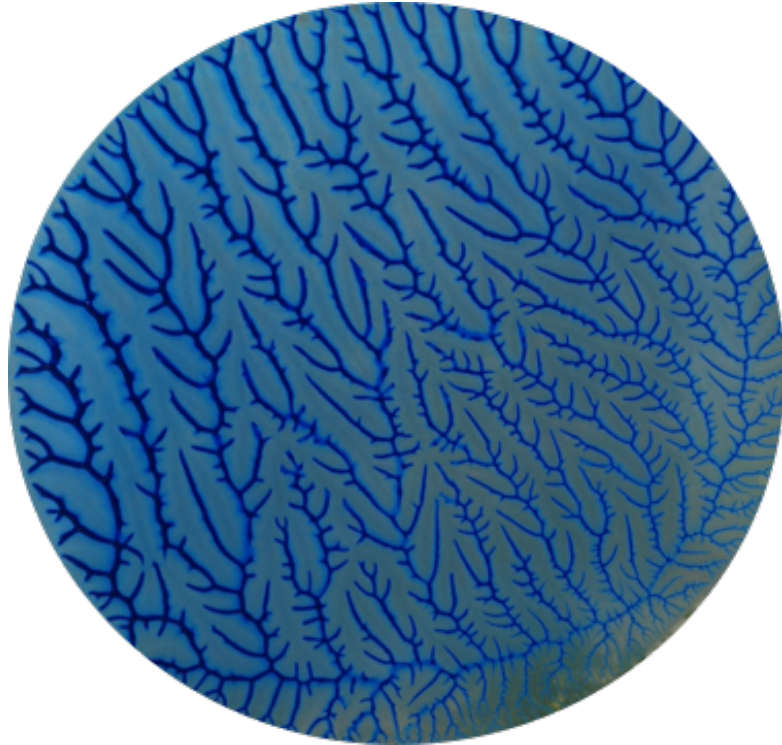


Impact and intrusion: patterns, structure and the texture of our world

KITP; February 28, 2018



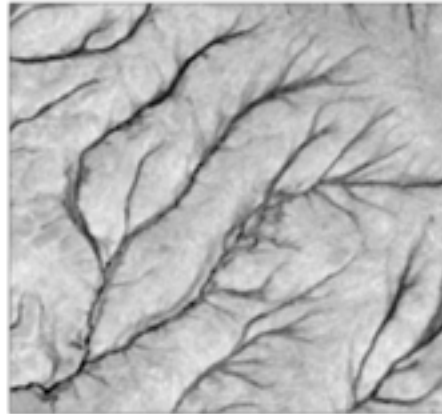
“Philosophy begins in wonder.” Plato

Dilation symmetry and penetration of space emergence of structure

Tree branches



River network

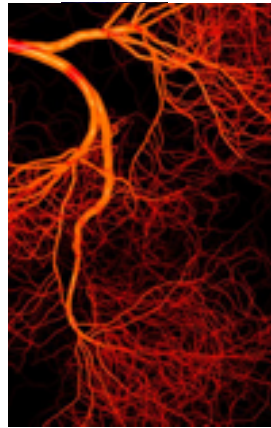


www.mdpi.com/2072-4292/7/7/8779/htm

Discharge



Blood vessel



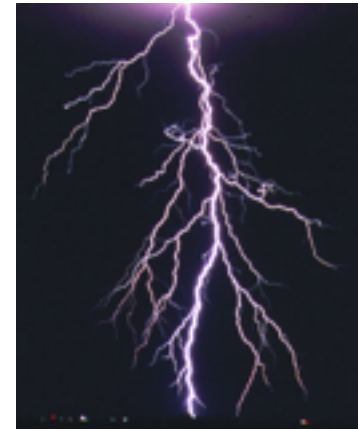
www.fi.edu/heart/blood-vessels

Aggregation



en.wikipedia.org/wiki/Diffusion-limited_aggregation

Lightning

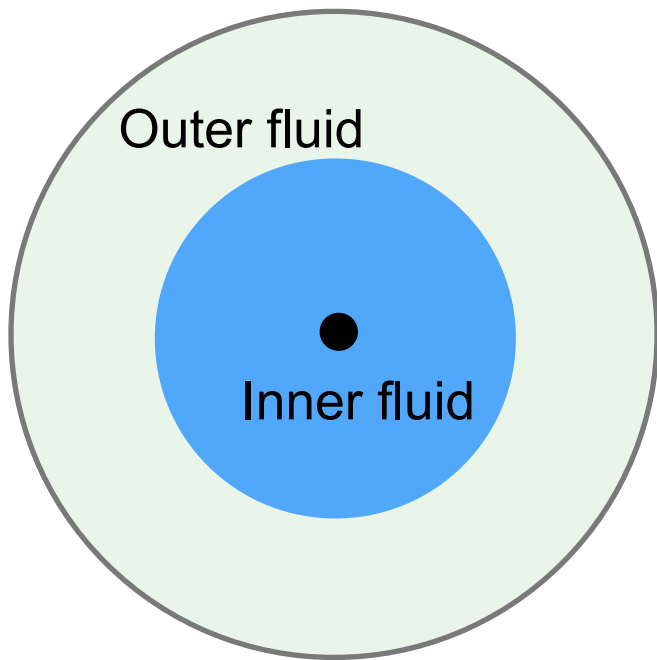
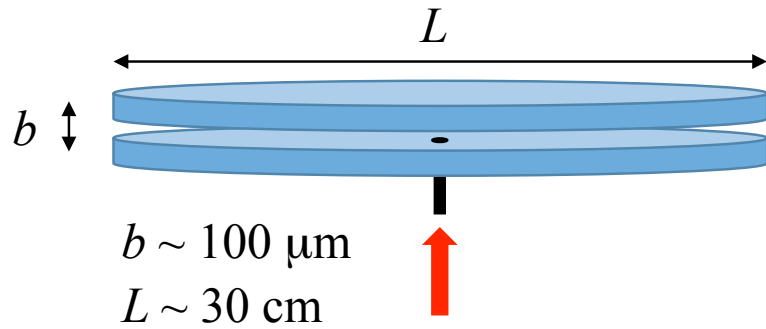


www.grahamisd.com/page.cfm?p=938

Spans many scales and many branches of science

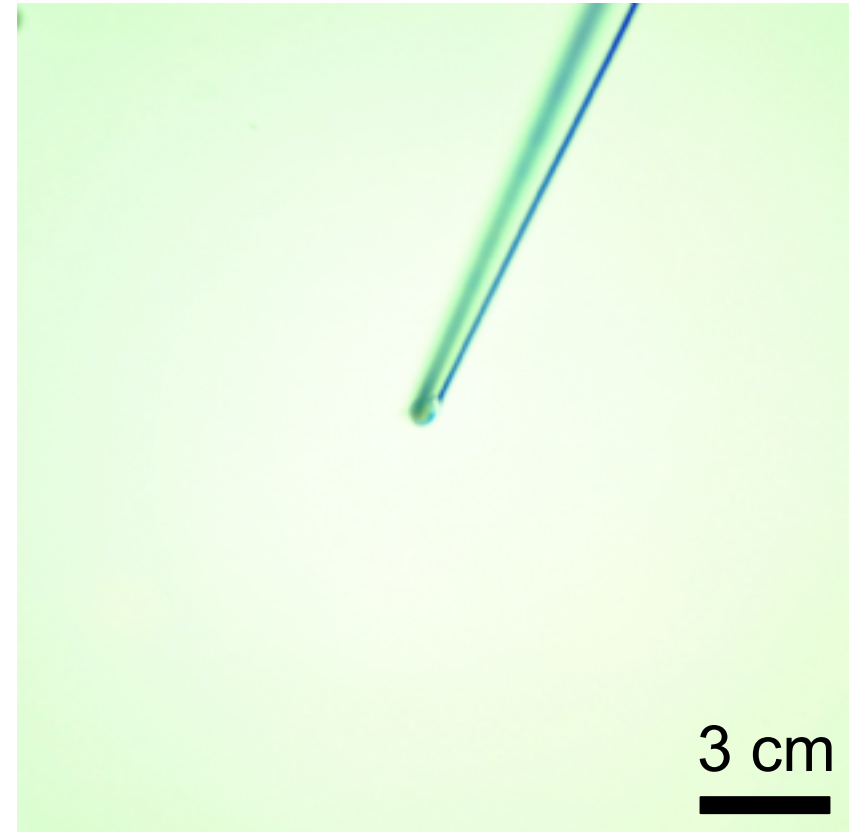
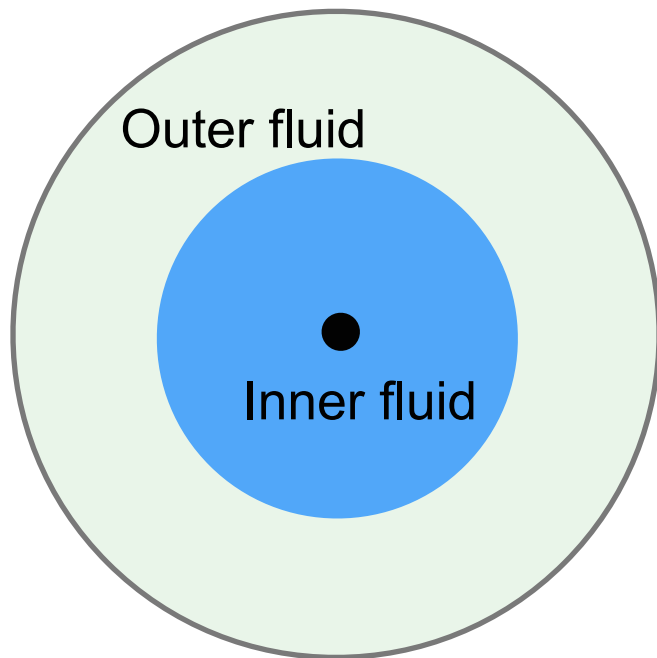
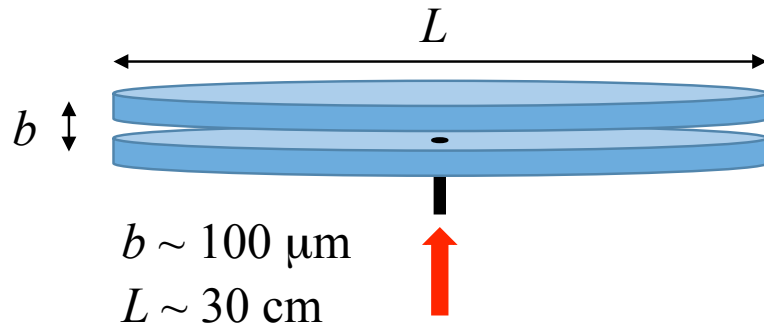
Viscous-fingering instability

One fluid displaces another



Viscous-fingering instability

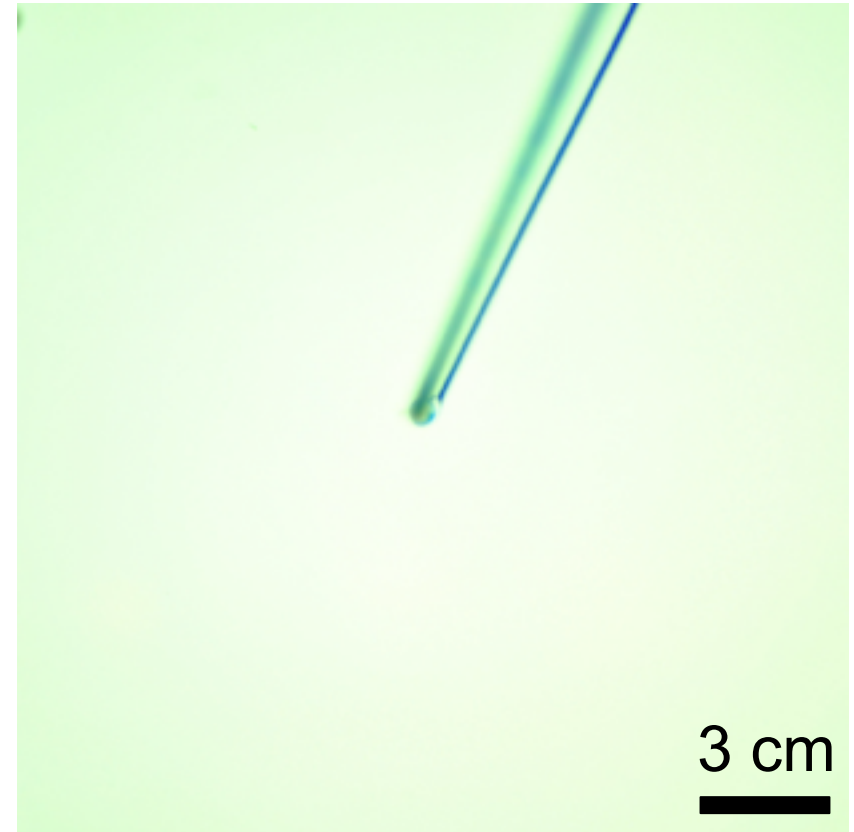
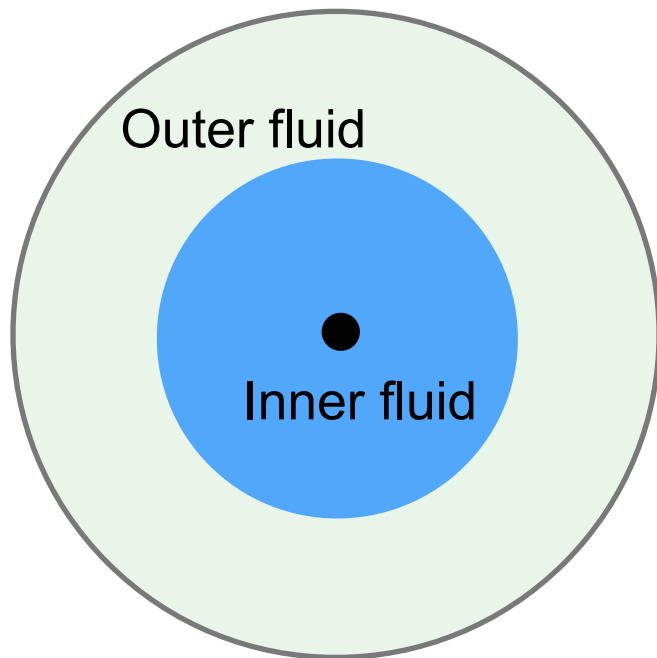
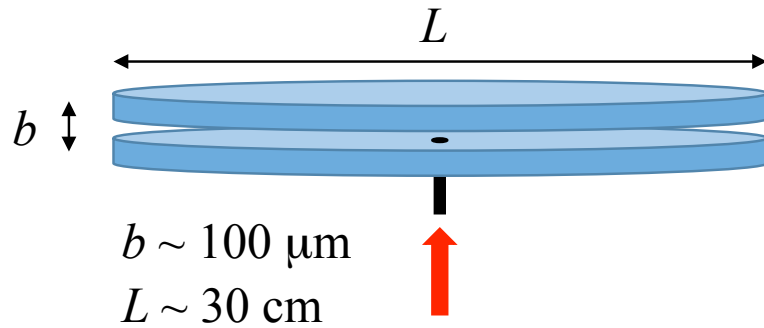
One fluid displaces another



Unstable if inner fluid
less viscous than outer fluid

Viscous-fingering instability

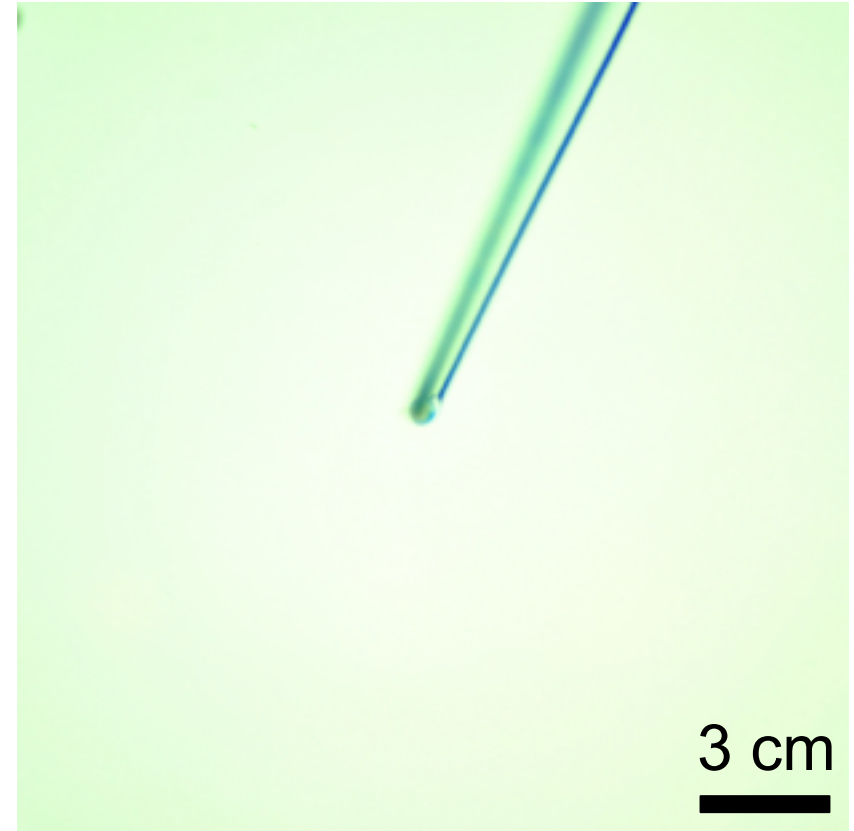
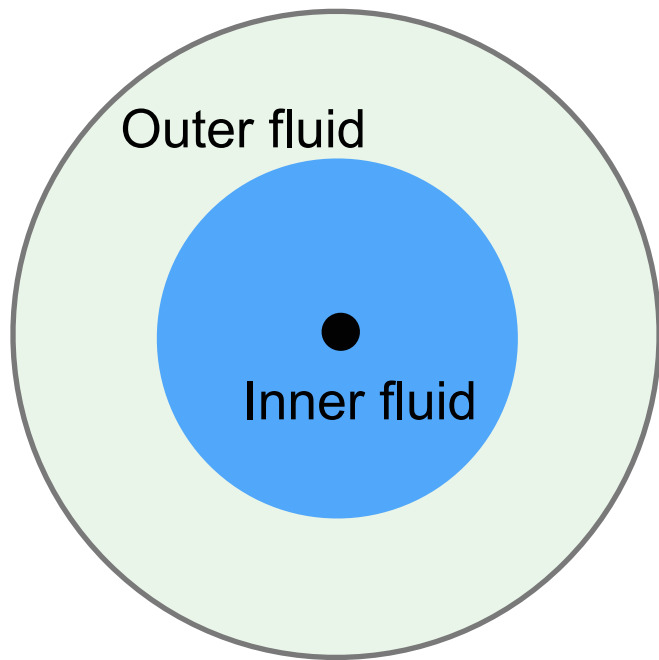
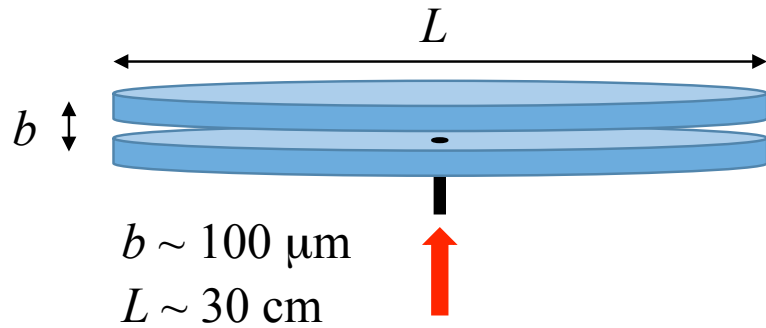
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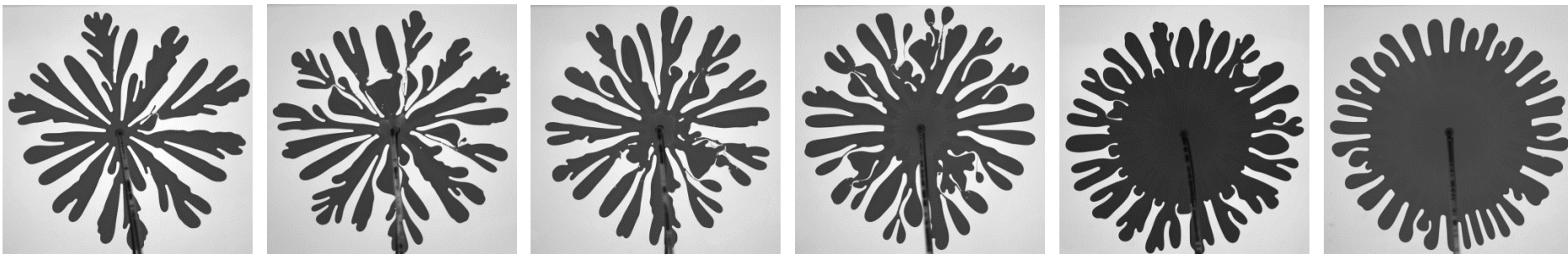


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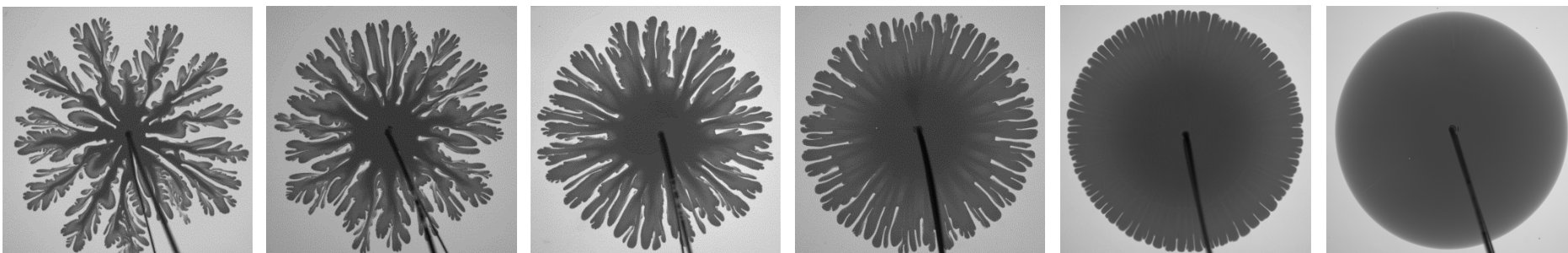
Surface tension - stabilizing force

Keep everything same *except* surface tension

Immiscible fluids: surface tension



Miscible fluids: no surface tension



Viscosity ratio

Removing surface tension stabilizes patterns!
New length scale \Rightarrow global patterns

New regime: toes miscible fluids



Viscosity ratio ≈ 0.004



Viscosity ratio ≈ 0.2

New regime: toes miscible fluids



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New regime: toes miscible fluids



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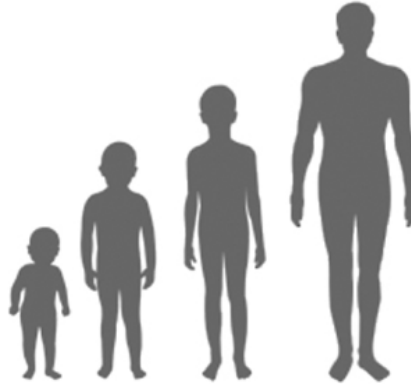
Viscosity ratio ≈ 0.004



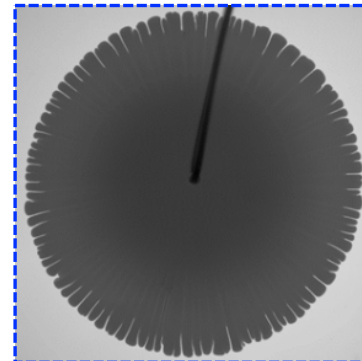
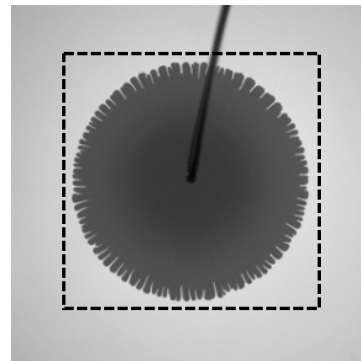
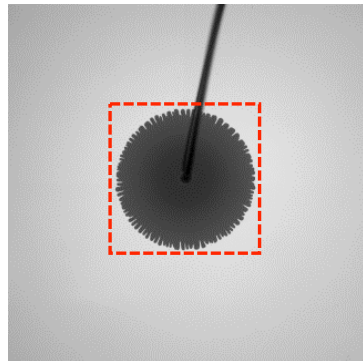
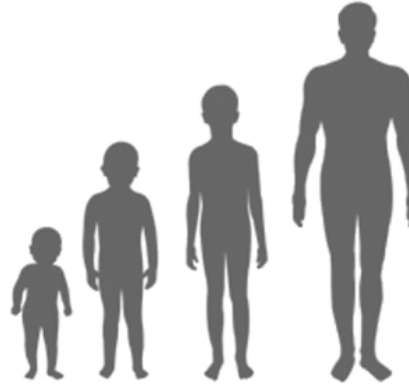
Viscosity ratio ≈ 0.2

Once toe forms it no longer splits
Instability turns itself off

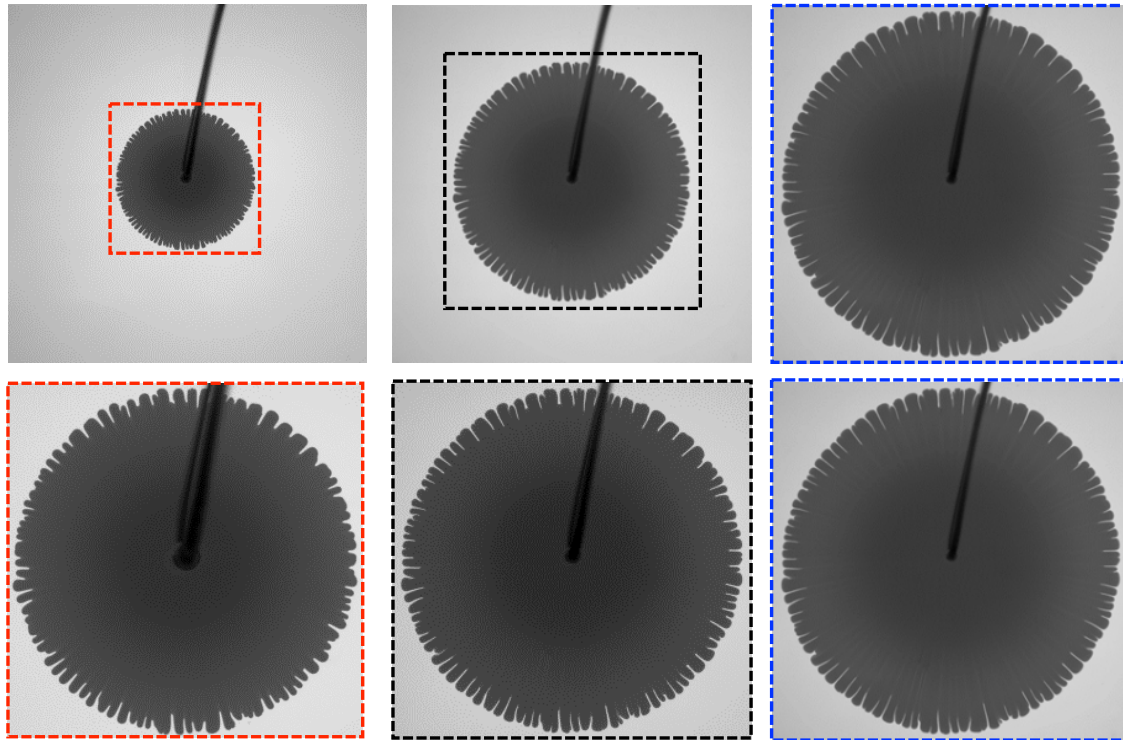
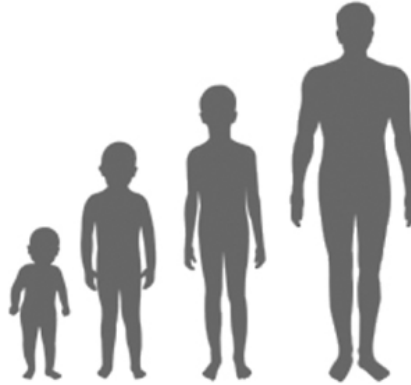
Proportionate growth - how mammals grow



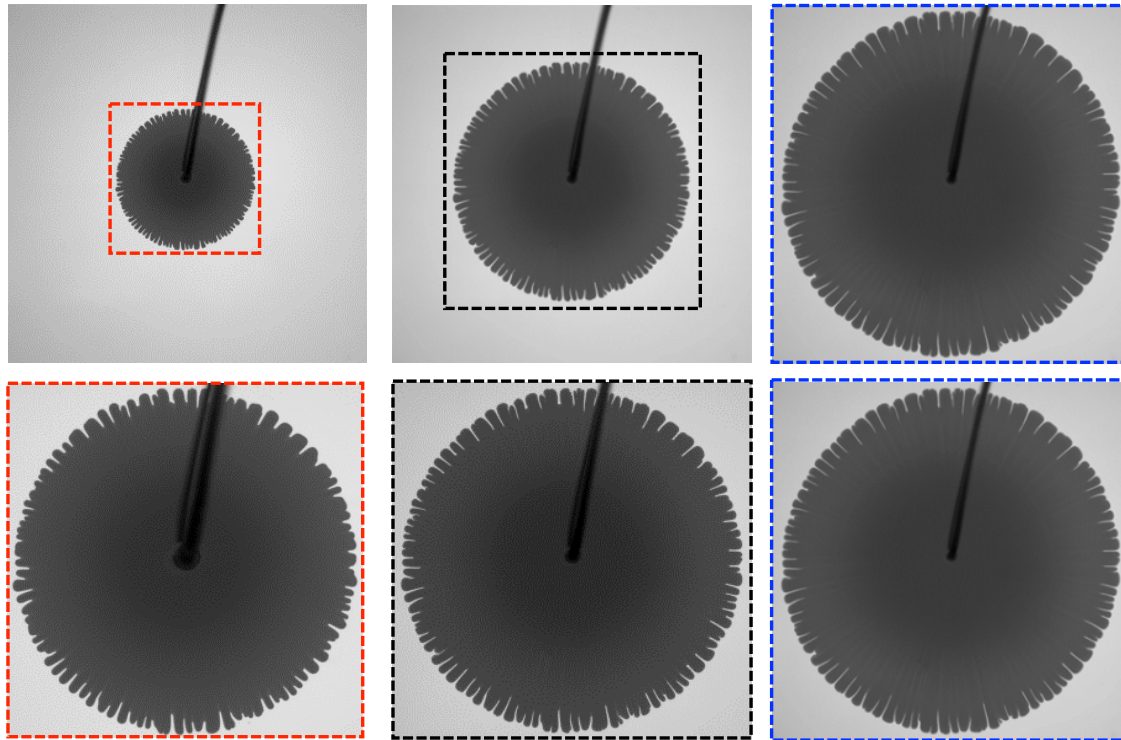
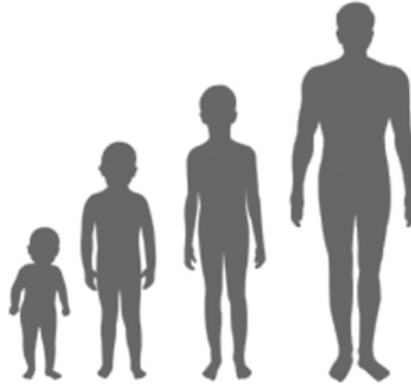
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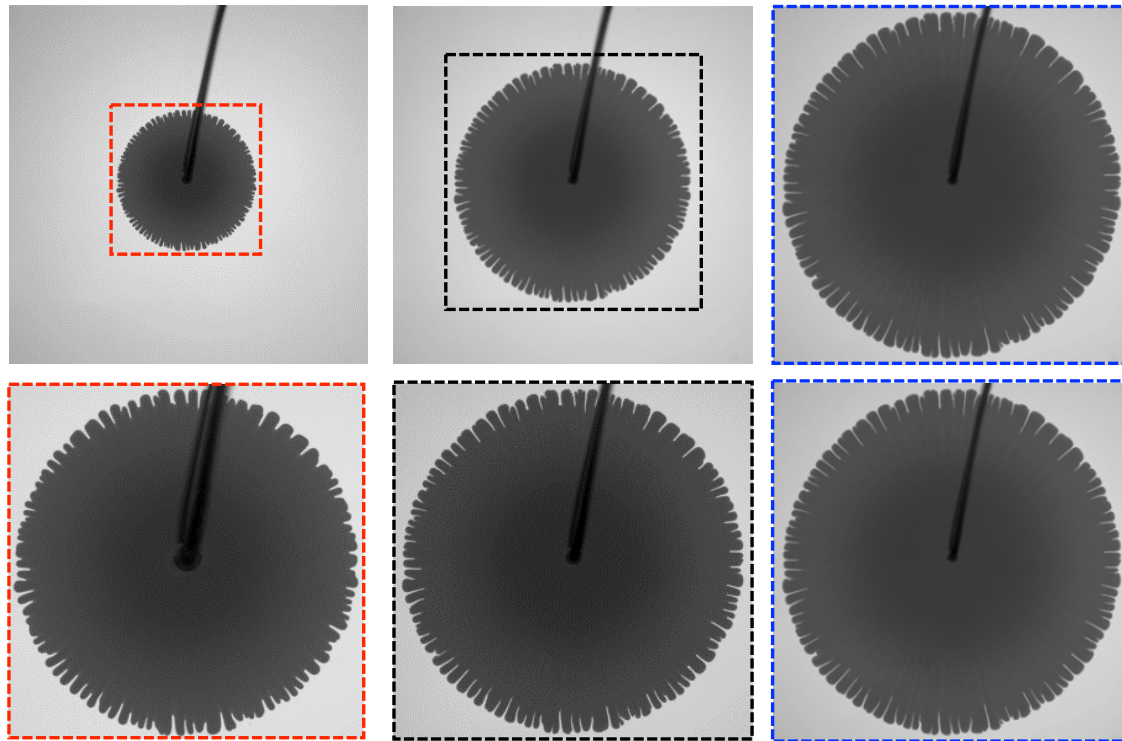
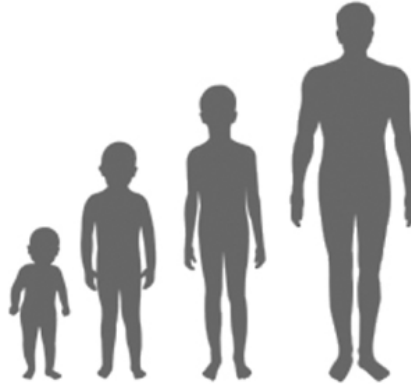


Proportionate growth - how mammals grow



Only physical (as distinct from biological) example known

Proportionate growth - how mammals grow



Only physical (as distinct from biological) example known

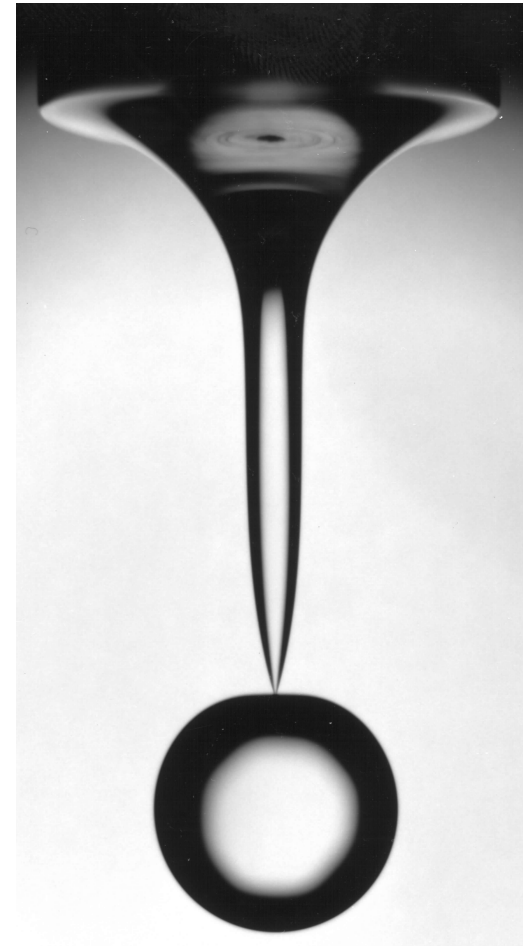
Memory of structure

How do drops break apart? example of transition

Topology change \Rightarrow transition

Neck radius $\rightarrow 0$ Pressure $\rightarrow \infty$

Cannot simulate to get past snapoff



Similar behavior: Star formation

PILLARS OF CREATION IN STAR-FORMING REGION

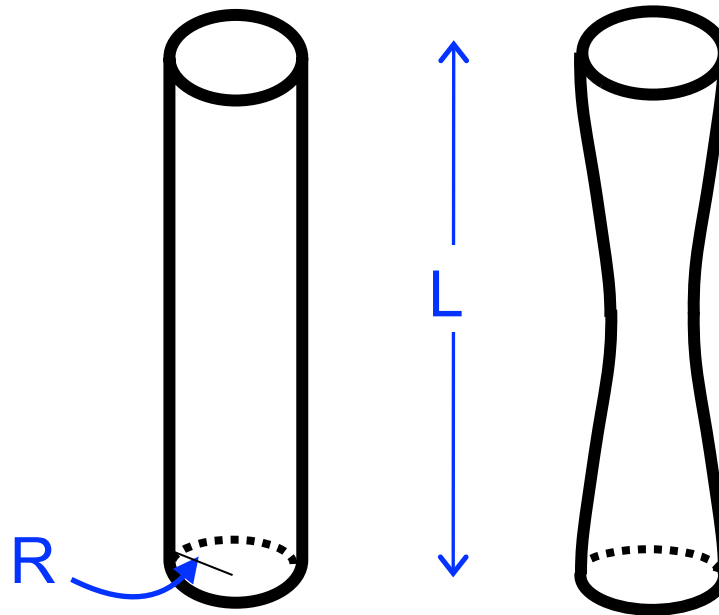
Gas Pillars - Eagle Nebula
Hubble Space Telescope



Similar behavior everywhere
celestial \Rightarrow microscopic \Rightarrow nuclear fission...

Cylinder of fluid

“Rayleigh-Plateau Instability”

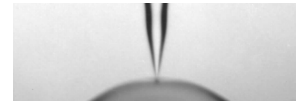
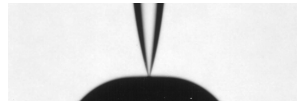


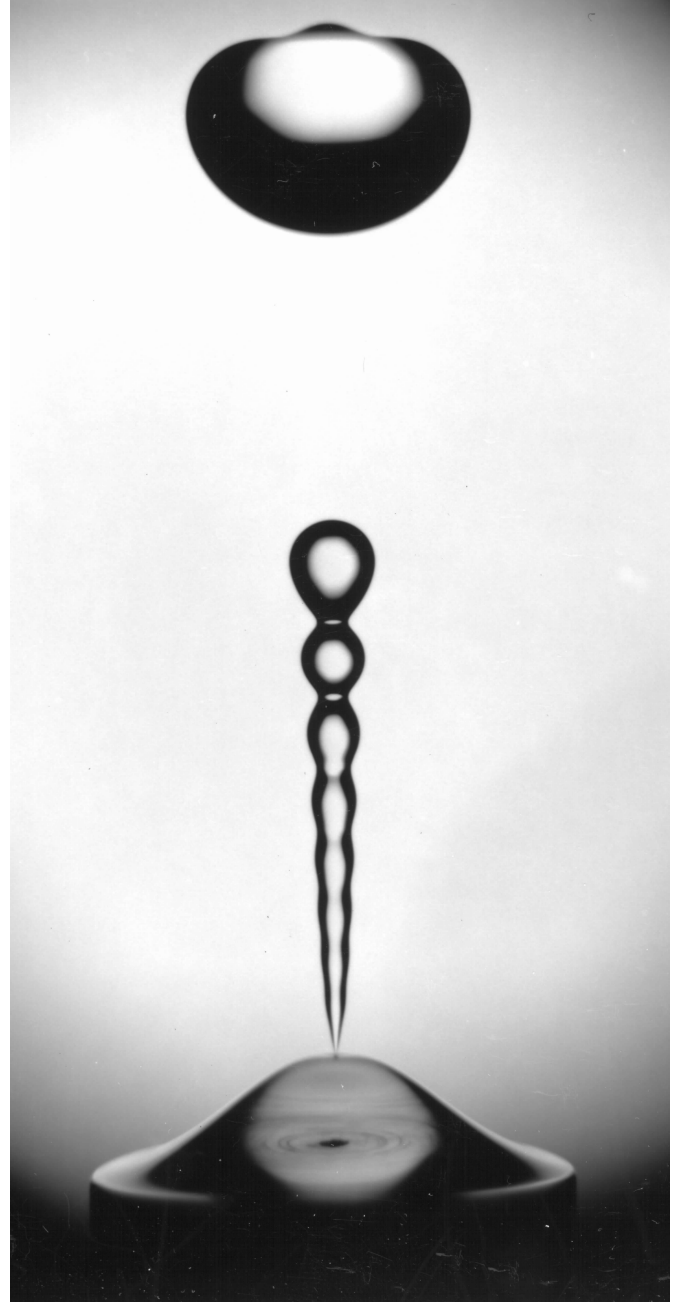
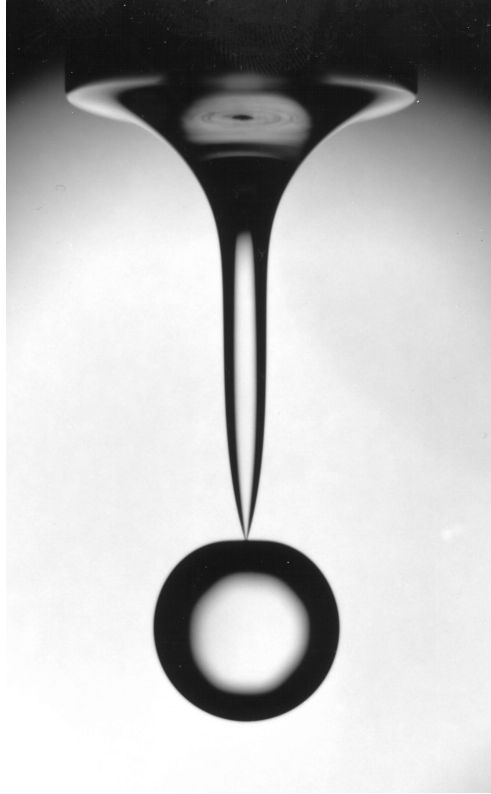
Surface area decreases if $L > 2\pi R$
 \Rightarrow unstable

Bolas Spider

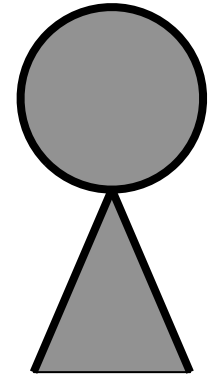
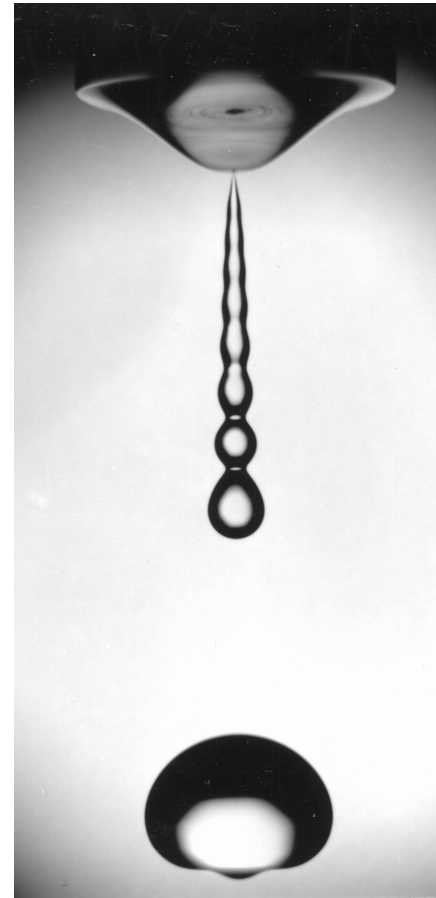
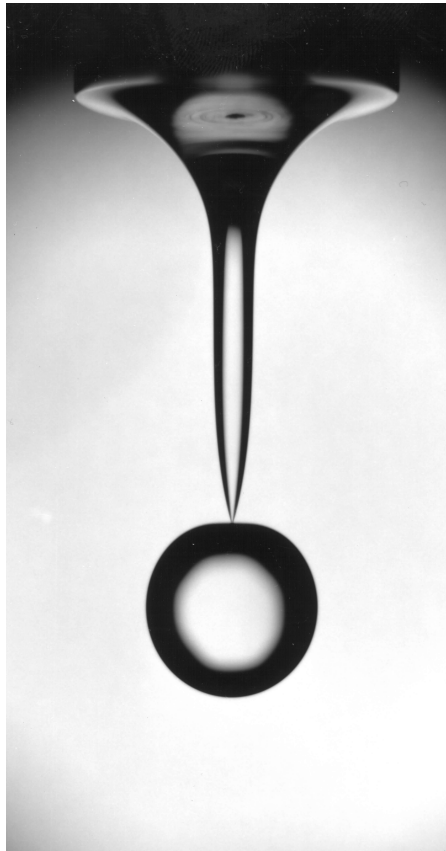
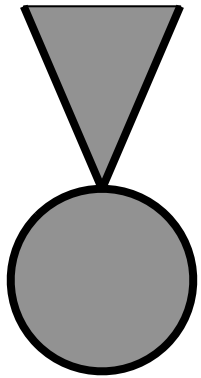


Singularity





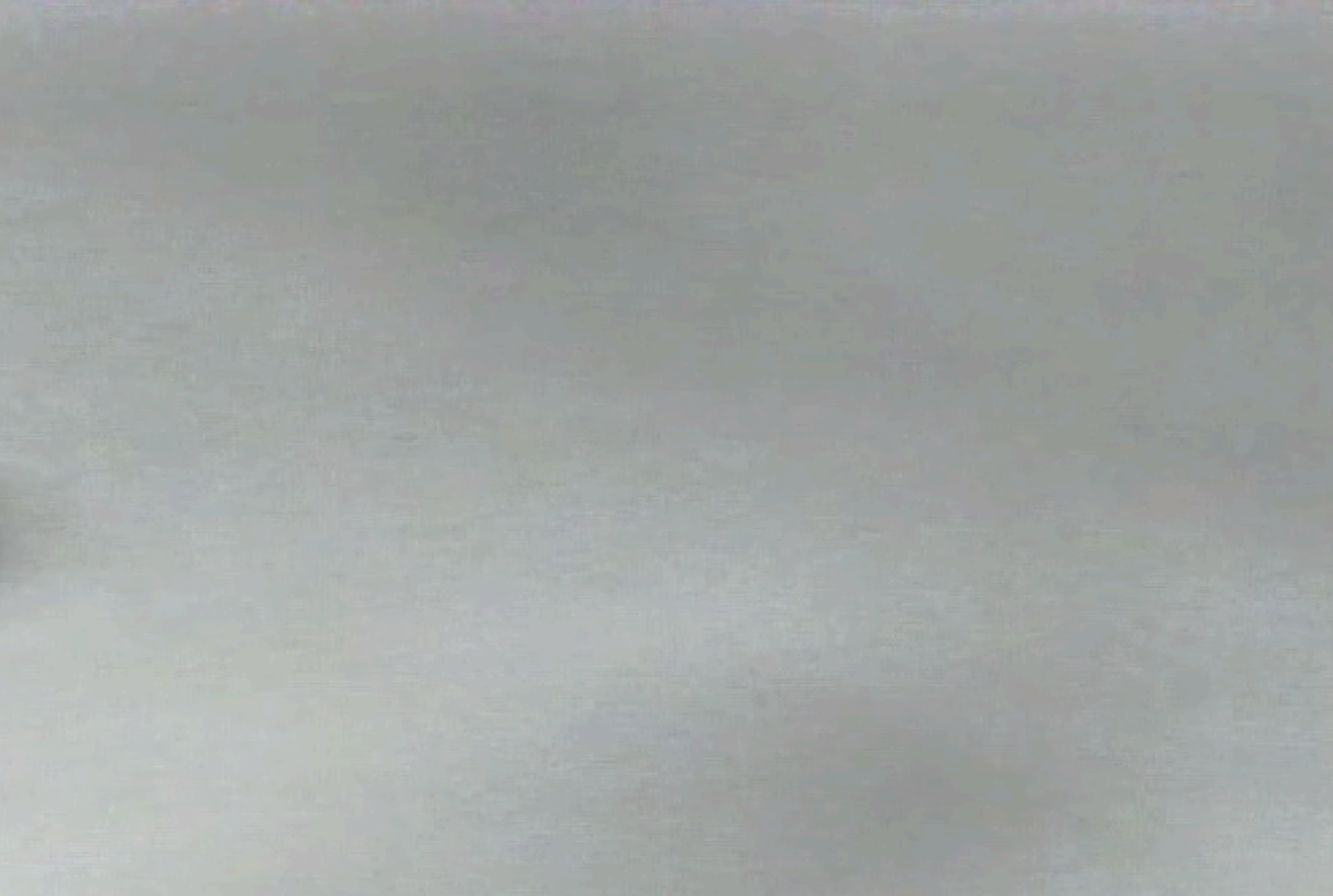
Singularity



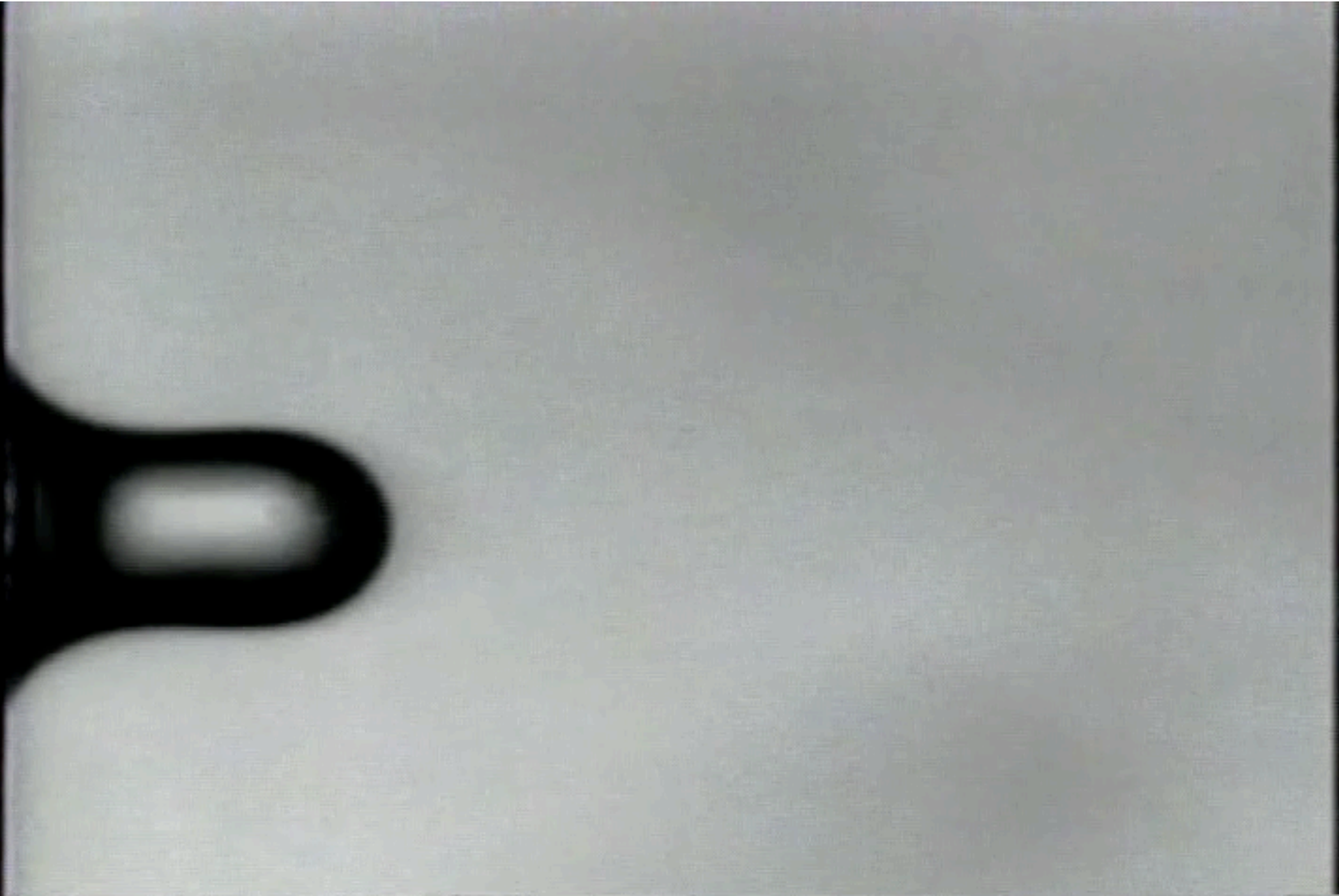
Pinch-off same even though gravity in opposite direction

Something is universal

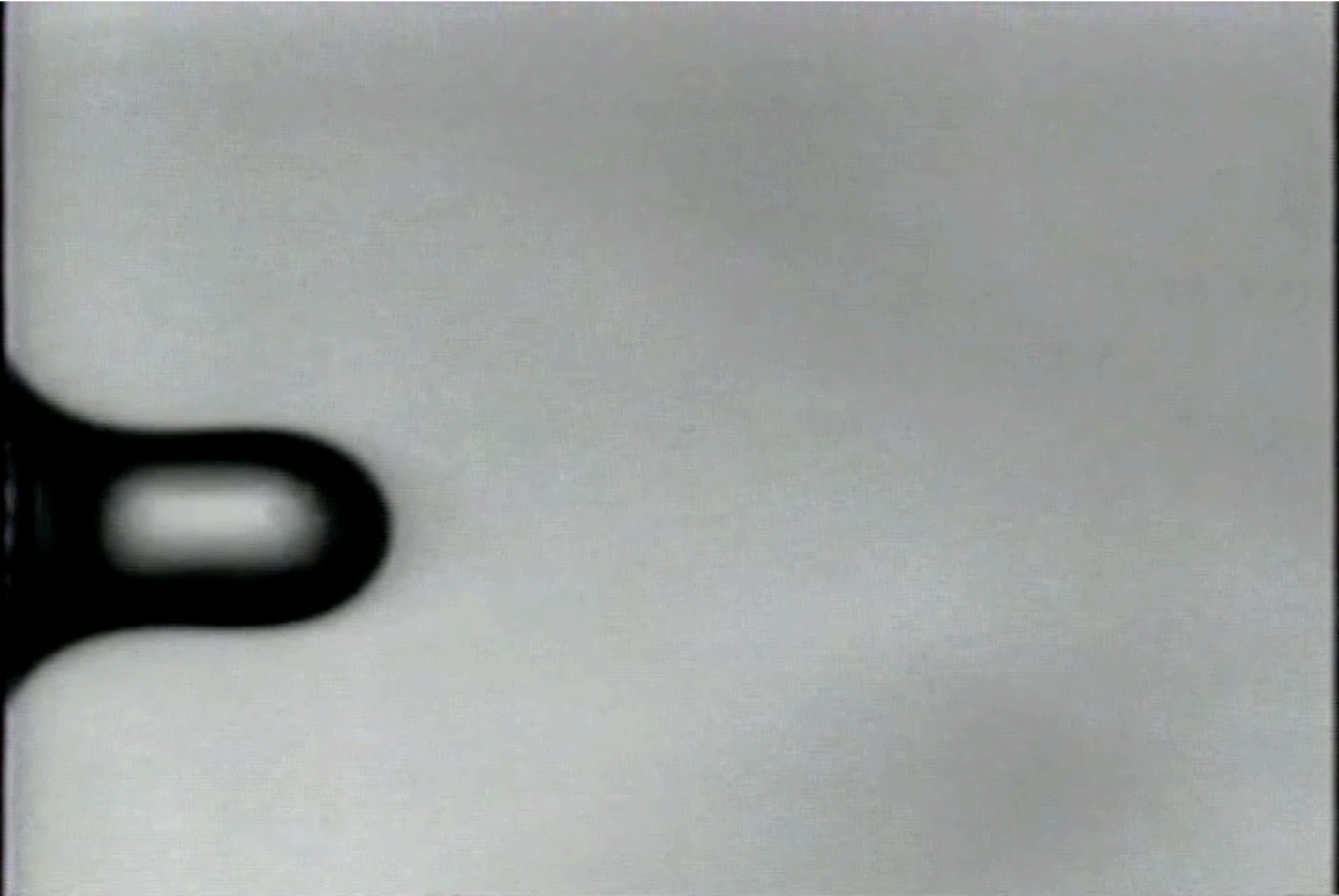
Water drops



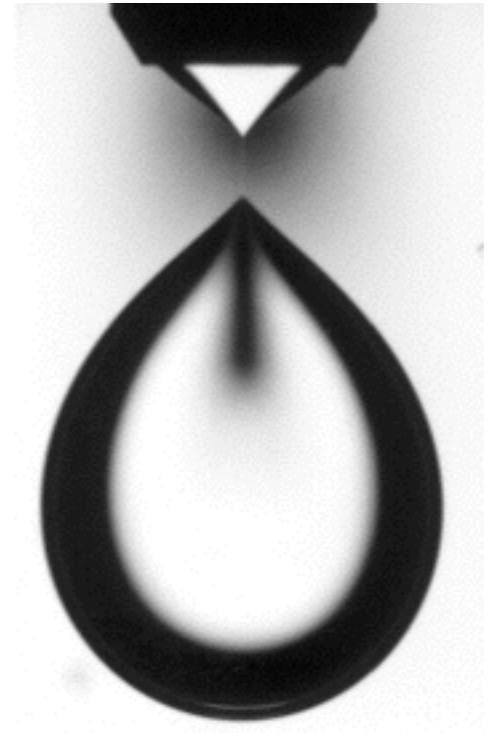
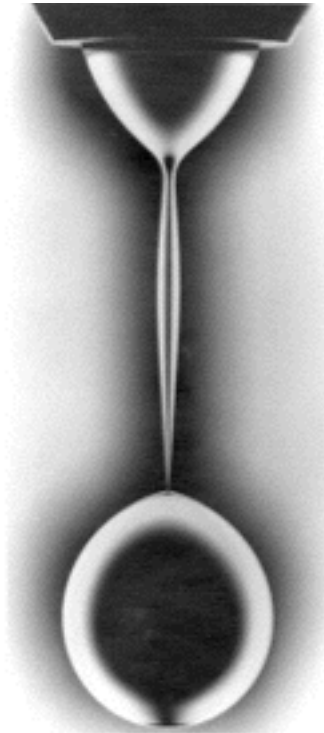
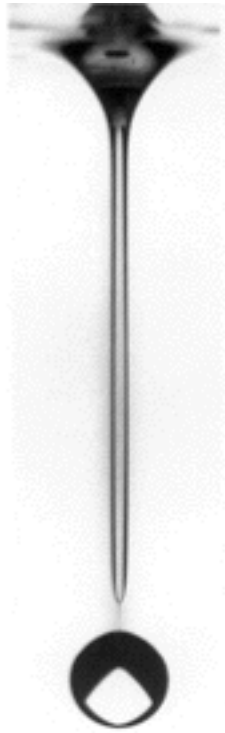
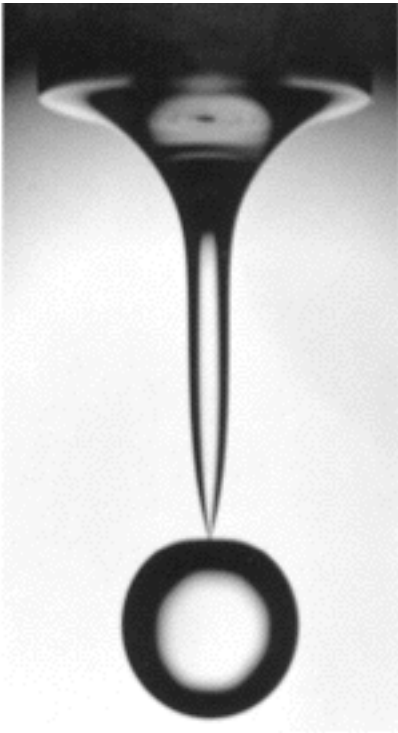
Water drops



Water drops



Each unhappy drop is unhappy in its own way



Different regimes depend on:

viscosity inner fluid
viscosity outer fluid
density inner fluid
density outer fluid
surface tension
nozzle diameter

How to think about shapes: scale invariance

Breakup \Rightarrow radius smaller than any other length.

Dynamics insensitive to all other lengths.

Flow depends only on shrinking radius.

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But: Radius depends on flow

(which depends on radius

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...

Self-similar structure*

Blow up any part \Rightarrow regain original

Universal shapes

* Keller & Miksis *SIAM* (1983)

* Eggers & Dupont *JFM* (1993)

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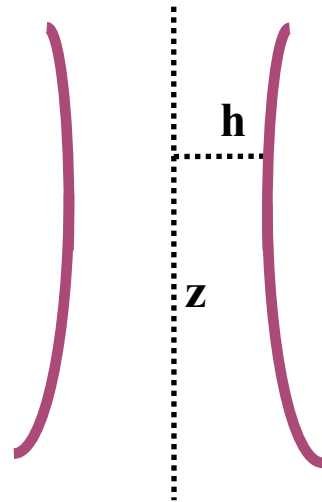
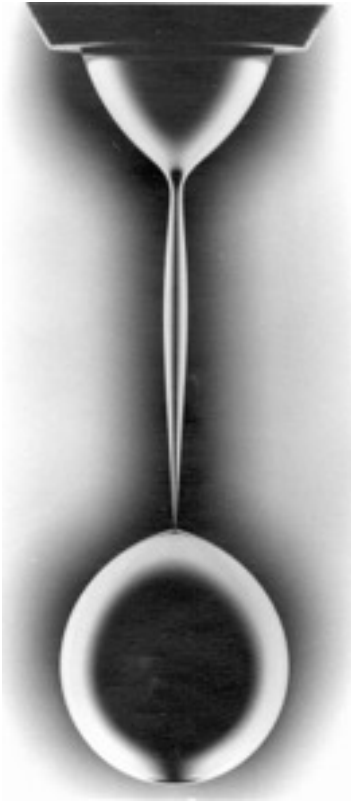
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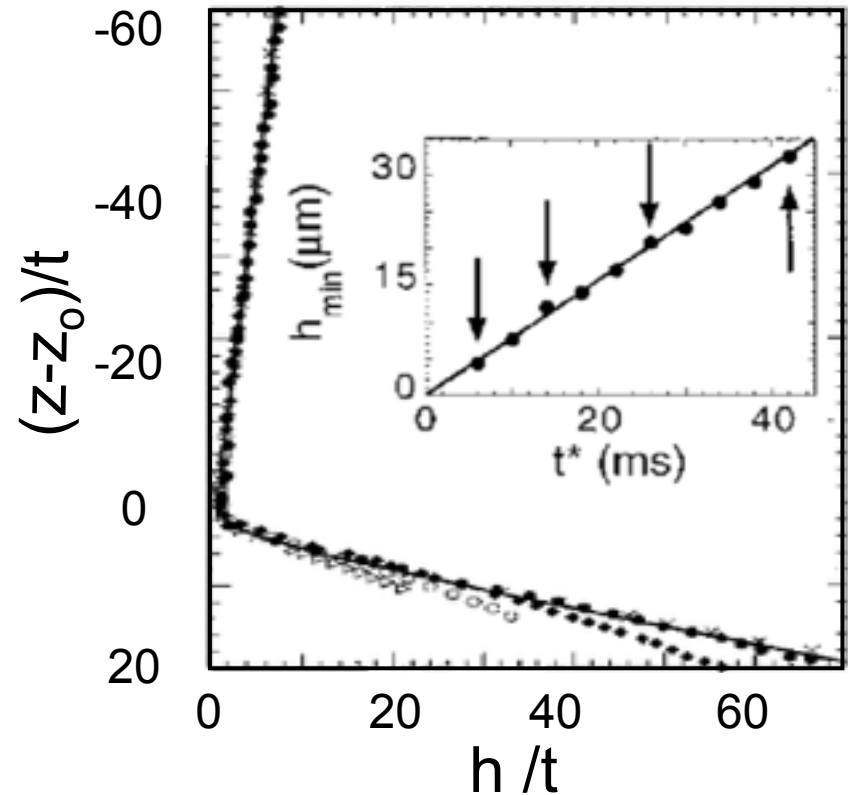
Implication

stretch axes \Rightarrow curves overlap

$$h(z,t) = f(t) H[(z-z_0)/f(t)^\beta]$$



Example: glycerol into oil

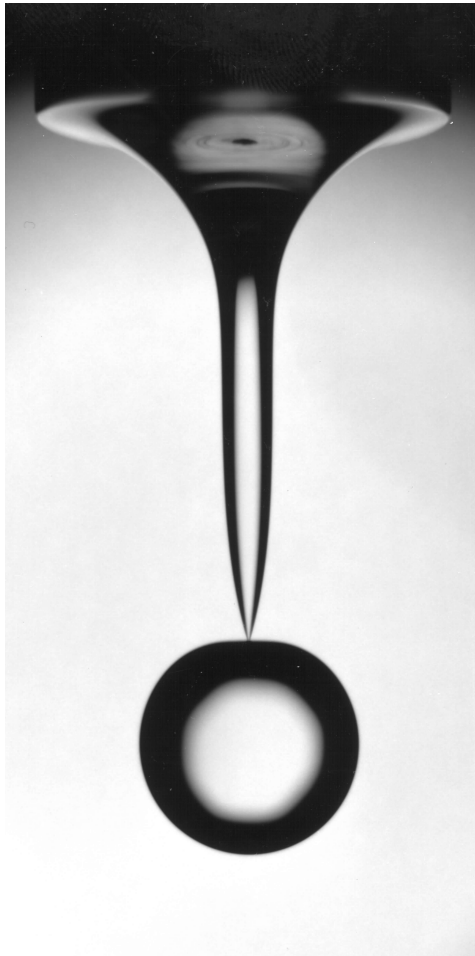


Emphasizes what is universal

BUT ...

Remember water drop in air?

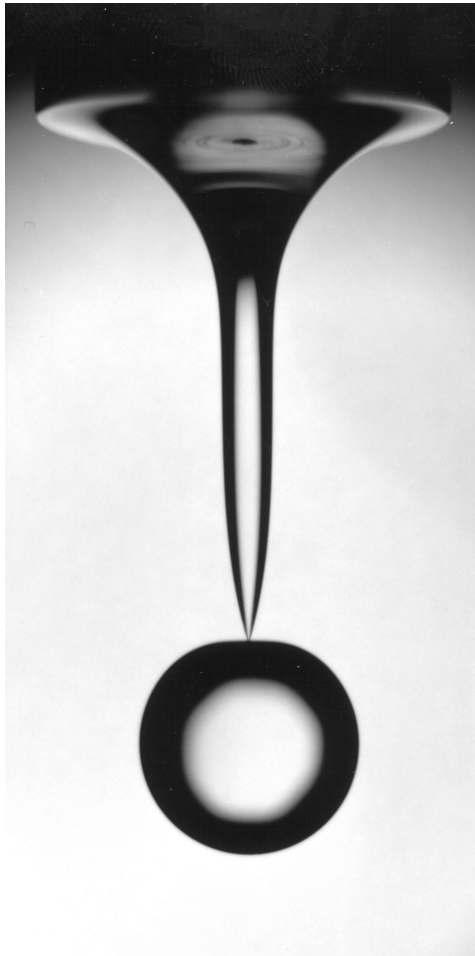
What about air bubble in water?



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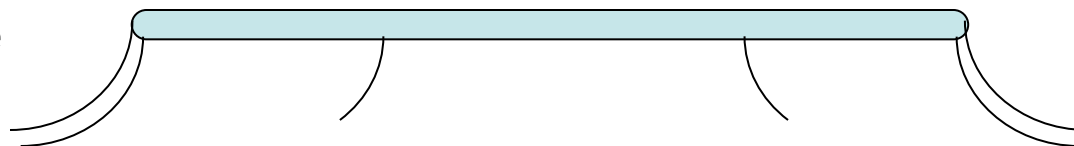


Different response to perturbations

change nozzle shape



slot nozzle

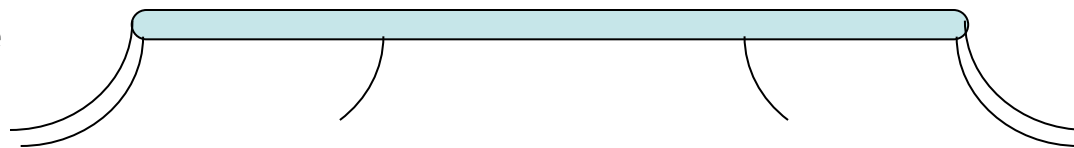


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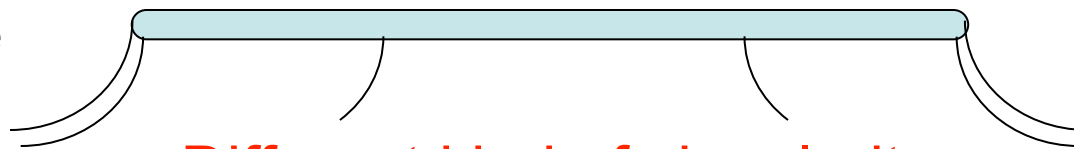
slot nozzle



Different response to perturbations change nozzle shape



slot nozzle



Different kind of singularity

Two possibilities: Nature vs. Nurture

Nature

Lose identity:

Evolution to singularity depends only on material

⇒ no memory

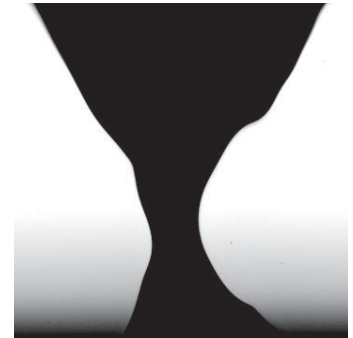
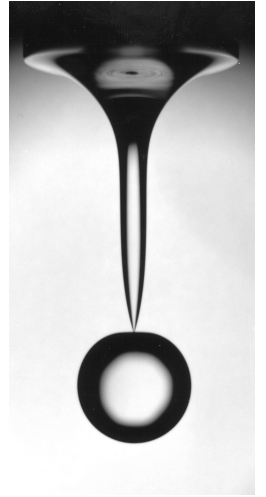
or

Nurture

Retains identity:

Early life determines evolution

⇒ nearly complete memory



Liquid jet impact on target

“water bells”



How general is “bell” formation?

Liquid jet impact on target

“water bells”



How general is “bell” formation?

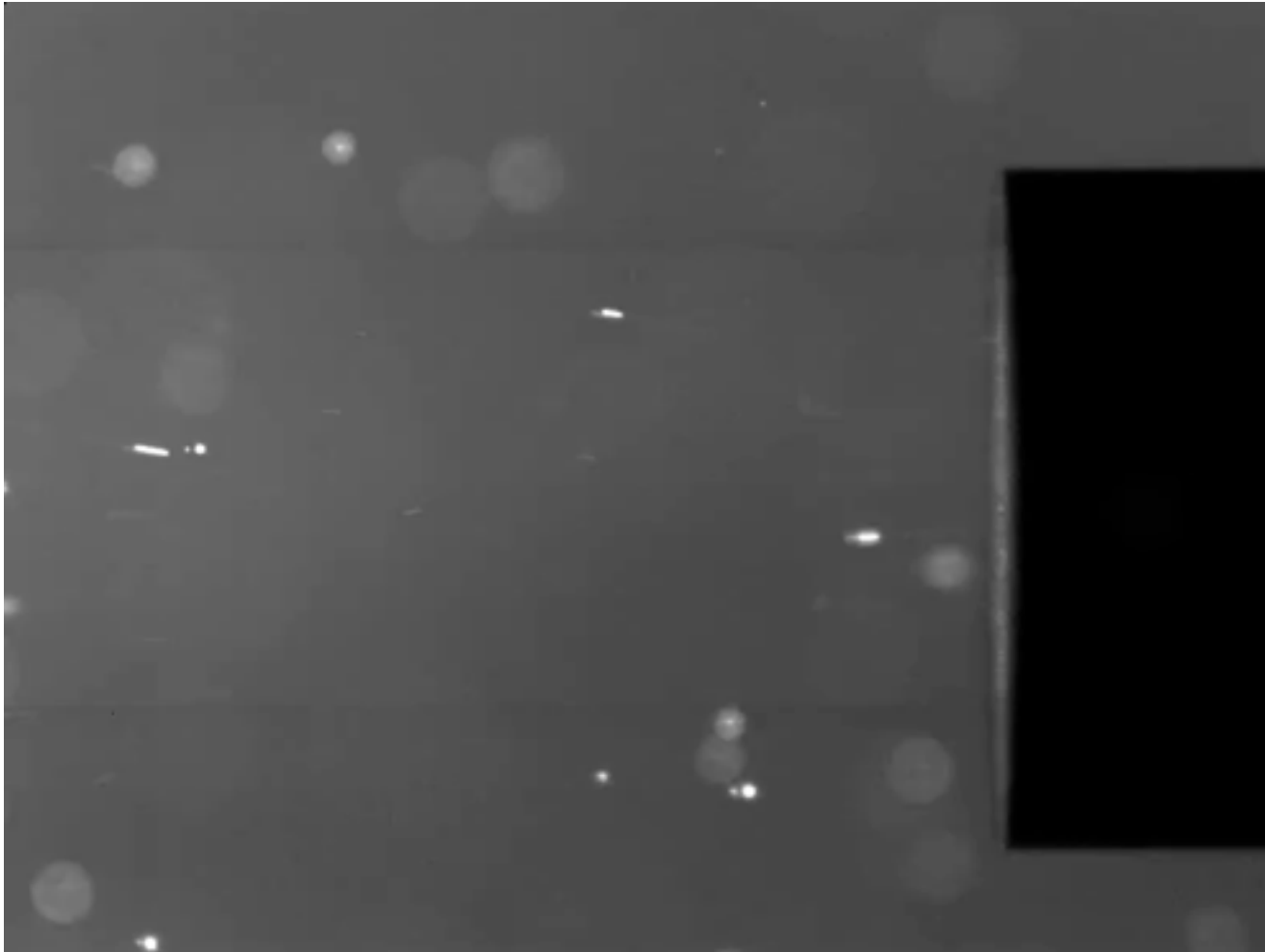
Individual particle collisions with target



500µm glass beads hitting aluminum target

How about jet of granular material?

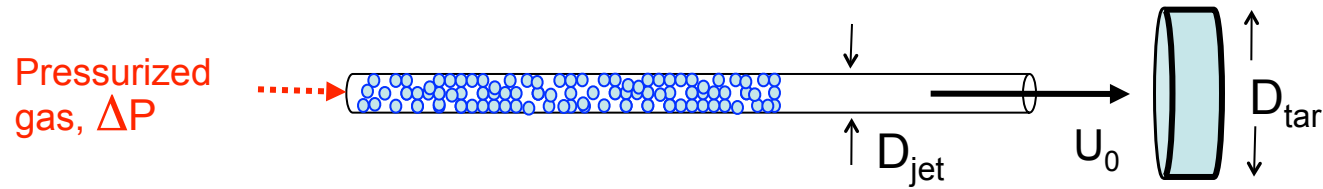
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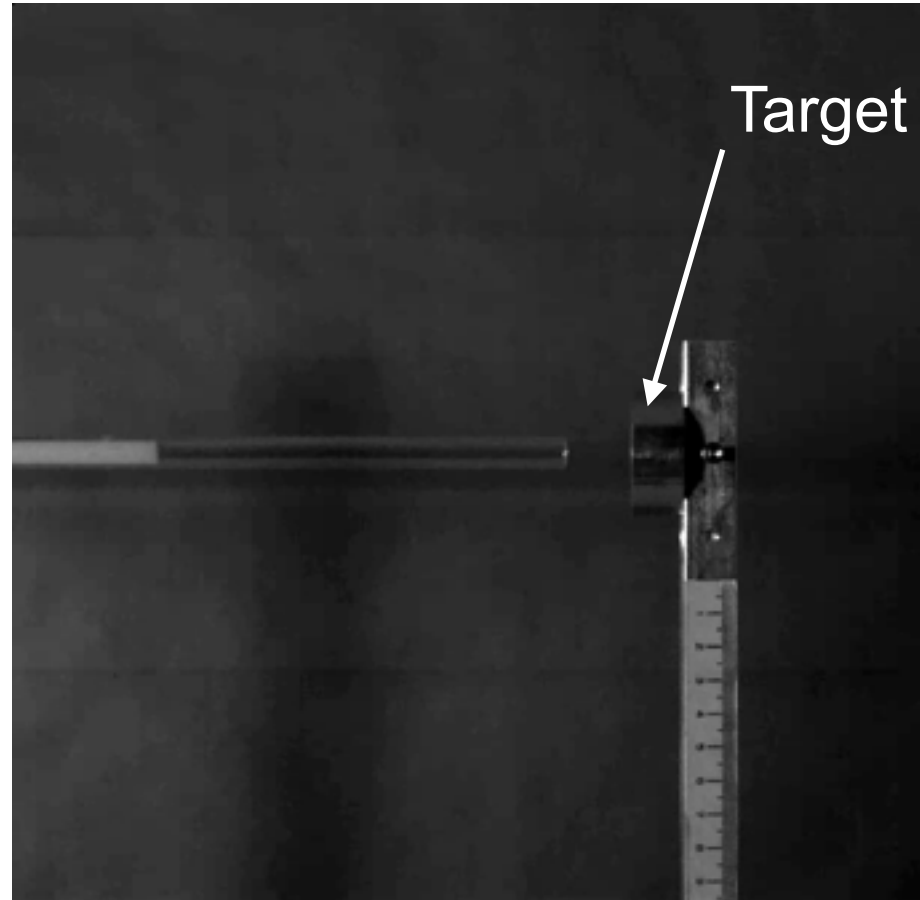
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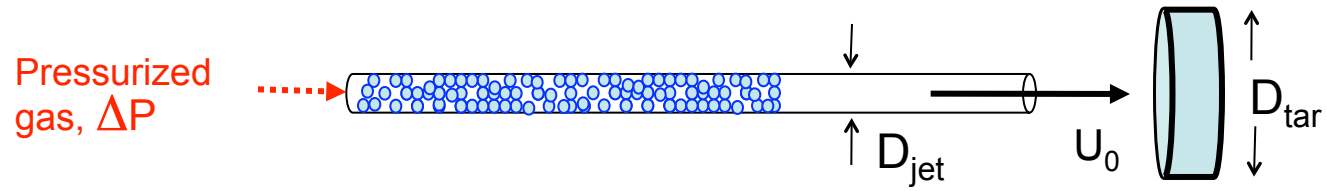


100 μm
glass beads
 $D_{\text{tar}}/D_{\text{jet}} = 4.5$

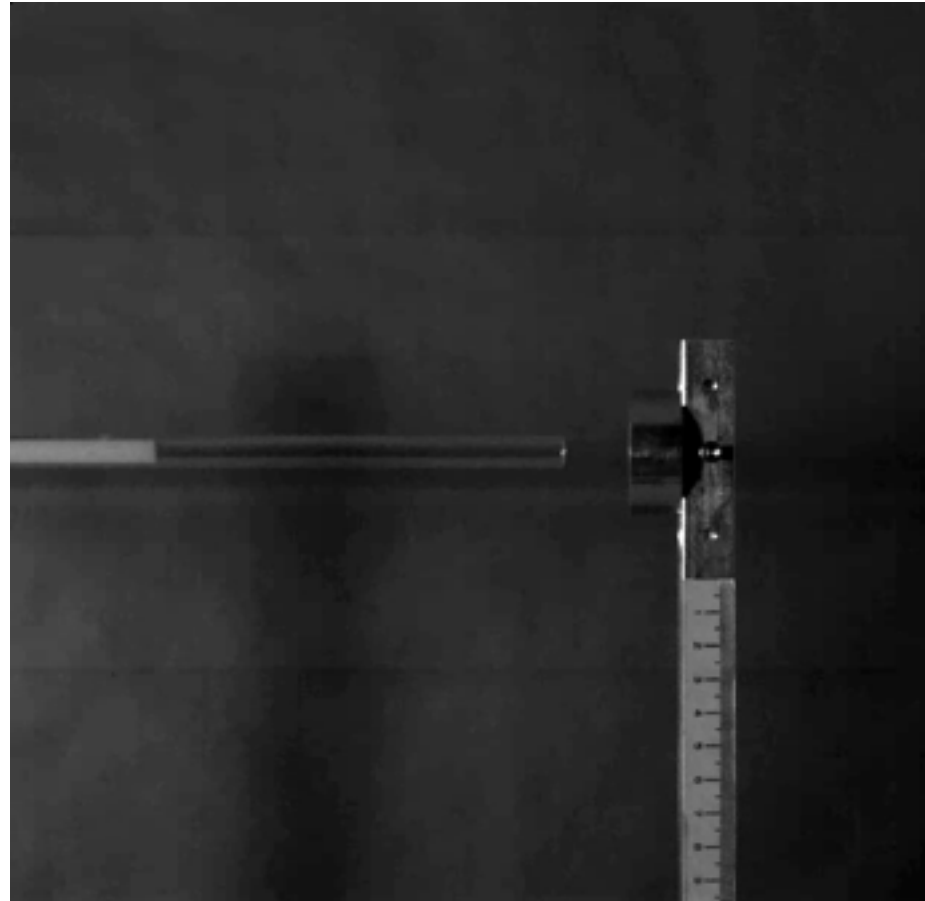


Side view

Granular jet hitting target

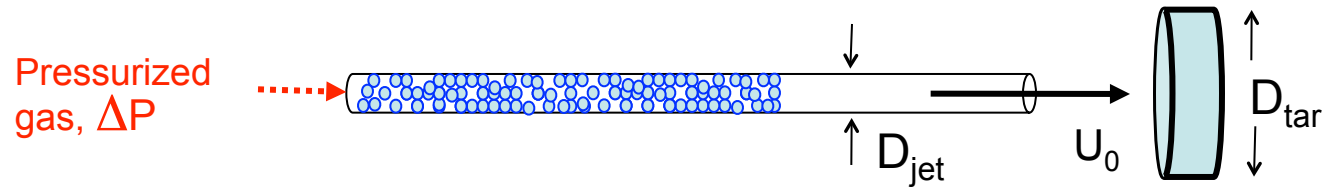


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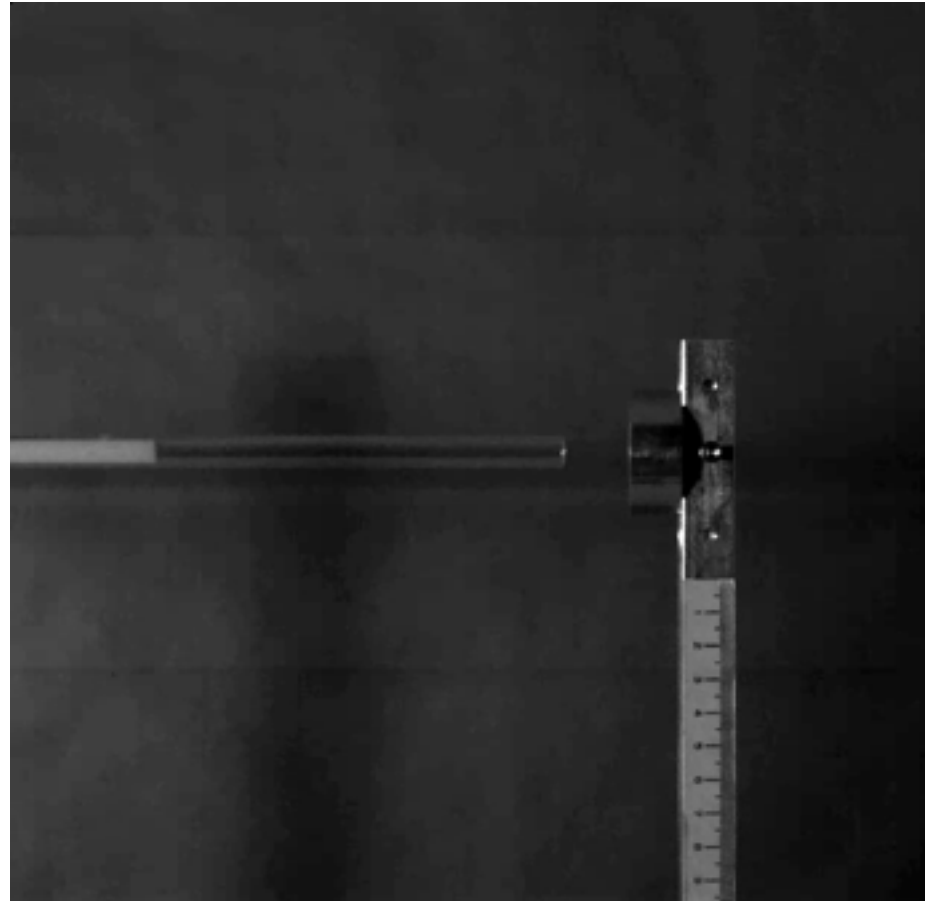


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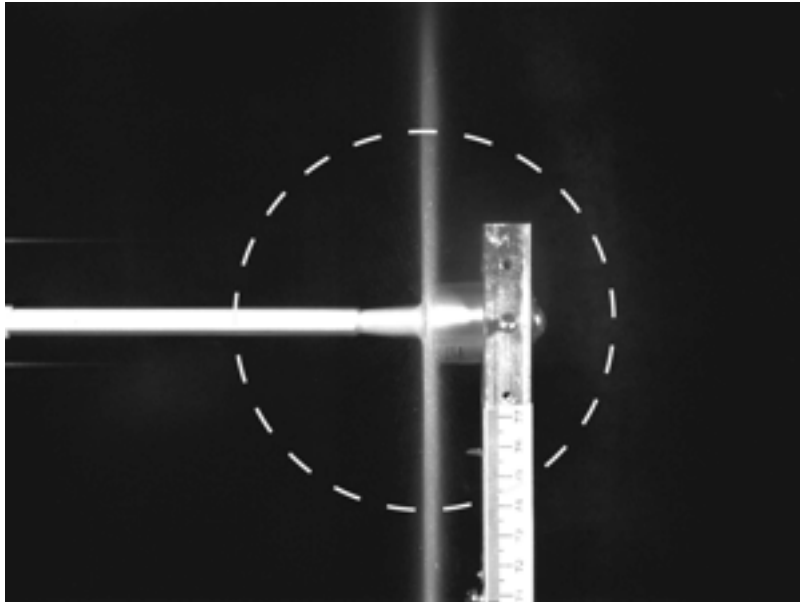
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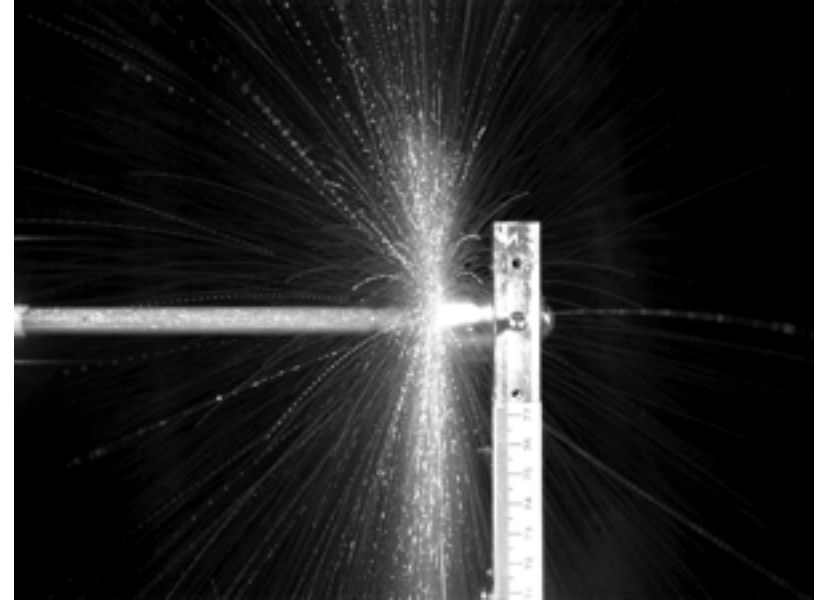
Side view

From fluid to particle

100 μm



500 μm



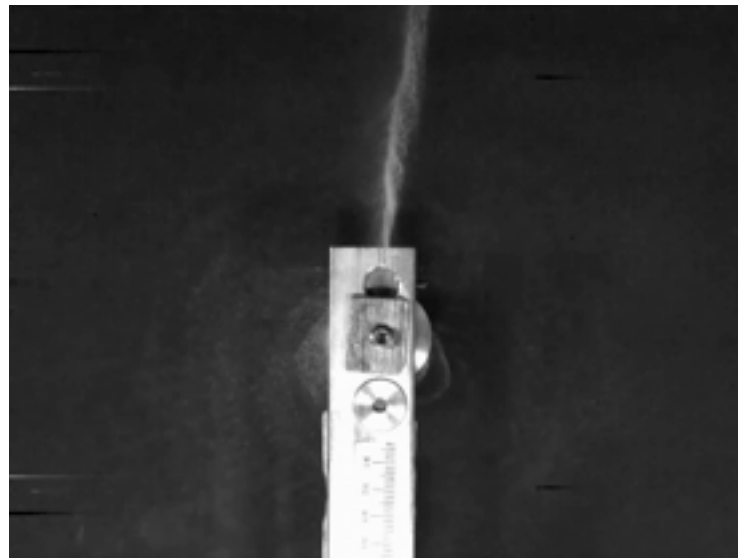
2.1 mm



Liquid formation from discrete particles

Not due to attraction
Not due to confinement
Just kinematics

Classical analog to heavy-ion collider physics: RHIC, CERN
collide gold nuclei \Rightarrow quark-gluon plasma \Rightarrow liquid !!!

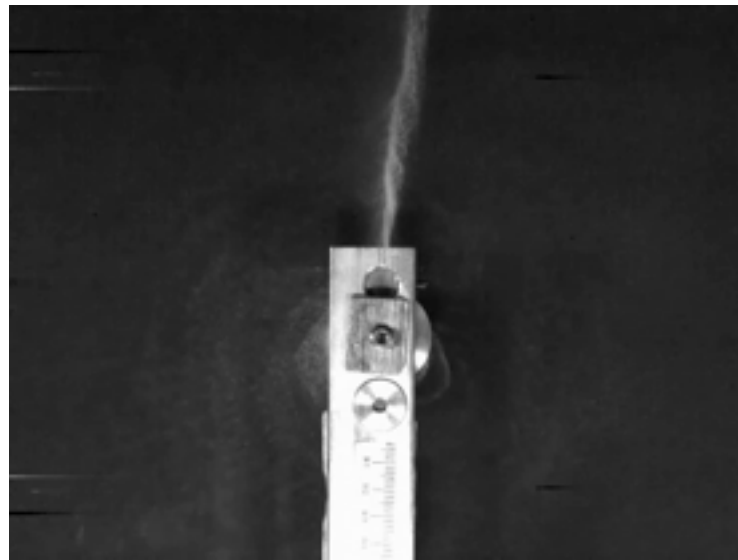


same reason granular gas was liquid

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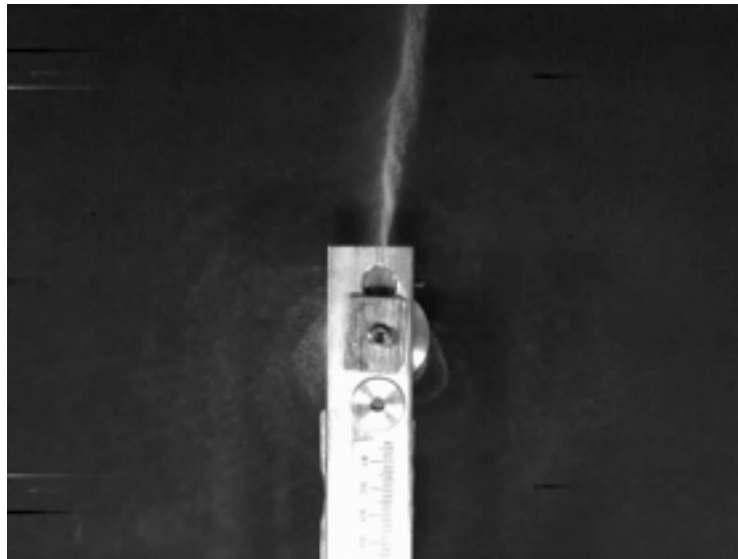


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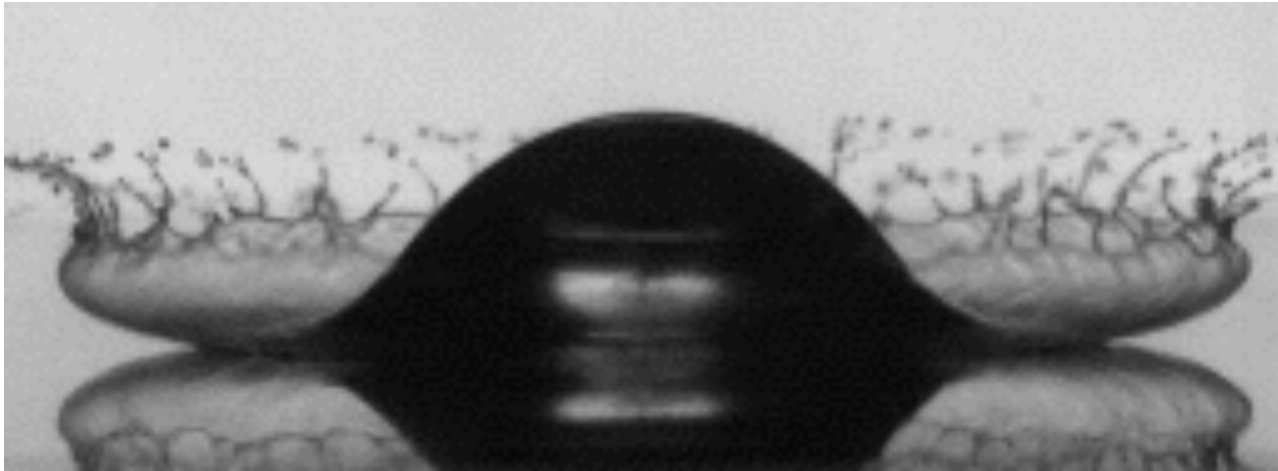
Classical analog to heavy-ion collider physics: RHIC, CERN
collide gold nuclei \Rightarrow quark-gluon plasma \Rightarrow liquid !!!



same reason granular gas was liquid

Raises issue of what it means to be a liquid

Splashing



Drop splashes



Drop of alcohol hitting
smooth, dry slide

Drop splashes



Drop of alcohol hitting
smooth, dry slide

Drop splashes



atmospheric pressure



1/3 atmospheric pressure
(Mt. Everest)

Drop splashes



atmospheric pressure



1/3 atmospheric pressure
(Mt. Everest)

Drop splashes

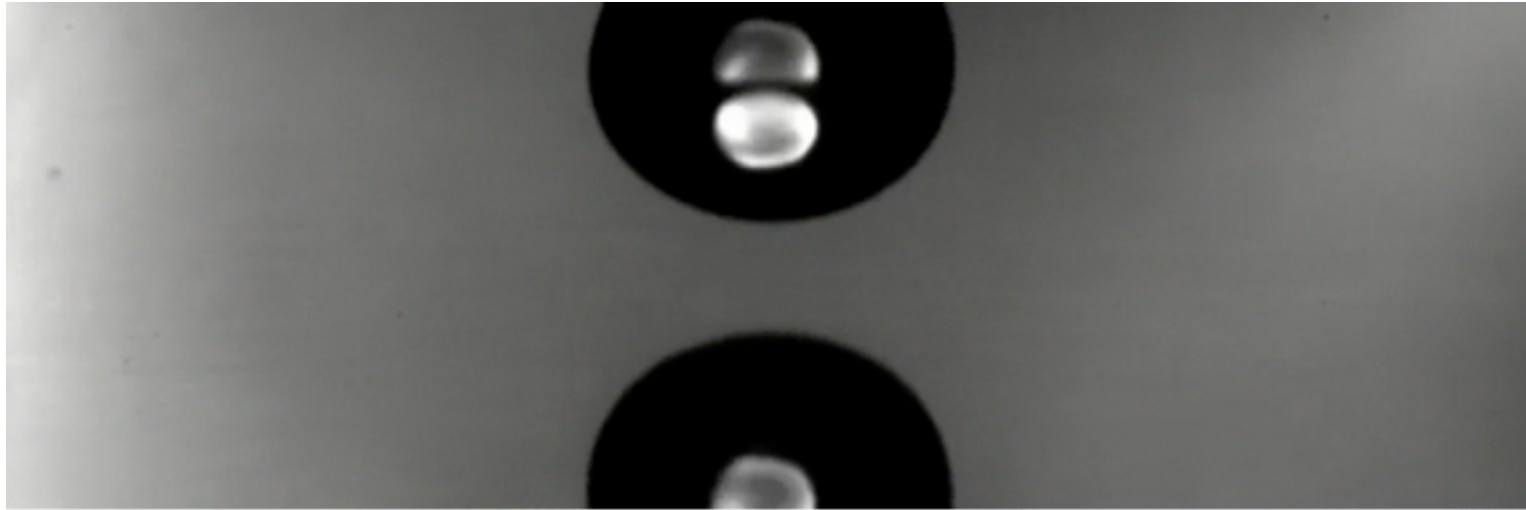


atmospheric pressure



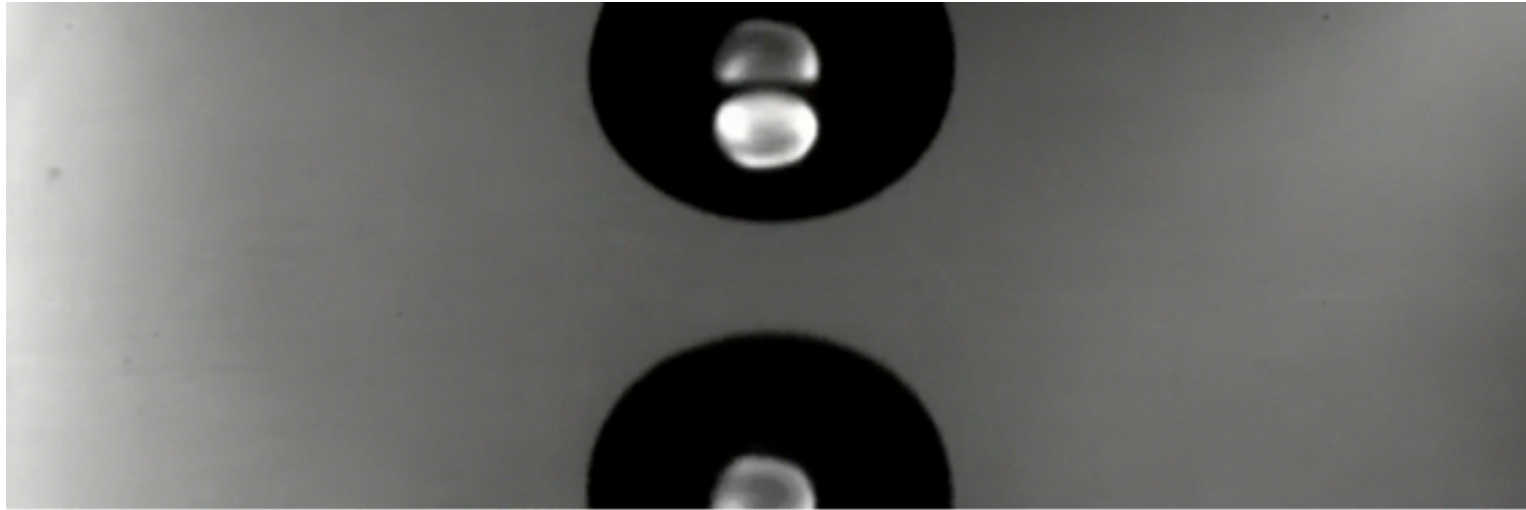
1/3 atmospheric pressure
(Mt. Everest)

10 x higher viscosity



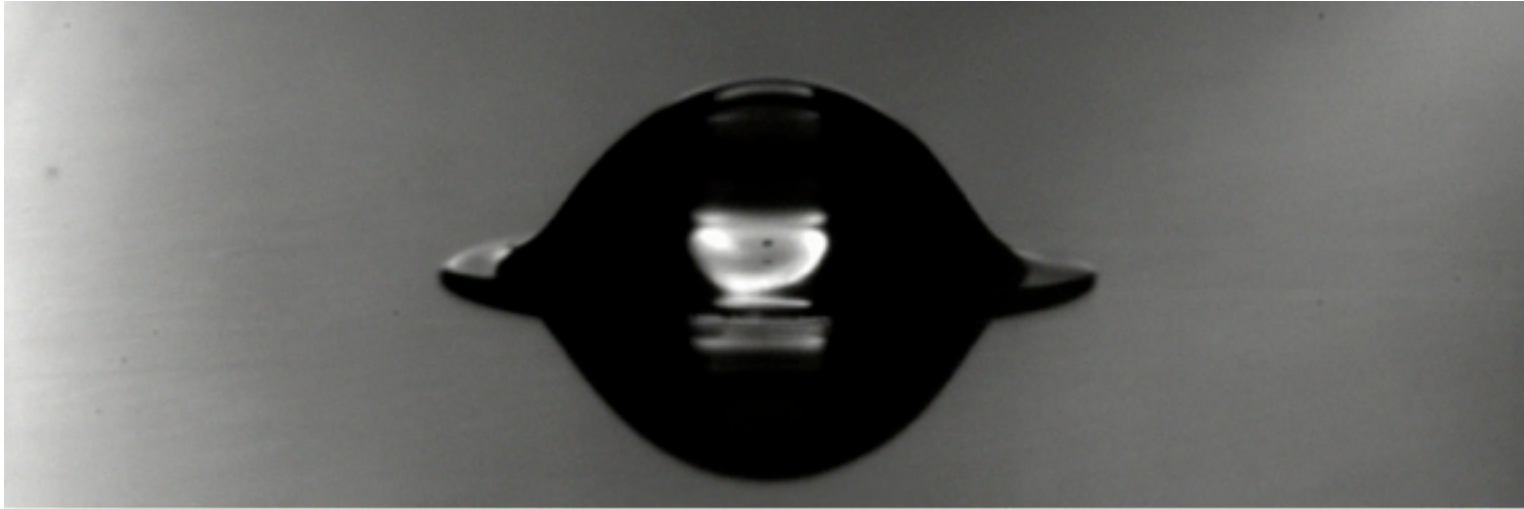
101 kPa

10 x higher viscosity



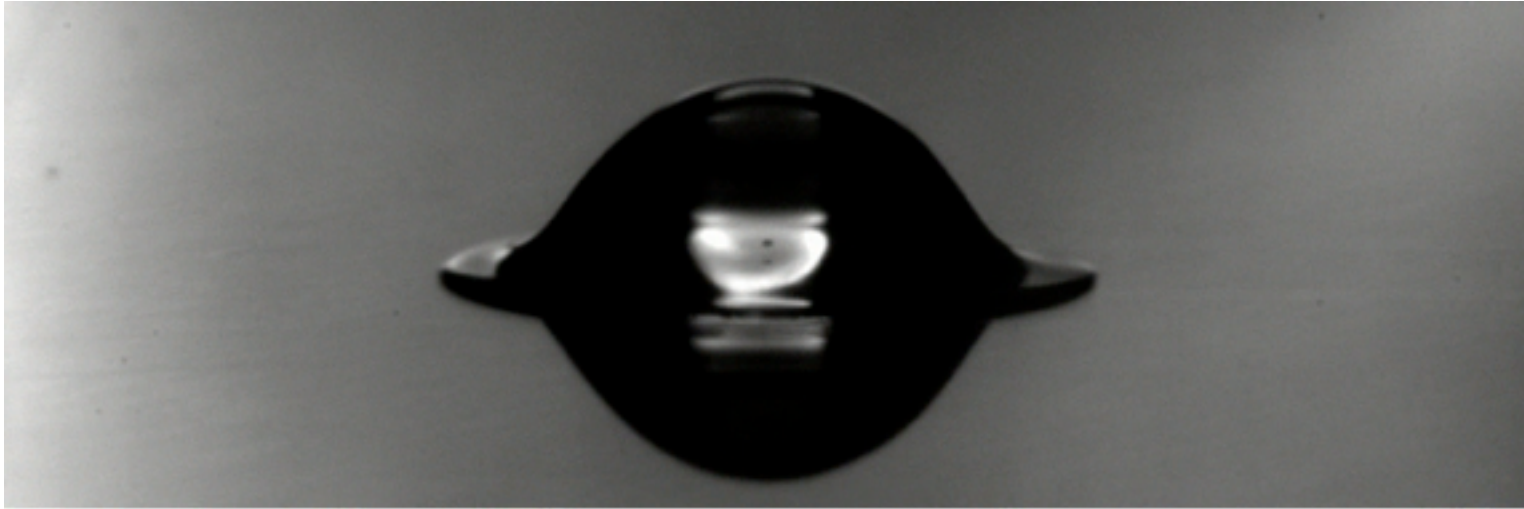
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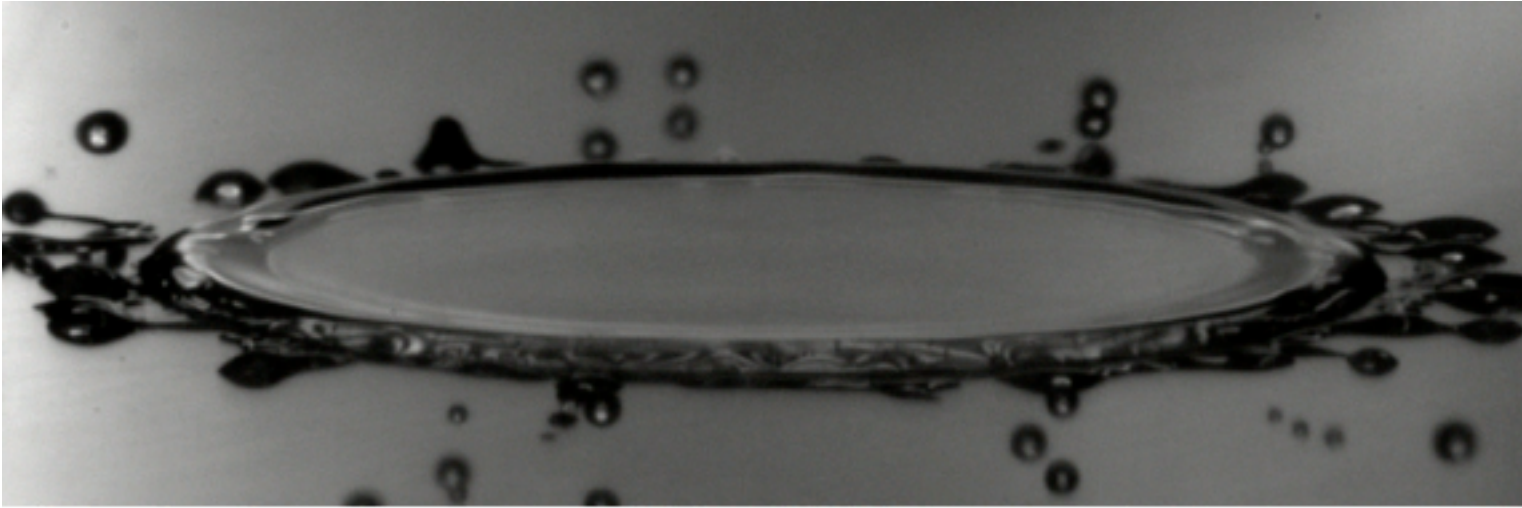
101 kPa

10 x higher viscosity

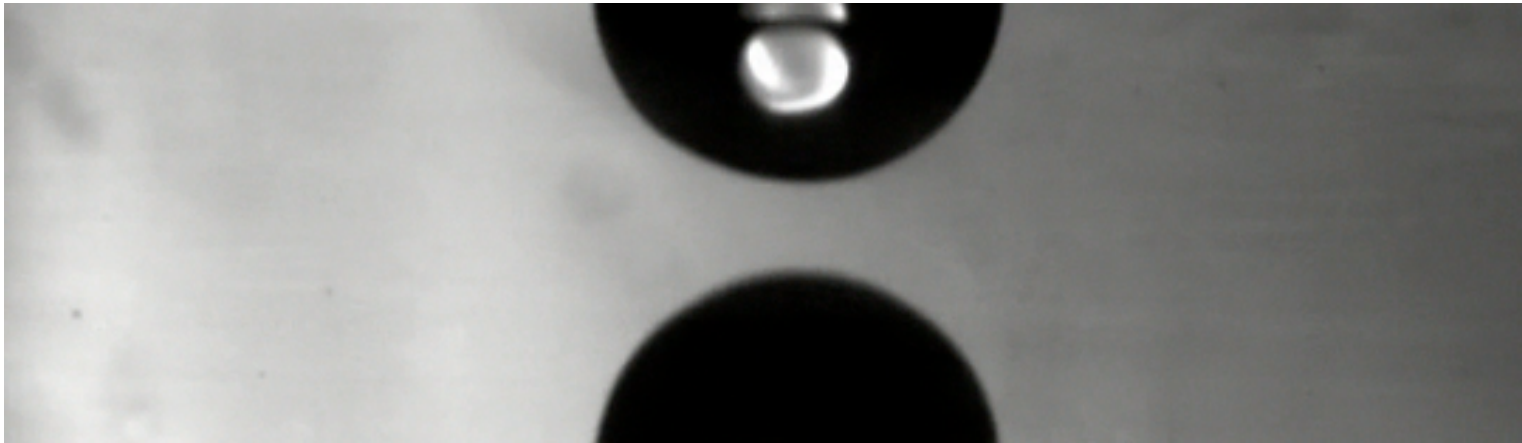


101 kPa

10 x higher viscosity



101 kPa

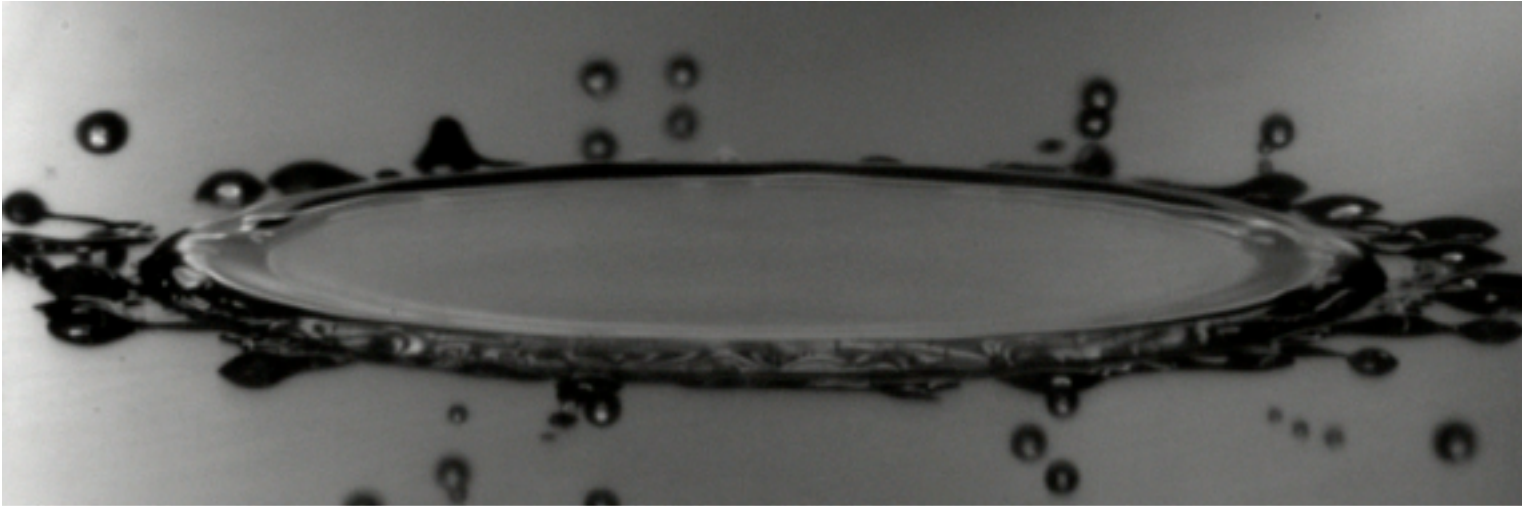


20 kPa

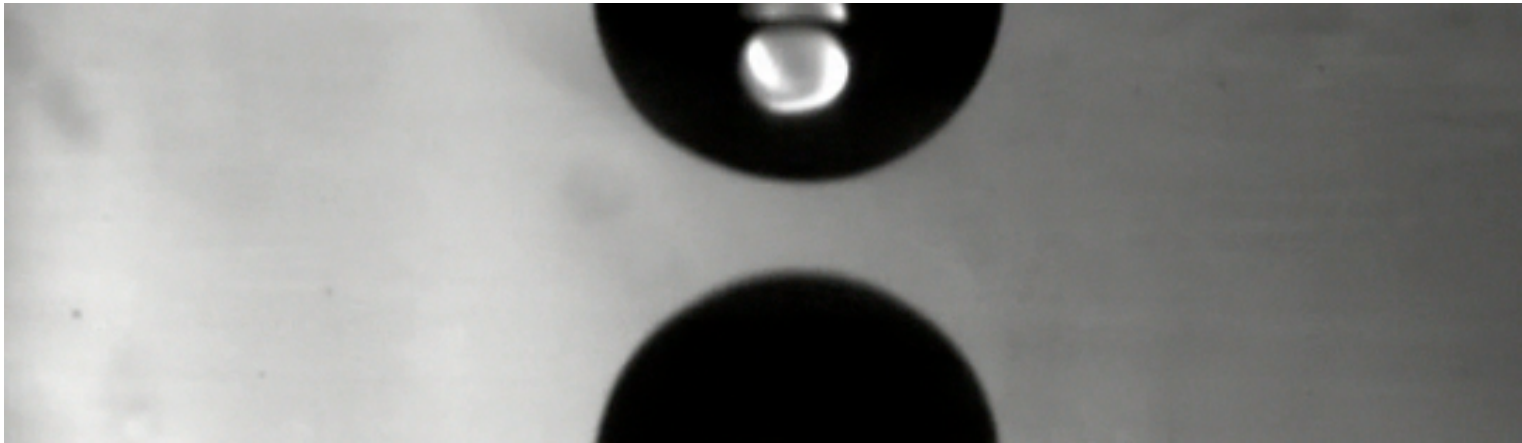
Late-time sheet ejection; low velocity

Air still matters!

10 x higher viscosity



101 kPa

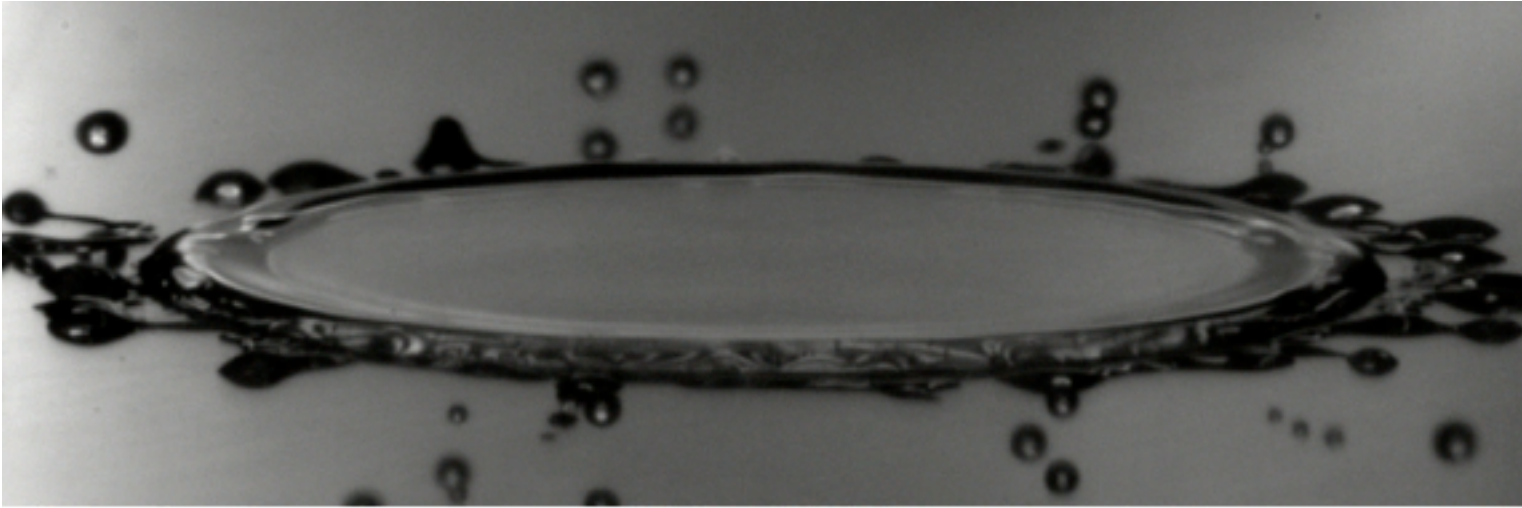


20 kPa

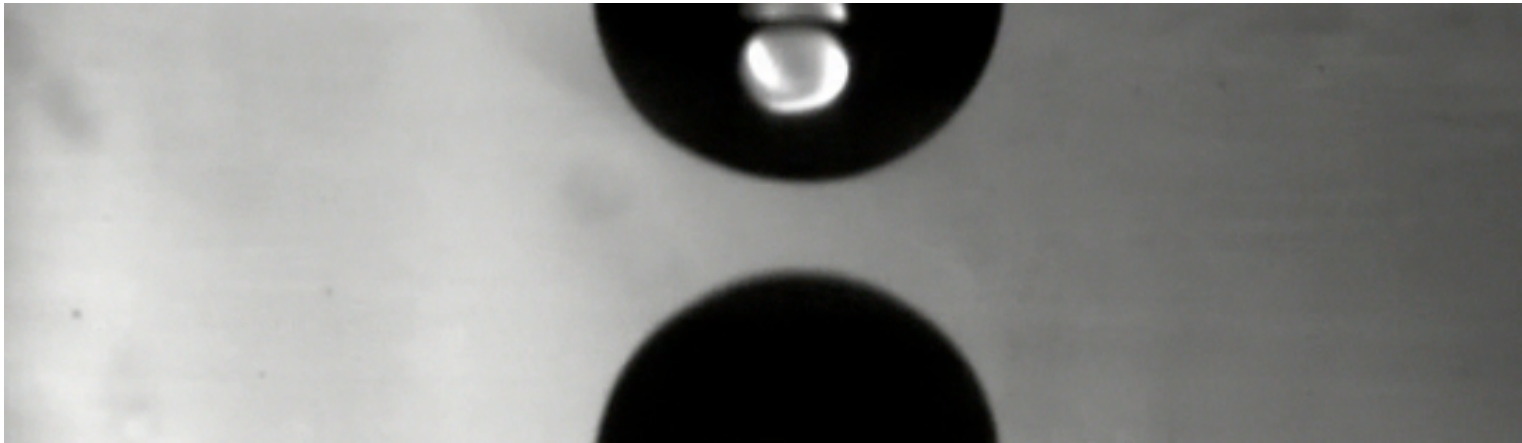
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101 kPa

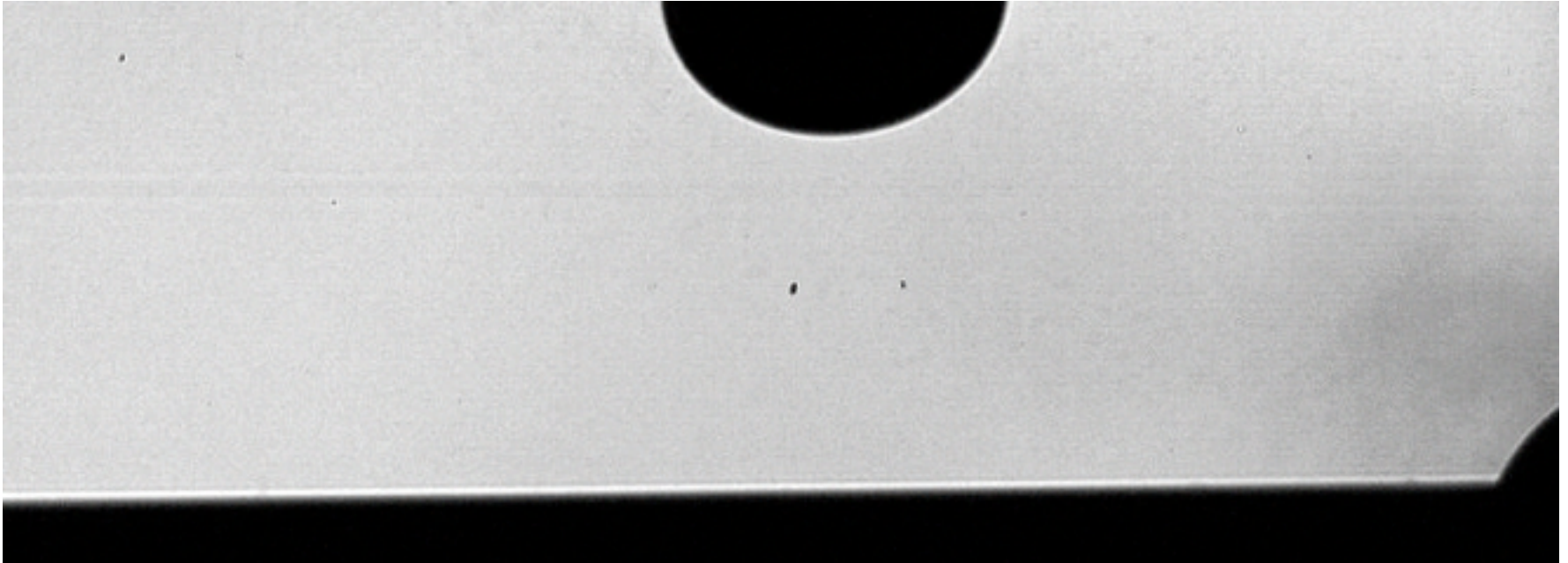


20 kPa

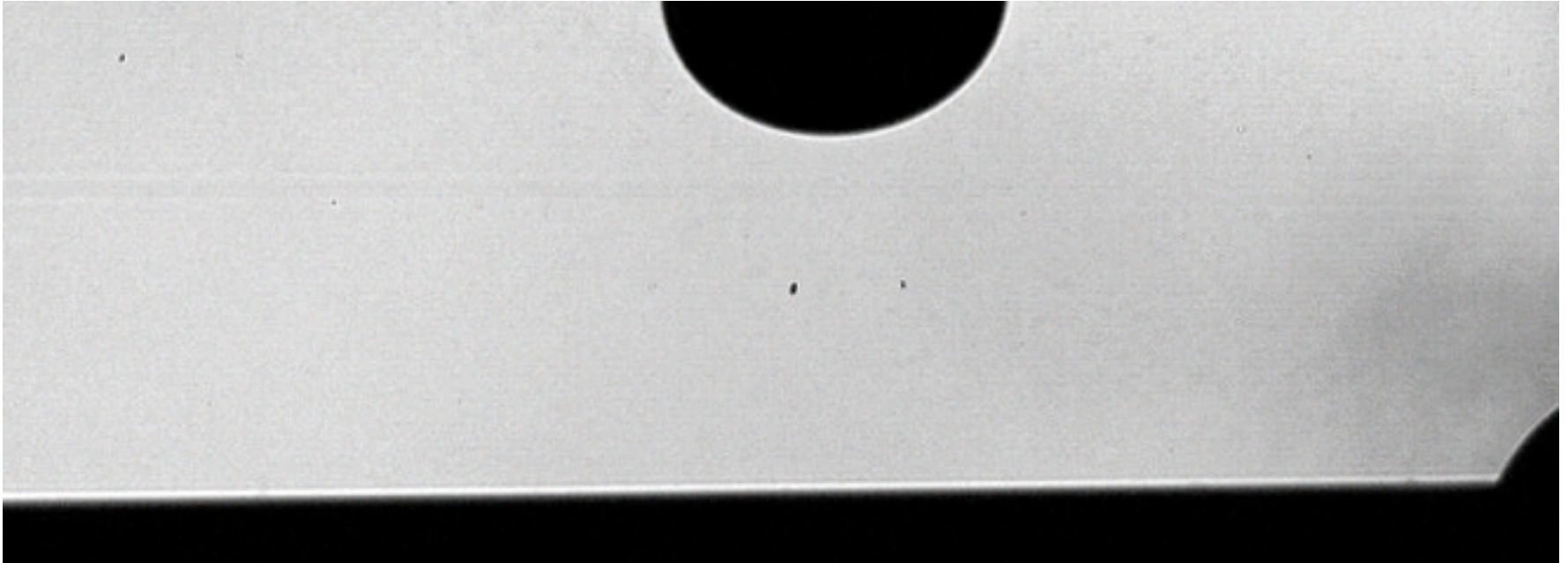
Late-time sheet ejection; low velocity

Air still matters!

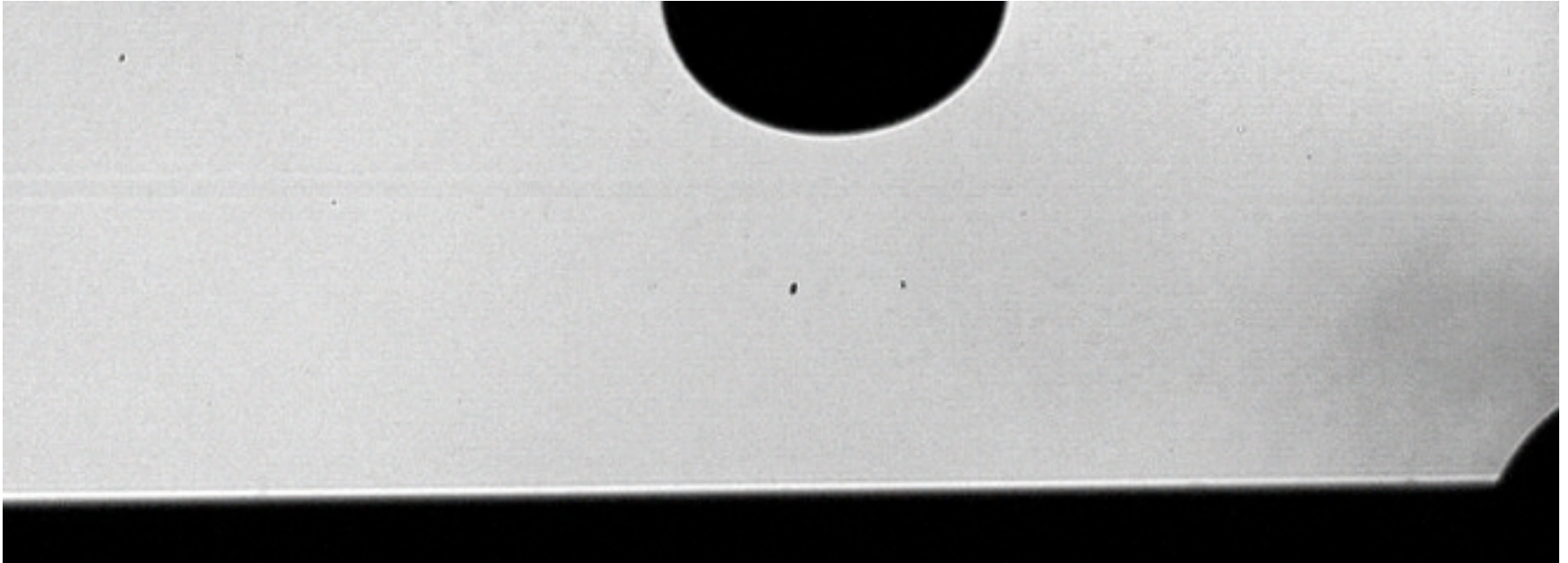
Visualize air above drop



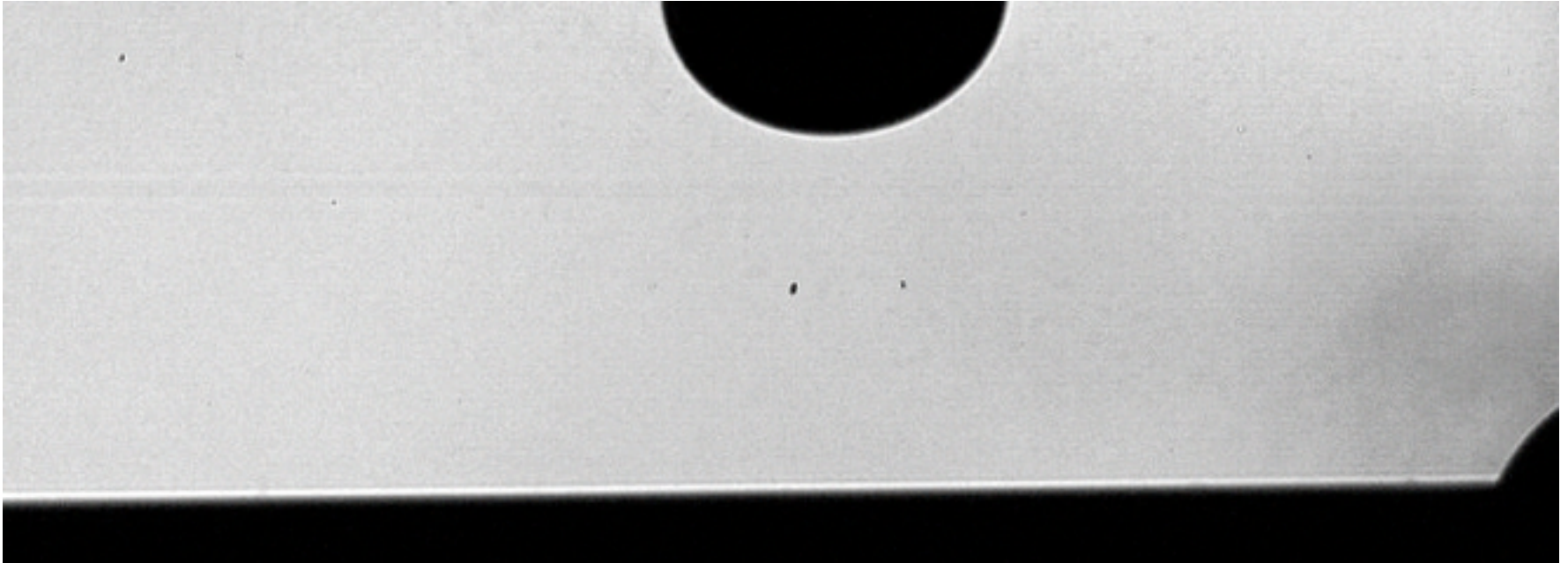
Visualize air above drop



Visualize air above drop



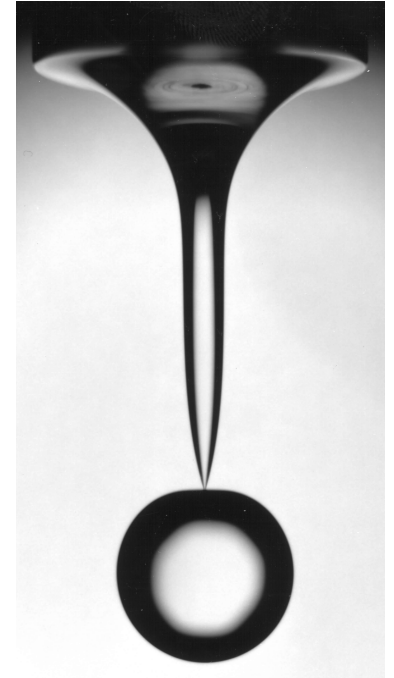
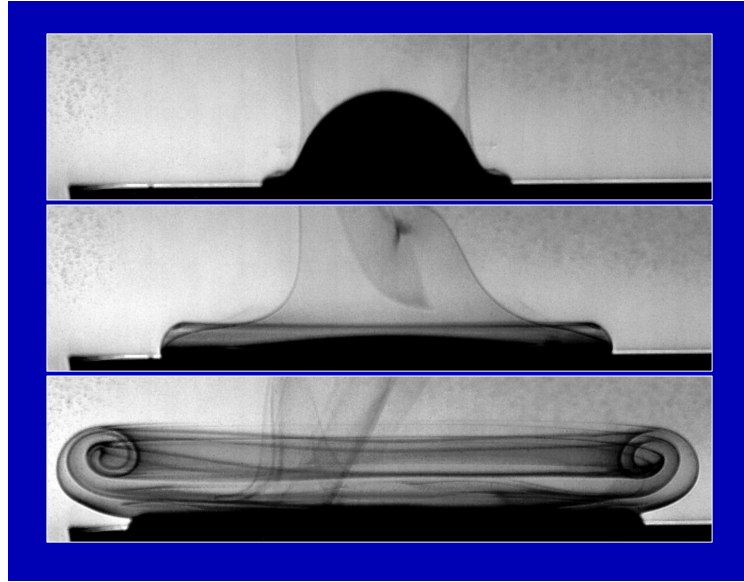
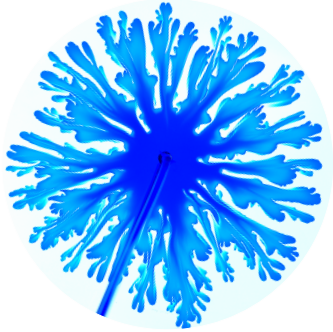
Visualize air above drop



Emergence of structure \Rightarrow nature's texture

Renewed appreciation of world around us

Connections \Rightarrow biology, memory, quark-gluon plasma



Nature reuses same ideas in different phenomena

Scientists reuse same ideas to explain them...

A great idea "is like a phantom ocean beating upon the shores of human life in successive waves of specialization."

A. N. Whitehead



Irmgard
Bischofberger



Radha
Ramachandran



Michael
Brenner



Itai
Cohen



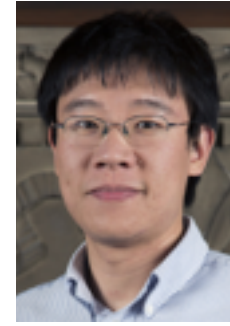
Wendy
Zhang



Nathan
Keim



Laura
Schmidt



Xiang
Cheng



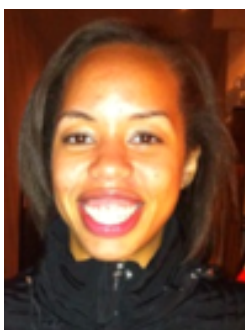
Heinrich
Jaeger



Michelle
Driscoll



Lei
Xu



Cacey
Stevens



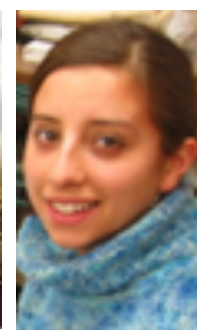
Kelly
Mauser



Andrzej
Latka



Ariana
Strandburg-Peshkin



Loretto
Barcos



Samantha
Jones