

# LSND & Rare Muon Decay

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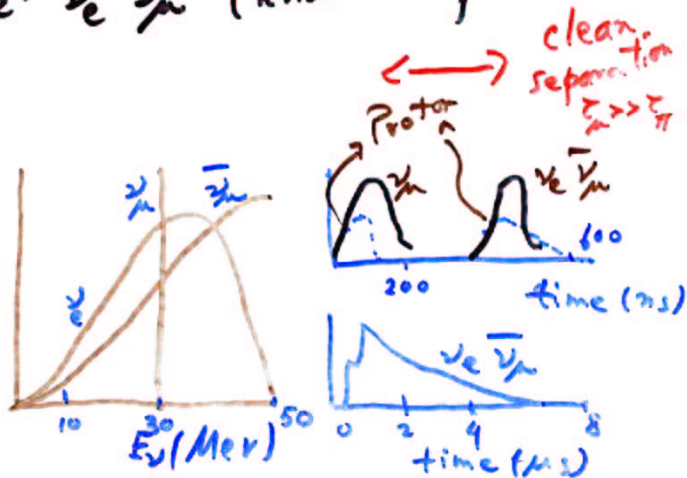
KITP, SB  
3/25/03

1. Description of LSND & KARMEN & Results
2. Possible Explanations:
  - $\nu$  oscillations  $\left[ \begin{array}{l} \text{sterile} \\ \text{CPTV} \end{array} \right.$
  - Rare  $\mu$  Decay Mode
3. Possible Exptl Tests
4. Model for Rare  $\mu$  Decay Mode
5. Summary.

LSND  $\equiv$  Liquid Scintillator  
Neutrino Detector  
@ Los Alamos

KARMEN  $\equiv$  Karlsruhe et al.  
@ Rutherford - Medium-Energy-Neutrino-experiment

$\pi^+$  decay at rest (DAR)  
 $\pi^+ \rightarrow \mu^+ \nu_\mu$  (Both mono-energetic)  
 $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$  (Known spectra).



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G. Drexlin: LSND and Karmen (3/38)

### $\bar{\nu}_\mu - \bar{\nu}_e$ Oscillation Searches at Beam Stop Sources

short baseline geometry  
 $\langle L_\nu \rangle = 15-30$  m from target  
 $\langle E_\nu \rangle = 35$  MeV  
 $\langle L_\nu / E_\nu \rangle \sim 1$  m/MeV  
 $\Delta m^2$  scale  $\sim 1$  eV<sup>2</sup>

$\pi^+ \rightarrow \mu^+ + \nu_\mu$   
 $\downarrow$   
 $e^+ + \nu_e + \bar{\nu}_\mu$

$\bar{\nu}_e + p \rightarrow e^+ + n$

*inverse  $\beta$ -decay off free protons:  
 delayed coincidence signature*

$\pi^-$  and  $\mu^-$  captured by nuclei  
 $\rightarrow$  small intrinsic  $\bar{\nu}_e$  contamination (few  $\times 10^{-4}$ )

Search for  $\bar{\nu}_e$  in LS Detector via Reines-Cowan Technique.



$e^+ \rightarrow e^+ e^- \rightarrow 2\gamma$  prompt signal.

$n \rightarrow n + p \rightarrow d + \gamma \rightarrow 2.2 \text{ MeV}$  Delayed signal  $\Delta t \sim 0(\text{ms})$ .

Same technique in all Reactor expts & KamLAND.

Expected BG.

$\pi^-$  decay in flight  $\rightarrow \mu^- \bar{\nu}_\mu$

$\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$   
(DAR)

Rate from this expected of order  $(0.8) \cdot 10^{-3}$

Further suppressed by software cuts

e.g. total BG events in KARMEN  $\sim 0(10)$   
 ...  $\sim 0(100)$

LSND sees a signal for  $\bar{\nu}_e$  in  $\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_\mu$

KARMEN sees no signal.

Final joint Analysis yields small allowed region in  $\delta m^2 - \sin^2 2\theta$  plane assuming neutrino oscillation. This is the ONLY (claimed) observation of APPEARANCE yet.

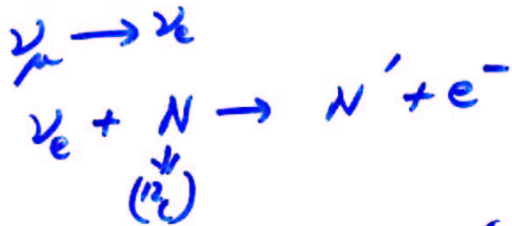
$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = \sin^2 2\theta \sin^2(\phi)$$

$$\phi = \delta m^2 L / 4E$$

$L \sim 10 \dots$   $E \sim 2 \text{ MeV} \dots$

• LSND looked for  $\nu_\mu \rightarrow \nu_e$  oscillations from  $\nu_\mu$ 's in  $\pi^+$  Decay in Flight (D/F)

$\pi^+ \rightarrow \mu^+ \nu_\mu$  (not monochromatic)

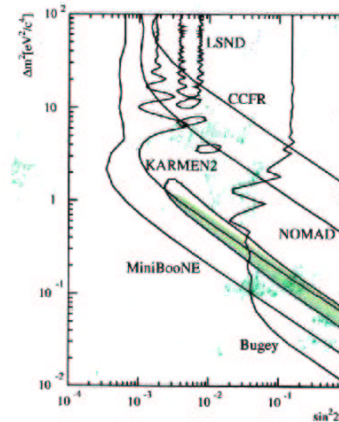


- Evidence Weak (~ 2σ).
- Signature Poor (no tag)
- BE High.
- Less Convincing than  $\bar{\nu}_e$ .

From now on we will ignore this (weak) signal.

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### Joint Analysis of LSND + KARMEN Data.



Slight dependence on whether D/F  $\nu_\mu \rightarrow \nu_e$  signal included or NOT.

FIG. 10: Parameter regions deduced in this work (grey area) compared with existing limits of experiments (Bugey  $\nu_\mu \rightarrow \nu_e$  [18], CCFR  $\nu_\mu \rightarrow \nu_e$  [19] and NOMAD  $\nu_\mu \rightarrow \nu_e$  [20]) and the envisaged sensitivity of the MiniBooNE experiment (with final single horn design [21]).

applied a unified frequentist approach to both likelihood analyses individually. The results underline the feasibility of as well as the necessity for such an approach.

A quantitative joint statistical analysis has been performed leading to a level of 36% incompatibility of the experimental outcomes, corresponding to individual confidence levels of 60%. For the cases of statistical compatibility, the common parameter regions have been identified on the basis of the unified frequentist approach applied to the combined likelihood function of KARMEN 2 and LSND. The derived confidence regions in  $(\sin^2(2\theta), \Delta m^2)$  clearly differ from an often applied but incorrect graphical overlap of the confidence regions of the individual experiments. There are two oscillation scenarios with either  $\Delta m^2 \approx 7 \text{ eV}^2/c^4$  or  $\Delta m^2 < 1 \text{ eV}^2/c^4$  compatible with both experiments.

We performed a joint statistical analysis incorporating some of the systematic uncertainties of the experiments, such as neutrino flux uncertainty, accuracy of known cross sections and resolution functions of both experiments. Further -unknown- systematic uncertainties

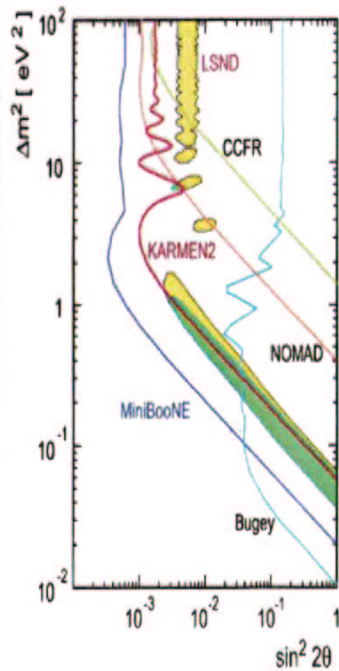
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G. Drexlin: LSND and Karmen (31/38)

### Conclusions

final oscillation results from LSND and KARMEN2 published and compatibility analysis submitted for publication



#### LSND (1993-98)

combined DAR & DIF analysis (new reconstr.)  
 $87.9 \pm 22.4 \pm 6.0$  beam excess events  
 $P = (0.264 \pm 0.067 \pm 0.045)\%$

#### KARMEN2 (1997-01)

final DAR oscillation analysis 4y of data  
 15 evts.  $\rightarrow (15.8 \pm 0.5)$  bg expect. *no excess*  
 $\sin^2 2\theta < 1.7 \times 10^{-3}$ , most stringent limit so far

#### LSND & KARMEN2

detailed statistical analysis using full inform.  
 incompatibility at individual 60% Confid. Levels  
 areas of stat. compatibility only at  $\Delta m^2 < 1 \text{ eV}^2$   
 L-number violating  $\mu$ -decays excluded

## LSND Effect

- $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$  normal mode
- In DAR see  $\bar{\nu}_e$  at a level  $(1-3) \cdot 10^{-3}$ .

What could be the origin?

- $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillations?

need  $\Delta m^2 \sim O(\text{eV}^2)$   
 $\sin^2 2\theta \sim 0.005$ .

- New Rare Decay Mode?

$$\mu^+ \rightarrow e^+ \bar{\nu}_e X.$$

- In  $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$  with B.R.  $\leq O(10^{-3})$  channel DIF evidence weaker.

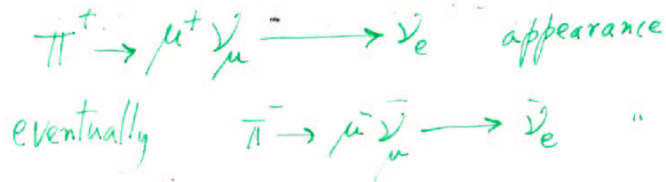
If oscillations, need 4th sterile  $\nu$ ,  
 4th  $\rightarrow$  • Because  $\Delta m_{sol}^2 + \Delta m_{ATM}^2 + \Delta m_{LSND}^2 \neq 0$

ster  $\rightarrow$  • Because of  $\Gamma(Z \rightarrow \nu_i \bar{\nu}_i)$ .

Options (for Theorists)

- A • Ignore LSND
- B • Live with 4th sterile neutrino
- C • Give up CPT conservation
- D • Rare Decay of  $\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_x$

Mini-Boone Will test (B) & (C)



But does not check LSND because it does not use  $\nu_e$ 's from A-day.

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Possible  $4\nu$  schemes

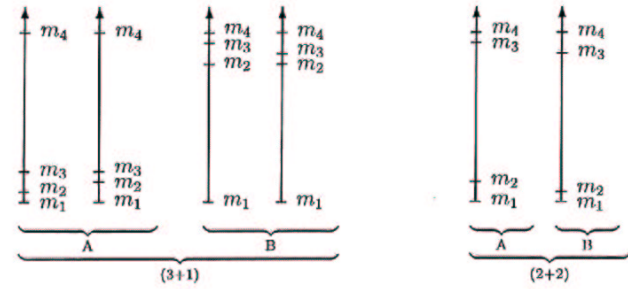
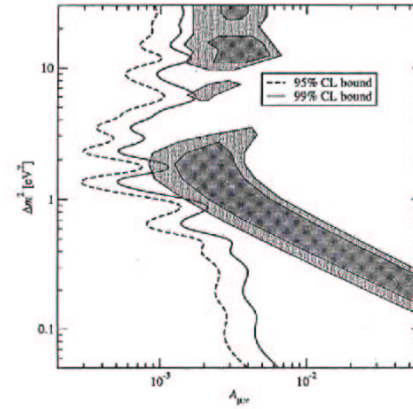


FIG. 39. The six types of 4-neutrino mass spectra. The different distances between the masses on the vertical axes represent the different scales of mass-squared differences required to explain solar, atmospheric and LSND data with neutrino oscillations.



Possible Problem?

FIG. 40. Upper bounds (at 95 and 99% CL) on  $A_{\mu e} \equiv 4|U_{e4}U_{\mu 4}|^2$  in the context of (3+1)-schemes. The shaded regions are the regions allowed by LSND at 90 and 99% CL.

In (3+1) scheme  $P_{\mu e}(LSND) = A_{\mu e} \sin^2 \frac{\Delta m^2 L}{4E}$   
 $A_{\mu e} = 4U_{\mu 4}^2 U_{e4}^2$  Bounded by ROGEY / CHOOZ  
 $\rightarrow$  Bounded by CDHS

# Problems with 4ν scenarios for LSND

*Maltoni, Schatz, Valle (2002)*

• In 3⊕1 schemes

$$P_{\mu e} = A_{\mu e} \sin^2(\delta m_{21}^2 L/4E)$$

↳  $4U_{\mu 4}^2 U_{e4}^2$

↓                      ↳ bounded by Bugey/CDHS

bounded by CDHS

With  $A_{\mu e}$  thus constrained  
&  $P_{\mu e}$  (LSND + KARMEN).

no fit is possible.

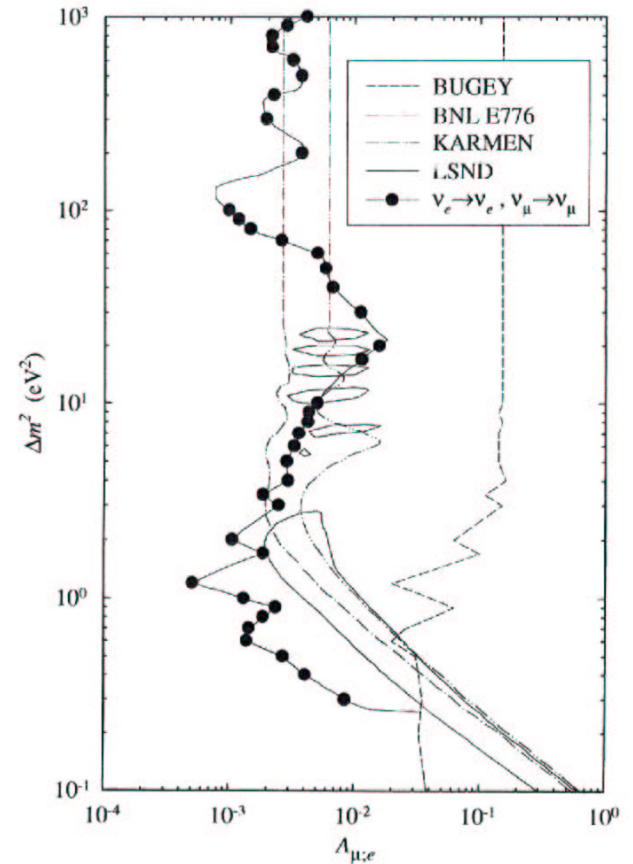
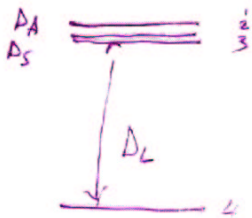


Figure 2: Exclusion regions at 90% CL in the  $A_{\mu e}$   $\Delta m^2$  plane for small  $|U_{e4}|^2$  and  $|U_{\mu 4}|^2$  in the model with mixing of four neutrinos and a mass hierarchy discussed in Section 3. The regions excluded by the BNL E776 and KARMEN  $\nu_{\mu} \rightarrow \nu_e$  appearance experiments are bounded by the dash-dotted and dash dot-dotted curves, respectively. The dashed line represents the results of the Bugey experiment. The curve passing through the circles is obtained from the results of the Bugey, CDHS and CCFR84 experiments using Eq.(20). The region allowed by the LSND experiment is shown as the shadowed region limited by the two solid curves.

Pierce & Murayama  
Post-WMAP

Maltoni et al.

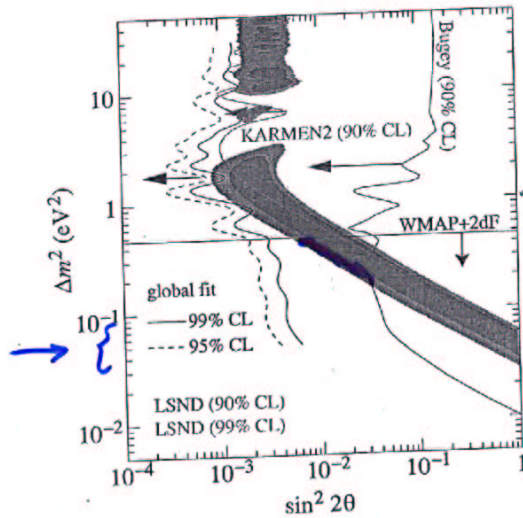


FIG. 1: The LSND Allowed region, with Bugey and Karmen [17] exclusion regions. The constraints from the global fit [18] as well as the limit from the combination of WMAP and 2dFGRS data are also shown. The contours from the global fit would, of course, continue on to lower values of  $\Delta m^2$ , but Ref. [18] did not show this region.

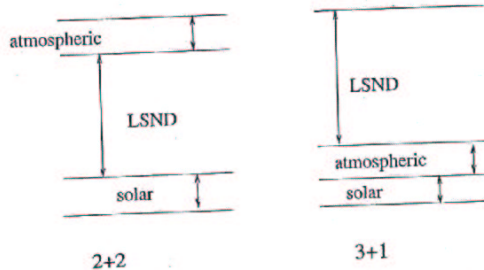


FIG. 2: Sample neutrino spectra in the light of LSND. Different permutations are also possible.

couplings to the other particles of the standard model.

[16] found this 2+2 while a 3+1 spectrum level [16, 18]. The in large part due baseline disappears and Bugey. Add only marginally in next two sections, contradicted by cos

III. BIG-B

By measuring  $t_l$  can place bounds on at the time of Big Bang. These bounds are of effective allowed degrees of freedom of the universe,  $w$  an earlier time, at translates into  $m_c$  to photon ratio,  $\eta$   $^4\text{He}$  abundance and  $\eta$  places a bound fixed  $N_{eff}$ , a high primordial  $^4\text{He}$ ; so the constraint on

In the era before data alone were measurements of primordial for the separate analysis by [23] and consequently disfavored by BBN light element abundances some measurements substantially lower presence of these often taken [25]. found that even confidence level.

However, after the situation has determined [9]  $\Omega$  to an  $\eta = 6.5$  above, the expected  $N_{eff} = 0.949 \pm 0.0$

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In 2+2 schemes there must be some  $\nu_s$  mixing present in solar & atm.  $\nu$ 's. Current limits getting strong enough to rule out this fit to LSND.

Current Bounds:

$$\frac{1}{2} \Delta_A$$

$$\frac{3}{4} \Delta_S$$

$$P_s(\text{atm}) < 0.45$$

$$P_s(\text{solar}) < 0.35$$

$$(Global) @ 99\% CL$$

$$\Rightarrow P_s(\text{total}) < 0.8$$

Possible Problem?

However, Pas & Weiler....  
Tune in Tomorrow.

↓ getting smaller with time!



Maltoni, Smets, Valle

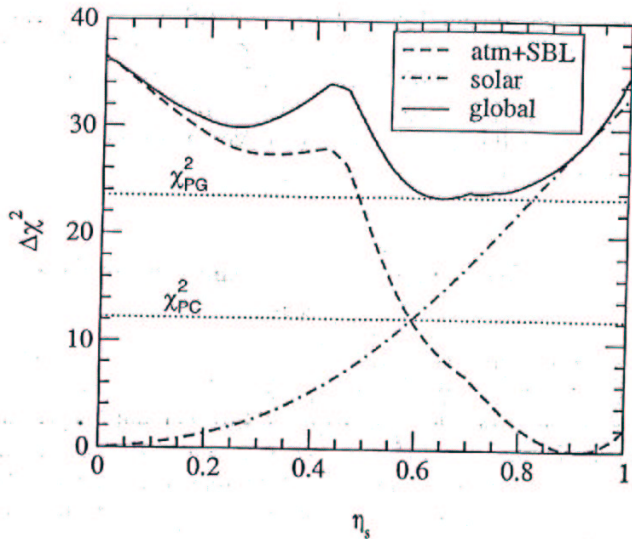


Figure 6.  $\Delta\chi^2_{\text{SOL}}$ ,  $\Delta\chi^2_{\text{ATM+SBL}}$  and  $\bar{\chi}^2_{\text{global}}$  as a function of  $\eta_s$  in (2+2) oscillation schemes. Also shown are the values  $\chi^2_{\text{PC}}$  and  $\chi^2_{\text{PG}}$  relevant for parameter consistency and parameter g.o.f., respectively.

For the parameter obtained from the two data sets and calculating the C.L. at which the difference is consistent with zero. According to Eq. (A.5) we find

$$\chi^2_{\text{PG}} \equiv \bar{\chi}^2_{\text{min}} = 23.5. \quad (5)$$

evaluated for 1 d.o.f. such a high  $\chi^2$ -value leads to the marginal parameter g.o.f. of  $1.3 \times 10^{-6}$ .

From Eqs. (4) and (5) we conclude that (3) is not a

Caveat: Pais, Soyr, Weiler hep-ph/0209373

If  $\nu_{e3}$  (and its generalisations  $\nu_{e3}, \nu_{\mu 3}$  in 4x4 MNS matrix) allowed to be non-zero,

Then fits for  $2\oplus 2$  are possible.

Need a general analysis (global) of solar  $\oplus$  Atm.  $\oplus$  SBL  $\oplus$  LSND with  $\nu_{e3} \& \nu_{\mu 3} \neq 0$  before ruling out  $2\oplus 2$  possibility.

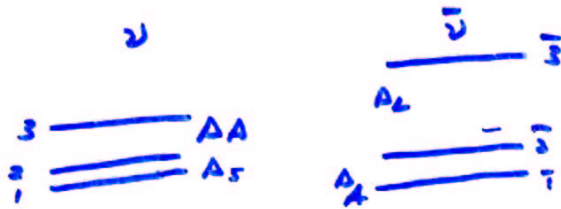
i.e.

Solar	$\nu_e \rightarrow \nu'' = a\nu_e + b\nu_s + \epsilon\nu_\mu$
ATM	$\nu_\mu \rightarrow \nu' = \alpha\nu_e + \beta\nu_s + \delta'\nu_e$
LSND	$\nu_e \rightarrow \nu''' = \zeta\nu_\mu + \xi\nu_s$

Then  $b^2 + \beta^2 \neq 1$  but  $\underline{b^2 + \beta^2 = 1 - \xi^2}$

82 CPTV with 3 flavors & LSND  
 (Murgano, Yanagida, Barenboim, Boissier, Lykken, Denton)

Proposal:

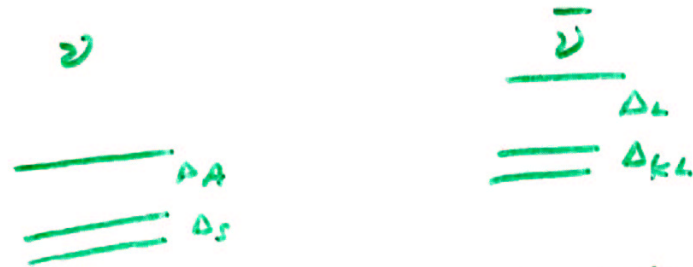


- Implications:
- Mini-BoONE will see oscillation ONLY in  $\bar{\nu}$  channel
  - Even if LMA correct for Solar, KamLand will not see it. (depletion)
  - LSND result for  $\nu \rightarrow \nu_e$  fluctuation

DEC. 6, 2002 Kamland observes depletion of  $\bar{\nu}_e$ 's at  $L/E \sim \frac{175 \text{ km}}{(2-8) \text{ MeV}}$   
 consistent with LMA & with CPT.

- Interesting Theoretical issues.  
 Higgs - non-local but seemingly  $\rightarrow$   $\nu$  propagator is LV.

84 New (post-Kamland) Proposal Barenboim et al. <http://arxiv.org>  
 for CPTV & LSND



- To test, need to distinguish  $\nu$  &  $\bar{\nu}$  events in atm. data  
 e.g. } INO
- Borzino/KL discrepancy... -
- $\Delta_{KL} \neq \Delta_{\text{solar}}$  (near equality is an accident)
- Mini-BoONE should see  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$   
 BUT NOT  $\nu_\mu \rightarrow \nu_e$  with  $\Delta_{LSM}$ .

Comments on CPTV

- For CPTV give up
  - Lorentz Inv.
  - Locality [or hermiticity...]

e.g.  $H_0 = \int \frac{d^3p}{(2\pi)^3} \sum_s \left[ \sqrt{p^2+m^2} a_p^{s\dagger} a_p^s + \sqrt{p^2+m^2} b_p^{s\dagger} b_p^s \right]$

→ seems Lorentz Inv. & is non-local.

But Greenberg showed that  $\nu$  propagators (off-shell) violate L.I.  
 So all loops or virtual  $\nu$ 's lead to L.V. [not clear how much!]

- Origin of CPTV?
  - Quantum Gravity
  - Extra Dimensions...
- Why large only in Neutrinos?
  - RH  $\nu$ 's "different"
  - may live in bulk

L.V.-CPTV e.g.  $\left\{ \begin{array}{l} \text{Coleman-Glashow} \\ \text{L. to L.} \end{array} \right\} \psi \gamma_\mu \psi b_\mu \dots \left\{ \begin{array}{l} b = \text{constant} \\ \text{4-vector} \end{array} \right\}$

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MINI BOONE @ FNAL.

$\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow E \sim 0.5 - 1.5 \text{ GeV}$   
 ( $\nu_e$  BG  $\sim 10^4$ )

$L \sim 500 \text{ m.}$

$[L/E \sim 1 \text{ m/MeV} \sim \text{as in LSND}]$   
 so probe similar  $\delta m^2$

Started Data Taking in June 2002.

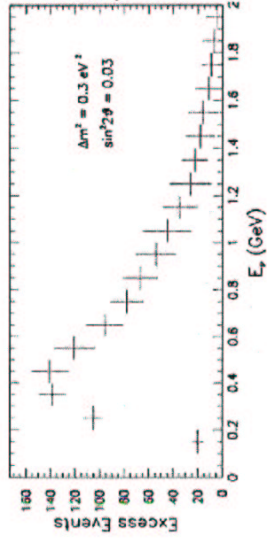
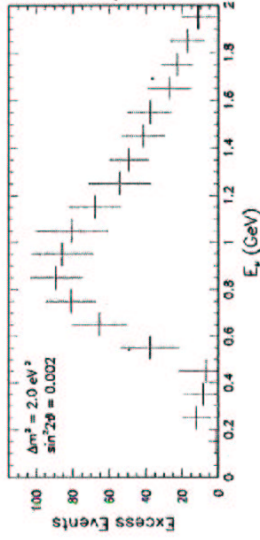
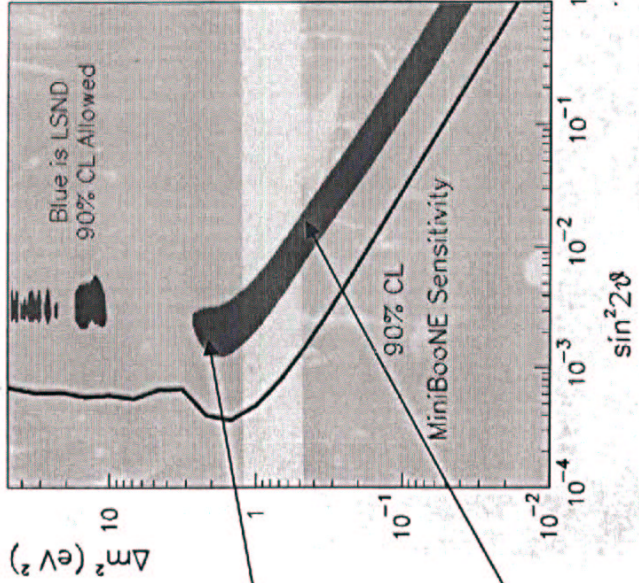
Expected to announce results by June 2004.

Confirm or Rule out Oscillation Interpretation of LSND with a 4th  $\nu$  (or CPTV).

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# MiniBooNE expected sensitivity

With two years of running MiniBooNE should be able to confirm or rule out the entire LSND signal region.



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# Rare $\mu$ -Decay Hypothesis

## Possible Modes:

$\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_i$  ( $i=e, \mu, \tau$ )

Can be related to  $\mu^+ \rightarrow e^+ e^+ \bar{l}_i$  by  $SU(2)$  with unacceptable rates

$i=e \Rightarrow \mu \rightarrow 3e$   $Br < 10^{-12}$

$i=\mu \Rightarrow \mu^+ + e^- \leftrightarrow \bar{\mu} + e^+$   $Br < 10^{-6}$

$i=\tau \Rightarrow \tau^+ \rightarrow \mu^+ + e^- + e^-$   $Br < 10^{-6}$

Even with  $SU(2)$  violation, not possible to account for  $Br(\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_i) \sim 2 \cdot 10^{-3}$

So lepton flavor violation not enuf!  
 [Grossman, Bergmann, Herczeg, S.P.]  
 [Also ruled out by KARMEN  $\Rightarrow Br < 0.8 \cdot 10^{-3}$ ]

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 Flavor Violation not enuf.  
 Need L-violation.

$$(A) \mu^+ \rightarrow e^+ + \bar{\nu}_e + \bar{\nu}_i \quad (i=e, \mu, \tau)$$

[Of course  $\bar{\nu}_i \equiv \nu_{st}$  OK but uninteresting]  
 (models: Babu (S-P))

Safe after  $SU(2)$  rotation.

Possible couplings describing (A)

$$\frac{1}{\Lambda^5} (\bar{\mu}_L e_R) (\nu_{eL}^T \bar{c}^1 \nu_{iL}) \quad \left. \begin{array}{l} \text{Possible to} \\ \text{construct} \end{array} \right\}$$

$$\frac{1}{\Lambda^5} (\bar{\mu}_R e_L) \text{ or } (\nu_{eL}^T \bar{c}^1 \nu_{iL}) \quad \left. \begin{array}{l} \text{Baroque Models} \\ \text{new particles } \sim 400 \\ \text{GeV} \end{array} \right\}$$

These could come from:

$$O_1 \equiv \frac{1}{\Lambda^5} (\bar{\psi}_\mu e_R \Phi) (\psi_e^T \bar{c}^1 \psi_i \Phi \Phi)$$

$$\text{or } O_2 \equiv \frac{1}{\Lambda^5} (\bar{\mu}_R \psi_e \Phi^\dagger) (\psi_e^T \bar{c}^1 \psi_i \Phi \Phi)$$

Safe after  $SU(2)_L$  rotation?

e.g.  $(\bar{\mu}_L e_R) (\nu_{eL}^T \bar{c}^1 \nu_{\mu L})$

$$\xrightarrow{SU(2)} (\bar{\nu}_{\mu L} e_R) (\nu_{eL}^T \bar{c}^1 \tau_L)$$

$\Rightarrow$  gives rise to rare decay

mode (L-violat) of  $\tau$ :

$$\tau^- \rightarrow e^- \bar{\nu}_{\mu L} \nu_e$$

etc

Existence Proof

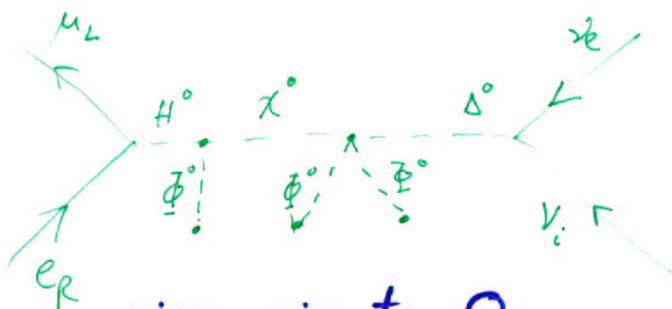
Gauge Models in which operators such as  $O_1$  or  $O_3$  arise

- new scalar fields

$$\Delta (I=1, Y=\frac{1}{2})$$

$$\chi (I=1, Y=0) \quad H (I=\frac{1}{2}, Y=\frac{1}{6})$$

$$\mathcal{L} = h_{\mu e} \bar{\psi}_\mu e_R H + f_{ei} \psi_e^T C^{-1} \psi_i \Delta + M_0 H^\dagger \chi \phi + \lambda' \Delta \chi \phi^\dagger \phi + h.c.$$



gives rise to  $O_1$

$$G_{eff} = \frac{h_{\mu e} f_{ei} \lambda' M_0 \nu^3}{(m_\chi^2 m_H^2 m_{\Delta_0}^2)}$$

$$BR(2 \cdot 10^{-3}) \Rightarrow \text{lowest mass } M_1 < 440 \text{ GeV}$$

Similar Models for  $O_2$ .

Other L-violating Processes.

If  $i=e$  :  $L_e + 3L_\mu$  &  $L_\tau$  unbroken  
No  $\mu \rightarrow 3e$ ,  $\tau \rightarrow 3ee$  etc

$i=\mu$  :  $L_\mu, L_\tau$  unbroken

$i=\tau$  :  $L_\mu + L_\tau$  &  $L_e + 2L_\mu$  unbroken.

- No other unwanted L-violating Decays
  - No large Majorana  $\nu$ -masses induced (Protected by these symmetries)
- [New scalars have no vevs]

[ $\nu$  mass will have to be generated by the "conventional" see-saw mechanism].

- $\phi_H$  cannot have vev (fine tuning).

Other Effects

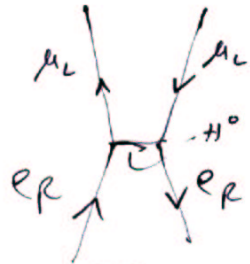
- Radiative Corrections to  $\mu$  Decay shifted by 0.1 %.

$$G_{T\mu} = \frac{\pi\alpha}{\sqrt{2} m_W^2 (1 - m_W^2/m_Z^2) (1 - \Delta R)}$$

$$\Delta R = \Delta R_{SM} + 0.001$$

Current uncertainty in  $\Delta R \approx \pm 0.002$   
(from  $\pm 5$  GeV in  $m_t$  alone).

- $e^+e^- \rightarrow \mu^+\mu^-$  gets contribution from

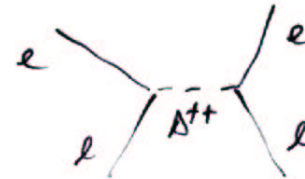


$$G_{eff} = |h_{\mu e}|^2 / 2m_{H^0}^2$$

$$m_{H^0} / |h_{\mu e}| \gtrsim 380 \text{ GeV}$$

- $e^+e^- \rightarrow l_i \bar{l}_i$

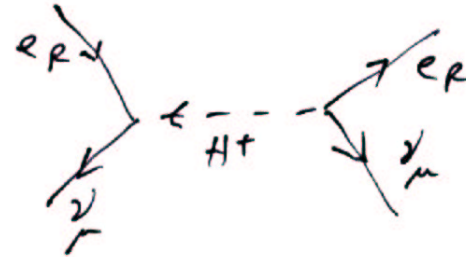
via



$$G_{eff} = f_{ei}^2 / 2m_{\Delta^{++}}^2$$

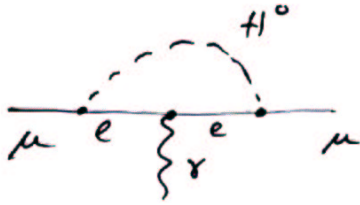
$$m_{\Delta^{++}} / |f_{ei}| \gtrsim \begin{cases} 760 \text{ GeV} & i=e \\ 1460 \text{ GeV} & i=\mu \\ 780 \text{ GeV} & i=\tau \end{cases}$$

- $e^+e^- \rightarrow \nu \bar{\nu}$



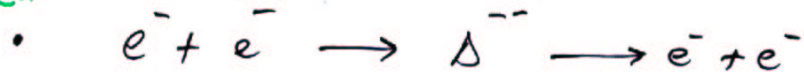
$$m_{H^+} / |h_{\nu e}| \gtrsim 375 \text{ GeV}$$

•  $(g-2)_\mu$



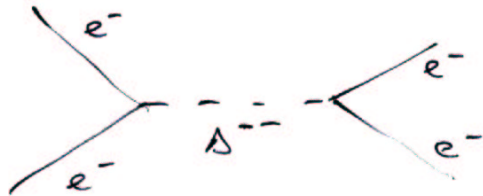
$$\Delta a_\mu = \frac{h_{\mu e}^2}{24\pi^2} \frac{m_\mu^2}{m_{H^0}^2} \sim 47 \cdot 10^{-10} \left| h_{\mu e} \left( \frac{100 \text{ GeV}}{m_{H^0}} \right) \right|^2$$

Can be within the sensitivity of current  $g-2$  experiment  
Current 'Discrepancy'  $\sim (30-36) \cdot 10^{-10}$ . (Hagiwara et al.)



Resonant Production of  $\Delta^{--}$

at  $e^- e^-$  Collider.



### Summary

- L-violating Mode  $\mu^+ \rightarrow e^+ \bar{\nu}_e + \bar{\nu}_\mu$   
can account for LSND data  
(consistently with KARMEN) for  $B.R. \sim 1.5 \cdot 10^{-3}$

• Tests:

- No L/E dependence of Rate
- NULL Result at Mini-Boone
- Need to look at  $\mu$ -decays & not  $\pi$ -decays to test LSND  
e.g. {ORLAND  $\leftarrow$  SNS}
- $\nu$ -Factories.

- Await results from TWIST to check  $\rho = 0.7485 \neq \frac{1}{0.75}$

- Expect new scalar fields with some ( $H^0$ ) with masses  $< 450 \text{ GeV}$



### $\mu^-$ Decay Distribution

$$\frac{d^2\Gamma^\pm}{dx d(\cos\theta_e)} = \frac{m_\mu}{4\pi^3} W_{e\mu}^4 G_F^2 \sqrt{x^2 - x_0^2} \left[ x(1-x) + \rho \left\{ \frac{2}{9} (4x^2 - 3x - x_0^2) \right\} + \eta x_0(1-x) \pm P_\mu \cos\theta_e \left\{ \xi \left( \frac{1}{3} \sqrt{x^2 - x_0^2} [1-x + \frac{2}{3} \delta [4x-3 + \sqrt{1-x_0^2}]] \right) \right\} \right]$$

Where  $x = E_e/m_\mu$   $x_0 = m_e/W_{e\mu} \{x_0 \leq x \leq 1\}$   
 $W_{e\mu} = (m_\mu^2 + m_e^2)/2m_\mu$

S.M. (V-A)  $\Rightarrow \rho = 3/4, \eta = 0, \xi = 1, \delta = 3/4$

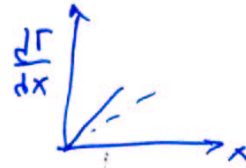
For  $\nu_1 \Rightarrow \rho = 0, \eta = 0, \xi = -3/4, \delta = 0$

For  $\nu_2 \Rightarrow \rho = 0, \eta = 0, \xi = +3/4, \delta = 0$

Shifts in  $\rho, \eta, \xi, \delta$

$\rho = 3/4 - 3/4 \epsilon, \eta = 0, \xi = 1 - \frac{\epsilon}{2}, \delta = 3/4 - 3/4 \epsilon$

Michel parameter	SM	This model	Current Value	TWIST Sensitivity
$\rho$	3/4	3/4 - 3/4 $\epsilon$	0.7518 $\pm$ 0.0026	$\pm$ 0.0001
$\eta$	0	0	-0.007 $\pm$ 0.013	$\pm$ <del>0.003</del> 0.003
$\xi$	3/4	3/4 - 3/4 $\epsilon$	0.7486 $\pm$ 0.0038	$\pm$ 0.0014
$\delta$	1	1 - $\frac{\epsilon}{2}$	1.0027 $\pm$ 0.0079	$\pm$ 0.00013



TWIST to sensitivity to couplings

Coupling	Value in this model	TWIST limit
$g_{LR}^V$	<del>0.08</del> 0.08	0.018
$g_{RL}^V$	<del>0.08</del> 0.08	0.012

TWIST @ TRIUMF

## TWIST (TRIUMPH)

sensitivity for  $\rho \sim 10^{-9}$

• Radiative Corrections?

• Order  $\alpha$  (Kinoshita, Sirlin, 1959)  
Berman

$\sim 4.5\%$

taken into account

• Order  $\alpha^2 \ln m_\nu/m_e$ ,  $\alpha^2 (\ln m_\nu/m_e)^2$   
calculated recently  
Arbuzov, Melnikov  
et al. (2002)

$\delta\rho \sim \text{few} \cdot 10^{-9}$

• order  $\alpha^2$  yet to be calculated  
 $\Rightarrow$  theoretical error  $\sim 0(2 \cdot 10^{-9})$

This is adequate to test  
an effect at a level of  $10^{-3}$ .

## Predictions of Rare Decay

Explanation of LSND

- No L/E Dependence at LSND or similar expts
- MINI-BOONE will NOT see any effect since they do NOT look at  $\mu$  Decays (only  $\pi$  decays)
- Effective  $\rho$  in  $\mu$ -decay will deviate from  $3/4$  to 0.7485 Currently  $0.75 \pm 0.0026$   
Future TWIST@TRIUMF sensitivity  $\sim 10^{-4}$
- Expect new scalar particles in mass range below  $\Lambda < 400 \text{ GeV}$   
 $\rightarrow$  see below.

$\Delta L = 2$   $\mu$ -decay explanation  
 for LSND already  
 living dangerously!!  
 $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\alpha$ .

• KARMEN Bound:  
 (for  $p=0$ ) B.R.  $< 1.7 \cdot 10^{-3}$  @ 90%  
 hep-ex/0302017 c.l.

• LSND Requirement: (W. Louis, p.c.)  
 (for  $p=0$ ) B.R.  $\cong (3.4 \pm 0.9) 10^{-3}$

Small Window  
 All explanations of LSND  
 live dangerously.