

The LSP in M-Theory

Eric Kuflik

with Bobby Acharya and Gordon Kane

Michigan Center for Theoretical Physics
University of Michigan, Ann Arbor

May 5 / SVP

Outline

- 1 M-Theory Overview
- 2 Wino LSP
- 3 R-Parity

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – **Wino LSP**

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – **Wino LSP**

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – Wino LSP

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – Wino LSP

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – Wino LSP

Moduli Stabilization in the G_2 MSSM

- All Moduli are stabilized – in detail.
- G_2 moduli z_j are stabilized by hidden sector Gaugino Condensation

$$W = A_1 \Phi^{a_1} e^{ib_1 f_1(z)} + A_2 \Phi^{a_2} e^{ib_2 f_2(z)} + \dots$$

- SUSY breaking is dominated by the hidden sector meson fields.
- MSSM scalar masses $\sim m_{3/2} \gtrsim 10$ TeV
- Meson fields (to leading order) do not appear in the gauge kinetic function
- Gaugino Masses are suppressed – **Wino LSP**

Non-Thermal LSP Acharya, Kumar, Bobkov, Kane, Shao, Watson arXiv:0804.0863

- Moduli dominate the early universe and Decay to LSPs
- The gravitino mass and Moduli masses need to be $\gtrsim 10$ TeV for succesful BBN
- Gives the correct relic abundance !

Note: Probably generic in String Theory - SUGRA Lagrangian suggests at least one Moduli Mass \sim Gravitino Mass

Non-Thermal LSP Acharya, Kumar, Bobkov, Kane, Shao, Watson arXiv:0804.0863

- Moduli dominate the early universe and Decay to LSPs
- The gravitino mass and Moduli masses need to be $\gtrsim 10$ TeV for succesful BBN
- Gives the correct relic abundance !

Note: Probably generic in String Theory - SUGRA Lagrangian suggests at least one Moduli Mass \sim Gravitino Mass

Non-Thermal LSP Acharya, Kumar, Bobkov, Kane, Shao, Watson arXiv:0804.0863

- Moduli dominate the early universe and Decay to LSPs
- The gravitino mass and Moduli masses need to be $\gtrsim 10$ TeV for succesful BBN
- Gives the correct relic abundance !

Note: Probably generic in String Theory - SUGRA Lagrangian suggests at least one Moduli Mass \sim Gravitino Mass

Non-Thermal LSP Acharya, Kumar, Bobkov, Kane, Shao, Watson arXiv:0804.0863

- Moduli dominate the early universe and Decay to LSPs
- The gravitino mass and Moduli masses need to be $\gtrsim 10$ TeV for succesful BBN
- Gives the correct relic abundance !

Note: Probably generic in String Theory - SUGRA Lagrangian suggests at least one Moduli Mass \sim Gravitino Mass

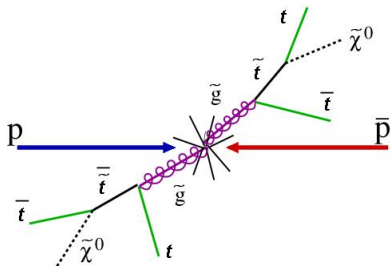
Non-Thermal LSP Acharya, Kumar, Bobkov, Kane, Shao, Watson arXiv:0804.0863

- Moduli dominate the early universe and Decay to LSPs
- The gravitino mass and Moduli masses need to be $\gtrsim 10$ TeV for succesful BBN
- Gives the correct relic abundance !

Note: Probably generic in String Theory - SUGRA Lagrangian suggests at least one Moduli Mass \sim Gravitino Mass

LHC Phenomonology Acharya, Grajek, Kane, Kuflik, Suruliz, Wang arXiv:0901.3367

- Rich LHC Phenomonology
- Gluinos are produced in pairs
- $\sigma \approx \text{pb}$
- Gluinos decay to 4 tops and Missing Energy
- Can be discovered early and easily at the LHC



Wino LSP

Question:

How robust is the prediction that the LSP is Wino?

Wino LSP

- The LSP is a combination of Bino, Wino and Higgsino Components

$$\chi = \epsilon_{\tilde{B}} \tilde{B} + \epsilon_{\tilde{W}} \tilde{W} + \epsilon_{\tilde{h}_u} \tilde{h}_u + \epsilon_{\tilde{h}_d} \tilde{h}_d$$

- Even small Higgsino components can have large effects on direct detection of dark matter.
- **We need a theory of the μ term**
- Why is the LSP stable?

Wino LSP

- The LSP is a combination of Bino, Wino and Higgsino Components

$$\chi = \epsilon_{\tilde{B}} \tilde{B} + \epsilon_{\tilde{W}} \tilde{W} + \epsilon_{\tilde{h}_u} \tilde{h}_u + \epsilon_{\tilde{h}_d} \tilde{h}_d$$

- Even small Higgsino components can have large effects on direct detection of dark matter.
- We need a theory of the μ term
- Why is the LSP stable?

Discrete Symmetries in M-Theory

- Witten (hep-ph/0201018) constructed a **geometric** discrete symmetry that can
 - forbid μ term $H_u H_d$ while allowing the Higgs triplet mass DD^c – Solved $D - T$ splitting.
 - forbid Dimension 4 and 5 proton decay
 - forbids R-parity violating operators
- **This symmetry must be broken since μ cannot be zero**
 - Moduli may be charged under this symmetry, but get vevs

$$\langle z \rangle \approx m_p + \theta^2 m_{1/2} m_p$$

- Will reintroduce dangerous couplings.

Discrete Symmetries in M-Theory

- Witten (hep-ph/0201018) constructed a **geometric** discrete symmetry that can
 - forbid μ term $H_u H_d$ while allowing the Higgs triplet mass DD^c – Solved $D - T$ splitting.
 - forbid Dimension 4 and 5 proton decay
 - forbids R-parity violating operators
- **This symmetry must be broken since μ cannot be zero**
 - Moduli may be charged under this symmetry, but get vevs

$$\langle z \rangle \approx m_p + \theta^2 m_{1/2} m_p$$

- Will reintroduce dangerous couplings.

Discrete Symmetries in M-Theory

- Witten (hep-ph/0201018) constructed a **geometric** discrete symmetry that can
 - forbid μ term $H_u H_d$ while allowing the Higgs triplet mass DD^c – Solved $D - T$ splitting.
 - forbid Dimension 4 and 5 proton decay
 - forbids R-parity violating operators
- This symmetry must be broken since μ cannot be zero
 - Moduli may be charged under this symmetry, but get vevs

$$\langle z \rangle \approx m_p + \theta^2 m_{1/2} m_p$$

- Will reintroduce dangerous couplings.

Discrete Symmetries in M-Theory

- Witten (hep-ph/0201018) constructed a **geometric** discrete symmetry that can
 - forbid μ term $H_u H_d$ while allowing the Higgs triplet mass DD^c – Solved $D - T$ splitting.
 - forbid Dimension 4 and 5 proton decay
 - forbids R-parity violating operators
- **This symmetry must be broken since μ cannot be zero**
 - Moduli may be charged under this symmetry, but get vevs

$$\langle z \rangle \approx m_p + \theta^2 m_{1/2} m_p$$

- Will reintroduce dangerous couplings.

Discrete Symmetries in M-Theory

- Witten (hep-ph/0201018) constructed a **geometric** discrete symmetry that can
 - forbid μ term $H_u H_d$ while allowing the Higgs triplet mass DD^c – Solved $D - T$ splitting.
 - forbid Dimension 4 and 5 proton decay
 - forbids R-parity violating operators
- **This symmetry must be broken since μ cannot be zero**
 - Moduli may be charged under this symmetry, but get vevs

$$\langle z \rangle \approx m_p + \theta^2 m_{1/2} m_p$$

- Will reintroduce dangerous couplings.

Moduli Induced R-Parity Problem

- Axionic shift symmetries

$$z_j \rightarrow z_j + a_j$$

will forbid superpotential couplings.

- But the μ term and R-parity violating couplings are allowed in the Kahler potential
 - $K \supset (Im z_j + i Im z_k) H_u H_d \rightarrow W \supset m_{1/2} H_u H_d$
 - $K \supset (Im z_j + i Im z_k) (M_{\bar{5}} h_5 + M_{10} M_{\bar{5}} M_{\bar{5}}) \rightarrow m_{1/2} M_{\bar{5}} h_5 + \frac{m_{1/2}}{m_p} M_{10} M_{\bar{5}} M_{\bar{5}}$

Moduli Induced R-Parity Problem

- Axionic shift symmetries

$$z_j \rightarrow z_j + a_j$$

will forbid superpotential couplings.

- But the μ term and R-parity violating couplings are allowed in the Kahler potential
 - $K \supset (Im z_j + i Im z_k) H_u H_d \rightarrow W \supset m_{1/2} H_u H_d$
 - $K \supset (Im z_j + i Im z_k) (M_{\bar{5}} h_5 + M_{10} M_{\bar{5}} M_{\bar{5}}) \rightarrow m_{1/2} M_{\bar{5}} h_5 + \frac{m_{1/2}}{m_p} M_{10} M_{\bar{5}} M_{\bar{5}}$

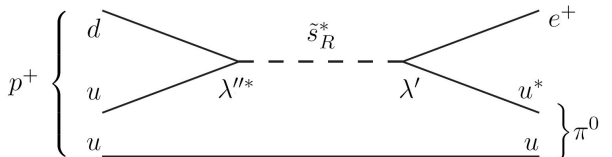
Proton Decay

- Baryon and lepton number are violated

$$W_R = \lambda' L Q d^c + \lambda'' u^c d^c d^c + \lambda''' L L e^c$$

$$\lambda' \sim \lambda'' \sim \lambda''' \sim \frac{m_{1/2}}{m_p}$$

- Dimension-4 proton decay is really Dimension-6



$$\approx \left(\frac{m_{1/2}}{m_p} \right)^2 \frac{1}{m_{3/2}^2} \quad \text{Experimentally Allowed}$$

LSP Lifetime

- The LSP will decay

$$\tau \approx \frac{10^{-17} \text{ sec}}{\lambda^2} \left(\frac{m_{\tilde{q}, \tilde{l}}}{\text{TeV}} \right)^4 \left(\frac{100 \text{ GeV}}{m_{\tilde{N}_1}} \right)^5$$

- For $m_{\tilde{q}, \tilde{l}} \sim 10 \text{ TeV}$, $m_{\tilde{N}_1} \sim 100 \text{ GeV}$, $\lambda \sim 10^{-15}$

$$\tau \sim 10^{17} \text{ sec} \sim t_0 \quad \text{Age of the Universe}$$

- Indirect detection requires

$$\tau \gtrsim 10^{26} \text{ sec}$$

LSP Lifetime

- The LSP will decay

$$\tau \approx \frac{10^{-17} \text{ sec}}{\lambda^2} \left(\frac{m_{\tilde{q}, \tilde{l}}}{\text{TeV}} \right)^4 \left(\frac{100 \text{ GeV}}{m_{\tilde{N}_1}} \right)^5$$

- For $m_{\tilde{q}, \tilde{l}} \sim 10 \text{ TeV}$, $m_{\tilde{N}_1} \sim 100 \text{ GeV}$, $\lambda \sim 10^{-15}$

$$\tau \sim 10^{17} \text{ sec} \sim t_0 \quad \text{Age of the Universe}$$

- Indirect detection requires

$$\tau \gtrsim 10^{26} \text{ sec}$$

R-Parity from GUTs

- Where is R -Parity?
- Try a local continuous $U(1)$ – Moduli are uncharged.
- Which $U(1)$ s?
 - Simple GUT Groups - Additional $U(1)$ s are difficult to understand in global embeddings
 - Chiral Theory
 - Anomaly free theory
 - E_6 , $SO(10)$ and $SU(5)$
- It is well known that these contain R -Parity

R-Parity from GUTs

- Where is R -Parity?
- Try a local continuous $U(1)$ – Moduli are uncharged.
- Which $U(1)$ s?
 - Simple GUT Groups - Additional $U(1)$ s are difficult to understand in global embeddings
 - Chiral Theory
 - Anomaly free theory
 - E_6 , $SO(10)$ and $SU(5)$
- It is well known that these contain R -Parity

R-Parity from GUTs

- Where is R -Parity?
- Try a local continuous $U(1)$ – Moduli are uncharged.
- Which $U(1)$ s?
 - Simple GUT Groups - Additional $U(1)$ s are difficult to understand in global embeddings
 - Chiral Theory
 - Anomaly free theory
 - E_6 , $SO(10)$ and $SU(5)$
- It is well known that these contain R -Parity

GUT Review Slansky

$$\begin{array}{c}
 E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi \quad SM \times U(1)_\chi \times U(1)_\eta \\
 \hline
 27 \left\{ \begin{array}{l}
 16_1 \left\{ \begin{array}{l}
 10_{-1} \left\{ \begin{array}{l}
 Q \\
 u^c \\
 e^c
 \end{array} \right. \\
 \bar{5}_3 \left\{ \begin{array}{l}
 d^c \\
 L
 \end{array} \right. \\
 1_{-5} \quad \nu^c
 \end{array} \right. \\
 10_{-2} \left\{ \begin{array}{l}
 5_2 \left\{ \begin{array}{l}
 D \\
 H_u
 \end{array} \right. \\
 \bar{5}_{-2} \left\{ \begin{array}{l}
 D^c \\
 H_d
 \end{array} \right.
 \end{array} \right. \\
 1_4 \quad 1_0 \quad S
 \end{array} \right.
 \end{array}
 \left| \begin{array}{l}
 (\mathbf{3}, \mathbf{2})_1 \quad -1 \quad 1 \\
 (\bar{\mathbf{3}}, \mathbf{1})_{-4} \quad -1 \quad 1 \\
 (\mathbf{1}, \mathbf{1})_6 \quad -1 \quad 1 \\
 (\bar{\mathbf{3}}, \mathbf{1})_2 \quad 3 \quad 1 \\
 (\mathbf{1}, \mathbf{2})_{-3} \quad 3 \quad 1 \\
 (\mathbf{1}, \mathbf{1})_0 \quad -5 \quad 1 \\
 (\mathbf{3}, \mathbf{1})_{-2} \quad 2 \quad -2 \\
 (\mathbf{1}, \mathbf{2})_3 \quad 2 \quad -2 \\
 (\bar{\mathbf{3}}, \mathbf{1})_2 \quad -2 \quad -2 \\
 (\mathbf{1}, \mathbf{2})_{-3} \quad -2 \quad -2 \\
 (\mathbf{1}, \mathbf{1})_0 \quad 0 \quad 4
 \end{array} \right.
 \end{array}$$

Wilson Line Breaking

- How will the symmetries be broken?

- By Wilson Lines
- $E_6, SO(10) \rightarrow SM \times U(1)_\chi (\times U(1)_\eta)$
 $U(1)_\chi$ cannot be broken by Wilson lines – Witten 85
- $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$
- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$
- $SU(6)$, Pati-Salam

Wilson Line Breaking

- How will the symmetries be broken?

- By Wilson Lines

- $E_6, SO(10) \rightarrow SM \times U(1)_X (\times U(1)_\eta)$

- $U(1)_X$ cannot be broken by Wilson lines – Witten 85

- $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_X (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$

- $SU(6),$ Pati-Salam

Wilson Line Breaking

- How will the symmetries be broken?
 - By Wilson Lines
 - $E_6, SO(10) \rightarrow SM \times U(1)_\chi (\times U(1)_\eta)$
 $U(1)_\chi$ cannot be broken by Wilson lines – Witten 85
 - $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$
 - $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$
 - $SU(6)$, Pati-Salam

Wilson Line Breaking

- How will the symmetries be broken?
 - By Wilson Lines
 - $E_6, SO(10) \rightarrow SM \times U(1)_\chi (\times U(1)_\eta)$
 $U(1)_\chi$ cannot be broken by Wilson lines – Witten 85
 - $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$
 - $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$
 - $SU(6)$, Pati-Salam

Wilson Line Breaking

- How will the symmetries be broken?
 - By Wilson Lines
 - $E_6, SO(10) \rightarrow SM \times U(1)_\chi (\times U(1)_\eta)$
 $U(1)_\chi$ cannot be broken by Wilson lines – Witten 85
 - $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$
 - $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$
 - $SU(6)$, Pati-Salam

Wilson Line Breaking

- How will the symmetries be broken?
 - By Wilson Lines
 - $E_6, SO(10) \rightarrow SM \times U(1)_\chi (\times U(1)_\eta)$
 $U(1)_\chi$ cannot be broken by Wilson lines – Witten 85
 - $E_6 \rightarrow SU(10) \times U(1)_\eta$
 $SO(10)$ broken by $16, \bar{16}$
 - $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi (\times U(1)_\eta)$
 $SU(5)$ broken by $10, \bar{10}$
 - $SU(6)$, Pati-Salam

$E_6, SO(10) \rightarrow SM \times U(1)_\chi$

- $E_6, SO(10) \rightarrow SM \times U(1)_\chi$
- $U(1)_\chi$ Can be broken by $\langle \bar{\nu}^c \rangle$
- Will break R-Parity
- How will a small vev be generated?
- Even if we could

$$K \supset (Im z_j + i Im z_k) \nu^c L H_u$$

$$\rightarrow W \supset m_{1/2} \frac{m_{3/2}}{m_p} L H_u \rightarrow W \supset \frac{m_{3/2}}{m_p} L L e^c$$

LSP decays as before

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	10 ₋₁	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1
			u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1
			e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1
		5 ₃	d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1
			L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1
	1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1	
	10 ₋₂	5 ₂	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
			H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
			D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
		5 ₋₂	H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
S			$(\mathbf{1}, \mathbf{1})_0$	0	4	
1 ₄	1 ₀					

$E_6, SO(10) \rightarrow SM \times U(1)_\chi$

- $E_6, SO(10) \rightarrow SM \times U(1)_\chi$
- $U(1)_\chi$ Can be broken by $\langle \bar{\nu}^c \rangle$
- Will break R-Parity
- How will a small vev be generated?
- Even if we could

$$K \supset (Im z_j + i Im z_k) \nu^c L H_u$$

$$\rightarrow W \supset m_{1/2} \frac{m_{3/2}}{m_p} L H_u \rightarrow W \supset \frac{m_{3/2}}{m_p} L L e^c$$

LSP decays as before

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	10 ₋₁	$\begin{cases} Q \\ u^c \\ e^c \end{cases}$	$\begin{cases} (\mathbf{3}, \mathbf{2})_1 \\ (\bar{\mathbf{3}}, \mathbf{1})_{-4} \\ (\mathbf{1}, \mathbf{1})_6 \end{cases}$	$\begin{pmatrix} -1 & 1 \\ -1 & 1 \\ -1 & 1 \end{pmatrix}$	
		$\bar{\mathbf{5}}_3$	$\begin{cases} d^c \\ L \end{cases}$	$\begin{cases} (\bar{\mathbf{3}}, \mathbf{1})_2 \\ (\mathbf{1}, \mathbf{2})_{-3} \end{cases}$	$\begin{pmatrix} 3 & 1 \\ 3 & 1 \end{pmatrix}$	
			1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	$\begin{pmatrix} -5 & 1 \end{pmatrix}$
		10 ₋₂	5 ₂	$\begin{cases} D \\ H_u \end{cases}$	$\begin{cases} (\mathbf{3}, \mathbf{1})_{-2} \\ (\mathbf{1}, \mathbf{2})_3 \end{cases}$	$\begin{pmatrix} 2 & -2 \\ 2 & -2 \end{pmatrix}$
			$\bar{\mathbf{5}}_{-2}$	$\begin{cases} D^c \\ H_d \end{cases}$	$\begin{cases} (\bar{\mathbf{3}}, \mathbf{1})_2 \\ (\mathbf{1}, \mathbf{2})_{-3} \end{cases}$	$\begin{pmatrix} -2 & -2 \\ -2 & -2 \end{pmatrix}$
	1 ₄			S	$(\mathbf{1}, \mathbf{1})_0$	$\begin{pmatrix} 0 & 4 \end{pmatrix}$

$E_6, SO(10) \rightarrow SM \times U(1)_\chi$

- $E_6, SO(10) \rightarrow SM \times U(1)_\chi$
- $U(1)_\chi$ Can be broken by $\langle \bar{\nu}^c \rangle$
- Will break R-Parity
- How will a small vev be generated?
- Even if we could

$$K \supset (Im z_j + i Im z_k) \nu^c L H_u$$

$$\rightarrow W \supset m_{1/2} \frac{m_{3/2}}{m_p} L H_u \rightarrow W \supset \frac{m_{3/2}}{m_p} L L e^c$$

LSP decays as before

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	10 ₋₁	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1
			u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1
			e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1
		$\bar{\mathbf{5}}_3$	d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1
			L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1
	1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1	
	10 ₋₂	5 ₂	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
			H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
			D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
		$\bar{\mathbf{5}}_{-2}$	H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
S			$(\mathbf{1}, \mathbf{1})_0$	0	4	
1 ₄	1 ₀					

$E_6, SO(10) \rightarrow SM \times U(1)_\chi$

- $E_6, SO(10) \rightarrow SM \times U(1)_\chi$
- $U(1)_\chi$ Can be broken by $\langle \bar{\nu}^c \rangle$
- Will break R-Parity
- How will a small vev be generated?
- Even if we could

$$K \supset (Im z_j + i Im z_k) \nu^c L H_u$$

$$\rightarrow W \supset m_{1/2} \frac{m_{3/2}}{m_p} L H_u \rightarrow W \supset \frac{m_{3/2}}{m_p} L L e^c$$

LSP decays as before

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$	$SM \times U(1)_\chi \times U(1)_\eta$
27	16_1 <ul style="list-style-type: none"> 10_{-1} <ul style="list-style-type: none"> Q $(\mathbf{3}, \mathbf{2})_1$ -1 1 u^c $(\bar{\mathbf{3}}, \mathbf{1})_{-4}$ -1 1 e^c $(\mathbf{1}, \mathbf{1})_6$ -1 1 $\bar{\mathbf{5}}_3$ <ul style="list-style-type: none"> d^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ 3 1 L $(\mathbf{1}, \mathbf{2})_{-3}$ 3 1 1_{-5} ν^c $(\mathbf{1}, \mathbf{1})_0$ -5 1
	10_{-2} <ul style="list-style-type: none"> 5_2 <ul style="list-style-type: none"> D $(\mathbf{3}, \mathbf{1})_{-2}$ 2 -2 H_u $(\mathbf{1}, \mathbf{2})_3$ 2 -2 $\bar{\mathbf{5}}_{-2}$ <ul style="list-style-type: none"> D^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ -2 -2 H_d $(\mathbf{1}, \mathbf{2})_{-3}$ -2 -2
	1_4 1_0 S $(\mathbf{1}, \mathbf{1})_0$ 0 4

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset H_{10} H_{10} h_5 + \bar{H}_{10} \bar{H}_{10} \bar{h}_5$ - Solves D-T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	Q	$(3, 2)_1$	-1	1	
		u^c	$(\bar{3}, 1)_{-4}$	-1	1	
		e^c	$(1, 1)_6$	-1	1	
		d^c	$(\bar{3}, 1)_2$	3	1	
		L	$(1, 2)_{-3}$	3	1	
	10 ₋₂	1 ₋₅	ν^c	$(1, 1)_0$	-5	1
		5 ₂	D	$(3, 1)_{-2}$	2	-2
			H_u	$(1, 2)_3$	2	-2
			D^c	$(\bar{3}, 1)_2$	-2	-2
		5 ₋₂	H_d	$(1, 2)_{-3}$	-2	-2
1 ₄	1 ₀		S	$(1, 1)_0$	0	4

$$K \supset (Im z_j + i Im z_k)(H_{10} \bar{H}_5 M_5) \rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p} \frac{m_{3/2}}{m_p} L H_u$$

- LSP decays faster than before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset H_{10} H_{10} h_5 + \bar{H}_{10} \bar{H}_{10} \bar{h}_5$ - Solves D-T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	Q	$(3, 2)_1$	-1	1	
		u^c	$(\bar{3}, 1)_{-4}$	-1	1	
		e^c	$(1, 1)_6$	-1	1	
		d^c	$(\bar{3}, 1)_2$	3	1	
		L	$(1, 2)_{-3}$	3	1	
	10 ₋₂	1 ₋₅	ν^c	$(1, 1)_0$	-5	1
		5 ₂	D	$(3, 1)_{-2}$	2	-2
			H_u	$(1, 2)_3$	2	-2
			D^c	$(\bar{3}, 1)_2$	-2	-2
		5 ₋₂	H_d	$(1, 2)_{-3}$	-2	-2
1 ₄	1 ₀		S	$(1, 1)_0$	0	4

$$K \supset (Im z_j + i Im z_k)(H_{10} \bar{H}_5 M_{\bar{5}}) \rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p} \frac{m_{3/2}}{m_p} L H_u$$

- LSP decays faster than before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset H_{10} H_{10} h_5 + \bar{H}_{10} \bar{H}_{10} \bar{h}_5$ - Solves D-T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	Q	$(3, 2)_1$	-1	1	
		u^c	$(\bar{3}, 1)_{-4}$	-1	1	
		e^c	$(1, 1)_6$	-1	1	
		d^c	$(\bar{3}, 1)_2$	3	1	
		L	$(1, 2)_{-3}$	3	1	
	10 ₋₂	1 ₋₅	ν^c	$(1, 1)_0$	-5	1
		5 ₂	D	$(3, 1)_{-2}$	2	-2
			H_u	$(1, 2)_3$	2	-2
			D^c	$(\bar{3}, 1)_2$	-2	-2
		5 ₋₂	H_d	$(1, 2)_{-3}$	-2	-2
1 ₄	1 ₀		S	$(1, 1)_0$	0	4

$$K \supset (Im z_j + i Im z_k)(H_{10} \bar{H}_5 M_{\bar{5}}) \rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p} \frac{m_{3/2}}{m_p} L H_u$$

- LSP decays faster than before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset H_{10} H_{10} h_5 + \bar{H}_{10} \bar{H}_{10} \bar{h}_5$ - Solves D-T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	Q	$(3, 2)_1$	-1	1	
		u^c	$(\bar{3}, 1)_{-4}$	-1	1	
		e^c	$(1, 1)_6$	-1	1	
		d^c	$(\bar{3}, 1)_2$	3	1	
		L	$(1, 2)_{-3}$	3	1	
	10 ₋₂	1 ₋₅	ν^c	$(1, 1)_0$	-5	1
		5 ₂	D	$(3, 1)_{-2}$	2	-2
			H_u	$(1, 2)_3$	2	-2
			D^c	$(\bar{3}, 1)_2$	-2	-2
		5 ₋₂	H_d	$(1, 2)_{-3}$	-2	-2
1 ₄	1 ₀		S	$(1, 1)_0$	0	4

$$K \supset (Im z_j + i Im z_k)(H_{10} \bar{H}_5 M_5) \rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p} \frac{m_{3/2}}{m_p} L H_u$$

- LSP decays faster than before

E_8

$$E_8 \rightarrow E_6 \times SU(3)$$

$$\lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_8 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

E_6	$U(1)_3$	$U(1)_8$
27	1	1
27	-1	1
27	0	-2

$$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi \quad SM \times U(1)_\chi \times U(1)_\eta$$

27	16_1	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1	
		u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1	
		e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1	
		d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1	
		L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1	
	10_{-2}	1_{-5}	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1
		5_2	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
			H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
			D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
			H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
1_4	1_0	S	$(\mathbf{1}, \mathbf{1})_0$	0	4	

Discrete symmetry revisited

- Can a discrete symmetry be broken to allow the μ -term while preserving R -parity.
- Witten's construction

Field	\mathcal{Z}_n
M_{10}	$e^{i\sigma}$
$M_{\bar{5}}$	$e^{i\tau}$
H_5	D $e^{i\alpha}$
	H_u $e^{i\alpha}$
	D^c $e^{i\gamma}$
$H_{\bar{5}}$	H_d $e^{i\delta}$

Discrete symmetry revisited

- Can a discrete symmetry be broken to allow the μ -term while preserving R -parity.
- Witten's construction

Field	\mathcal{Z}_n
M_{10}	$e^{i\sigma}$
$M_{\bar{5}}$	$e^{i\tau}$
H_5	D H_u
	$e^{i\alpha}$
	H_u
	$e^{i\alpha}$
	D^c
	$e^{i\gamma}$
$H_{\bar{5}}$	H_d
	$e^{i\delta}$

Discrete symmetry revisited

- Allow Yukawa couplings, Majorana neutrino masses, and the Higgs triplet masses

	Coupling	Constraint
Up Yukawa Coupling	$M_{10} M_{10} H_U$	$2\sigma + \alpha = 2\pi$
Down Yukawa Coupling	$M_{10} M_{\bar{5}} H_d$	$\sigma + \tau + \delta = 2\pi$
Majorana Neutrino Masses	$H_d H_d M_{\bar{5}} M_{\bar{5}}$	$2\alpha + 2\tau = 2\pi$
Triplet Masses	DD^c	$\alpha + \gamma = 2\pi.$

Discrete symmetry revisited

- Find the solution

$$\alpha = -2\sigma, \gamma = 2\sigma, \delta = -3\sigma + \pi, \tau = 2\sigma + \pi, \sigma = \sigma$$

- Then forbid μ -term and R-parity violation

	Coupling	Constraint
μ -term	$H_d H_u$	$-5\sigma + \pi \neq 2\pi$
R-Parity	$M_{10} M_{10} M_{\bar{5}}$	$5\sigma \neq 2\pi$
	$M_{\bar{5}} H_u$	$\pi \neq 2\pi$

Discrete symmetry revisited

- Can this symmetry be broken and preserve R-parity?
- Yes
- Example $N = 6, \sigma = 2\pi/6$

	Coupling	Charge	Z_6
μ - term	$H_d H_u$	$-5\sigma + \pi$	$e^{i2\pi\frac{4}{6}}$
R-Parity	$M_{10} M_{\bar{5}} M_{\bar{5}}$	5σ	$2e^{i2\pi\frac{5}{6}}$
	$M_{\bar{5}} H_u$	π	$e^{i2\pi\frac{3}{6}}$

- Vevs of moduli transforming as $z \rightarrow e^{i2\pi\frac{2}{6}} z$ preserve R-Parity
- Why do we live in this vacuum?

Discrete symmetry revisited

- Can this symmetry be broken and preserve R-parity?
- Yes
- Example $N = 6, \sigma = 2\pi/6$

	Coupling	Charge	Z_6
μ - term	$H_d H_u$	$-5\sigma + \pi$	$e^{i2\pi\frac{4}{6}}$
R-Parity	$M_{10} M_{\bar{5}} M_{\bar{5}}$	5σ	$2e^{i2\pi\frac{5}{6}}$
	$M_{\bar{5}} H_u$	π	$e^{i2\pi\frac{3}{6}}$

- Vevs of moduli transforming as $z \rightarrow e^{i2\pi\frac{2}{6}} z$ preserve R-Parity
- Why do we live in this vacuum?

Summary

- M-Theory is awesome.
- R-parity is non-generic.
- Geometric symmetries may or may not be enough.
- Simple GUT models in M-Theory will not provide R-parity.

- Outlook
 - Look for a stable LSP: Non-GUT $U(1)$ s, moduli vacuum, Monodromies ...

E_8

$$E_8 \rightarrow E_6 \times SU(3)$$

$$\lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_8 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

E_6	$U(1)_3$	$U(1)_8$
27	1	1
27	-1	1
27	0	-2

$$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi \quad SM \times U(1)_\chi \times U(1)_\eta$$

27	16_1	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1	
		u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1	
		e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1	
		d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1	
		L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1	
	10_{-2}	1_{-5}	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1
		5_2	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
			H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
			D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
			H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
1_4	1_0	S	$(\mathbf{1}, \mathbf{1})_0$	0	4	

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset HHh + \bar{H}\bar{H}\bar{h}$ - Solves D/T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$	$SM \times U(1)_\chi \times U(1)_\eta$	
27	16_1	Q $(\mathbf{3}, \mathbf{2})_1$ -1 1 u^c $(\bar{\mathbf{3}}, \mathbf{1})_{-4}$ -1 1 e^c $(\mathbf{1}, \mathbf{1})_6$ -1 1 d^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ 3 1 L $(\mathbf{1}, \mathbf{2})_{-3}$ 3 1 ν^c $(\mathbf{1}, \mathbf{1})_0$ -5 1
	10_{-2}	D $(\mathbf{3}, \mathbf{1})_{-2}$ 2 -2 H_u $(\mathbf{1}, \mathbf{2})_3$ 2 -2 D^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ -2 -2 H_d $(\mathbf{1}, \mathbf{2})_{-3}$ -2 -2
	1_4	1_0 S $(\mathbf{1}, \mathbf{1})_0$ 0 4

$$K \supset (Im z_j + i Im z_k)(H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p^2} M_{10} M_{10} M_{\bar{5}}$$

LSP decays as before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset HHh + \bar{H}\bar{H}\bar{h}$ - Solves D/T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$	$SM \times U(1)_\chi \times U(1)_\eta$	
27	16_1	Q $(\mathbf{3}, \mathbf{2})_1$ -1 1 u^c $(\bar{\mathbf{3}}, \mathbf{1})_{-4}$ -1 1 e^c $(\mathbf{1}, \mathbf{1})_6$ -1 1 d^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ 3 1 L $(\mathbf{1}, \mathbf{2})_{-3}$ 3 1 ν^c $(\mathbf{1}, \mathbf{1})_0$ -5 1
	10_{-2}	D $(\mathbf{3}, \mathbf{1})_{-2}$ 2 -2 H_u $(\mathbf{1}, \mathbf{2})_3$ 2 -2 D^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ -2 -2 H_d $(\mathbf{1}, \mathbf{2})_{-3}$ -2 -2
	1_4	1_0 S $(\mathbf{1}, \mathbf{1})_0$ 0 4

$$K \supset (Im z_j + i Im z_k)(H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p^2} M_{10} M_{10} M_{\bar{5}}$$

LSP decays as before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset HHh + \bar{H}\bar{H}\bar{h}$ – Solves D/T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$	$SM \times U(1)_\chi \times U(1)_\eta$	
27	16_1	$\begin{cases} Q & (\mathbf{3}, \mathbf{2})_1 & -1 & 1 \\ u^c & (\bar{\mathbf{3}}, \mathbf{1})_{-4} & -1 & 1 \\ e^c & (\mathbf{1}, \mathbf{1})_6 & -1 & 1 \\ d^c & (\bar{\mathbf{3}}, \mathbf{1})_2 & 3 & 1 \\ L & (\mathbf{1}, \mathbf{2})_{-3} & 3 & 1 \\ \nu^c & (\mathbf{1}, \mathbf{1})_0 & -5 & 1 \end{cases}$
	10_{-2}	$\begin{cases} D & (\mathbf{3}, \mathbf{1})_{-2} & 2 & -2 \\ H_u & (\mathbf{1}, \mathbf{2})_3 & 2 & -2 \\ D^c & (\bar{\mathbf{3}}, \mathbf{1})_2 & -2 & -2 \\ H_d & (\mathbf{1}, \mathbf{2})_{-3} & -2 & -2 \end{cases}$
	1_4	$1_0 \quad S \quad (\mathbf{1}, \mathbf{1})_0 \quad 0 \quad 4$

$$K \supset (Im z_j + i Im z_k)(H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p^2} M_{10} M_{10} M_{\bar{5}}$$

LSP decays as before

$E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$ - Flipped $SU(5)$

- $E_6, SO(10) \rightarrow SU(5) \times U(1)_\chi$
- Can be broken by
 $H = \langle 10_{-1} \rangle, \bar{H} = \langle \bar{10}_1 \rangle$
- $W \supset HHh + \bar{H}\bar{H}\bar{h}$ – Solves D/T Splitting
- Will break R-Parity
- Will need GUT scale vev
- Even if we could

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$				
27	16 ₁	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1	
		u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1	
		e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1	
		d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1	
		L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1	
	10 ₋₂	1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1
		5 ₂	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
			H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
			D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
		5 ₋₂	H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
1 ₄	1 ₀		S	$(\mathbf{1}, \mathbf{1})_0$	0	4

$$K \supset (Im z_j + i Im z_k)(H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT}}{m_p^2} M_{10} M_{10} M_{\bar{5}}$$

LSP decays as before

$E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$

- $E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$
- $U(1)_\eta$ Can be broken by $\langle S \rangle, \langle \bar{S} \rangle$
- Will break R-Parity

$$K \supset (Im z_j + i Im z_k) (\langle \bar{S} \rangle H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT} \langle \bar{S} \rangle}{m_p^3} M_{10} M_{10} M_{\bar{5}}$$

LSP is stable enough for $\langle \bar{S} \rangle \sim \frac{m_{3/2}}{m_p}$

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$			
16 ₁	10 ₋₁	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1
		u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1
	$\bar{\mathbf{5}}_3$	e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1
		d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1
		L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1
1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1	
10 ₋₂	5 ₂	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
		H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
	$\bar{\mathbf{5}}_{-2}$	D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
		H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
		S	$(\mathbf{1}, \mathbf{1})_0$	0	-4
1 ₄	1 ₀				

$E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$

- $E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$
- $U(1)_\eta$ Can be broken by $\langle S \rangle, \langle \bar{S} \rangle$
- Will break R-Parity

$$K \supset (Im z_j + i Im z_k) (\langle \bar{S} \rangle H_{10} M_{10} M_{10} M_{\bar{5}})$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT} \langle \bar{S} \rangle}{m_p^3} M_{10} M_{10} M_{\bar{5}}$$

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$			
16 ₁	10 ₋₁	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1
		u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1
	$\bar{\mathbf{5}}_3$	e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1
		d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1
		L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1
1 ₋₅	ν^c	$(\mathbf{1}, \mathbf{1})_0$	-5	1	
10 ₋₂	5 ₂	D	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
		H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
	$\bar{\mathbf{5}}_{-2}$	D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
		H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
1 ₄	1 ₀	S	$(\mathbf{1}, \mathbf{1})_0$	0	-4

LSP is stable enough for $\langle \bar{S} \rangle \sim \frac{m_{3/2}}{m_p}$

$E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$

- $E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$
- $U(1)_\eta$ Can be broken by $\langle S \rangle, \langle \bar{S} \rangle$
- Will break R-Parity

$$K \supset (Im z_j + i Im z_k) (\langle \bar{S} \rangle H_{10} M_{10} M_{10} M_{\bar{5}}) \quad 27$$

$$\rightarrow W \supset \frac{m_{1/2} m_{GUT} \langle \bar{S} \rangle}{m_p^3} M_{10} M_{10} M_{\bar{5}}$$

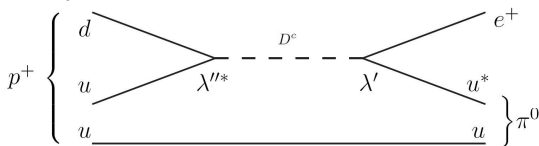
$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$	$SM \times U(1)_\chi \times U(1)_\eta$
10_{-1}	Q $(\mathbf{3}, \mathbf{2})_1$ -1 1
	u^c $(\bar{\mathbf{3}}, \mathbf{1})_{-4}$ -1 1
	e^c $(\mathbf{1}, \mathbf{1})_6$ -1 1
16_1	d^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ 3 1
	L $(\mathbf{1}, \mathbf{2})_{-3}$ 3 1
	ν^c $(\mathbf{1}, \mathbf{1})_0$ -5 1
10_{-2}	D $(\mathbf{3}, \mathbf{1})_{-2}$ 2 -2
	H_u $(\mathbf{1}, \mathbf{2})_3$ 2 -2
	D^c $(\bar{\mathbf{3}}, \mathbf{1})_2$ -2 -2
	H_d $(\mathbf{1}, \mathbf{2})_{-3}$ -2 -2
1_4	1_0 S $(\mathbf{1}, \mathbf{1})_0$ 0 -4

LSP is stable enough for $\langle \bar{S} \rangle \sim \frac{m_{3/2}}{m_p}$

$E_6 \rightarrow SU(5) \times U(1)_\chi \times U(1)_\eta$

- **Doublet-Triplet Splitting and proton decay is spoiled**
 $\bar{H}\bar{H}\bar{h}$ is forbidden

- Details are complicated – proton will decay



$$\approx \gamma^2 \frac{1}{m_{3/2}^2}$$

$E_6 \rightarrow SO(10)_\eta \rightarrow SU(5)_\chi$		$SM \times U(1)_\chi \times U(1)_\eta$		
10_{-1}	Q	$(\mathbf{3}, \mathbf{2})_1$	-1	1
	u^c	$(\bar{\mathbf{3}}, \mathbf{1})_{-4}$	-1	1
	e^c	$(\mathbf{1}, \mathbf{1})_6$	-1	1
	d^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	3	1
	L	$(\mathbf{1}, \mathbf{2})_{-3}$	3	1
16_1	$\bar{\mathbf{5}}_3$	$(\mathbf{3}, \mathbf{1})_2$	3	1
	1_{-5}	$(\mathbf{1}, \mathbf{1})_0$	-5	1
10_{-2}	5_2	$(\mathbf{3}, \mathbf{1})_{-2}$	2	-2
	H_u	$(\mathbf{1}, \mathbf{2})_3$	2	-2
	D^c	$(\bar{\mathbf{3}}, \mathbf{1})_2$	-2	-2
$\bar{\mathbf{5}}_{-2}$	H_d	$(\mathbf{1}, \mathbf{2})_{-3}$	-2	-2
	1_4	$(\mathbf{1}, \mathbf{1})_0$	0	4
	1_0	S	0	4