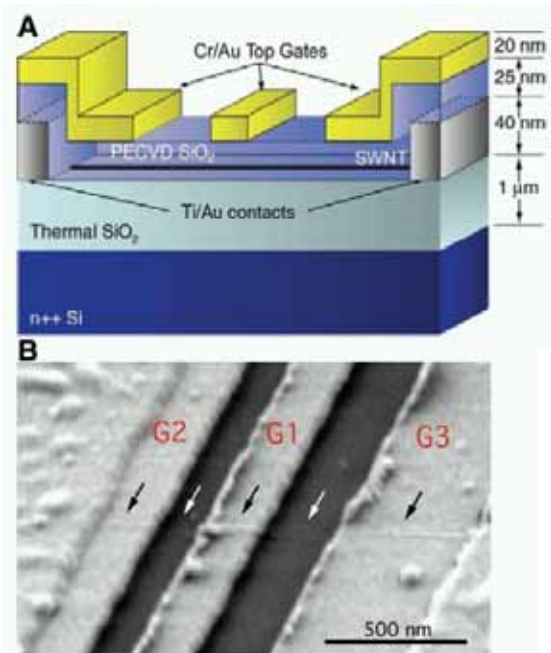
# Carbon Nanotube Devices



# Local Gate Control of a Carbon Nanotube Double Quantum Dot

N. Mason,\*† M. J. Biercuk,\* C. M. Marcus†

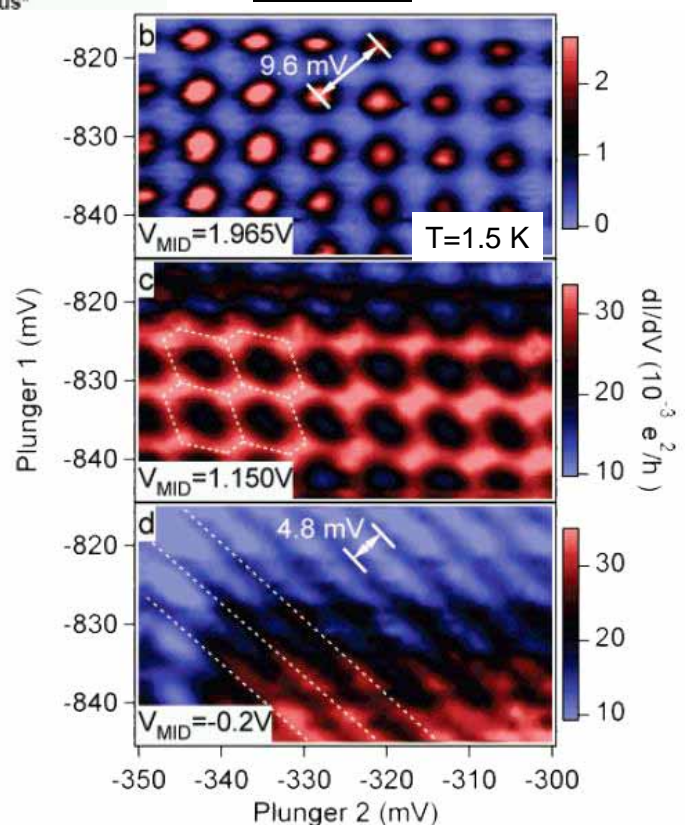
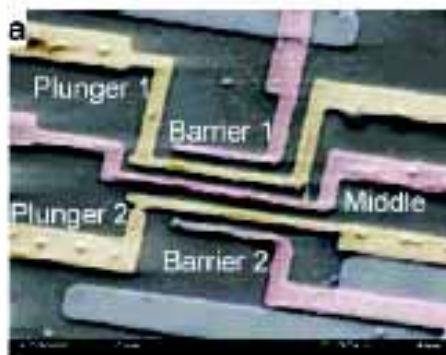
SCIENCE VOL 303 30 JANUARY 2004



# Gate-Defined Quantum Dots on Carbon Nanotubes

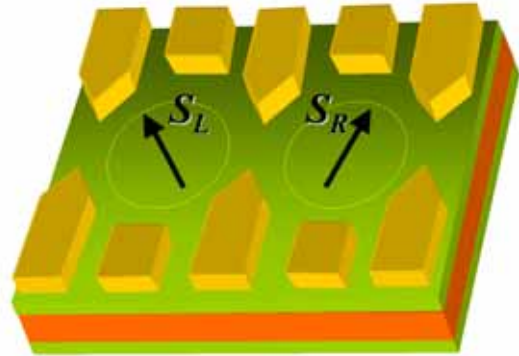
M. J. Biercuk, S. Garaj, N. Mason, J. M. Chow, and C. M. Marcus\*

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2005  
Vol. 5, No. 7  
1267-1271



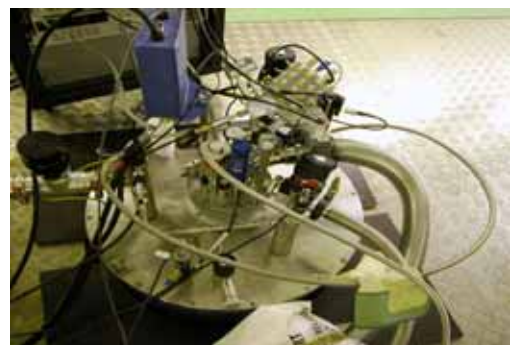
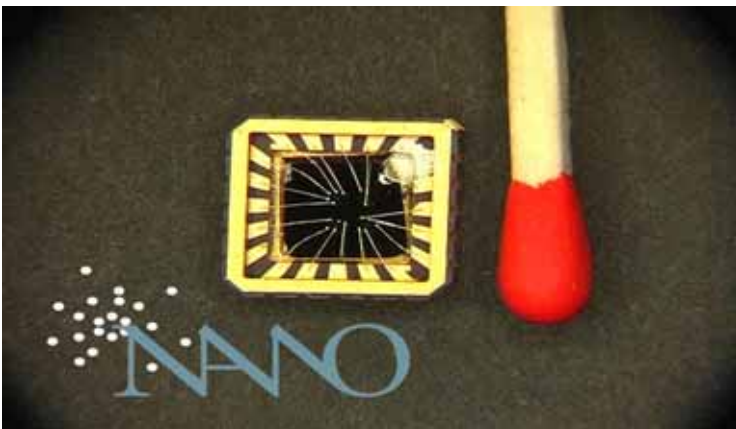
# Motivation

- Local gate control of electronic transport in nanotubes
- Probing and controlling quantum effects
- Spin in a quantum dot as quantum bit?
- Long spin dephasing times in nanotubes?

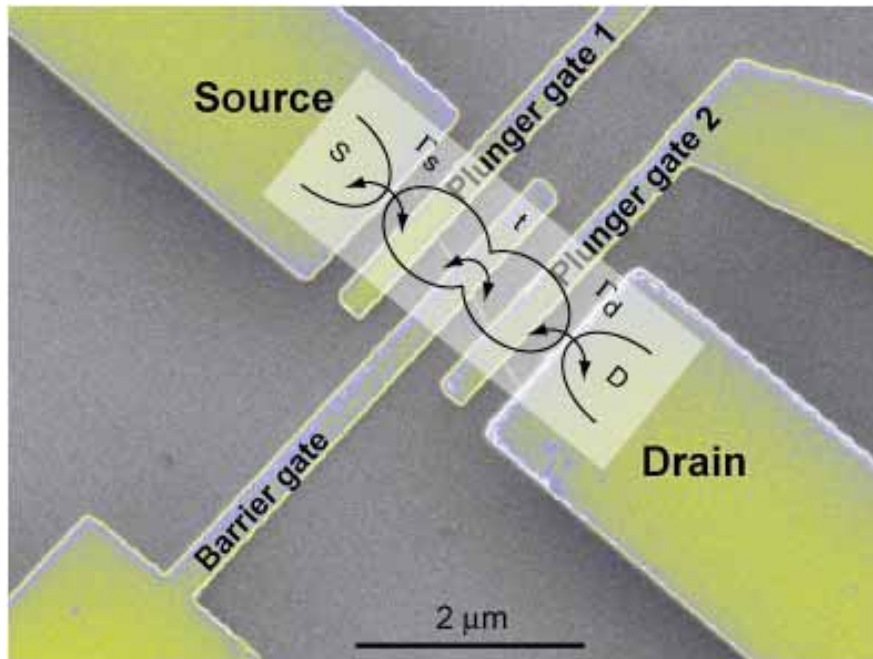


*D. Loss and D. P. DiVincenzo Phys. Rev. A 57, 120-126 (1998)*

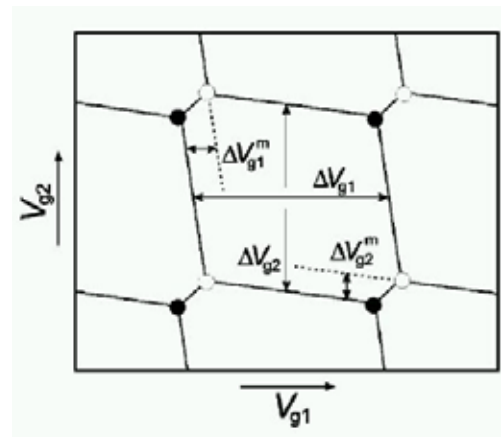
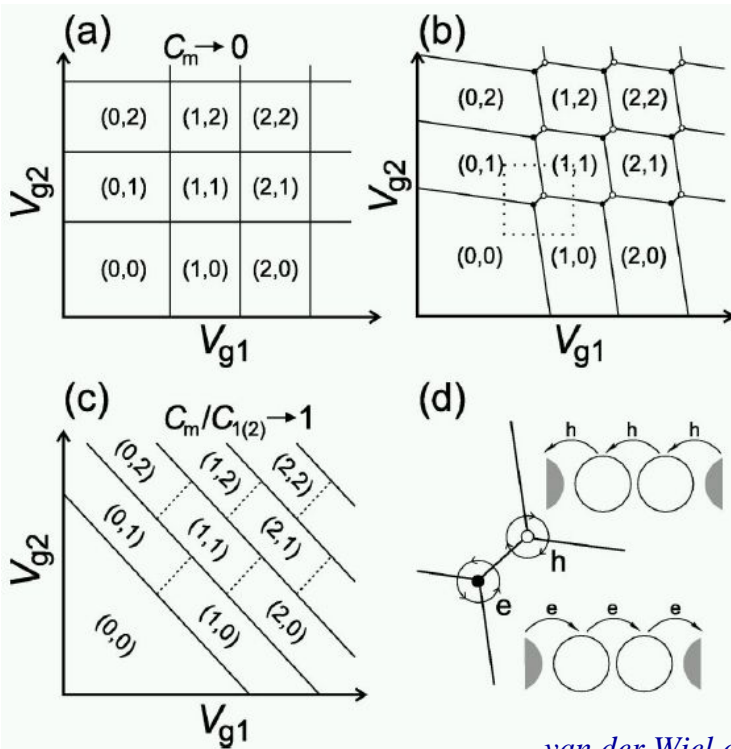
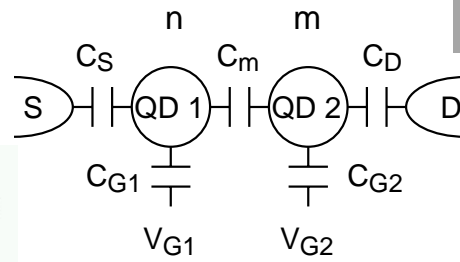
## Experimental



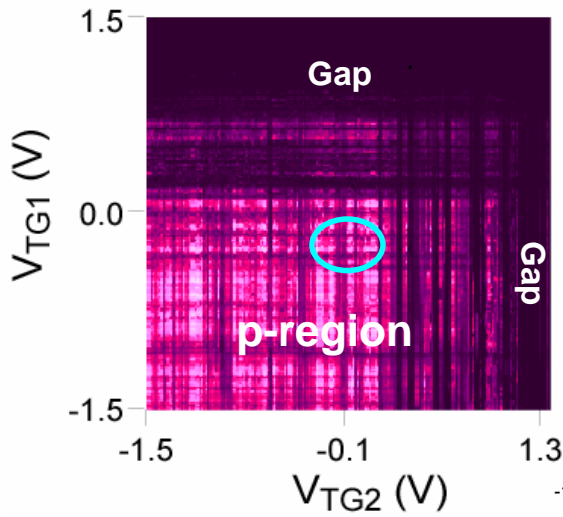
# Carbon Nanotube Double Dots



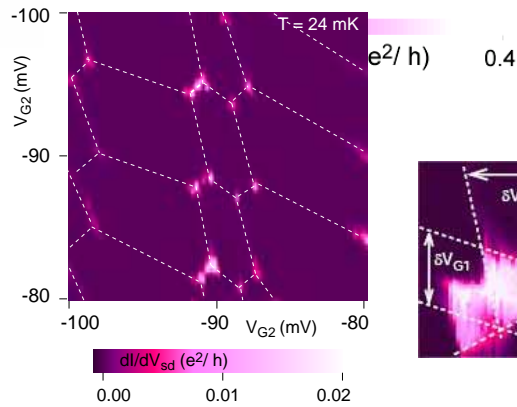
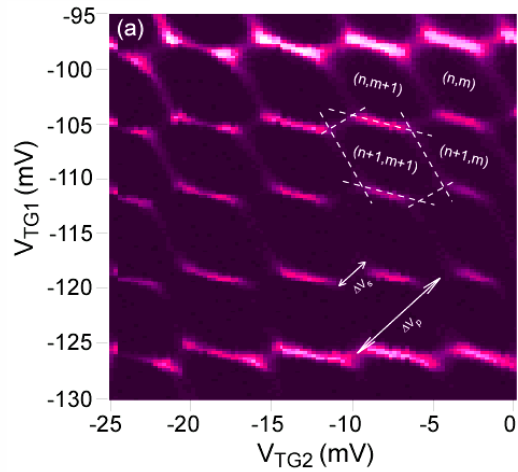
# Charge Stability Diagram



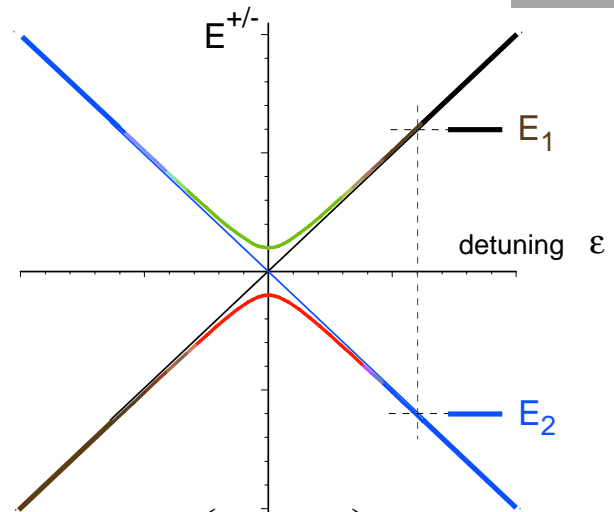
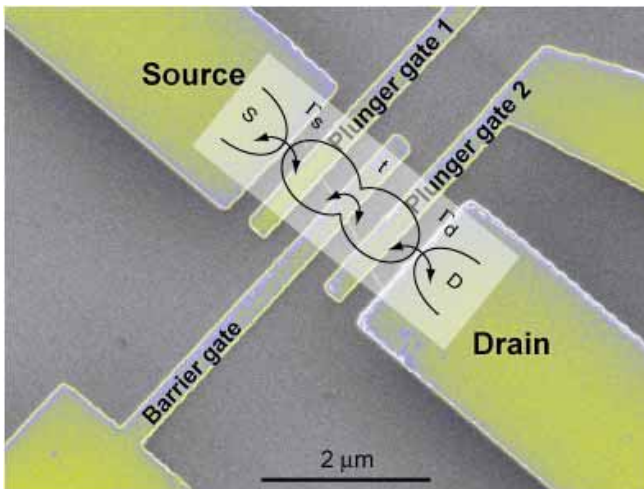
# Carbon Nanotube Double Dot



if two dots are weakly coupled



# molecular states (hybridization)



$$H\psi = \begin{pmatrix} E_1 & t \\ t^* & E_2 \end{pmatrix} \psi$$

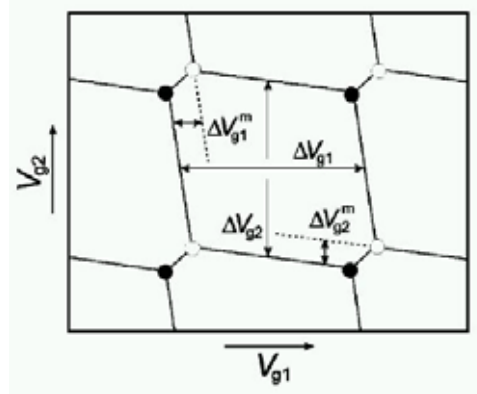
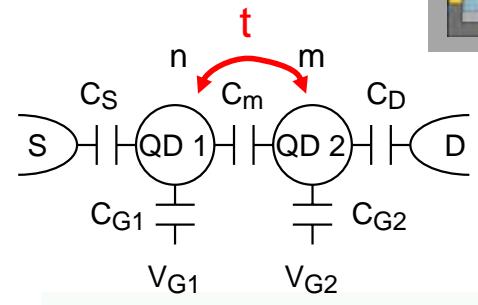
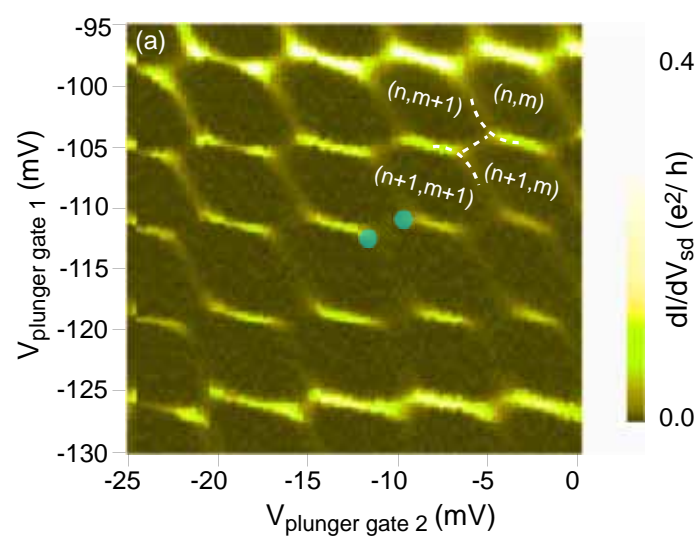
$$\Delta = \frac{E_1 + E_2}{2} \quad \varepsilon = \frac{E_1 - E_2}{2}$$

$$E^{\pm} = \Delta \mp \sqrt{\varepsilon^2 + |t|^2}$$

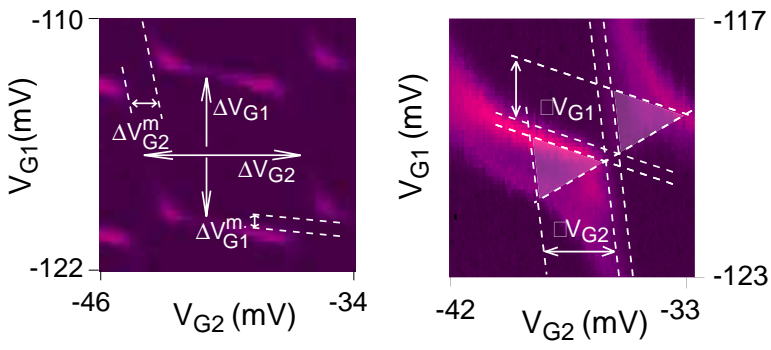
$$C_{100'000} \rightarrow (C_{100'000})_2$$



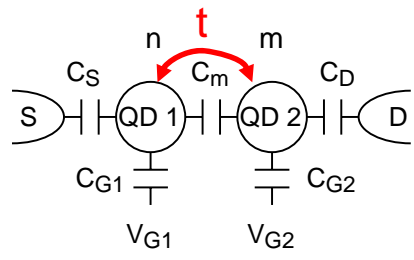
# characterization



$C_{g1,g2} \sim 20 \text{ aF}$   
 $C_{1=S}, C_{2=D} \sim 85, 145 \text{ aF}$   
 $C_m \sim 15 \text{ aF}$

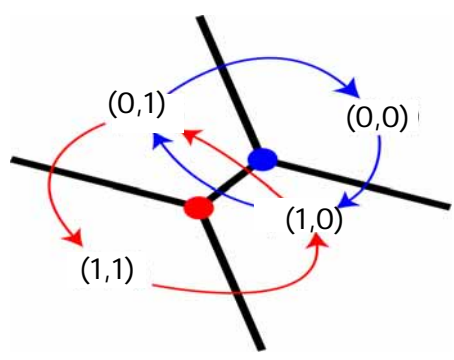


# add tunnel coupling

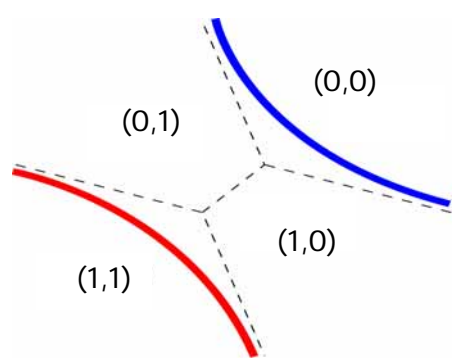


$$E^{+/-} = \Delta \mp \sqrt{\epsilon^2 + |t|^2}$$

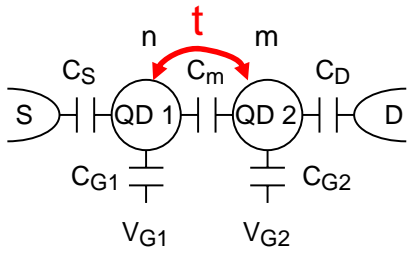
No tunnel-coupling



Tunnel-coupling



# add tunnel coupling

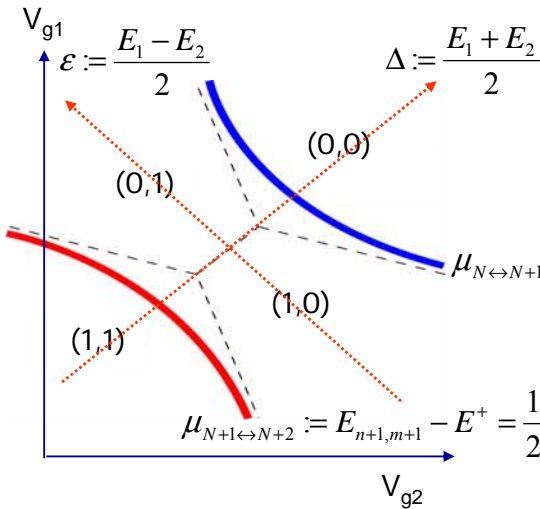


$$E^{+/-} = \Delta \mp \sqrt{\epsilon^2 + |t|^2}$$

$$E_{n+1,m} - E_{n,m} = Un + U'm + E_1(V_{g1})$$

$$E_{n,m+1} - E_{n,m} = Um + U'n + E_2(V_{g2})$$

$$\psi^\pm = \alpha|n+1,m\rangle \pm \beta|n,m+1\rangle$$

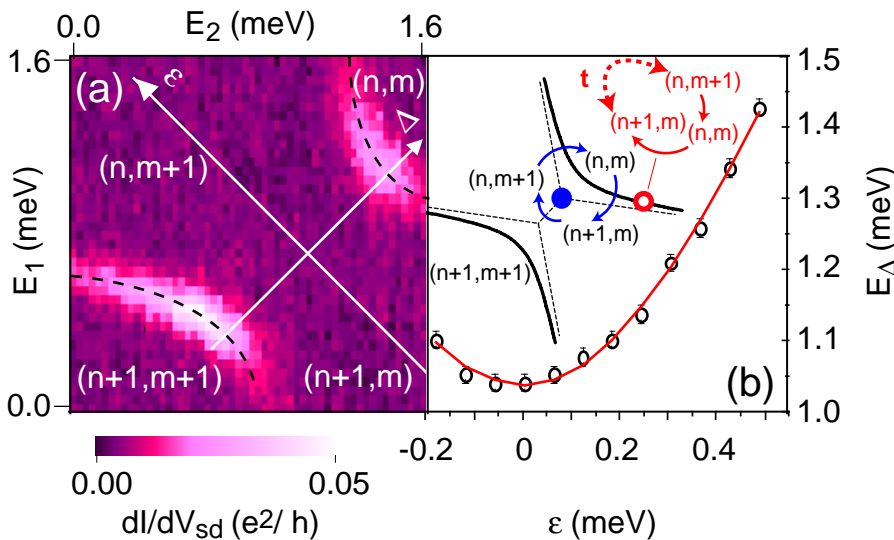


$$\mu_{N \leftrightarrow N+1} := E^+ - E_{n,m} = \frac{1}{2}(U + U')(n+m) + \Delta_{N \leftrightarrow N+1}(\epsilon) - \sqrt{\epsilon^2 + |t|^2}$$

$$\mu_{N+1 \leftrightarrow N+2} := E_{n+1,m+1} - E^+ = \frac{1}{2}(U + U')(n+m) + U' + \Delta_{N+1 \leftrightarrow N+2}(\epsilon) + \sqrt{\epsilon^2 + |t|^2}$$

$$\mu_{reservoirs} = \mu_{N \leftrightarrow N+1} = \mu_{N+1 \leftrightarrow N+2} \quad \longrightarrow \quad \Delta_r(\epsilon) - \Delta_l(\epsilon) = U' + 2\sqrt{\epsilon^2 + |t|^2}$$

# level anti-crossing



$$E^{+/-} = \Delta \mp \sqrt{\epsilon^2 + |t|^2}$$

$$E_\Delta := |\Delta_l - \Delta_r| = U' + 2\sqrt{\epsilon^2 + |t|^2}$$

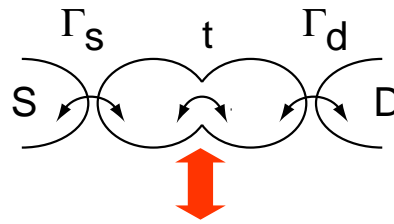
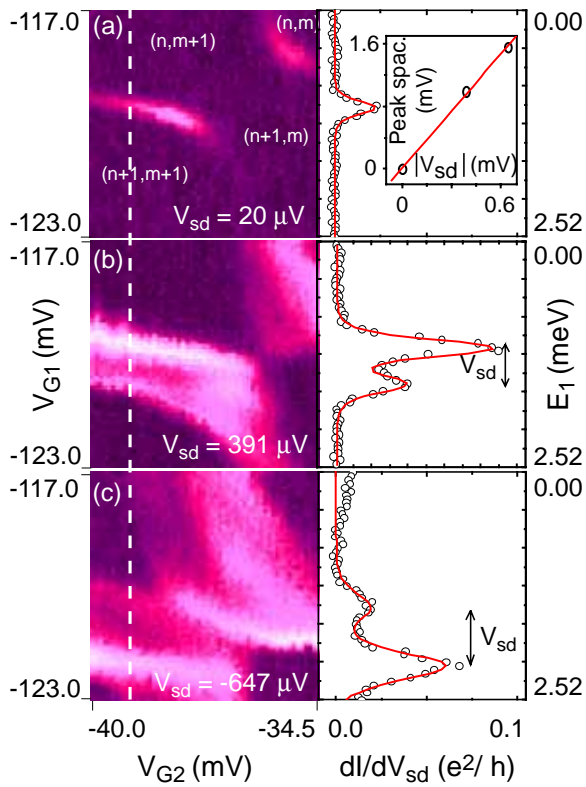
$$U' = \frac{2e^2 C_m}{C_1 C_2 - C_m}$$

$t \sim 310-360 \mu\text{eV}$

$U' < 100 \mu\text{eV}$



# energy-scale



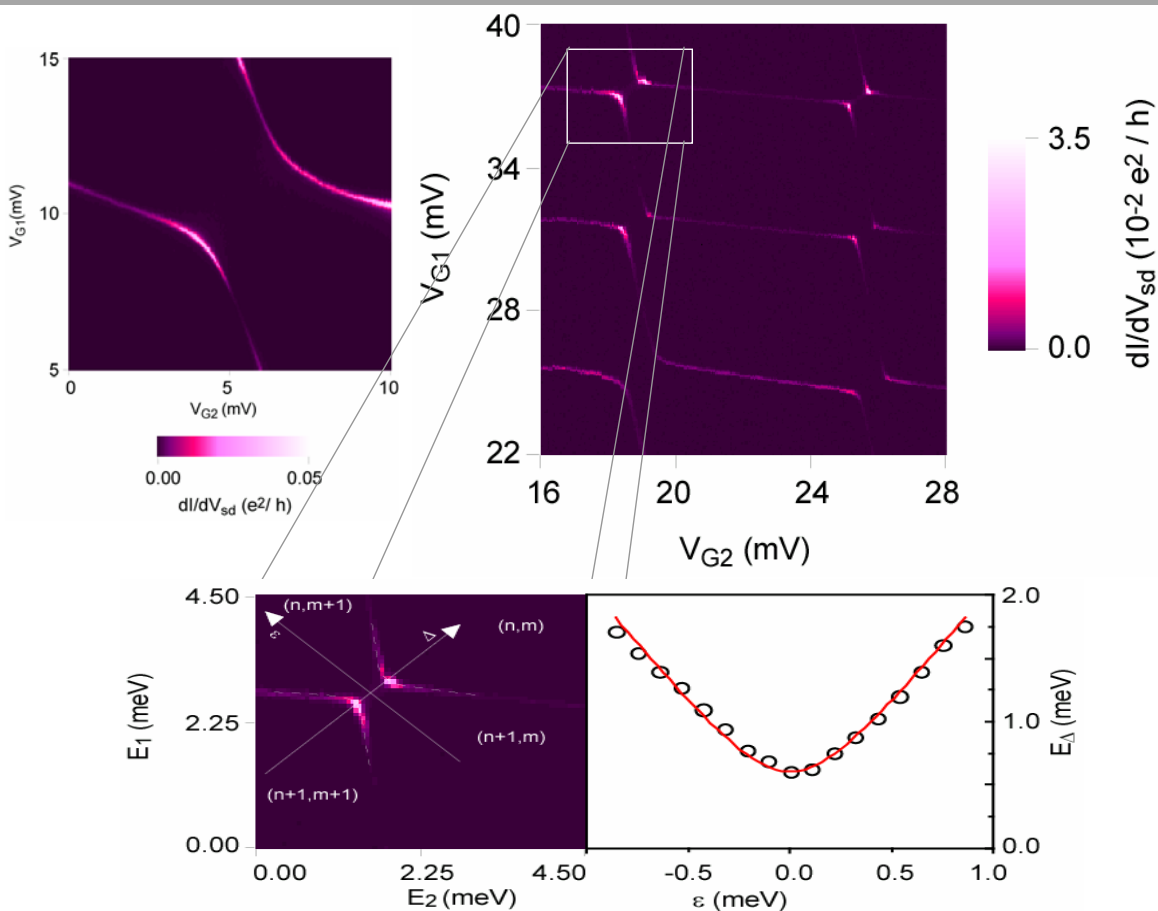
$$\psi^+ = \alpha |n+1, m\rangle + \beta |n, m+1\rangle$$

$$I = e\Gamma |\alpha \cdot \beta|^2 \{f(\mu_{2dot} - \mu_{source}) - f(\mu_{2dot} - \mu_{drain})\}$$

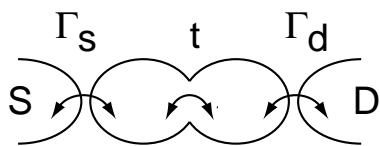
$$\frac{dI}{dV} = -e\Gamma |\alpha \cdot \beta|^2 \{(1-r)f'(\Delta\mu_S) + rf'(\Delta\mu_D)\}$$

$$r := \frac{\partial \mu_{2dot}}{\partial \mu_{source}} = \frac{C_S}{C_\Sigma}$$

# more data



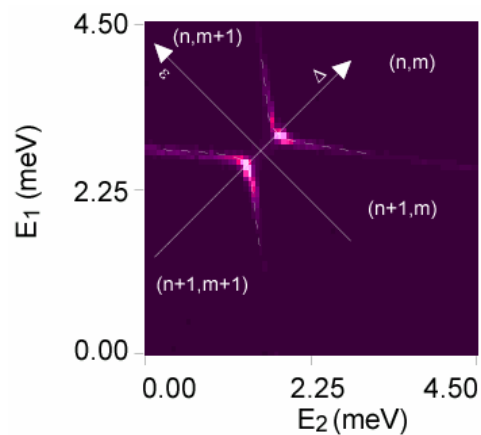
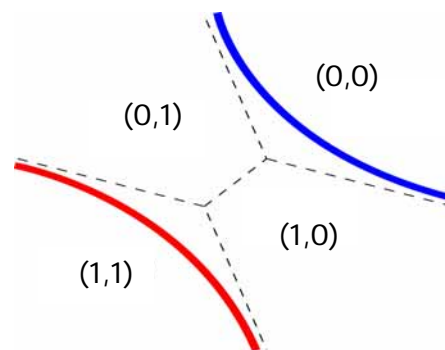
# mapping of molecular states



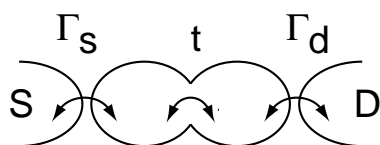
$$\psi = \alpha|n+1, m\rangle + \beta|n, m+1\rangle$$

$$\alpha, \beta(\varepsilon) = \frac{|t|^2}{|t|^2 + \left(\varepsilon \pm \sqrt{\varepsilon^2 + |t|^2}\right)^2}$$

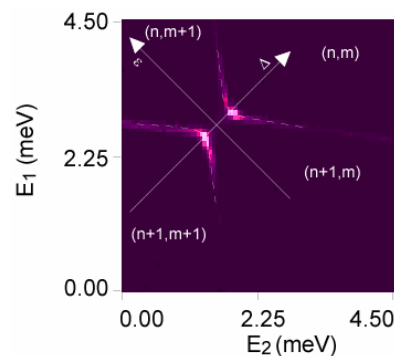
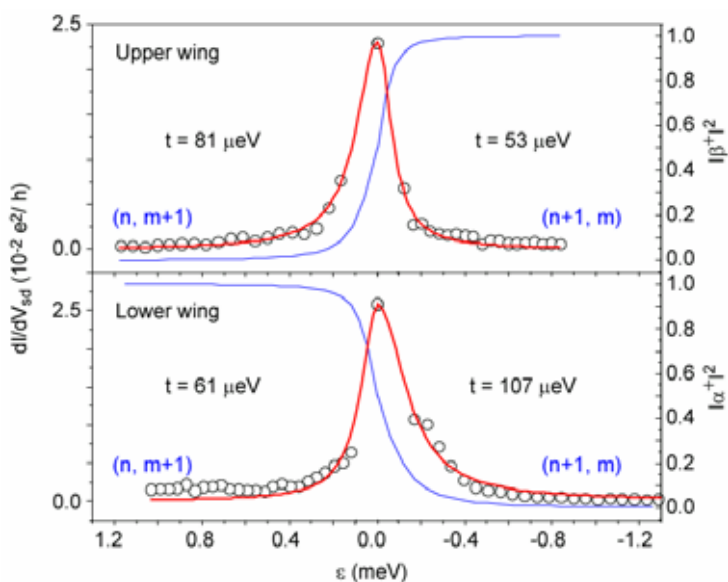
$$G = e\Gamma|\alpha(\varepsilon) \cdot \beta(\varepsilon)|^2$$

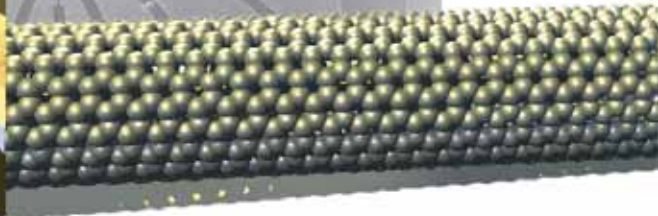
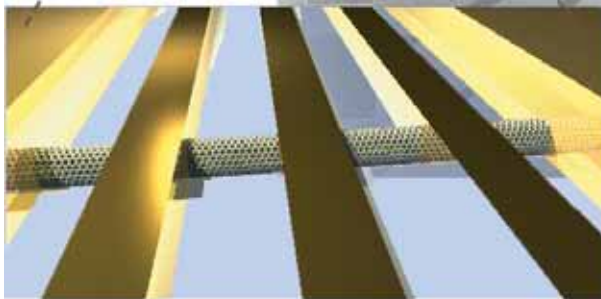
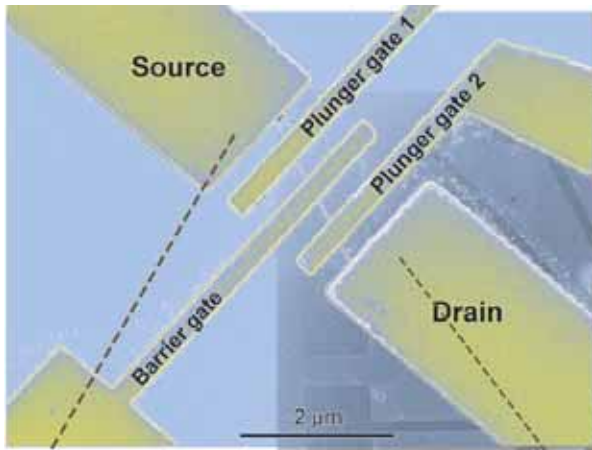


# mapping of molecular states



$$\psi = \alpha|n+1, m\rangle + \beta|n, m+1\rangle$$

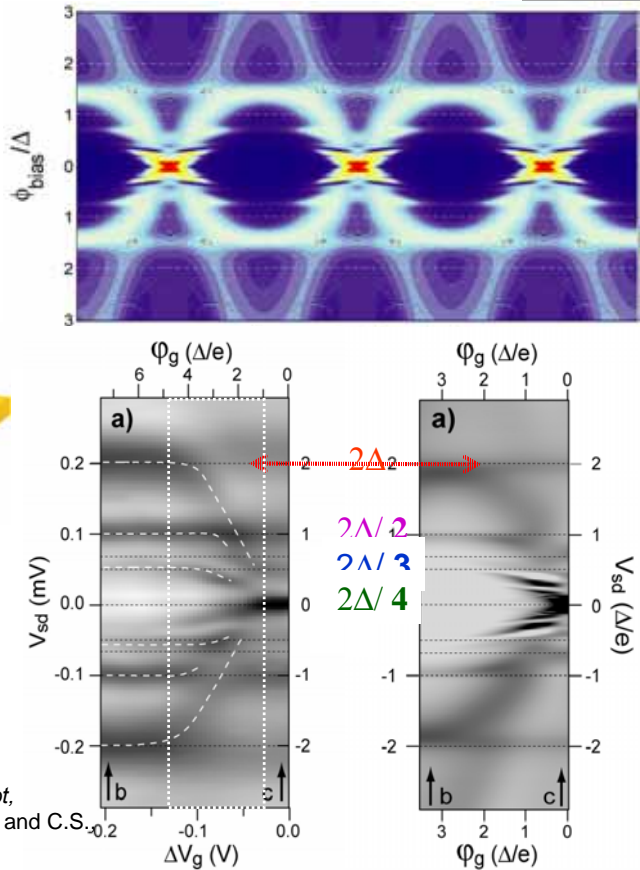
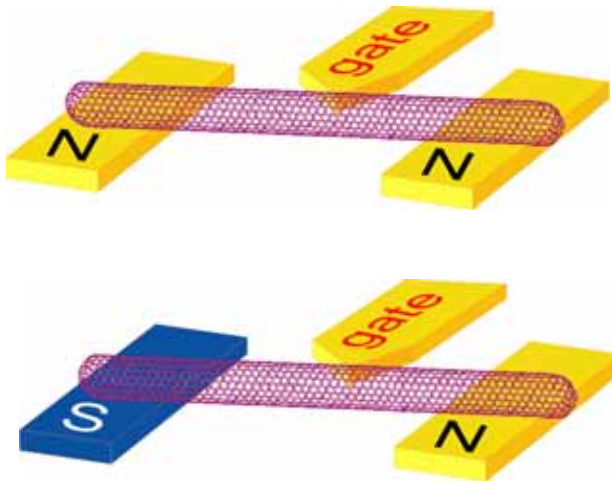




Accessing the quantum world through electronic transport in carbon nanotubes



# Carbon Nanotube Devices

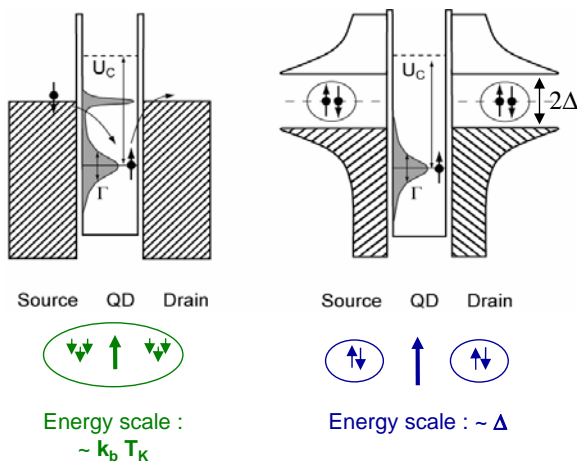


1. Multi-wall carbon nanotubes as quantum dots  
**M. R. Buitelaar**, A. Bachtold, T. Nussbaumer, M. Iqbal and C.S.,  
 Phys. Rev. Lett. 88, 156801 (2002).
2. A quantum dot in the Kondo regime coupled to superconductors,  
**M. R. Buitelaar**, T. Nussbaumer, and C. Schönberger,  
 Phys. Rev. Lett. 89(25):256801 (2002).
3. Multiple Andreev Reflections in a Carbon Nanotube Quantum Dot,  
**M. R. Buitelaar**, W. Belzig, T. Nussbaumer, B. Babić, B. Bruder, and C.S.,  
 Phys. Rev. Lett. 91:057005 (2003).

# Carbon Nanotube Hybrid Dots



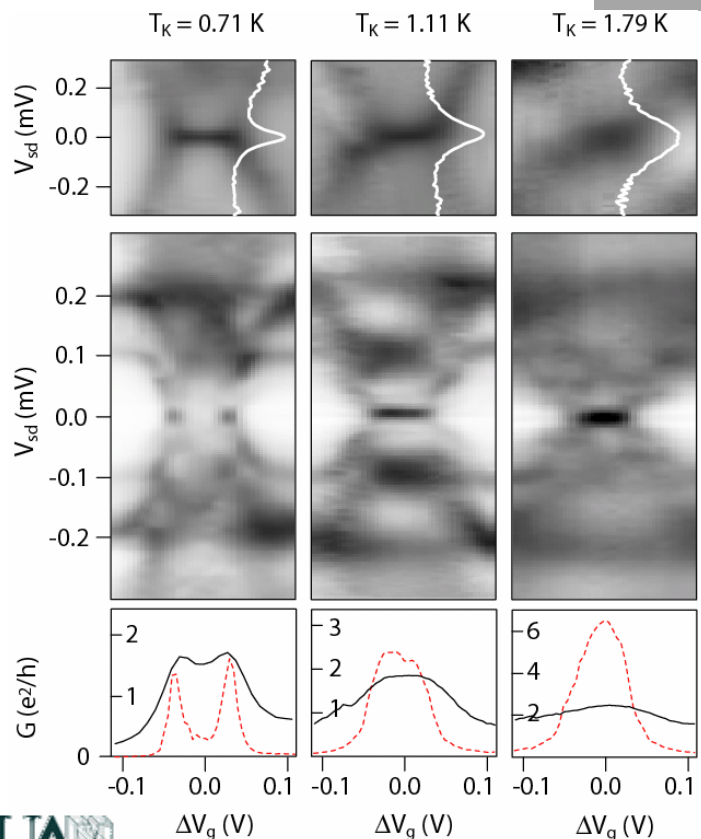
## Kondo effect & Superconductivity

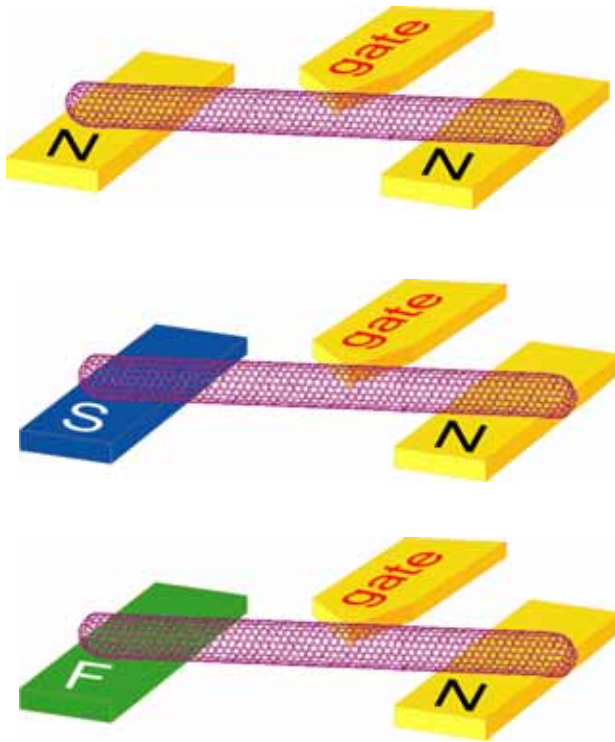


A cross-over at  $k_B T_K \sim \Delta$

*Phys. Rev. Lett.* 89, 256801 (2002)

*Solid-State Communications* 131, 625 (2004)

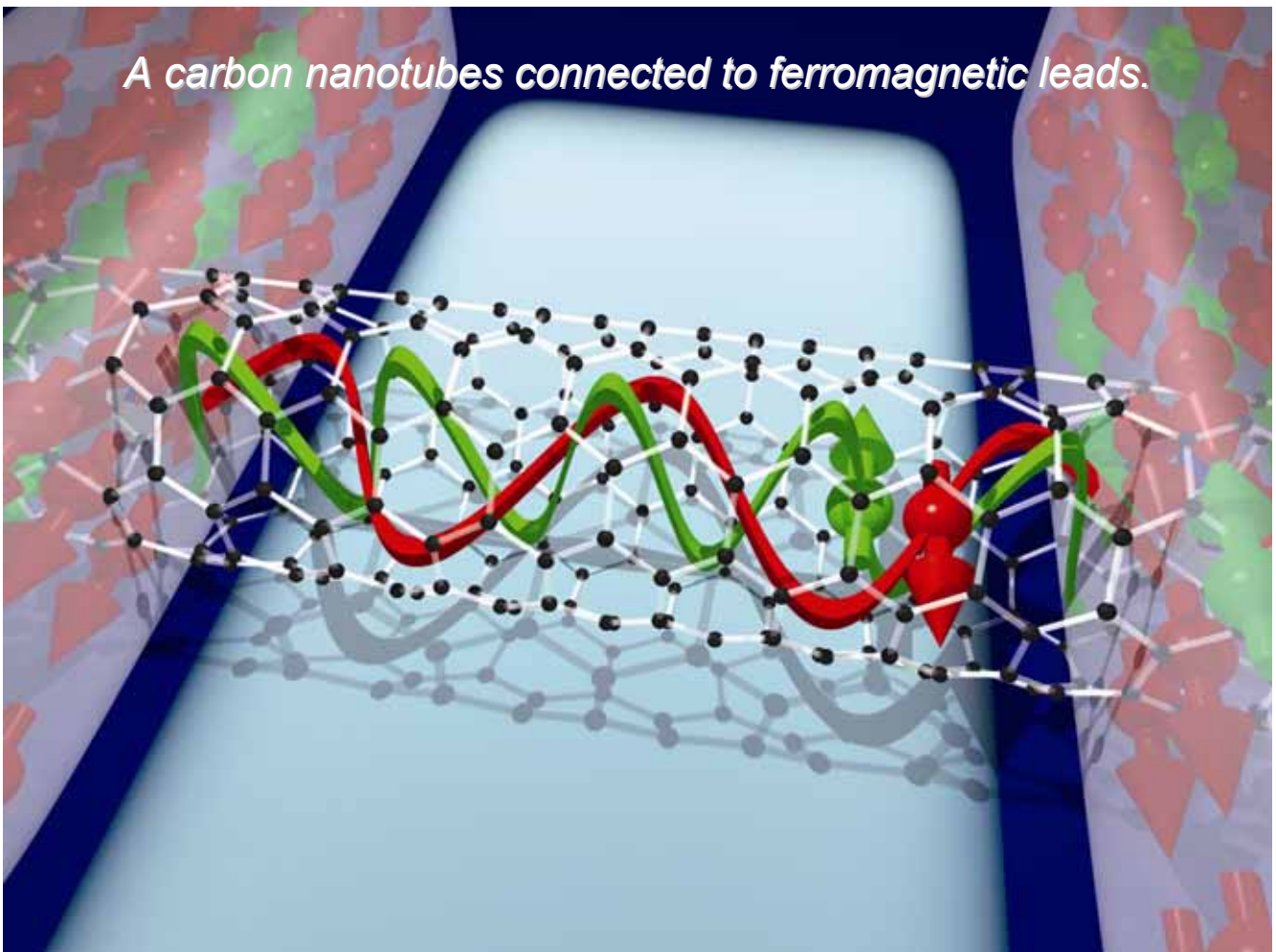




Carbon Nanotubes are great because novel quantum devices (hybrid devices) can be realized



*A carbon nanotubes connected to ferromagnetic leads.*





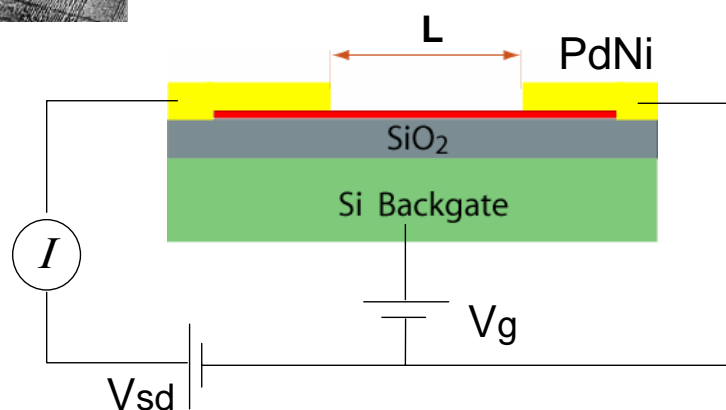
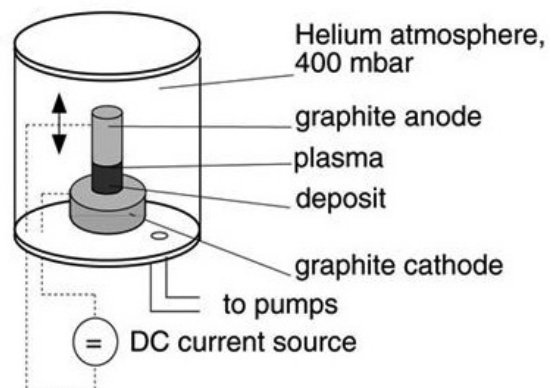
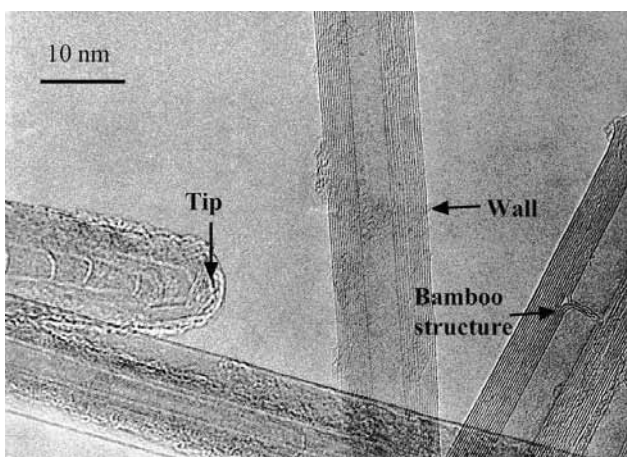
## Spin dependent transport in nanostructures

- Importance of quantum coherence and interference
- ➔ Effect of size quantization on spin transport ?

## Spin vs Charge in low dimensional conductors

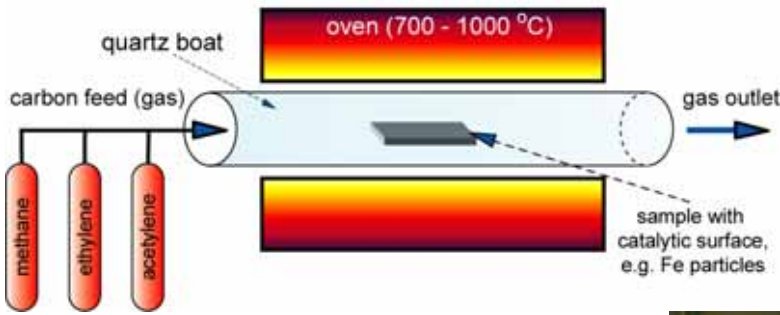
- Importance of electron-electron interactions
- Tunability of electronic transport (weak screening).
- ➔ Manipulation of spins for quantum computing.
- ➔ Realization of spin FETs.

# Multi-Wall Carbon Nanotubes

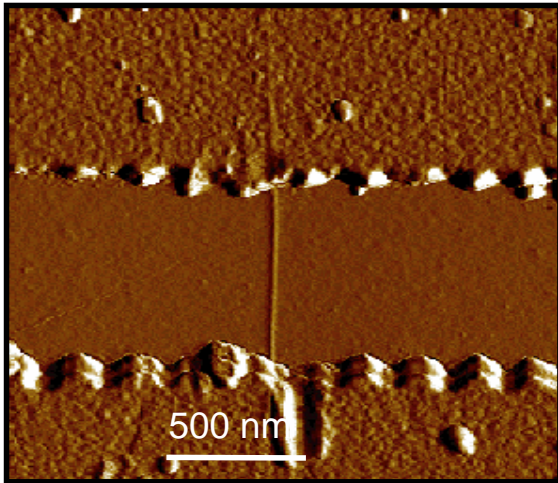


Laszlo Forró EPFL

# Single-Wall Carbon Nanotubes



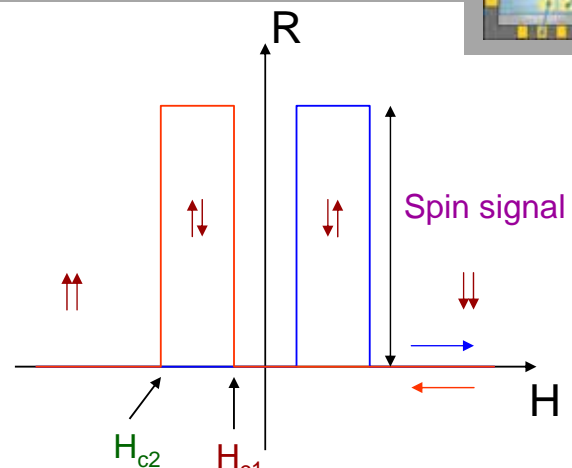
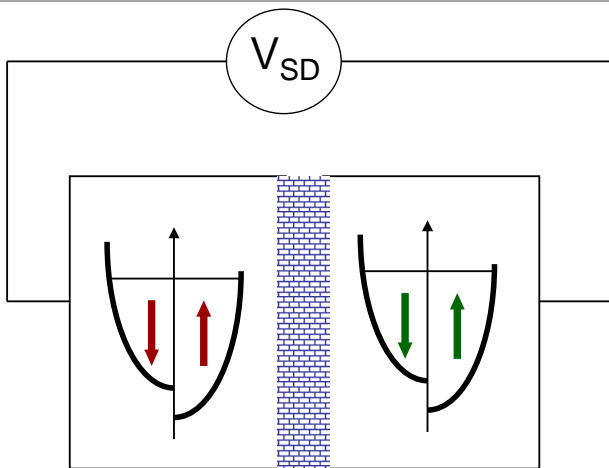
Bakir Babic



Jürg Furer

acknowledgment, also:  
Jing Kong and  
Herre van der Zant !

# Introduction: Spin Valve Effect



$H_{c1} < H_{c2}$  Jullière's model

$$G_{AP} \propto |t|^2 2N_{\uparrow}N_{\downarrow}$$

$$G_P \propto |t|^2 (N_{\uparrow}^2 + N_{\downarrow}^2)$$

$G_P > G_A$  because  $N_{\uparrow}^2 + N_{\downarrow}^2 > 2N_{\uparrow}N_{\downarrow}$

$$P = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$$

$$TMR = 2 \frac{G_P - G_{AP}}{G_P + G_{AP}} = 2P_L P_R$$

Assumes spin and energy independent transmission !

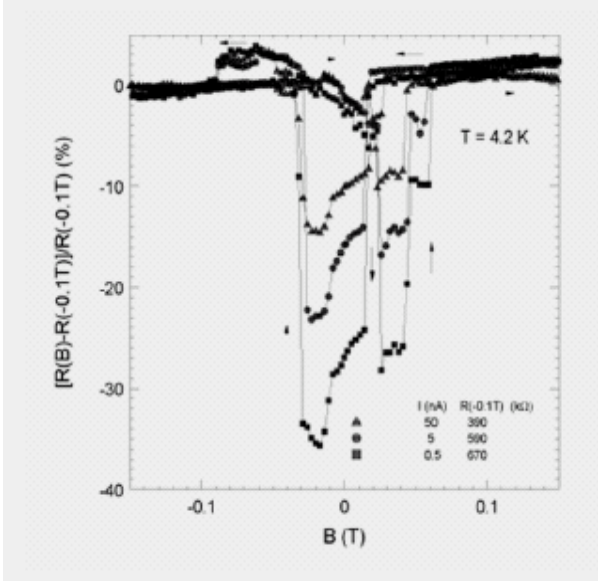
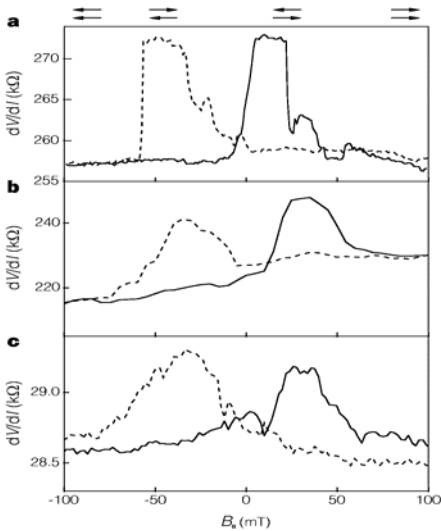


# Previous work

## Co contacts

K. Tsukagoshi et al., Nature, **401**, 572 (1999)

B. Zhao et al., J. Appl. Phys. , **91**, 7026 (2002)



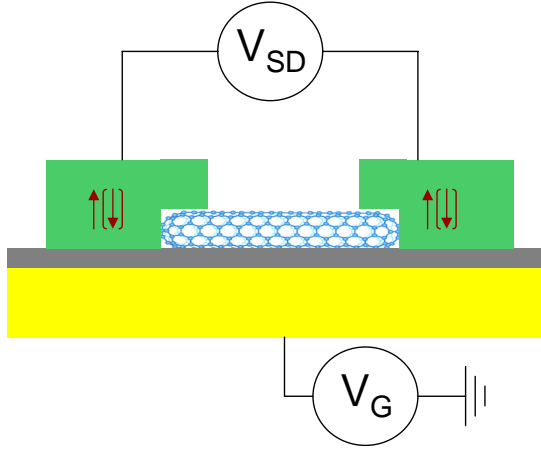
- Positive TMR ~5%
- No gate !

- Negative TMR ~ -30%
- No gate !

➔ Normal as well as anomalous TMR...?



# Spin Injection in NTs



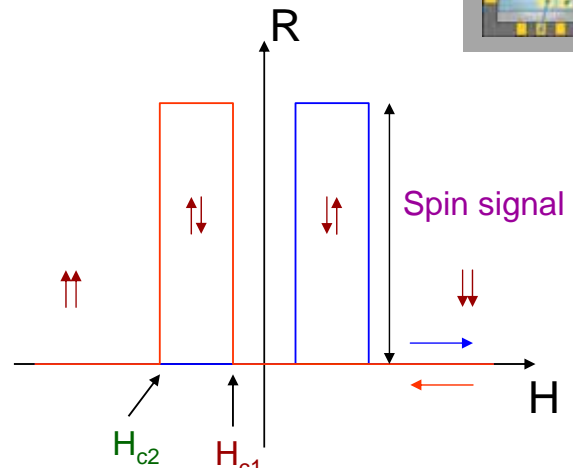
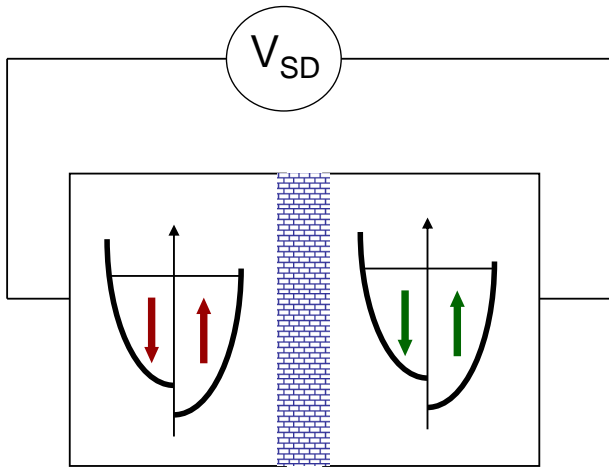
Gate

### Spin valve geometry (2 terminal)

- Injection and detection of spins with ferromagnetic electrodes.
- Study as a function of  $V_{SD}$  and  $V_G$ .



# Introduction: Spin Valve Effect



$H_{c1} < H_{c2}$  Jullière's model

$$P = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$$

$$G_{AP} \propto |t|^2 2N_{\uparrow}N_{\downarrow}$$

$$G_P \propto |t|^2 (N_{\uparrow}^2 + N_{\downarrow}^2)$$



$$TMR = 2 \frac{G_P - G_{AP}}{G_P + G_{AP}} = 2P_L P_R$$

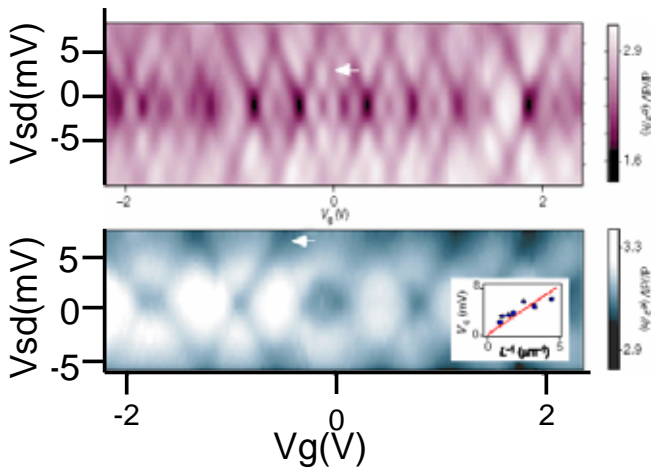
$G_P > G_A$  because  $N_{\uparrow}^2 + N_{\downarrow}^2 > 2N_{\uparrow}N_{\downarrow}$

**Assumes spin and energy independent transmission !**

# quantum interference and charging



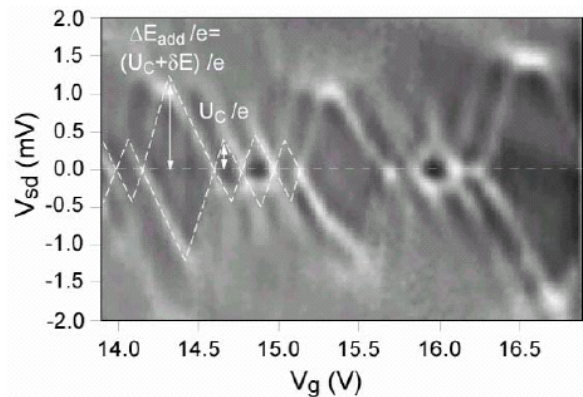
W. Liang et al., Nature **411**, p 665 (2001)



- Fabry-Perot in SWNTs

$$E = \hbar v_F / 2L \longrightarrow 1.67 \text{ meV}/\mu\text{m}$$

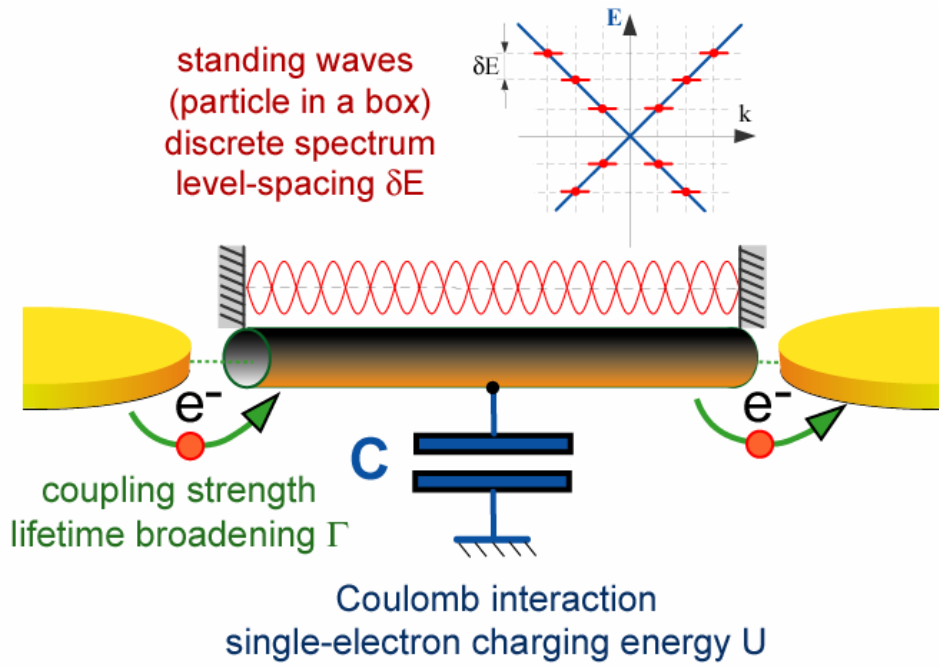
Mark Buitelaar et al., PRL **88**, 156801 (2002)



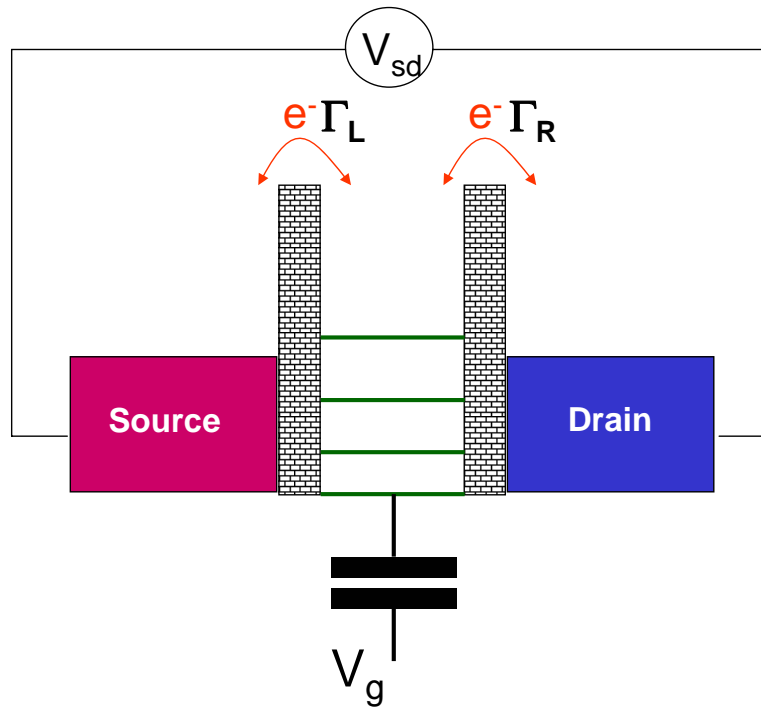
- Quantum dot in MWNTs

Energy dependent transmission in NTs...

# Nanotubes as quantum dots



# Nanotubes as quantum dots



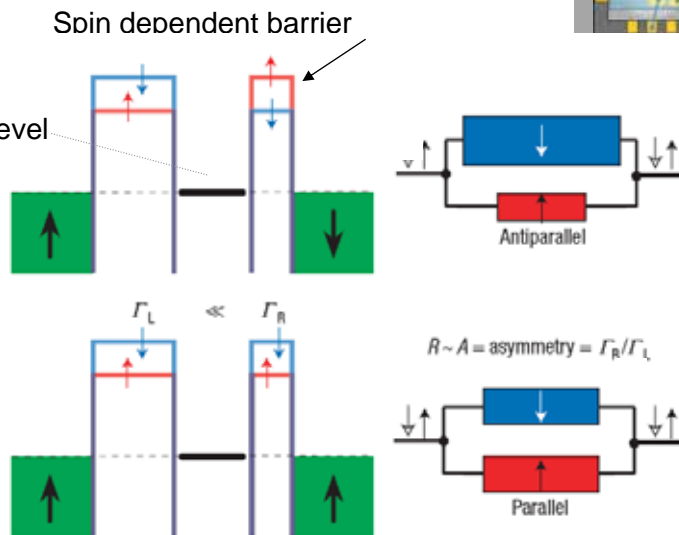


# TMR and quantum interference

$$T(E) = \frac{\Gamma_L \Gamma_R}{(E - E_0)^2 + ((\Gamma_L + \Gamma_R)/2)^2}$$

$$\Gamma_L = \Gamma_L (1 \pm P_L)$$

$$\Gamma_R = \Gamma_R (1 \pm P_R)$$



Off-resonance,

$$T(E) \propto \Gamma_R \Gamma_L, TMR = \frac{2P_L P_R}{1 - P_L P_R}$$

On resonance with asymmetry,

$$\Gamma_L \gg \Gamma_R \Rightarrow T(E) = 4\Gamma_R / \Gamma_L, TMR = \frac{-2P_L P_R}{1 + P_L P_R}$$

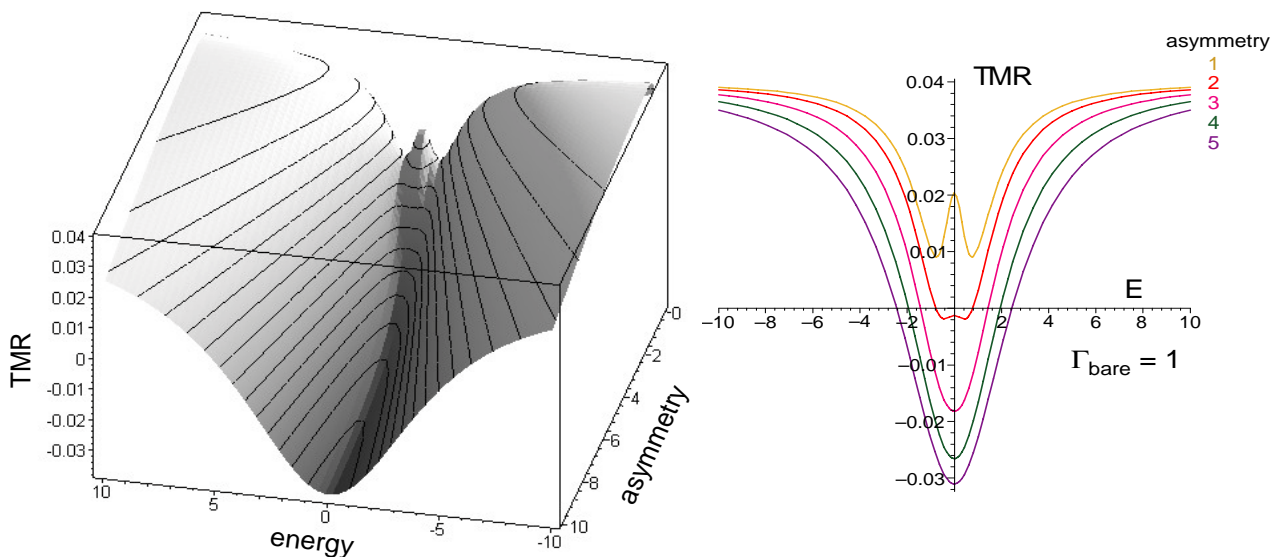
➔ SpinFET behavior because  $E_0$  controlled by gate.

See also E.Y. Tsymbal et al. PRL 90, 186602 (2003) in Ni/NiO/Co nanojunctions



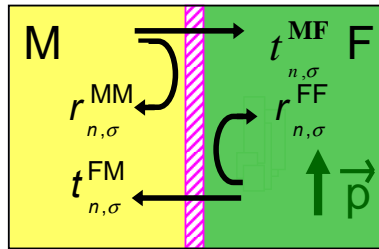
# RT yields a symmetric TMR

$\Gamma=1$  and  $P=0.2$ , one resonance





## Spin-Dependence of Interfacial Phase Shifts (SDIPS)



$n$  : channel index  
 $\sigma$  : spin

Transmission amplitude

$$t_{\sigma}^{\text{FM(MF)}} = \sqrt{T_{\sigma}} e^{i\phi_{\sigma}^{\text{FM(MF)}}$$

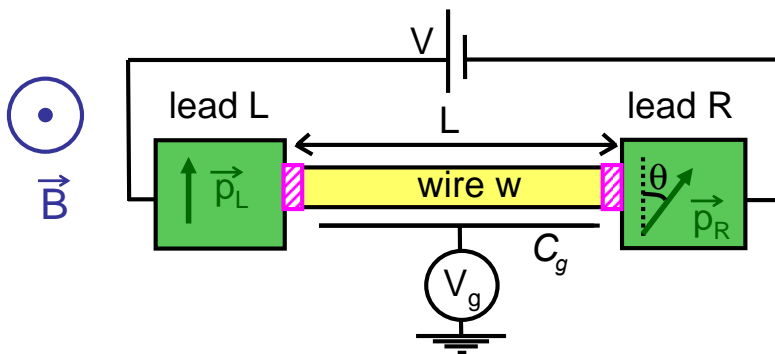
Reflexion amplitude

$$r_{\sigma}^{\text{FF(MM)}} = \sqrt{1-T_{\sigma}} e^{i\phi_{\sigma}^{\text{FF(MM)}}$$

SDIPS

A. Cottet, T. Kontos, W. Belzig, C.S and C. Bruder, to appear in Eur. Phys. Lett.

## Ballistic channel with F-leads



Assumptions :

- interactions neglected
- single channel wire
- $e\kappa V_g, g\mu_B B \ll E_F^W$   
 $\kappa = C_g / C_W$

Scattering description with parameters:

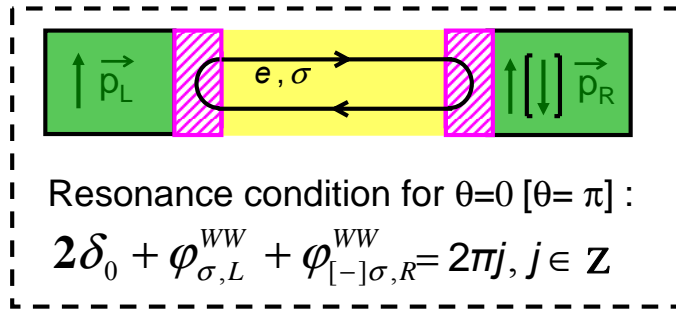
$\delta_0 = L(k_F^W + (e\kappa V_g - E_F^W) / \hbar v_F^W)$  Phase acquired by carriers along w at B=0

$$T_{L(R)} = (T_{L(R)}^{\uparrow} + T_{L(R)}^{\downarrow}) / 2 \quad P_{L(R)} = (T_{L(R)}^{\uparrow} - T_{L(R)}^{\downarrow}) / (T_{L(R)}^{\uparrow} + T_{L(R)}^{\downarrow})$$

$$\phi_{\sigma, L(R)}^{WW} \longrightarrow \Delta\phi_{L(R)}^{WW} = \phi_{\uparrow, L(R)}^{WW} - \phi_{\downarrow, L(R)}^{WW} \neq 0 \quad \text{SDIPS parameters}$$

A. Cottet, T. Kontos, W. Belzig, C.S and C. Bruder, to appear in Eur. Phys. Lett.

# Bound states are spin-dependent



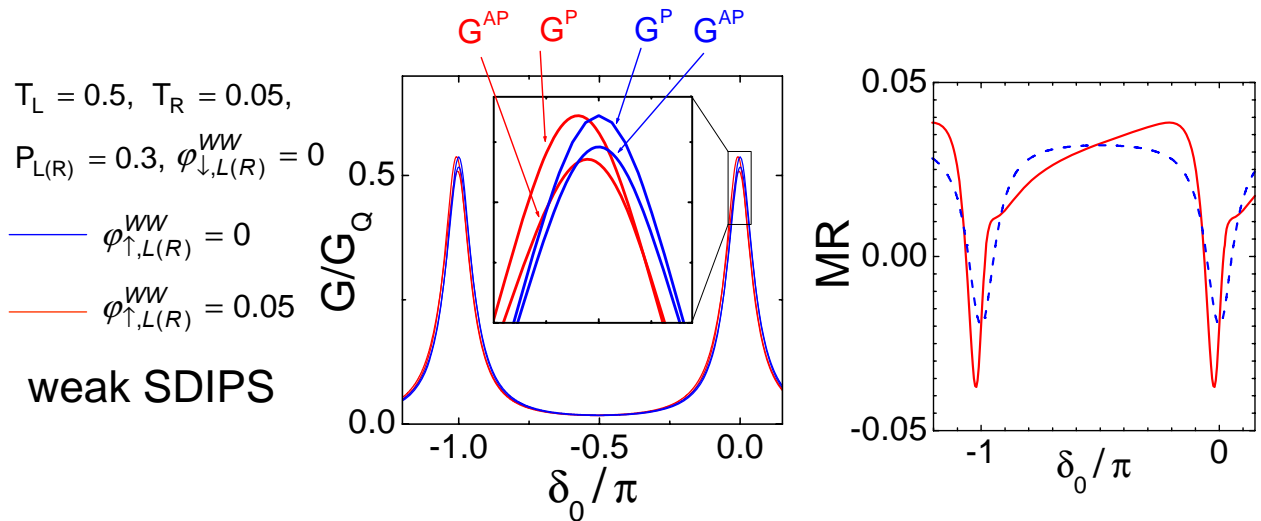
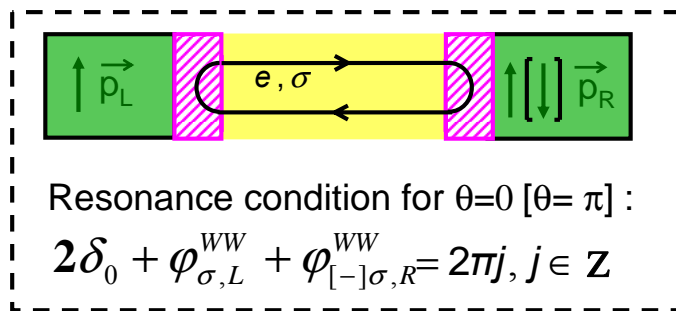
tunneling limit

$$T_{\sigma}^{m_1, m_2} = \frac{4\Gamma_{1\sigma}^{m_1} \Gamma_{2\sigma}^{m_2}}{4\epsilon^2 + (\Gamma_{1\sigma}^{m_1} + \Gamma_{2\sigma}^{m_2})^2} \quad (\text{no SDIPS})$$

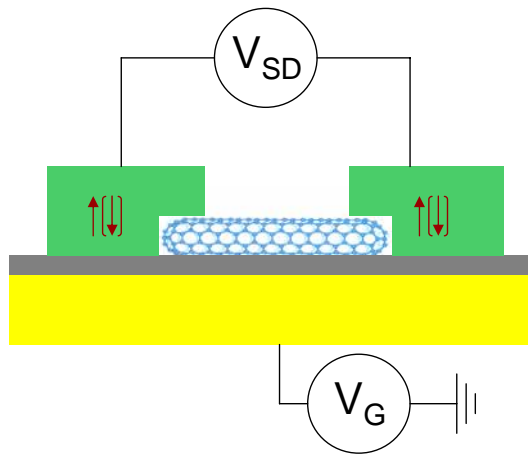
$$T_{\sigma}^{m_1, m_2} = \frac{4\Gamma_{1\sigma}^{m_1} \Gamma_{2\sigma}^{m_2}}{4(\epsilon_{\sigma}^{m_1, m_2})^2 + (\Gamma_{1\sigma}^{m_1} + \Gamma_{2\sigma}^{m_2})^2}$$

$$\epsilon_{\sigma}^{m_1, m_2} := \epsilon_0(V_g) + \kappa\sigma(P_1 m_1 + P_2 m_2)$$

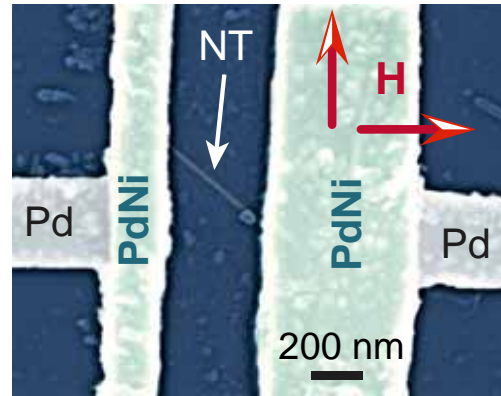
# extended model allows for asymmetric TMR



# an actual device (MWNT)

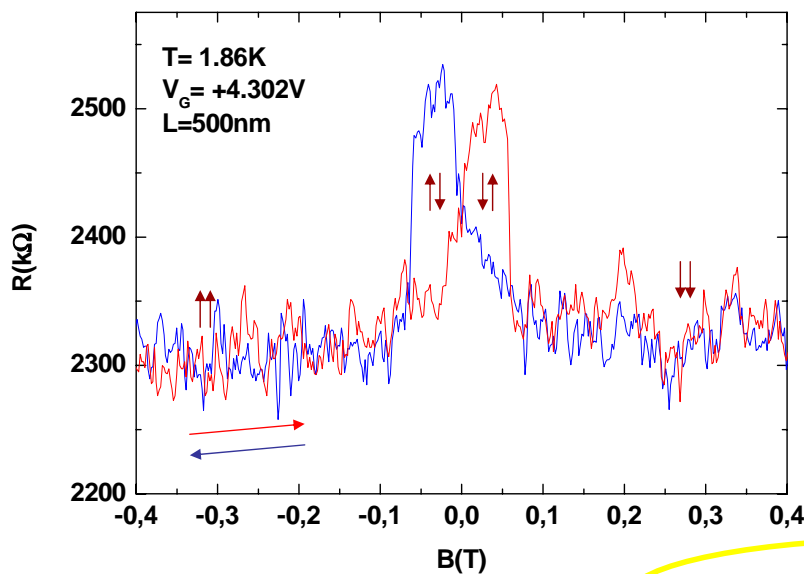


Spin valve geometry



- Transparent contacts using a new contacting scheme with Pd<sub>0.3</sub>Ni<sub>0.7</sub>
- Shape anisotropy to control switching of magnetizations.

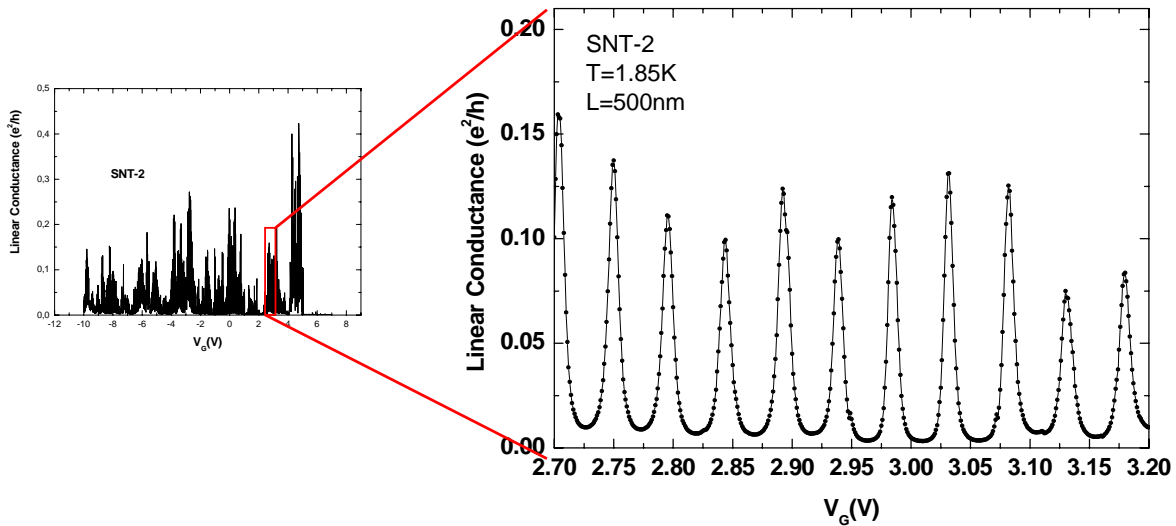
# Spin signal for a SWNT-device



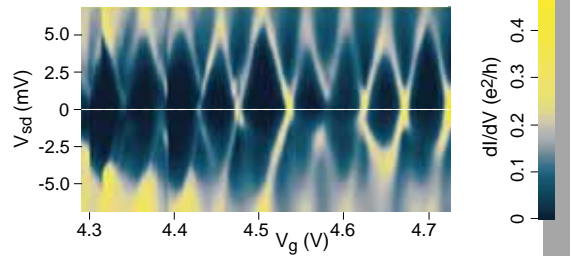
$$TMR = (R_{AP} - R_P) / R_P$$

- Hysteresis ~ 5-10 %
- Sharp switching for ~ 100mT
- TMR ~ 2P<sup>2</sup> with P~0.2

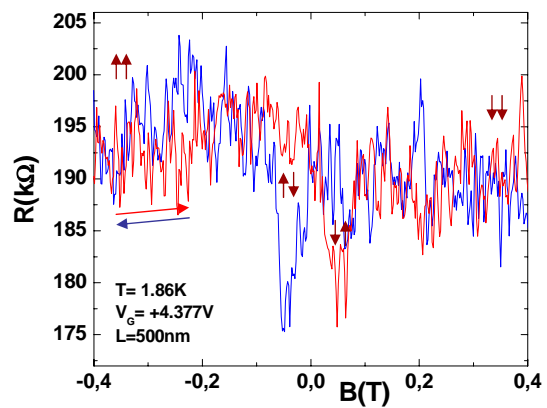
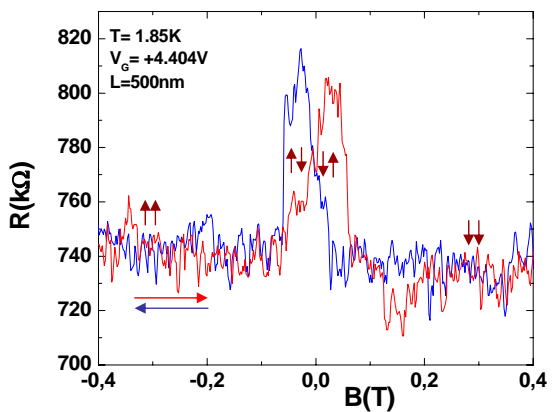
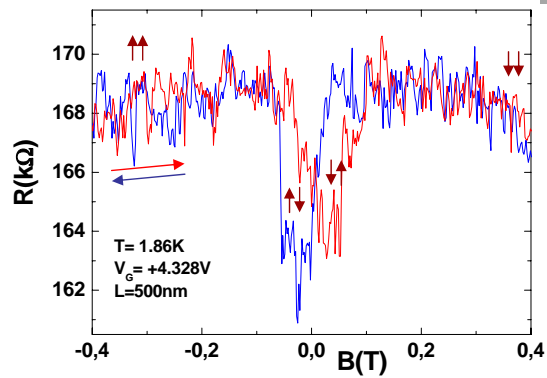
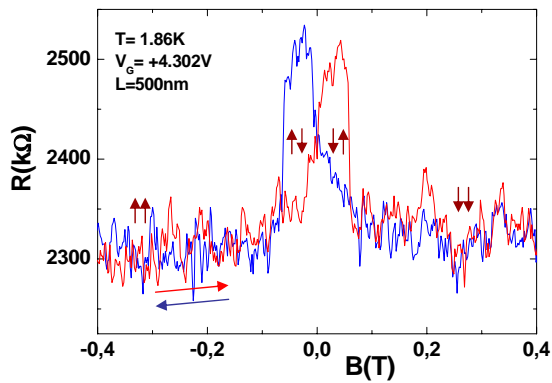
# Linear conductance



- Resonances in conductance at 1.85K
- Peaks always symmetric about maximum

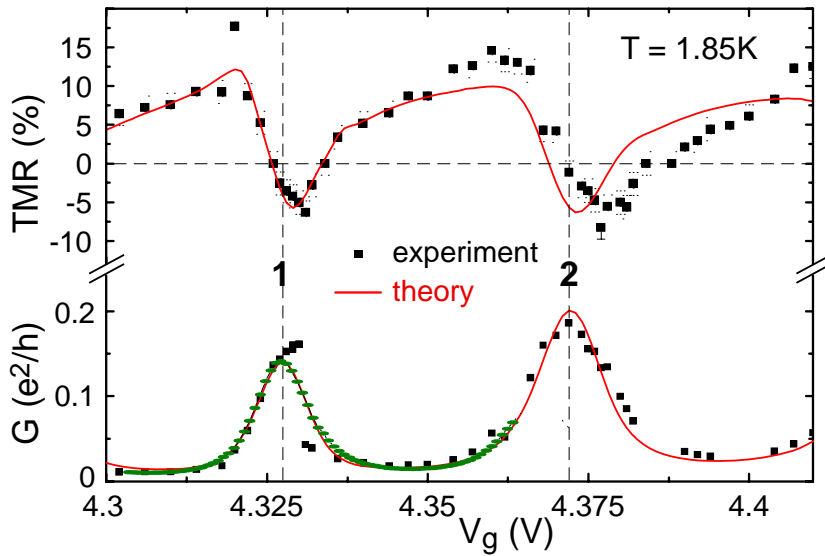


# Gate dependence of TMR

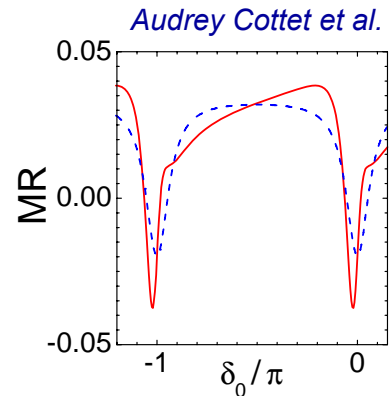
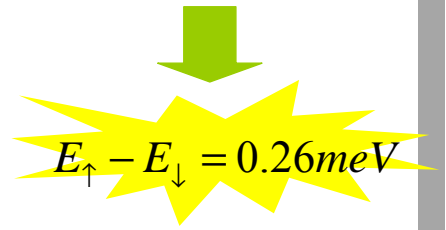


- Sign and amplitude of TMR gate controlled.

# Comparison G and TMR vs Gate



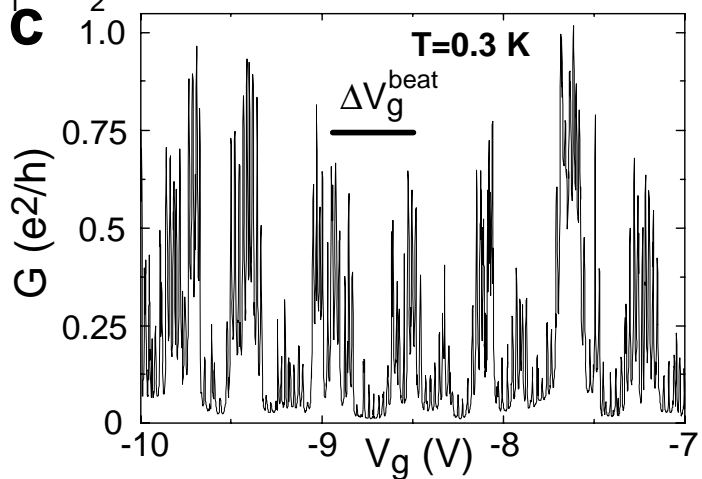
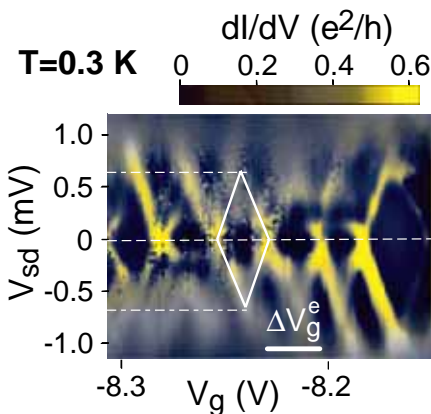
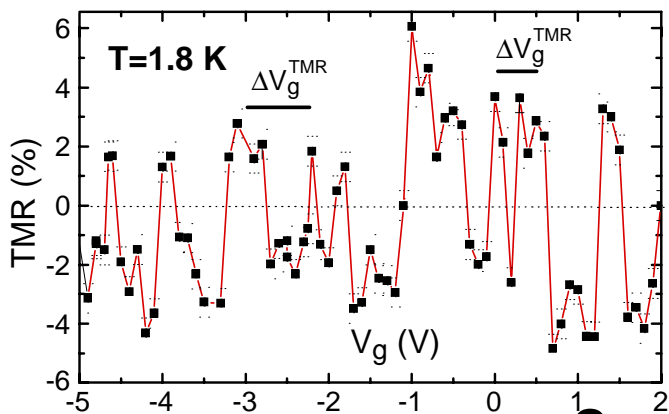
Asymmetry in TMR



- Oscillations of TMR between -8% and +17%.
- Spin dependent resonant tunneling mechanism.
- Direct measurement of spin imbalance  $\sim 2.2 T$ .

S. Sahoo, T. Kontos, J. Furer, C. Hoffmann M. Gräber, A. Cottet and C.S., Nature Phys., 2, 99 (2005)

# „universal“, also seen in MWNTs



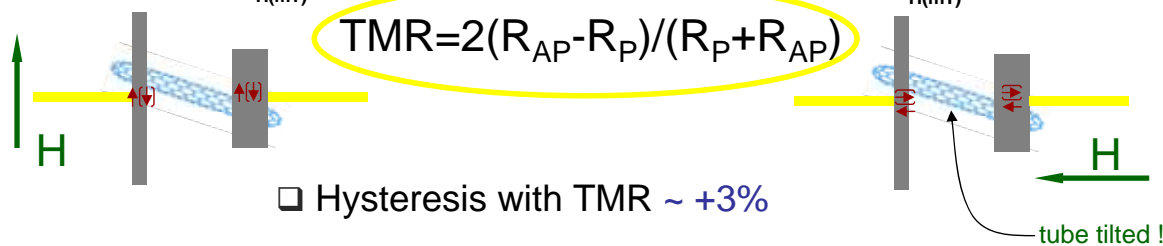
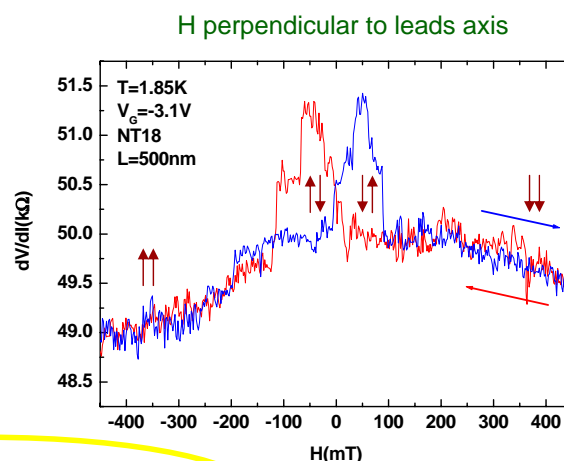
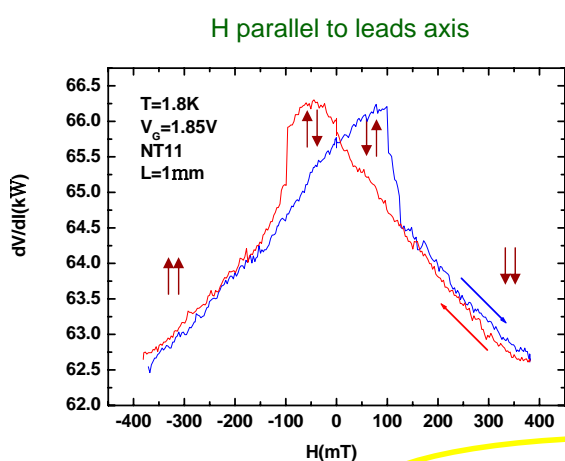




1. stray field
2. magneto-Coulomb effect
3. magnetostrictive effects very locally on the contacts

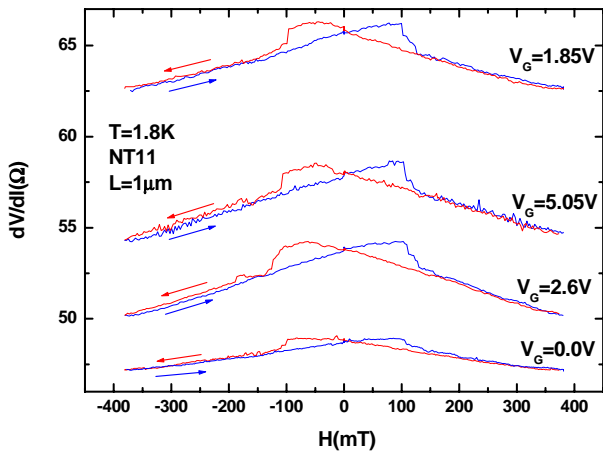
1. magnetic **stray-field** many change R via some „background“ MR of CNT (other than spin-valve)
  - ➔ have a look at background

## Background and MR

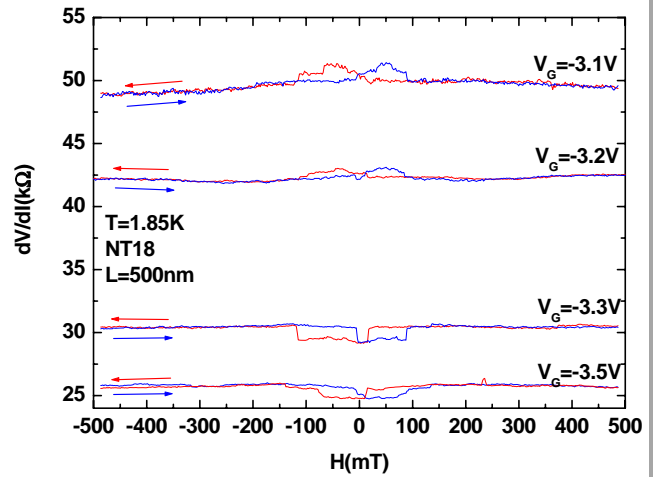


- Hysteresis with TMR ~ +3%
- Sharp switching for ~ 100mT
- Sharper switching for ~ 0mT for perpendicular H

# Background and MR



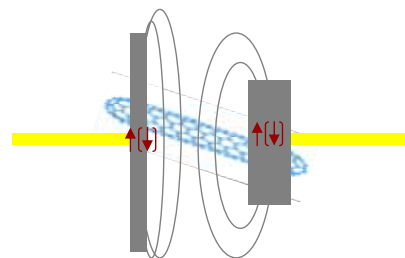
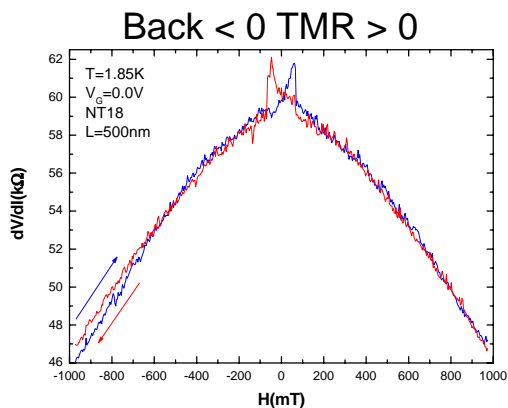
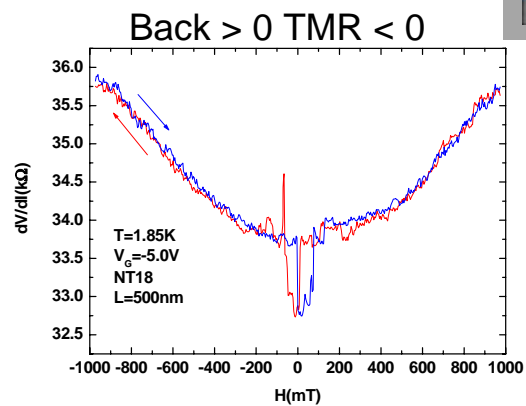
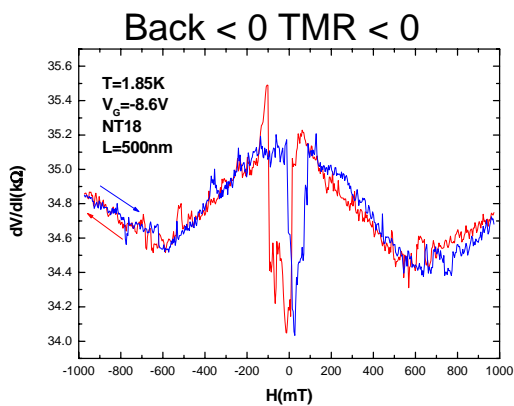
**NT11**



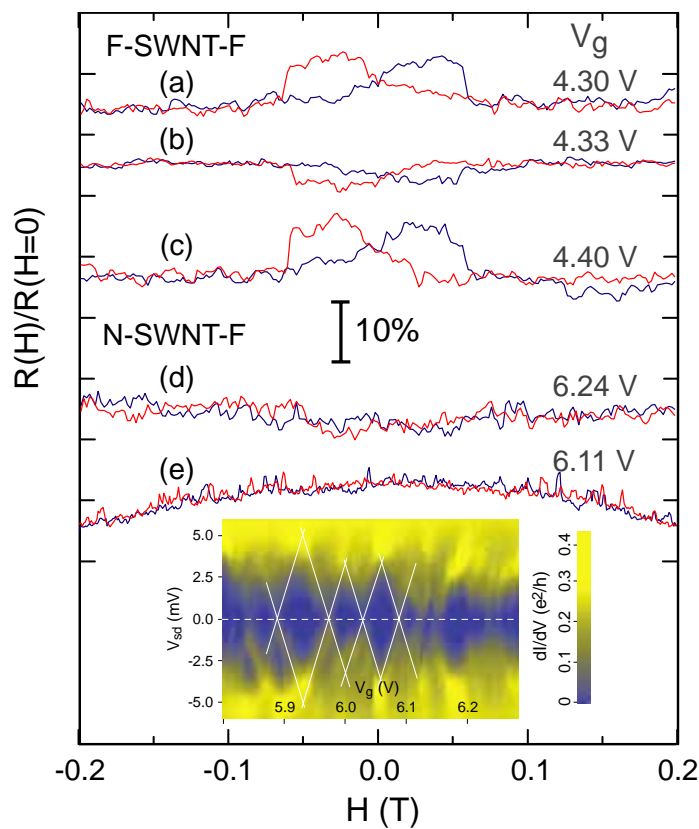
**NT18**

- Amplitude of TMR depends on gate voltage !
- Sign and amplitude** of TMR depend on gate voltage !

# Background and MR



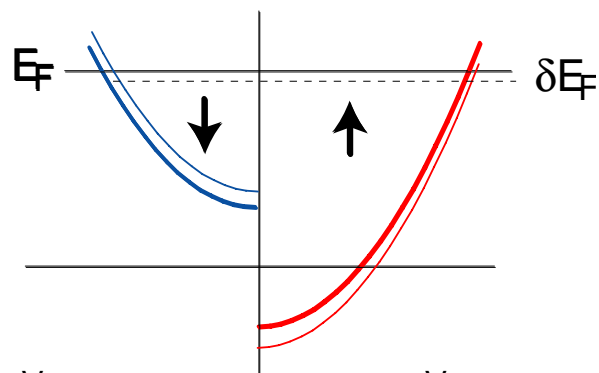
- No stray field effect...



## Magneto-Coulomb Effect

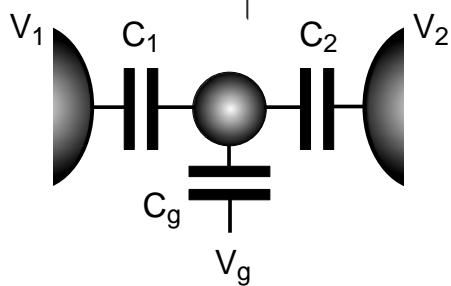


brought to my attention by Bart van Wees and Sense Jan van der Molen

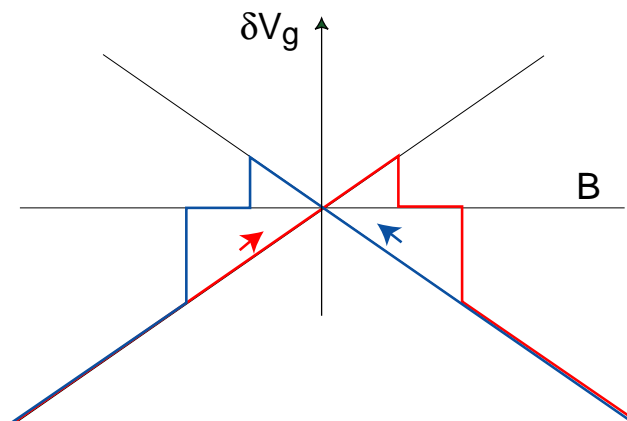


$$\delta E_F = -\frac{1}{2} g P \mu_B B$$

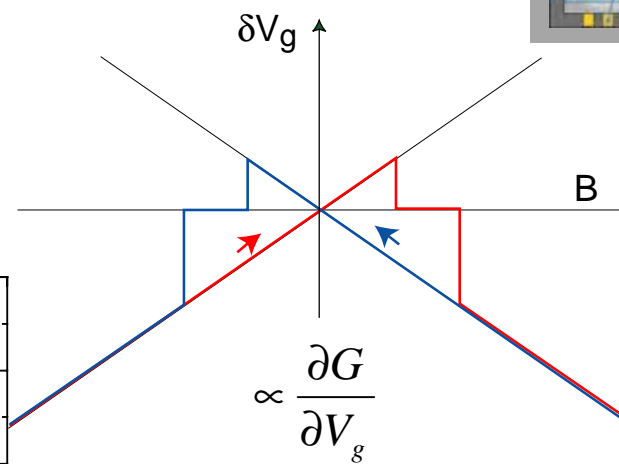
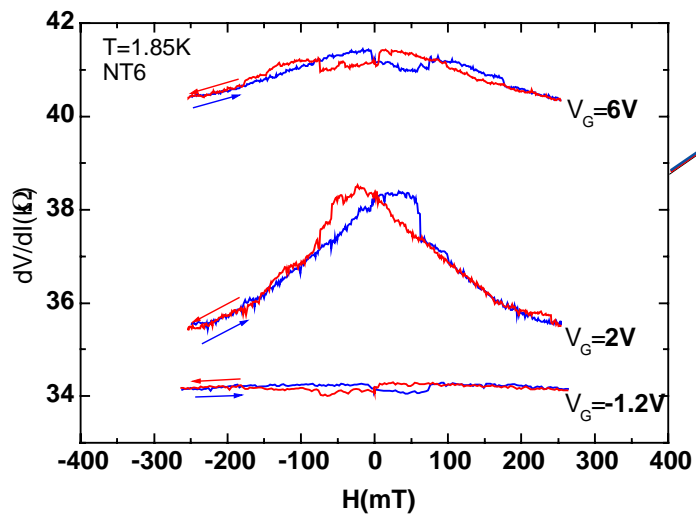
$$P := \frac{N_\uparrow - N_\downarrow}{N_\uparrow + N_\downarrow}$$



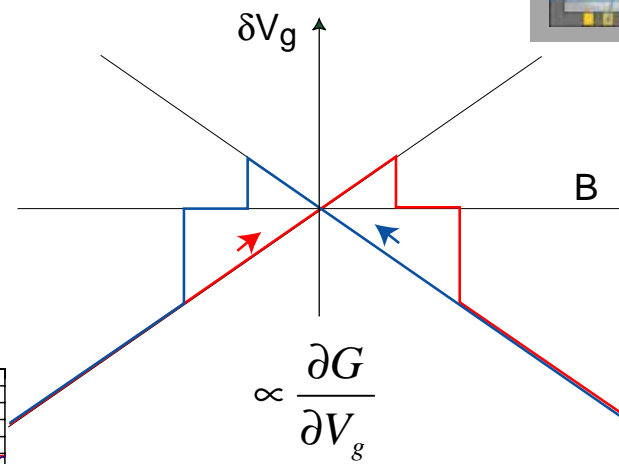
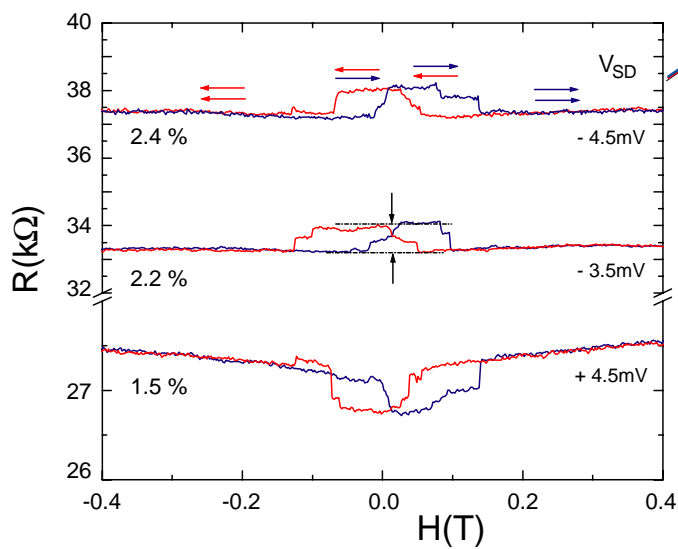
$$\delta V_g = \pm \frac{g \mu_B}{2e C_g} \vec{B} \cdot (C_1 \vec{P}_1 + C_2 \vec{P}_2)$$



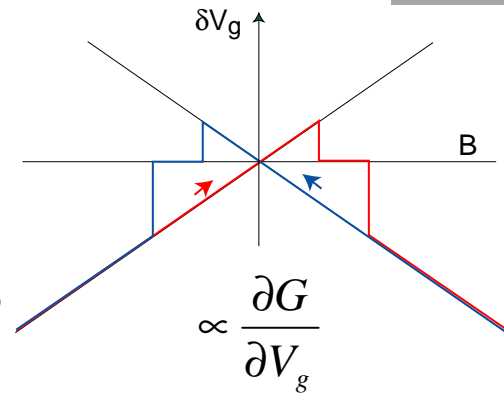
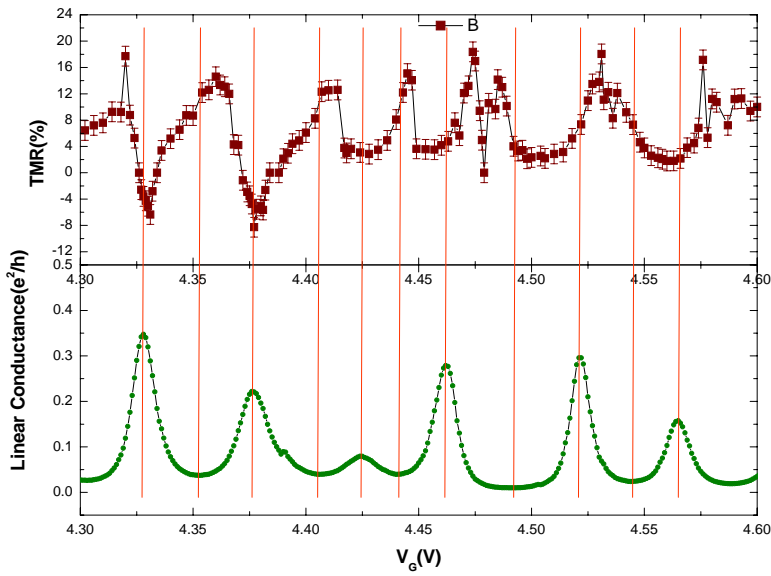
# Magneto-Coulomb



# Magneto-Coulomb



# Magneto-Coulomb

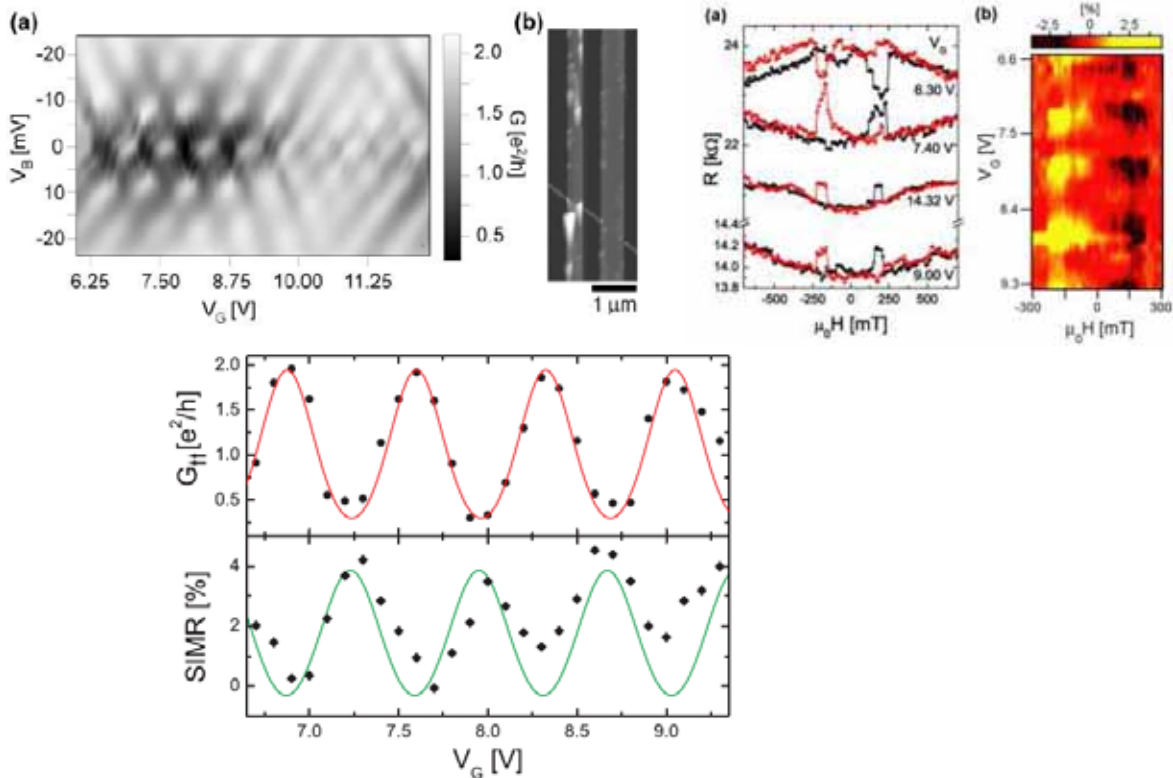


- Correlation between conductance and TMR.
- Not always sign change on a peak...

# Morpurgo et al.



*H.T. Man, I.J.W. Wever, and A.F. Morpurgo, condmat 0512505*





**Gated spin transport through an individual single wall carbon nanotube**

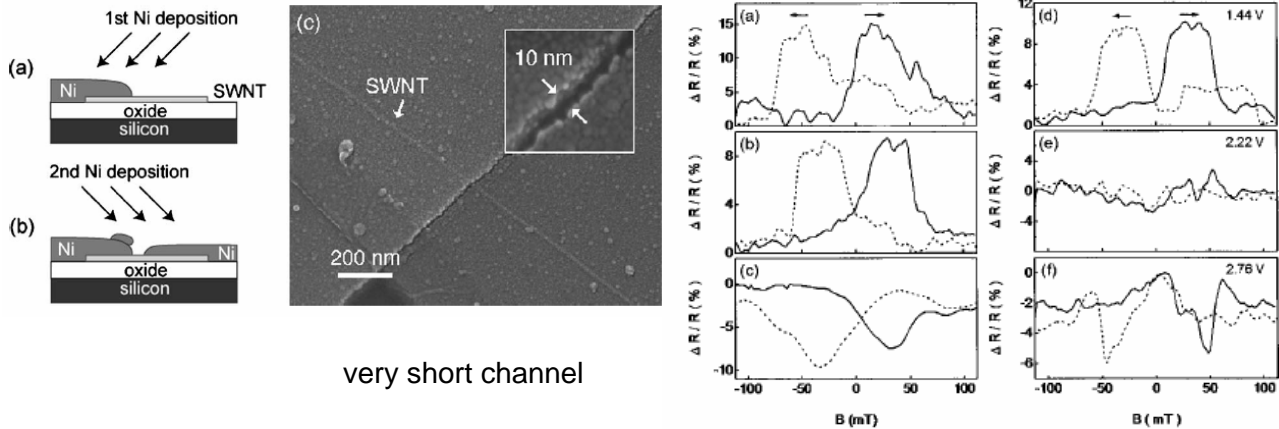
B. Nagabhirava, T. Bansal, G. U. Sumanasekera, and B. W. Alphenaar<sup>a)</sup>  
 Department of Electrical and Computer Engineering and Department of Physics, University of Louisville,  
 Louisville, Kentucky 40292

L. Liu  
 Department of Physics, McGill University, Montreal, Quebec H3A 2T8, Canada

(Received 19 October 2005; accepted 21 November 2005; published online 10 January 2006)

Hysteretic switching in the magnetoresistance of short-channel, ferromagnetically contacted individual single wall carbon nanotubes is observed, providing strong evidence for nanotube spin transport. By varying the voltage on a capacitively coupled gate, the magnetoresistance can be reproducibly modified between +10% and -15%. The results are explained in terms of wave vector matching of the spin polarized electron states at the ferromagnetic / nanotube interfaces. © 2006 American Institute of Physics. [DOI: 10.1063/1.2164367]

some non-trivial gate-effect,  
 but not (yet) periodic



very short channel

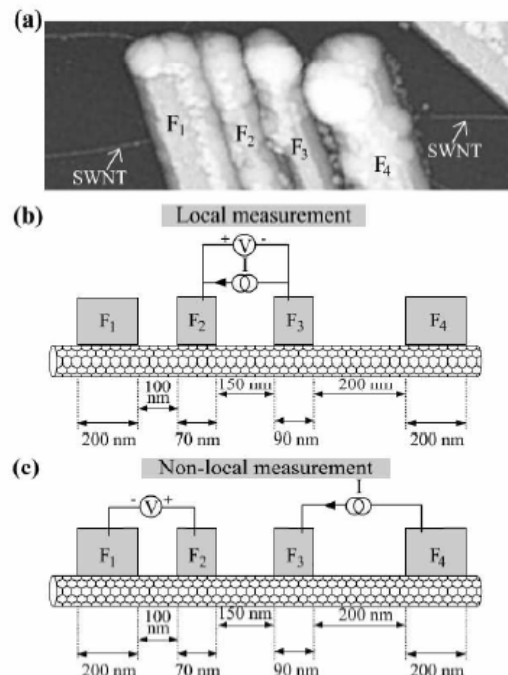
Comment by van Wees et al.



**Separating spin and charge transport in single wall carbon nanotubes**

We demonstrate spin injection and detection in single wall carbon nanotubes using a 4-terminal, non-local geometry. This measurement geometry completely separates the charge and spin circuits. Hence all spurious magnetoresistance effects are eliminated and the measured signal is due to spin accumulation only. Combining our results with a theoretical model, we deduce a spin polarization at the contacts,  $\alpha_F$ , of approximately 25%. We show that the magnetoresistance changes measured in the conventional two-terminal geometry are dominated by effects not related to spin accumulation.

- no gate
- all contacts ferro (rather than N-F-F-N)
- contact transparency may be critical





- Spin injection in carbon nanotubes TMR ~10% (SWNTs)
- Spin FET-like behavior in spin valves with nanotubes due to quantum dot behavior

→ Importance of spin dependent quantum interference

- Can one make effective spin FETs ?
- Direct control of spin possible ?
- Effect of e-e interactions ?

**Refs:**

*S. Sahoo, T. Kontos, CS and C. Sürgers, Appl. Phys. Lett. 86, 112109 (2005)*

*S. Sahoo, T. Kontos, J. Furer, C. Hoffmann, M. Gräber, A. Cottet and CS, Nature Phys. 2, 99 (2005)*

*A. Cottet, T. Kontos, W. Belzig, C.S and C. Bruder, to appear in Eur. Phys. Lett.*

*H.T. Man, I.J.W. Wever, and A.F. Morpurgo, cond-mat 0512505*

*B. Nagabhirava, T. Bansal, G. U. Sumanasekera, B. W. Alphenaar, Appl. Phys. Lett. 88, 023503 (2006)*

*N. Tombros, S.J. van der Molen, B.J. van Wees, cond-mat/0506538)*

## many thanks to

