

Laser intensity at nonlinear QED: A realizable scheme

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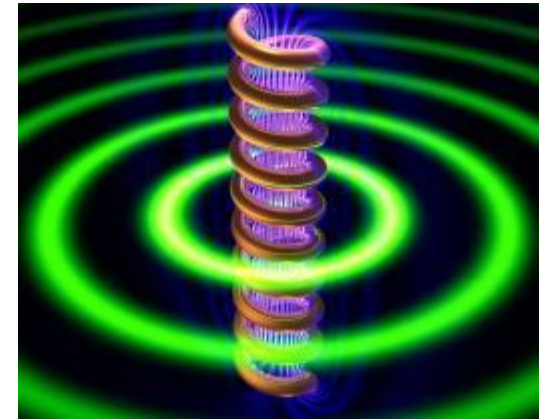
Motivation & Vision

- How to produce laser field with intensity that makes quantum vacuum nonlinear? Nonlinear QED: A New Science

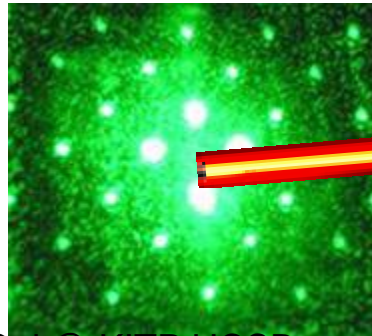


- Gravitational force of light

K S Ng and C H Raymond Ooi, (2013) “Gravitational Force of Bessel Light Beam”, Laser Physics 23, 035003.



- Shield for Directed Energy



Intense laser or
charged particles

- **A super laser that can destroy an asteroid and save mankind?**

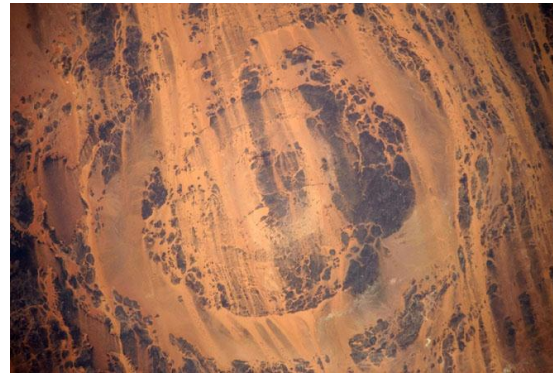
"Dinosaur-Killer" Asteroid Crater Imaged for First Time

National Geographic News

March 7, 2003

A high-resolution map from NASA's Shuttle Radar Topography Mission (SRTM), released yesterday, has provided the most telling visible evidence to date of a 112-mile (180-kilometer) wide, 3,000-foot (900-meter) deep impact crater, the result of a collision with a giant comet or asteroid on one of Earth's all-time worst days.

Asteroid Impact Craters on Earth as Seen From Space



- **Laser stargate**



Consequences of Dirac's Theory of the Positron

Zeitschr. Phys. 98, 714 (1936).

Folgerungen aus der Diracschen Theorie des Positrons.

Von W. Heisenberg und H. Euler in Leipzig.

Mit 2 Abbildungen. (Eingegangen am 22. Dezember 1935.)

$$\mathcal{L} = \frac{1}{2}(\mathfrak{E}^2 - \mathfrak{B}^2) + \frac{e^2}{\hbar c} \int_0^\infty e^{-\eta} \frac{d\eta}{\eta^3} \left\{ i\eta^2 (\mathfrak{E} \mathfrak{B}) \cdot \frac{\cos\left(\frac{\eta}{|\mathfrak{E}_k|} \sqrt{\mathfrak{E}^2 - \mathfrak{B}^2 + 2i(\mathfrak{E} \mathfrak{B})}\right) + \text{conj.}}{\cos\left(\frac{\eta}{|\mathfrak{E}_k|} \sqrt{\mathfrak{E}^2 - \mathfrak{B}^2 + 2i(\mathfrak{E} \mathfrak{B})} - \text{conj.}\right)} + |\mathfrak{E}_k|^2 + \frac{\eta^2}{3} (\mathfrak{B}^2 - \mathfrak{E}^2) \right\}$$

VOLUME 91, NUMBER 8

PHYSICAL REVIEW LETTERS

week ending
22 AUGUST 2003

Light Intensification towards the Schwinger Limit

Sergei V. Bulanov,^{*} Timur Esirkepov,[†] and Toshiki Tajima

REVIEWS OF MODERN PHYSICS, VOLUME 78, APRIL-JUNE 2006

Nonlinear collective effects in photon-photon and photon-plasma interactions

Mattias Marklund^{*} and Padma K. Shukla^{*}

Nonperturbative multiphoton electron-positron-pair creation in laser fields

Guido R. Mocken,^{*} Matthias Ruf,[†] Carsten Müller,[‡] and Christoph H. Keitel[§]

PRL 100, 010403 (2008)

PHYSICAL REVIEW LETTERS

week ending
11 JANUARY 2008

Nonperturbative Vacuum-Polarization Effects in Proton-Laser Collisions

A. Di Piazza,^{*} K. Z. Hatsagortsyan,[†] and C. H. Keitel[‡]

New Journal of Physics 14 (2012) 103002

Photon-photon scattering in collisions of intense laser pulses

B King^{1,2} and C H Keitel¹

VOLUME 79, NUMBER 9

PHYSICAL REVIEW LETTERS

1 SEPTEMBER 1997

Positron Production in Multiphoton Light-by-Light Scattering

PRL 97, 121302 (2006)

PHYSICAL REVIEW LETTERS

week ending
22 SEPTEMBER 2006

Signatures of the Unruh Effect from Electrons Accelerated by Ultrastrong Laser Fields

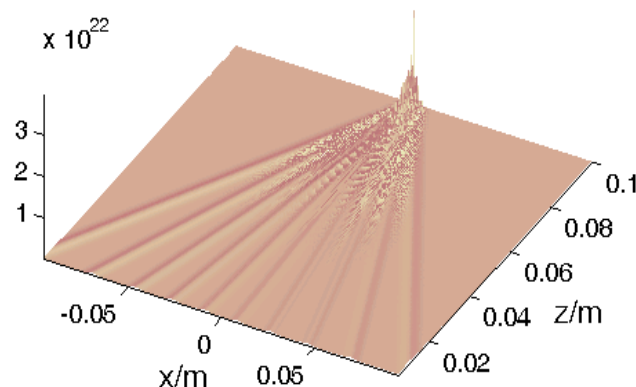
9/3/2014

R Ooi @ KITP UCSB
Ralf Schützhold,^{1,*} Gernot Schaller,¹ and Dietrich Habs²

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Outline

- Recent related works on nonlinear QED
- Scheme to generate superintense laser field
- Synchronization method
- Design constraints
- Theoretical justifications
- Simulated results of intensity distributions



Schwinger's limit

Schwinger field $E_S = m_0 c^2 / e \lambda_c$ 1.3233×10^{18} V/m

$$\lambda_c = \hbar / mc \sim c \delta t \sim 0.386 \text{ pm, Compton length}$$

Schwinger intensity $I_S = 10^{29} \text{ W/cm}^2$ or 10^{33} W/m^2

The probability of spontaneous production of pair creation per unit time per unit volume

$$w = \frac{1}{\pi^2} \frac{\alpha}{\delta t} \frac{1}{\lambda_c^3} \left(\frac{E}{E_S} \right)^2 \sum_{n=1}^{\infty} \frac{1}{n^2} \exp\left(-n\pi \frac{E_S}{E}\right)$$

J. Schwinger, Phys. Rev. 82, 664 (1951). $\delta t = \hbar / m_0 c^2$

The number of pair creation $N = V \tau_p w$

1 pair at 10^{27} W/cm^2

Petawatt-class ultra-short quantum beam facility(UQBF) of the APRI, GIST



ASILS 4
2008

	Erg/J	Duration /fs	P/PW	I/W/cm2	waist	focus
LLNL	660	440	1.5	0.7^{21}	3.2cm 10^{14}	5mic
HERCULES	20	60	0.3	0.5^{23}	4inch or 10cm	1.3mic
UK/Vulcan						

Table top max intensity 10^{23} W/cm²

For higher intensity we need larger beam size and pump power

NIF & LMJ :

2MJ at 350nm in 3ns

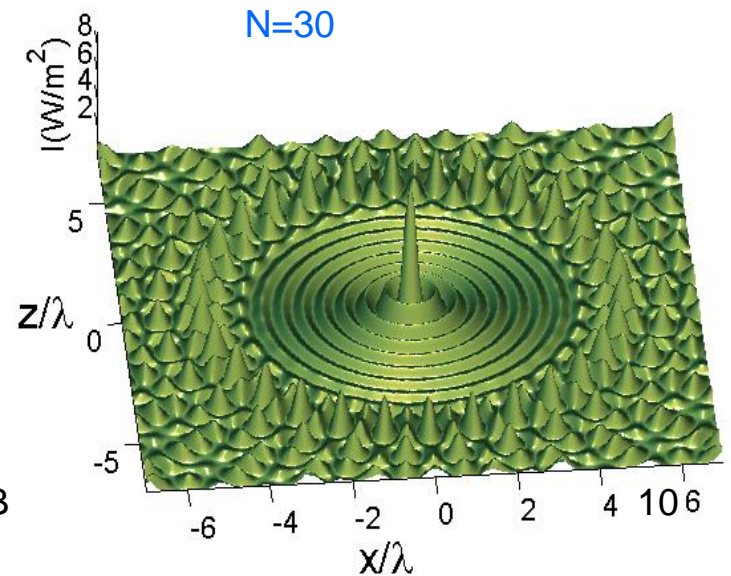
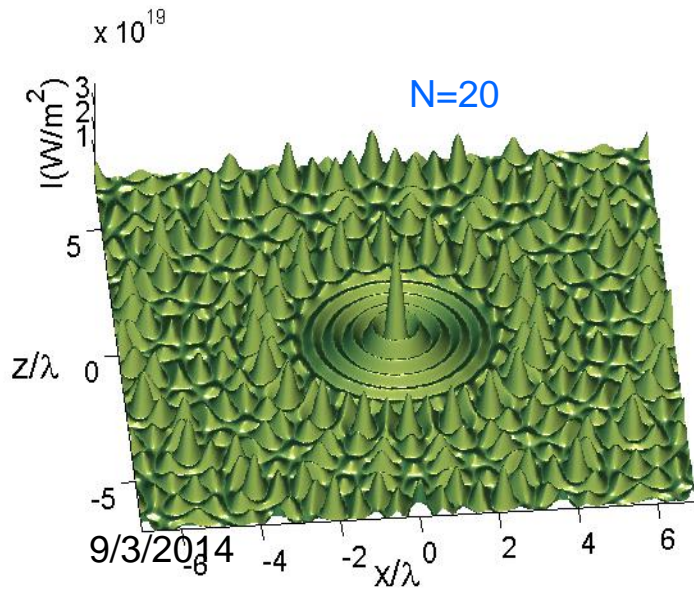
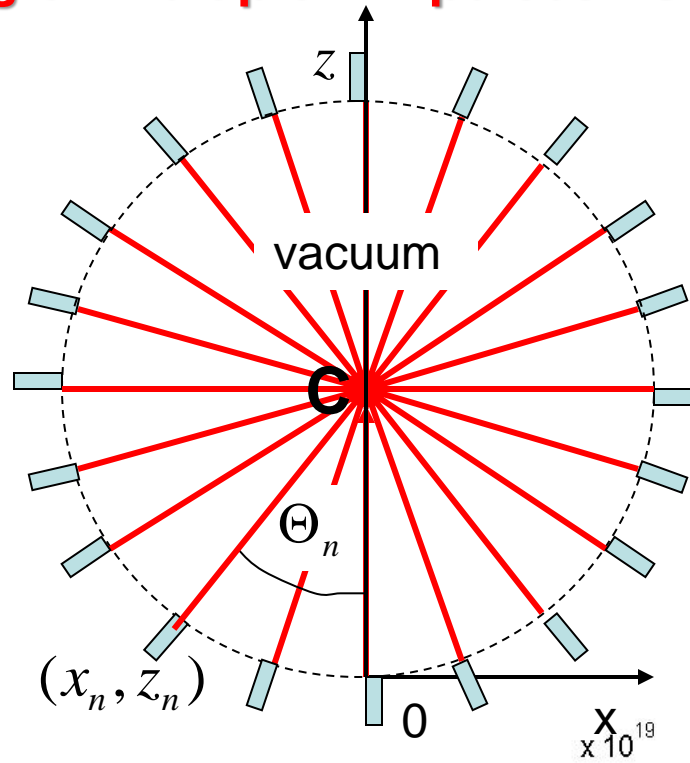
5MJ at 530nm in 10-20ns => pump CPA giving 1 MJ in 10fs (1 micron²) $I \sim P_{th} / \lambda^2$

Fsat of amplifier = $h\nu/\sigma$ ~1 for Ti:Sap , ~40 for Yb:glass

Grating: 10m , $F_d \sim 1$ J/m²

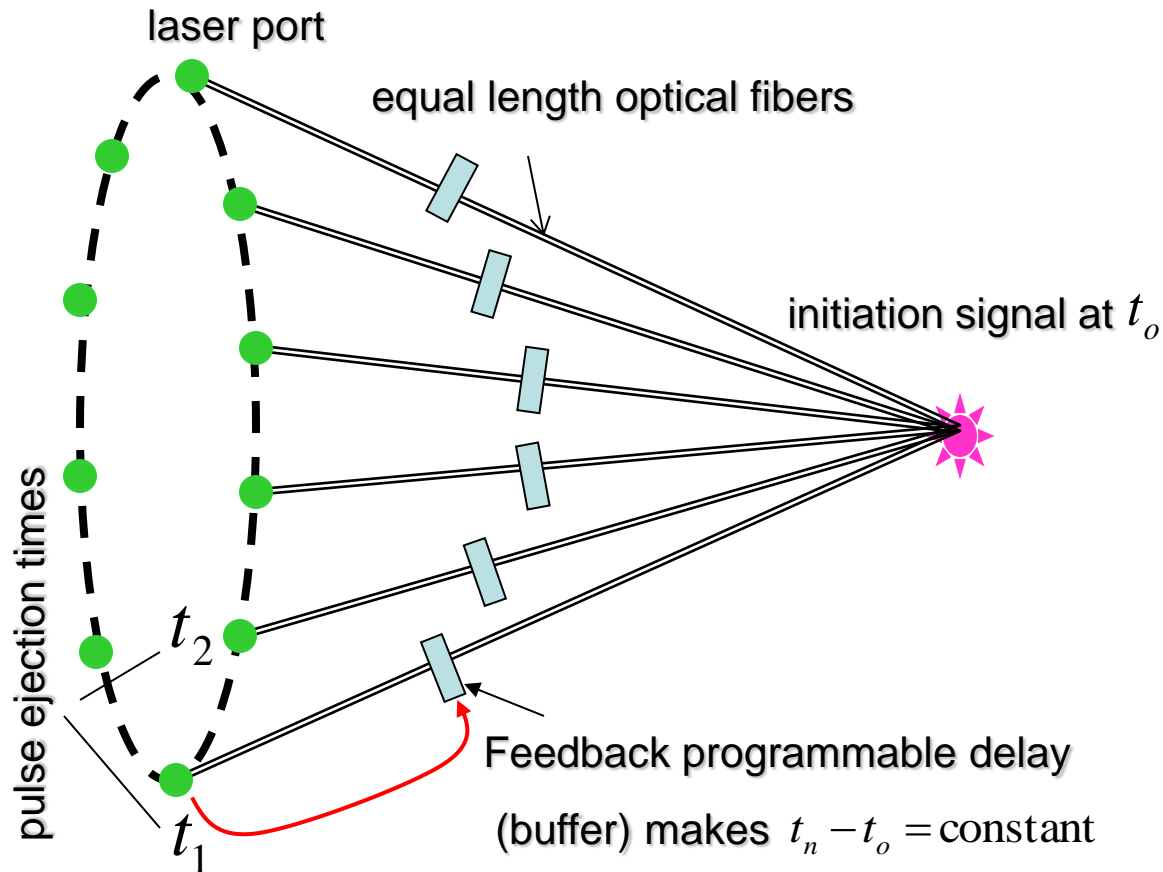
Phase controlled by deformable parabolic mirror

Merging of Multiple PW pulses - Unfocused



Pulse synchronization / initiation scheme

Superintense laser fields in circular array: effects of phase and pulse jitters,
C H Raymond Ooi & TY Tou, Appl Phys B (2010) 101: 825–833



Optical buffer compensates for the different amplification duration of each laser

Advanced Ti:Sa OPCPA can produce femtosecond laser pulse with

$$U_o = \frac{1}{2} \epsilon_0 E_0^2 c \tau A_o = 200 J$$

duration $\tau = 50 fs$ and a waist of $w_0 = 3.6 mm$ (cross section $A_o = \pi(w_0/2)^2 = 10^{-5} m^2$).

$$P_o = \frac{1}{2} \epsilon_0 E_0^2 c A_o = 4 PW,$$

$$I_o = \frac{1}{2} \epsilon_0 E_0^2 c = 4 \times 10^{20} W/m^2$$

$$E_0 = 5 \times 10^{11} V/m$$

Below damage threshold $10^{22} W/m^2$ of optical surfaces, multiple beams can still be manipulated by optics.

For $N = 10$ beams directed from the edge of a circle to the center, intensity increases by 100 time to $4 \times 10^{22} W/m^2$.

Intensity is still (10^4 times) lower than the current record $5 \times 10^{26} Wm^{-2}$.

Output waist is not focused to diffraction limit in order to avoid strong energy spread upon propagation towards C .

If PW lasers focused to the diffraction limit of $3.6 \mu m$ intensity would increase 10^6 times, towards $4 \times 10^{28} W/m^2$.

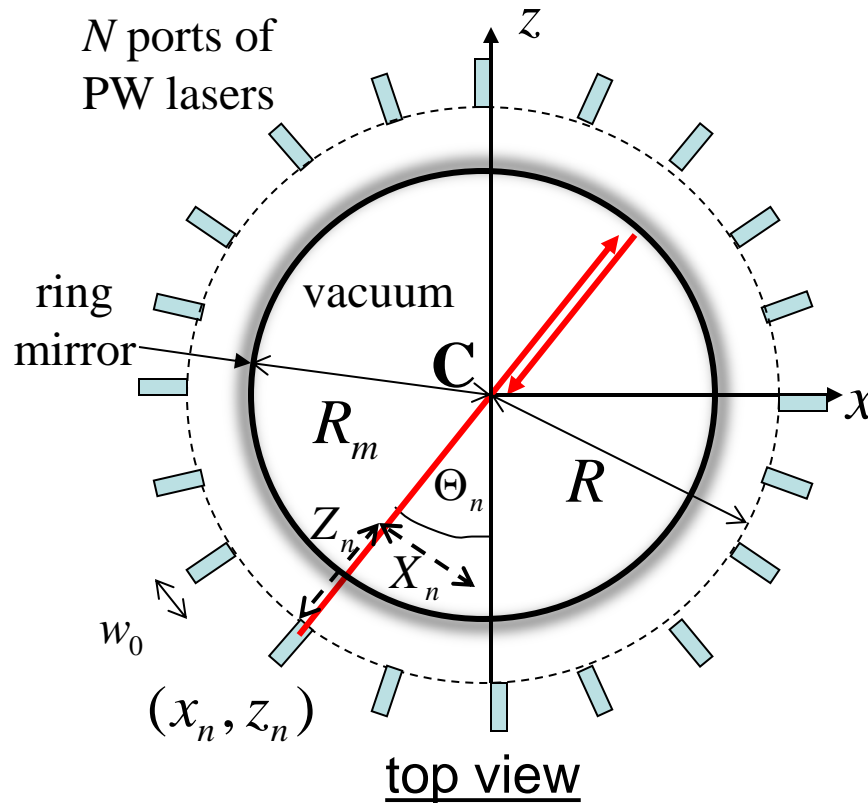
We don't stop at PW

PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS, VOLUME 5, 031301 (2002)

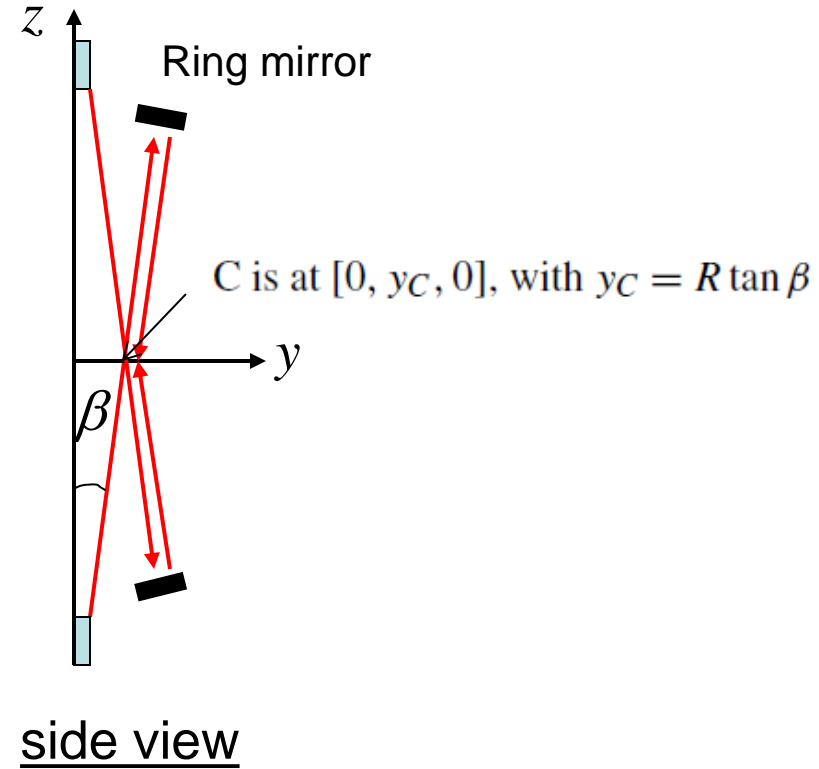
Zettawatt-exawatt lasers and their applications in ultrastrong-field physics

The Scheme: Multiple lasers in circular geometry

Multiple PW pulses

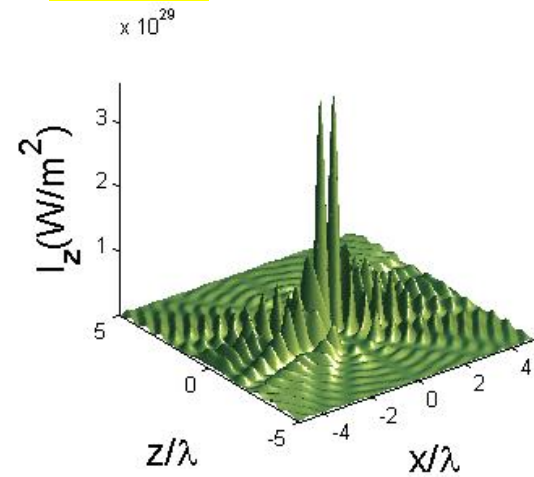
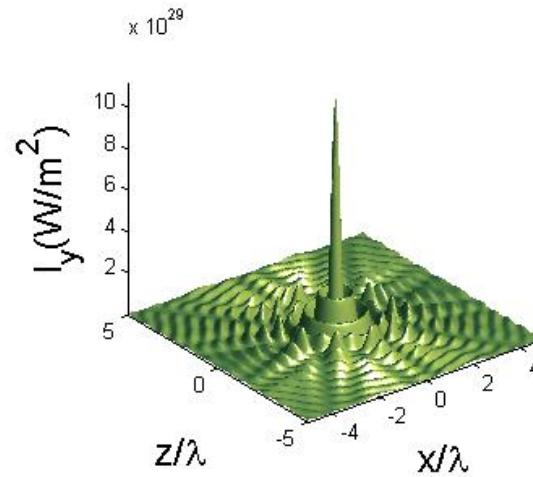
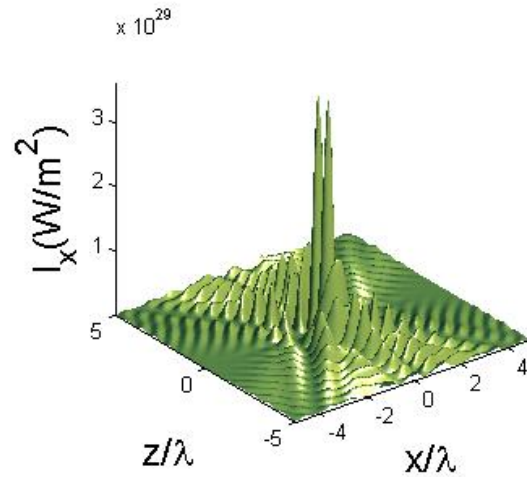
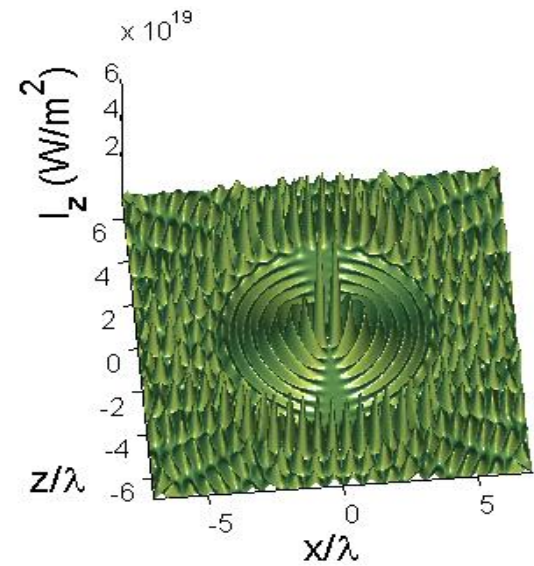
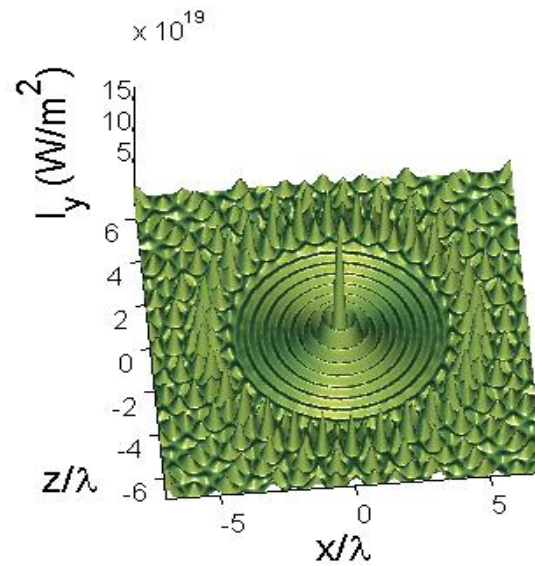
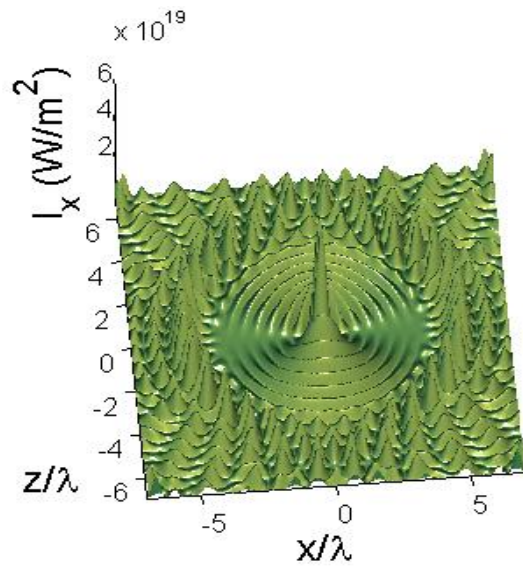


N^2 intensity enhancement at target C

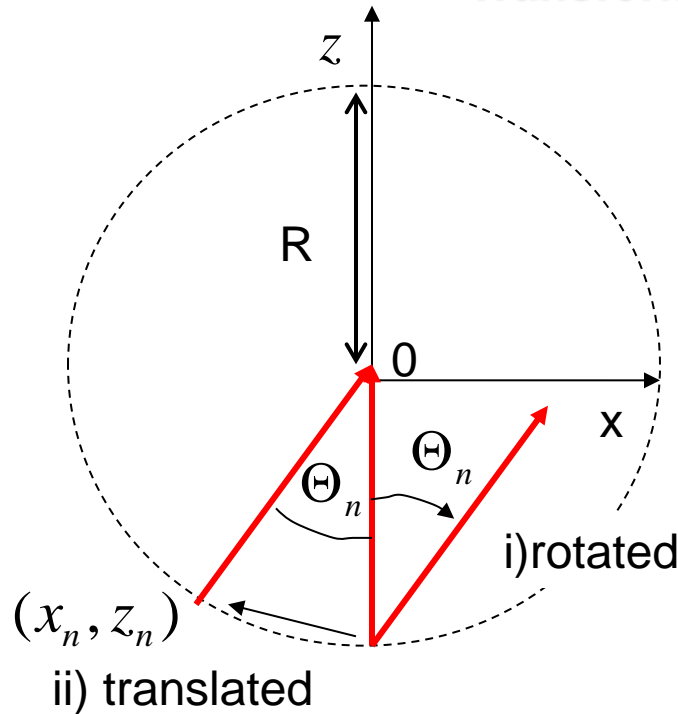


CH Raymond Ooi, JOURNAL OF APPLIED PHYSICS **107**, 043110 2010

The ring mirror does the “focusing” effect, replacing deformable mirror



Transformation to circular geometry



$$X_n = (x - x_n) \cos \Theta_n - (z - z_n) \sin \Theta_n$$

$$Z_n = (x - x_n) \sin \Theta_n + (z - z_n) \cos \Theta_n$$

$$x_n = -R \sin \Theta_n, \quad z_n = -R \cos \Theta_n$$

$$\mathbf{E}_n(x, y, z, t) = \hat{u}_n E_o e^{-i(\omega \tau_n + \varphi_n)} F(Z_n) \exp\{-F(Z_n) \rho_n^2\} \exp\left\{-\left(\frac{\tau_n + \delta_n}{T}\right)^2\right\}$$

CEP

Imperfect sync

$$F(Z_n) = \frac{1}{1 - iZ_n^r / z_R}$$

$$z_R = k_0 w_0^2 / 2$$

$$\rho_n = \sqrt{X_n^2 + y_n^2} / w_0$$

$$\tau_n = t - Z_n^r / c$$

$$\begin{pmatrix} Z_n^r \\ y_n^r \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} Z_n \\ y_n \end{pmatrix}$$

$$X_n = \Delta x_n \cos \Theta_n - \Delta z_n \sin \Theta_n$$

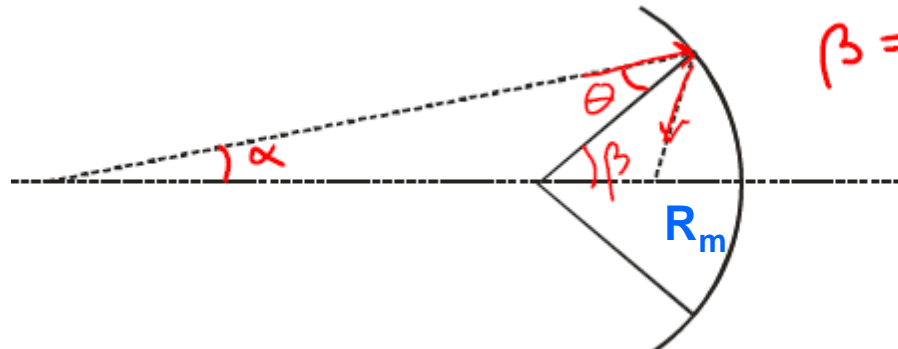
$$Z_n = \Delta x_n \sin \Theta_n + \Delta z_n \cos \Theta_n$$

$$\Delta x_n = x - x_n, \quad x_n = -R \sin \Theta_n,$$

$$\Delta z_n = z - z_n, \quad z_n = -R \cos \Theta_n$$

Reflection off mirror

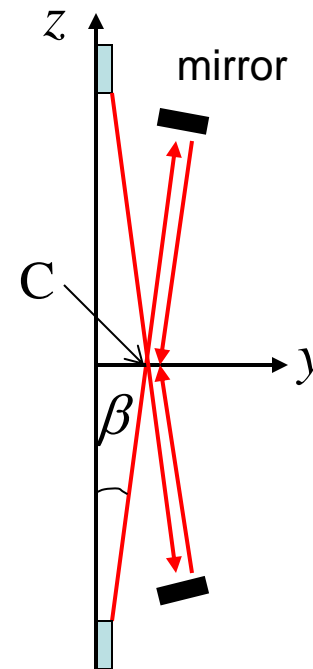
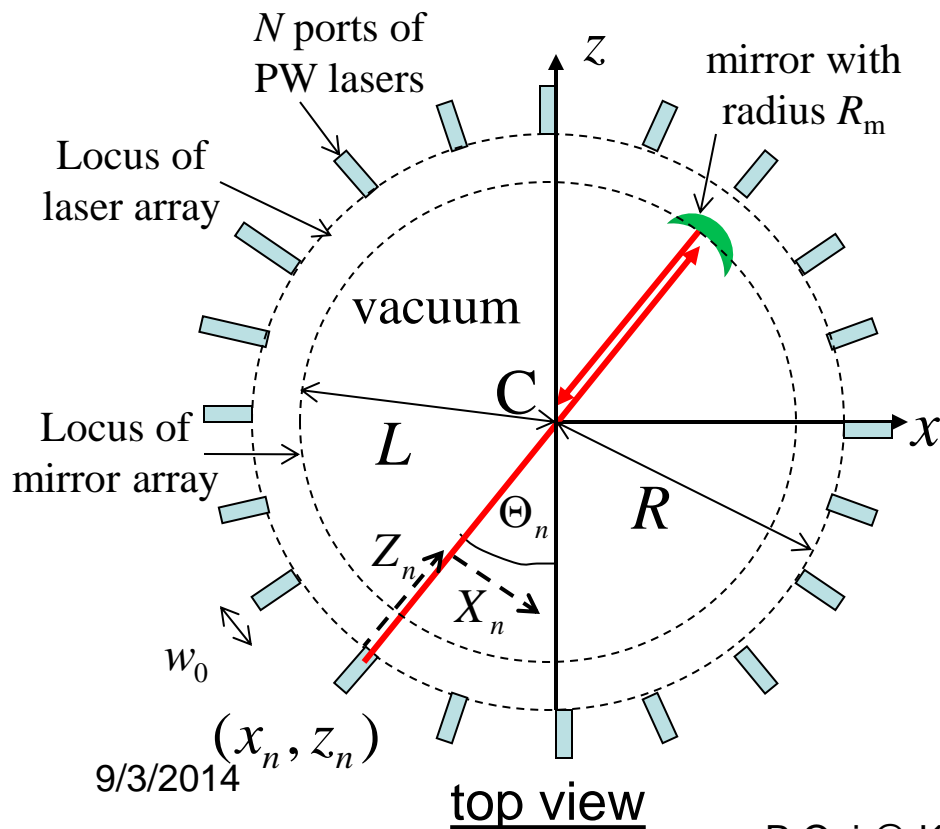
$$\beta = \alpha + \theta$$



Ring mirror : $L=R_m$ but focus will NOT be at C the center of the circle C but at $R_m/2$

C H Raymond Ooi & TY Tou, Appl Phys B (2010) 101: 825–833

Using piecewise mirrors with $R_m=2L$: Focus will be at C



$$\mathcal{R} = \frac{R}{\cos \beta} \text{ and } \mathcal{L} = \frac{L}{\cos \beta}$$

Electric field after reflection by mirror

$$\mathbf{E}'_n = \mathbf{E}'_{n,o} e^{-i(\omega\tau'_n + \varphi_n)} \mathcal{F}_n e^{-\mathcal{F}_n \rho_n'^2} e^{-\left(\frac{\tau'_n + \delta_n}{T}\right)^2}$$

$$\mathcal{F}_n = \mathcal{F}(Z'_n) = i \frac{z_{Rm}}{q_m(Z'_n)} \quad \rho'_n = \sqrt{X_n'^2 + (y_n^r)^2} / w_0$$

$$z_{Rm} = k_0 w_m^2 / 2, \quad q_m(Z'_n) = Z'_n + i z_{Rm} \quad w_m \simeq w_0 \mathcal{L} / z_R$$

$$X'_n = x \cos \Theta_n - z \sin \Theta_n$$

$$Z'_n = x \sin \Theta_n + z \cos \Theta_n$$

$$\tau'_n = t - (R + 2R_m)/c + Z'_n/c$$

$$w_m = w_0 \sqrt{\Lambda^2 \left(\frac{S^2}{z_R^2} + 1 \right) + \mathcal{L} \frac{(2\Lambda S + \mathcal{L})}{z_R^2}} = w_0 \xi \quad (7)$$

$$\text{where } S = \mathcal{L} + \mathcal{R}, \quad \mathcal{L} = \frac{L}{\cos \beta}, \quad \mathcal{R} = \frac{R}{\cos \beta} \quad \text{and} \quad \Lambda = 1 - \frac{2\mathcal{L}}{R_m}$$

Boundary condition: Matching the fields at \mathbf{E}_o and \mathbf{E}_o' at the mirror

$$E_o' F_n^*(\mathcal{L} + \mathcal{R}) = E_o' \mathcal{F}_n(\mathcal{L}) \quad \text{at the reflection points } \mathbf{R}_n^m$$

$$\text{mirror position } \mathbf{R}_n^m = \left[-\frac{L}{R} x_n, (R + L) \tan \beta, -\frac{L}{R} z_n \right]$$

Field enhancement factor

The boundary condition gives $E'_o = E_o \frac{1-i\mathcal{L}/z_{Rm}}{1-i(\mathcal{L}+\mathcal{R})/z_R}$

After reflection from the mirror, the intensity (at origin C) increases by a factor of

$$\epsilon = \frac{\mathcal{L}^2/z_{Rm}^2 + 1}{(\mathcal{L} + \mathcal{R})^2/z_R^2 + 1}$$

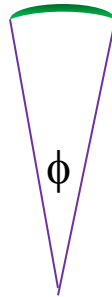
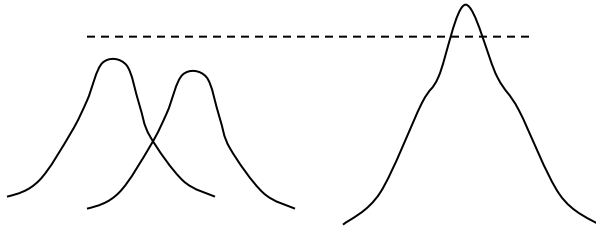
Intensity enhancement for N laser pulses at point C after reflection from the mirror

$$\eta = \frac{I_N}{I_o} = N^2 \epsilon \simeq \frac{N^2 \mathcal{L}^2}{z_{Rm}^2} = \frac{N^2 \mathcal{L}^2 \lambda^2}{\pi^2 w_m^4} = \left(N \frac{z_R}{\mathcal{L}}\right)^2$$

boosted by a small \mathcal{L} radius of mirror array?

Constraints

Mirror radius cannot be reduced below a value such that the beams overlap, and constructive interference creates region of intensity beyond the damage threshold



$$2\pi R = \alpha' N R 2\phi' \text{ with } \alpha' \geq 1$$

$$L = \frac{w_0}{\sin \phi} = \frac{w_0}{\sin \frac{\pi}{\alpha N}} \simeq \frac{\alpha N w_0}{\pi}$$

Paraxial approximation

$$\theta^2 = \left(\frac{\lambda}{\pi w_m}\right)^2 \simeq \left(\frac{w_0}{\mathcal{L}}\right)^2 \simeq \left(\frac{2w_0}{R_m} \cos \beta\right)^2 \ll 1$$

Combined constraint

$$\theta = \cos \beta \sin(\pi / \alpha N) \ll 1$$

$$N_{\min} = \frac{\pi}{\alpha \sin^{-1}(\theta_{\max} / \cos \beta)} \xrightarrow{\theta_{\max}=0.05} 63$$

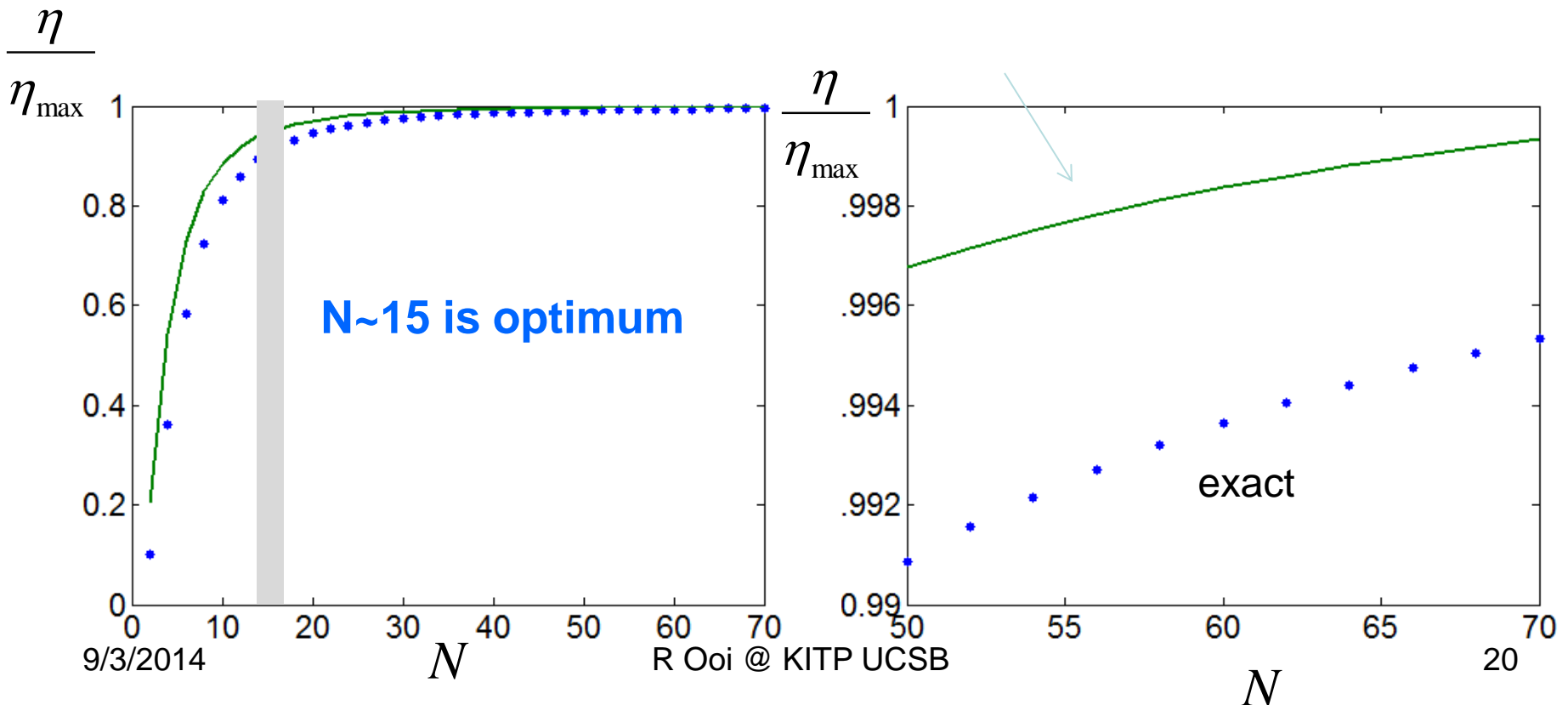
$$L_{\min} = \frac{w_0 \cos \beta}{\theta_{\max}} \xrightarrow{\quad} 20 w_0$$

Optimum number of lasers

$$\eta \simeq \left(\frac{N z_R}{\mathcal{L}} \right)^2 = \left(\frac{N \pi w_0}{\lambda} \sin \frac{\pi}{\alpha N} \cos \beta \right)^2$$

Limit of very large N gives maximum enhancement

$$\eta_{\max} = \left(\frac{\pi^2 w_0}{\alpha \lambda} \cos \beta \right)^2$$



Ultimate Super- field

Laser fluence must be less than the mirror damage threshold

$$\frac{1}{2}\epsilon_0 E(R_m)^2 cT < F_d \simeq 1\text{J}/\text{cm}^2$$

$$T = 100 \text{ fs} \quad I_o^{\max} = F_d/T = 10^{17} \text{Wm}^{-2}$$

Final expression for superintense field (scales with beam diameter), $\alpha=1$. $\beta=0$

$$I^{\max} = I_o^{\max} \left(\frac{\pi w_0}{\lambda} \right)^2$$

$$10^{27-28} \text{Wcm}^{-2}$$

$$10^{31-32} \text{Wm}^{-2}$$

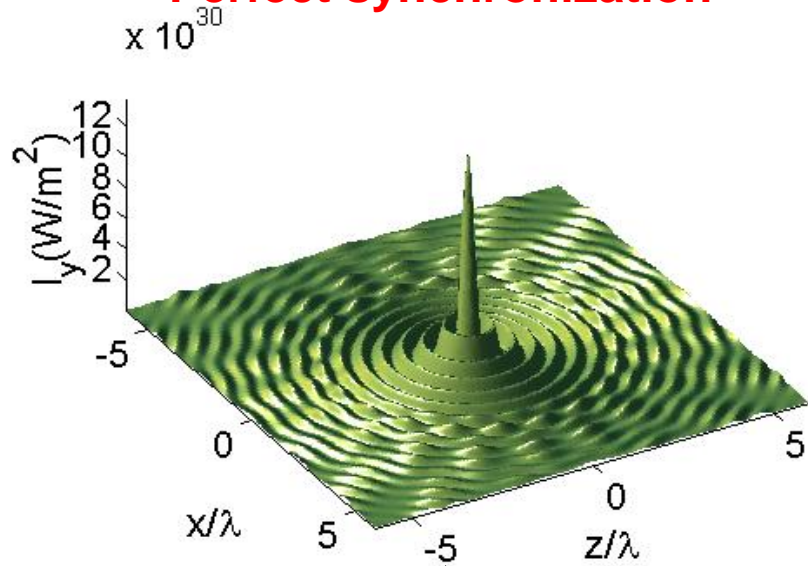
Nonlinear vacuum QED

$$N = 63, w_0 = 1\text{m}, I_o^{\max} = 10^{17} \text{Wm}^{-2} \text{ and } \lambda = 840\text{nm},$$

OR shorter (atto) pulses 10fs with $w_0=10\text{cm}$

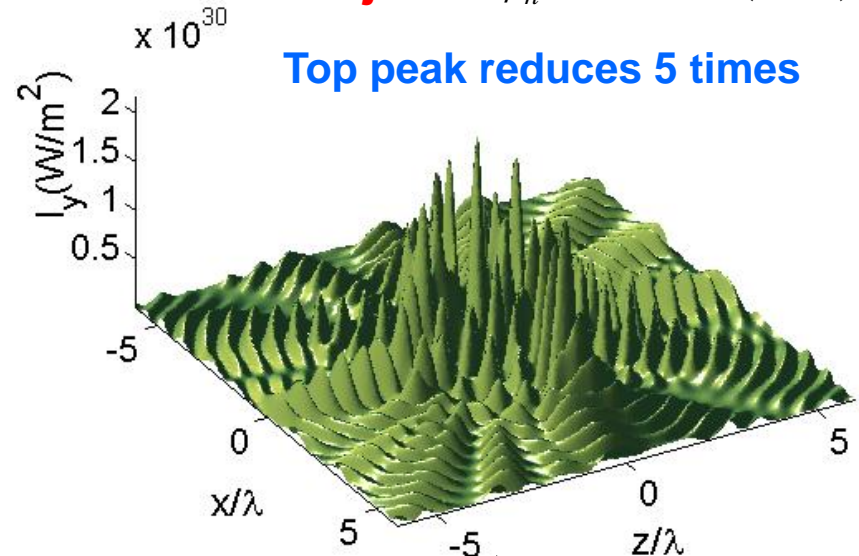
OR smaller laser near UV : $w_0=30\text{cm}$ and $\lambda=280\text{nm}$

Perfect synchronization



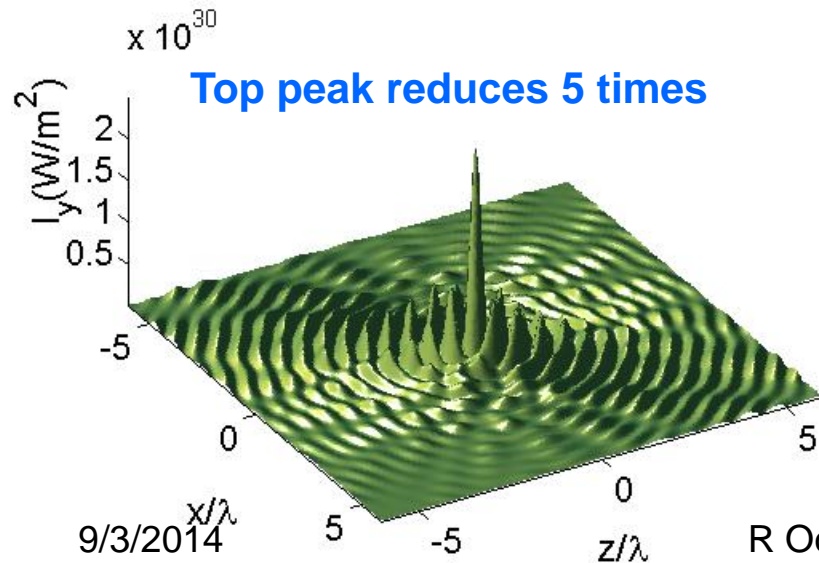
a)

CEP jitter $\varphi_n = 2\pi \text{ rand}(\pm 0.5)$



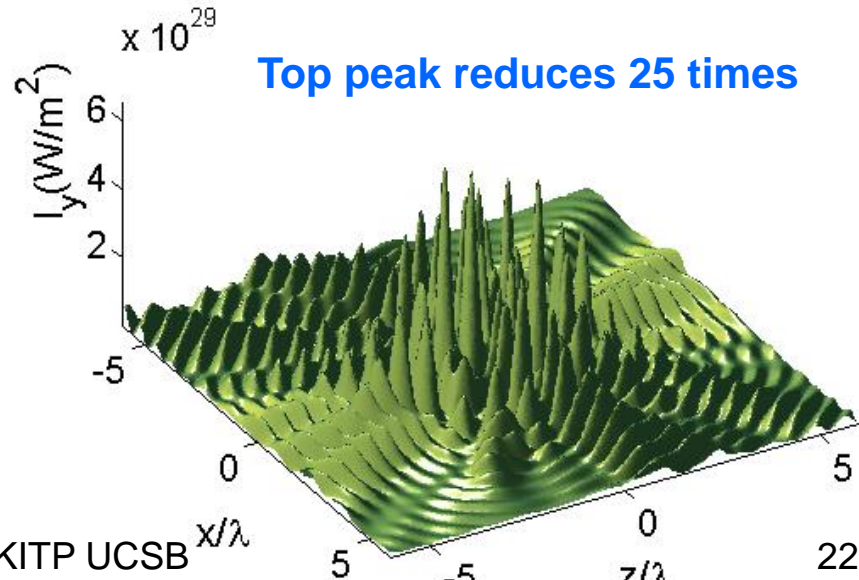
c)

pulse envelope jitter $\delta_n = 4T \text{ rand}(\pm 0.5)$



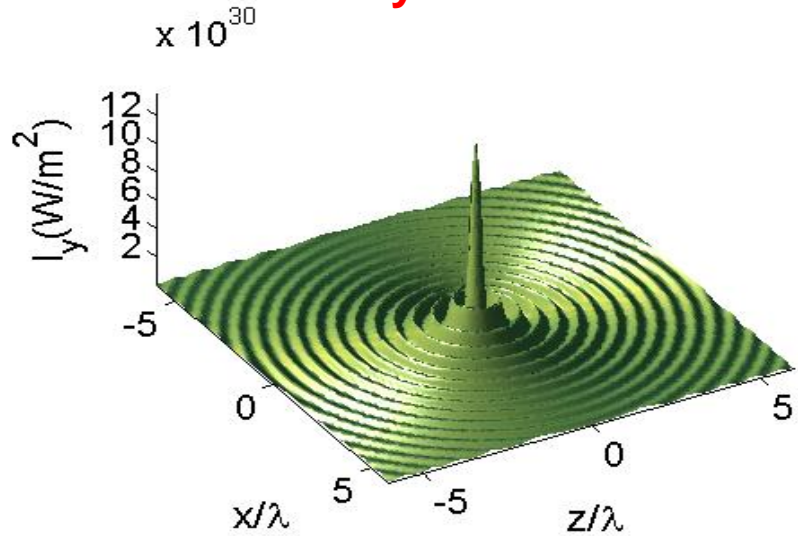
b)

pulse envelope and CEP jitters



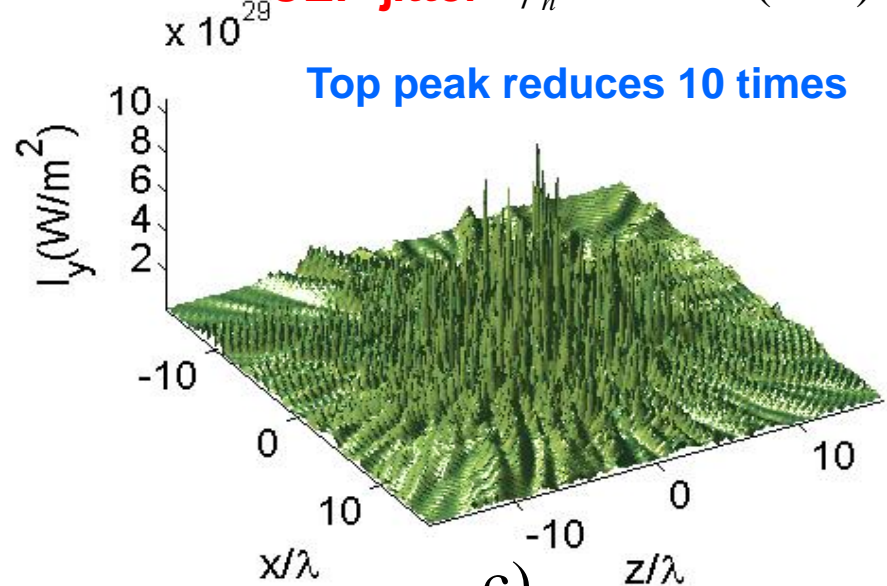
d)

Perfect synchronization



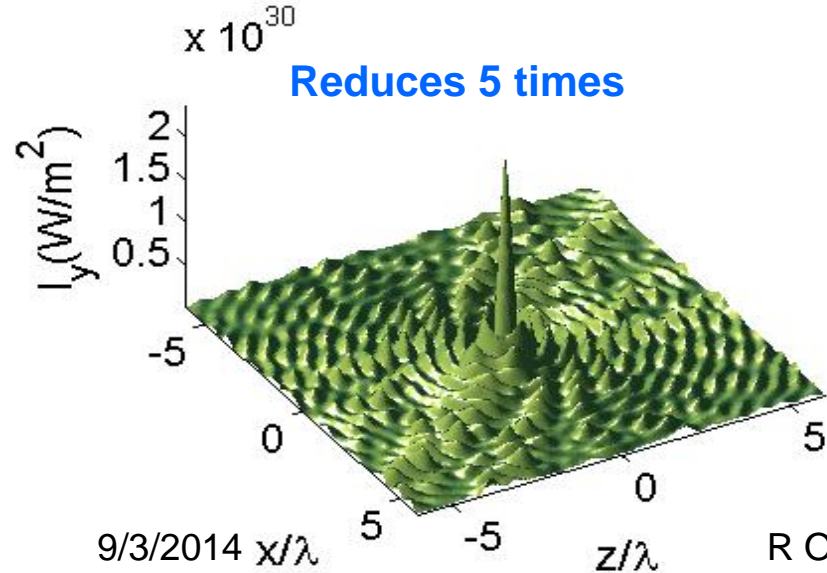
a)

CEP jitter $\varphi_n = 2\pi \text{rand}(\pm 0.5)$



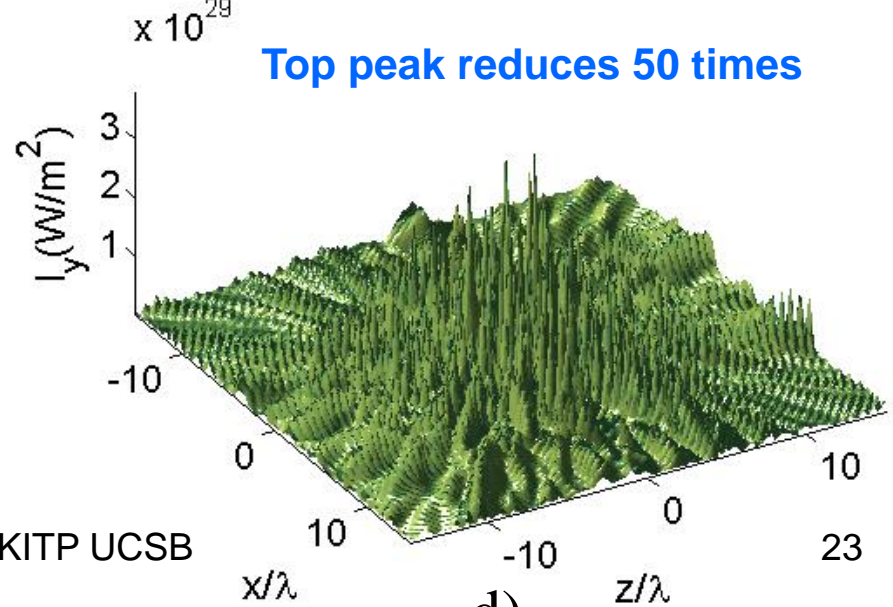
c)

pulse envelope jitter $\delta_n = 4T \text{rand}(\pm 0.5)$



b)

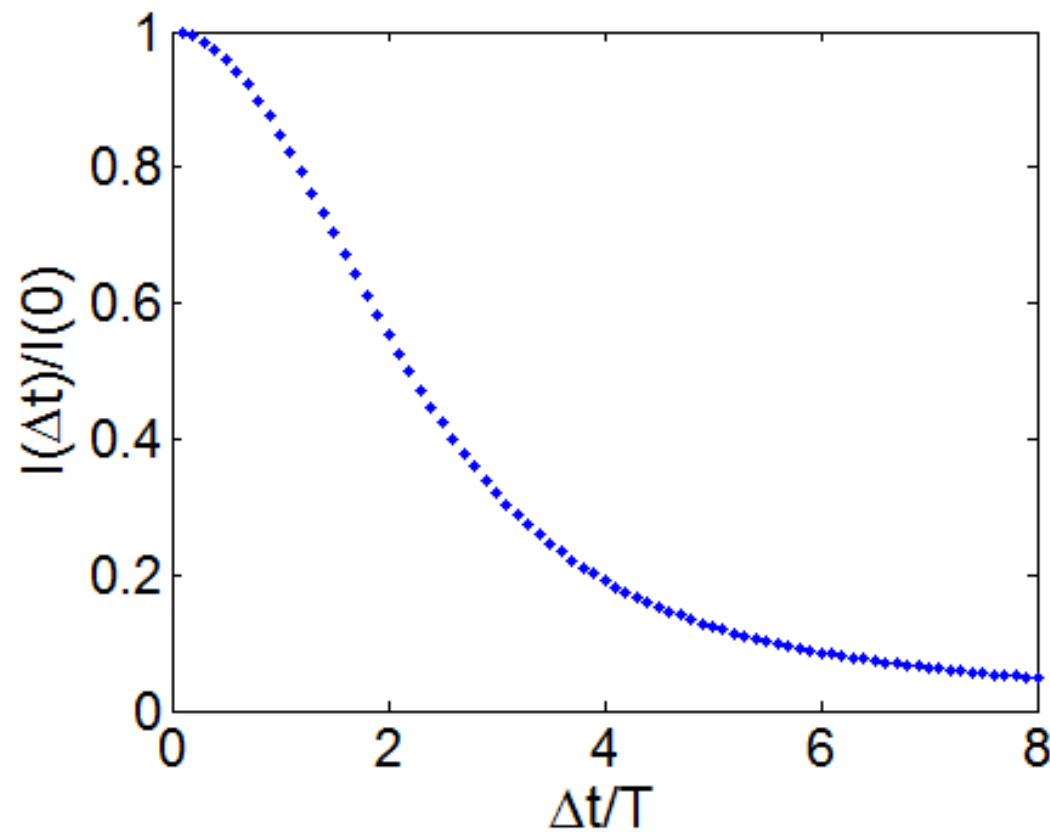
pulse envelope and CEP jitters



d)

Envelope Jitters

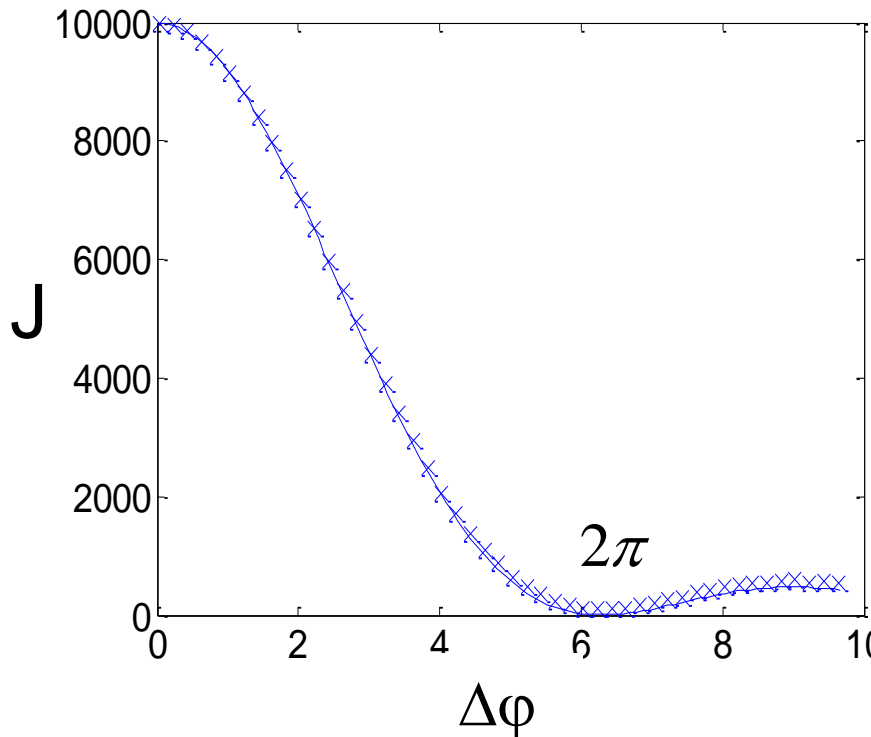
$$\frac{I(\Delta t)}{I(0)} = \frac{1}{(2N+1)^2} \left(2 \sum_{n=1}^N e^{-(n\Delta t/N2T)^2} + 1 \right)^2$$



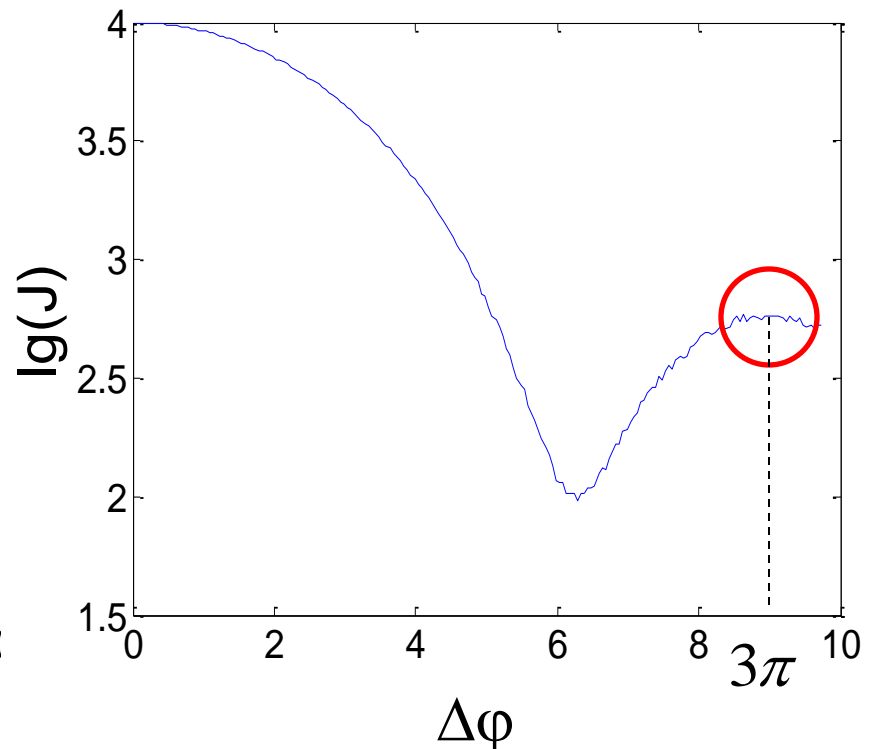
CEP Jitters

$$J(\Delta\varphi) = \frac{1}{M} \sum_{k=1}^M \left| \sum_{n=1}^N e^{i\phi_n} \right|^2 \underset{N \text{ large}}{\simeq} N^2 \frac{\sin^2(\frac{\Delta\varphi}{2})}{(\frac{\Delta\varphi}{2})^2}$$

Number of random trials $M=50$, $N=100$, $\Delta\varphi = 2\pi$



c) i

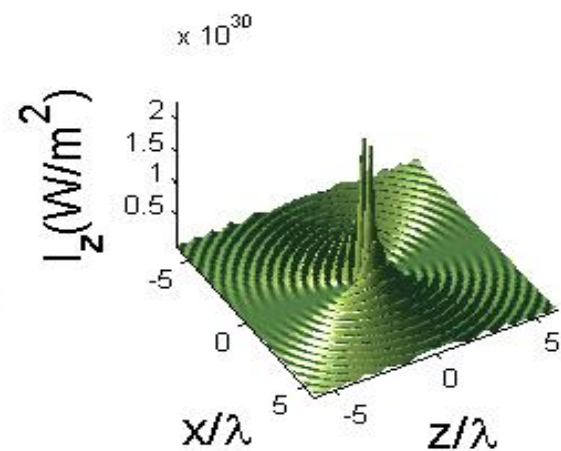
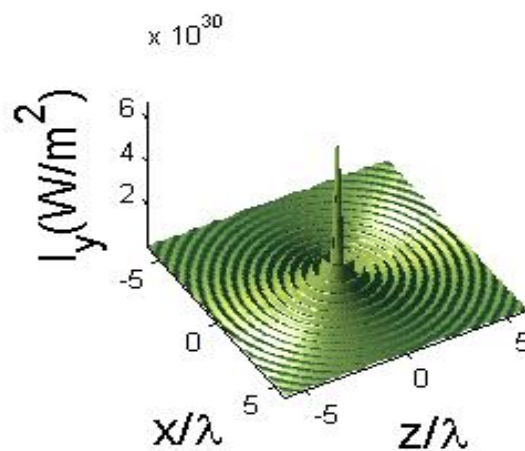
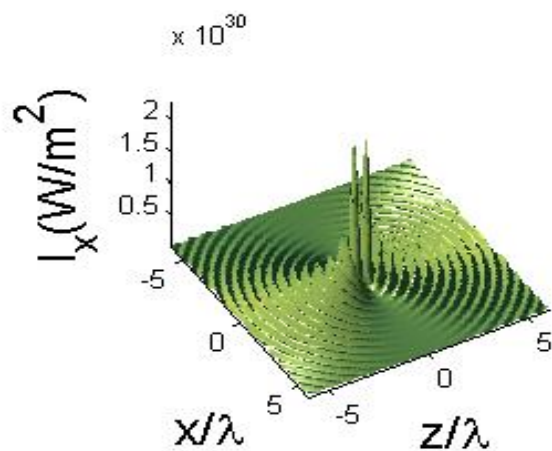


c) ii

Intensity distribution for circularly polarized lasers

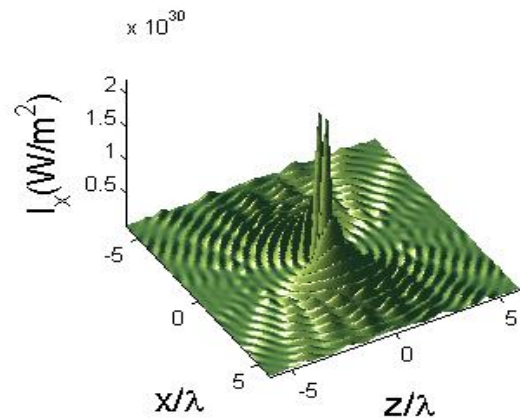
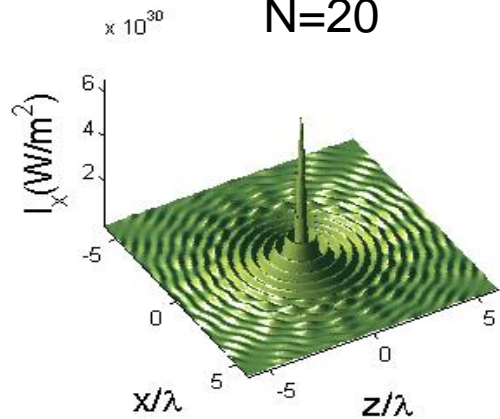
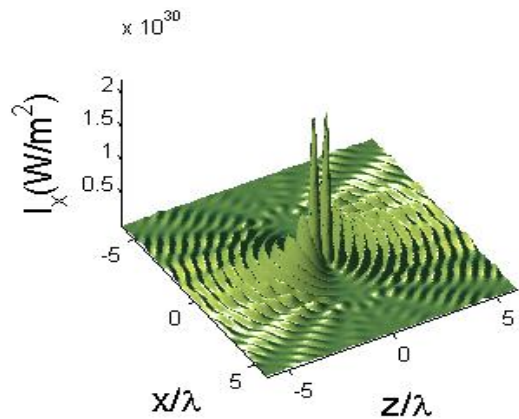
$$I^{lin} \approx I_y^{cir} + \sqrt{2}(I_x^{cir} + I_z^{cir}).$$

N=63

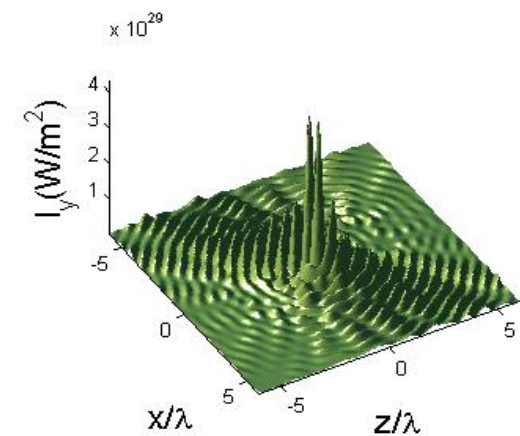
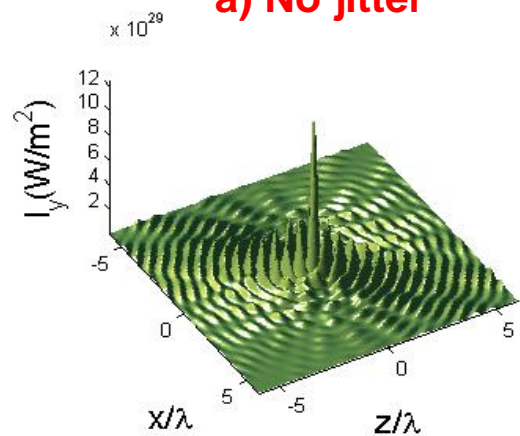
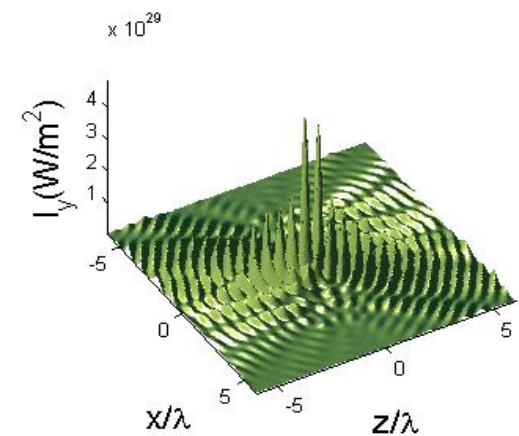


a) No jitter

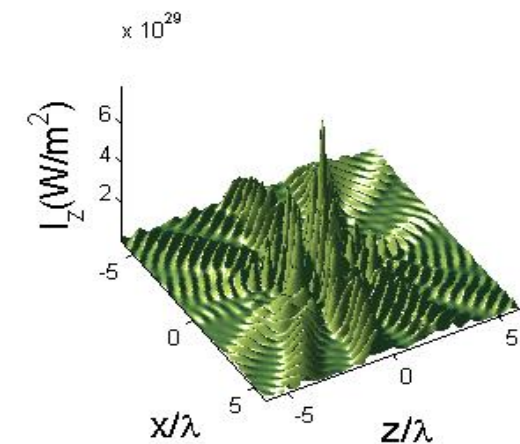
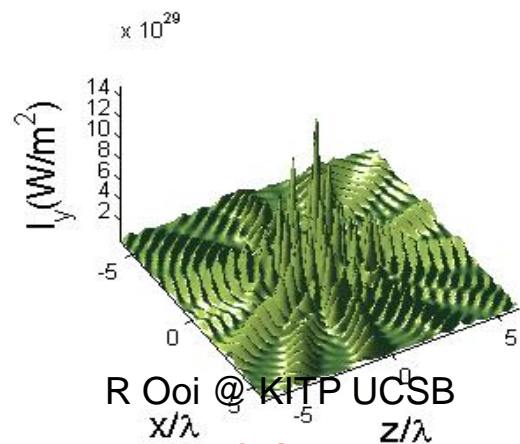
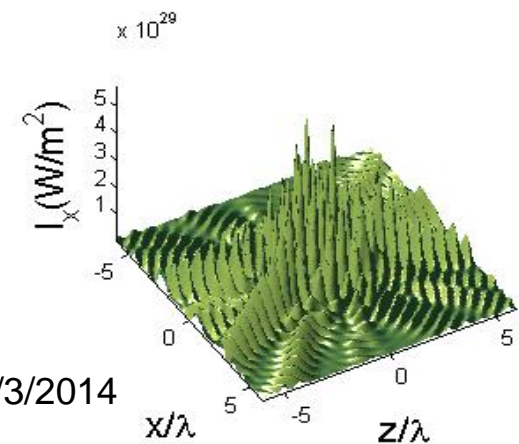
N=20



a) No jitter



b) Pulse envelope jitter



c) CEP jitter

Conclusion

- Multiple pulses in circular geometry can be scaled up to produce intensity beyond the nonlinear vacuum QED.
- Unexpectedly, the enhancement does not scale with N^2 but with area of beam.
- In the (worst) case without synchronizations of the CEP and the pulse timing, the intensity is sacrificed by a factor of 50 only.
- Superintense laser is possible and should be developed to safeguard the future of mankind.

Future research

- Super laser to destroy/deflect massive objects in space

Quantum & Laser Science group

Postdoc

Shailendra Singh (India)

PhDs

F Mathkoor (Yemen) - quantum correlation

Davoud Ghodsi (Iran) - nanophotonics

KS Ng (M'sia) - relativistic optics

PhD

C. Y. Lee (M'sia) - nonlinear photonics

Nor H (M'sia) - quantum optics

Ho Wai Loon (M'sia) - intense laser interactions

MSc

P C Seow (M'sia) - nonlinear scattering

KS Tan(M'sia) - quantum plasmonics

S. Ainisyahida (M'sia) - quantum information

KC Low (M'sia) - micro-nanophotonics

YY Khoo (M'sia) - qtm vacuum



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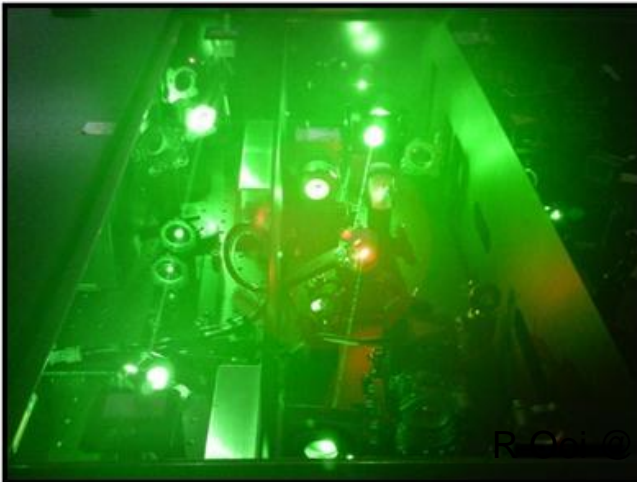
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Quantum and Laser Science, Femtosecond Laser Lab

HIR Building, Universiti Malaya



The Femtosecond Laser.



Opening: Visiting Scientists, Post-doc and PhD/MSc students



Department of Physics, Faculty of Science
50603 Kuala Lumpur, Malaysia

Research Topics

- **Quantum Optics and Quantum Information**
- **Nanophotonics and Plasmonics**
- **Nonclassical Photon Sources**
- **Nonlinear Optics and Laser Spectroscopy**
- **Novel Photonic Crystals and Structures**
- **Ultrafast and Ultraintense Laser Science**
- **Ultracold Gases, Laser Cooling and Trapping**

Offers:

- **Scholarships (allowances and tuition fees) for local students (CGPA > 3.2)**
- **Research assistantship for foreign students**
- **Incentives for ISI publications**

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Thank
You

