

# Top Partners and Fermion Masses

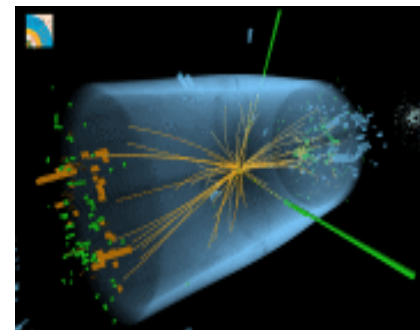
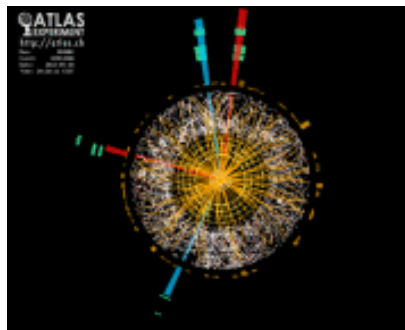
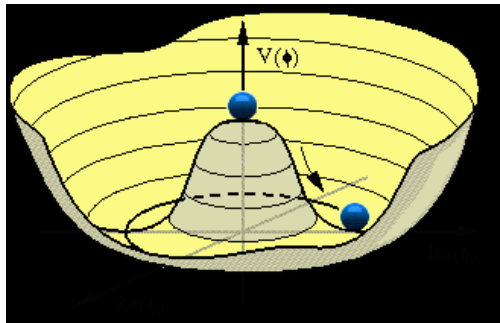
S. Dawson, BNL

July 9, 2013

S. Dawson, E Furlan, hep-ph/1205.4733

S. Dawson, E. Furlan, I. Lewis, hep-ph/1210.6663

S. Dawson, E. Furlan, coming soon



# The Higgs and Fermion Masses

- SM Higgs couples to fermion mass
  - Largest coupling is to heaviest fermion

$$L = -\frac{m_f}{v} \bar{f}fH = -\frac{m_f}{v} (\bar{f}_L f_R + \bar{f}_R f_L)H$$

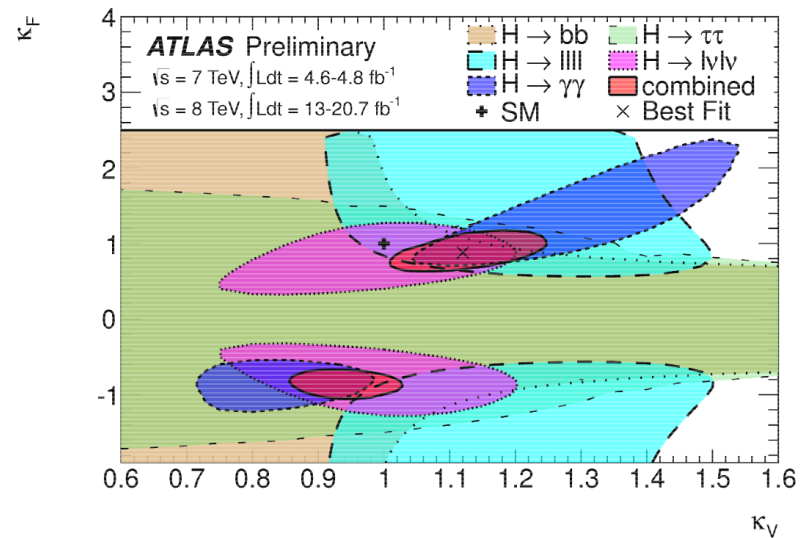
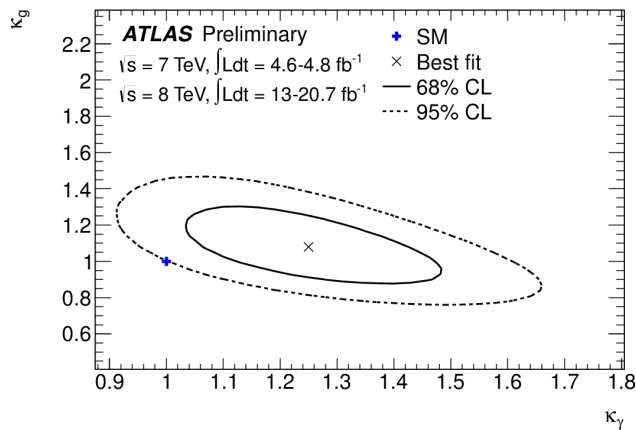
- Higgs couples to gauge boson masses
- Only free parameter is Higgs mass

*Are fermion masses from SM Yukawa interactions?*

$$L \sim \kappa_t \frac{m_t}{v} \bar{t}tH + \kappa_g \frac{\alpha_s}{12\pi} \frac{H}{v} G_{\mu\nu}^A G^{A,\mu\nu}$$

# LHC Measures $\sigma \cdot \text{BR}$

- Global fits extract couplings\*
- ATLAS now



- CMS future

L (fb <sup>-1</sup> )	$\kappa_\gamma$	$\kappa_V$	$\kappa_g$	$\kappa_b$	$\kappa_t$	$\kappa_\tau$
300	[5, 7]	[4, 5]	[6, 8]	[10, 13]	[14, 15]	[6, 8]
3000	[2, 5]	[2, 3]	[3, 5]	[4, 7]	[7, 10]	[2, 5]

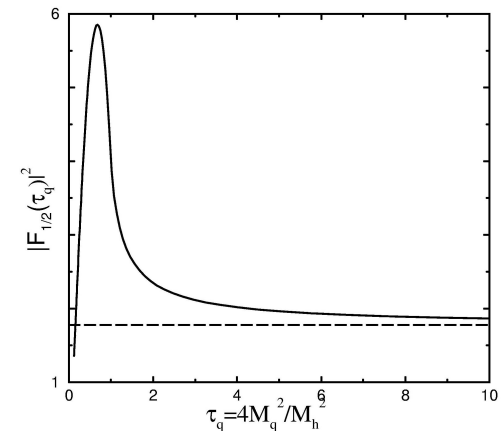
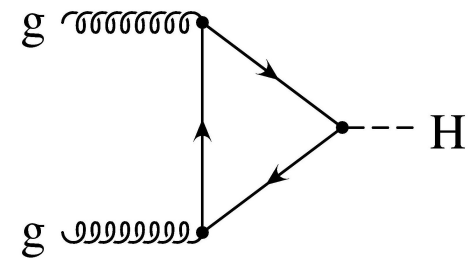
\* Assumptions about invisible decays required

# Gluon Fusion

- Sensitive to colored particles in loop
  - Heavy quarks:  $F_{1/2} \rightarrow -4/3$
  - Assumes SM Yukawa coupling

$$\hat{\sigma}_{gg \rightarrow h}(\hat{s}) = \frac{\alpha_s(\mu_R)^2}{1024\pi v^2} \left| \sum_q F_{1/2}(\tau_q) \right|^2 \delta\left(1 - \frac{M_h^2}{\hat{s}}\right)$$

Chiral 4<sup>th</sup> generation excluded



What can we learn about fermion masses from Higgs production and decay?

# Theory Precision

- What precision are we aiming for in order to claim discovery of new physics?
  - Parametric uncertainties (mostly  $m_b$  and  $\alpha_s$ )
  - Theory uncertainties (scale, missing higher order EW)

$M_H = 126 \text{ GeV}$	BR uncertainties		
Decay	TU	PU	Total
	[%]	[%]	[%]
$H \rightarrow \gamma\gamma$	$\pm 2.7$	$\pm 2.2$	$\pm 4.9$
$H \rightarrow b\bar{b}$	$\pm 1.5$	$\pm 1.9$	$\pm 3.3$
$H \rightarrow \tau\tau$	$\pm 3.5$	$\pm 2.1$	$\pm 5.6$
$H \rightarrow WW$	$\pm 2.0$	$\pm 2.2$	$\pm 4.1$
$H \rightarrow ZZ$	$\pm 2.0$	$\pm 2.2$	$\pm 4.2$

[Higgs cross section working group]

## Top Partners

- Many possibilities
- Simplest:
  - Fermion with charge 2/3,  $T_L^2, T_R^2$
  - $T_L^2, T_R^2$  have identical  $SU(2)_L$  couplings (vector-like)
- Mixes with SM fermions:  $\psi_L = (T_L^1, B_L^1), T_L^1, B_R^1$
- Motivated by **Little Higgs** and **composite Higgs** models which have vector-like top partner

## Top Partners can have Dirac Masses

- Physical t's are combinations of  $\mathcal{T}_L^1, \mathcal{T}_L^2$

$$\chi_L = \begin{pmatrix} t_L \\ T_L \end{pmatrix} \equiv U_L \begin{pmatrix} \mathcal{T}_L^1 \\ \mathcal{T}_L^2 \end{pmatrix}$$

- Most general mass terms:

$$-\mathcal{L}_{M,SM} = \lambda_2 \bar{\psi}_L^1 \tilde{H} \mathcal{T}_R^1 + h.c.$$

$$-\mathcal{L}_{M,1} = \lambda_3 \bar{\psi}_L^1 \tilde{H} \mathcal{T}_R^2 + \lambda_4 \bar{\mathcal{T}}_L^2 \mathcal{T}_R^1 + \lambda_5 \bar{\mathcal{T}}_L^2 \mathcal{T}_R^2 + h.c.$$

–  $\lambda_4$  can be rotated away by redefinition of  $\mathcal{T}_R^2$

– 4 physical parameters,  $m_b, m_t, M_T, \theta_L$

- Higgs, neutral current, charged couplings changed

## Decoupling of Heavy Top Partners

- Remember SM top doesn't decouple

$$M^t = \begin{pmatrix} \frac{\lambda_2 v}{\sqrt{2}} & \frac{\lambda_3 v}{\sqrt{2}} \\ \lambda_4 & \lambda_5 \end{pmatrix}$$

- Small mixing:  
$$\lambda_2 \sim \frac{\sqrt{2}m_t}{v} \left[ 1 + \frac{s_L^2}{2} \left( \frac{M_T^2}{m_t^2} - 1 \right) \right]$$
$$\lambda_5 \sim M_T \left[ 1 - \frac{s_L^2}{2} \left( \frac{M_T^2 - m_t^2}{M_T^2} \right) \right]$$

- Decoupling of T requires:

$$s_L \sim \frac{v}{M_T}$$

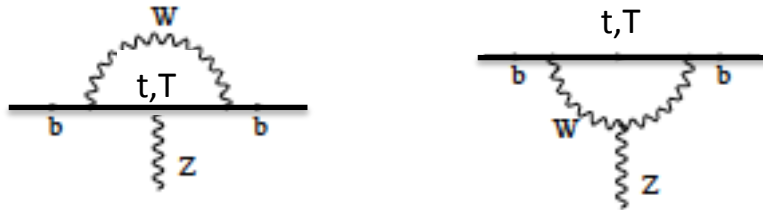


## Couplings to W/Z/H Modified

- t-T mixing modifies  $Z \rightarrow b\bar{b}$  at one loop

$$L_W \sim \frac{g}{\sqrt{2}} W_\mu^+ \left\{ c_L \bar{t}_L \gamma^\mu b_L + s_L \bar{T}_L \gamma^\mu b_L \right\}$$

$$\delta L \sim \frac{g}{c_W} Z_\mu \left\{ \bar{t}_L \gamma^\mu \left( -\frac{s_L^2}{2} \right) t_L + \bar{T}_L \gamma^\mu \left( -\frac{c_L^2}{2} \right) T_L + \bar{t}_L \gamma^\mu \left( \frac{s_L c_L}{2} \right) T_L + hc \right\}$$



$$\delta g_L^b \sim \delta g_L^{b,SM} \left\{ 1 + s_L^2 \left[ -(1 + c_L^2) + s_L^2 \frac{M_T^2}{M_t^2} + 2c_L^2 \frac{M_T^2}{M_T^2 - m_t^2} \log \left( \frac{M_T^2}{m_t^2} \right) \right] \right\}$$

- Vector-like top partners only decouple when  $s_L \sim v/M_T$*

## Limits from $Z \rightarrow b\bar{b}$

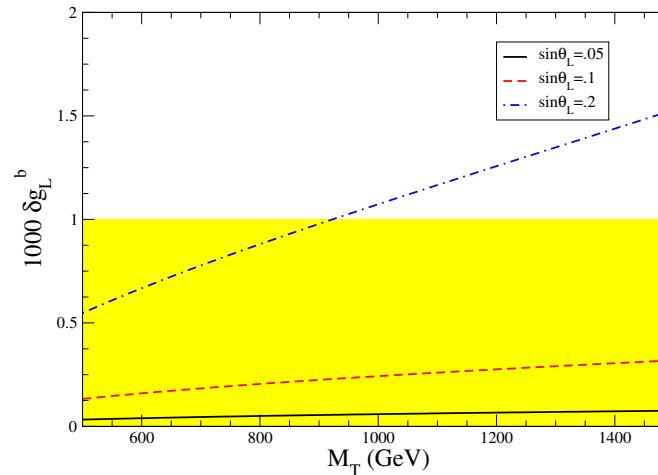
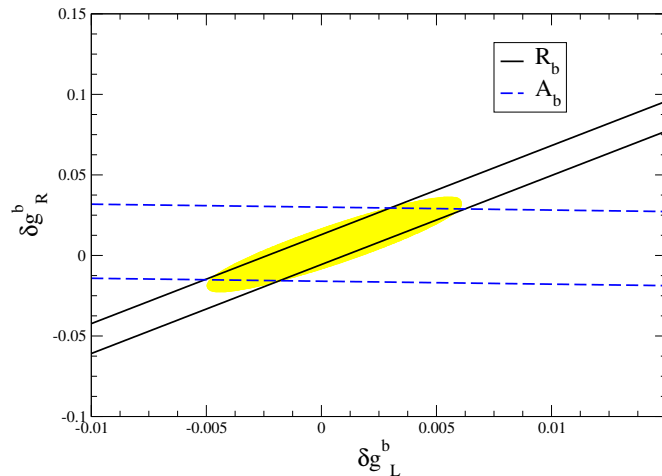
- Top partner (& top) couplings to Z change  $Z \rightarrow b\bar{b}$

$$R_b \sim R_b^{SM} \left\{ 1 - 3.6\delta g_L^b + .65\delta g_R^b \right\}$$

$$A_b \sim A_b^{SM} \left\{ 1 - .32\delta g_L^b - 1.7\delta g_R^b \right\}$$

- Top partner increases  $\delta g_L^b$  and reduces  $R_b$

95% Confidence Level Limits



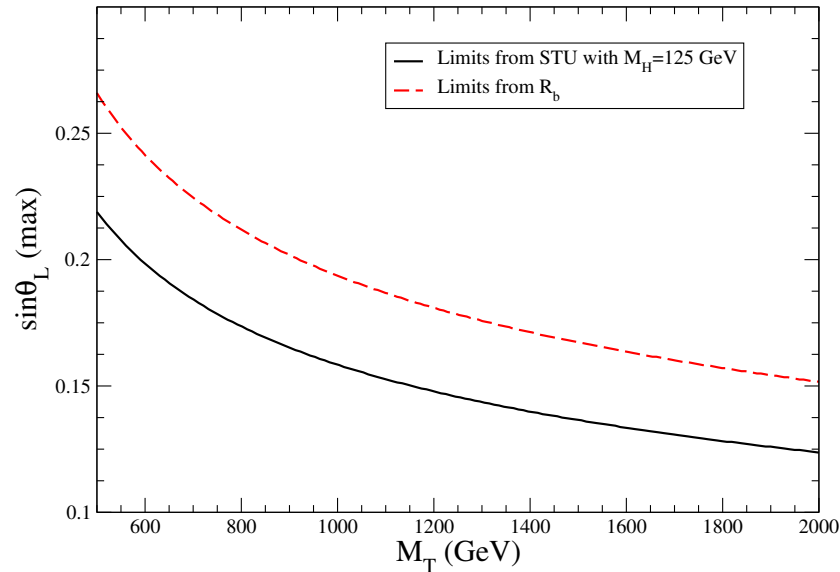
[Dawson, Furlan; Similar results in Aguilar-Saavedra, 1306.0572]

# Top Partner Mixing Limited by Precision EW

$$\Delta T \sim T_{SM} s_L^2 \left[ -(1 + c_L^2) + s_L^2 \frac{M_T^2}{m_t^2} + 2c_L^2 \log \left( \frac{M_T^2}{m_t^2} \right) \right]$$

$$\Delta S \sim -\frac{s_L^2}{6\pi} \left[ 5c_L^2 + (1 - 3c_L^2) \log \left( \frac{M_T^2}{m_t^2} \right) \right]$$

95% CL Upper Limits



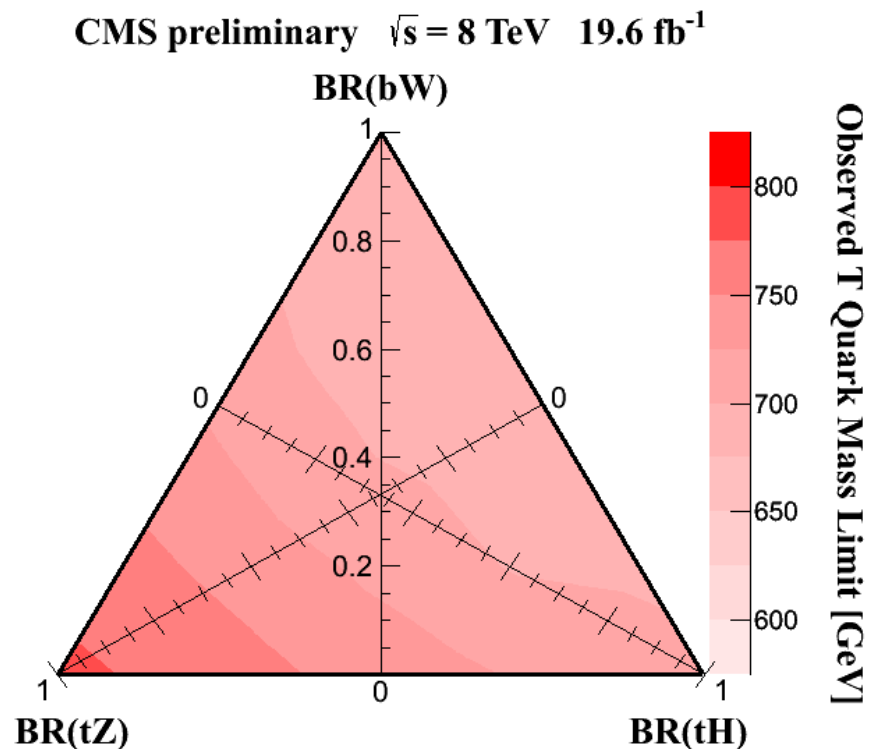
# Top Partner limits

- LHC limits model dependent, but  $M_T > 600-700 \text{ GeV}$ 
  - $T \rightarrow bW, T \rightarrow tH, T \rightarrow tZ$
  - $gg \rightarrow T\bar{T}$  model independent

- **Unitarity**

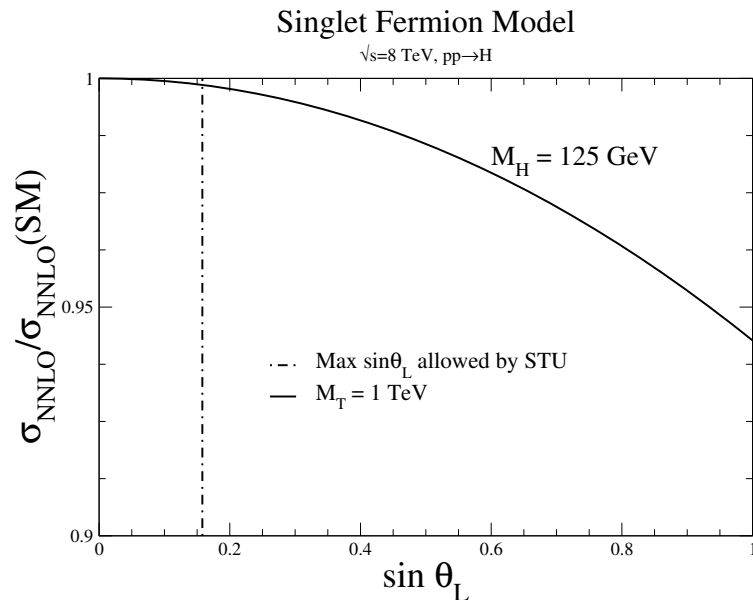
$$M_T < \frac{550 \text{ GeV}}{s_L^2}$$

CMS-PAS-B2G-12-015



# Top Partners and gluon fusion

- Top partner:  $\sigma \sim \sigma_{SM} \left\{ 1 - \frac{7M_H^2}{60m_t^2} s_L^2 \left( 1 - \frac{m_t^2}{M_T^2} \right) \right\}$



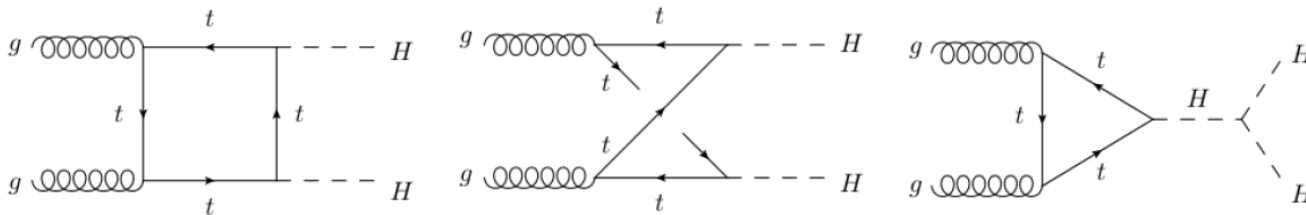
Large effects not possible  
 due to precision EW

$$L_H \sim \frac{m_t}{v} c_L^2 t\bar{t}H + \frac{M_T}{v} s_L^2 T\bar{T}H$$



Leading piece in  $M_H^2/M_t^2$  expansion  
 independent of top partner mixing

## Two Higgs Production and Top Partners

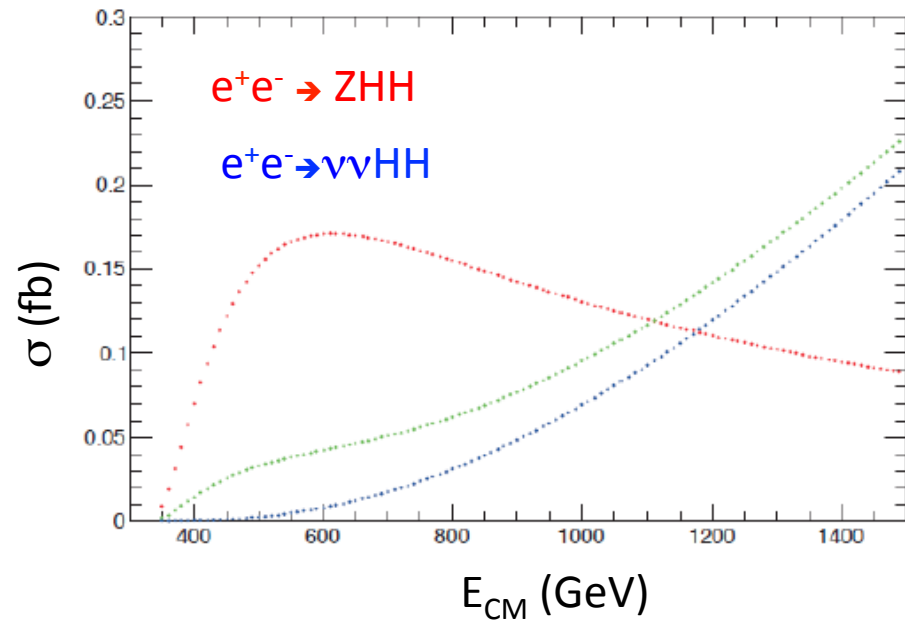
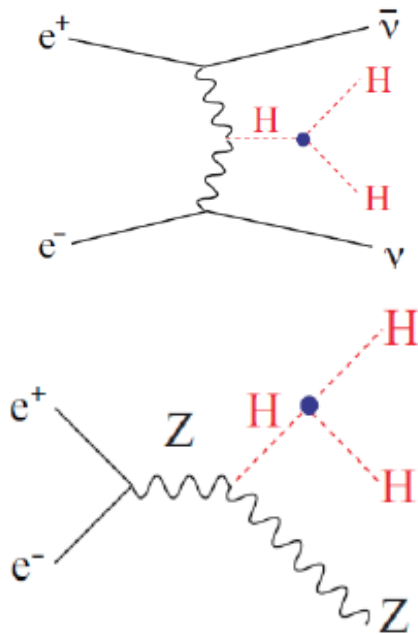


- Sensitive to HHH coupling and new particles in loops
  - Cancellation between box and triangle reduces sensitivity
- Small rate: 3 fb at 8 TeV, 15 fb at 14 TeV
  - $b\bar{b}\gamma\gamma$  gives  $3\sigma$  with  $3 \text{ ab}^{-1}$  (270 events with  $3 \text{ ab}^{-1}$ )
  - 30% measurement of  $\lambda_{\text{HHH}}$

[ATLAS/CMS HL-LHC study]

## ILC doesn't do that much better with HHH

- Low rates: 400 events at 500 GeV, 1000 events at 3 TeV
- Large backgrounds



$$\frac{\Delta\lambda_{HHH}}{\lambda_{HHH}} \sim 25\%(ILC), 15\%(CLIC)$$

## Two Higgs Production at LHC

- Cross section has spin-0 and spin-2 contributions

$$\frac{d\sigma(gg \rightarrow HH)}{dt} = \frac{\alpha_s^2}{32768\pi^3 v^4} \left( |F_0|^2 + |F_2|^2 \right)$$

- $M_t^2 \gg s$  (low energy theorem)

$$F_0 \rightarrow -\frac{4}{3} + \frac{4M_H^2}{s - M_H^2} (\delta\lambda_{HHH})$$

$$F_2 \rightarrow 0$$

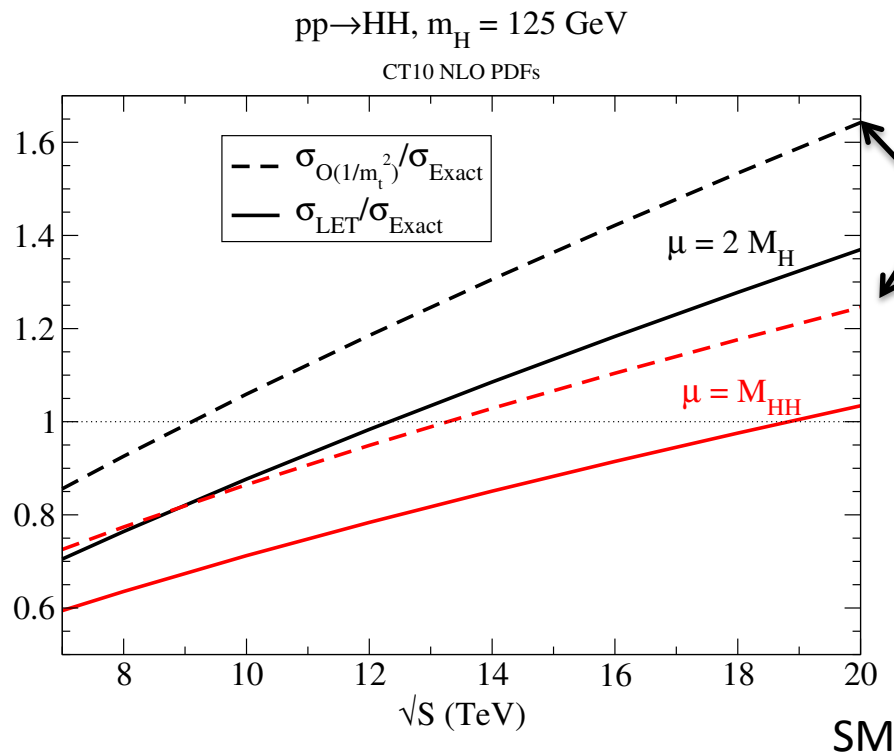
↑  
HHH coupling (1 for SM)

- Singlet top partner model has  $s_L$  and  $c_L$  in appropriate places
- Also has new diagrams with tTH vertices



## Low Energy Expansion ( $M_H \ll M_t$ )

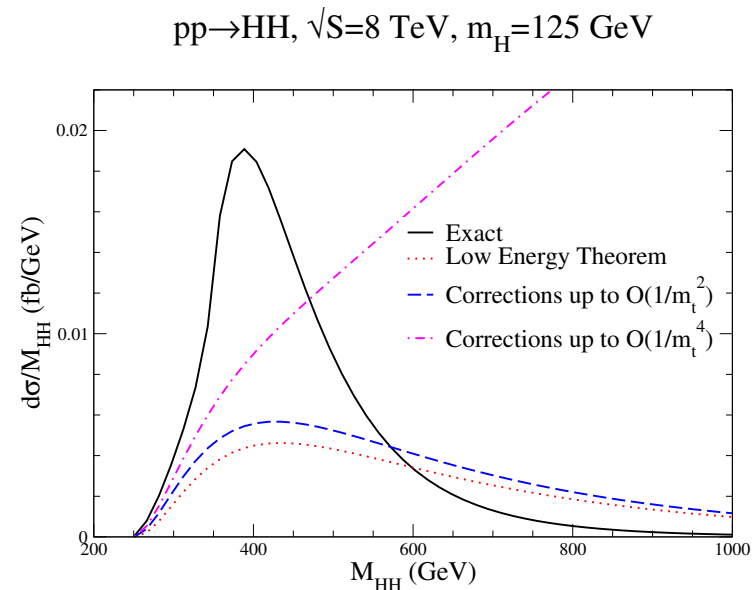
- Works spectacularly well for  $gg \rightarrow H$ 
  - Not so well for  $gg \rightarrow HH$  (more scales in problem)
  - Same conclusion for  $gg \rightarrow gH$  [Harlander et al., 1206.0157]



Add in first term of  $s/M_t^2$  expansion

# Low Energy Expansions and Distributions

Low energy expansion doesn't work for distributions



Could show similar plots for top partner singlet model, but they aren't interesting!! They look like SM

## Mirror Fermions

- Can have very different effects on single and double Higgs production

$$\psi_L^1 = \begin{pmatrix} \mathcal{T}_L^1 \\ \mathcal{B}_L^1 \end{pmatrix}, \quad \mathcal{T}_R^1, \mathcal{B}_R^1; \quad \psi_R^2 = \begin{pmatrix} \mathcal{T}_R^2 \\ \mathcal{B}_R^2 \end{pmatrix}, \quad \mathcal{T}_L^2, \mathcal{B}_L^2$$

$$-\mathcal{L} = \lambda_A \bar{\psi}_L^1 \Phi \mathcal{B}_R^1 + \lambda_B \bar{\psi}_L^1 \tilde{\Phi} \mathcal{T}_R^1 + \lambda_C \bar{\psi}_R^2 \Phi \mathcal{B}_L^2 + \lambda_D \bar{\psi}_R^2 \tilde{\Phi} \mathcal{T}_L^2 \\ + \lambda_E \bar{\psi}_L^1 \psi_R^2 + \lambda_F \bar{\mathcal{T}}_R^1 \mathcal{T}_L^2 + \lambda_G \bar{\mathcal{B}}_R^1 \mathcal{B}_L^2 + \text{h.c.}$$

- 7 parameters in Lagrangian. Assume  $M_{T1} = M_{B1} = M$ ,  
 $M_{T2} = M_{B2} = M(1 + \delta)$ 
  - Leading terms in H, HH production independent of M
  - $\Delta$  : Deviation from SM  $gg \rightarrow H$
  - $\theta_-^t, \theta_+^b$

Assume for simplicity no mixing with SM fermions

## Relationships among Parameters

- In the limit of small mixing

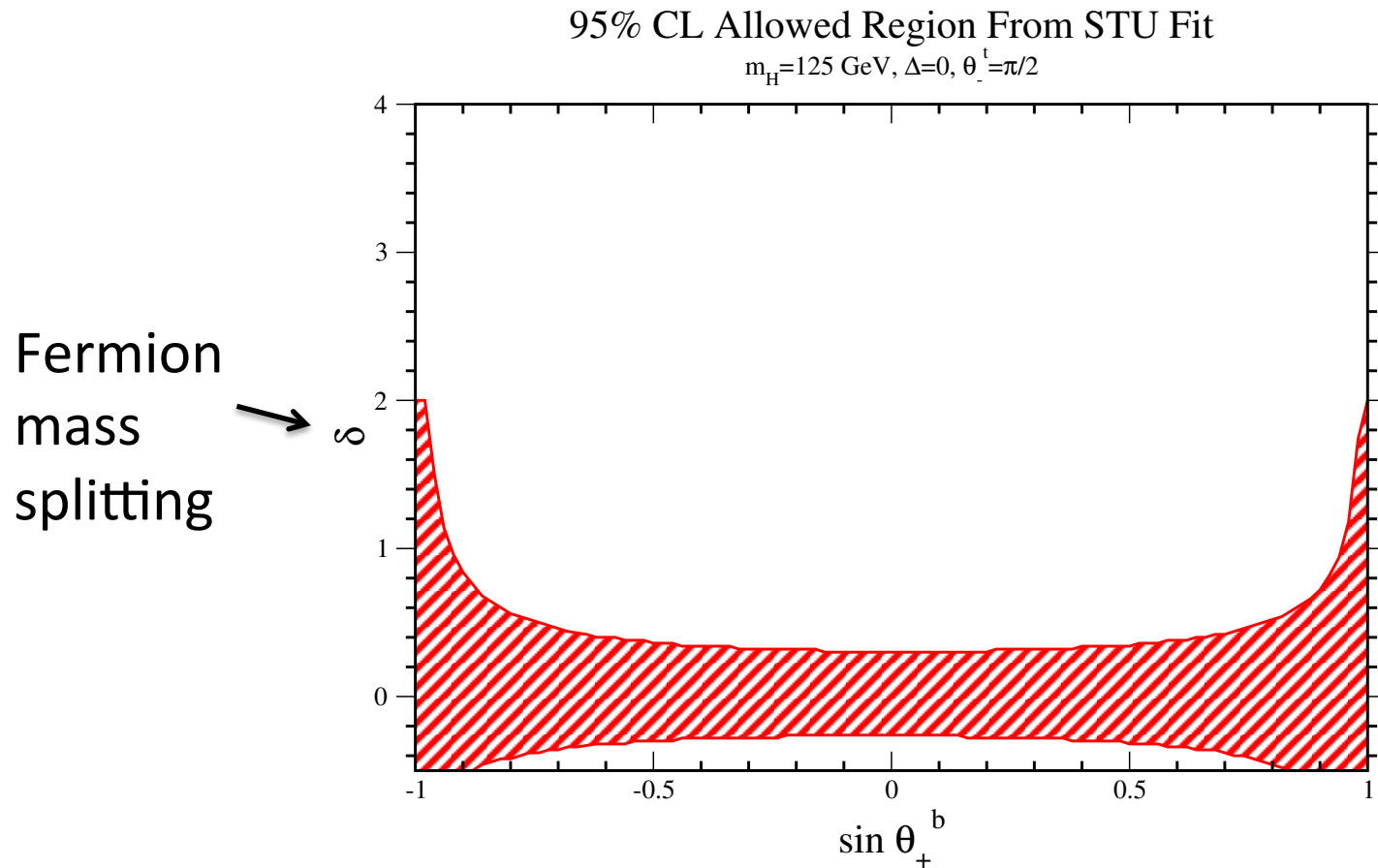
$$(s_L^t)^2 \sim \frac{m_t^2}{M_T^2} (s_R^t)^2, \quad (s_L^b)^2 \sim \frac{m_b^2}{M_B^2} (s_R^b)^2$$

$$(s_R^t)^2 \sim (s_R^b)^2 + \mathcal{O}(\delta)$$

- W/Z/H couplings modified by  $s_L^t, s_L^b$
- Limits from STU require (for  $M_T=1$  TeV),  $\delta < 2$

## Interesting Regions of Parameter Space

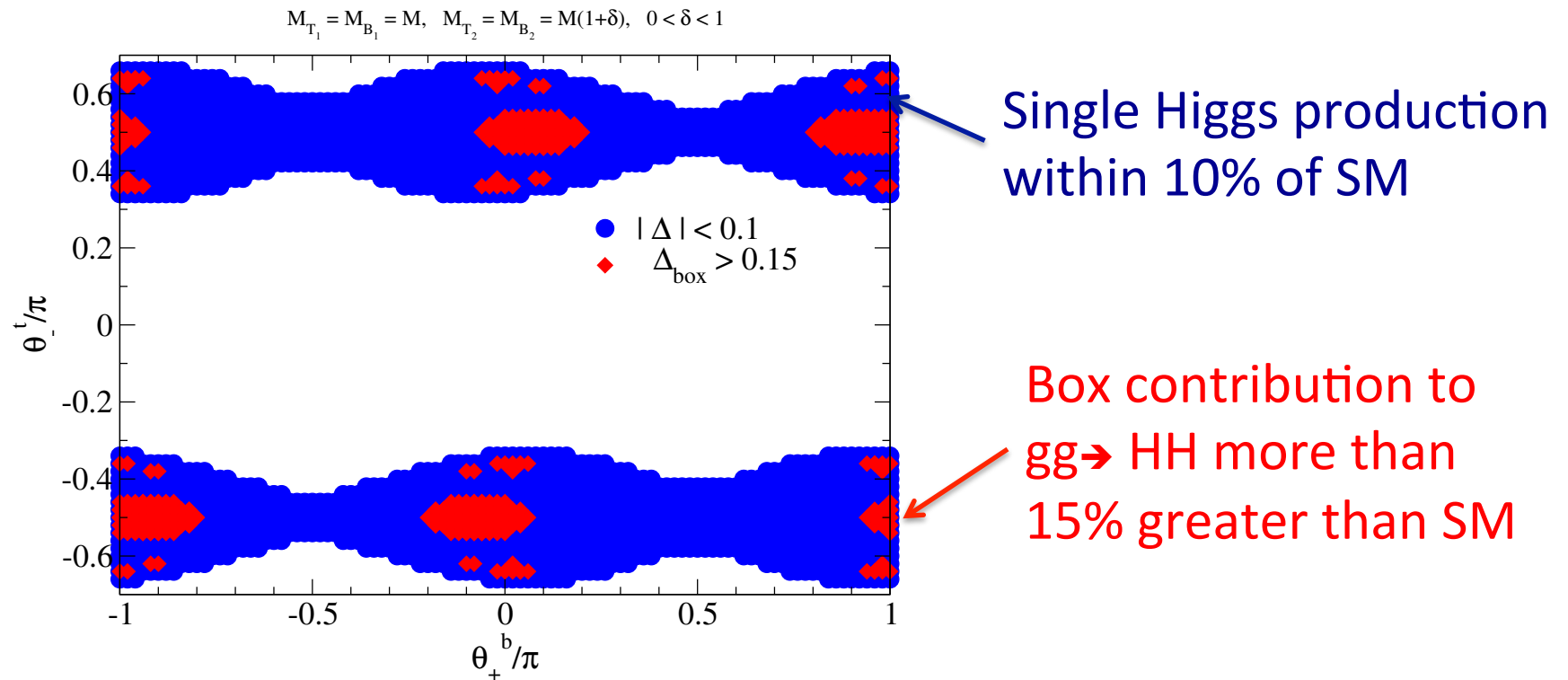
- All parameters in this plot give SM  $gg \rightarrow H$  rate



Dawson, Furlan, Lewis; Early work by He, Polonsky, and Su, hep-ph/0102144

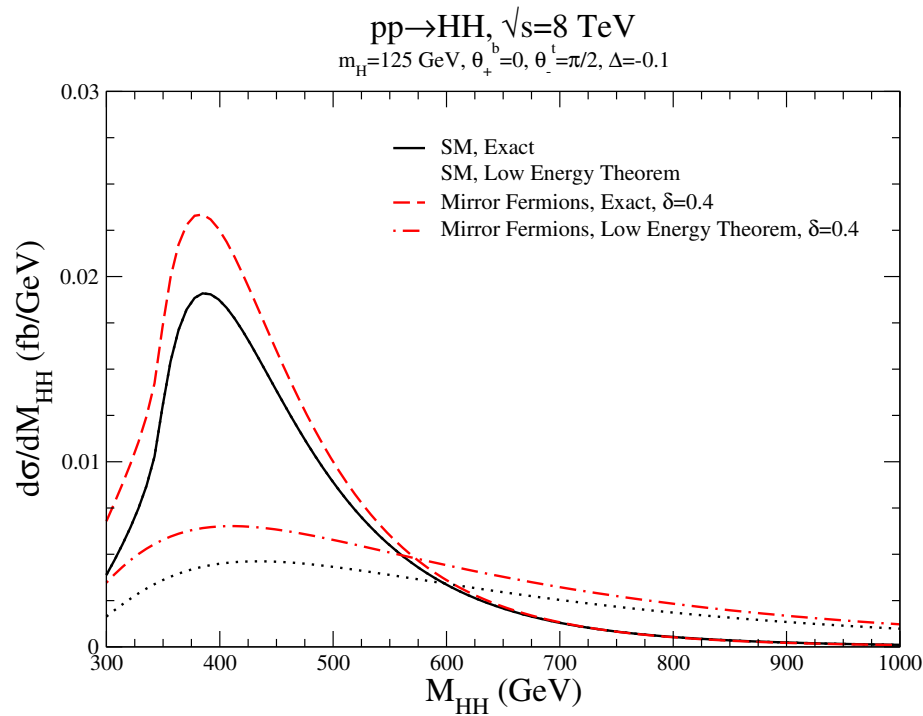
# Significant Deviations Possible in HH Production

- Parameter scan:



# Double Higgs Rate

- $gg \rightarrow HH$  rate increased by 17% relative to SM
- $gg \rightarrow H$  rate assumed to be 90% of SM

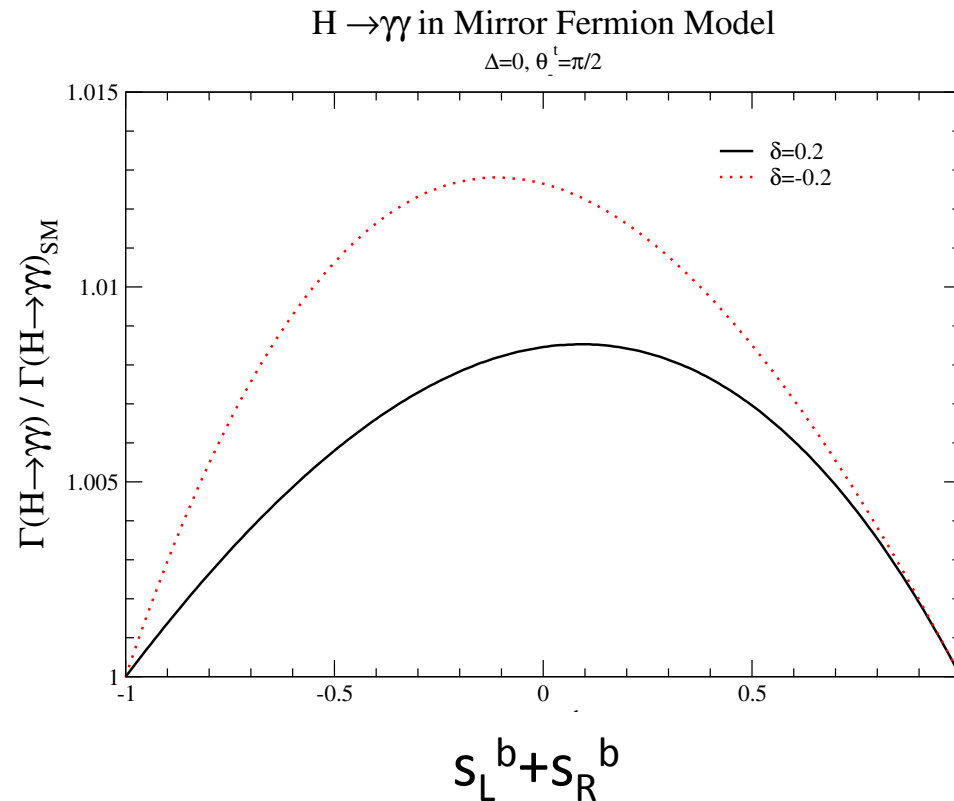


Optimal choice  
of parameters

# $H \rightarrow \gamma\gamma$

- Top singlet model,  $H \rightarrow \gamma\gamma$  is within .5% of SM rate
- Mirror Fermion model can have  $\sim 1\%$  deviations

(Require  $gg \rightarrow H$  rate to be SM; can have  $\sim 10\%$  differences without this requirement)





# Effective Higgs Gluon Interactions

- If fermion masses arise from electroweak symmetry breaking, they have the form

$$C_2 O_{LE} = \frac{\alpha_s}{24\pi} C_2 G_{\mu\nu}^A G^{A,\mu\nu} \log\left(\frac{H^+ H}{v^2}\right) = \frac{\alpha_s}{12\pi} C_2 G_{\mu\nu}^A G^{A,\mu\nu} \left(\frac{H}{v} - \frac{H^2}{2v^2}\right)$$

- A general expansion could generate

$$\text{SM: } C_1=0, C_2=1$$

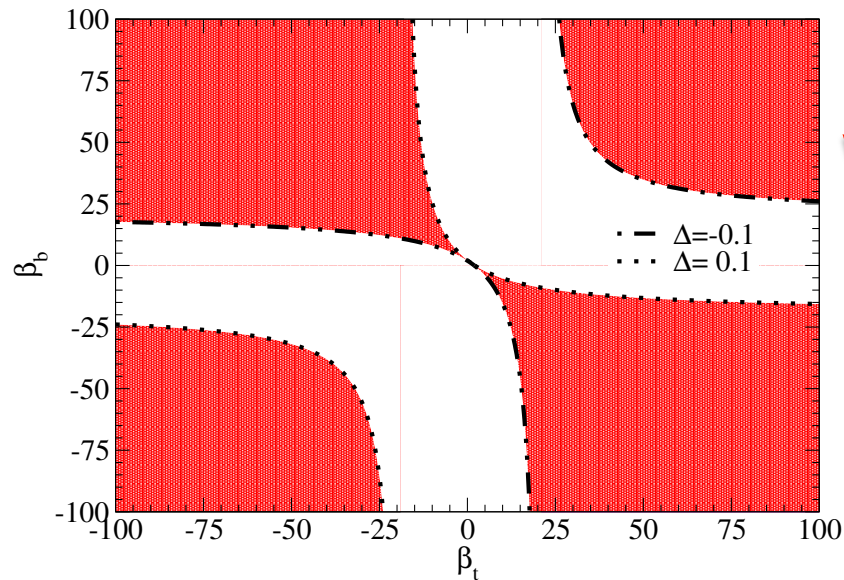
$$C_1 O_{eff} = \frac{\alpha_s}{12\pi} C_1 G_{\mu\nu}^A G^{A,\mu\nu} \left|\frac{H^+ H}{v^2}\right|^2 = \frac{\alpha_s}{12\pi} C_1 G_{\mu\nu}^A G^{A,\mu\nu} \left(\frac{H}{v} + \frac{H^2}{2v^2}\right)$$

- Measuring single and double Higgs production is window into source of EWSB

$$\begin{aligned} C_H &= C_1 + C_2 \rightarrow 1 + \Delta \\ C_{HH} &= C_1 - C_2 \rightarrow 2C_1 - (1 + \Delta) \end{aligned}$$

## Large effects in HH?

- Mirror model:  $C_1^i = \frac{-2\beta_i}{(1-\beta_i)^2}$ ,  $C_2^i = 1 + \frac{2}{(1-\beta_i)^2}$
- $\beta_i \rightarrow 0$ ,  $C_i \rightarrow \text{SM}$  ( $\beta$  is function of Yukawa couplings)
  - Happens when Dirac mass term for partners vanish



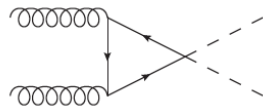
$gg \rightarrow H$  within  
10% of SM

# Compare Double Higgs Production

- Effective Lagrangian with mirror fermions and  $\delta=0$ :

$$L_{eff} = \frac{\alpha_s}{12\pi} G_{\mu\nu}^A G^{A,\mu\nu} \left[ (1 + 4 \cos^2 \theta_-^b) \frac{H}{v} - (1 - 4 \cos^2 \theta_-^b + 8 \cos^4 \theta_-^b) \frac{H^2}{2v^2} \right]$$

- Composite Models (or Little Higgs)
  - Non-renormalizable  $t\bar{t}HH$  interaction can give enhancement of factors of 2
  - Partially due to cancellation in SM between diagrams



[Gillioz et al, hep-ph/1206.7120]

## Conclusions

- Vector like top partners are natural extensions of SM
- Parameters allowed by EW precision observables give  $gg \rightarrow H$  rate close to SM
- *STU + Higgs production the new precision EW parameters*
- $gg \rightarrow HH$  can be enhanced by  $\sim 17\%$ 
  - Small effects in  $H \rightarrow \gamma\gamma$
  - Higgs branching ratio deviations much smaller than theory uncertainties
- Aside: Low energy limit not valid for  $2 \rightarrow 2$  processes
- Look for top partners directly in single T production\*
  - $\sigma < 20 \text{ fb}$  at 8 TeV for  $M_T \sim 1 \text{ TeV}$

[\* Aguilar-Saavedra, hep-ph/1306.0572]