

Unstratified hydrodynamic keplerian-like flows: Turbulent or not turbulent ?

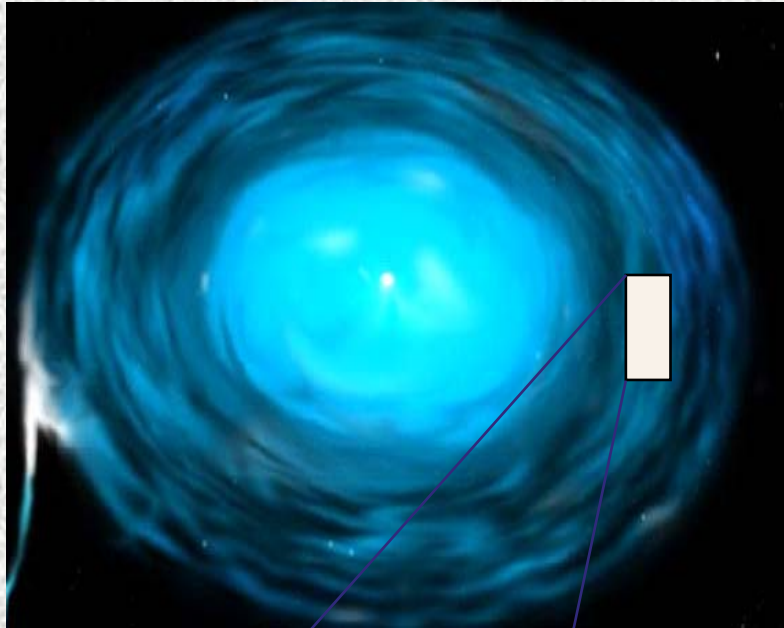
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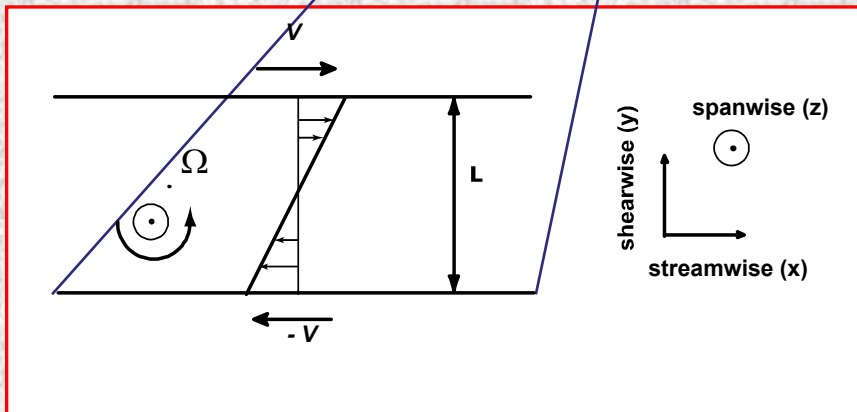
Modelling



Boundary conditions:

**Periodic+rigid
(experiments on
rotating plane Couette
flows)**

**Shearing sheet (local
disk model)**



Equations and characteristic quantities

Rotating plane Couette and shearing sheet:

$$\frac{\partial w}{\partial t} + w \cdot \nabla w = -\frac{\nabla P^*}{\rho} - 2\Omega_0 \times w + \nu \Delta w$$

Scales:

$$\text{Length } L; \quad \text{Time: } t_s = S^{-1}, \quad t_\Omega = (2\Omega_0)^{-1}, \quad t_\nu = \frac{L^2}{\nu}$$

Dimensionless numbers:

$$\text{Re} = \frac{\text{advection}}{\text{dissipation}} = \frac{t_\nu}{t_s} = \frac{|S|L^2}{\nu}; \quad \text{R}_\Omega = \frac{\text{Coriolis}}{\text{advection}} = \frac{2\Omega_0}{S}$$

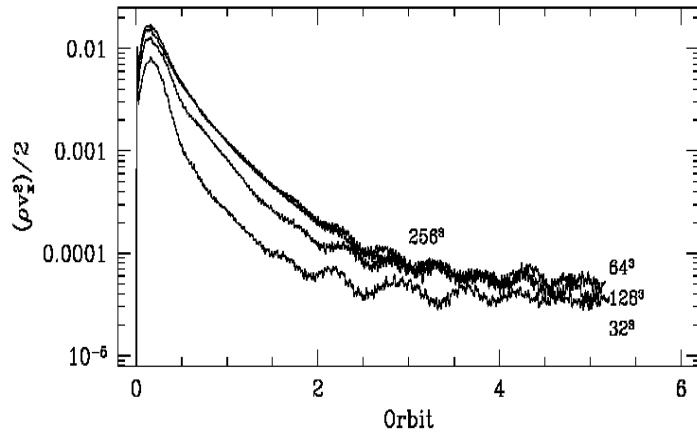
Linear stability limits:

$$\kappa^2 = S^2 \text{R}_\Omega (1 + \text{R}_\Omega) < 0 \Leftrightarrow -1 < \text{R}_\Omega < 0$$

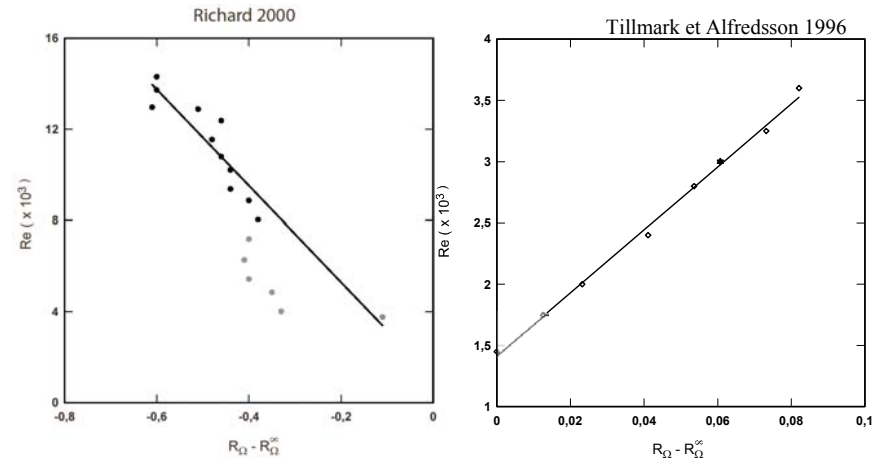
**N.B.: $\text{R}_\Omega > 0$: cyclonic rotation ; $\text{R}_\Omega < 0$: anticyclonic rotation
Keplerian : $\text{R}_\Omega = -4/3$**

Experiments vs simulations

Simulations



Expériences



BHW99: Coriolis force induces loss of turbulence in keplerian-like flows

TA96, R00: turbulence for high enough Reynolds number in keplerian-like flows

Resolution/Reynolds limited ?

**Boundary conditions ?
Secondary flows ?**

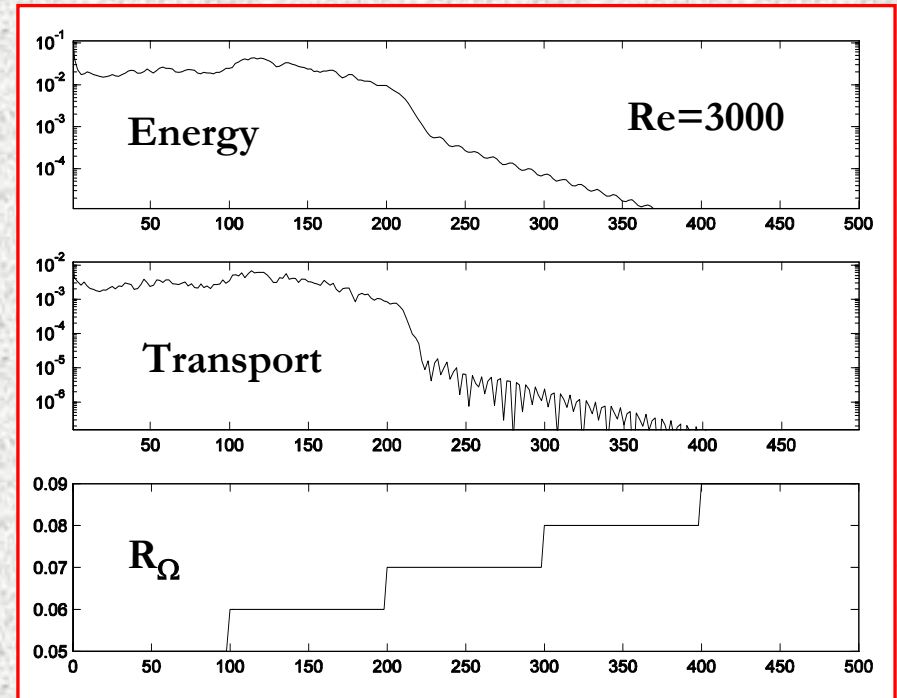
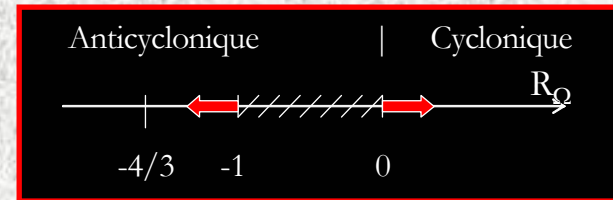
Simulations revisited

1. Choose a resolution
2. Choose a Reynolds number
3. Evolve from marginal stability until turbulence is lost

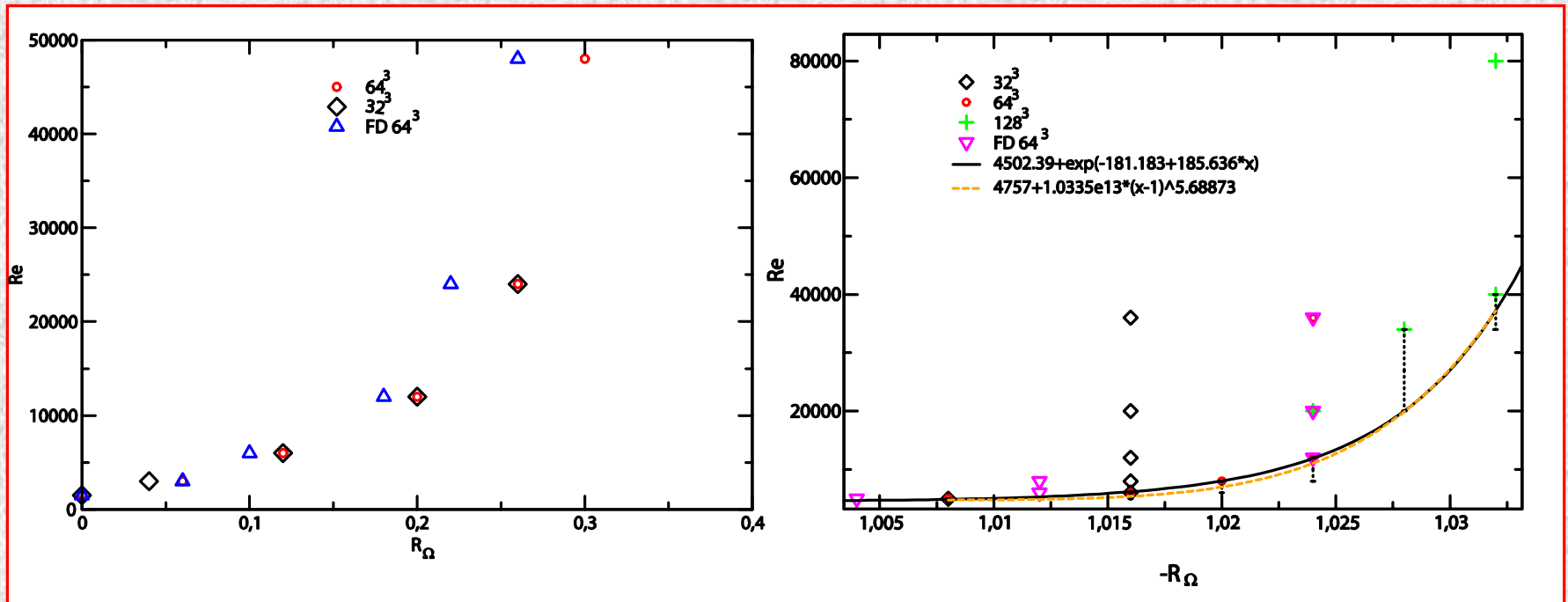
Aims:

Characterize the link between resolution and Reynolds number

Quantify turbulent transport

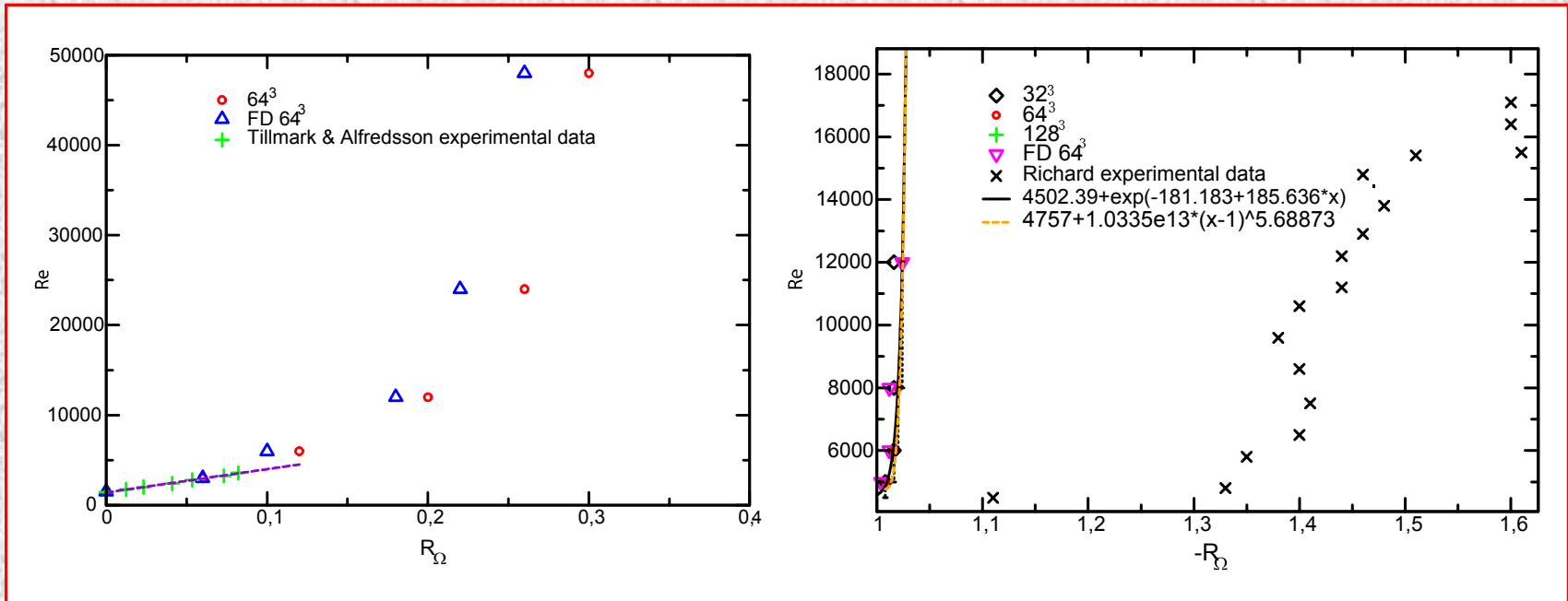


Transition Reynolds number



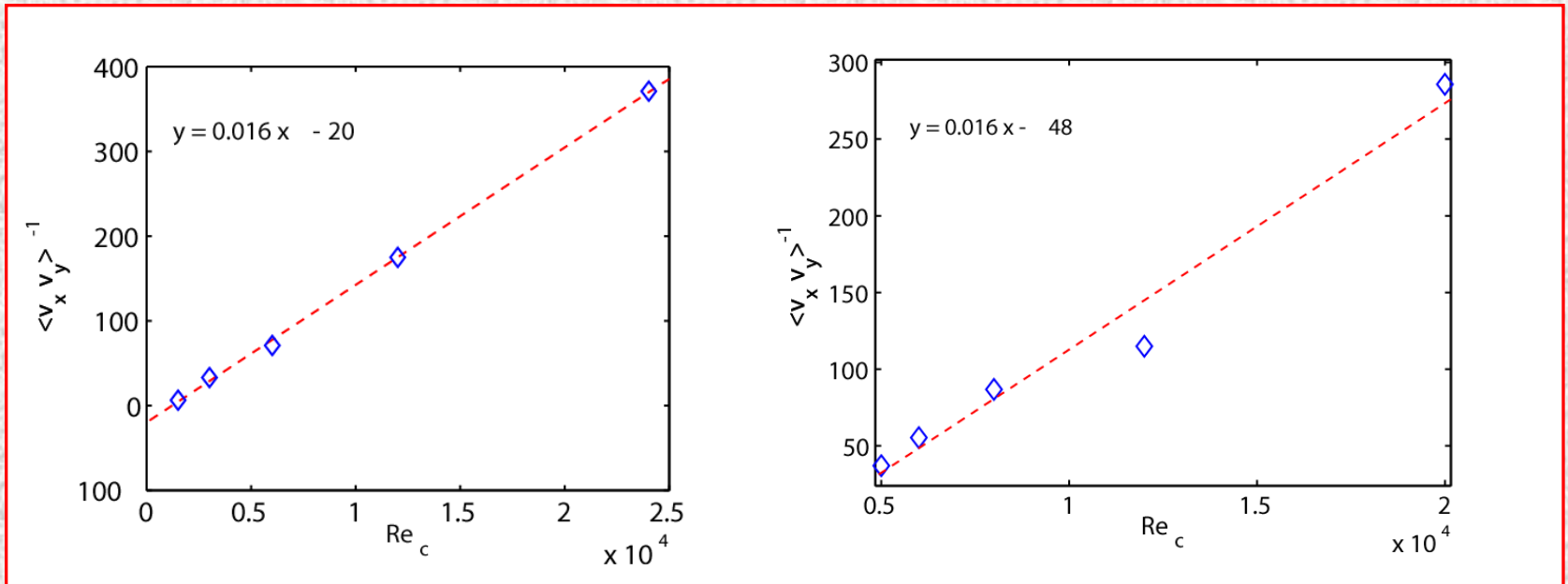
- Turbulence not quenched by a stabilizing Coriolis force
- Resolution demand increases extremely steeply with increasing Coriolis force for anticyclonic flows
- Keplerian regime out of reach

Simulations and experiments:



- **Cyclonic flows: little role of boundary conditions and aspect ratio**
- **Anticyclonic flows: experiments more easily perturbed by secondary flows (from stability criterion)**

Turbulent transport



- $\langle v_x v_y \rangle \sim 5 / Rg$ (both cyclonicities)
- Minimal extrapolation $\longrightarrow \alpha < 10^{-5}$

hydrodynamic subcritical turbulence not relevant to accretion disk transport

Conclusions

**Large resolution demand to simulate keplerian flows
flows (1.000^3 to 10.000^3)**

**Coriolis force does not quench turbulence in linearly
linearly stable flows but efficiently reduces
turbulent transport**

**Transport orders of magnitude too small for
astrophysical purposes**