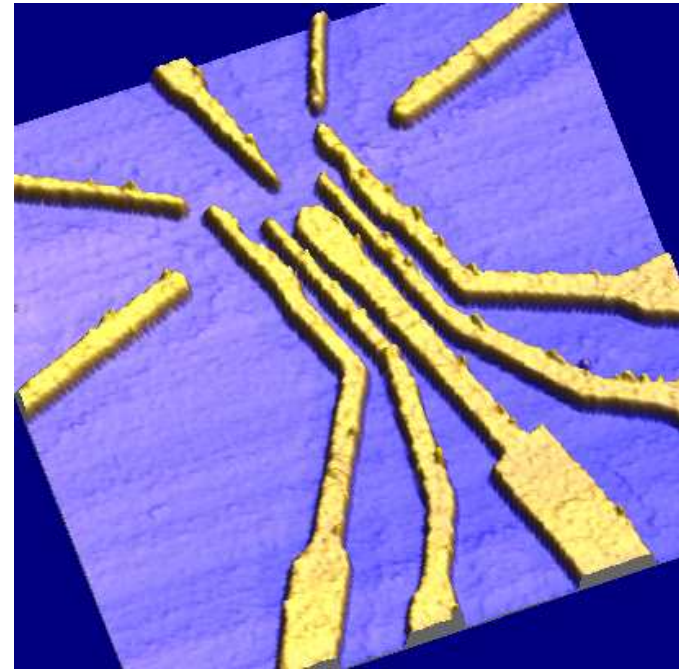
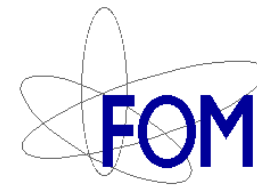


# Control of electron and nuclear spins in GaAs quantum dots

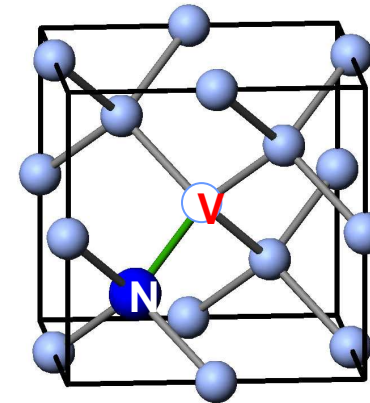
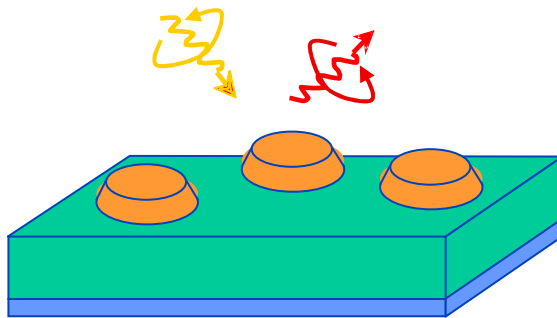
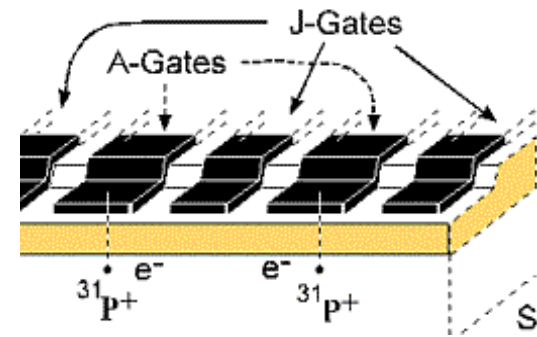
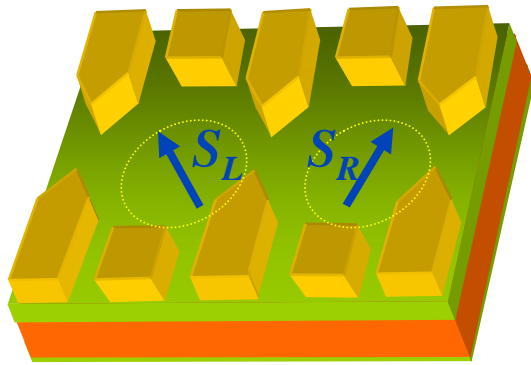
KITP workshop on  
Quantum Information Science  
Santa Barbara, CA  
1 Dec 2009



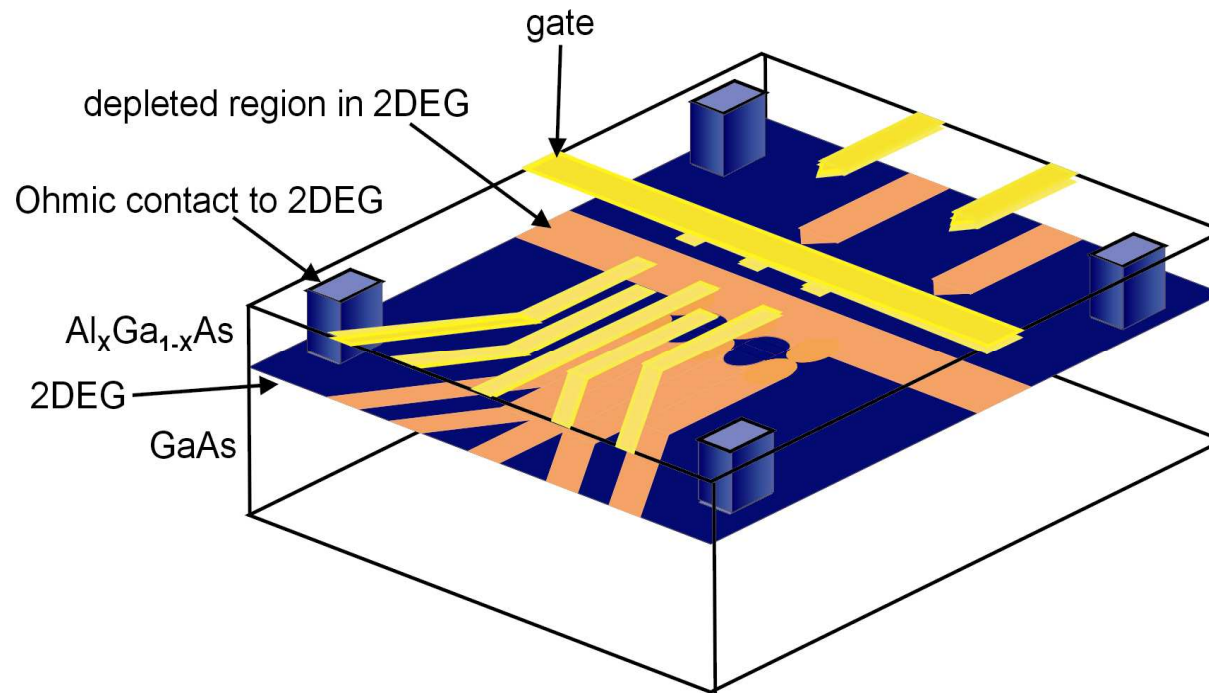
Lieven Vandersypen



# Controlling *single spins*



# A well-controlled and fully tunable quantum dot system

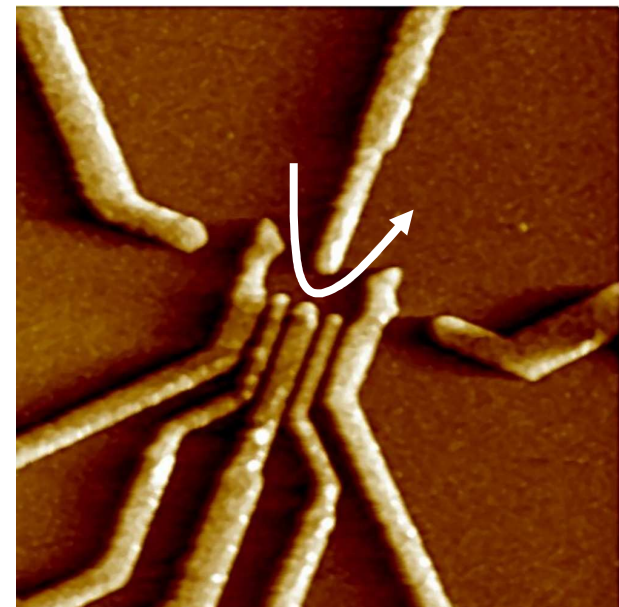


## Confinement

- Discrete # charges
- Quantized orbitals

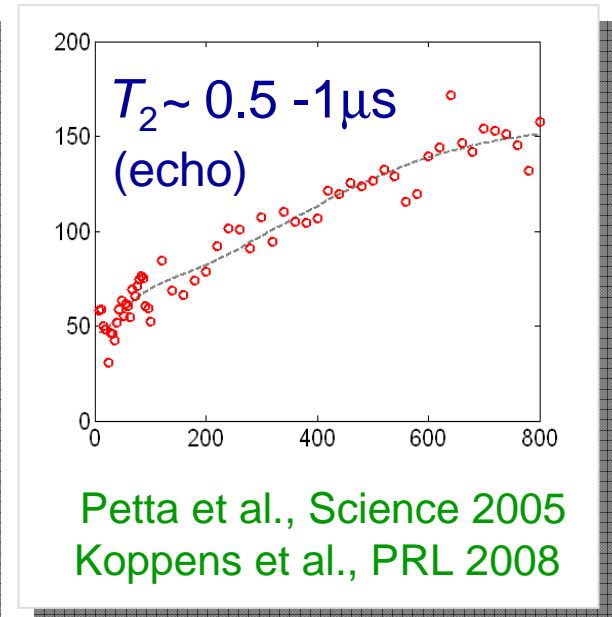
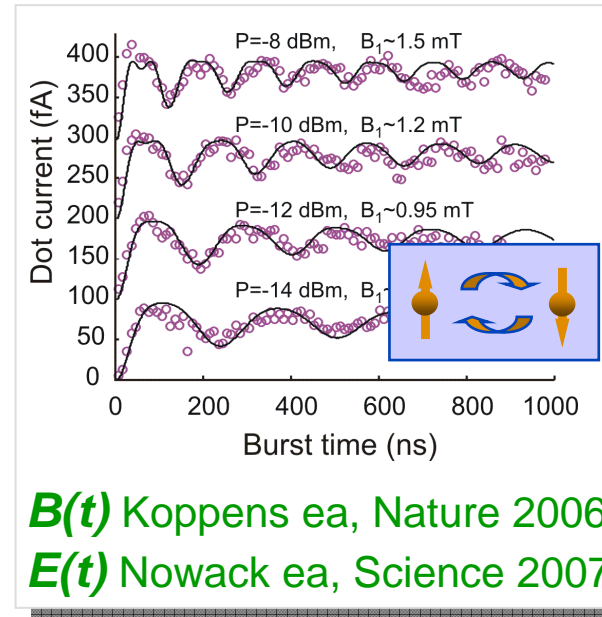
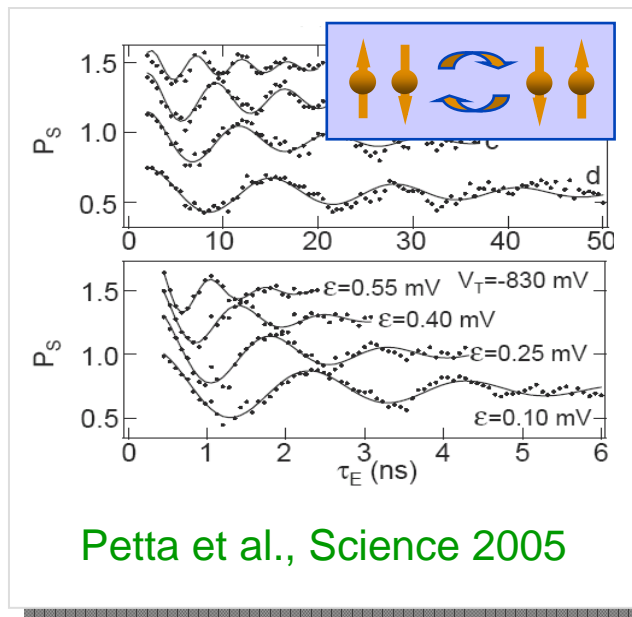
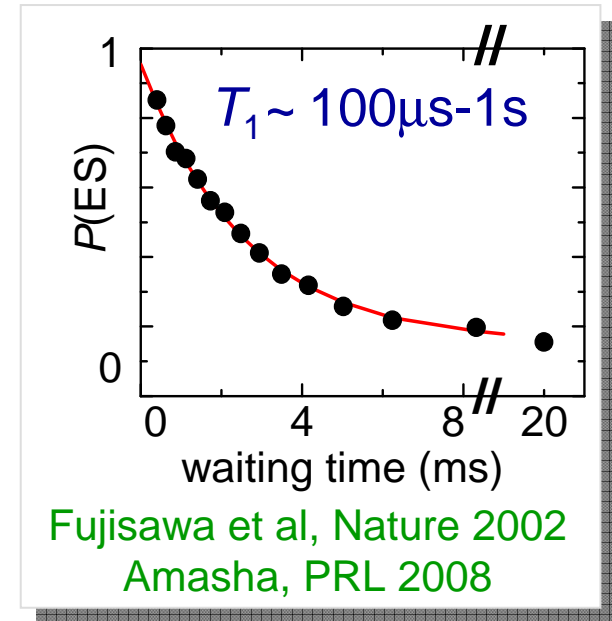
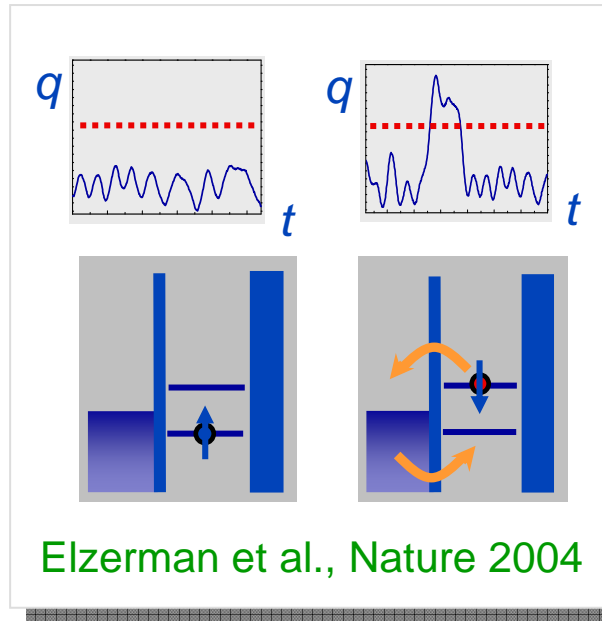
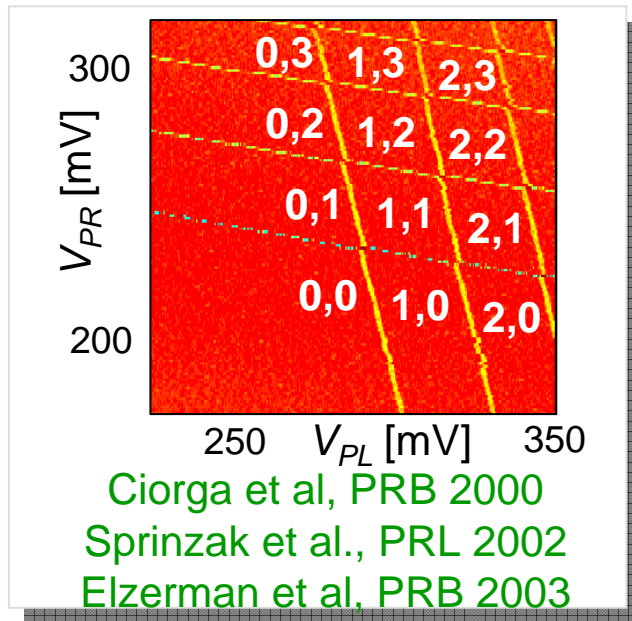
## Electrical control and detection

- Tunable # of electrons
- Tunable tunnel barriers
- Electrical contacts



# Single-spin qubits in GaAs dots

See also *Hanson et al, Rev. Mod. Phys. 2007*

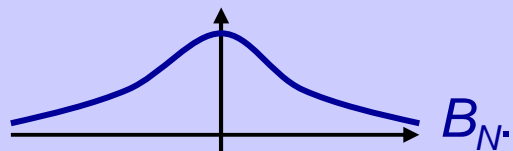


# Electron spin dephasing in the random nuclear field

$$\mathcal{H} = g\mu_B \vec{S} \cdot \vec{B} + \vec{S} \cdot \sum_i A_i \vec{I}_i$$

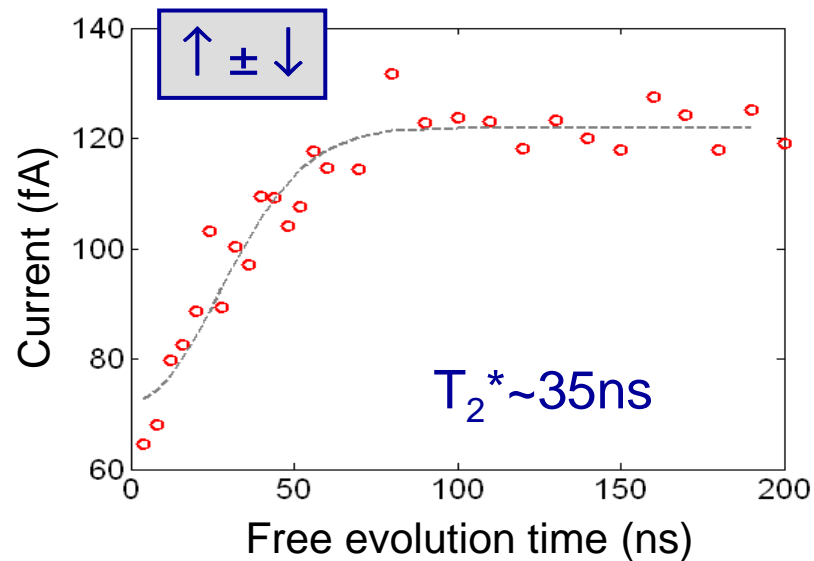
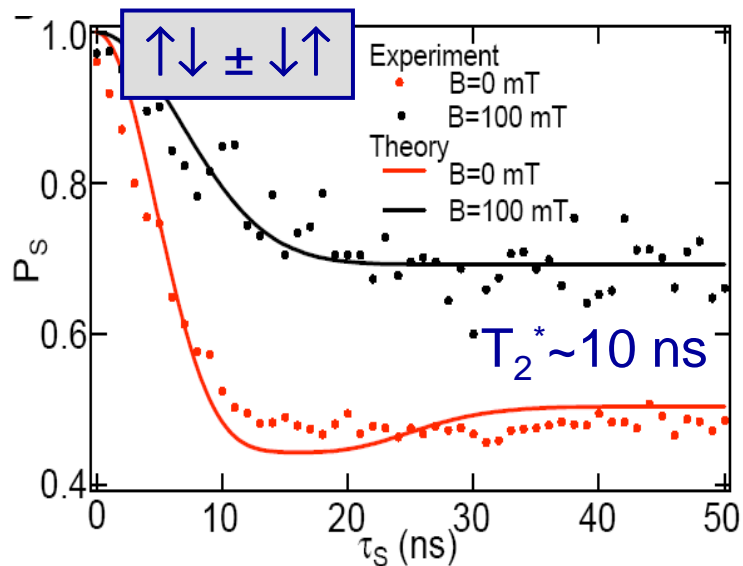
Overhauser field  $B_N$

$B_N$  is random and unknown



~ 20 ns dephasing time

Merkulov, Efros, Rosen, PRB 2002, Khaetskii, Loss, Glazman, PRL 2002

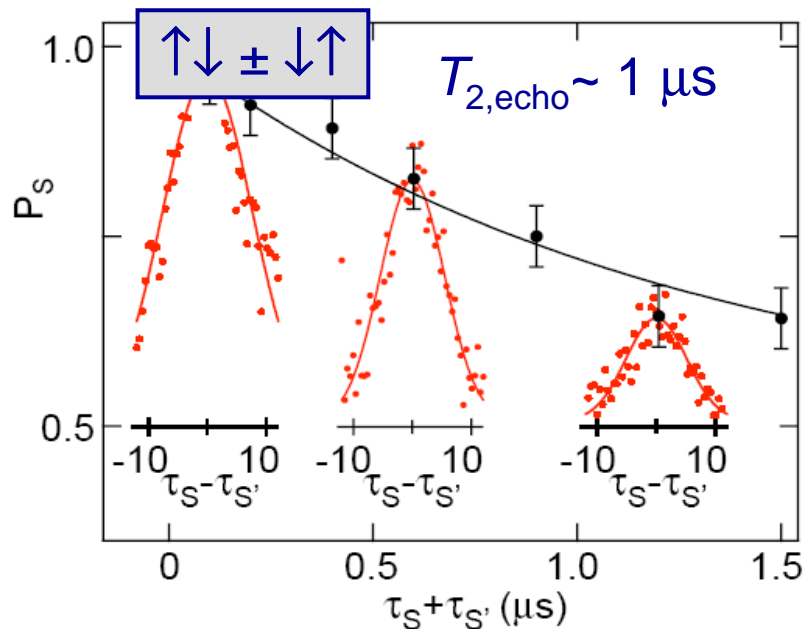


# Electron spin decoherence due to random nuclear spin dynamics

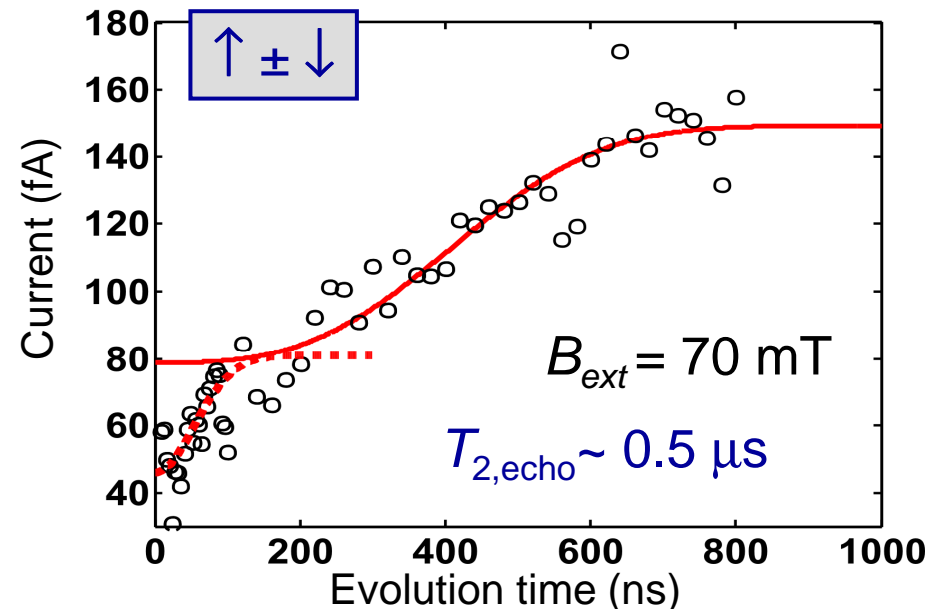
$B_N$  fluctuates due to (1) dipole-dipole  
(2) hyperfine-mediated

$B_N$  evolves slowly on the timescale of the electron spin dynamics  
 $\Rightarrow T_{2,\text{echo}} \sim 1\text{-}100 \mu\text{s}$

Coish & Loss PRB 2004, Witzel & Das Sarma PRB 2006, PRL 2007,  
 Yao, Liu, Sham, PRB 2006, ...

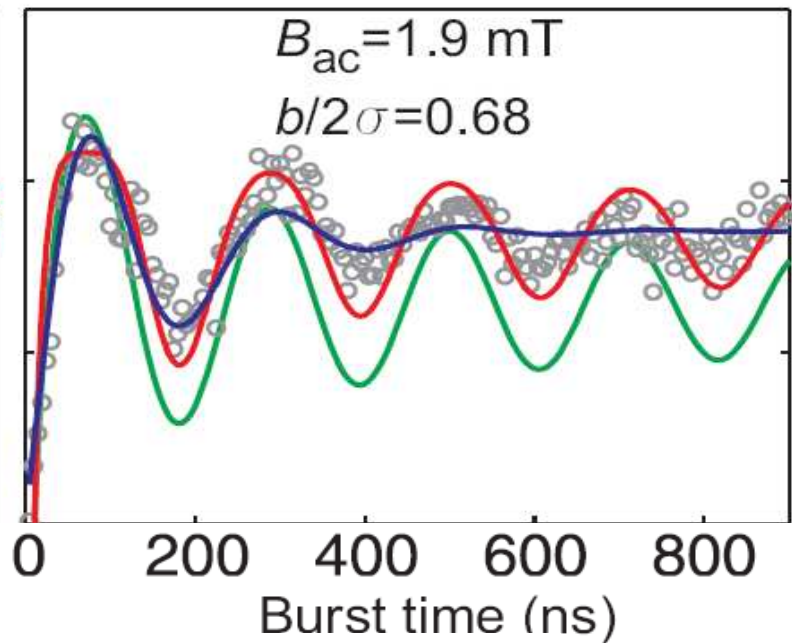
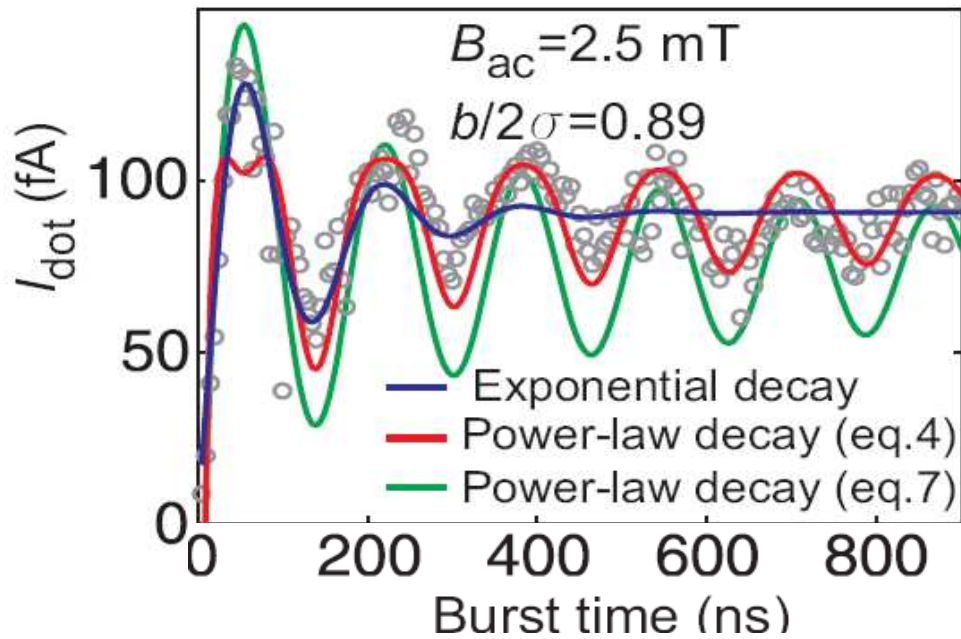
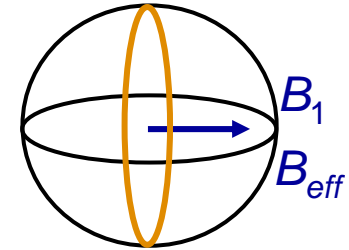
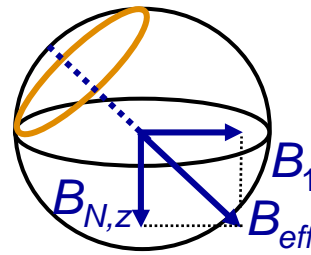
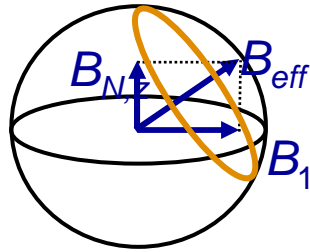
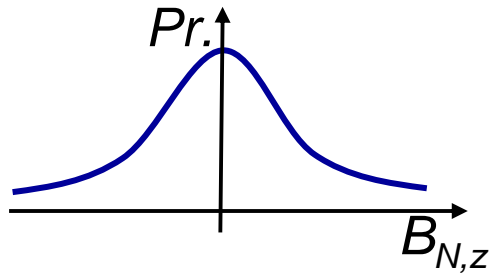


Petta *et al*, Science 2005



Koppens, Nowack, LMKV, PRL 2008

# Decay of driven oscillations

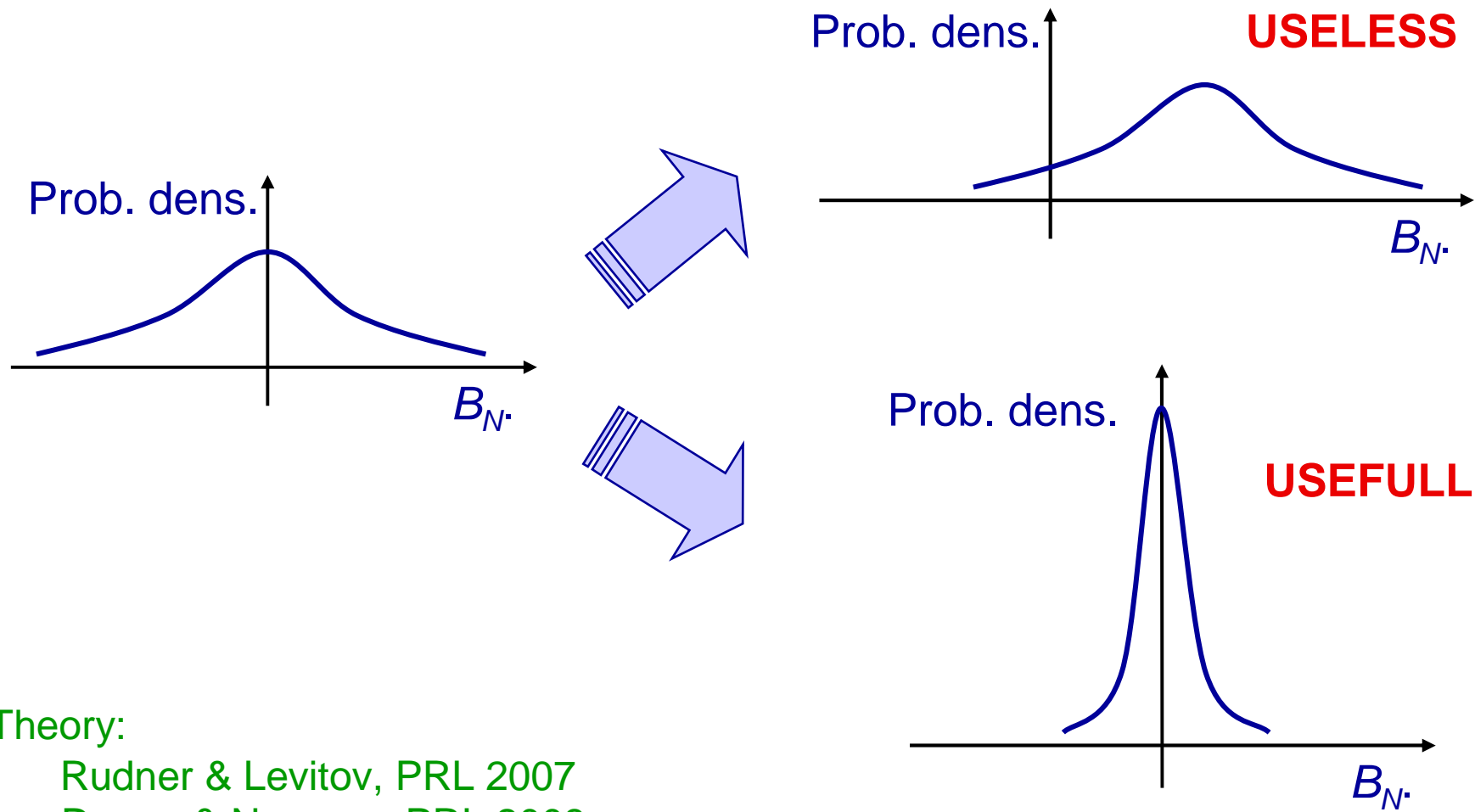


$$P_{\uparrow}(t) \sim \frac{1}{2} + C + \sqrt{\frac{b}{8\sigma^2 t}} \cos\left(\frac{b}{2}t + \frac{\pi}{4}\right) + \mathcal{O}\left(\frac{1}{t^{3/2}}\right)$$

Power-law decay

Phase shift

# Can we reduce dephasing by nuclear spins?

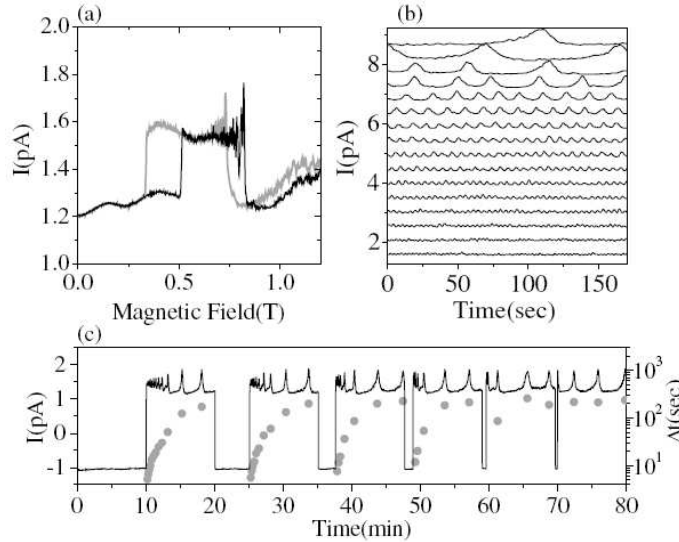


Theory:

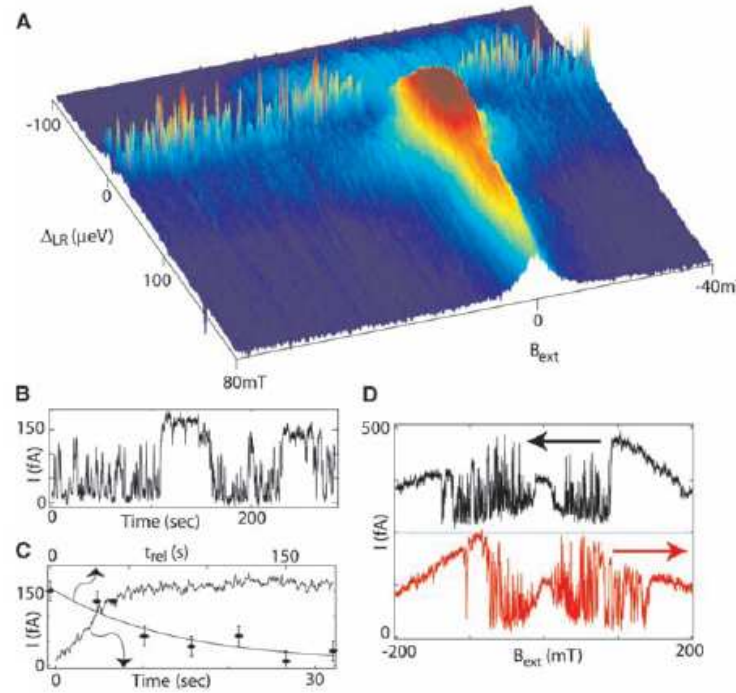
Rudner & Levitov, PRL 2007  
Danon & Nazarov, PRL 2008



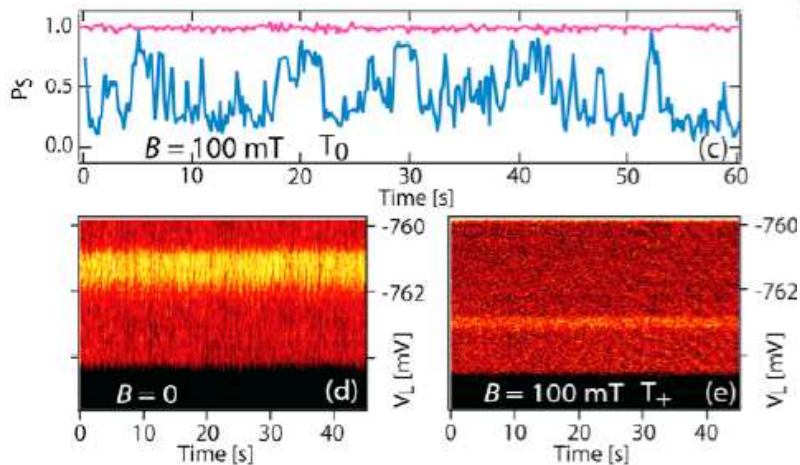
# Dynamic nuclear spin polarization from electron-nuclear feedback



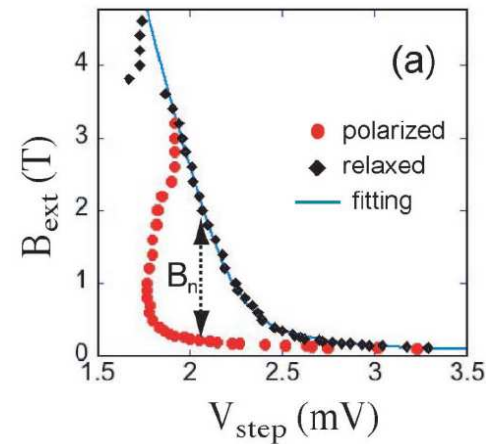
Ono & Tarucha, PRL 2004



Koppens, Folk et al, Science 2005



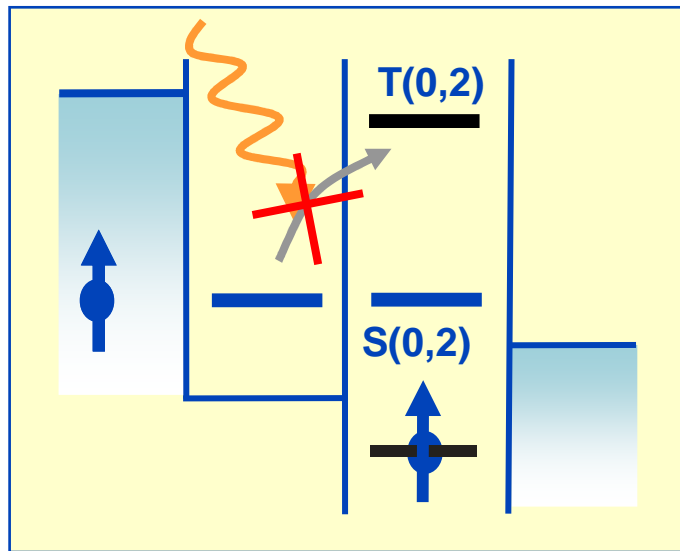
Reilly et al, PRL 2007



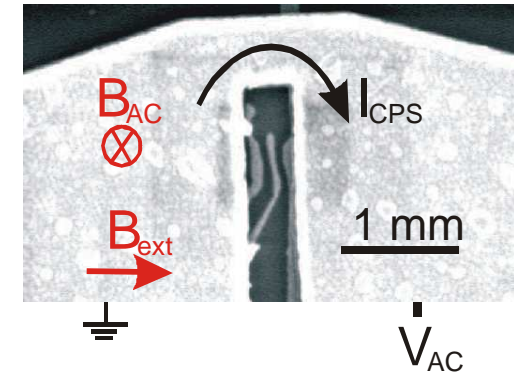
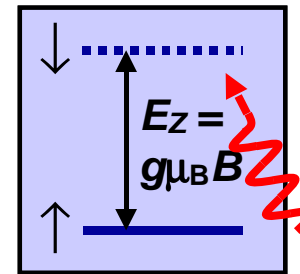
Baugh et al, PRL 2007

# Single-electron spin resonance

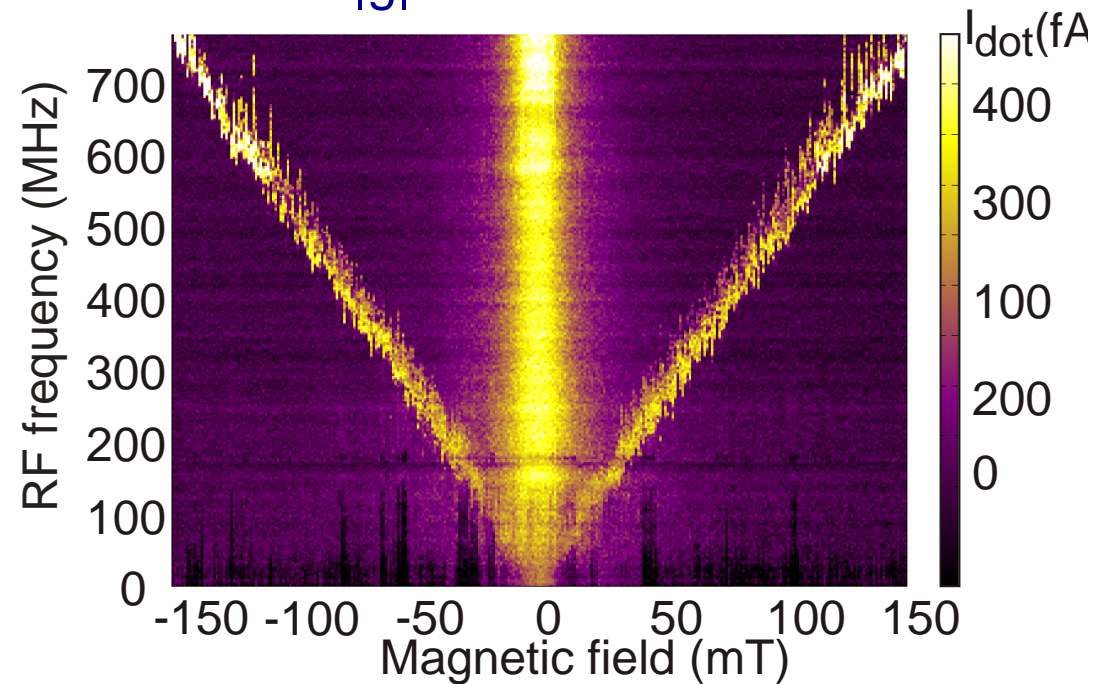
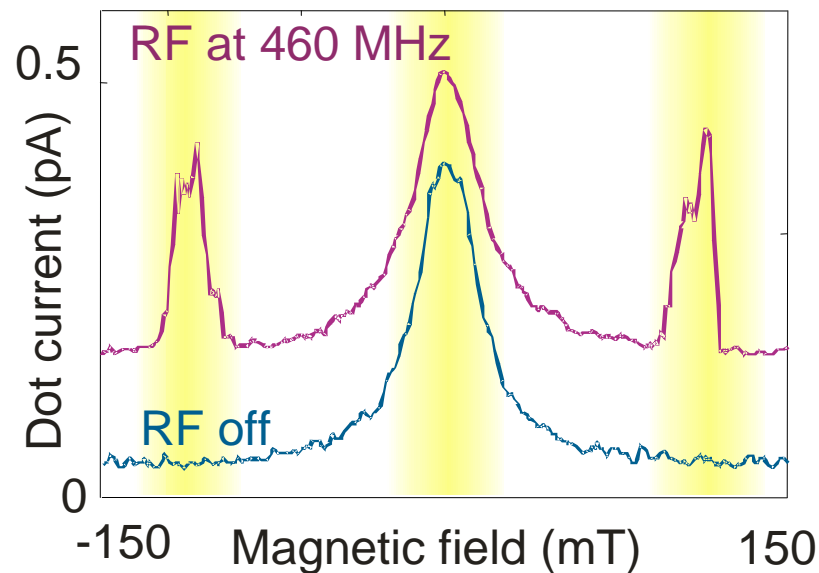
F. Koppens *et al.*, Nature 2006



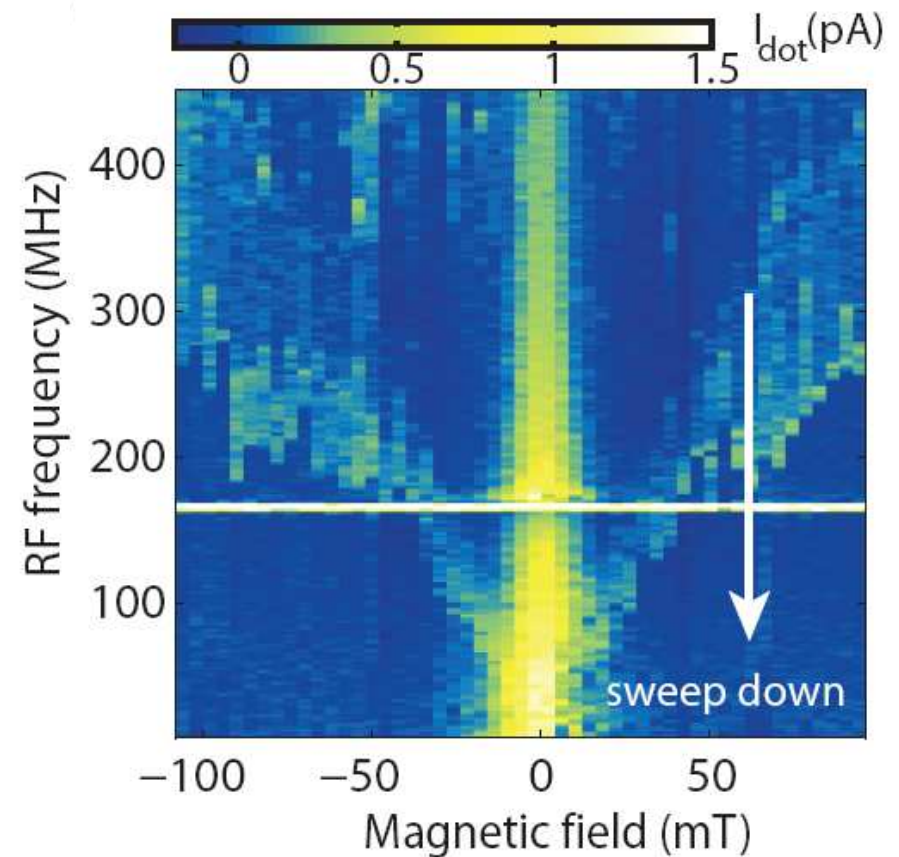
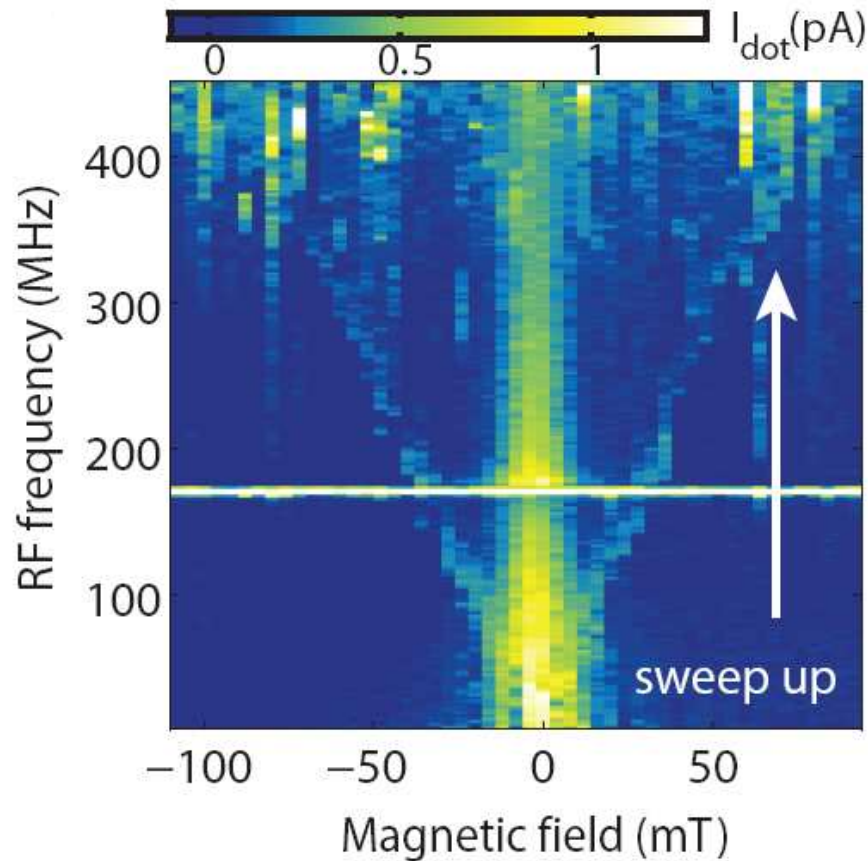
Inspiration: Engel & Loss PRL 2001



$|g|$ -factor  $\sim 0.35$



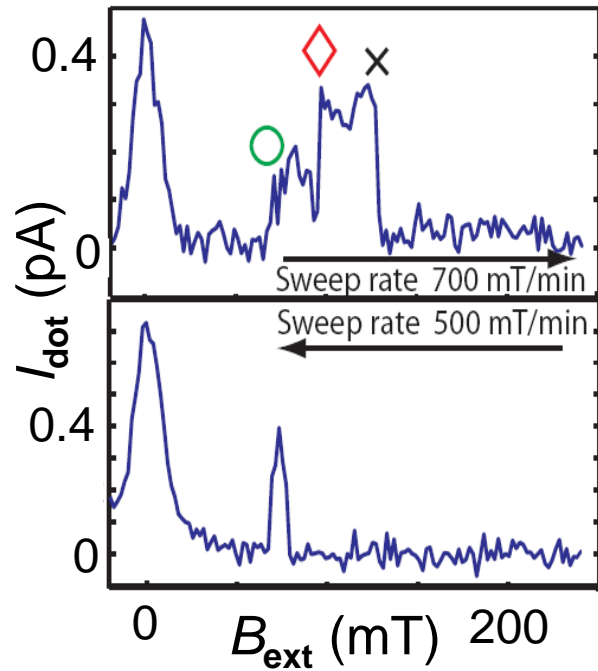
# A surprising observation



Difference with earlier data:

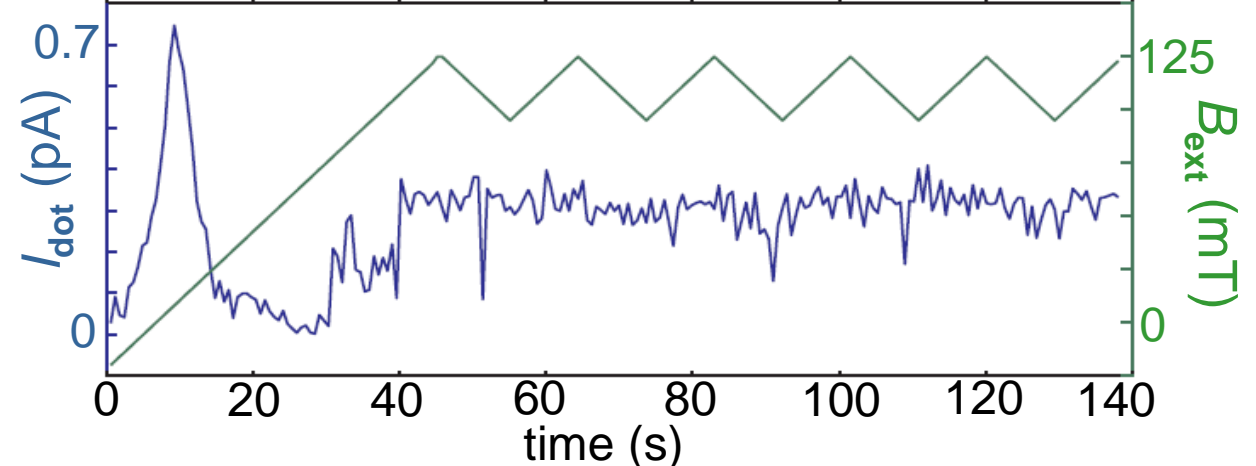
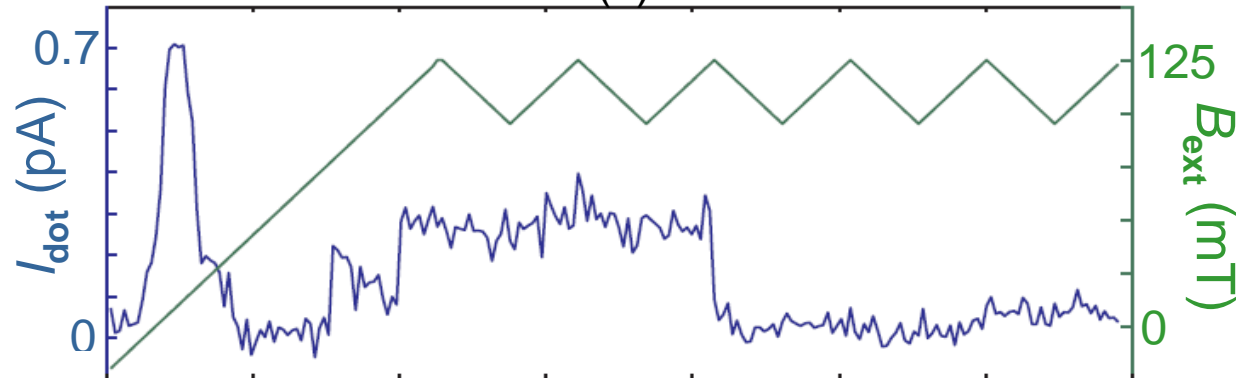
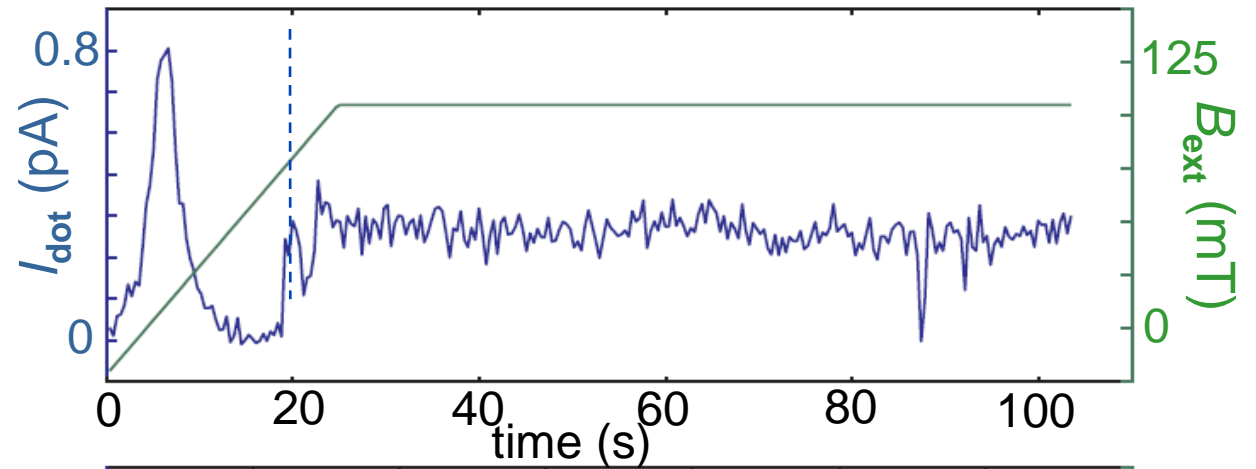
Larger interdot tunnel coupling  
Stronger tunnel coupling to leads  
Negative alignment of dot potentials

# Feedback in $B_N$ locks electron spin on resonance

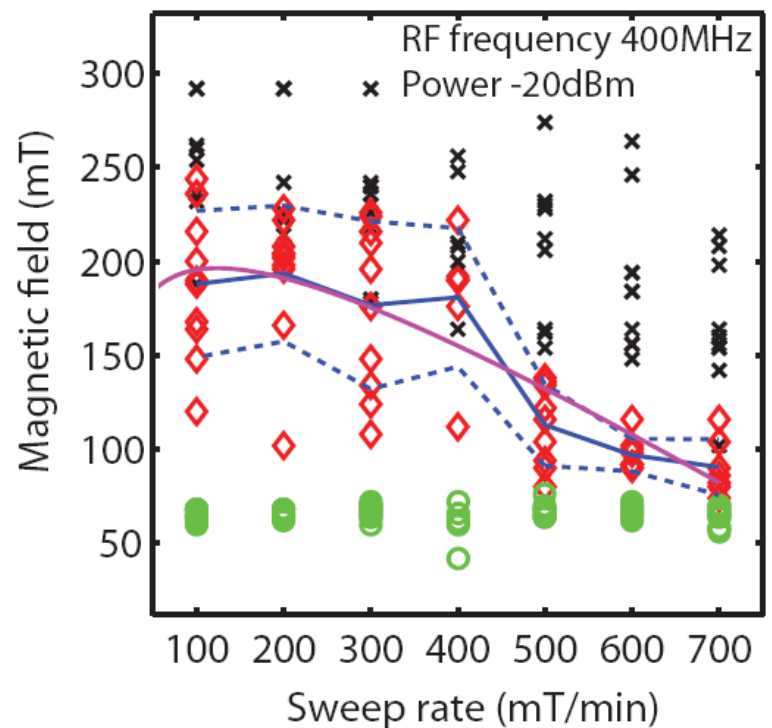
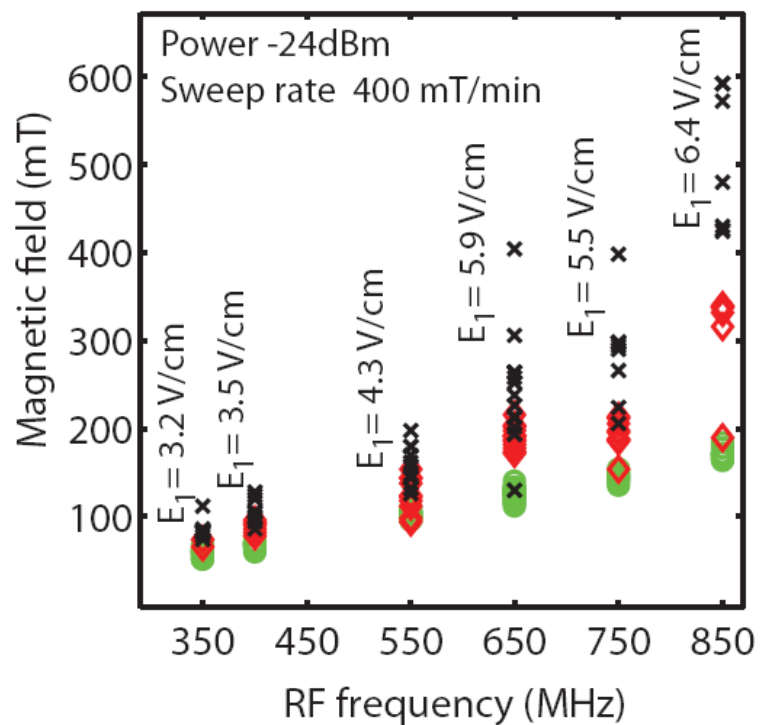
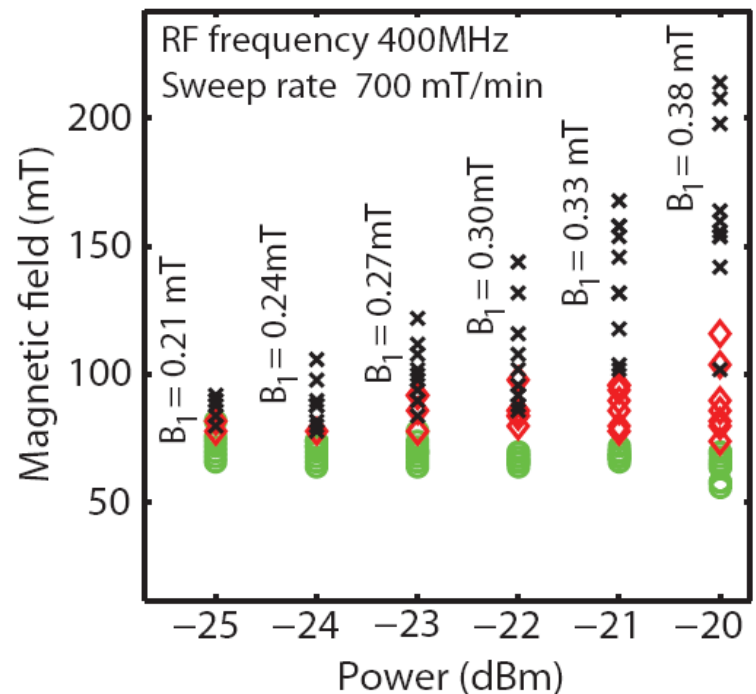
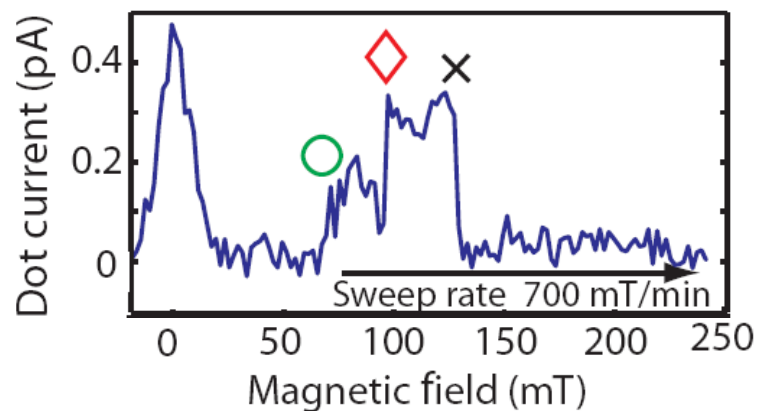


ESR condition:

$$hf = g\mu_B(B_{\text{ext}} + B_N)$$

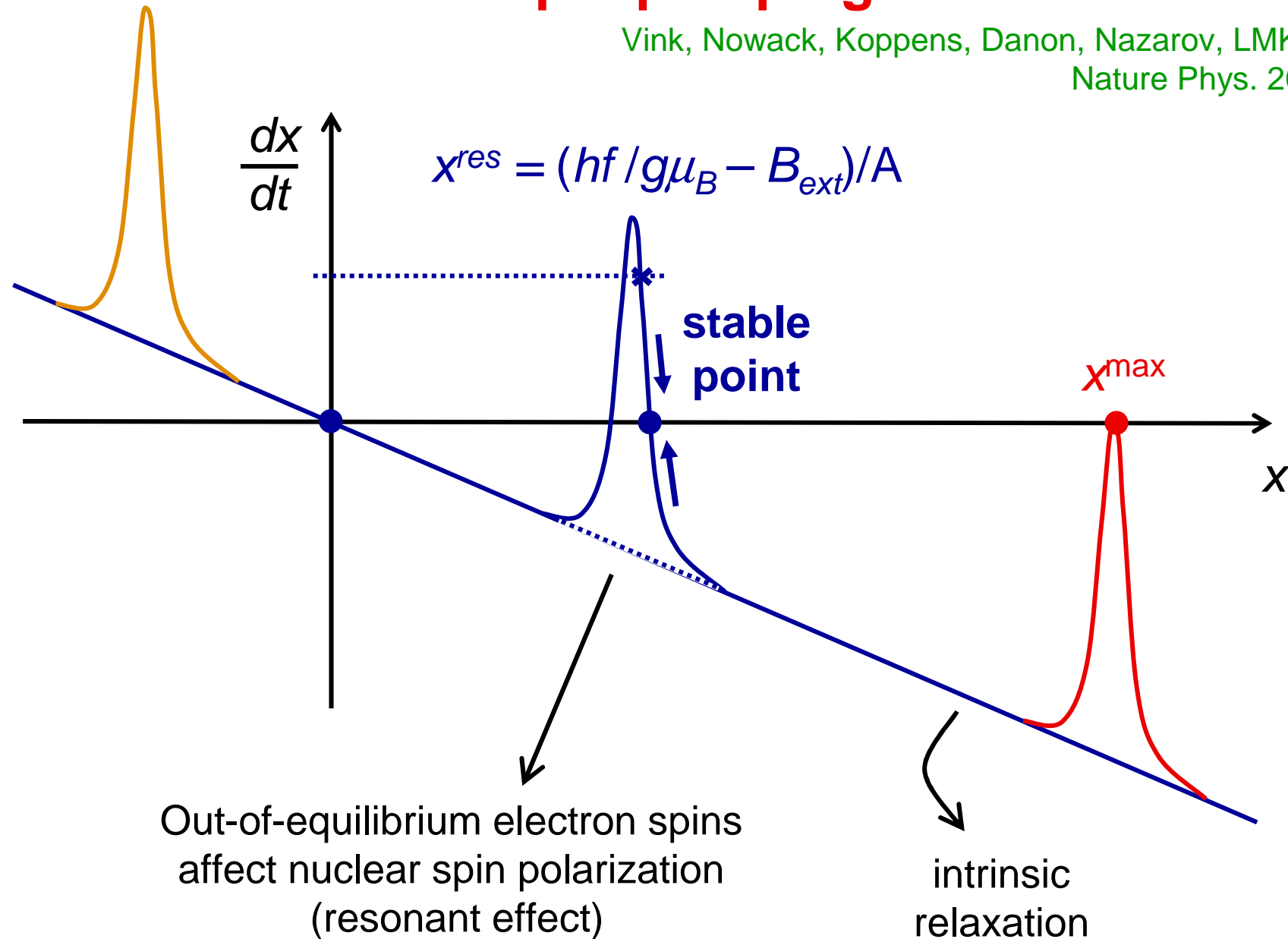


# Power, frequency and sweep rate dependence

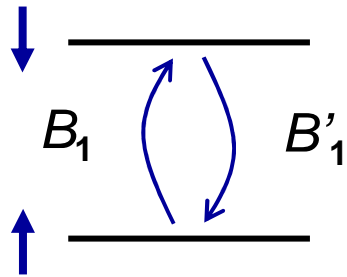


# Origin of spin resonance locking – nuclear spin pumping curve

Vink, Nowack, Koppens, Danon, Nazarov, LMKV,  
Nature Phys. 2009



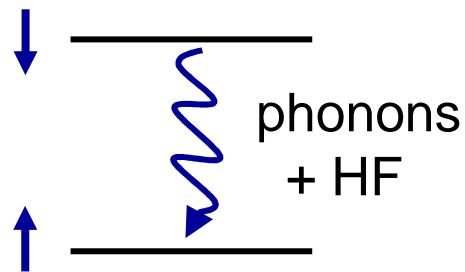
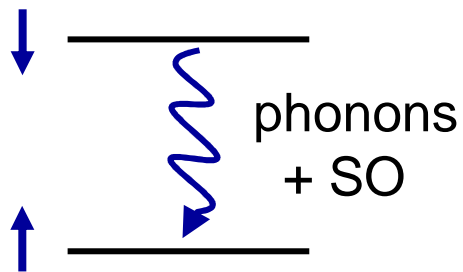
# Microscopic pumping mechanism



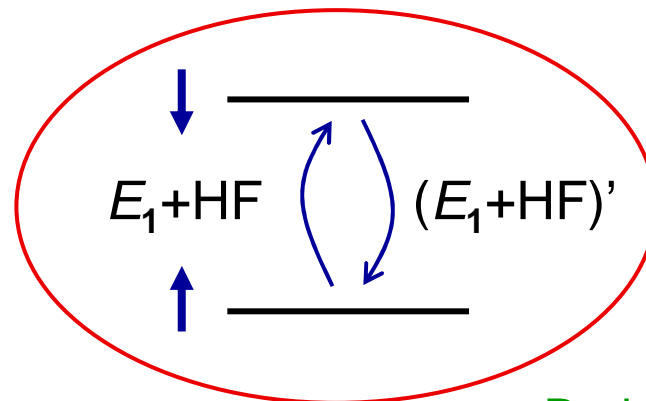
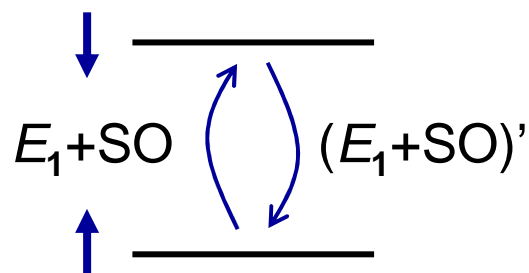
Observations:

$B_N$  points against  $B_{\text{ext}}$

$B_N^{\text{max}}$  increases with  $B_{\text{ac}}, E_{\text{ac}}$



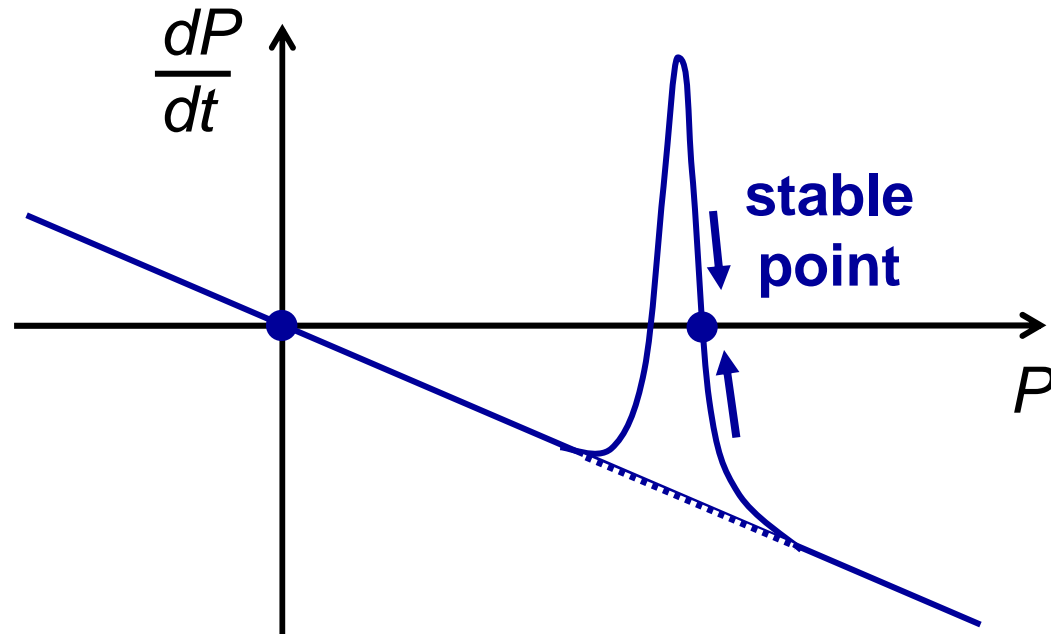
Overhauser  
 $B_N$  adds to  $B_{\text{ext}}$



Sign  $B_N$  depends on

- electron spin polar.
- nuclear spin polar.
- matrix elements

# Suppression of nuclear spin fluctuations



Feedback keeps  $P$  pinned around stable point  
slope sets "feedback strength"

no feedback

$$\sigma = \frac{A}{\sqrt{N}}$$



with feedback

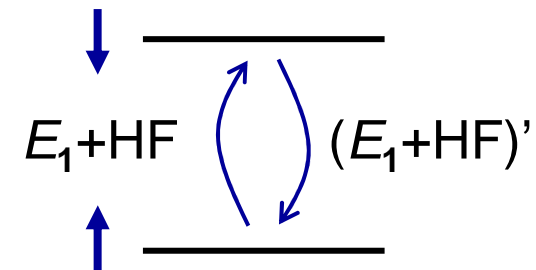
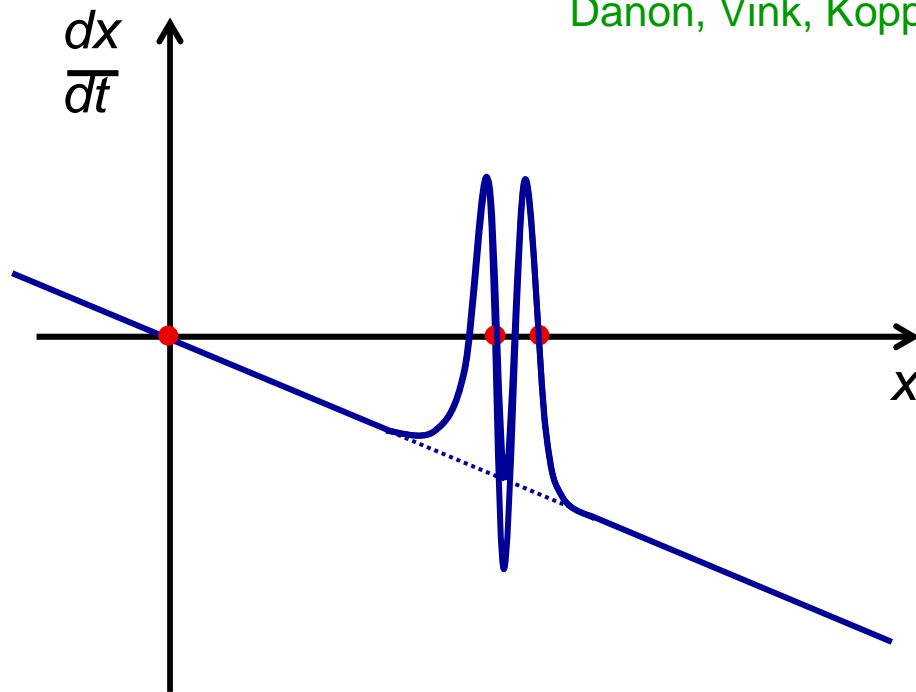
$$\sigma \approx \frac{A}{\sqrt{N}} \sqrt{\frac{B_1}{B_N^{\max}}}$$

>10x narrower



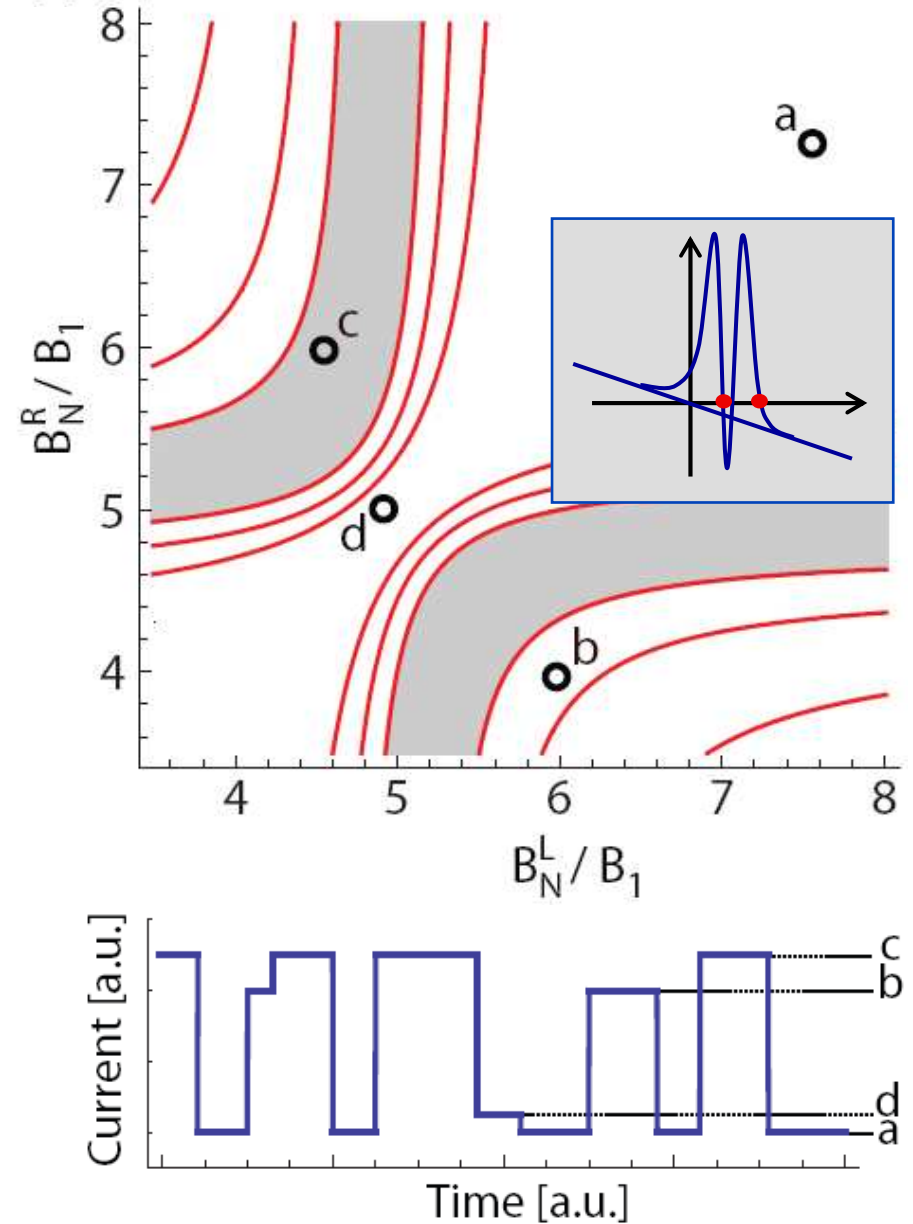
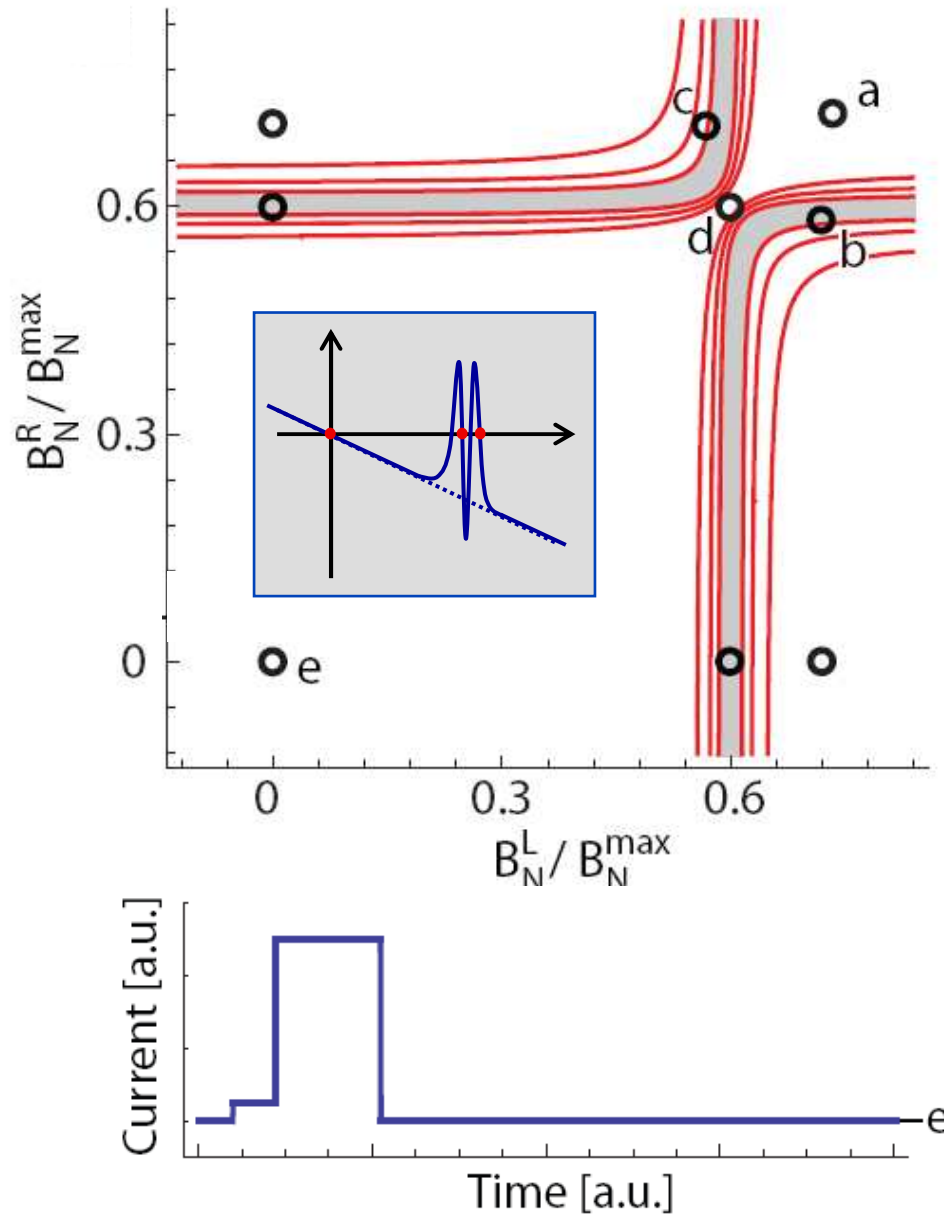
# Still richer physics for strong driving: multiple stable points

Danon, Vink, Koppens, Nowack, LMKV, Nazarov, PRL 2009

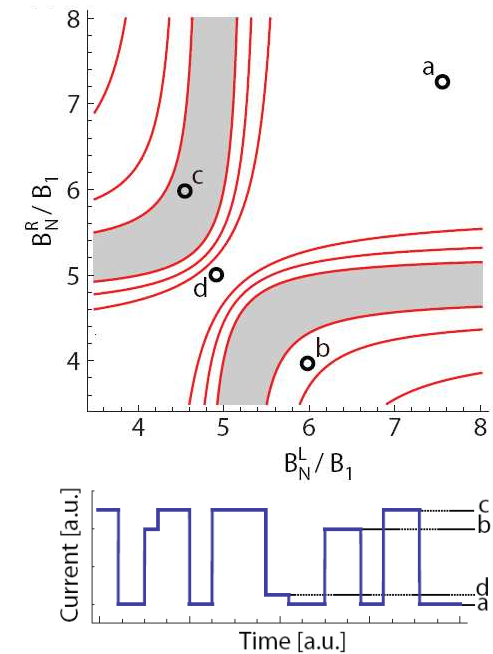
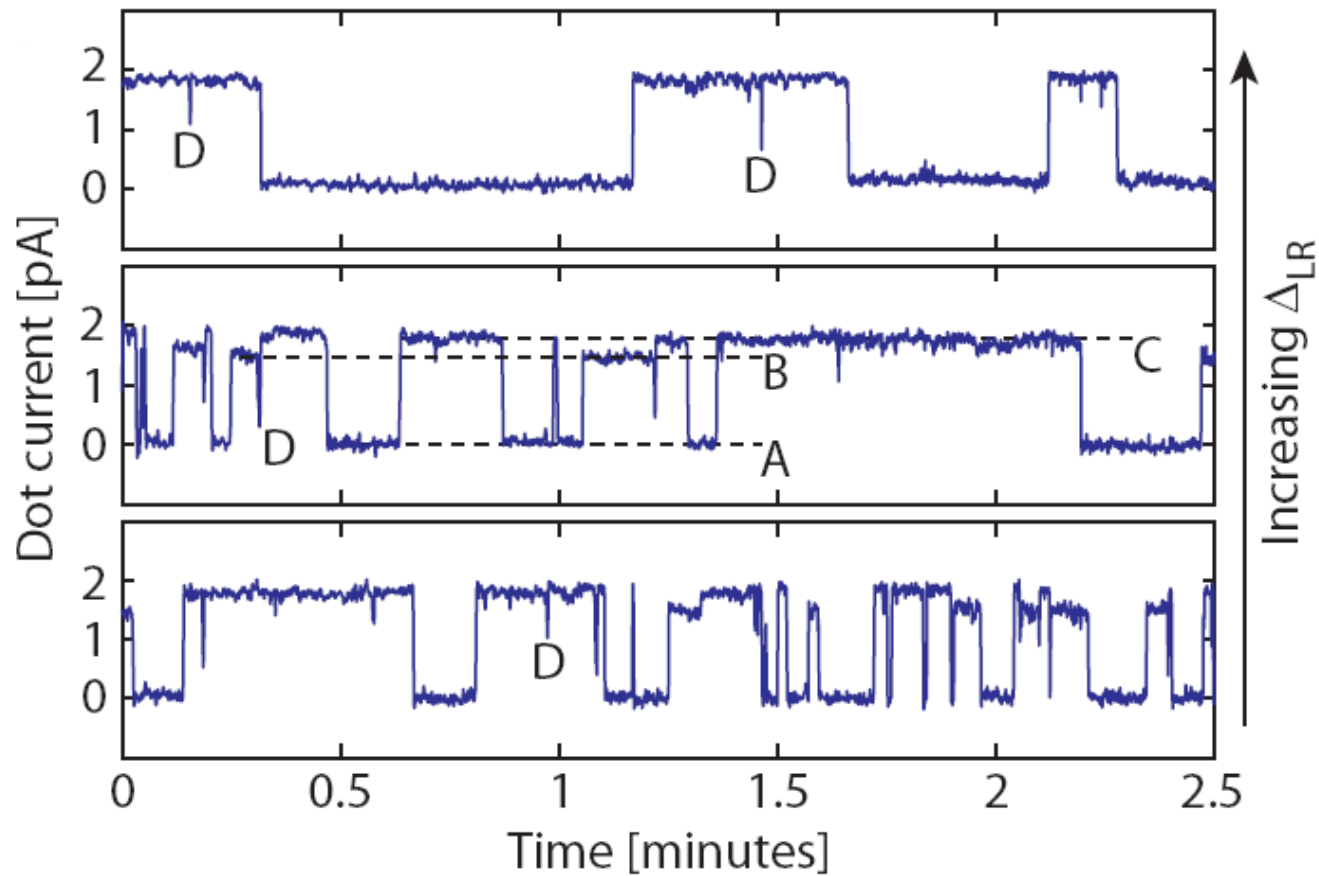


- 1) Equal  $\uparrow$  and  $\downarrow$  populations, hence no net nuclear spin pumping
- 2) Resonantly enhanced nuclear spin relaxation  
(nuclear spins flipped both ways)

# Switching between stable points



# Switching between stable points



Danon, Vink, Koppens, Nowack, LMKV, Nazarov, PRL 2009

# Other work on suppression of nuclear field randomness

C. Latta et al (Imamoglu group) Nature Phys. 2009

single self-assembled dot  
CW resonant trion excitation

X. Xu et al (Steel/Gammon group) Nature 2009

single self-assembled dot  
coherent dark state spectroscopy (Raman resonance)

A. Greilich et al. (Bayer group), Science 2007, PRL 2008

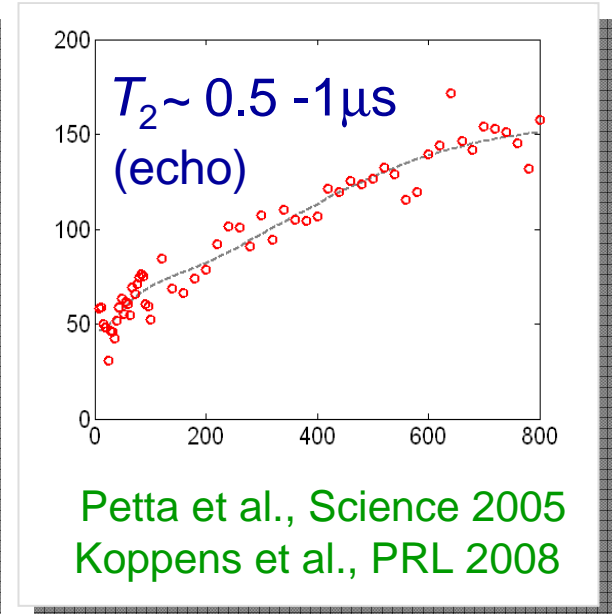
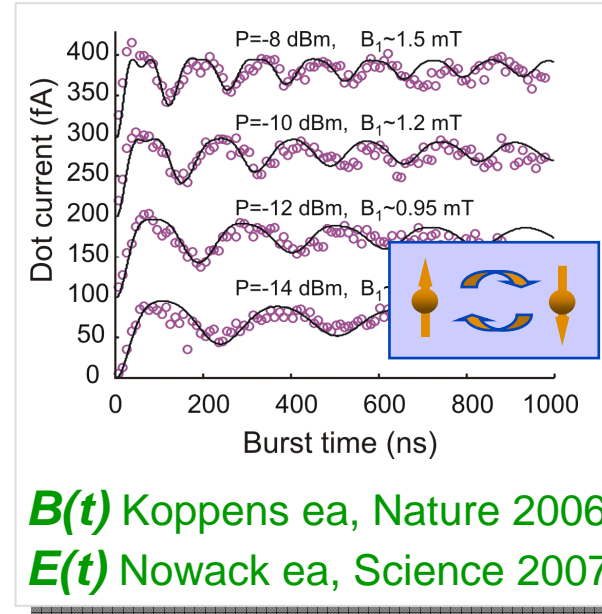
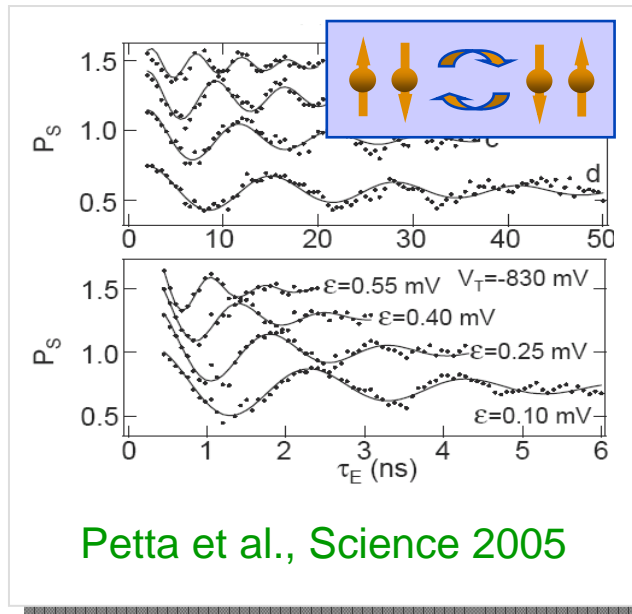
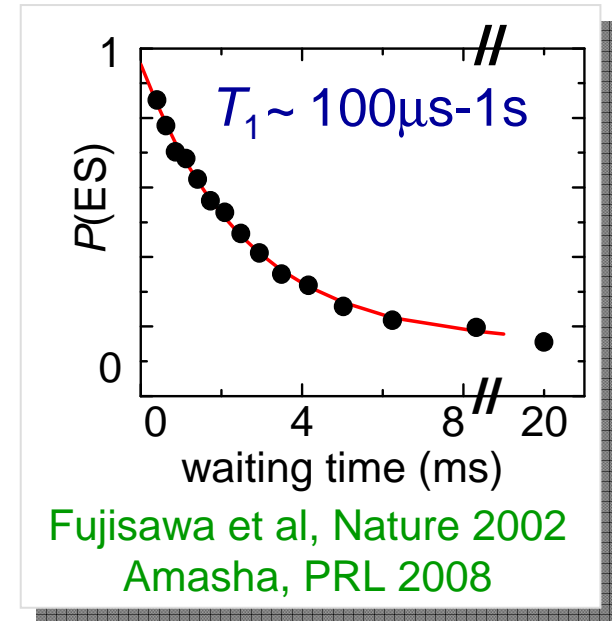
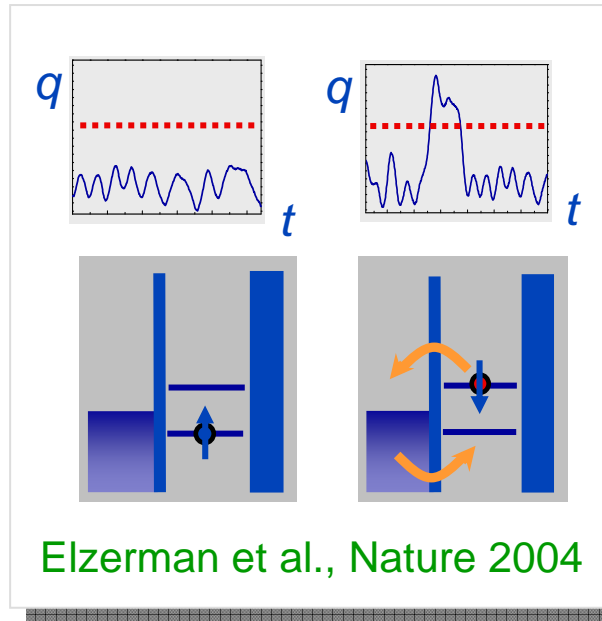
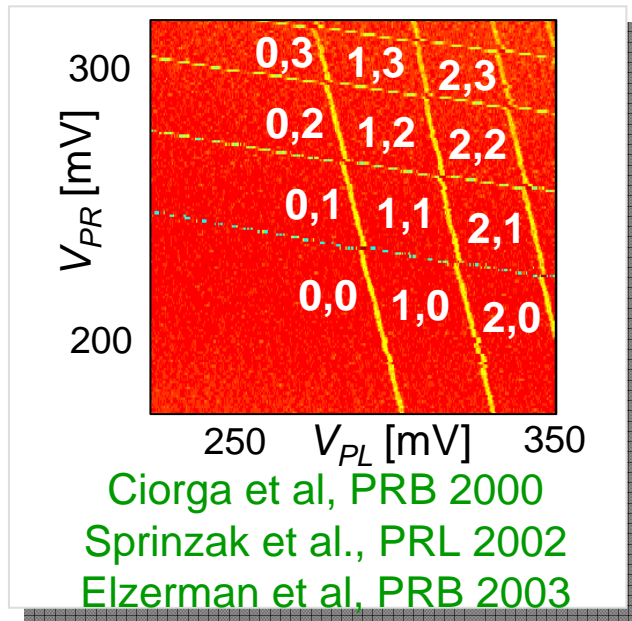
ensemble of self-assembled dots  
laser pulse train resonant with trion transition

D. Reilly et al (Marcus group), Science 2008

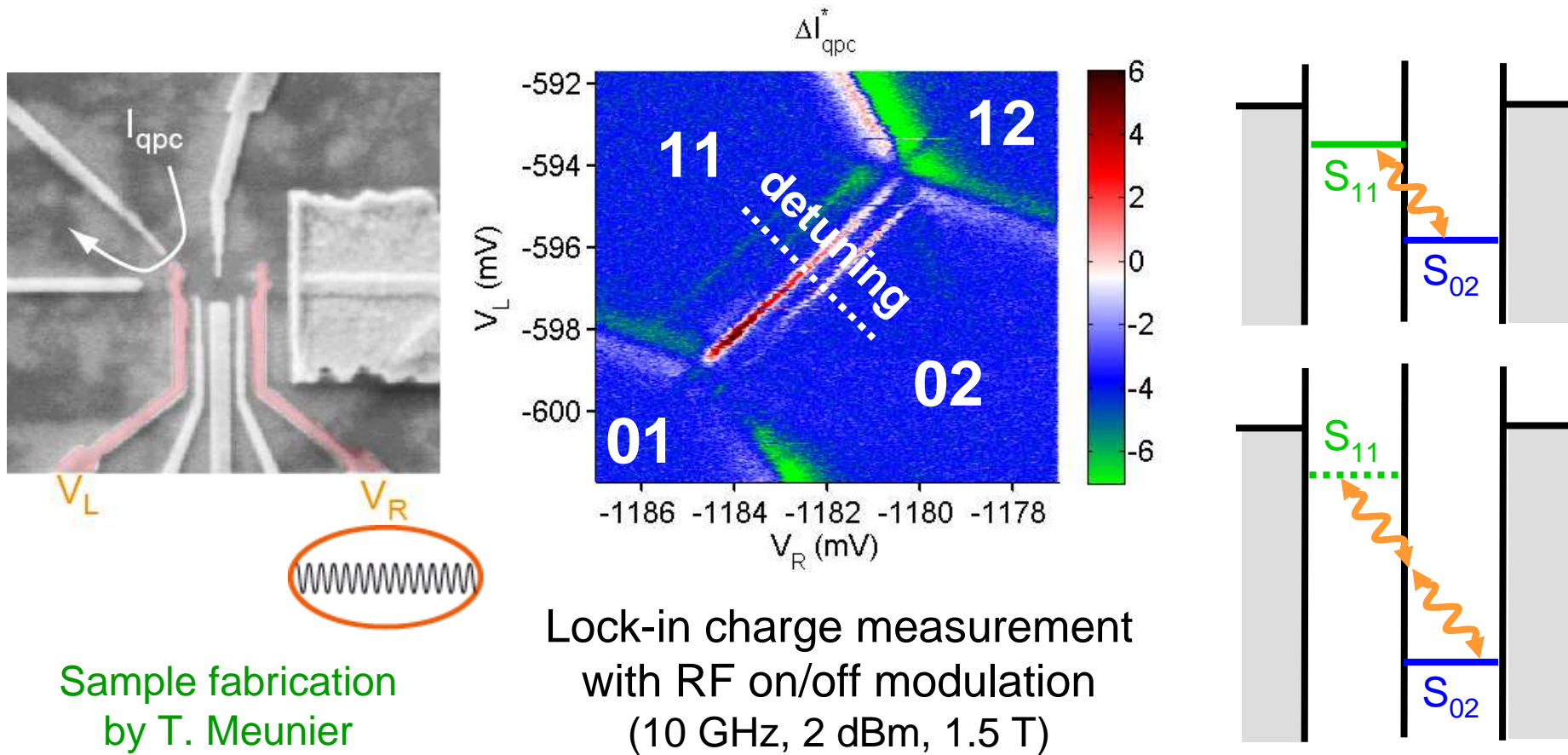
gate voltage pulse protocol  
suppression of *difference* in  $B_N$  between two dots

# Single-spin qubits in GaAs dots

See also *Hanson et al, Rev. Mod. Phys. 2007*



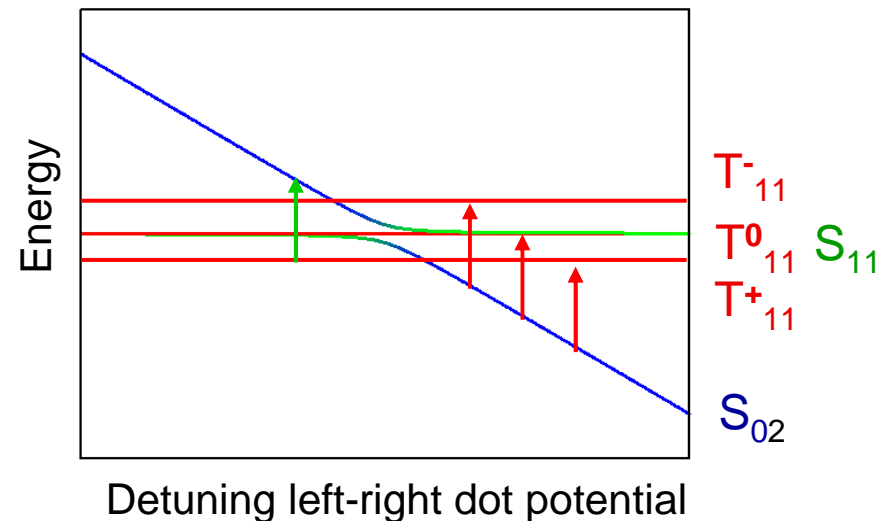
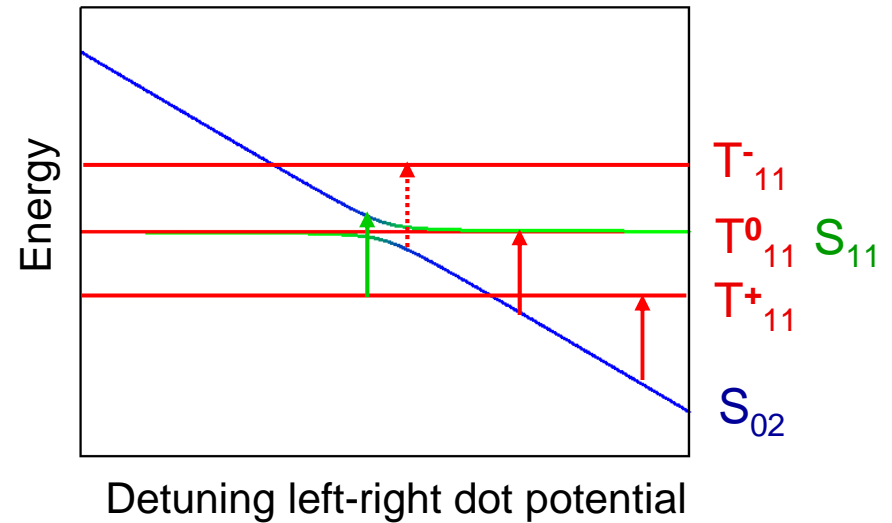
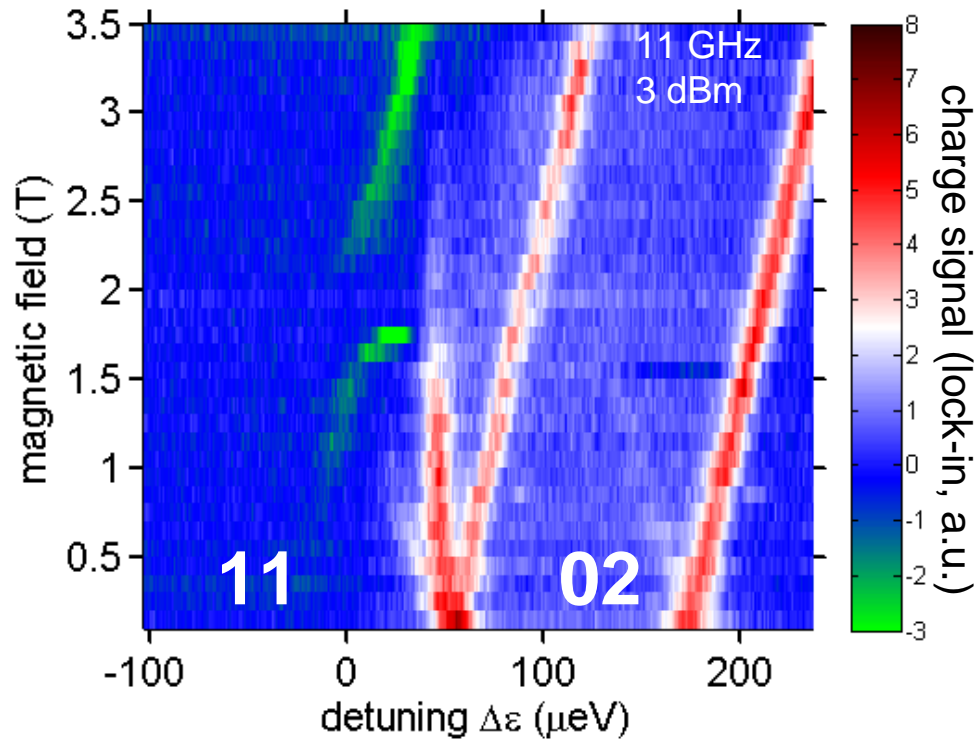
# Photon-assisted tunneling (spin-conserving)



just the well-known photon-assisted tunneling sidebands?

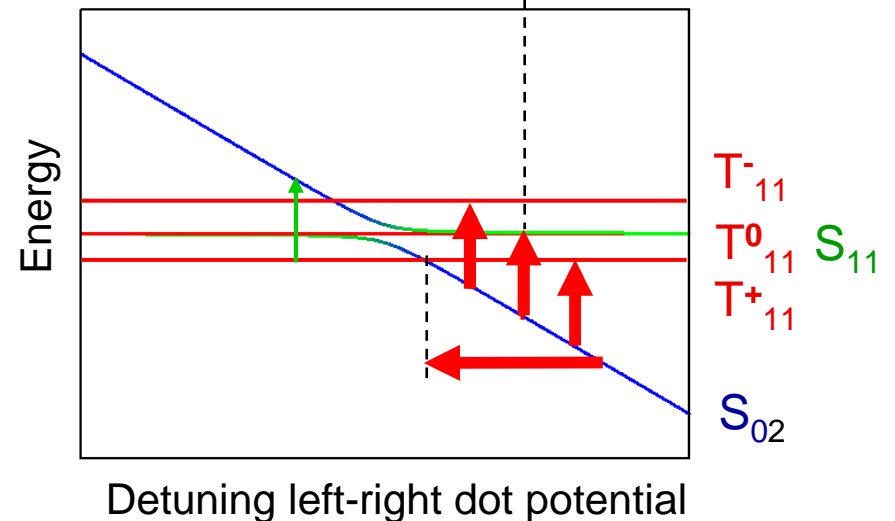
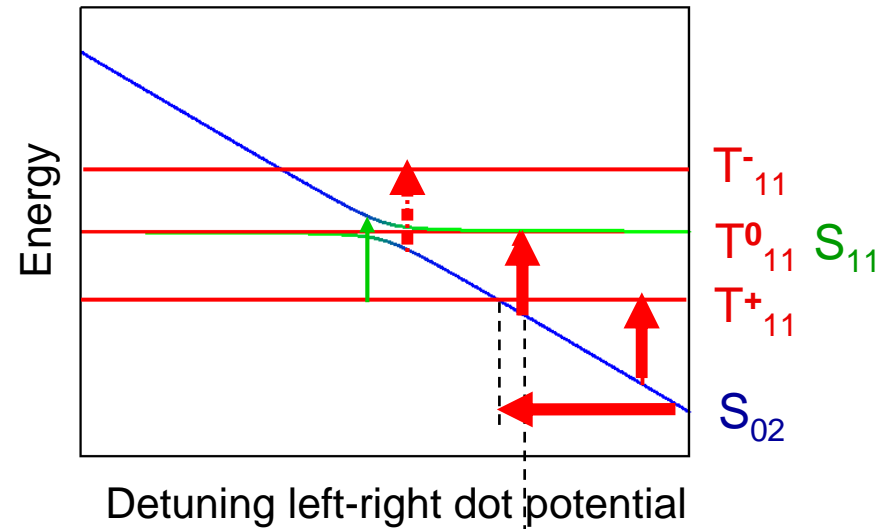
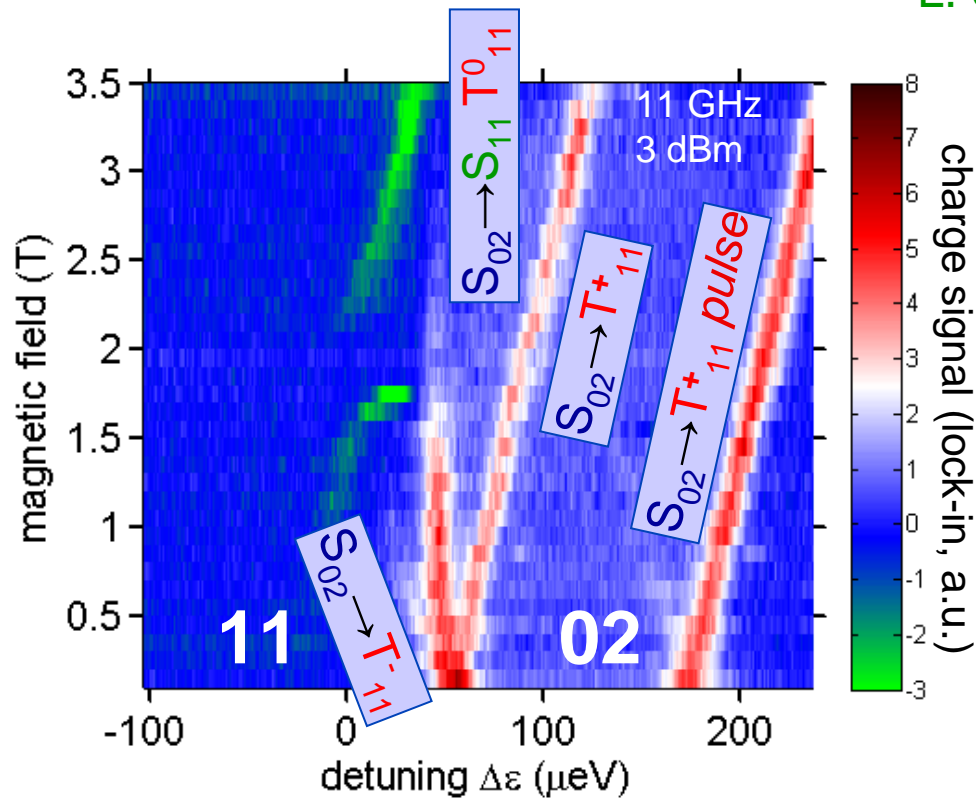
# Two-electron spin transitions

L. Schreiber, F. Braakman et al, unpublished



# Two-electron spin transitions

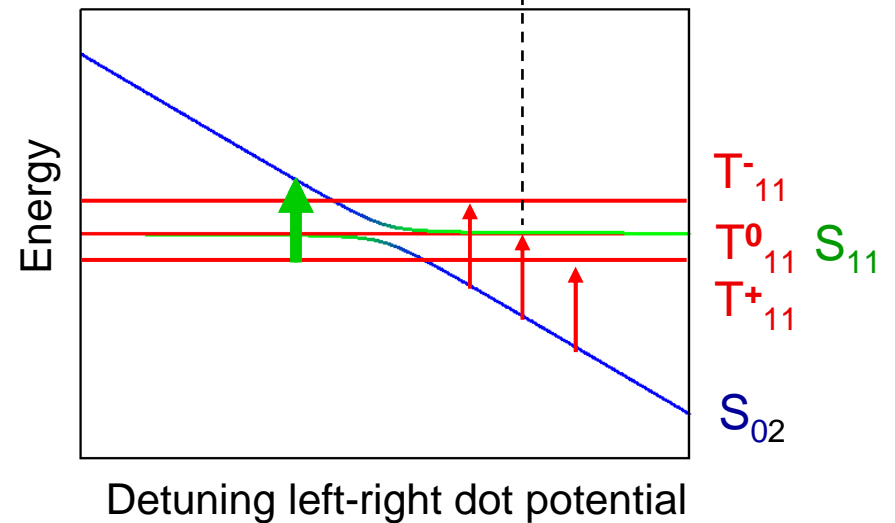
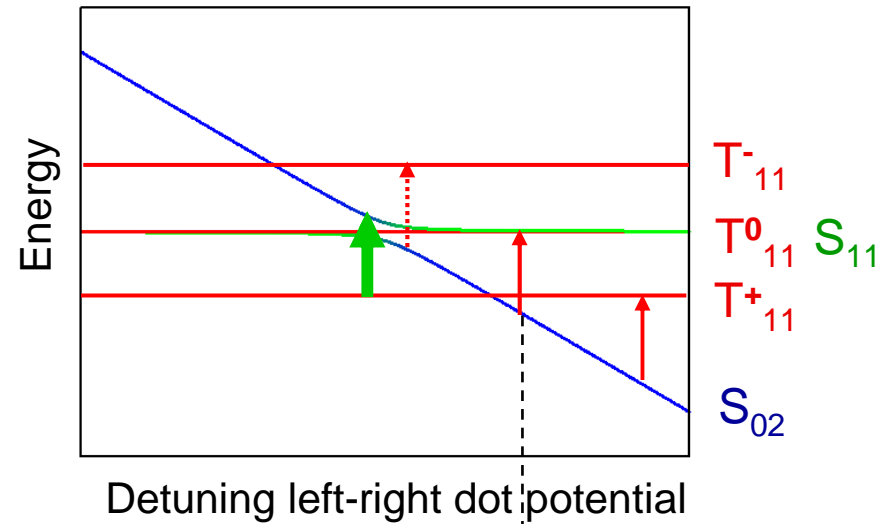
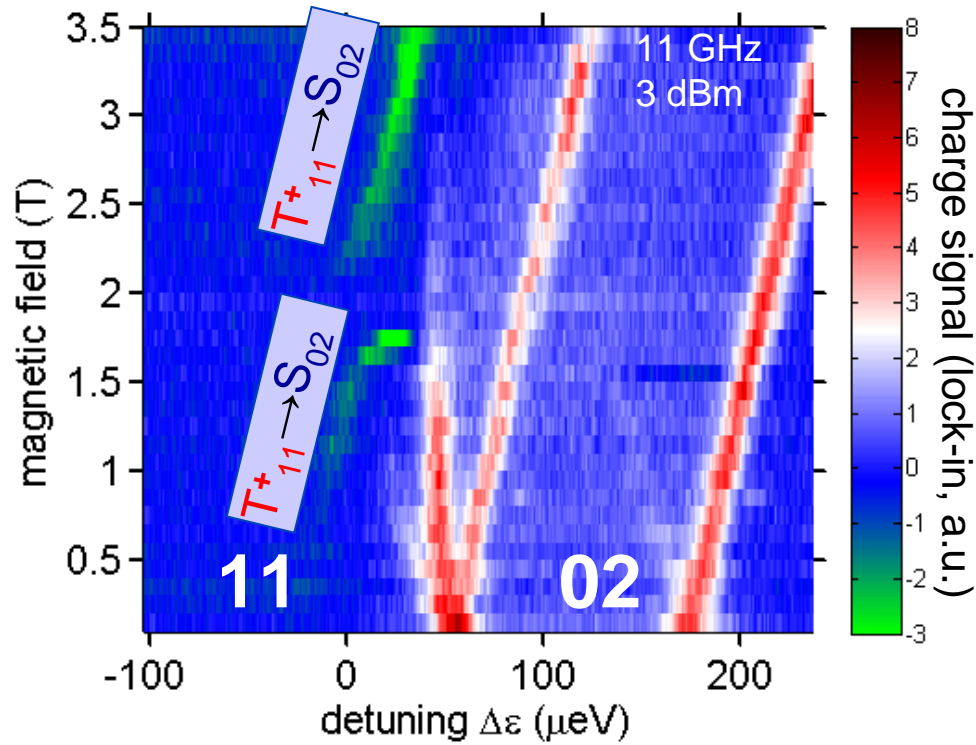
L. Schreiber, F. Braakman et al, unpublished



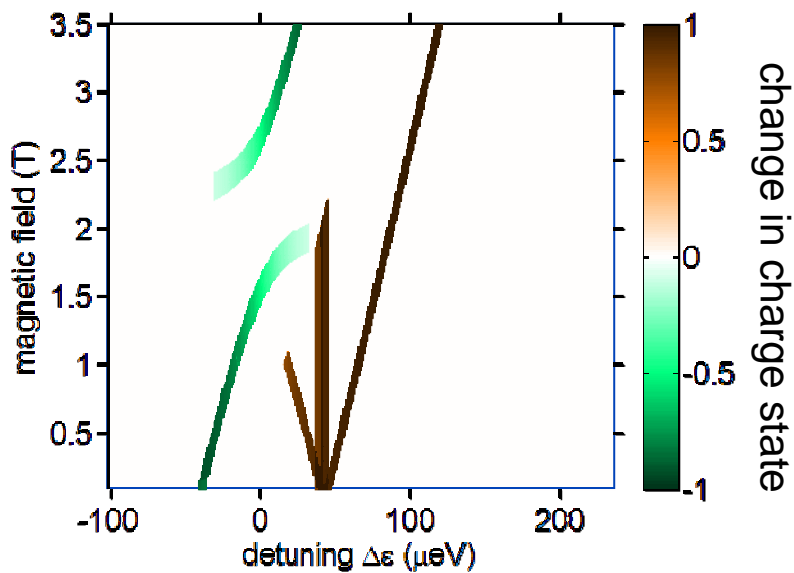
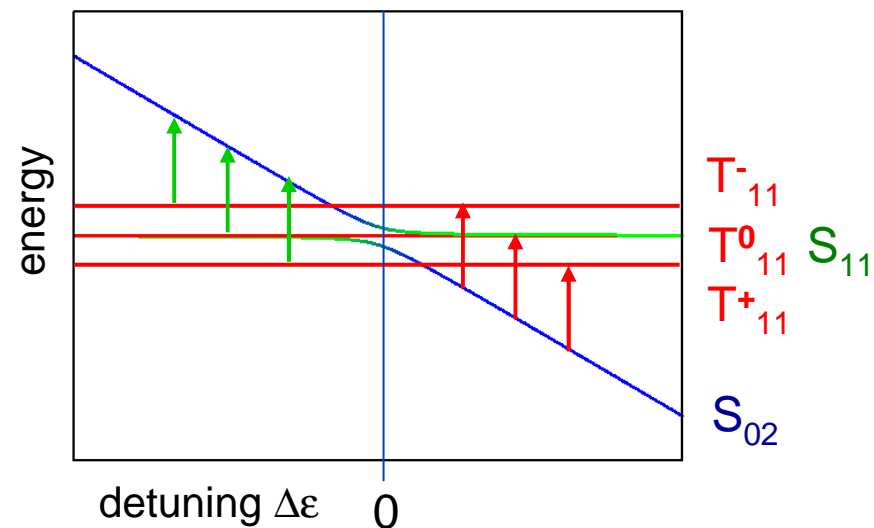
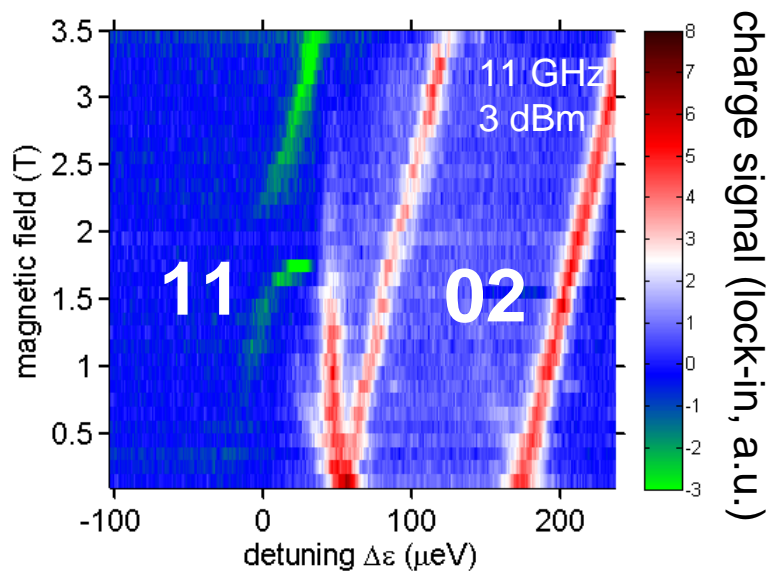


# Two-electron spin transitions

L. Schreiber, F. Braakman et al, unpublished



# spin-PAT simulation

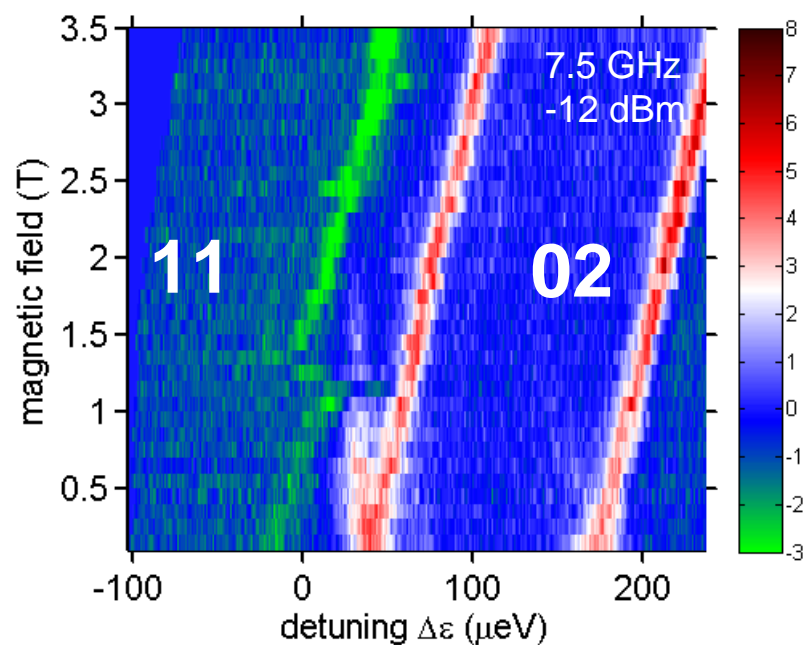
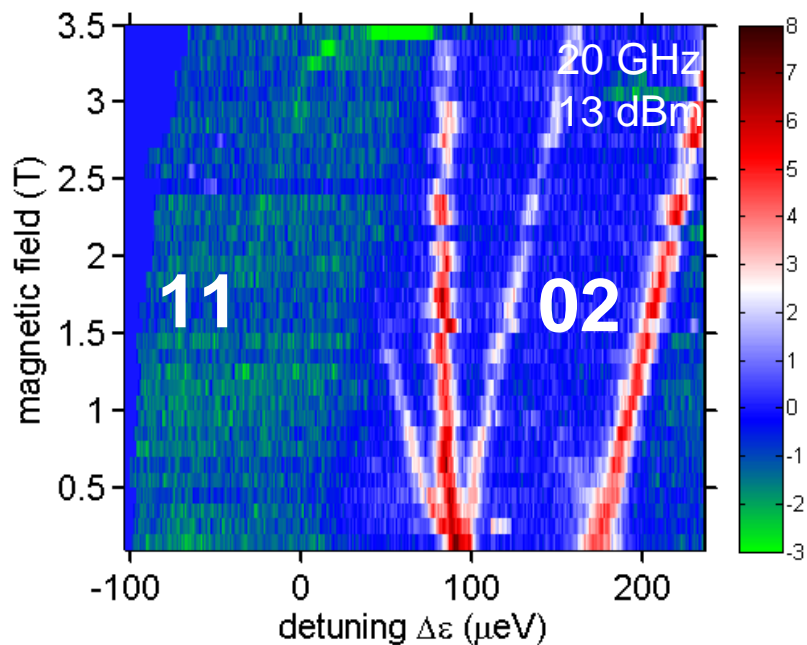
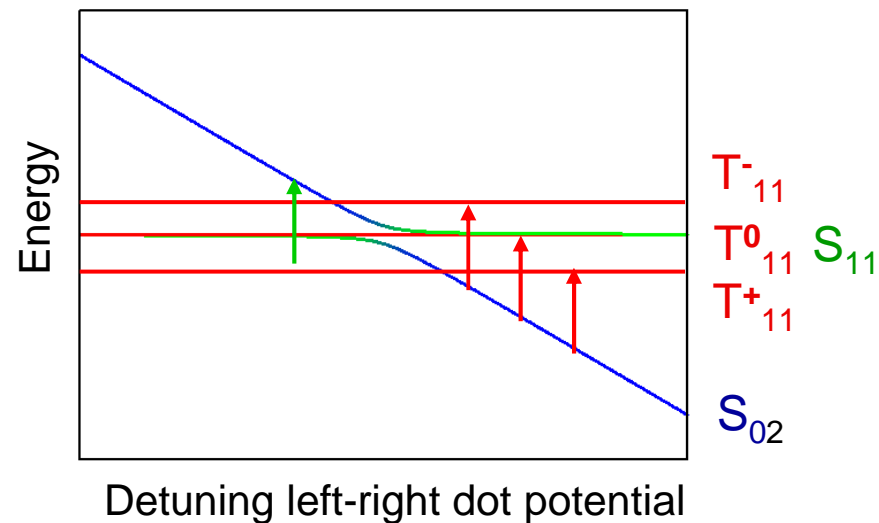
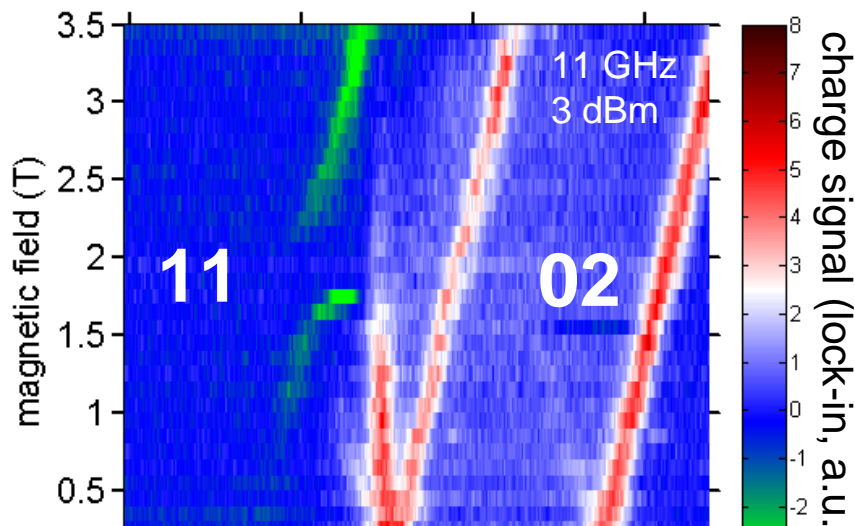


Extracted from comparison with data:

tunnel coupling  $t_c = 12 \mu\text{eV}$   
 $|g|$ -factor = 0.37  
 (given frequency 11 GHz)

# Spin-flip-PAT Spectroscopy

L. Schreiber, F. Braakman et al, unpublished



# Spin-orbit mechanism

## Spin-orbit Hamiltonian

Dresselhaus (bulk property)  $\mathcal{H}_D^{2D,(001)} = \beta[-p_x\sigma_x + p_y\sigma_y]$

Rashba (heterostructure property)  $\mathcal{H}_R = \alpha(-p_y\sigma_x + p_x\sigma_y)$

## For bound states (quantum numbers $n, l$ )

$$\langle p_x \rangle = \langle p_y \rangle = 0$$

$$\langle nl \downarrow | H_{SO} | nl \uparrow \rangle \propto \langle nl | p_{x,y} | nl \rangle \langle \downarrow | \sigma_{x,y} | \uparrow \rangle = 0$$

## Spin-orbit Hamiltonian directly couples states with different spin & orbital

$$\langle n'l' \uparrow | H_{SO} | nl \downarrow \rangle \neq 0$$

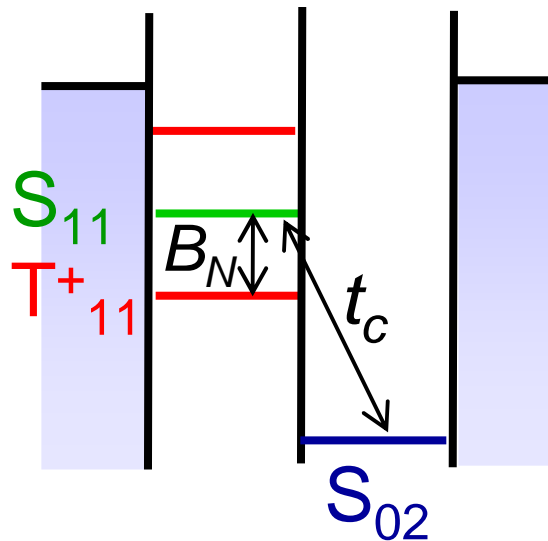
direct SO matrix element  
between  $S_{02}$  and  $T_{11}$

Matrix element  $S_{02}$  to  $T_{11}^{+,-} \sim t_c l_{\text{dot}} / l_{SO} \sim 0.01 t_c$

# Hyperfine mechanism

Resonant transition from  $S_{02}$  to  $T_{11}^{+}$  via two-step process involving virtual transition to  $S_{11}$ :

- (1)  $t_c$  couples  $S_{02}$  to  $S_{11}$
- (2) nuclei couple  $S_{11}$  to  $T_{11}^{+,-}$  (suppressed with  $B$ )

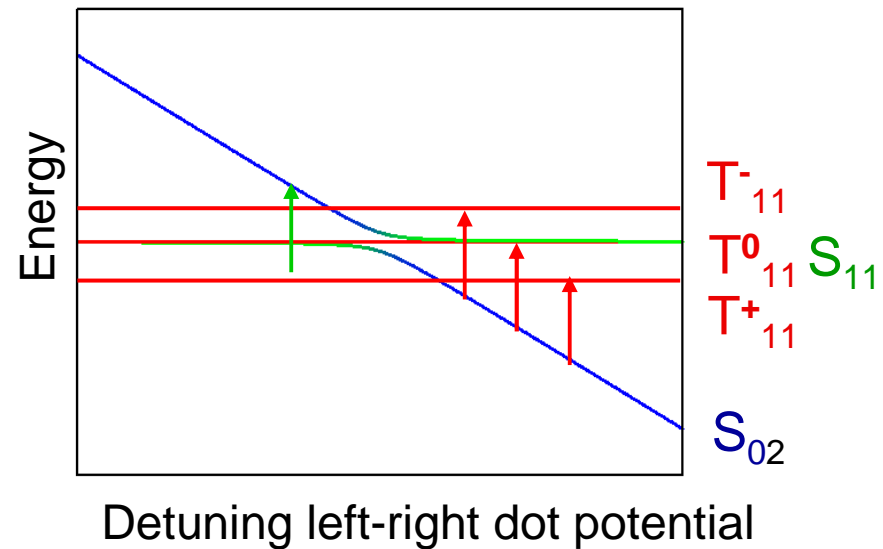
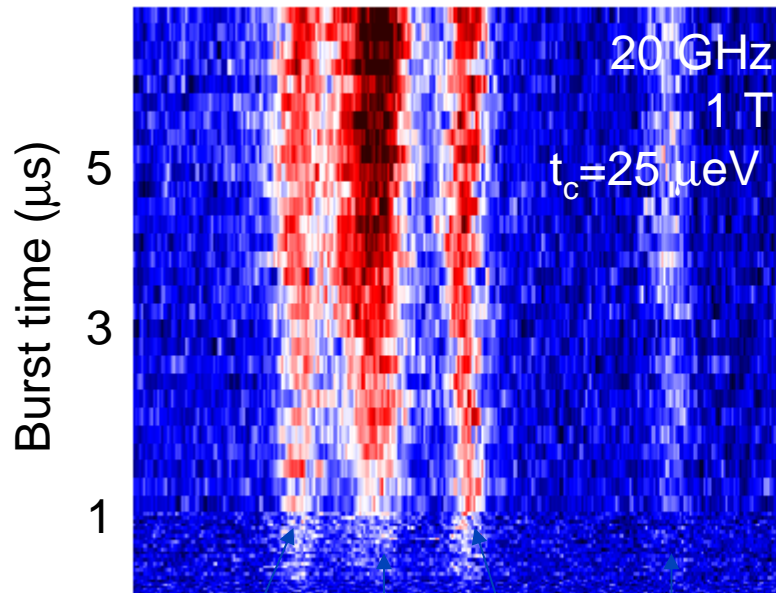


Matrix element  $S_{02}$  to  $T_{11}^{+,-}$   
 $\sim t_c B_{\text{nuc}} / B_{\text{ext}} \sim 0.001 t_c$

# Excitation by microwave bursts

microwave burst + 7  $\mu\text{s}$  free relaxation (no initialization):

Raw data



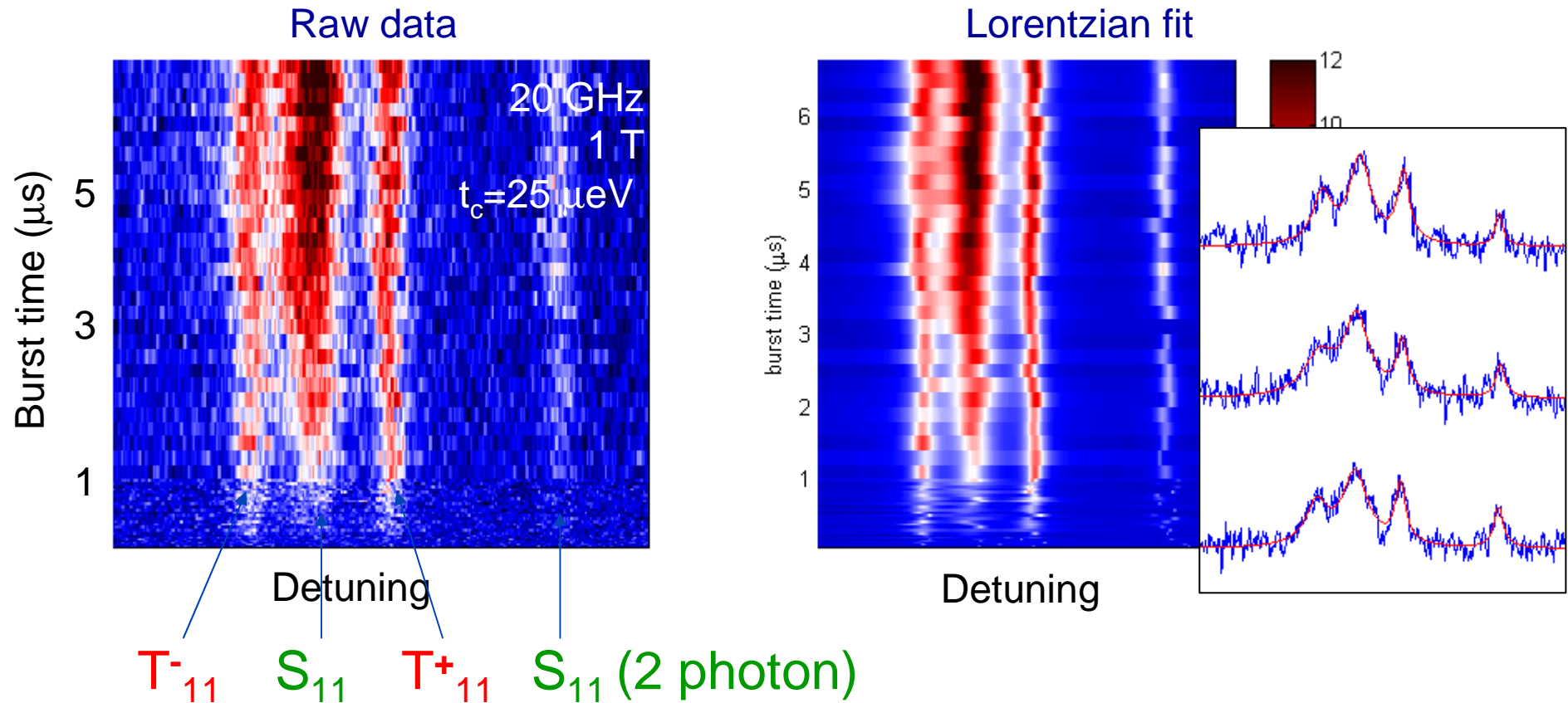
Detuning

$T^-_{11}$   $S_{11}$   $T^+_{11}$   $S_{11}$  (2 photon)

Signal increases with burst time and power  
 Transition to  $T^+_{11}$  and  $T^-_{11}$  show same behavior  
 Transition to  $S_{11}/T^0_{11}$  gives stronger signal

# Excitation by microwave bursts

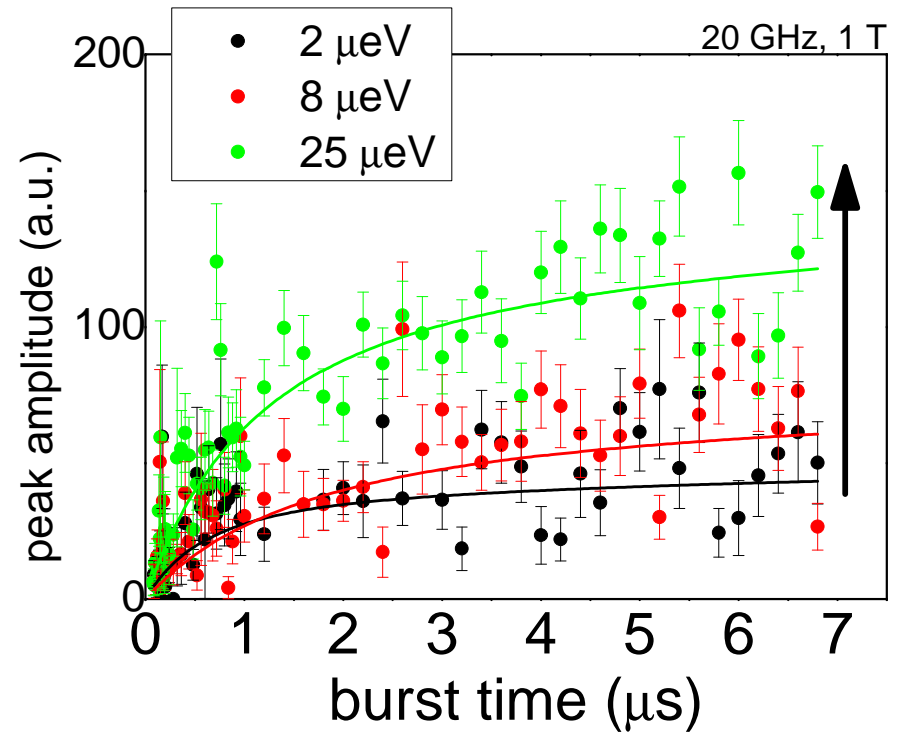
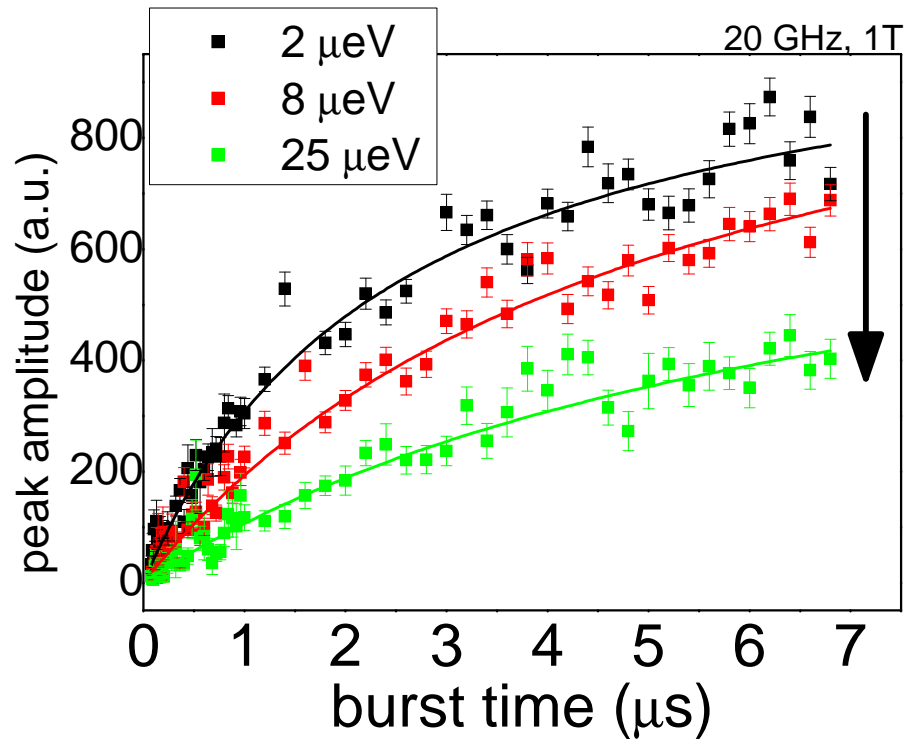
microwave burst + 7  $\mu\text{s}$  free relaxation (no initialization):



# Dependence on interdot tunnel coupling

$$S_{02} \rightarrow S_{11}$$

$$S_{02} \rightarrow T^+_{11}$$

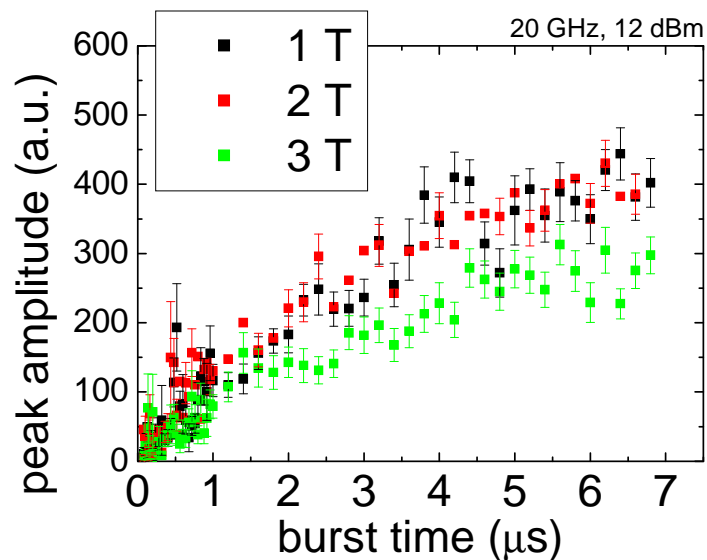


Preliminary data – datapoints represent peak area  
Signal is sensitive to both relaxation and excitation rates

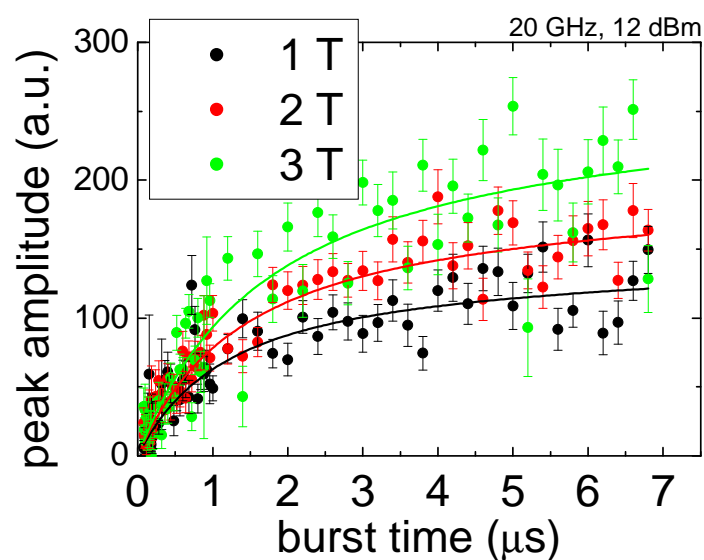


# Dependence on magnetic field

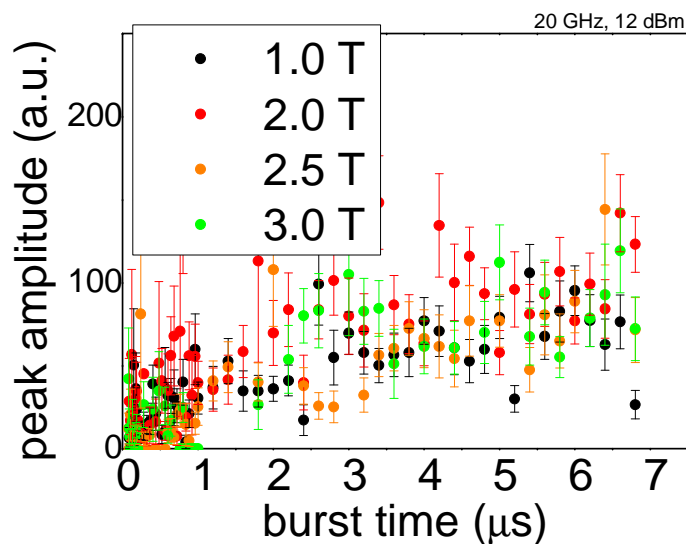
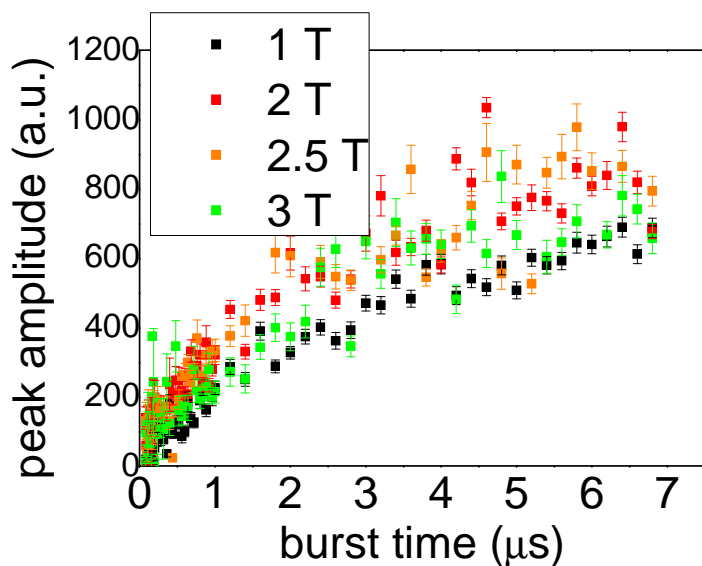
$S_{02} \rightarrow S_{11}$



$S_{02} \rightarrow T^+_{11}$



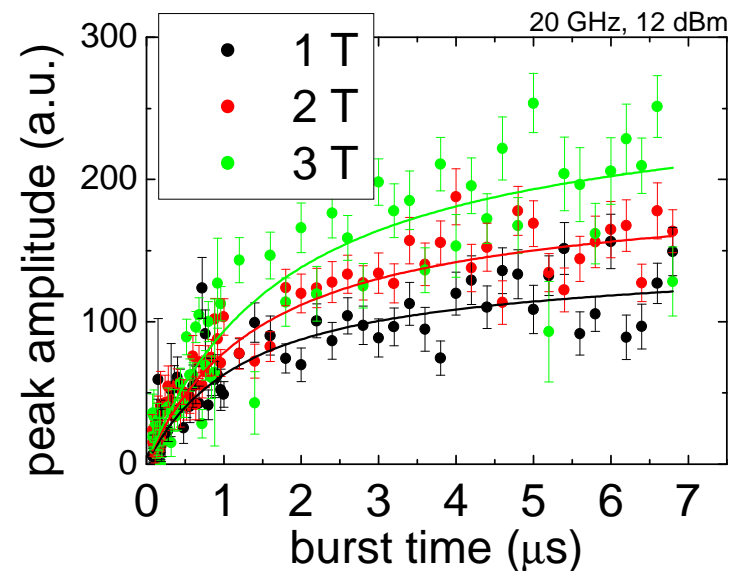
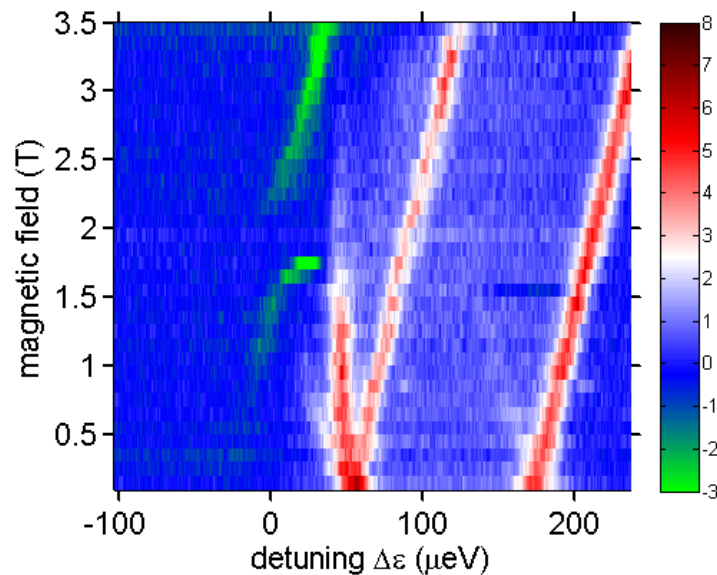
$t_c = 25 \mu\text{eV}$



$t_c = 8 \mu\text{eV}$

# Summary part II

- Electrically-induced spin-flip tunneling transitions
- Implications for electron spin shuttling
- Likely mediated by spin-orbit interaction
- Permits double-dot spectroscopy – all transitions identified
- Incoherent process (spins entangled with orbitals)



# People and collaborations

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Laurens Willems v Beveren (UNSW)  
Josh Folk (UBC)  
Frank Koppens (Harvard)  
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