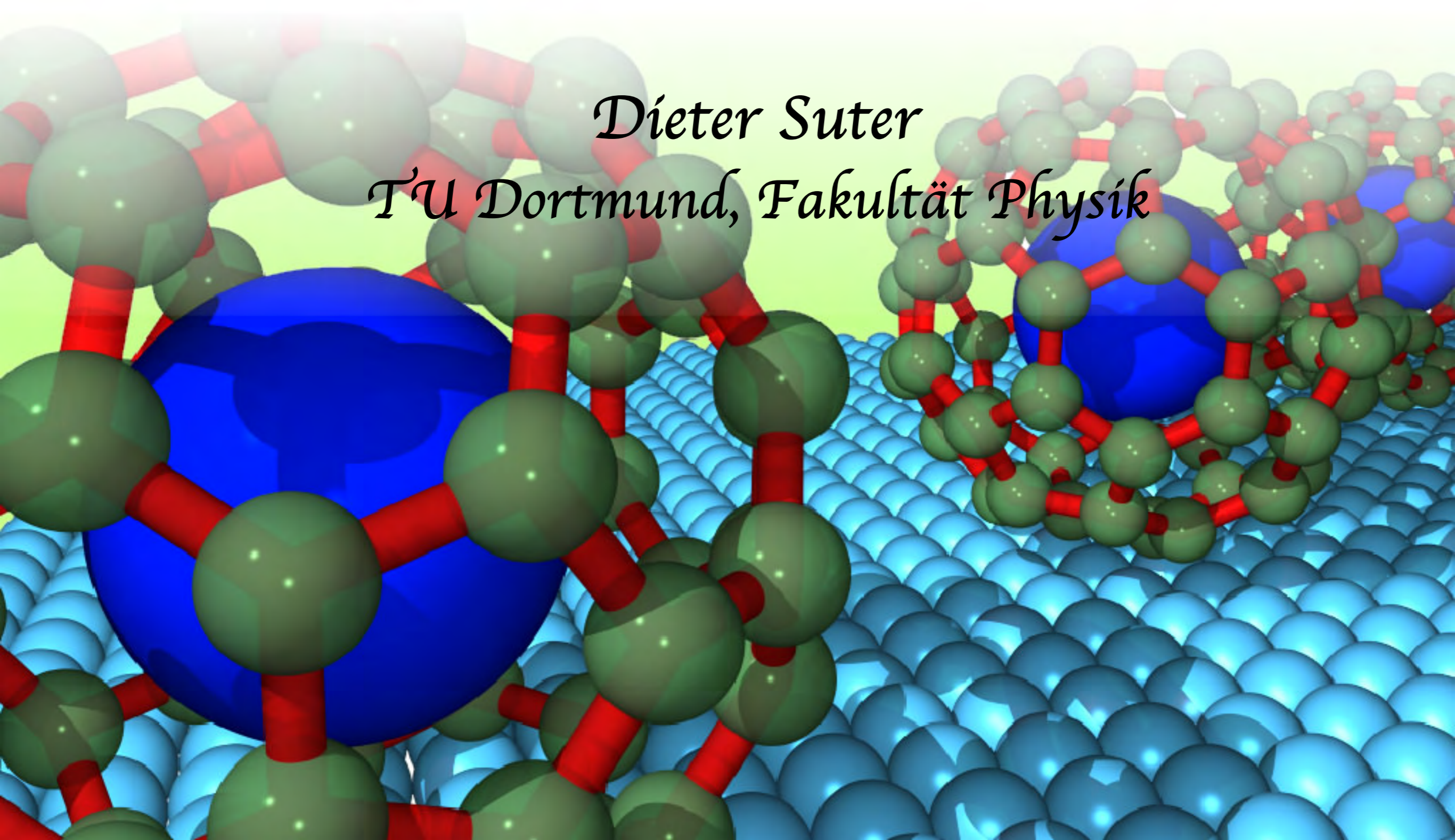


# Robust Control in RF-Optical Double Resonance Experiments

*Dieter Suter*  
*TU Dortmund, Fakultät Physik*



# *The Team*

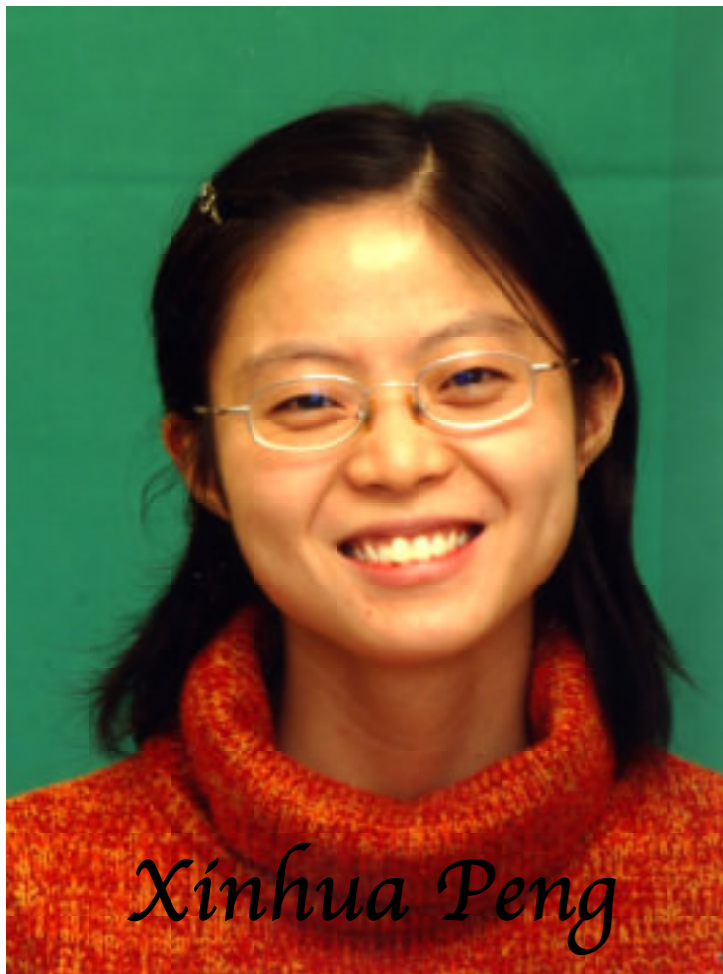
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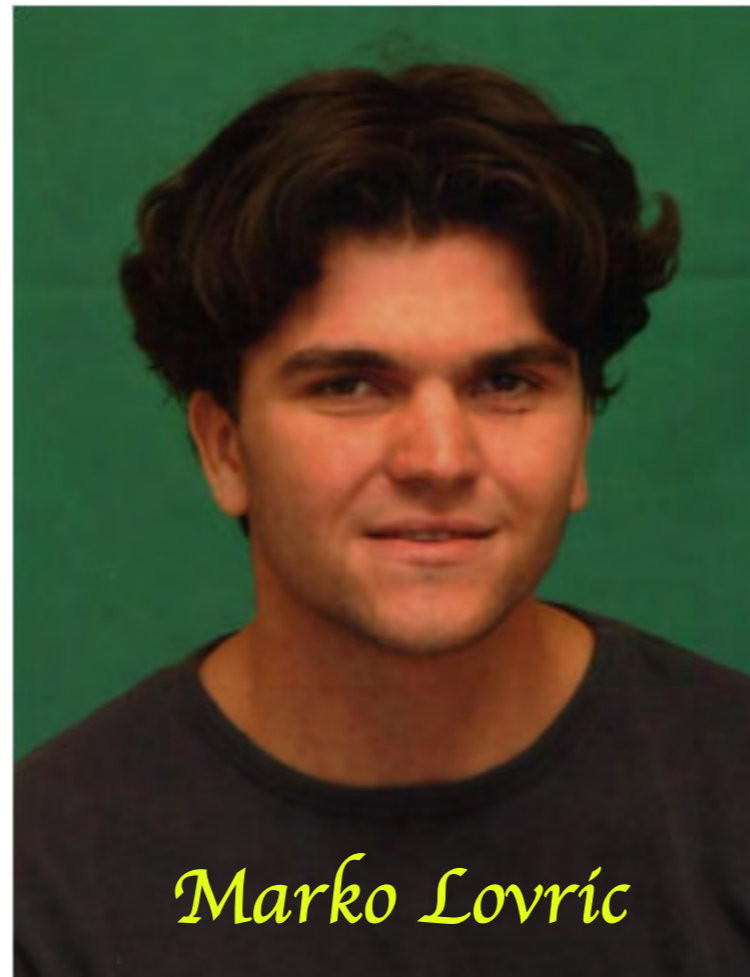
*Mahesh  
Tirthahalli*



*Christina Hopfgarten*



*Xinhua Peng*

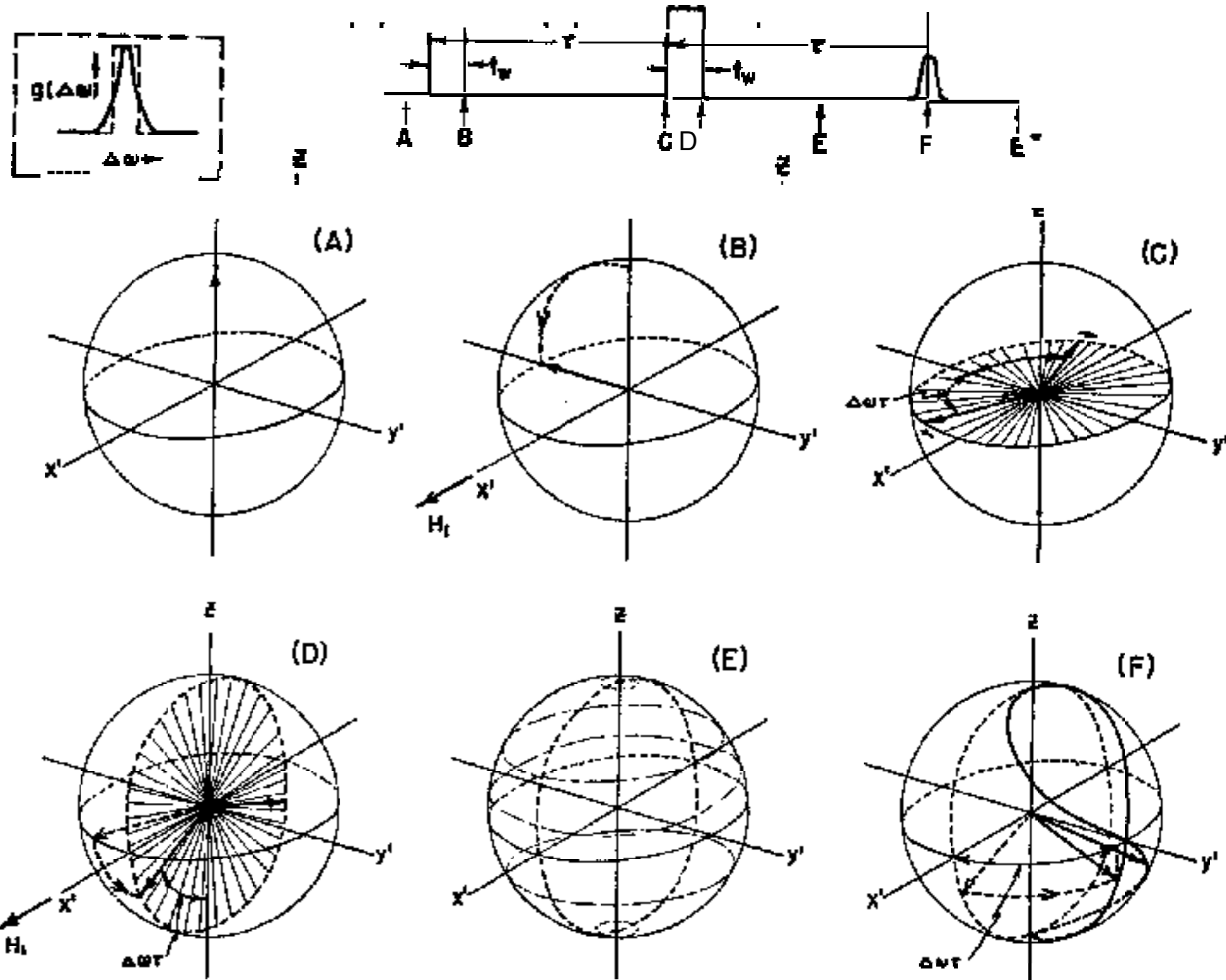


*Marko Lovric*

# Erwin Hahn

# Bits of History

## 1950@Berkeley



# Bits of History

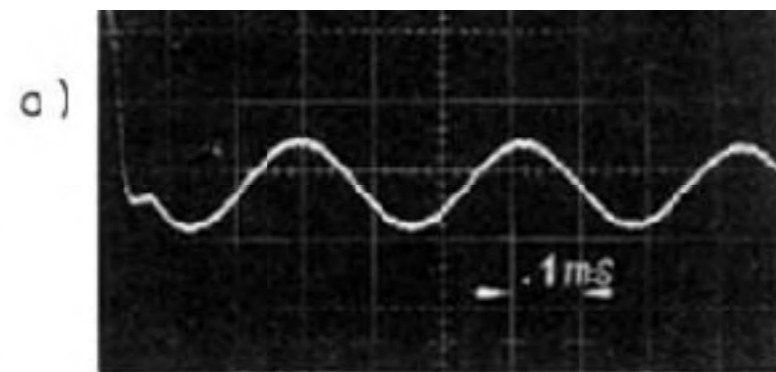
APPROACH TO HIGH-RESOLUTION nmr IN SOLIDS\*

1968@MIT

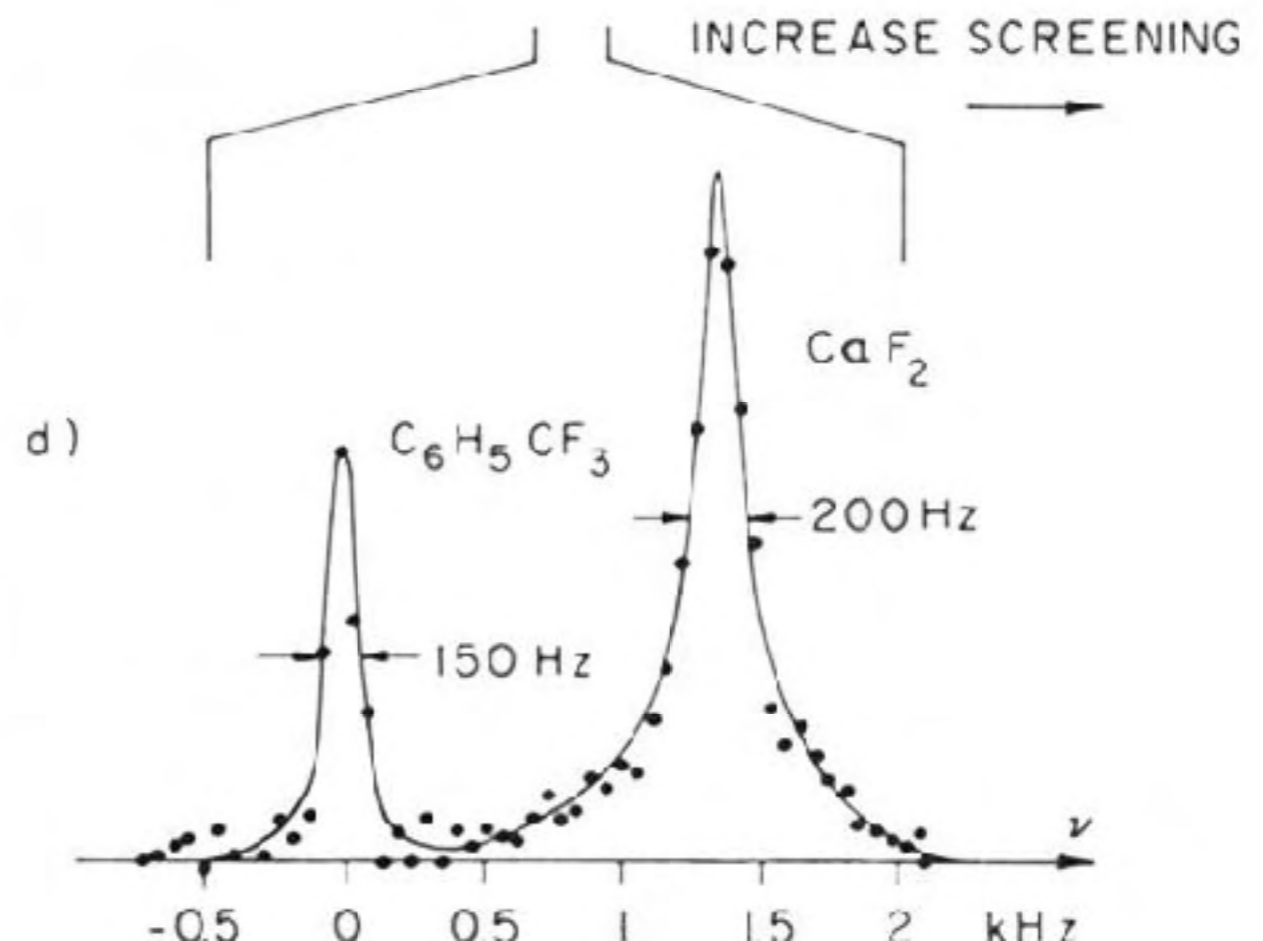
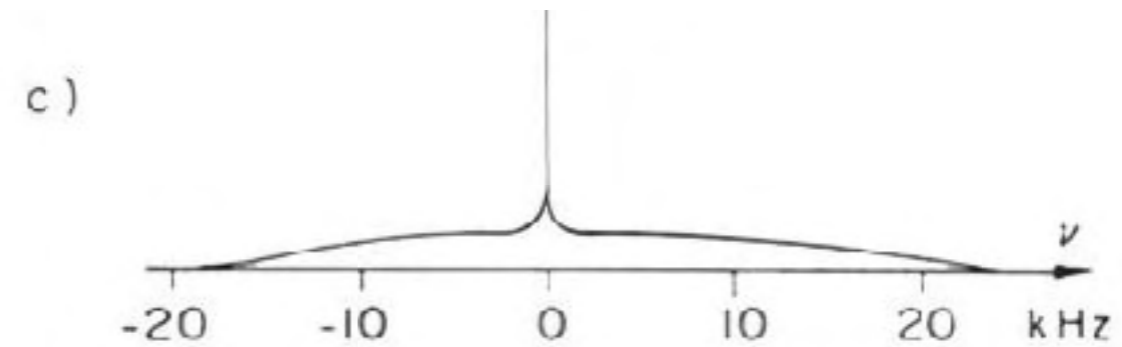
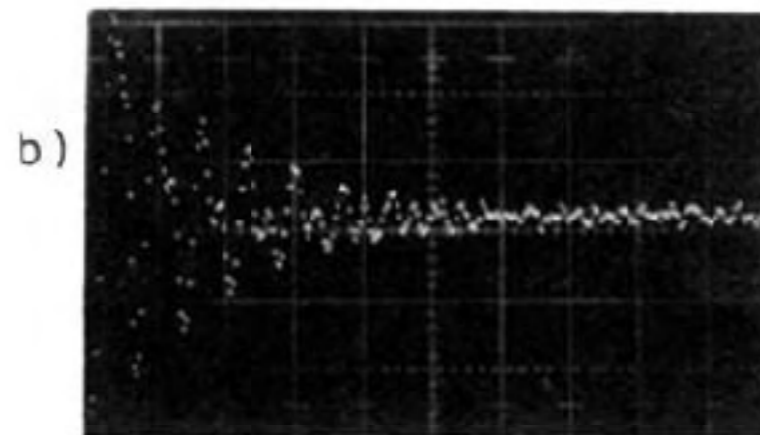
J. S. Waugh, L. M. Huber, and U. Haeberlen†

Department of Chemistry and Research Laboratory of Electronics,  
Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

(Received 27 December 1967)



100  $\mu$  sec / cm



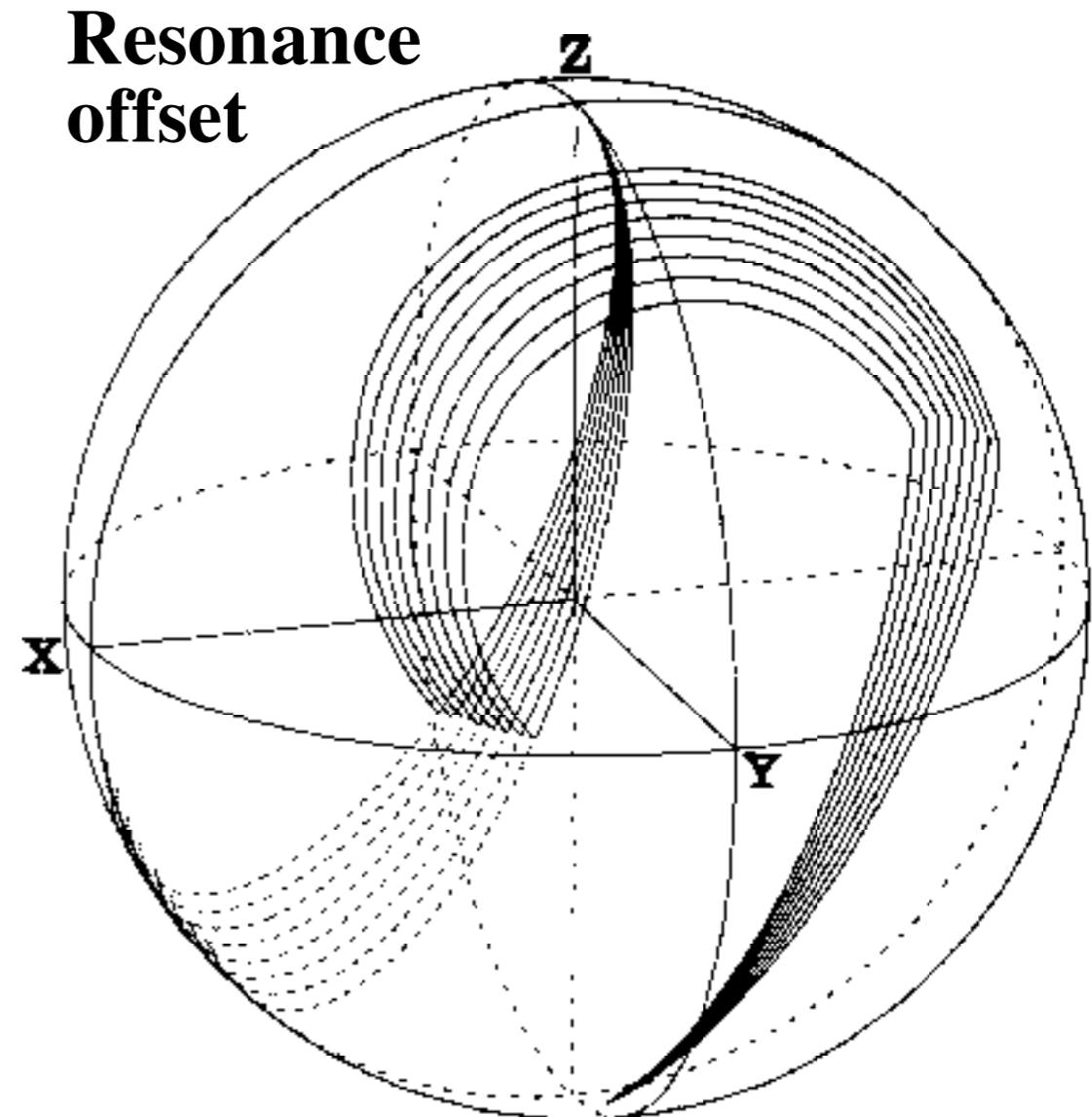
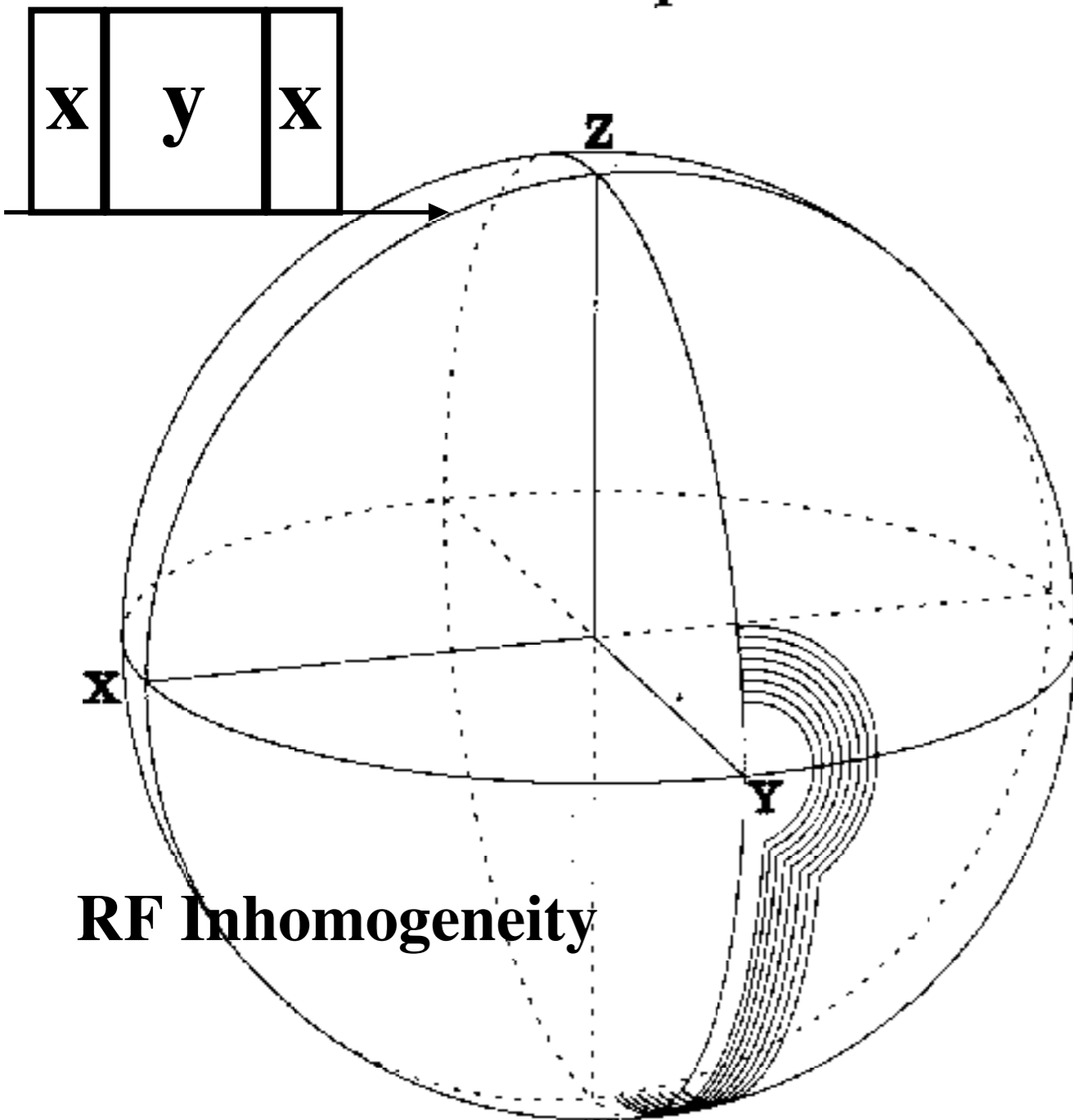
# Composite Pulses

1979@Oxford

JOURNAL OF MAGNETIC RESONANCE 33, 473-476 (1979)

## NMR Population Inversion Using a Composite Pulse

MALCOLM H. LEVITT  
RAY FREEMAN



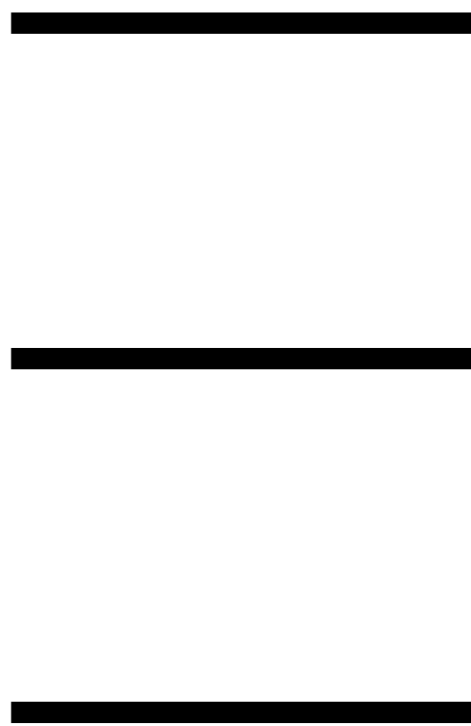
# Larger Systems

Before: 2 levels



Spin 1/2  
 $^1\text{H}$

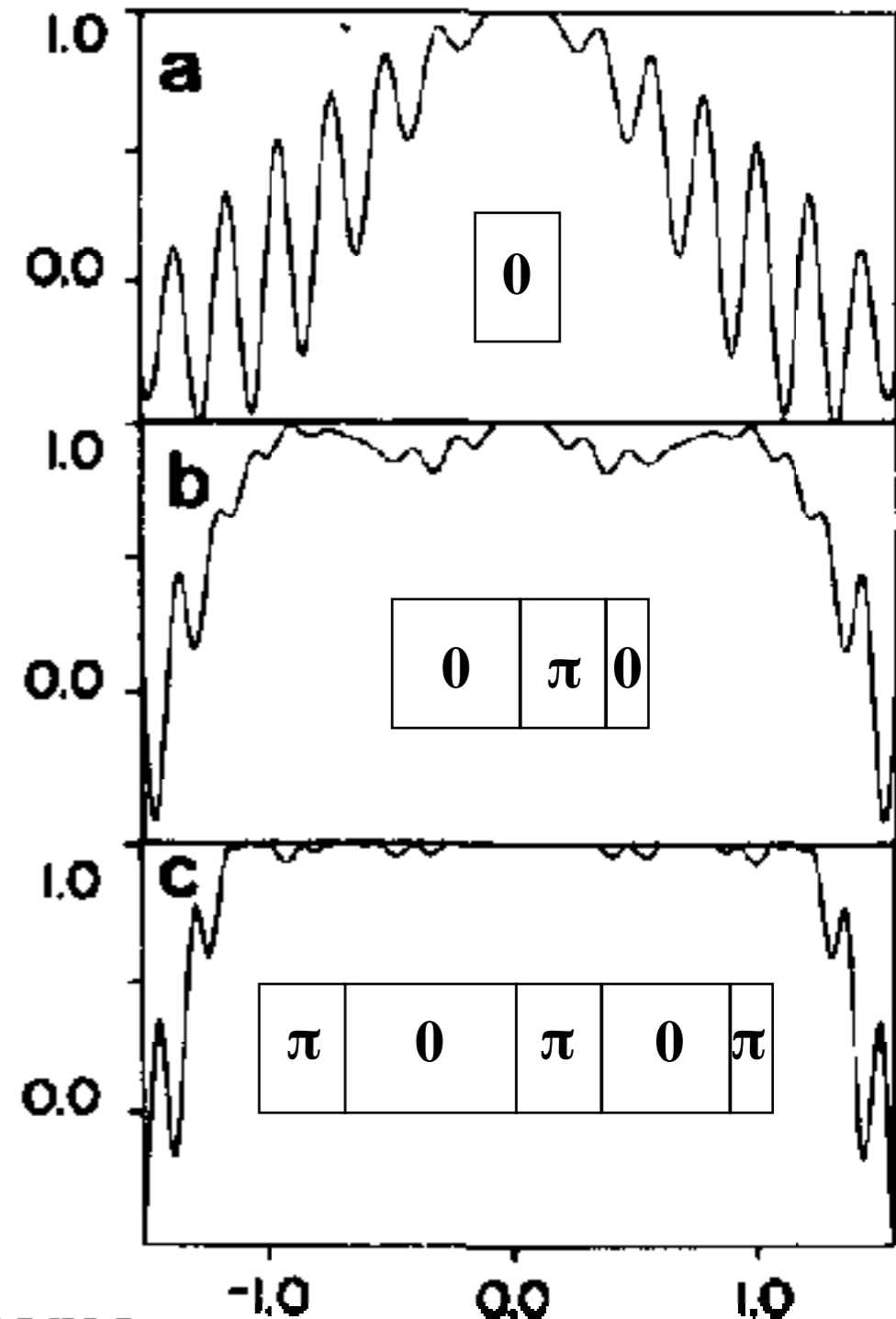
3 levels



Spin 1  
 $^2\text{D}$

$\langle I_y \rangle$

1984@Zürich



Composite pulse excitation in three-level systems

M. H. Levitt, D. Suter, and R. R. Ernst

*J. Chem. Phys.* 80, 3064 (1984).  $\omega_Q/\omega_1$

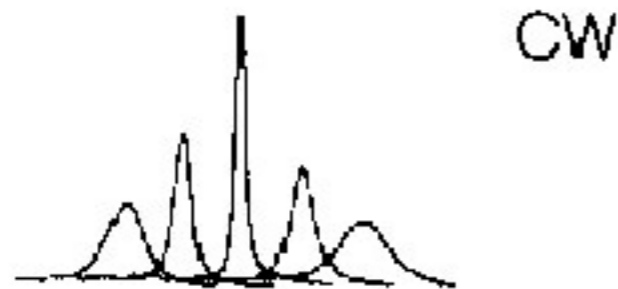
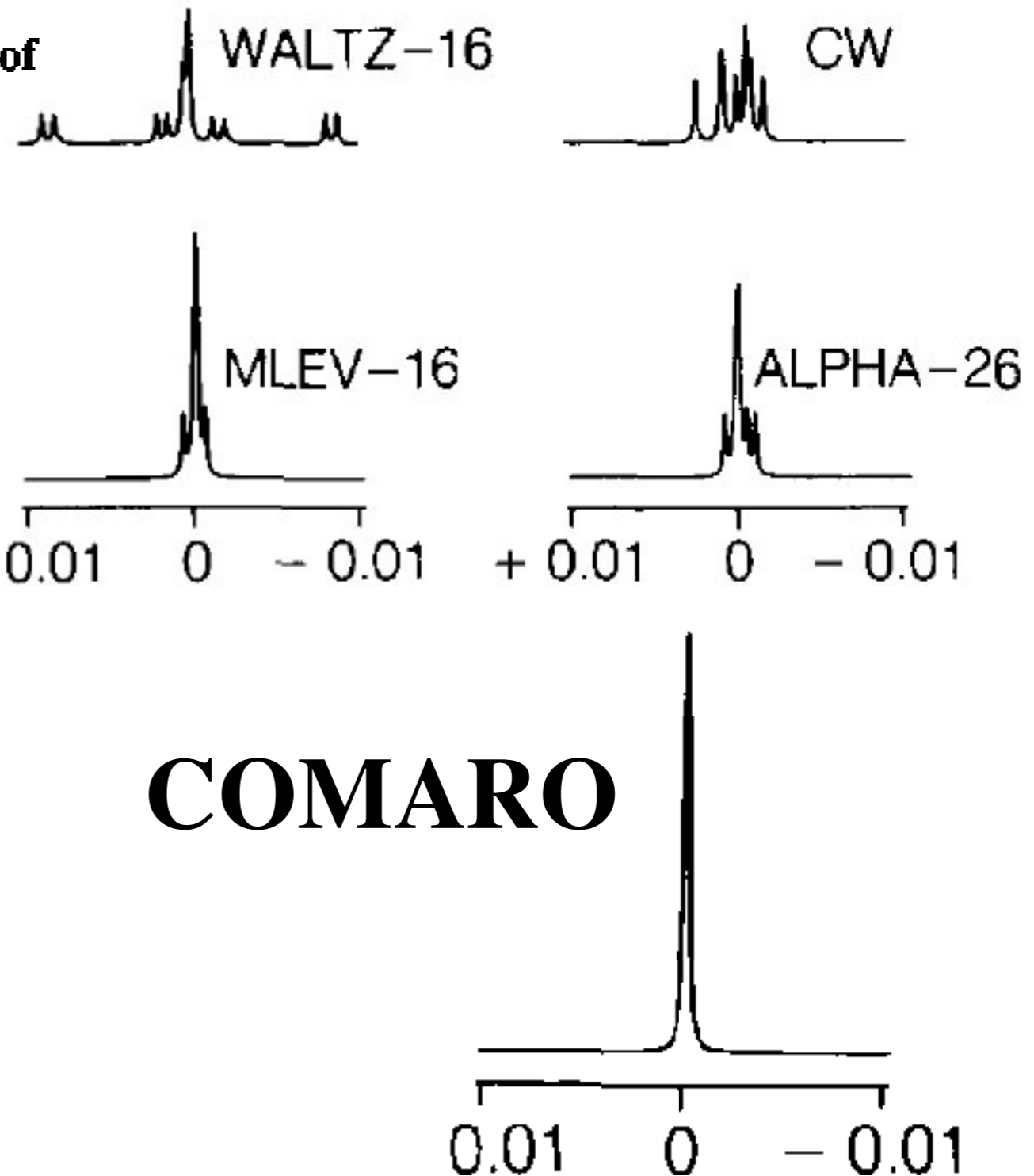
# Larger Systems

## Multiple Spins Multiple Interactions

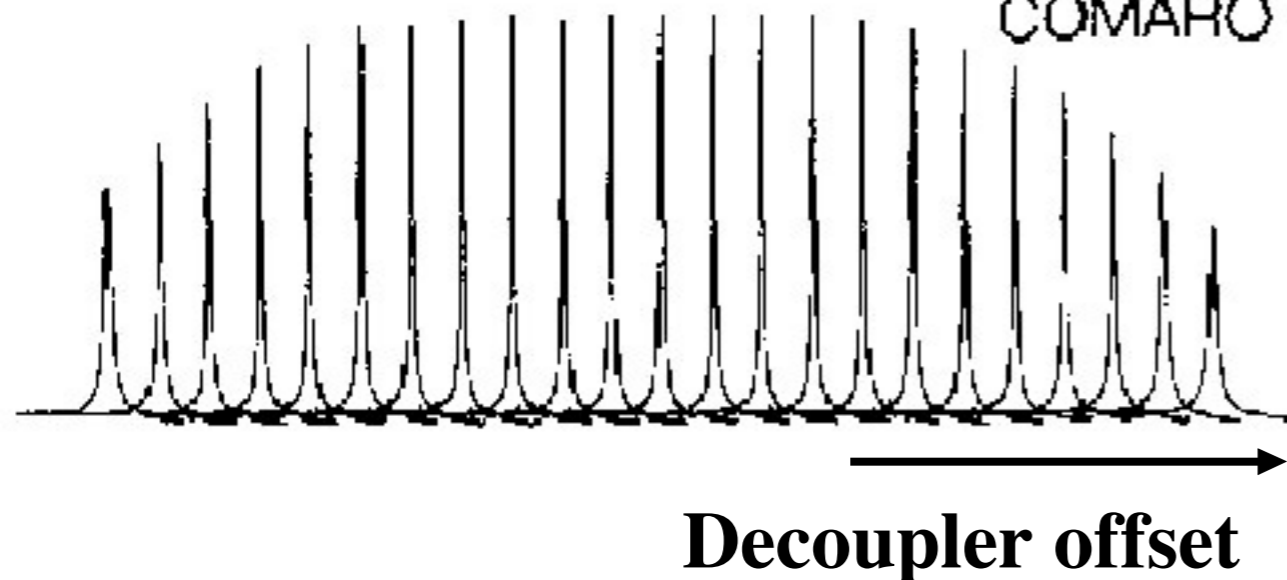
1987@Berkeley

Broadband Heteronuclear Decoupling in the Presence of  
Homonuclear Dipolar and Quadrupolar Interactions

K. V. SCHENKER, D. SUTER, AND A. PINES



COMARO - 2



# 1st Conclusion

---

**Quantum Control =  
Teaching spins new tricks**



**... even in the presence of distraction**



# NMR Quantum Computing

**Spins  
inside**

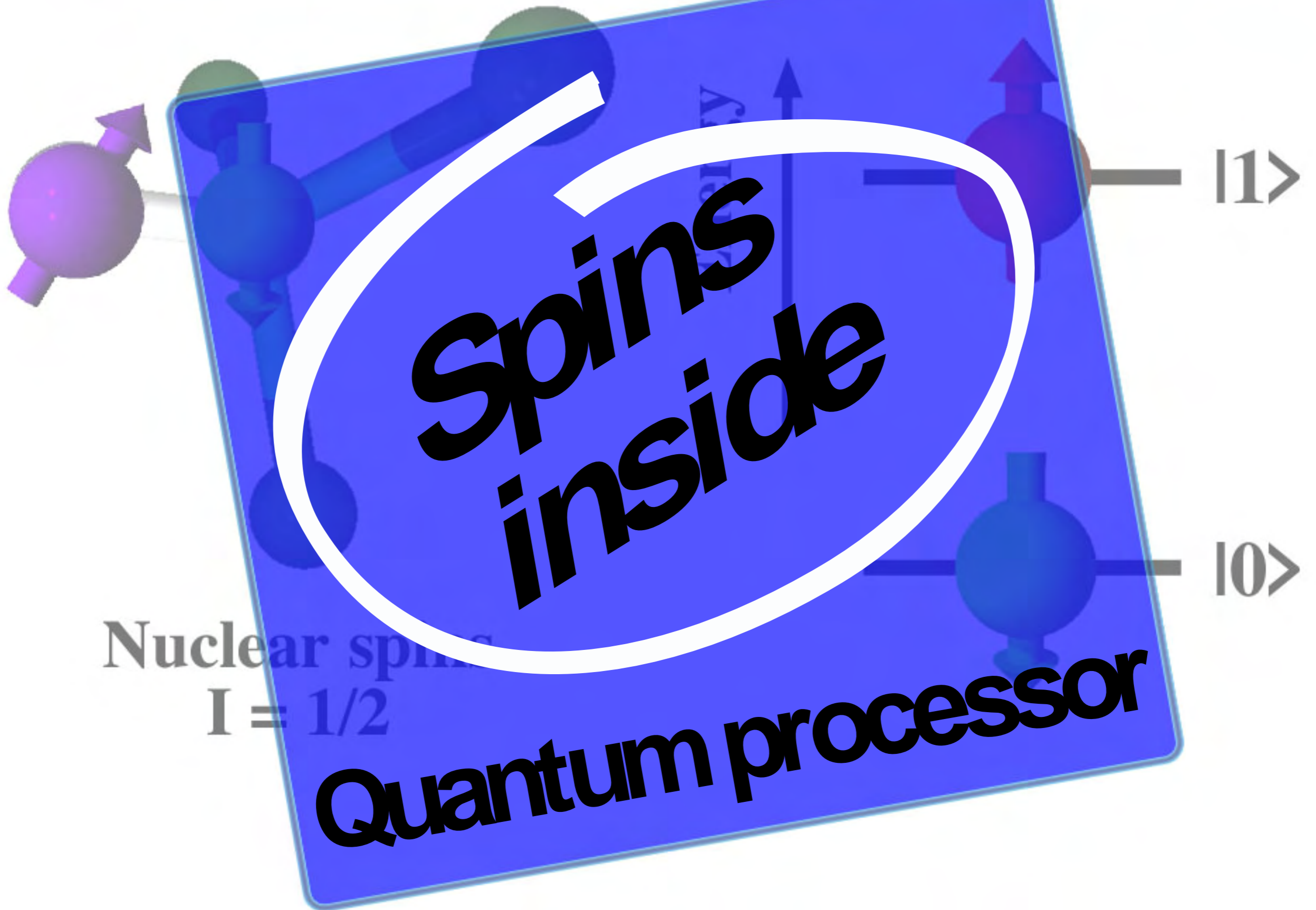
Nuclear spins

$$I = 1/2$$

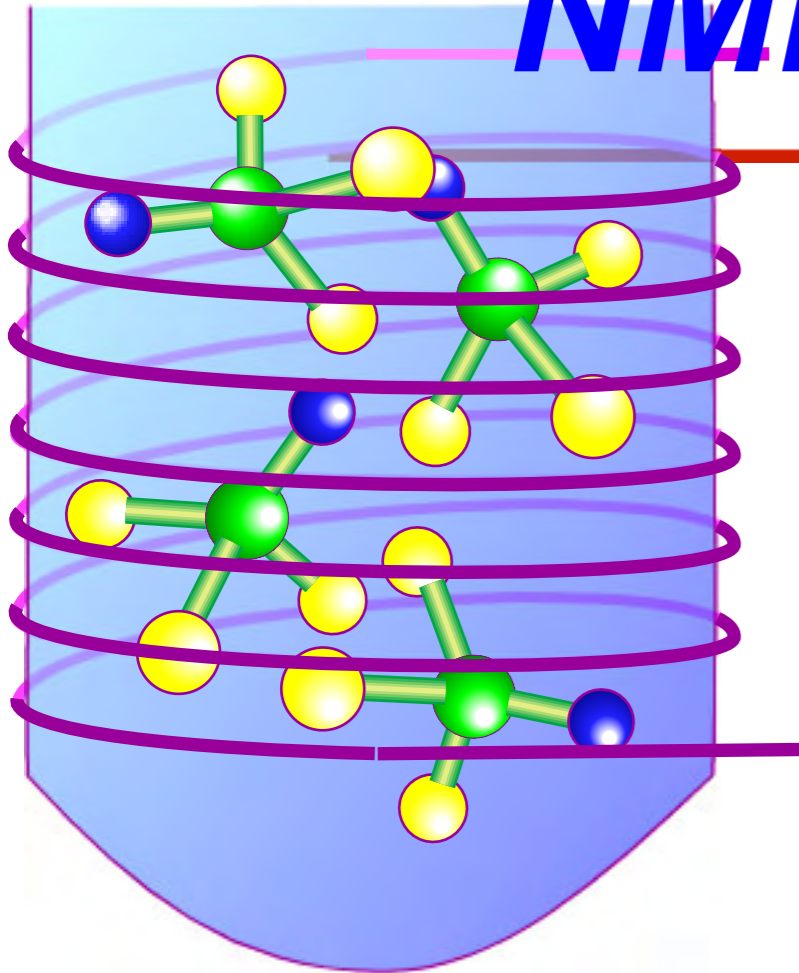
**Quantum processor**

$|1\rangle$

$|0\rangle$

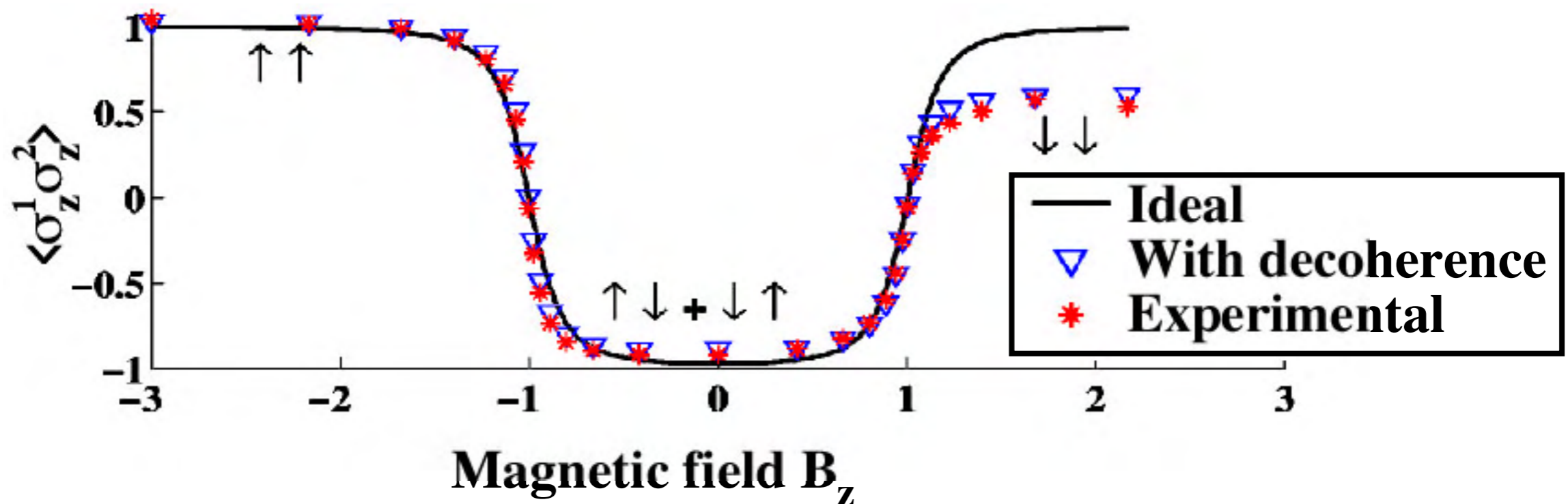


# NMR Quantum Computing

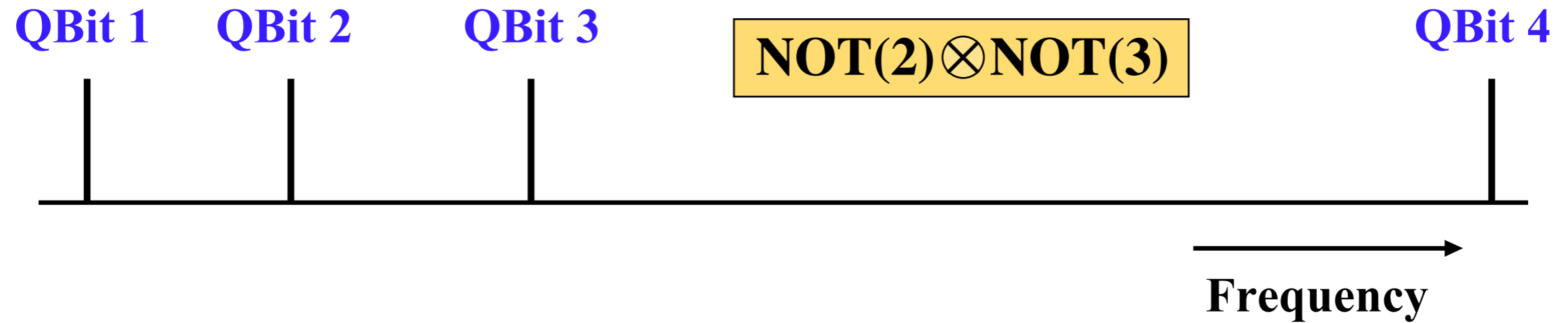


- **Liquid state NMR is an excellent system for small quantum registers.**

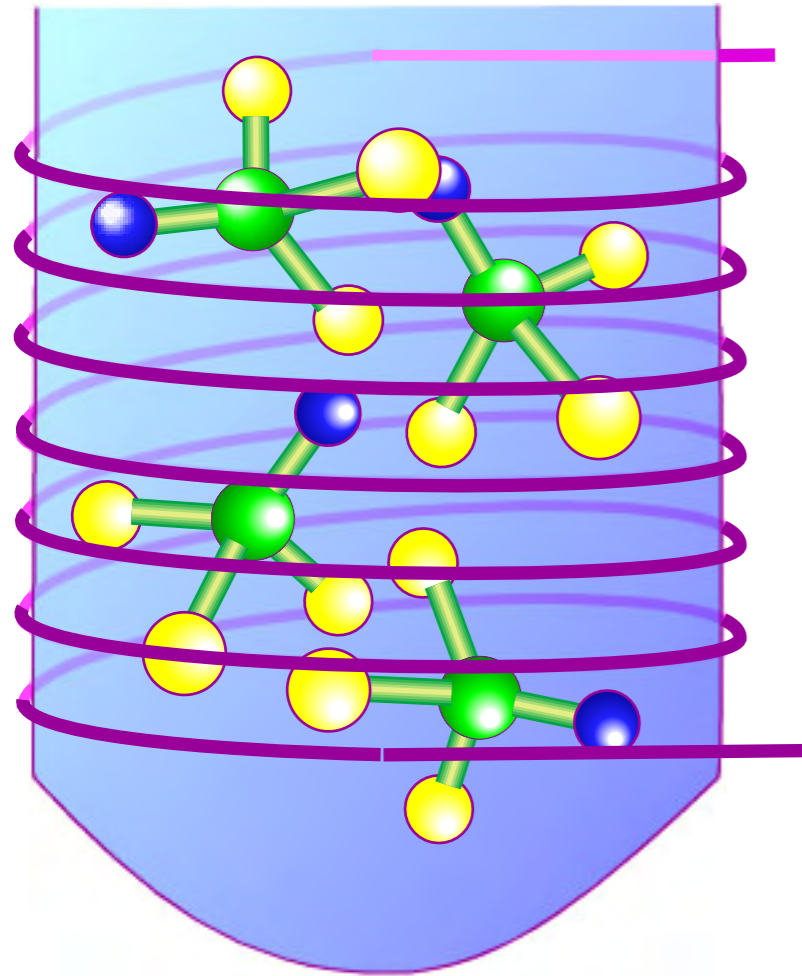
**e.g. Simulation of Quantum Phase Transition**



# *NMR Quantum Computing*



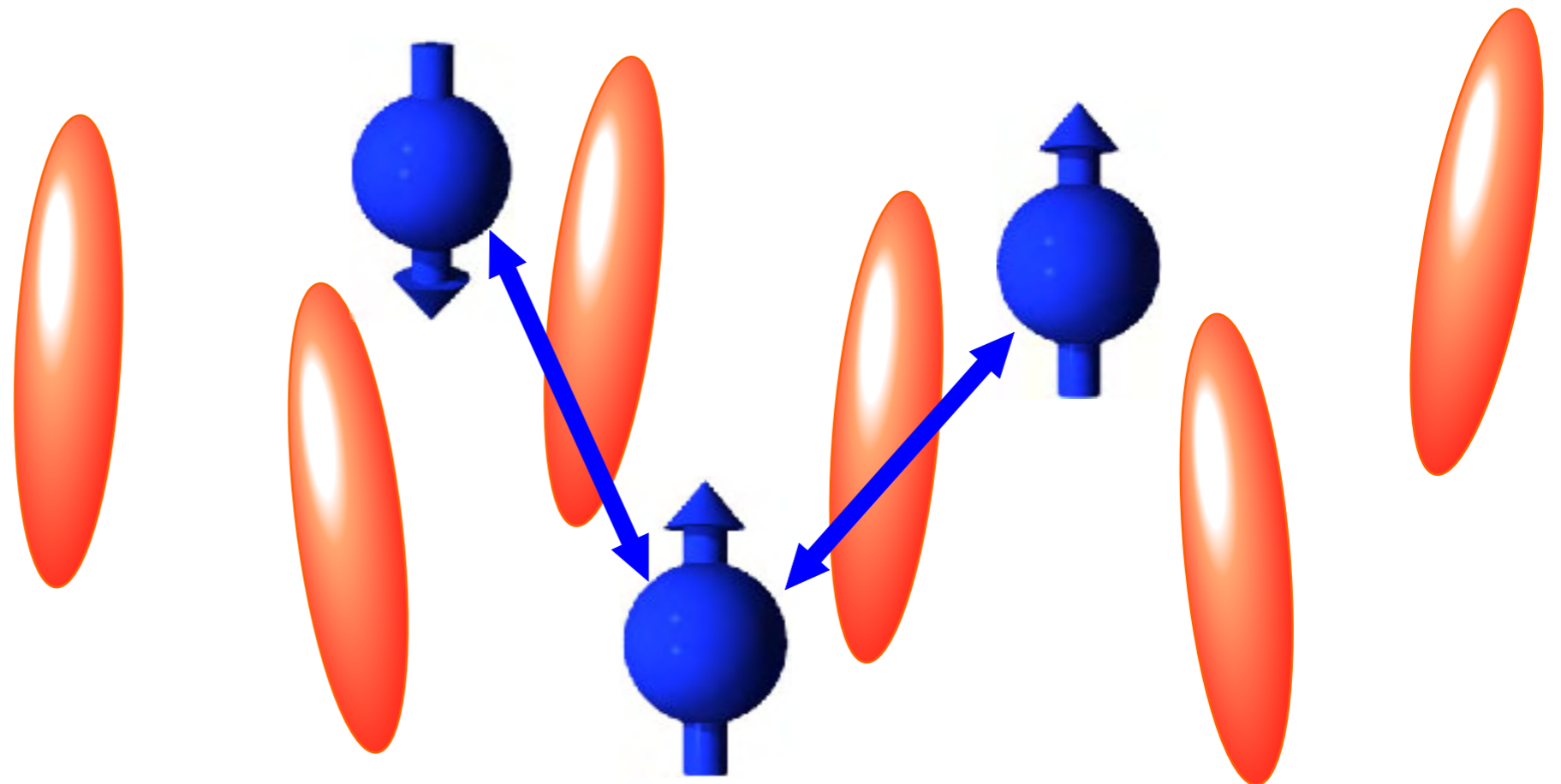
# Liquid Crystal NMR



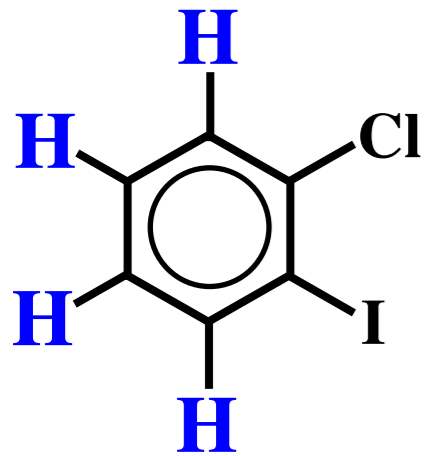
**Liquids are simple, easy to handle**

**Main problem: couplings are weak ( $\sim 10$  Hz)**

**Stronger couplings  
in liquid crystals :  $\sim 1$  kHz**



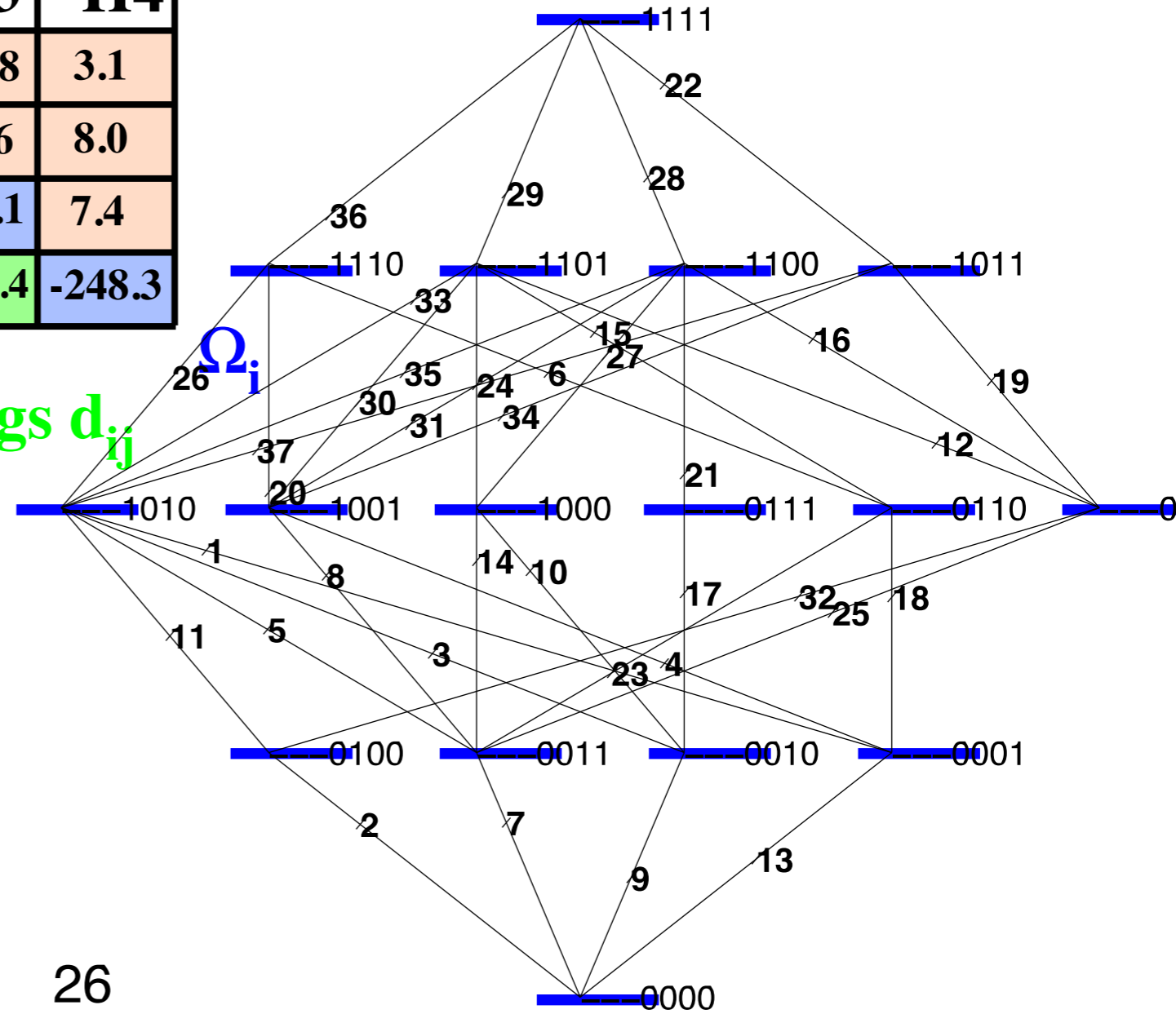
# Dipolar Coupled System



in ZLI-1132

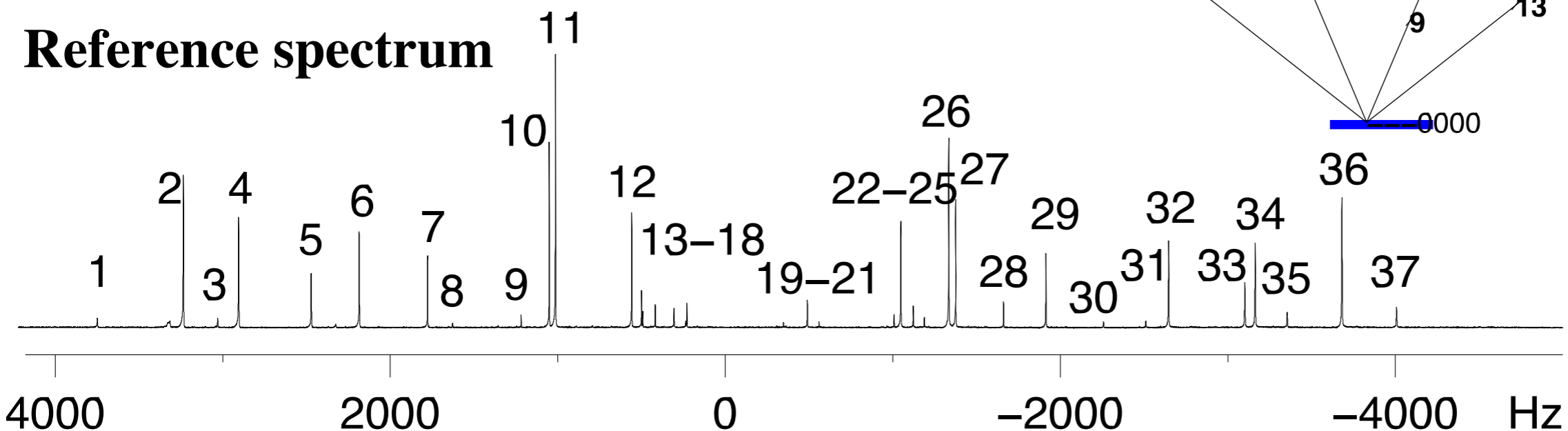
|    | H1     | H2     | H3      | H4     |
|----|--------|--------|---------|--------|
| H1 | -303.7 | 7.7    | 0.8     | 3.1    |
| H2 | -788.0 | -3.5   | 7.6     | 8.0    |
| H3 | 85.7   | -278.5 | -208.1  | 7.4    |
| H4 | 71.0   | -667.2 | -1873.4 | -248.3 |

dipolar couplings  $d_{ij}$



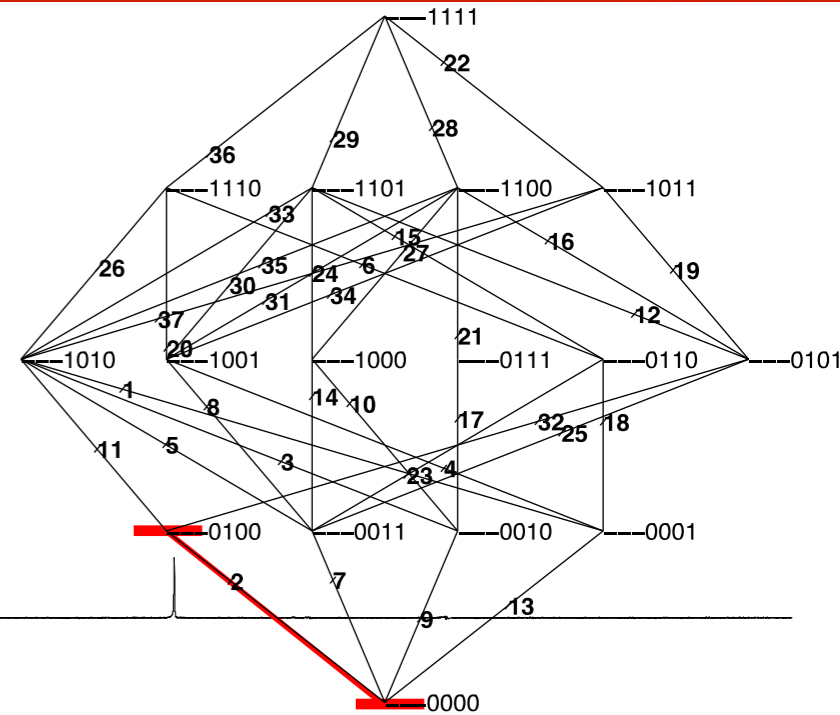
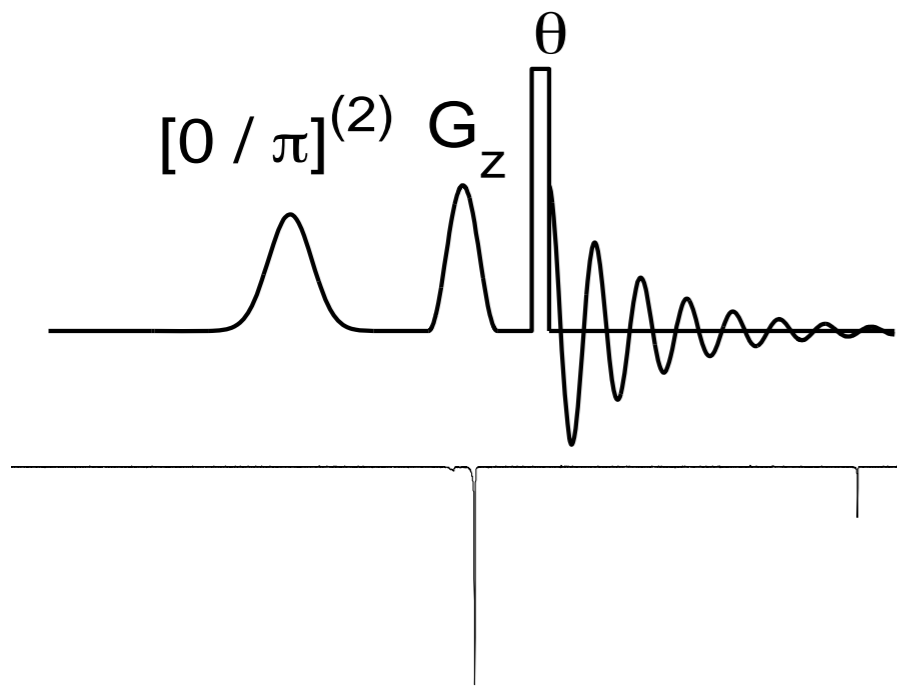
How do we implement quantum gates ?

Reference spectrum



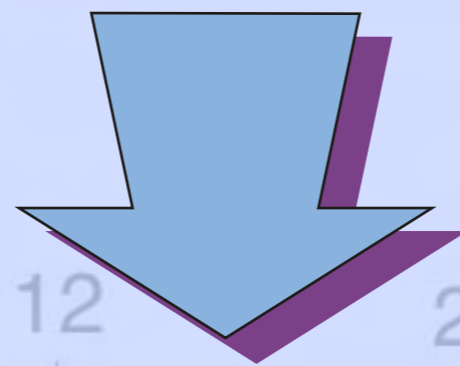
# Gate Operations

e.g State Preparation (POPS)

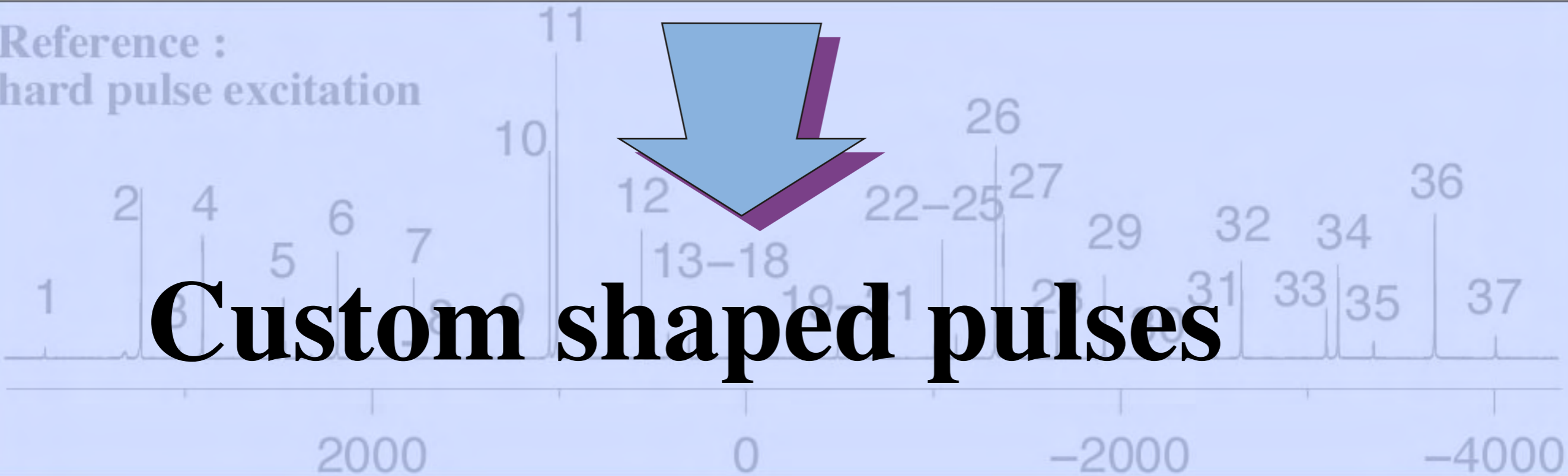


**Not possible for all transitions**

Reference :  
hard pulse excitation



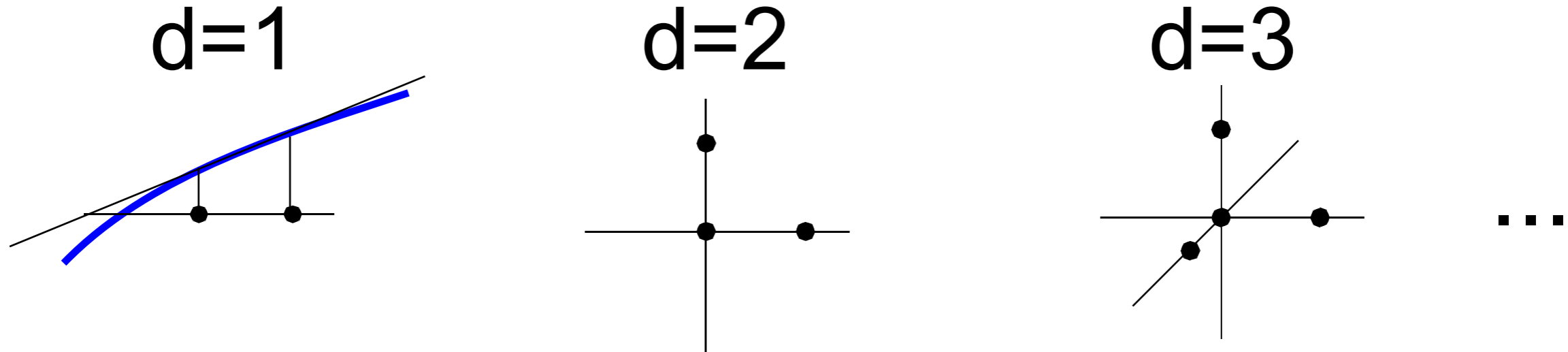
**Custom shaped pulses**



# Gradient estimation

## Classical

requires  $\geq d+1$  function evaluations in  $d$  dimensions



## Quantum gradient estimation

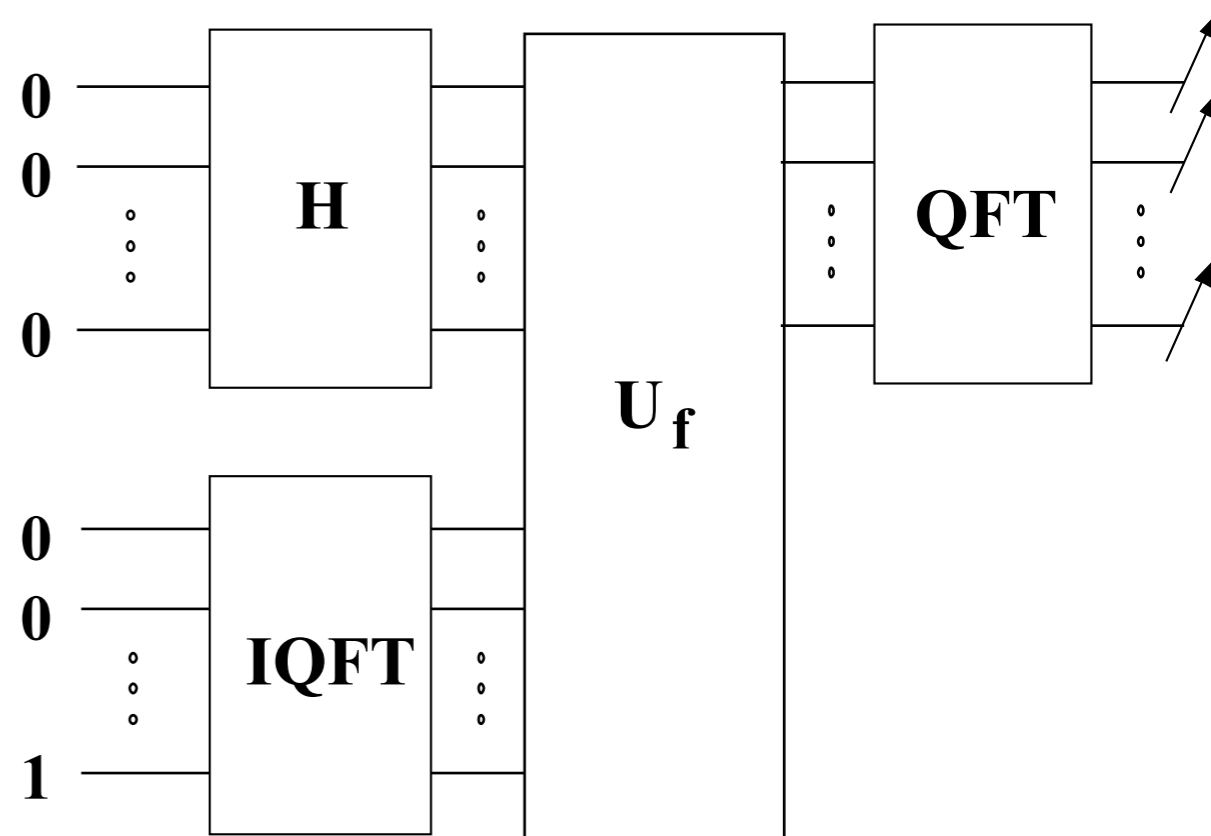
requires 1 function evaluation

*S. P. Jordan,*  
*Phys. Rev. Lett. 95, 050501 (2005).*

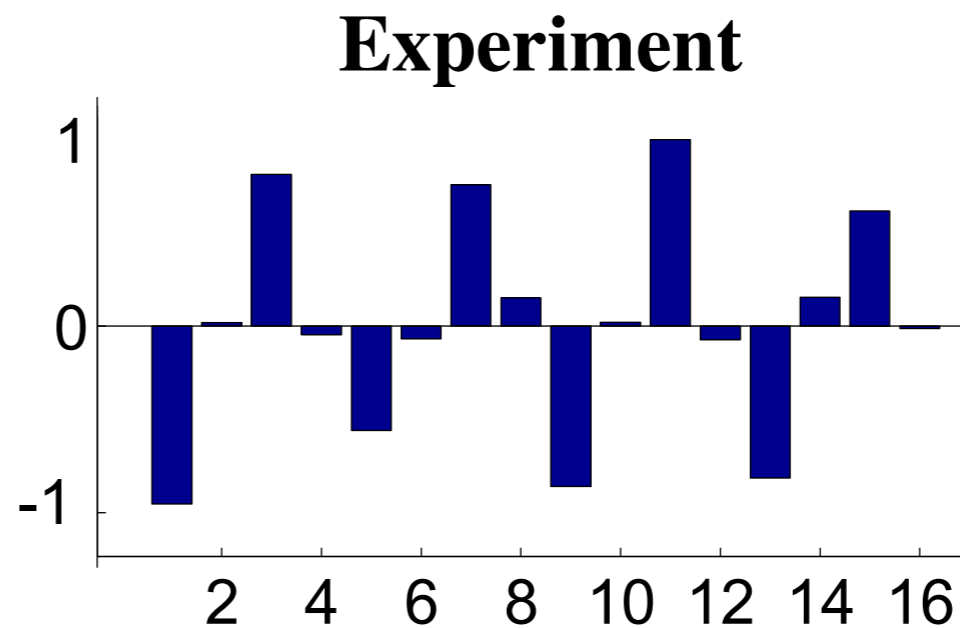
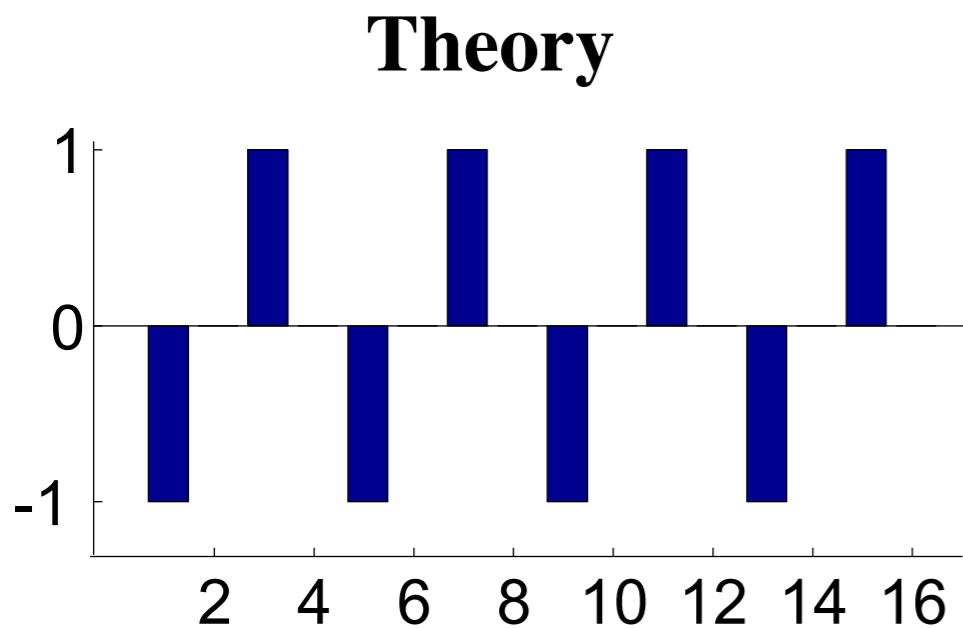
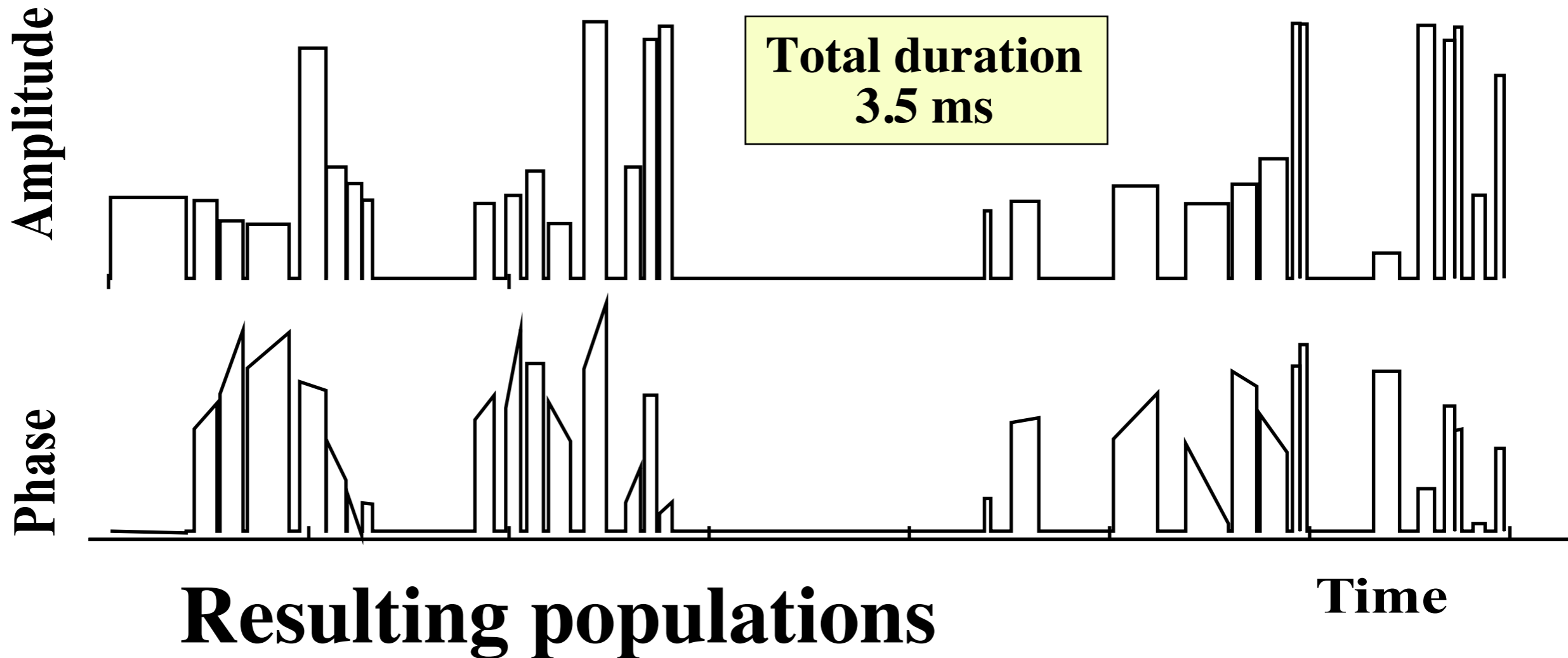
Here:  $d = 1$

Input  
register

Ancilla  
register



# Optimized Sequence

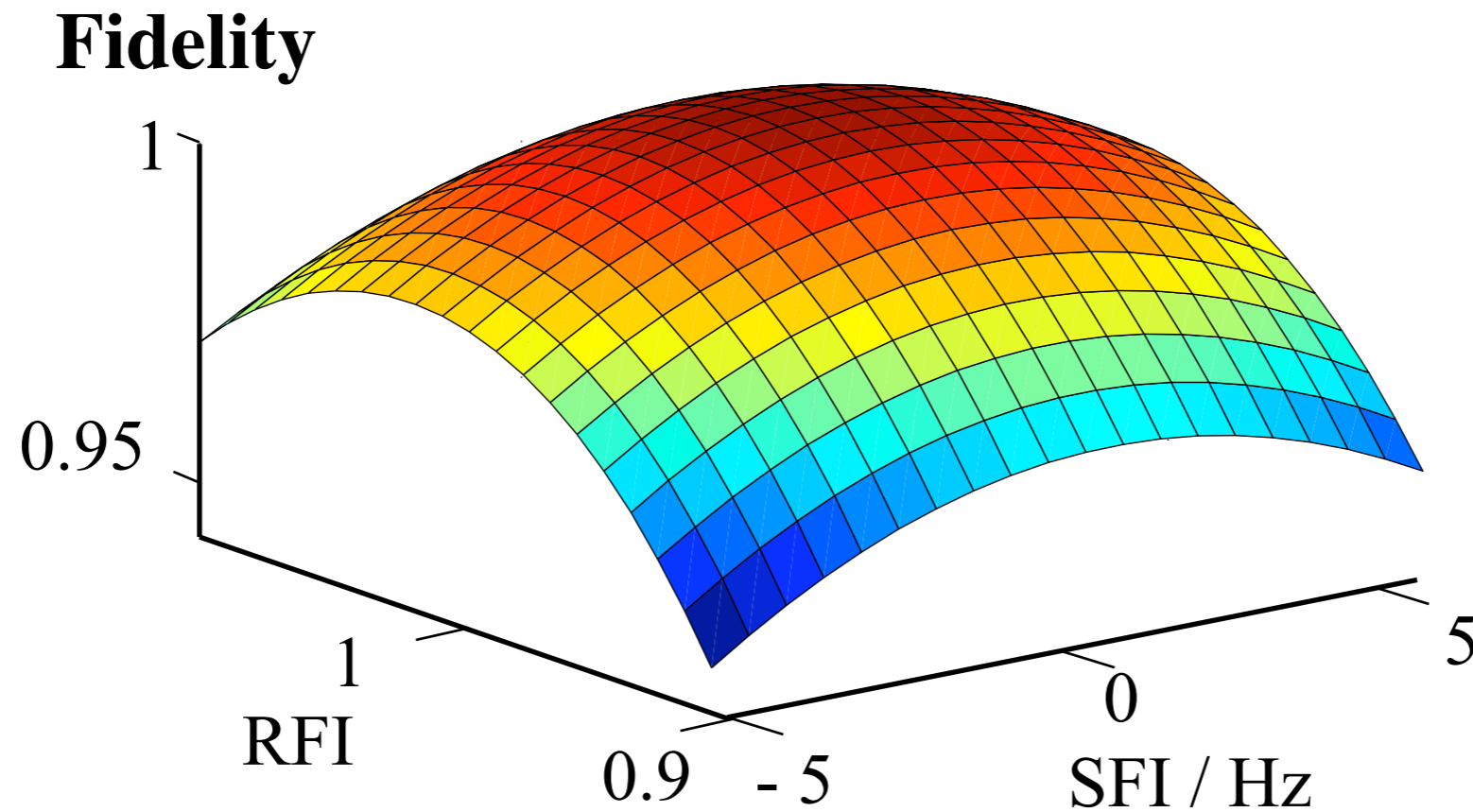
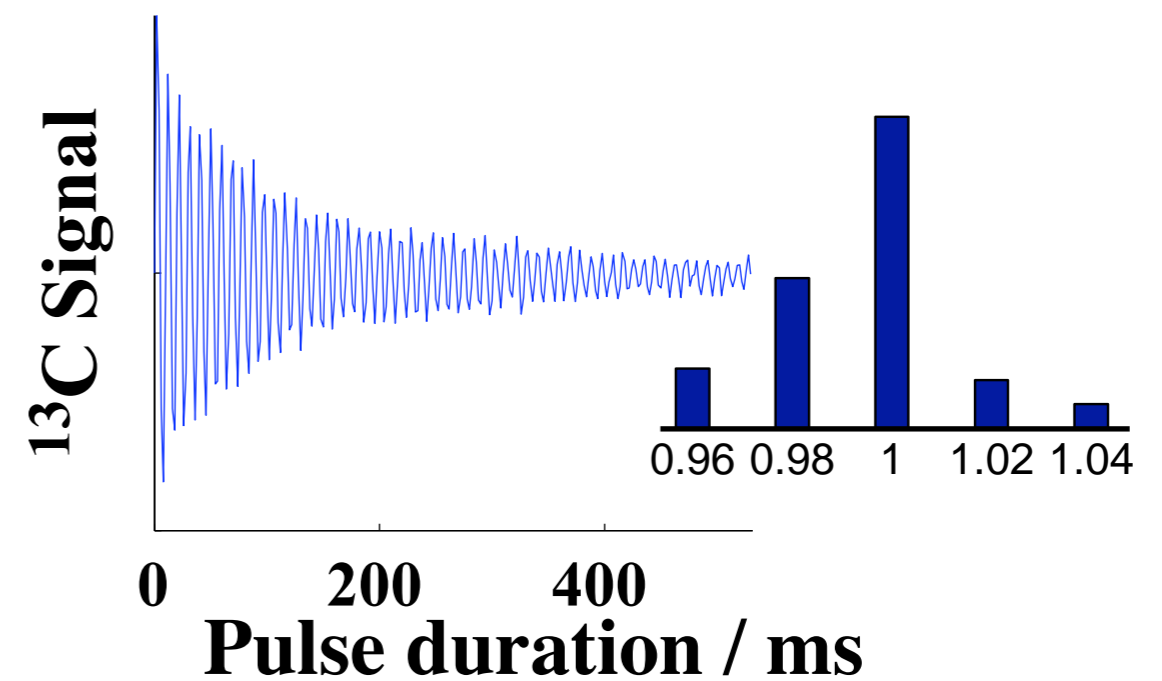
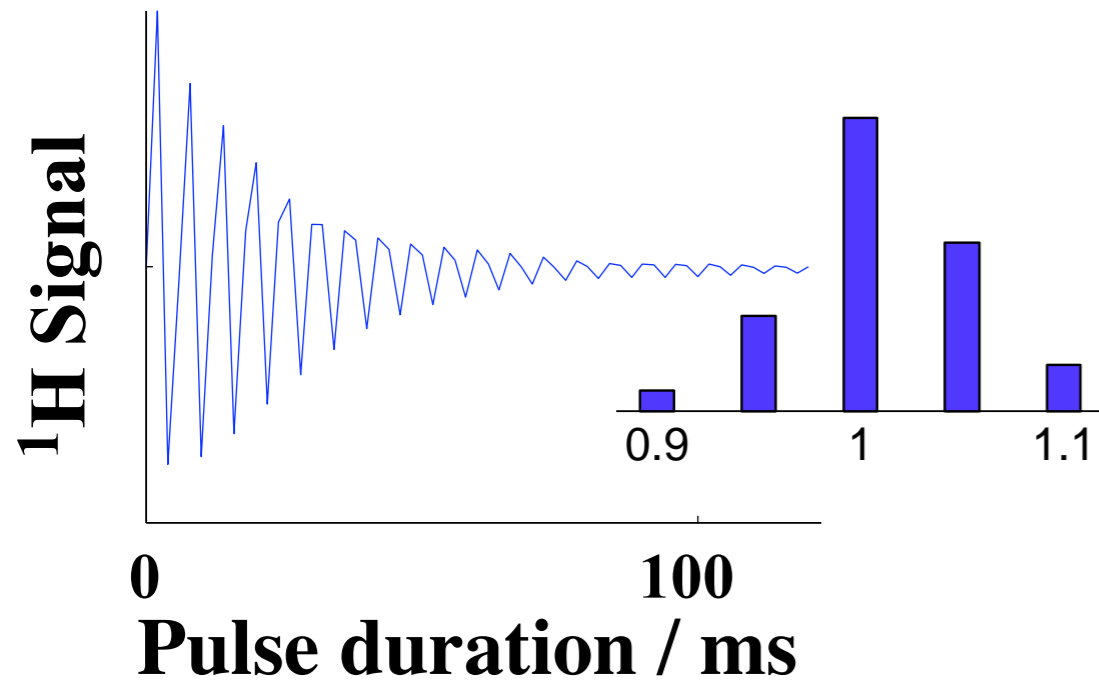


**Result :**  
Input qubits  
 $= |10\rangle$   
 $\nabla f = 2$

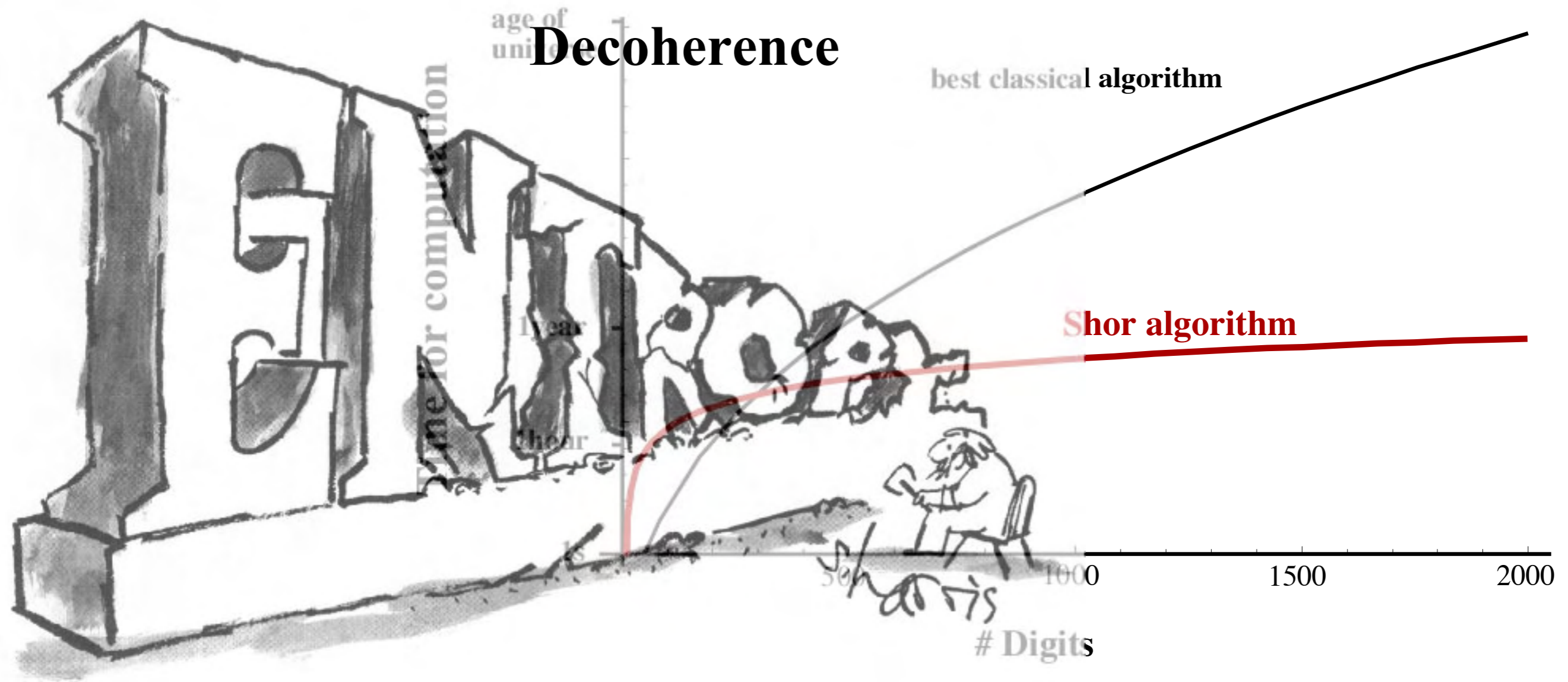


# Robustness

## RF inhomogeneity

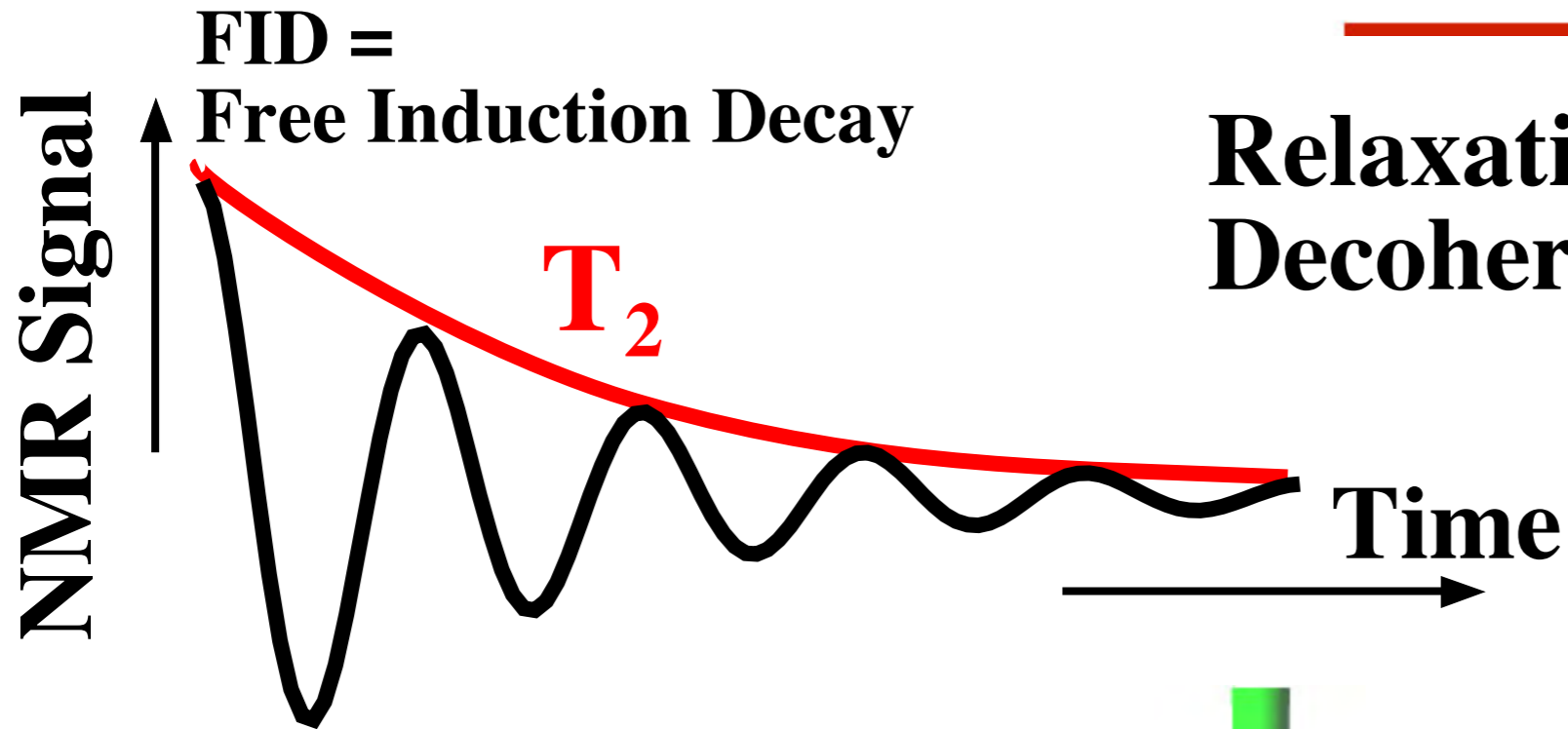


# Scalability and Decoherence

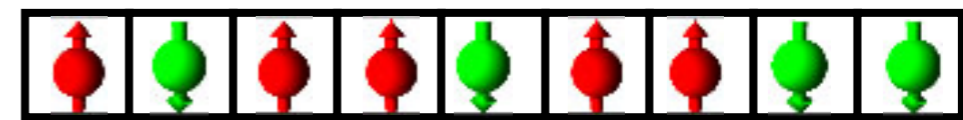
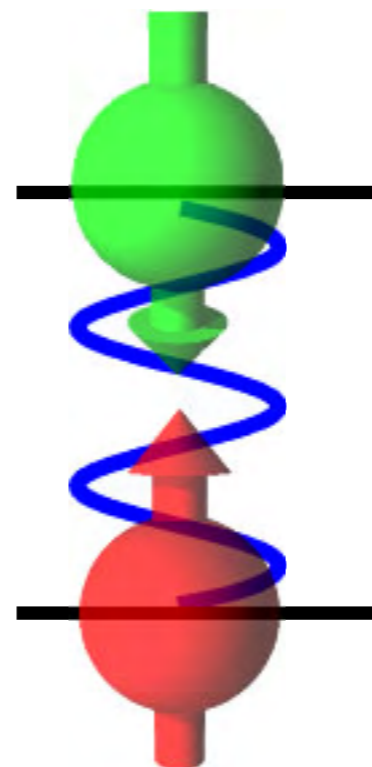


**Main source : coupling to environment**

# Decoherence



observable magnetization  
=  
single qubit coherence

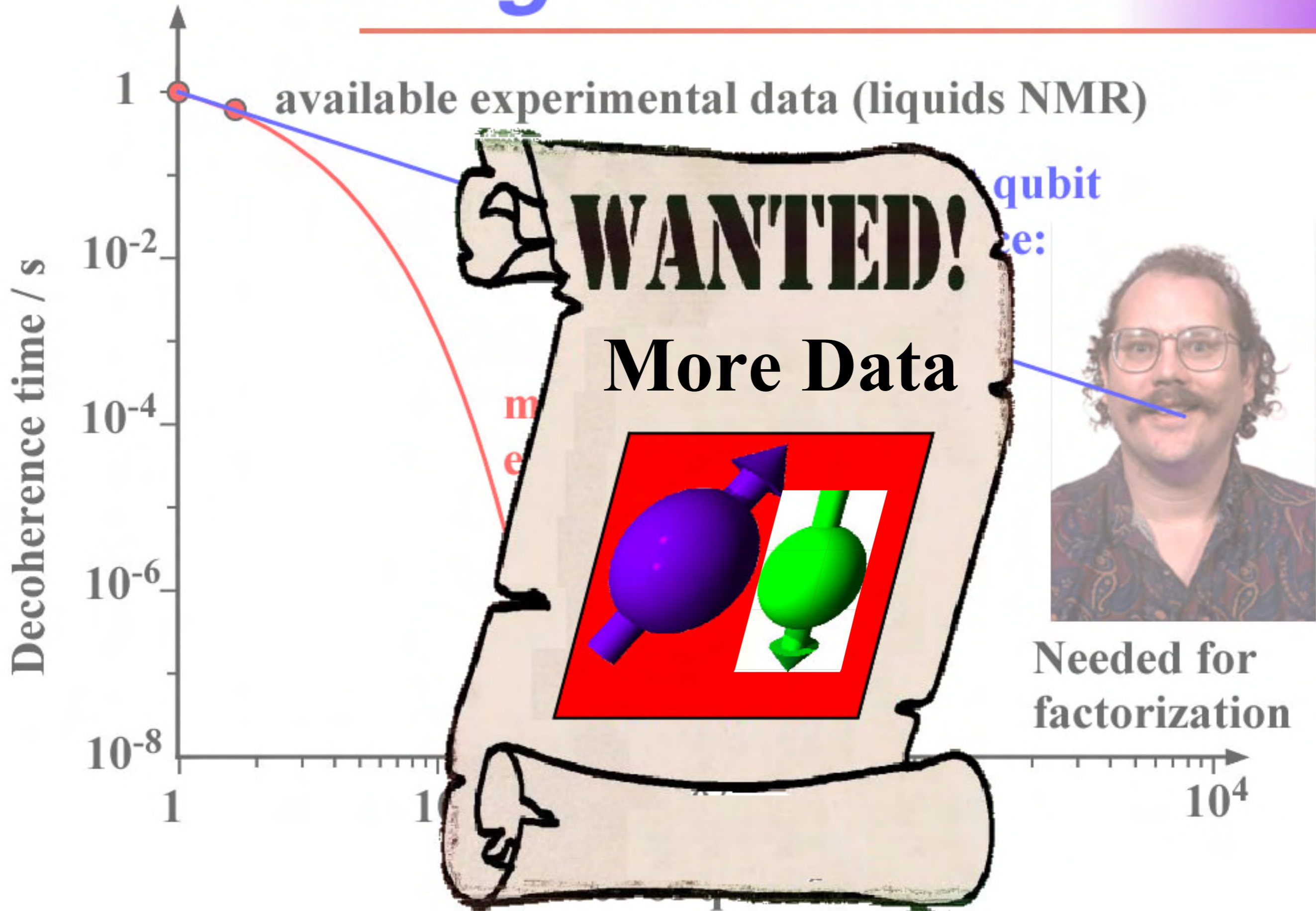


Quantum register  
involves coherence  
of many qubits

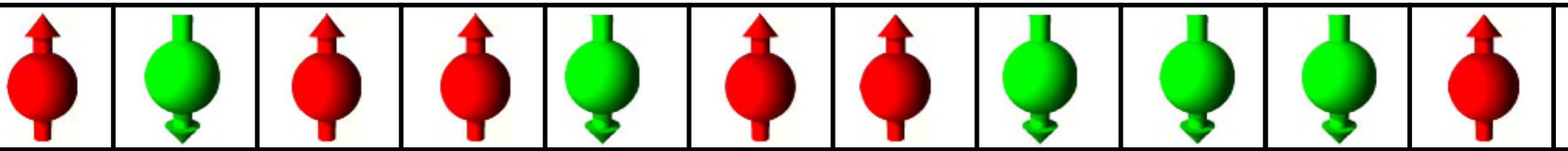
How fast will a “useful” quantum register  
lose information ?



# Scaling of Decoherence

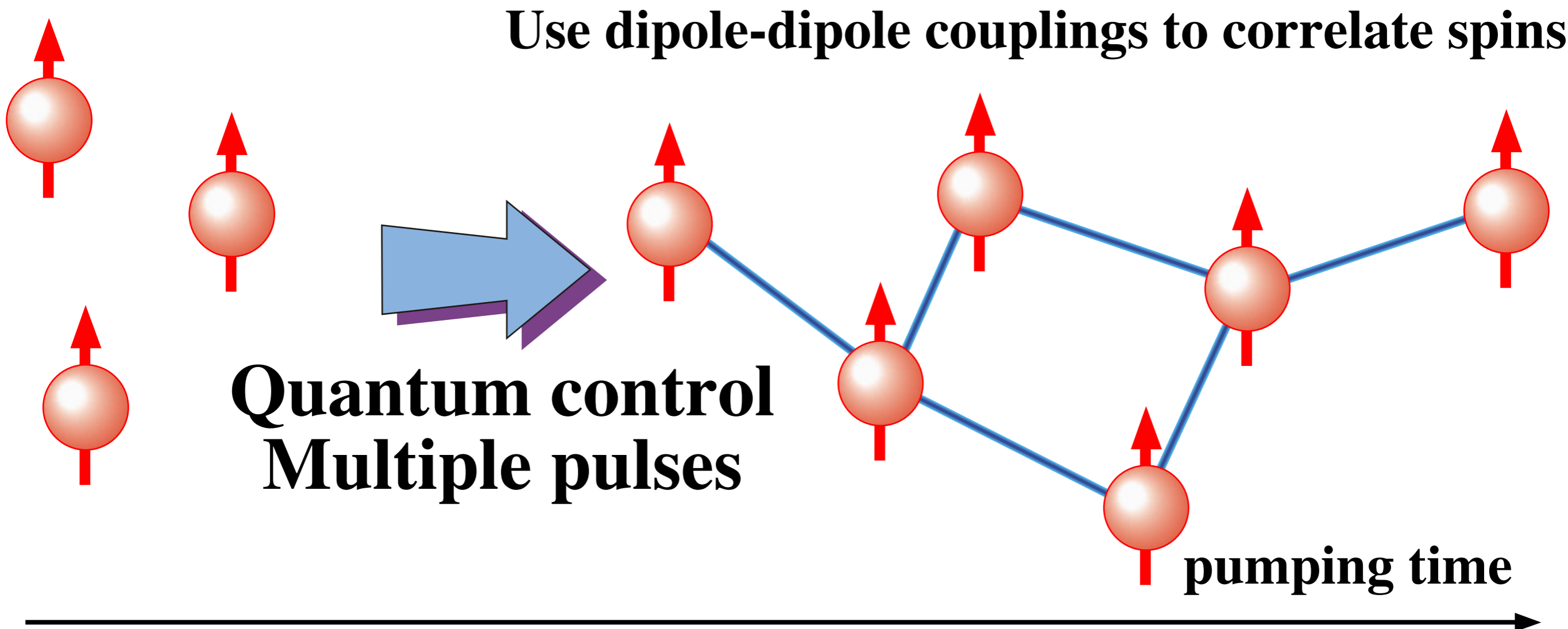


# Wide Quantum Registers

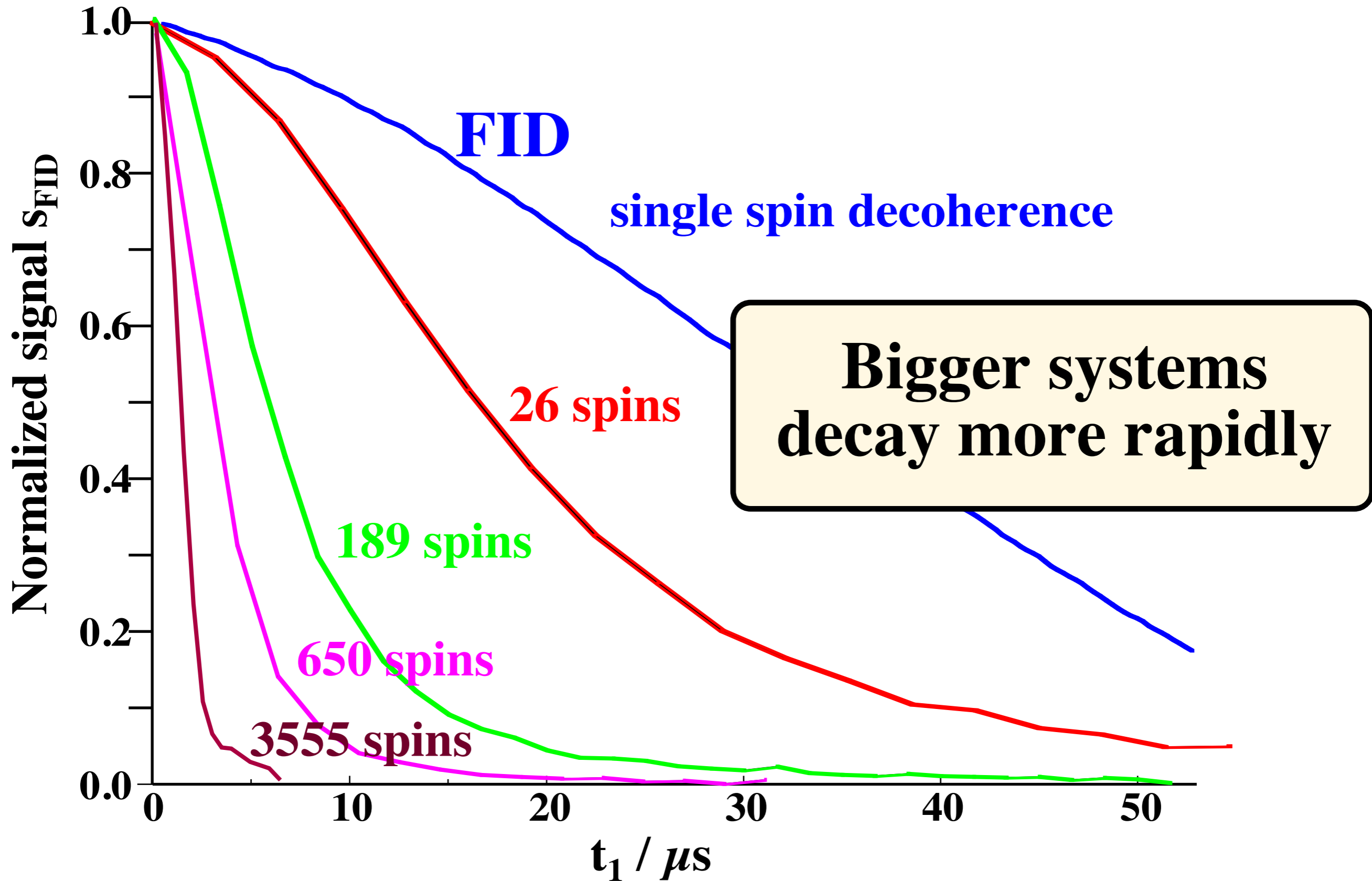


Model quantum register with 1000's of nuclear spin qubits

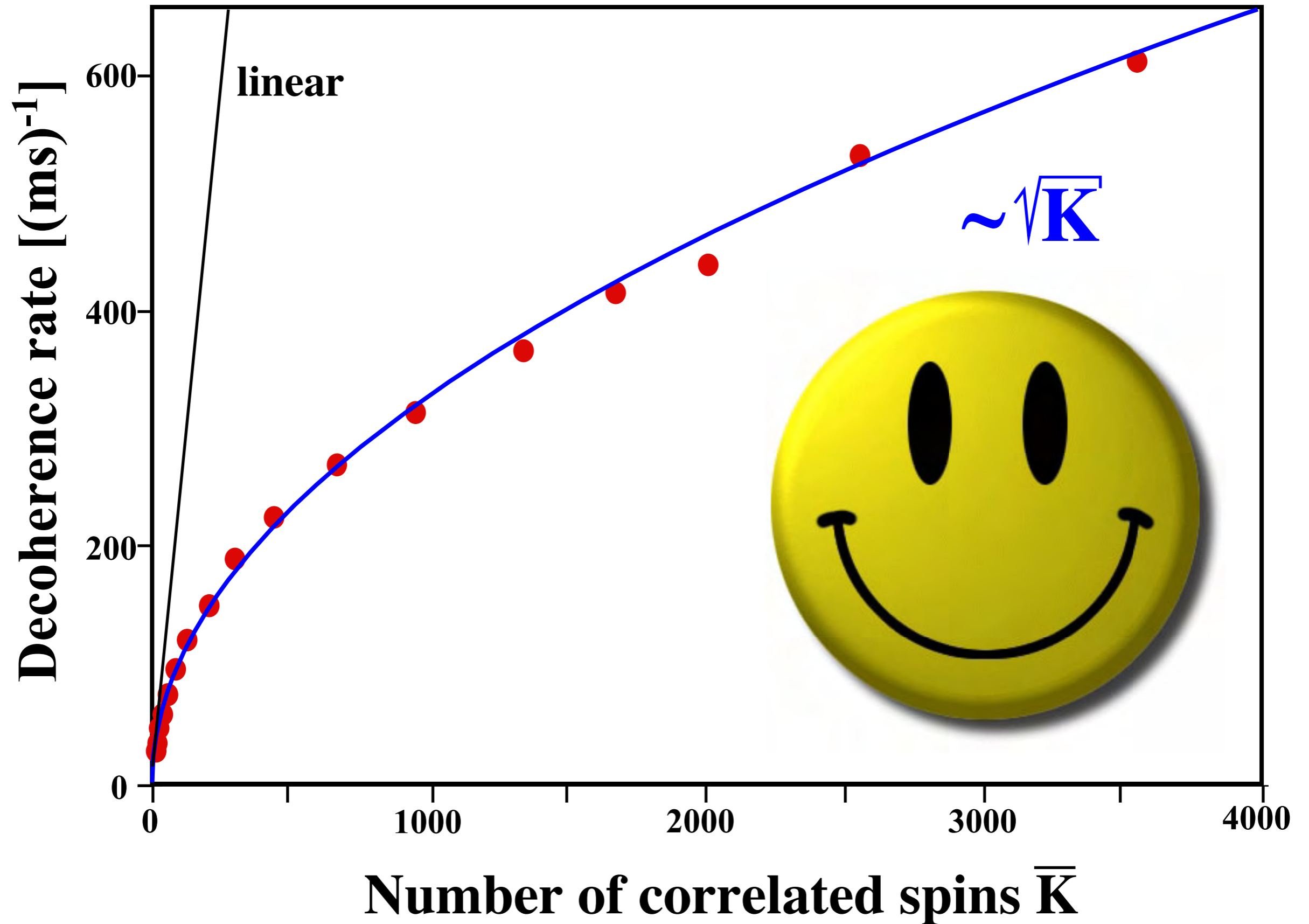
Thermal equilibrium: independent spins



# Observed Decays



# Decoherence Rates



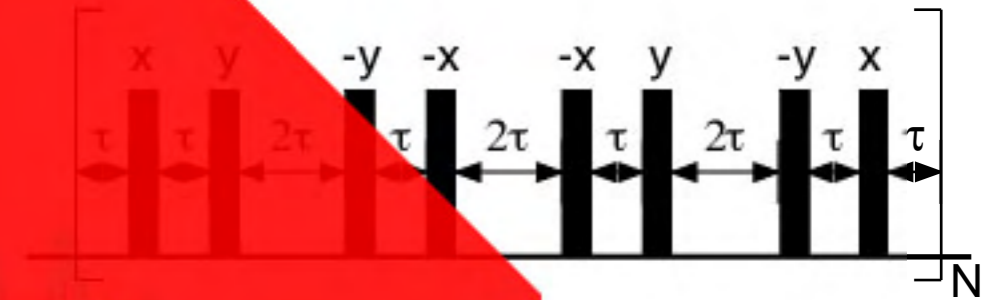
# Can We Reduce Decoherence ?

**Goal:**

**Bath**



**Idea:**  
modulate coupling with bath



average = 0

**STOP**

**Decoherence**

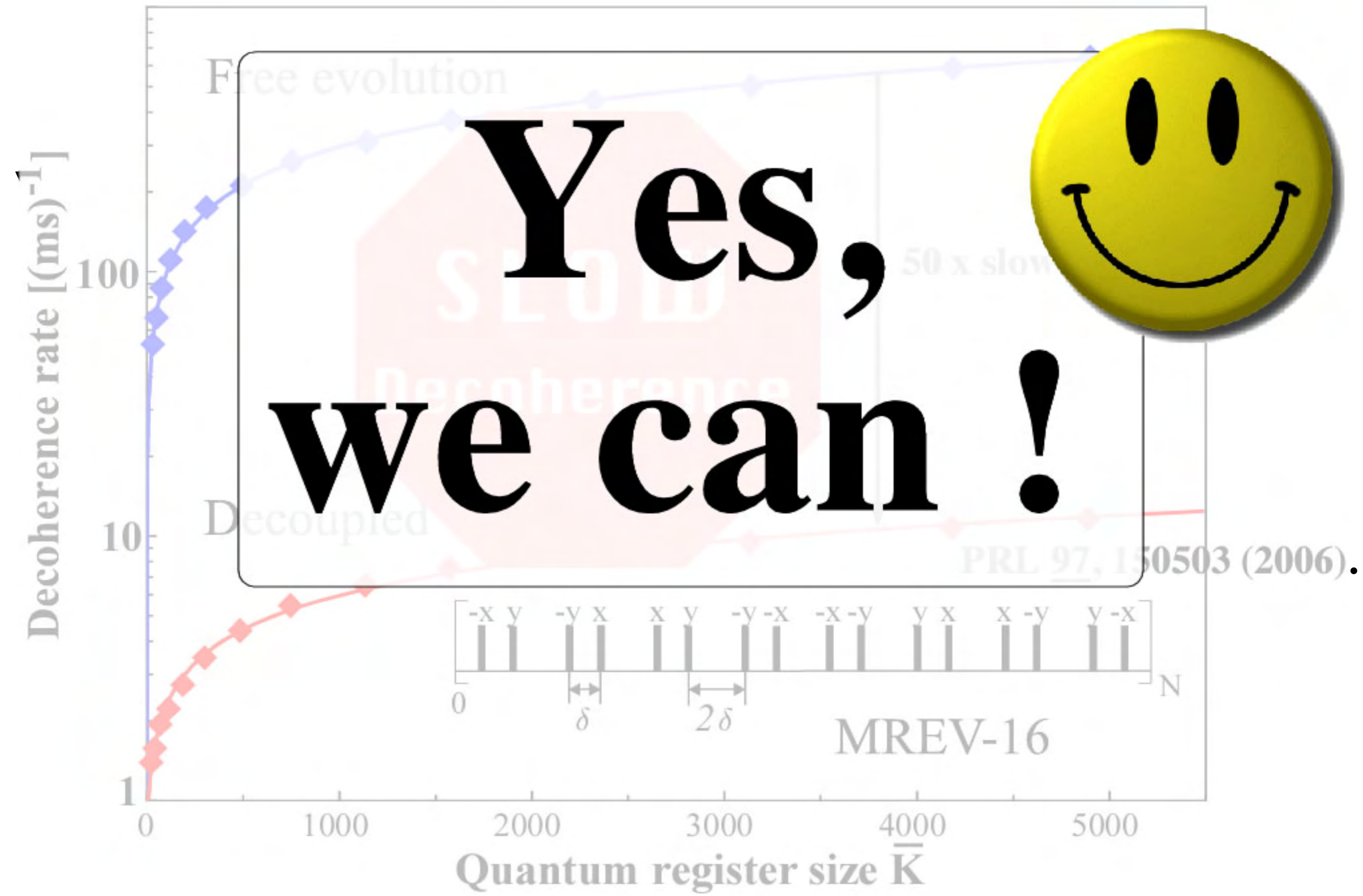
**Bath**

**long-lived coherence**





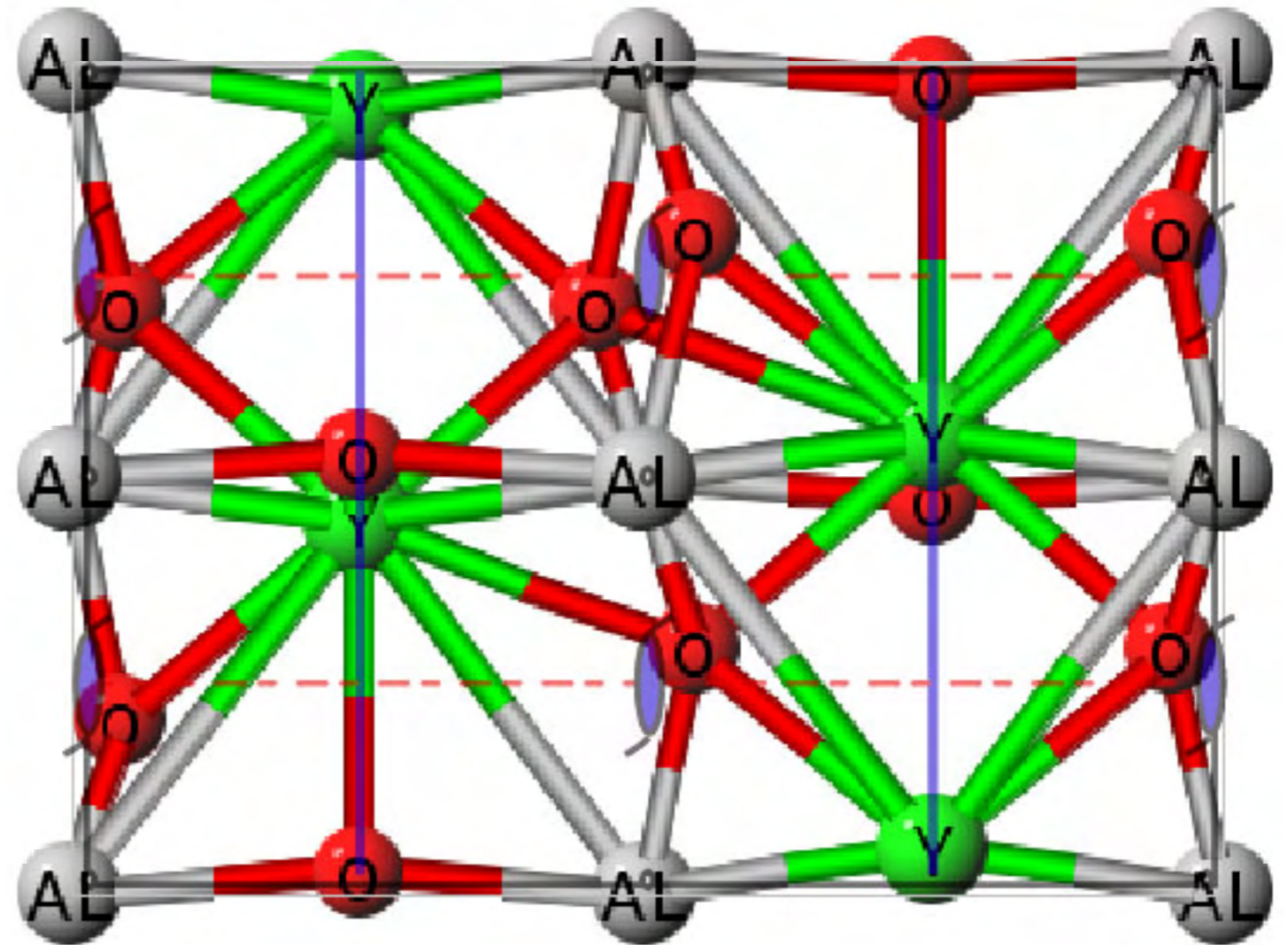
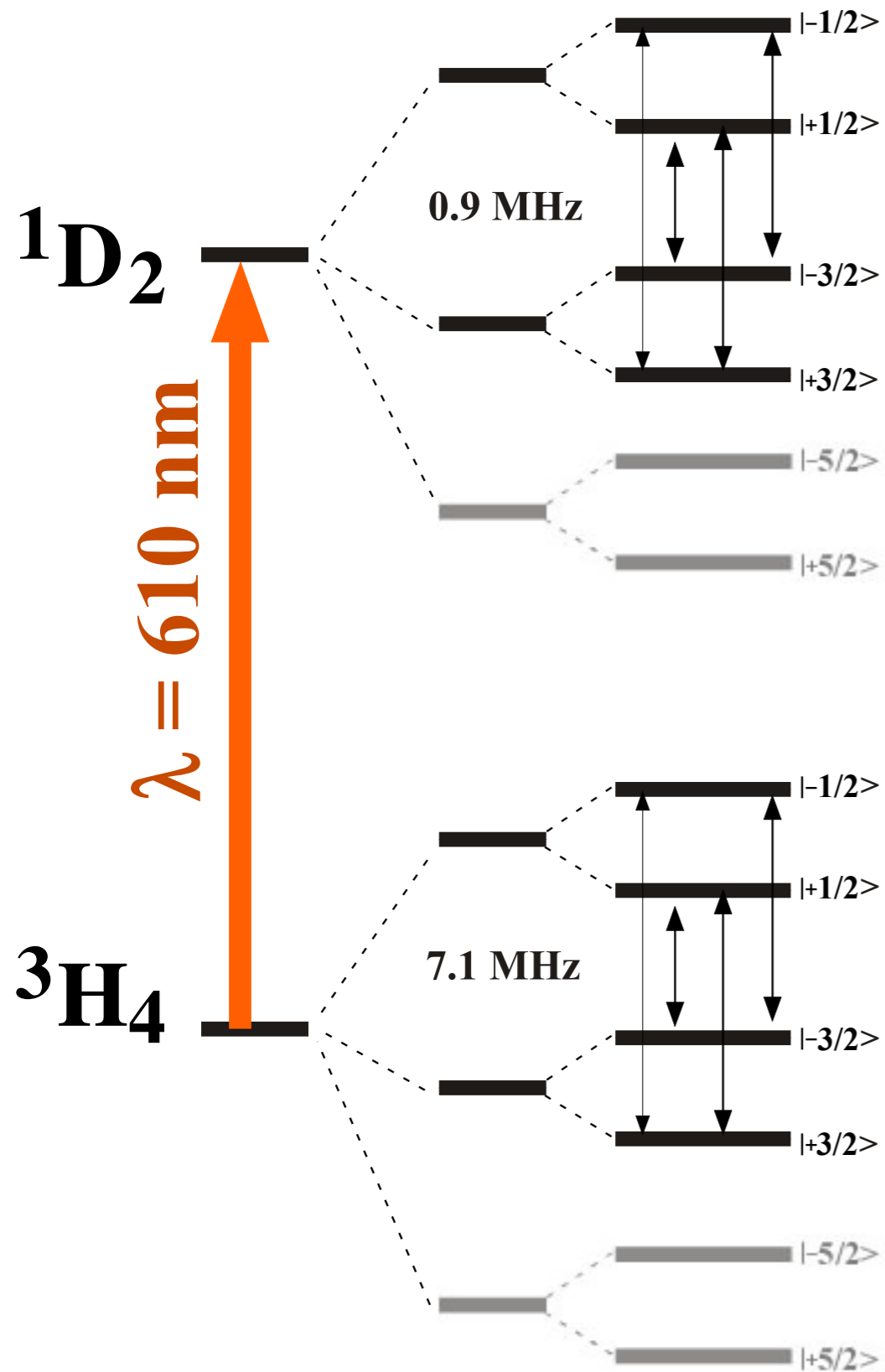
# Decoupling Quantum Registers



# Magneto-Optics

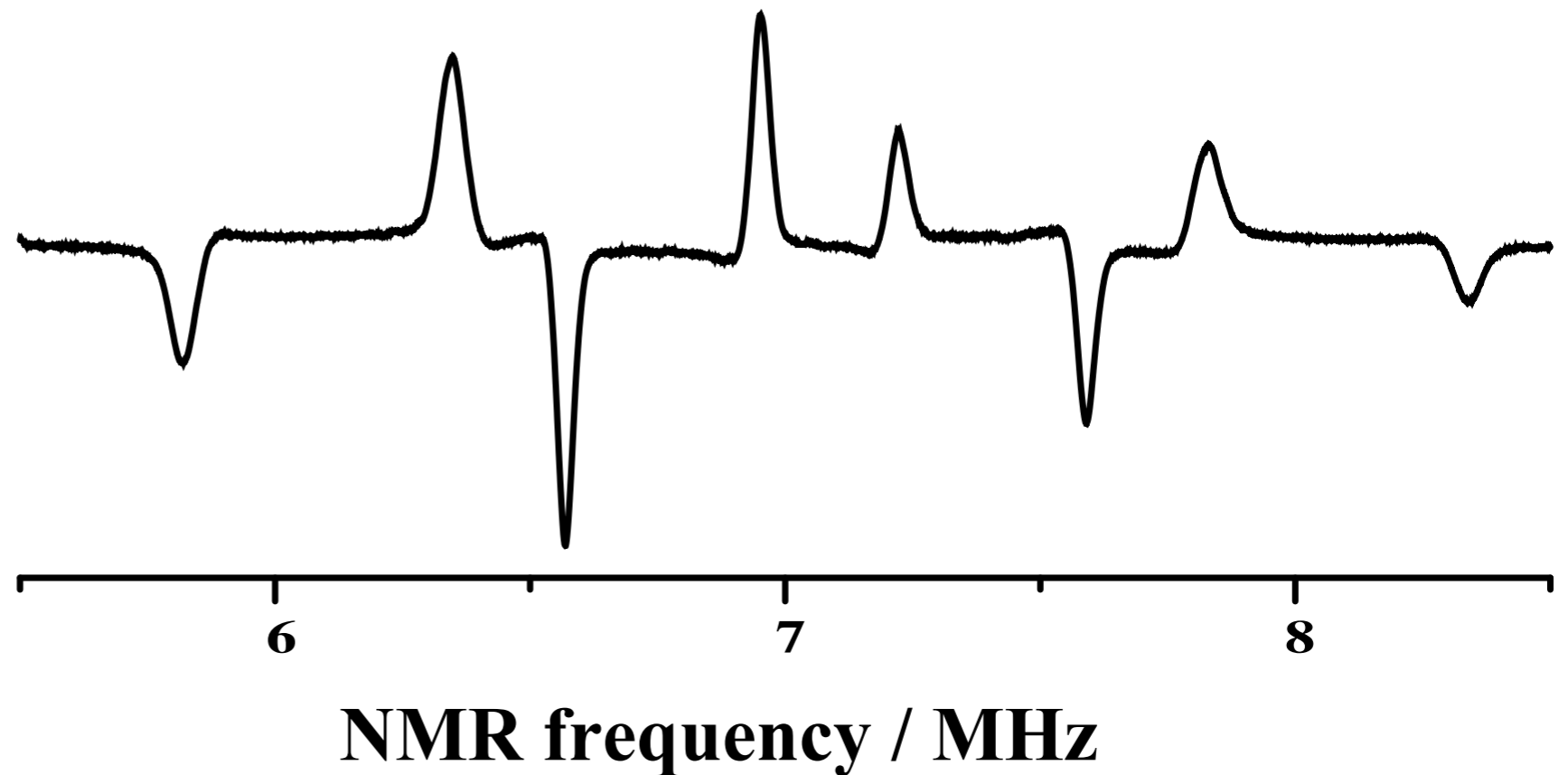
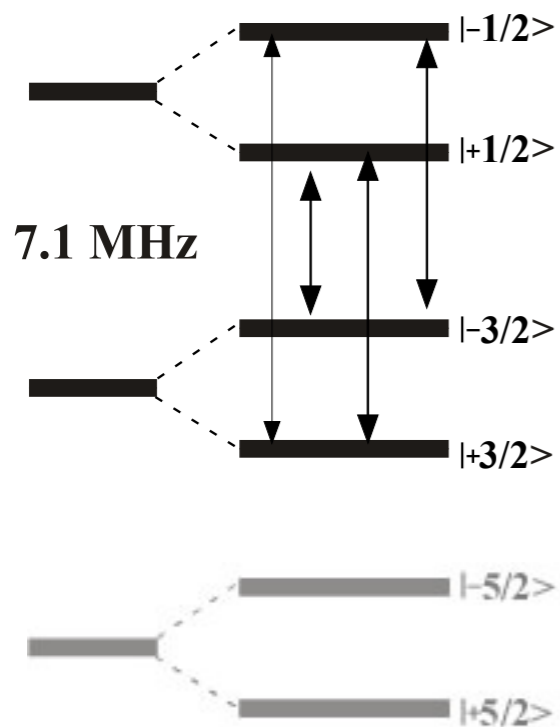
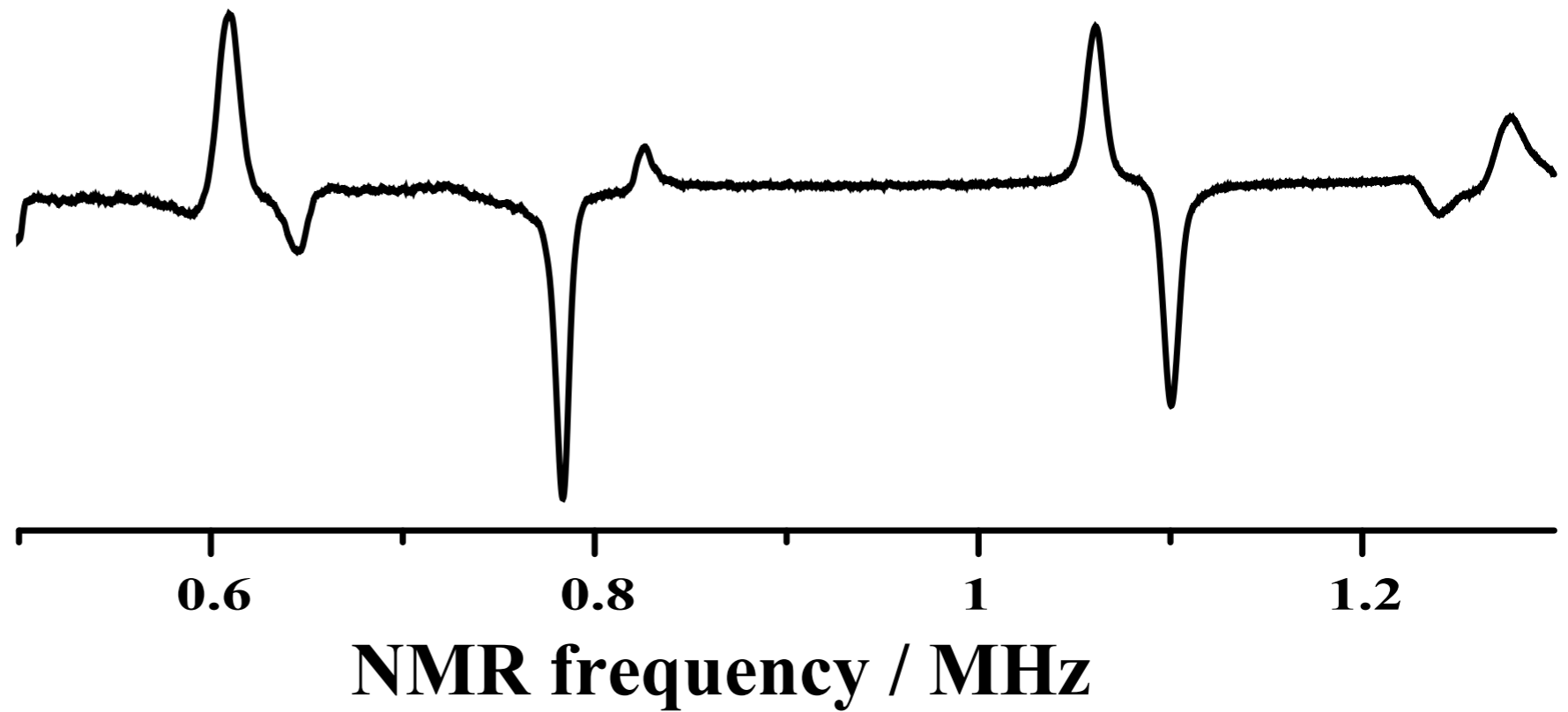
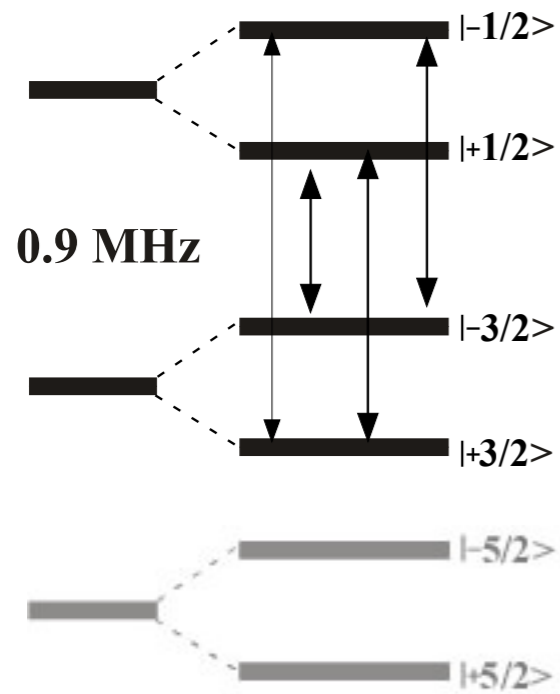
$^{141}\text{Pr} : I = 5/2$

## Pr:YAlO<sub>3</sub>



$^{141}\text{Pr} : I = 5/2$

# Spin Transitions

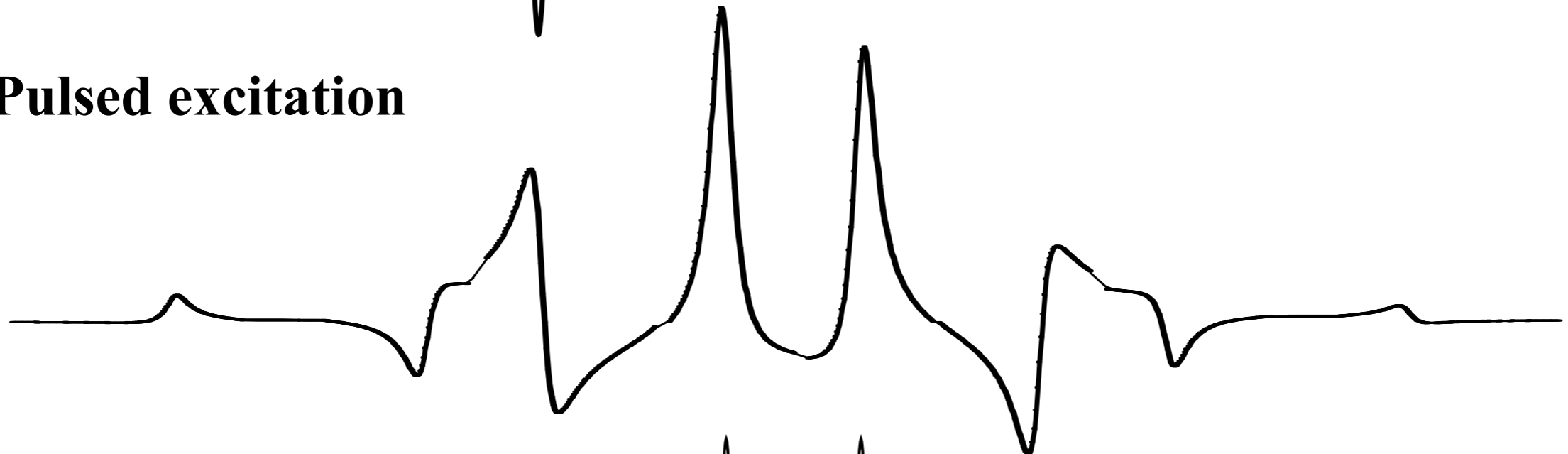


# *NMR Target*

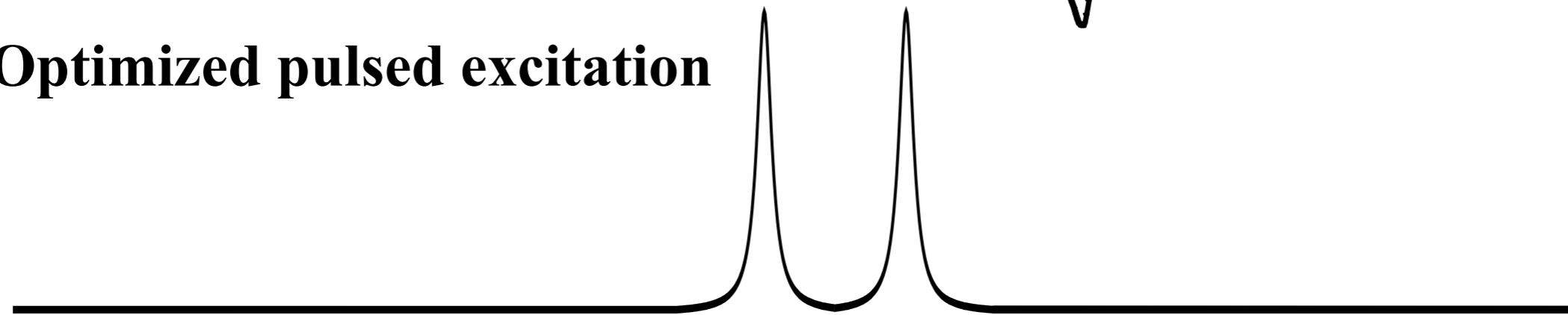
**CW (exp.)**



**Pulsed excitation**



**Optimized pulsed excitation**



6

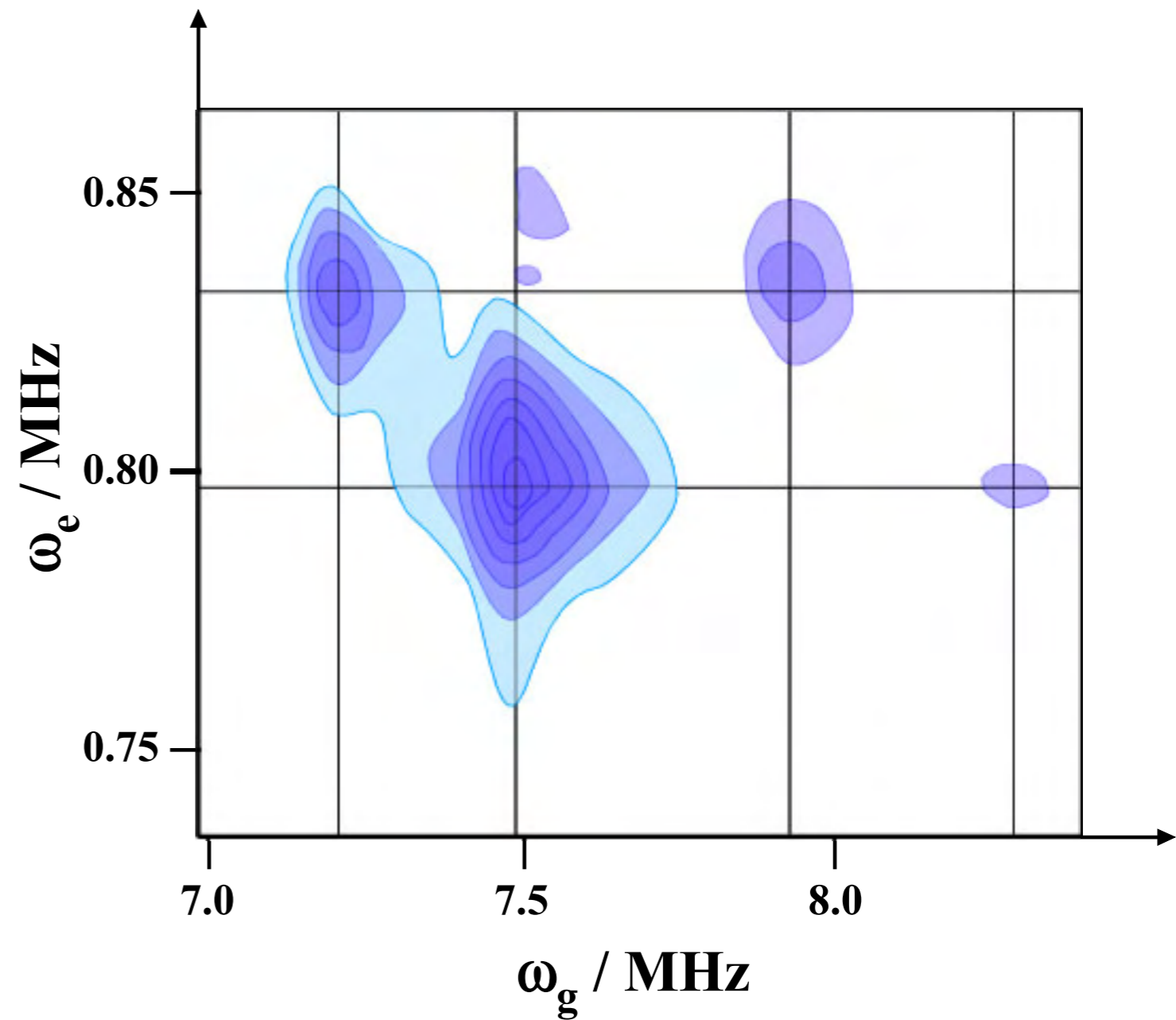
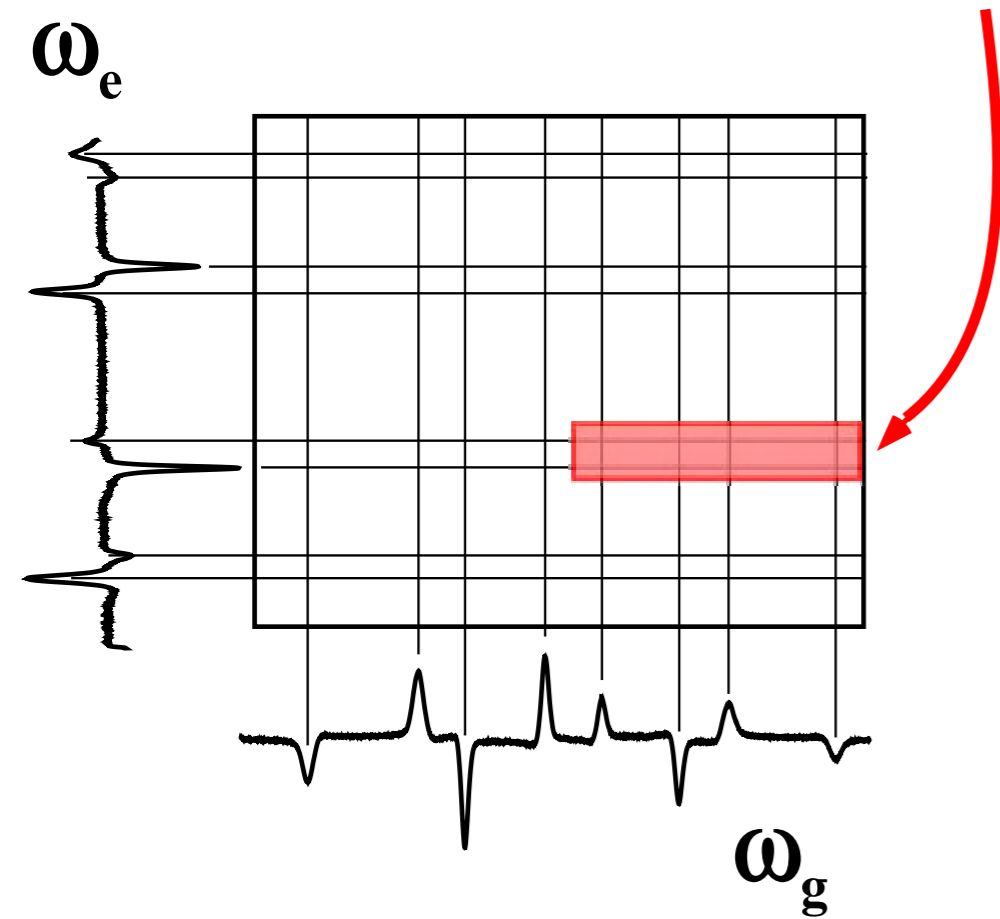
7

8

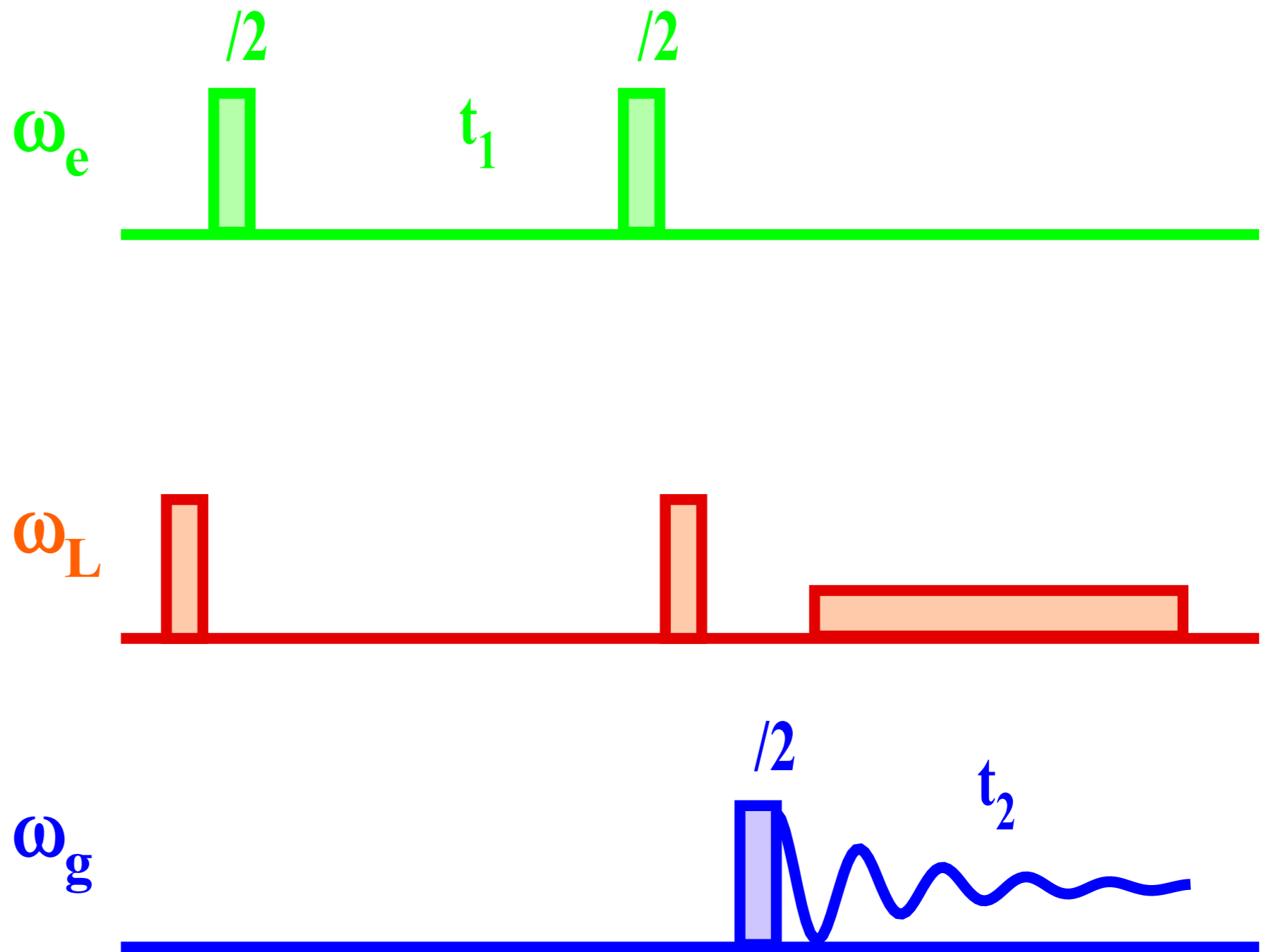
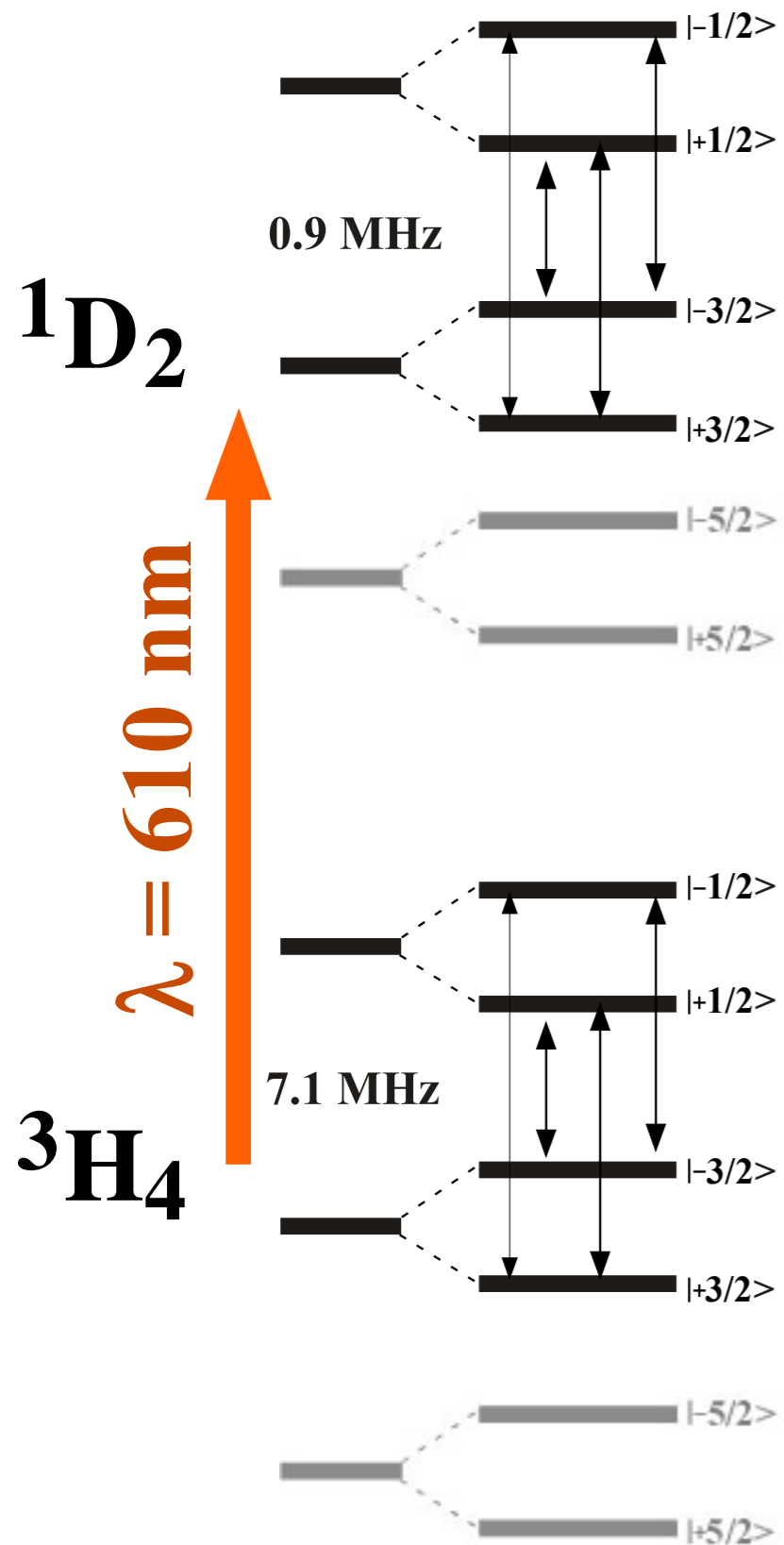
**Frequency / MHz**

# 2D Spectrum

Range covered by  
single 2D experiment

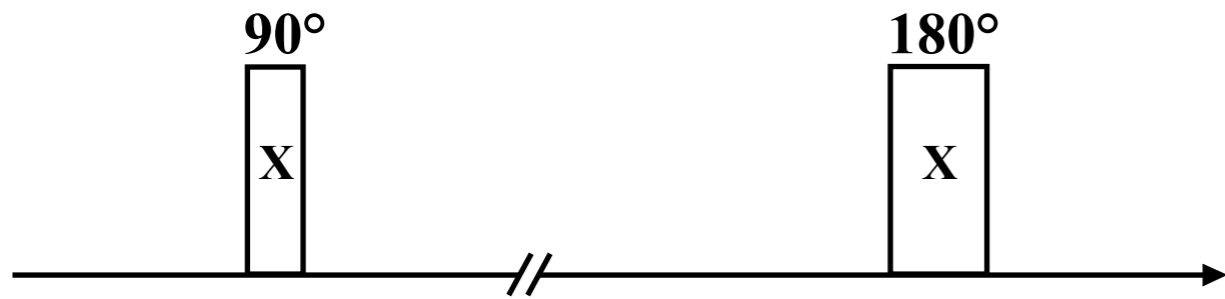


# Pulsed Excitation

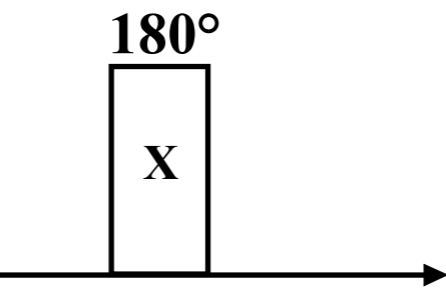


# Composite Laser Pulses

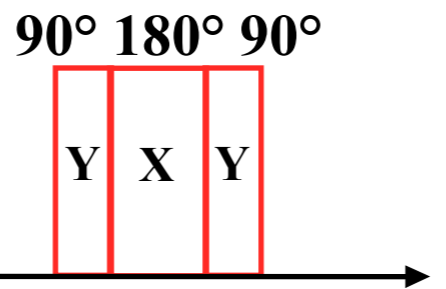
## Photon Echo



## $\pi$ -Pulse



## Offset-compensated $\pi$ -pulse



385° 320° 25°      336° 246° 10° 74° 10° 246° 336°

