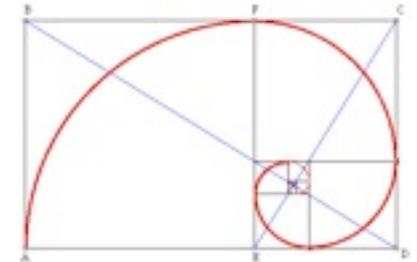
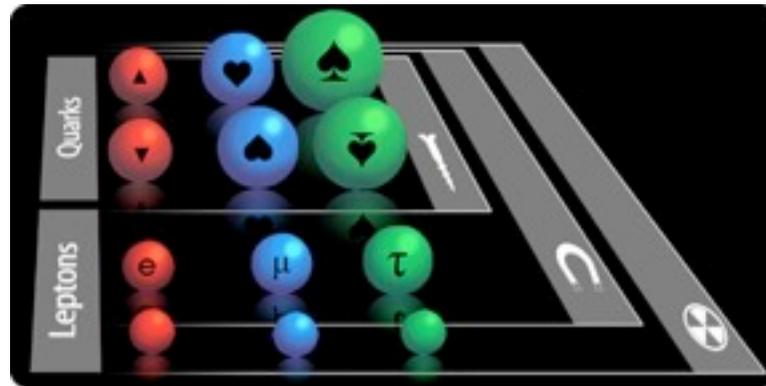
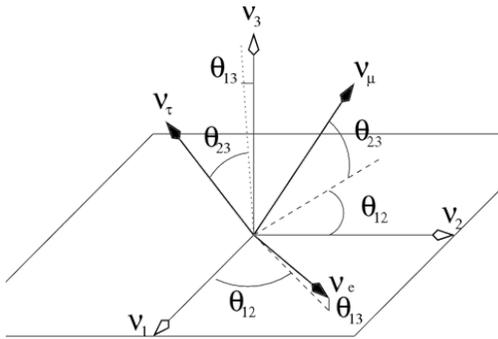


# Perspectives on Neutrino Mass Models



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# The Big Picture -- Many Questions Remain

- How many light neutrinos?

Anomalies: LSND, MiniBooNE, Gallium, Reactor  
eV-scale sterile neutrinos? But tension still with all oscillation data  
see e.g. Kopp et al., [1303.3011](#), Abazajian et al. [1204.5379](#) (white paper),...

Thus: restrict here to 3-family neutrino models only

$$\text{SM} \longrightarrow \nu\text{SM}$$

- Still, many questions:

Nature of neutrino mass suppression? Majorana? Dirac?  
Mass hierarchy? **Lepton mixing angle pattern?** CP violation?  
**Implications for BSM paradigms?** Connections to other NP?

# The Flavor Puzzle, Rejuvenated

Flavor puzzle of SM is notoriously difficult...

Still difficult in  $\nu$ SM, but more interesting --

One primary reason: two large mixing angles!

$$\theta_{23} \simeq 45^\circ \pm 5^\circ \quad \theta_{12} \simeq 34^\circ \pm 1^\circ$$

3-family models: handwave a bit (in diagonal charged lepton basis)

3	small angles	→	~ diagonal $\mathcal{M}_\nu$	} (“easy”)
1	large, 2 small	→	~ Rank $\mathcal{M}_\nu < 3$	
3	large angles	→	anarchical $\mathcal{M}_\nu$	} (“harder”)
2	large, 1 small	→	fine-tuning, non-Abelian	

# Anarchy vs. Structure

→ The question: is  $\theta_{13}$  large or small?

$$\theta_{13} \simeq 9^\circ \pm 1^\circ$$

Post-March 2012 case for anarchy: [de Gouvea and Murayama, 1204.1249](#)

some recent explicit realizations: [Bai and Torroba, 1210.2394](#)  
[Altarelli et al., 1207.0587,...](#)

Focus here on structure (symmetry):

**Paradigm:** discrete non-Abelian family symmetry  
(subgroup of  $SO(3)$  or  $SU(3)$ , broken  
to some appropriate coset space)

Main issue/challenge: many theoretical starting points

# Role of Small (Cabibbo-sized?) Corrections

Quark sector:

$$\mathcal{U}_{\text{CKM}} \sim 1 + O(\lambda_C)$$

Cabibbo angle  $\lambda_C$  (or some power) as a flavor expansion parameter

Lepton sector:

$$\mathcal{U}_{\text{MNSP}} \sim \mathcal{W} + O(\lambda')$$

“bare” mixing angles  $(\theta_{12}^0, \theta_{13}^0, \theta_{23}^0)$       perturbations

choice of bare mixing angles? depends on perturbations

Unification paradigm (broad sense): useful to take

$$\lambda' = \lambda_C$$

ideas of quark-lepton complementarity and “Cabibbo haze”

Raidal '04, Minakata+Smirnov, '04, many others...

Ramond and collaborators (including yours truly...)

Long before 2012, it was conjectured that  $\theta_{13}$  is a Cabibbo effect

$$\theta_{13} \sim \frac{\lambda_C}{\sqrt{2}} \sim \lambda_C \cos \theta_{23}^0 \quad \text{Ramond '03, '04,...}$$

(general idea often called “charged lepton corrections”)  $\mathcal{U}_{\text{MNSP}} \sim \mathcal{U}_{\text{CKM}}^\dagger \mathcal{W}$

good fit to data! but nontrivial to implement...

one reason: now  $\sim \lambda_C$  corrections floating around

# Family Symmetry Model (Broad) Taxonomy

Pre-March 2012      most models:  $\theta_{23}^0 = 45^\circ$      $\theta_{13}^0 = 0^\circ$

Choices for “bare” solar angle  $\theta_{12}^0$ :

(1) within  $\sim \lambda_C^2$  of exp:

**tri-bimaximal** mixing

“the beautiful matrix  
with the ugly name”

$$\tan \theta_{12}^0 = \frac{1}{\sqrt{2}} \quad \theta_{12}^0 = 35.26^\circ$$

Harrison, Perkins, Scott '02

(100s of papers. Key players include  
Ma, Chen et al., Altarelli et al.,...)

others, such as **golden ratio** mixing  $\phi = (1 + \sqrt{5})/2$

$$\tan \theta_{12} = \phi^{-1} \quad \theta_{12} = 31.72^\circ \quad \text{or} \quad \cos \theta_{12} = \frac{\phi}{2} \quad \theta_{12} = 36^\circ$$

Ramond, Kajiyama et al.,  
LE+Stuart (+Ding), Feruglio et al.,...

Rodejohann et al.,...

(2) within  $\sim \lambda_C$  of exp:

**bimaximal** mixing

$$\tan \theta_{12}^0 = 1$$

(quark-lepton  
complementarity)

## Post-March 2012

- **Keep**  $\theta_{23}^0 = 45^\circ$   $\theta_{13}^0 = 0^\circ$

(1) within  $\sim \lambda_C^2$  of exp:

need to **control corrections** to ensure other angles not shifted out of experimentally allowed ranges

**TBM (or other mixing scenarios)** as leading order framework  
original scenarios need modifying; this however is doable  
(CP phases often play a significant role)

Lin 0905.3534 -- anticipated issue and proposed a solution  
See also e.g. Ma '12, King+Stuart et al. '12, other talks here,...

(2) within  $\sim \lambda_C$  of exp: resurgence?

- **Modify**  $\theta_{23}^0 = 45^\circ$   $\theta_{13}^0 = 0^\circ$

$\theta_{13}$  numerology

drop maximal  $\theta_{23}$  (some hints in data)?

# Some final thoughts...

- **Exciting times!** Lots of ideas, lots of room for more
- issue of **connection to observations** and **testability**
  - requires NP!
    - but NP generically comes with its own flavor puzzle
    - how to disentangle?
- role of **CP phases** -- new focus
  - connection to **leptogenesis** highly model dependent
  - better **soundbite/motivation** for exp program??