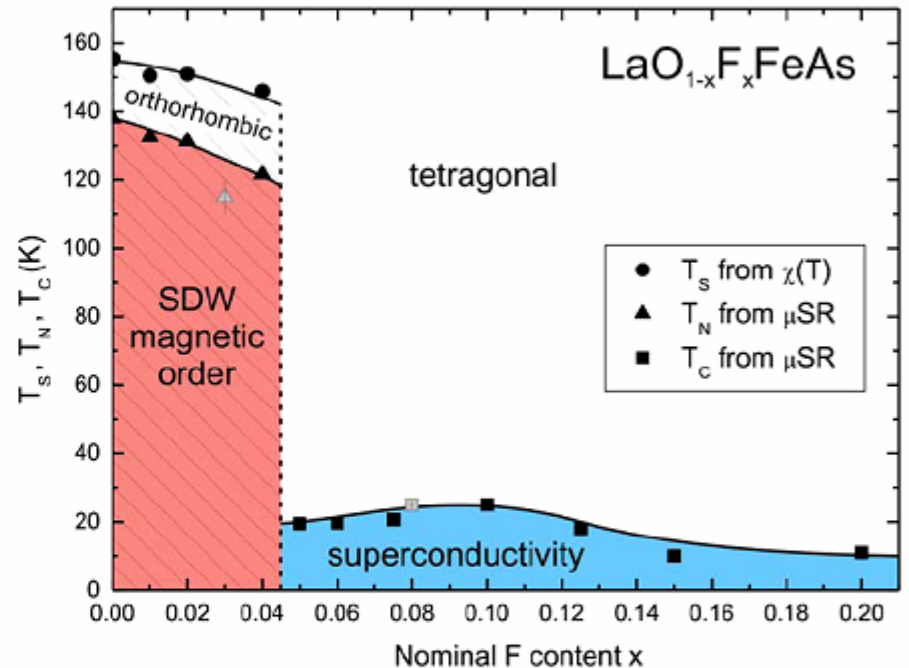
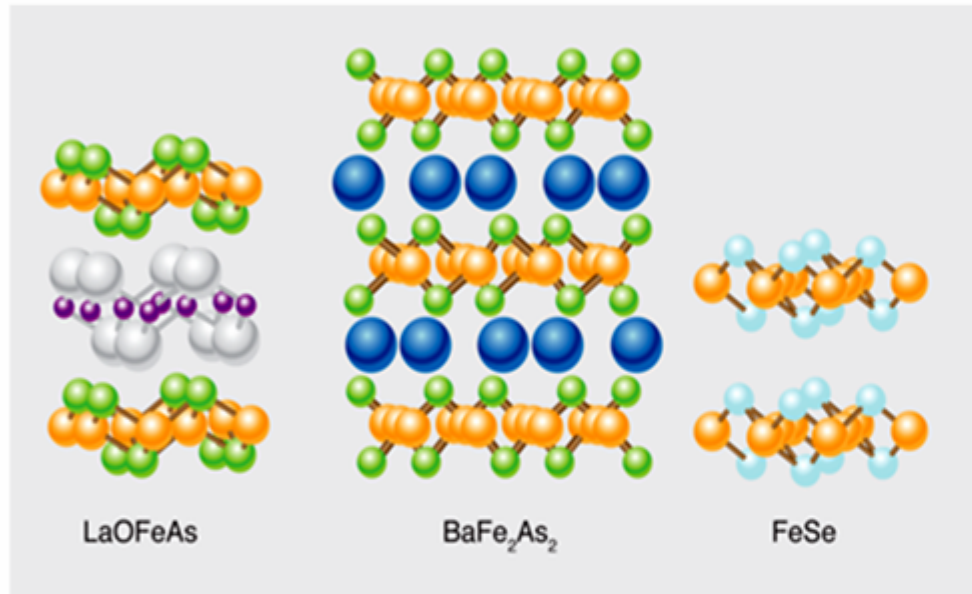


Explaining the band structure and itinerant magnetism of **iron-arsenide** superconductors

**Lilia Boeri, Alexander Yaresko,
and O. K. Andersen**

*Max-Planck-Institute for Solid-State Research,
Stuttgart*

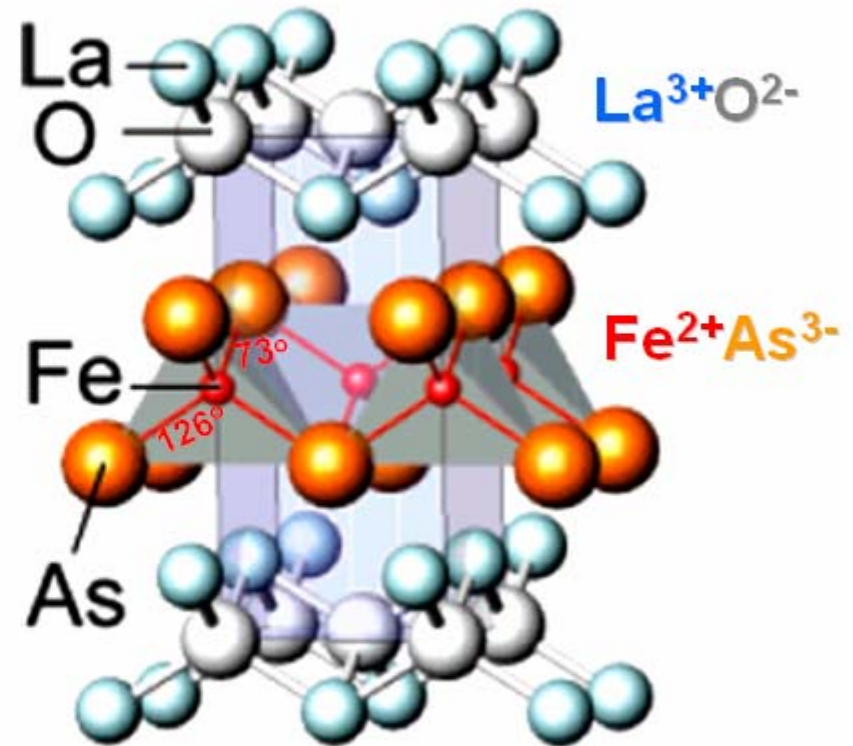
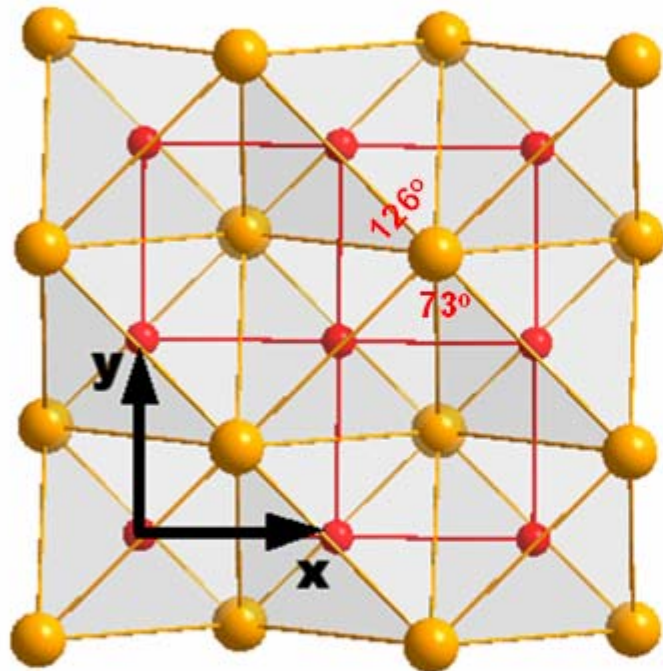
Superconductivity in F-doped iron pnictides (d^6) was discovered early in 2008. Within a few months, T_c was increased from 26 K in LaOFeAs to 55 K in SmOFeAs. In addition to the LnOFeAs compounds, $A_{1/2}$ FeAs, and Fe_{1+x} Se superconducting compounds have been found.



The superconductivity seems to be unconventional ($s_{+/-}$, d , $s+id$) since the calculated electron-phonon interaction is weak (Boeri: $\lambda \sim 0.2$) and the parent compound displays a transition to a striped AFM state, with a small moment $m \sim 0.3 \mu_B$ in LnOFeAs and $\sim 0.9 \mu_B$ in Ba_{1/2}FeAs.

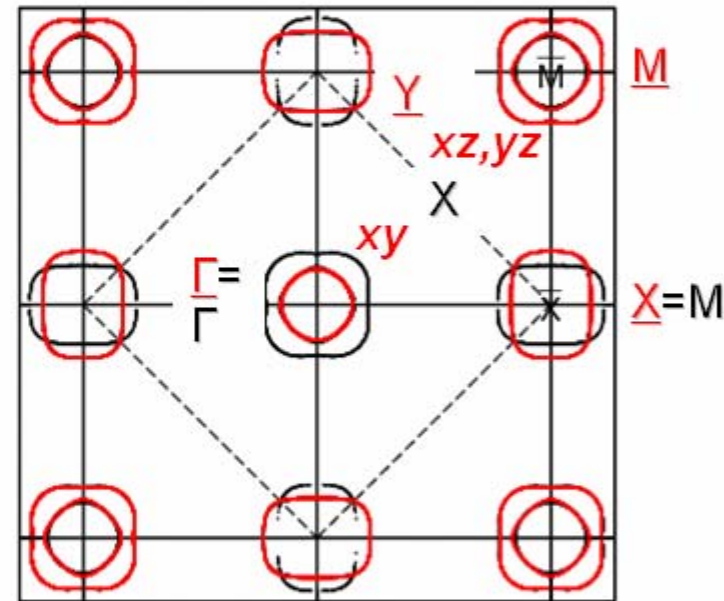
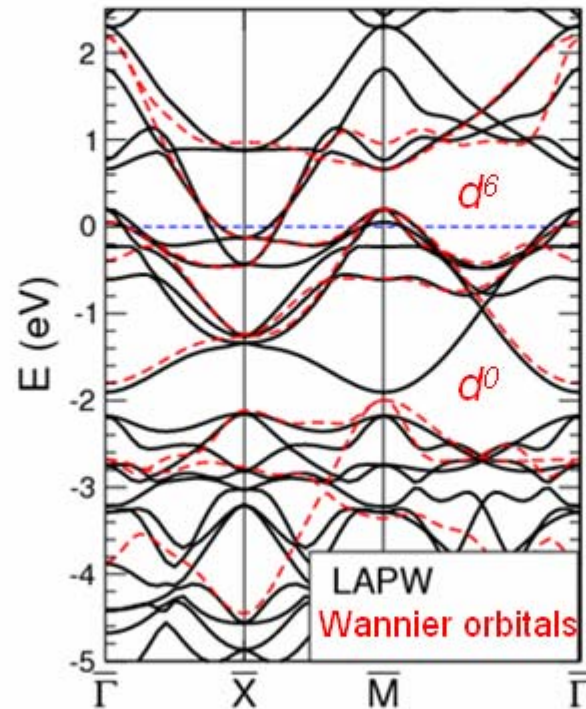
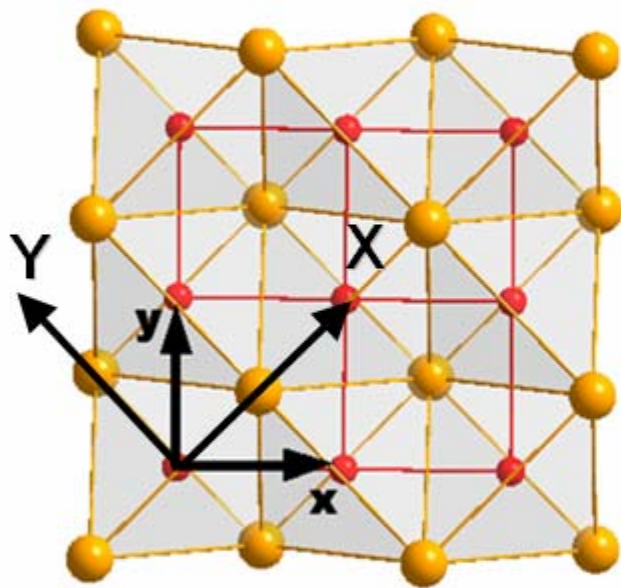
The common motive is square **Fe** lattice with **As** atoms placed alternately above and below the centers of the squares.

The FeAs_4 tetrahedron is squeezed.



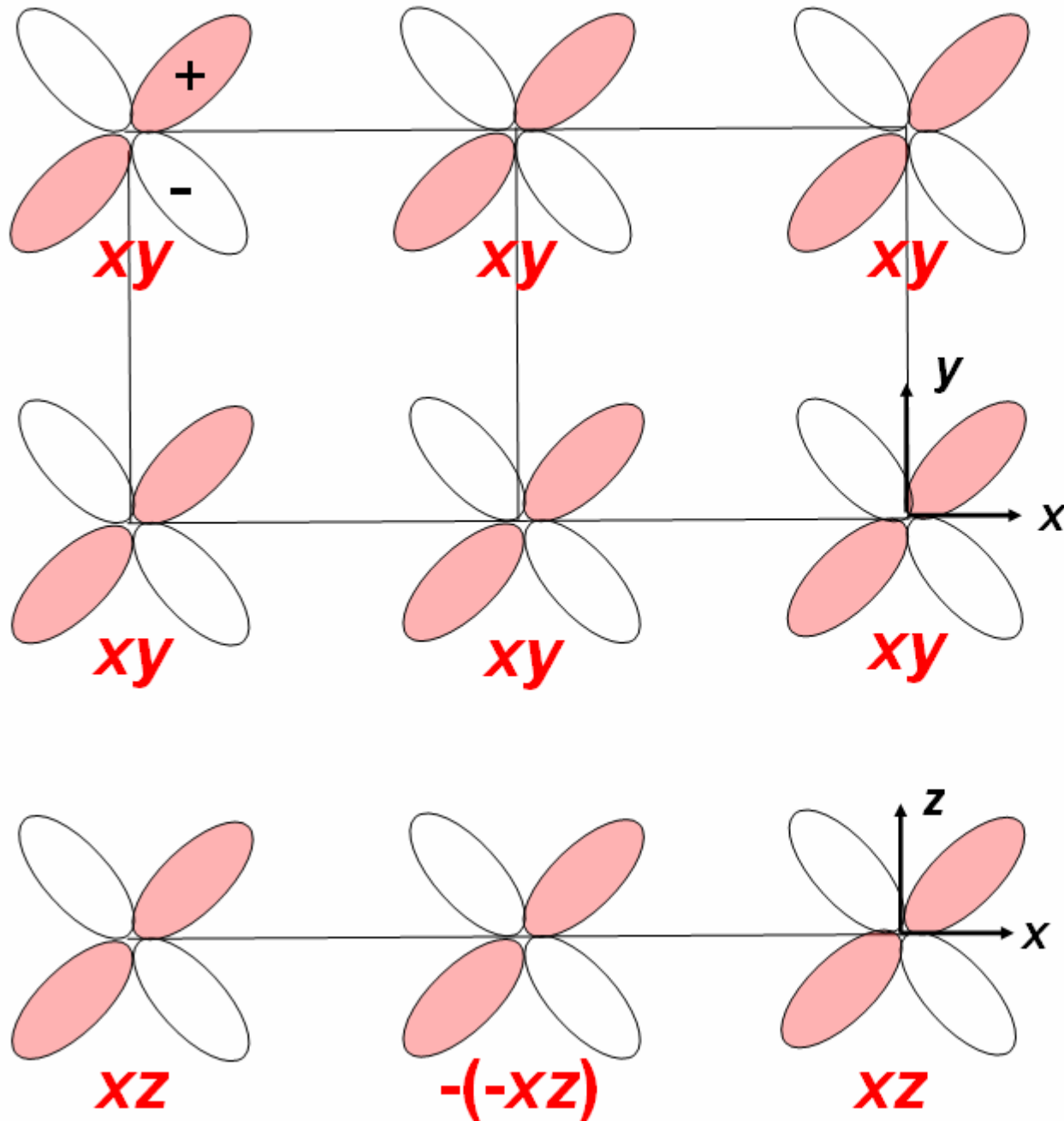
The physical properties and even the basic electronic structure of these materials are not well understood. In contrast to the cuprates, the Fe compounds are always metals, the electronic correlations seem to be weak, the magnetism itinerant, and the LSDA seems to work.

Published band structures are complicated. Even without magnetism they have 2×5 d bands and 2×3 p bands in the Fe_2As_2 translational cell. We simplify them by using the space group generated by a primitive translation of the square lattice *followed by mirroring* in the Fe plane. This reduces the formula unit to FeAs and makes the 2D Brillouin zone identical to the one used for the cuprate superconductors. Below we show the **unfolding** (red) of the LAPW bands (black) and Fermi surface.



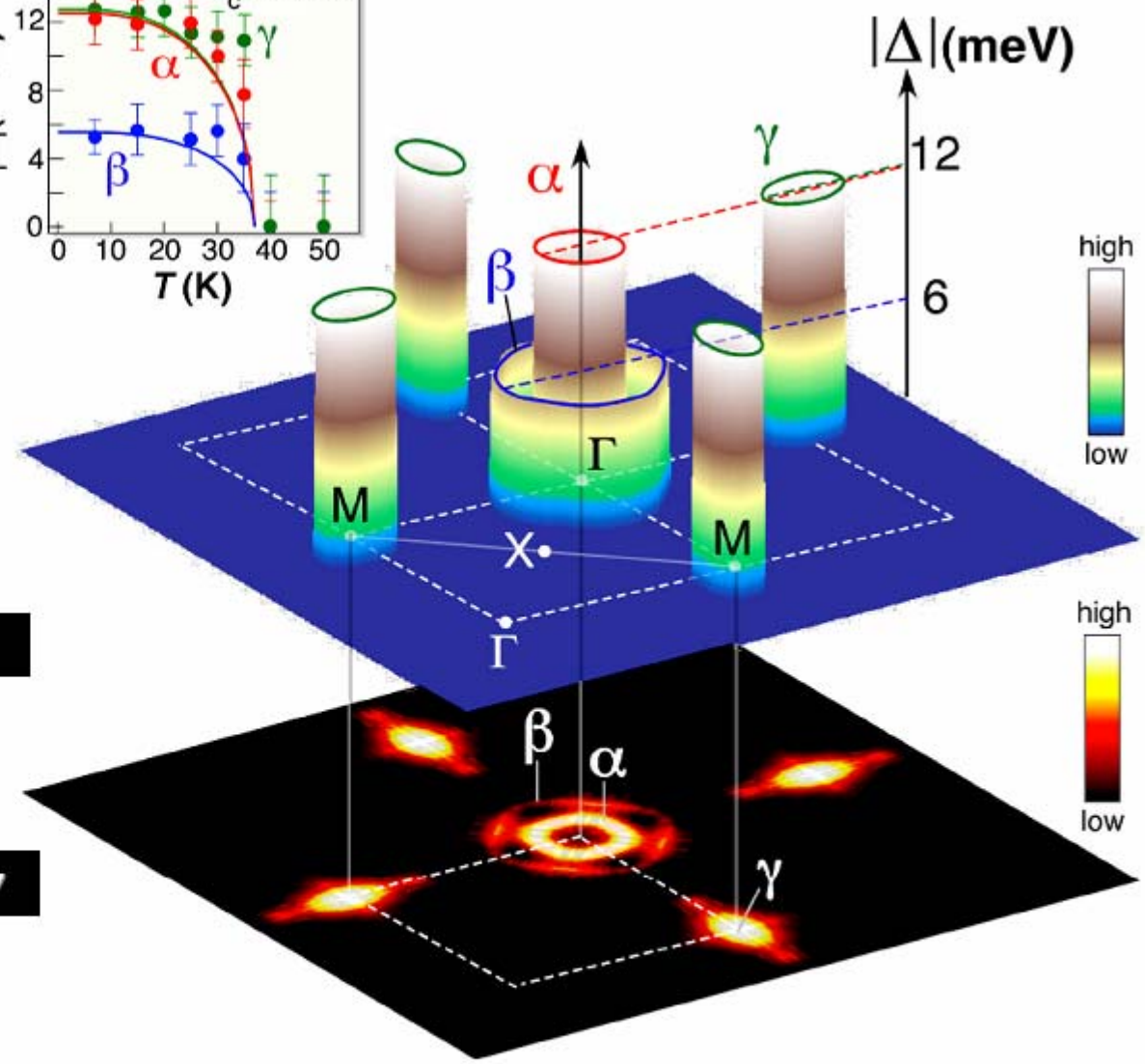
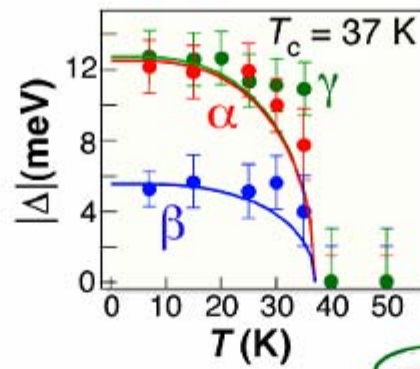
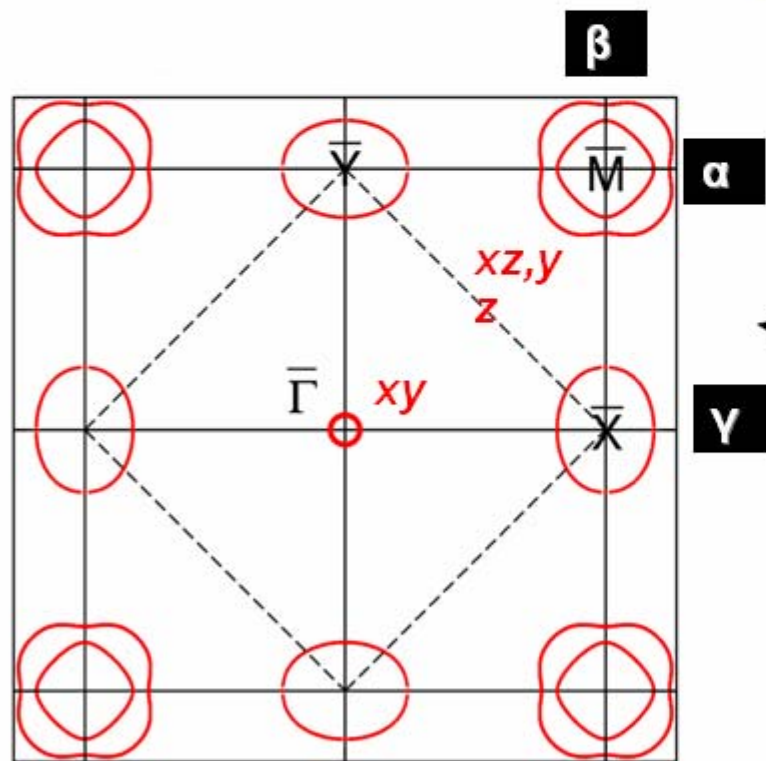
We have derived a generally applicable (e.g. for studies of magnetism and superconductivity) and accurate tight-binding (TB) model describing the LDA single-particle wavefunctions of the bands near the Fermi level in terms of the 3 As p and 5 Fe d Wannier orbitals by means of downfolding plus N-ization (NMTO).

Positions of the hole pockets in the large BZ:



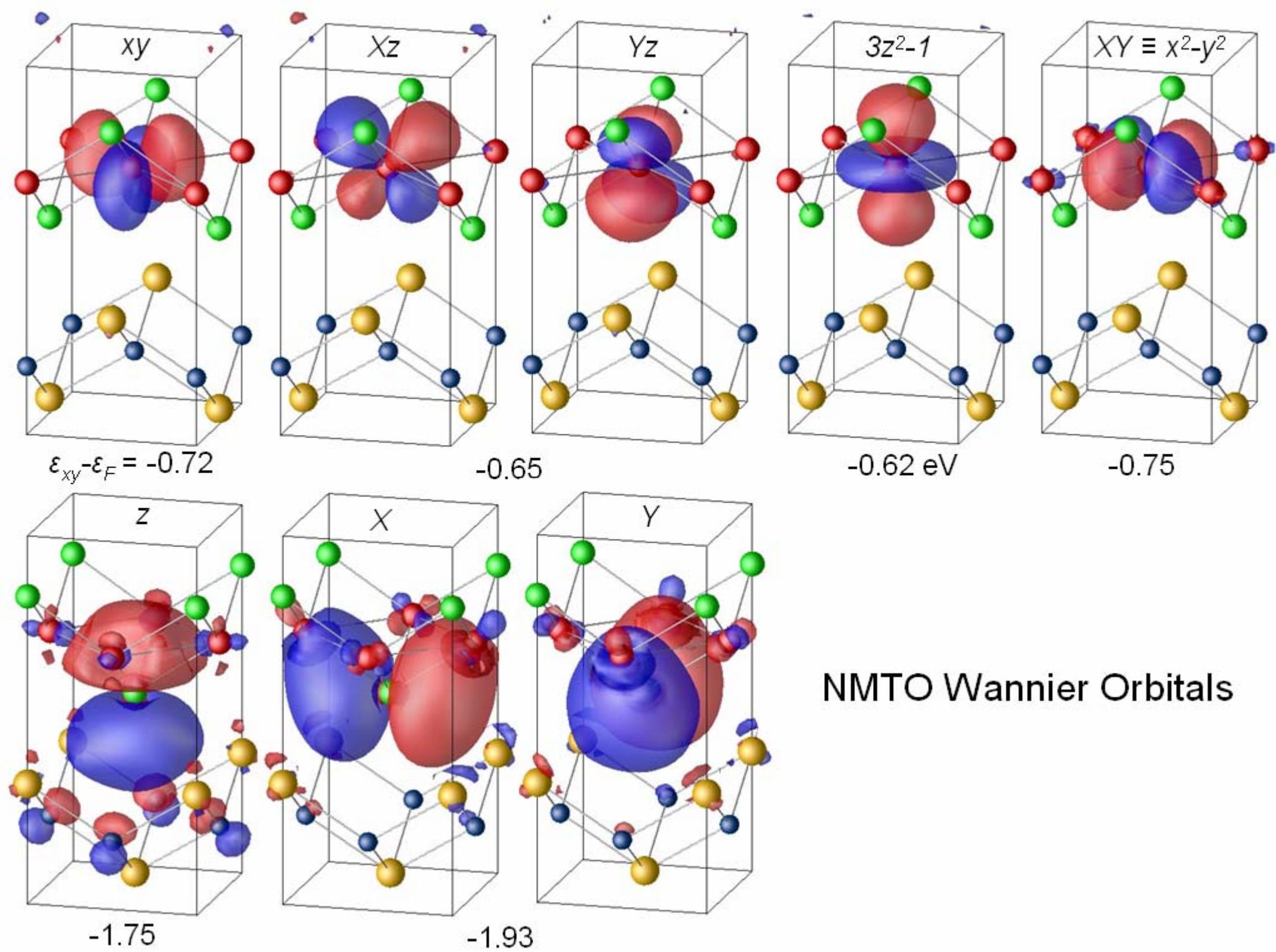
At $\mathbf{k} = (0, 0)$ the **Fe xy** Blochwave is anti-bonding, i.e. the **xy** band has its **top at Γ** .

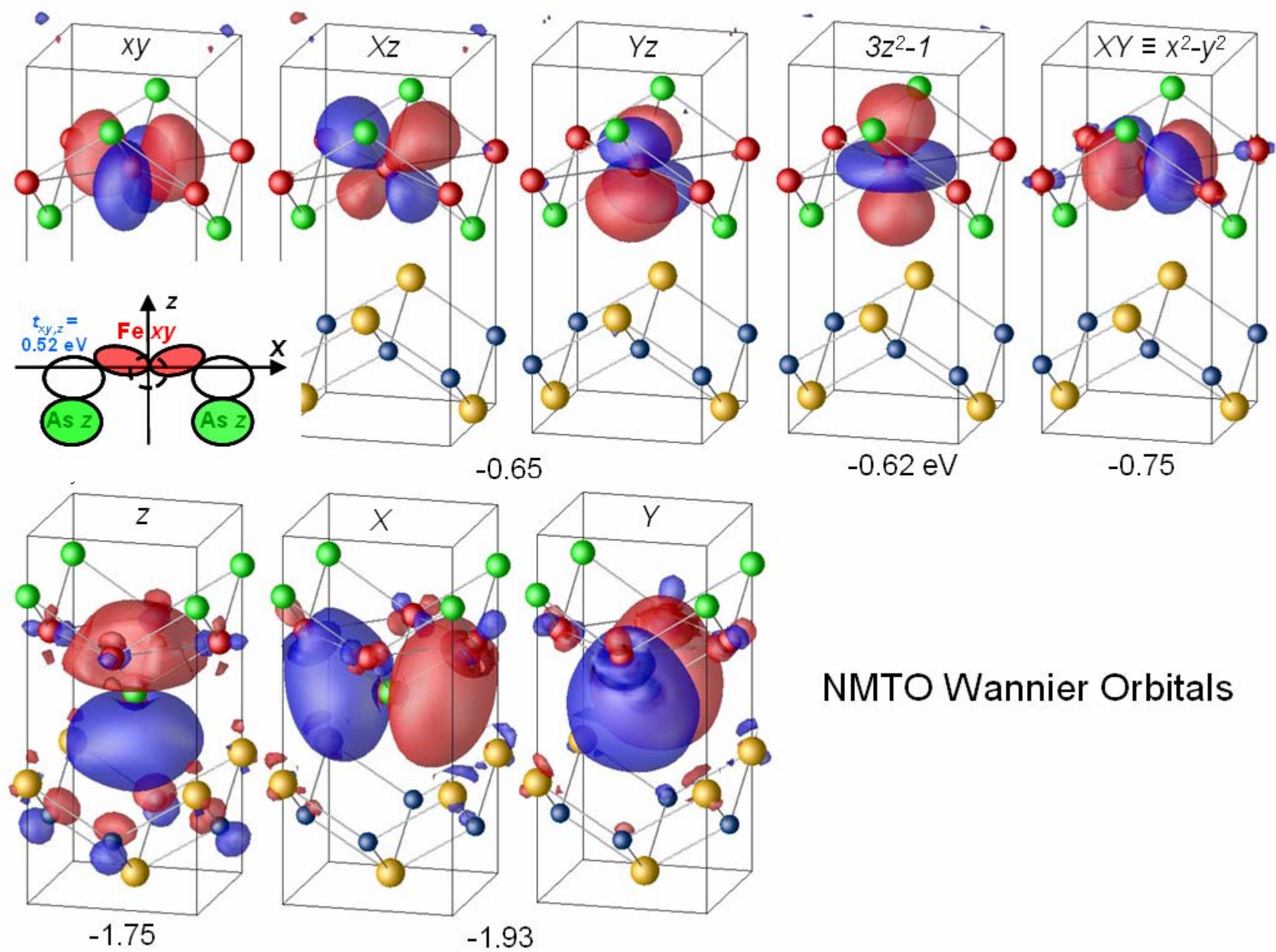
At $\mathbf{k} = (\pi, \pi)$ the **Fe xz** Blochwave is anti-bonding, i.e. the **xz** band has its **top at \underline{M}** .

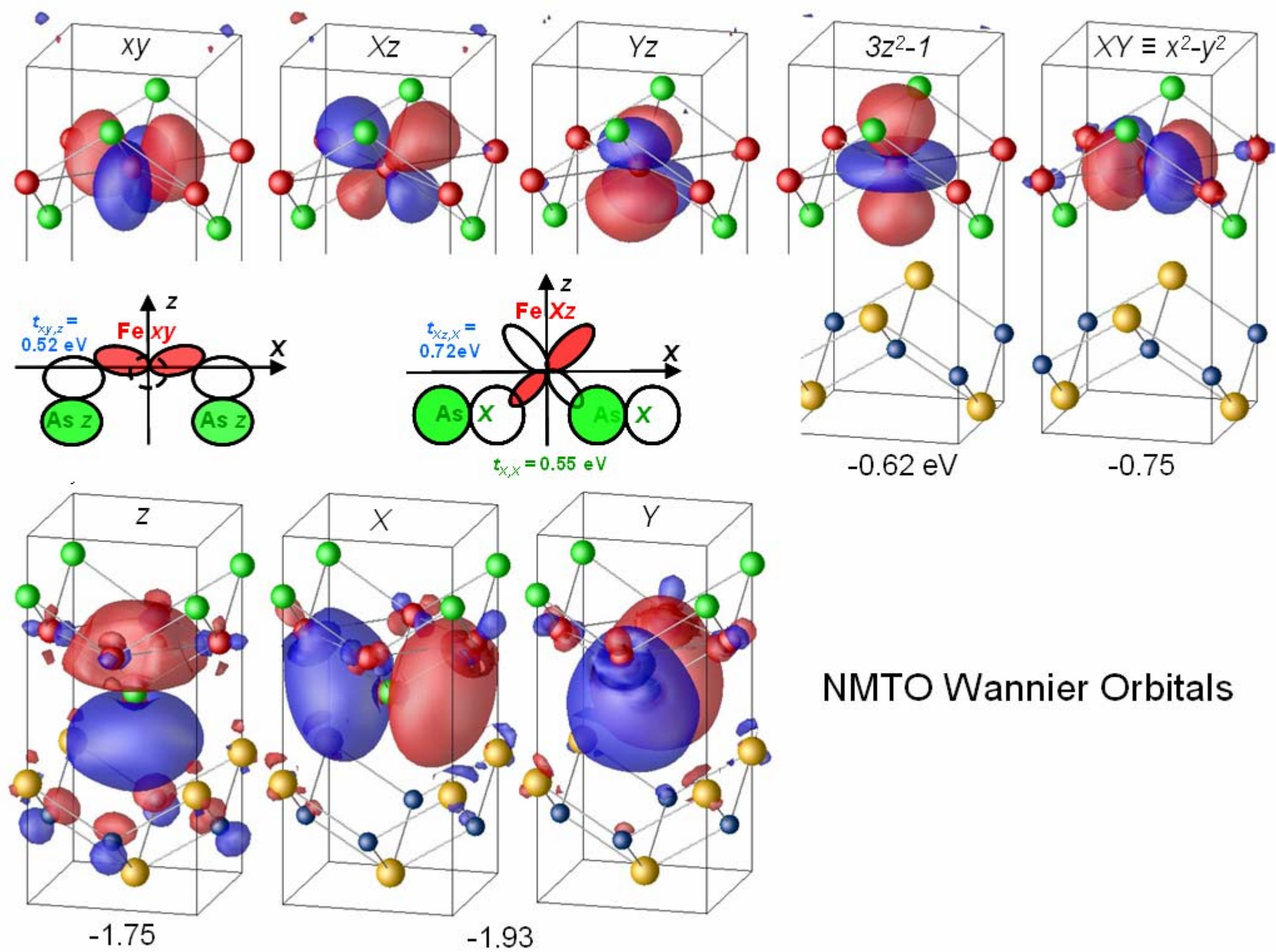


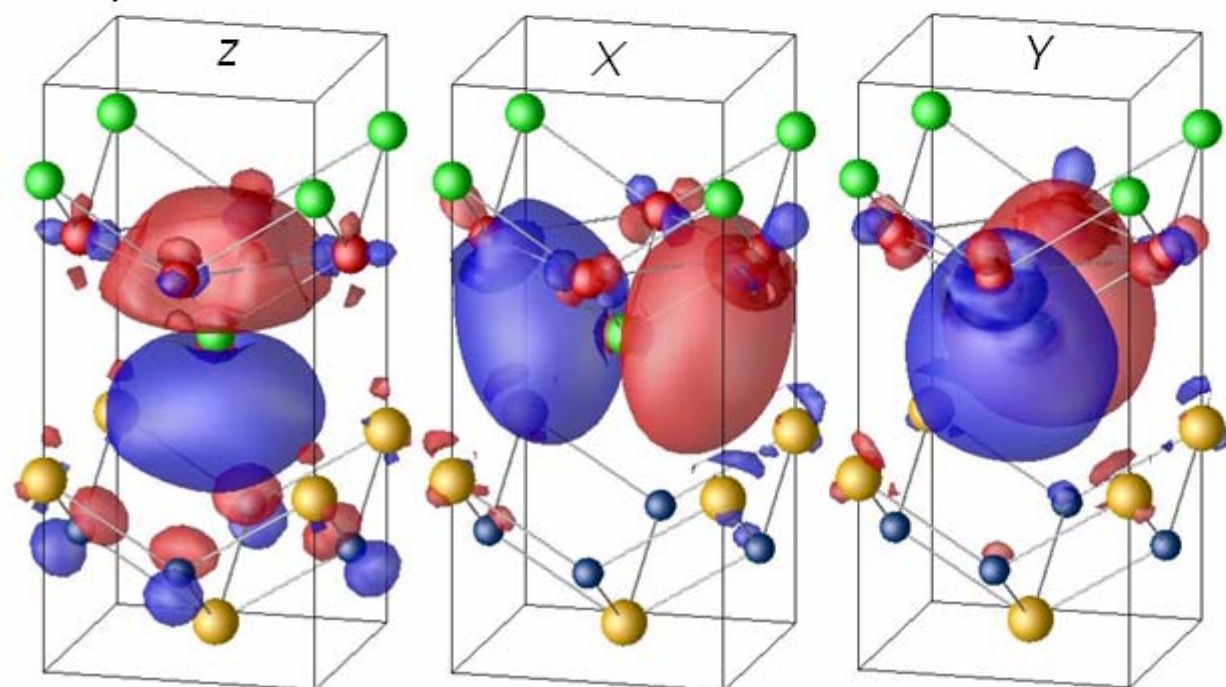
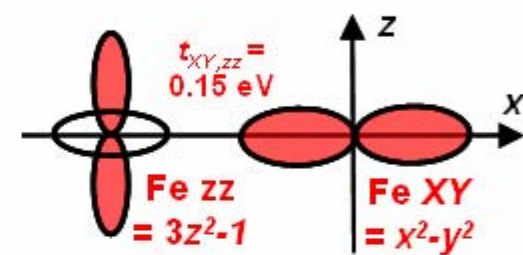
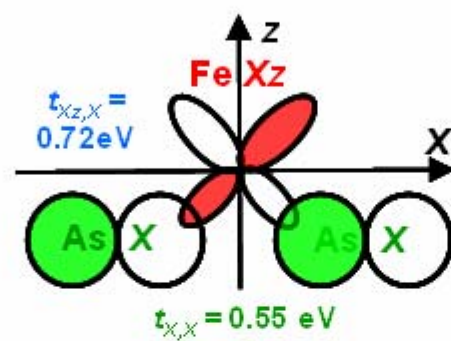
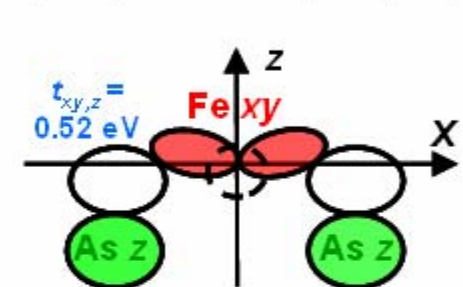
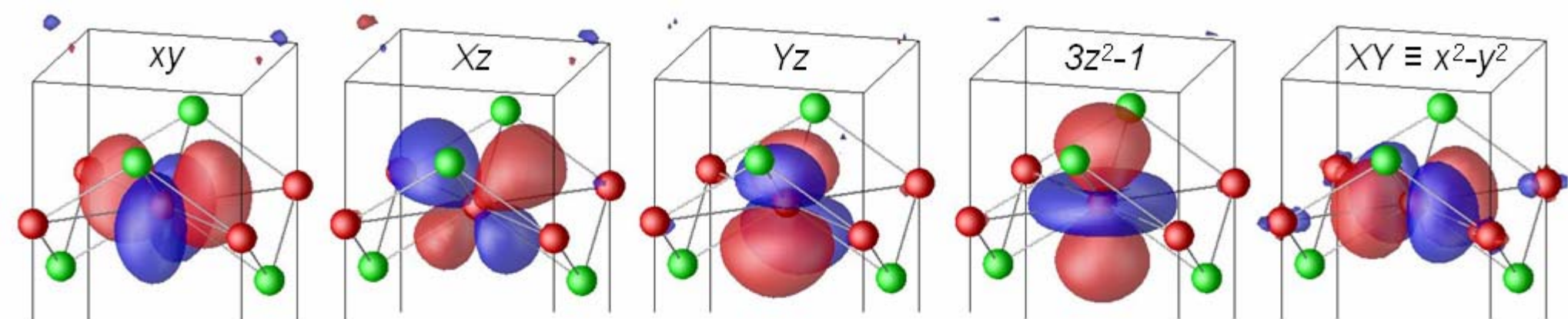
Observation of Fermi-surface-dependent nodeless superconducting gaps in $\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$

H. Ding¹, P. Richard², K. Nakayama³, T. Sugawara³, T. Arakane³, Y. Sekiba³,
 A. Takayama³, S. Souma², T. Sato³, T. Takahashi^{2,3}, Z. Wang⁴, X. Dai¹, Z. Fang¹,
 G. F. Chen¹, J. L. Luo¹, and N. L. Wang¹





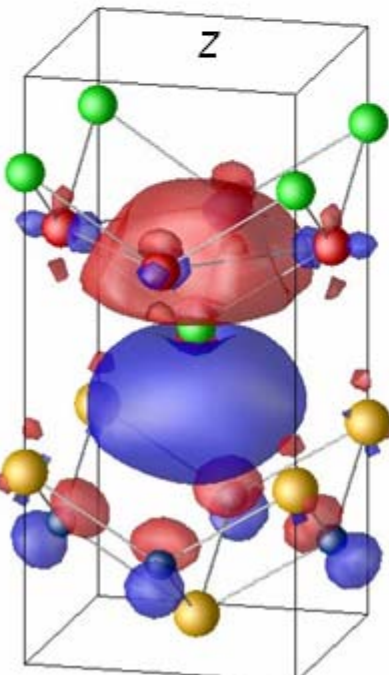
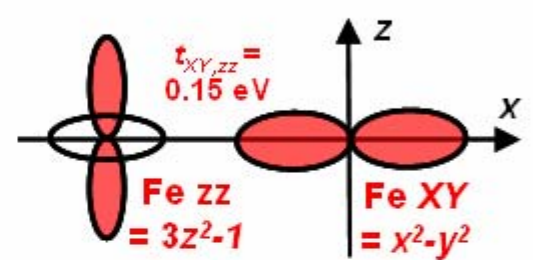
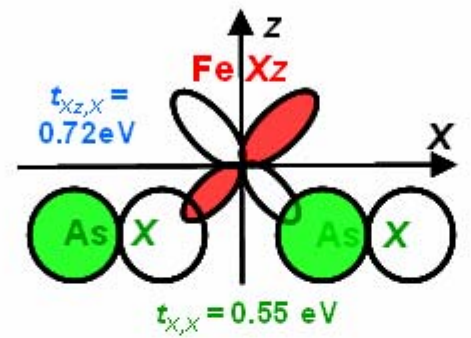
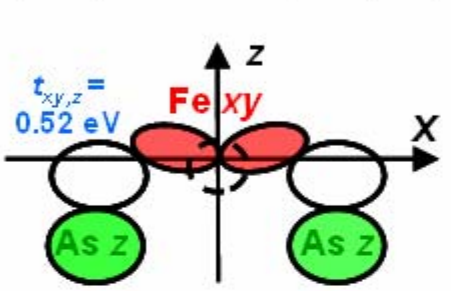
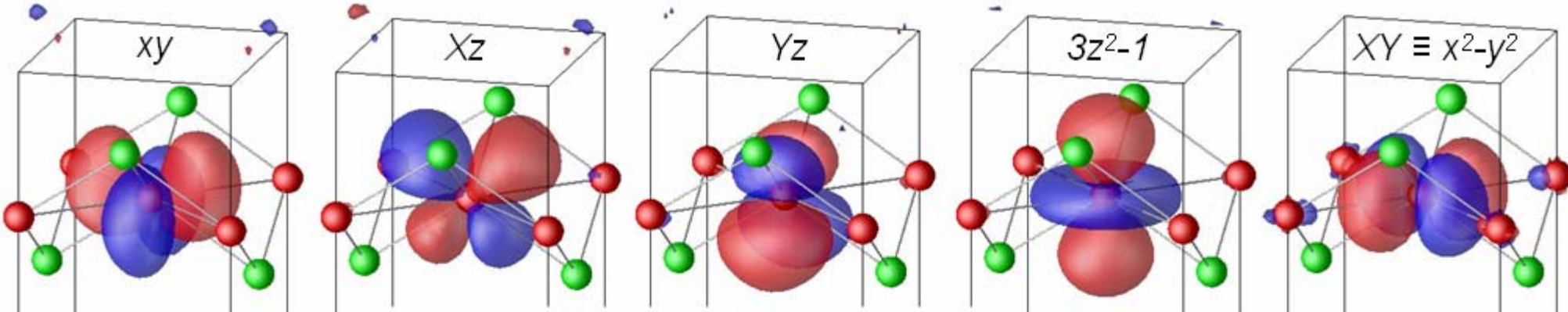




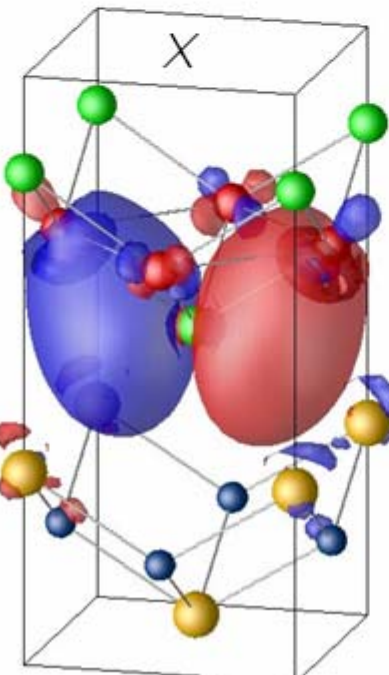
-1.75

-1.93

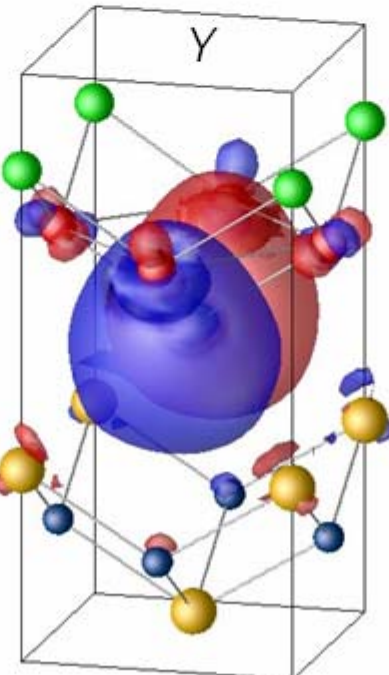
NMTO Wannier Orbitals



-1.75

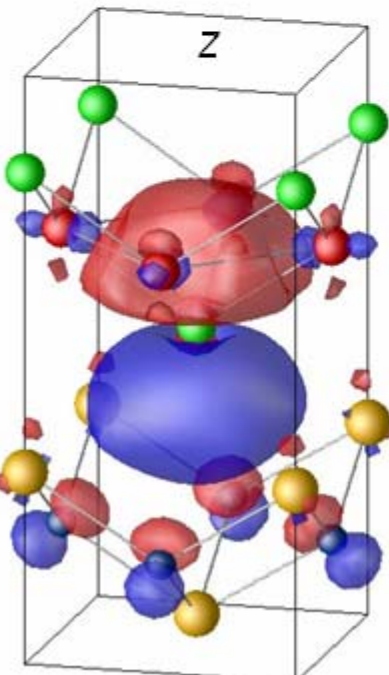
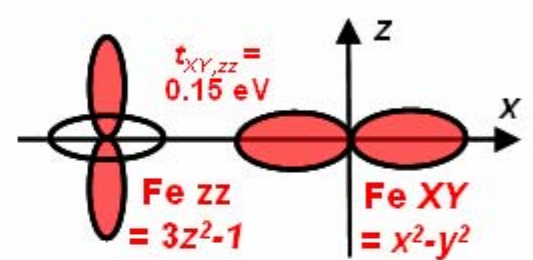
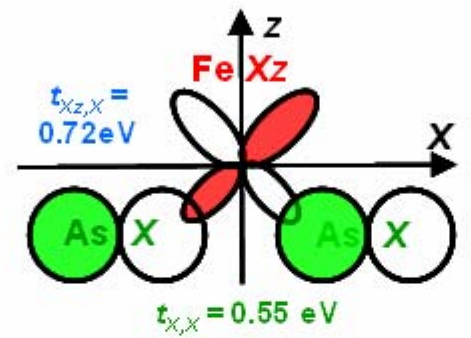
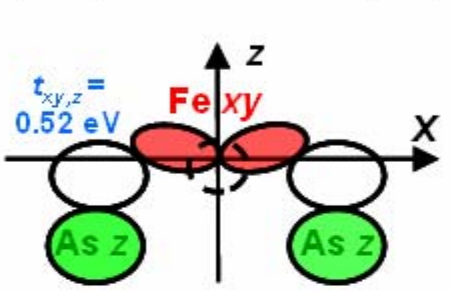
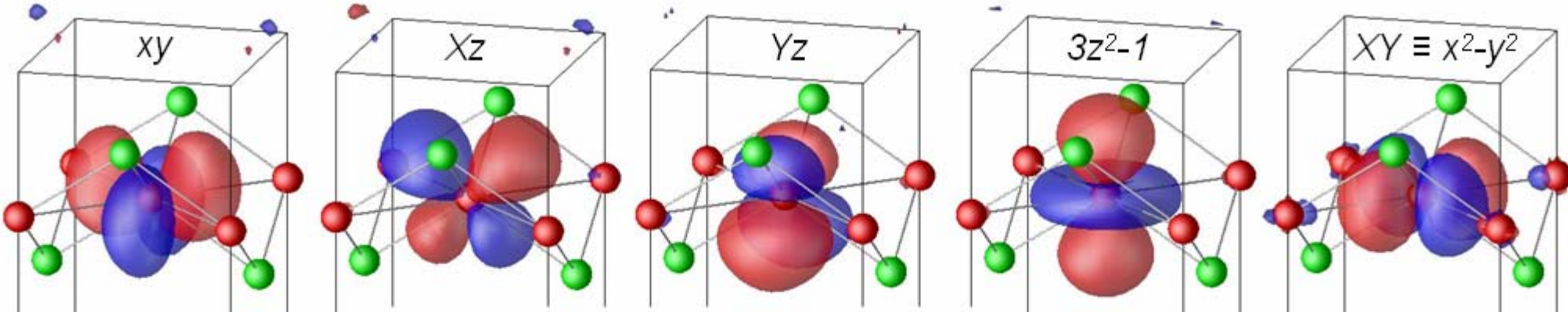


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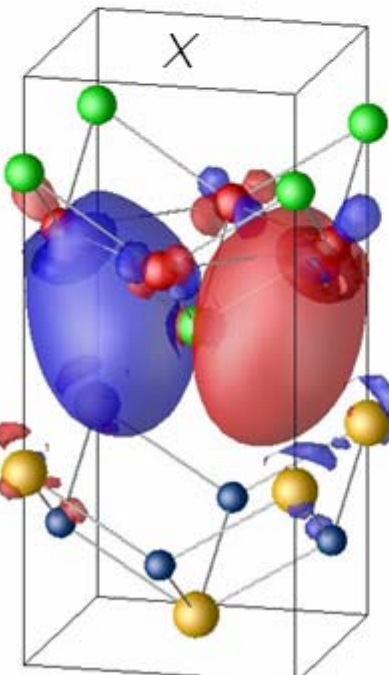


NMTO Wannier Orbitals

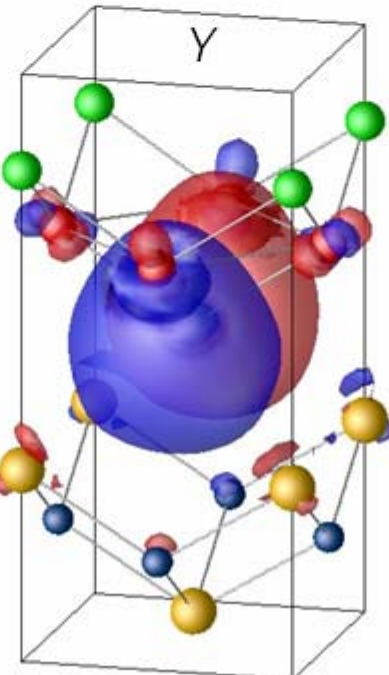
Hopping ranges are long due to incomplete covalent pairing of orbitals, i.e. the bonding is partly covalent and partly metallic.



-1.75



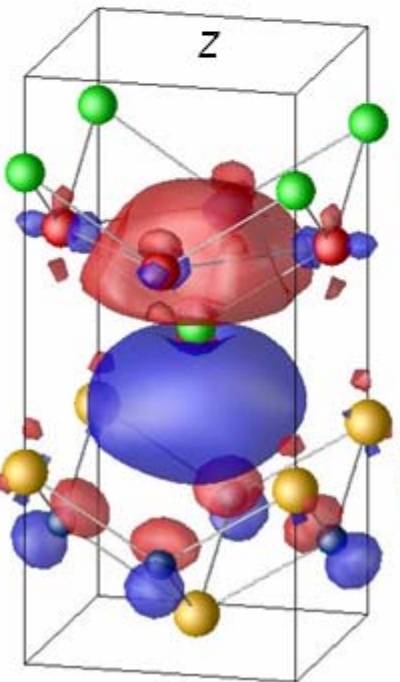
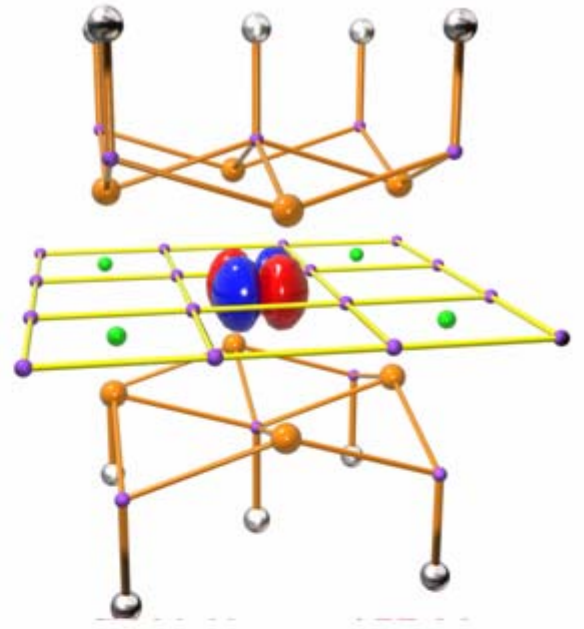
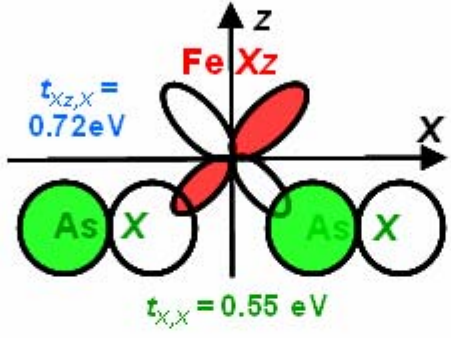
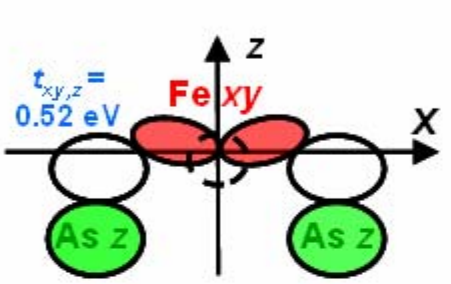
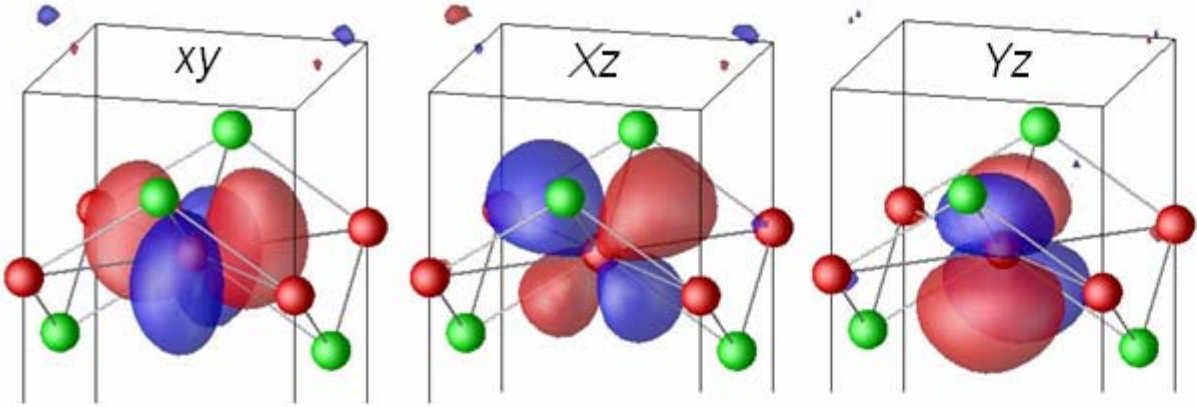
-1.93



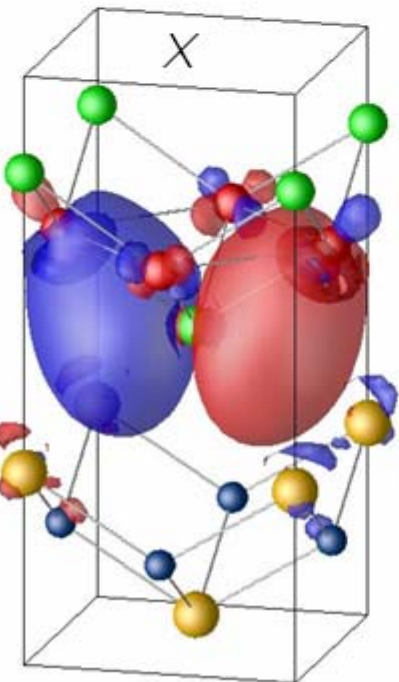
NMTO Wannier Orbitals

Hopping ranges are long due to incomplete covalent pairing of orbitals, i.e. the bonding is partly covalent and partly metallic.

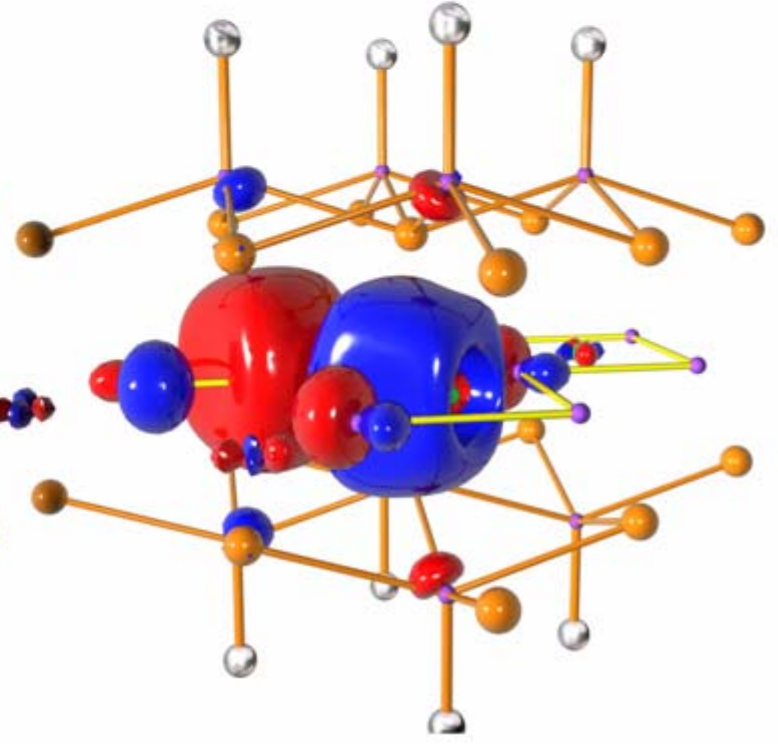
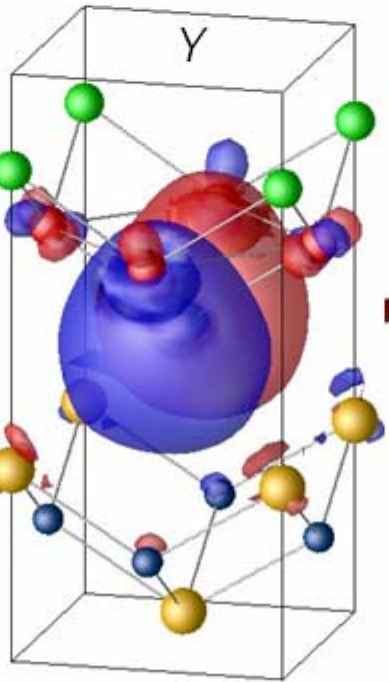
Cuprates have $pd\sigma$ geometry and d^9



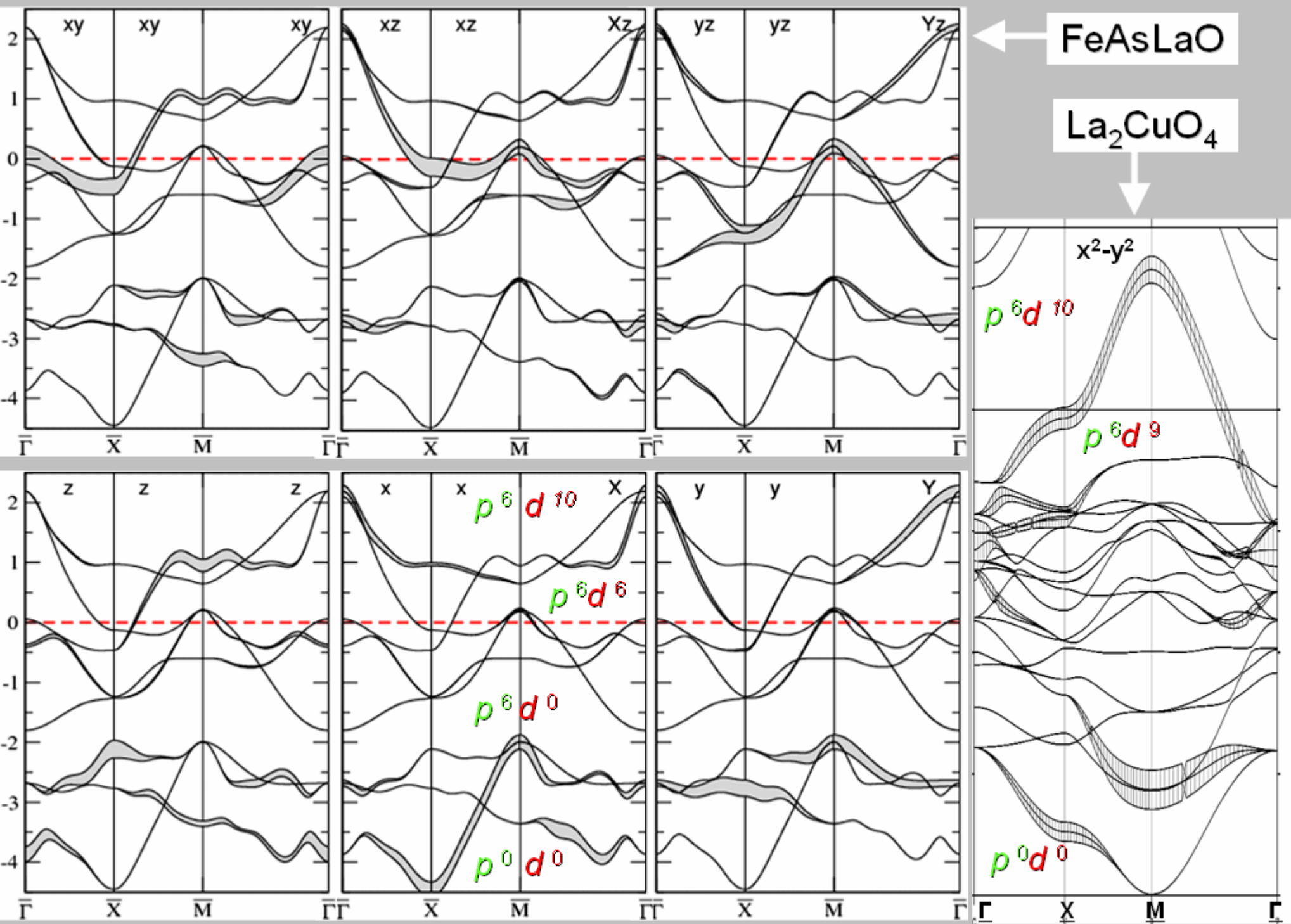
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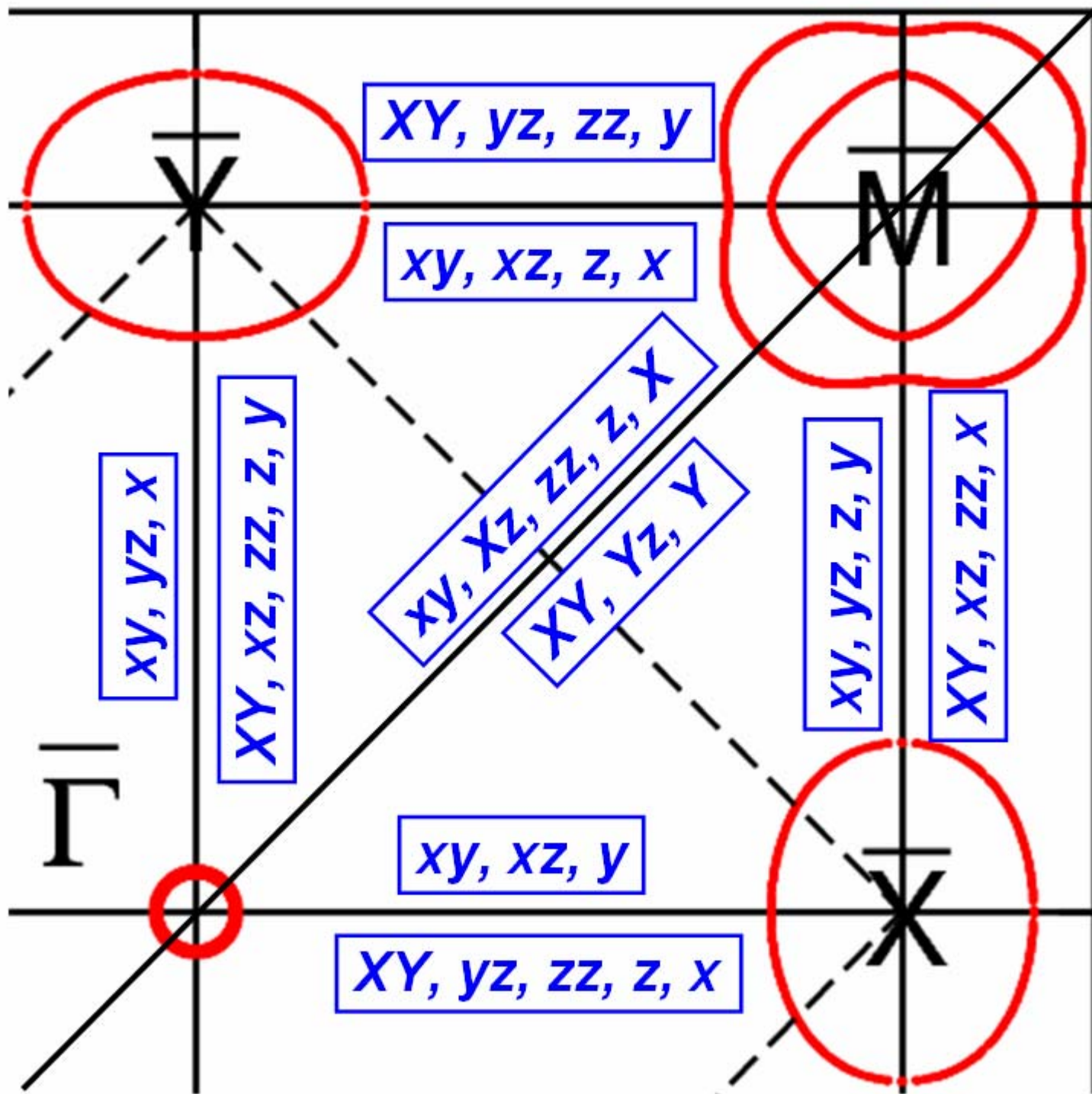


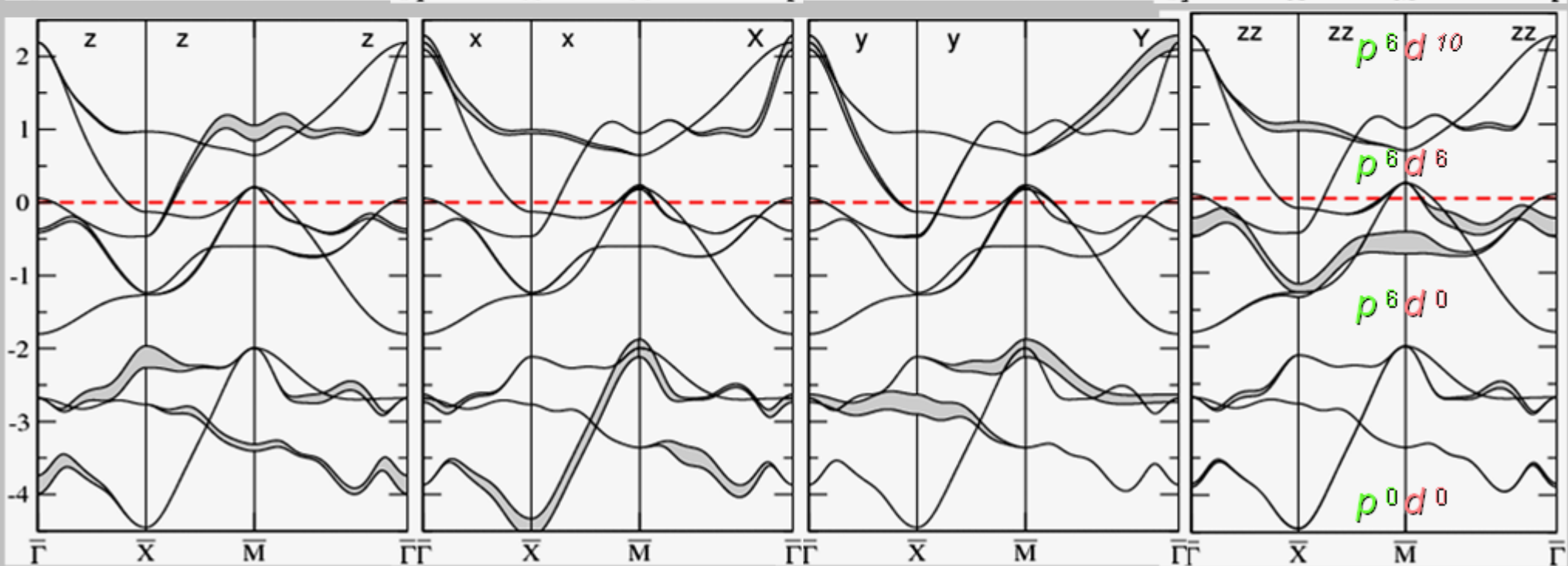
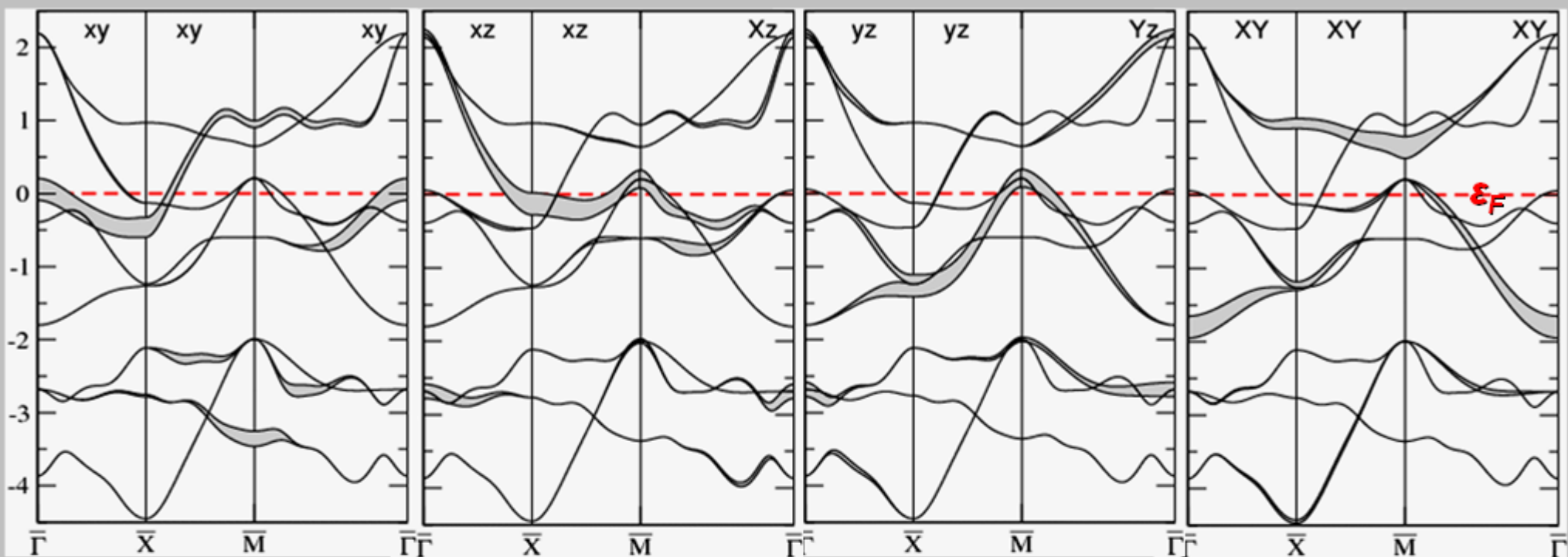
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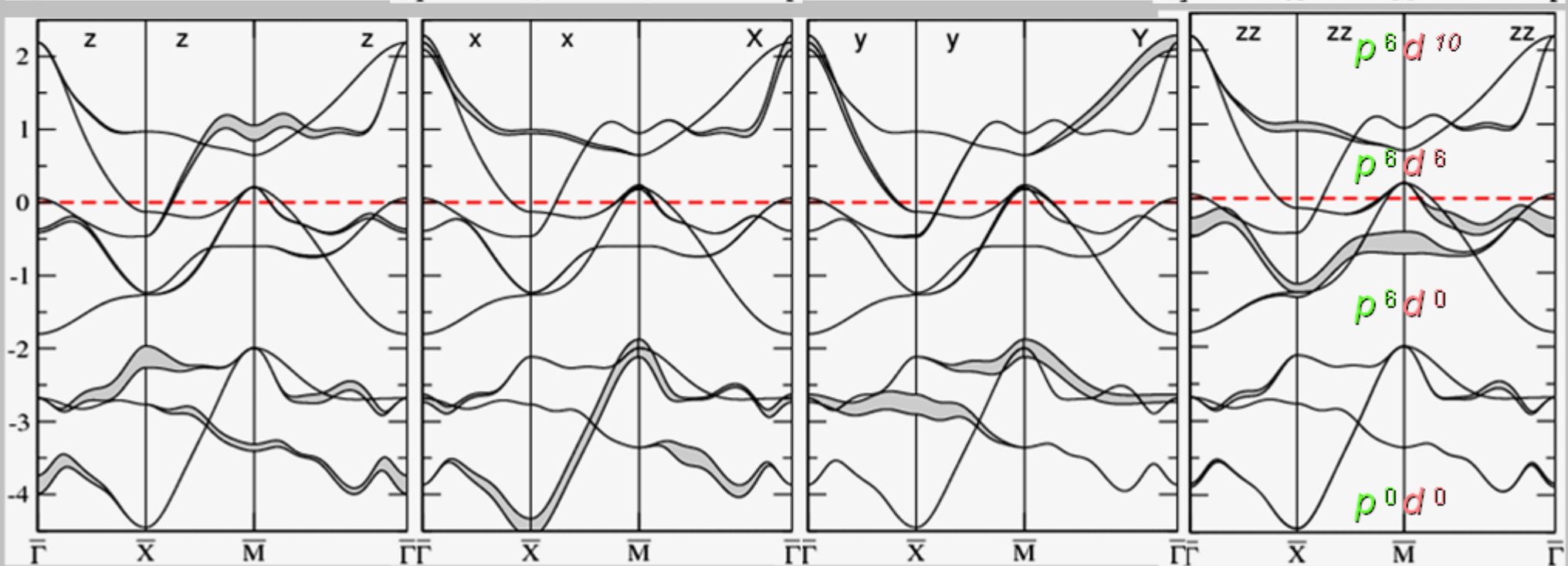
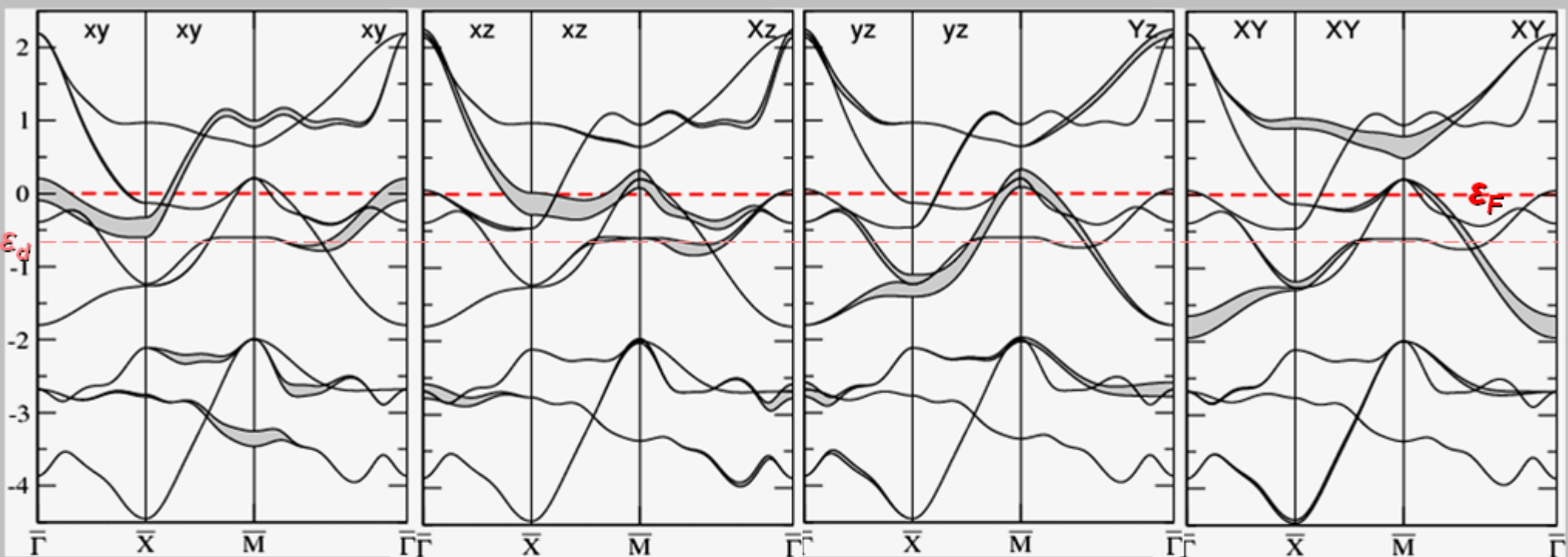


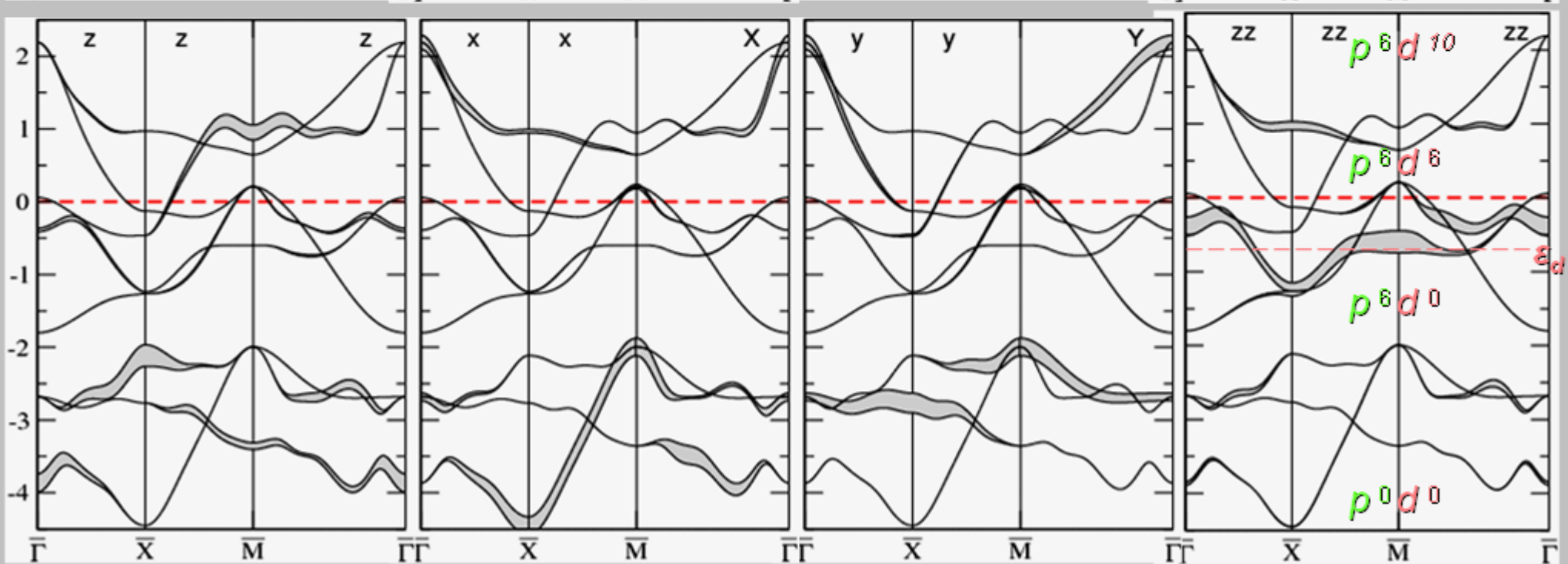
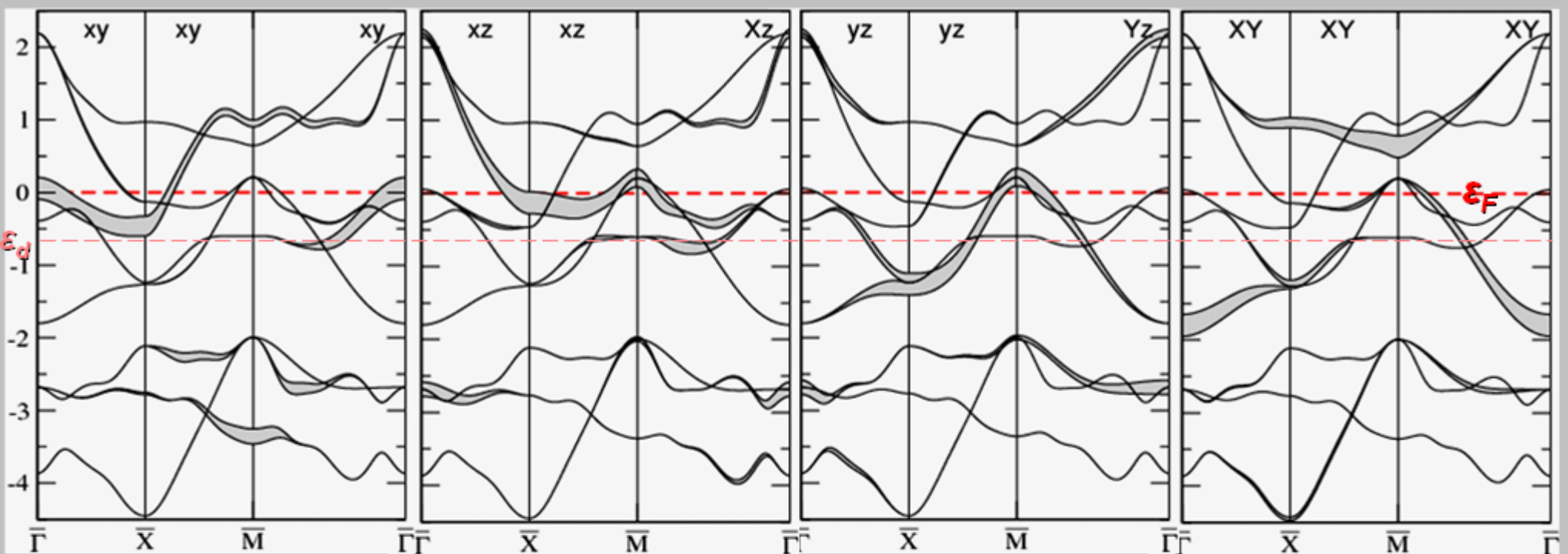
Cuprates have $pd\sigma$ geometry and d^9

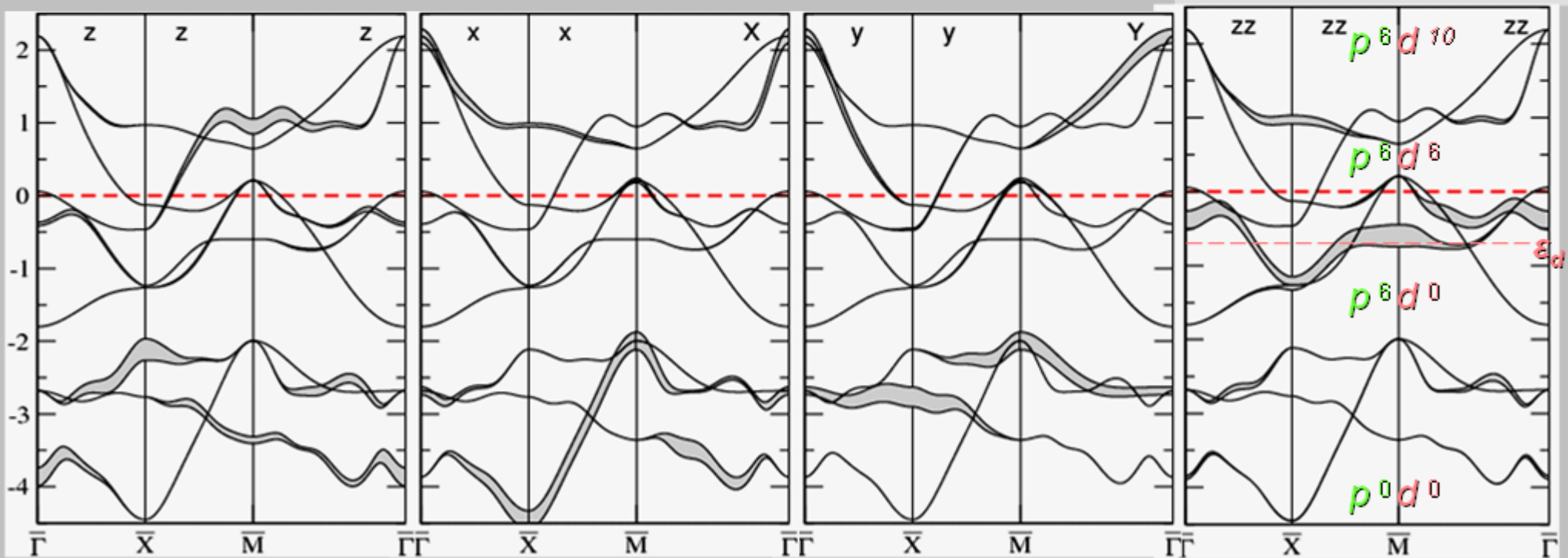
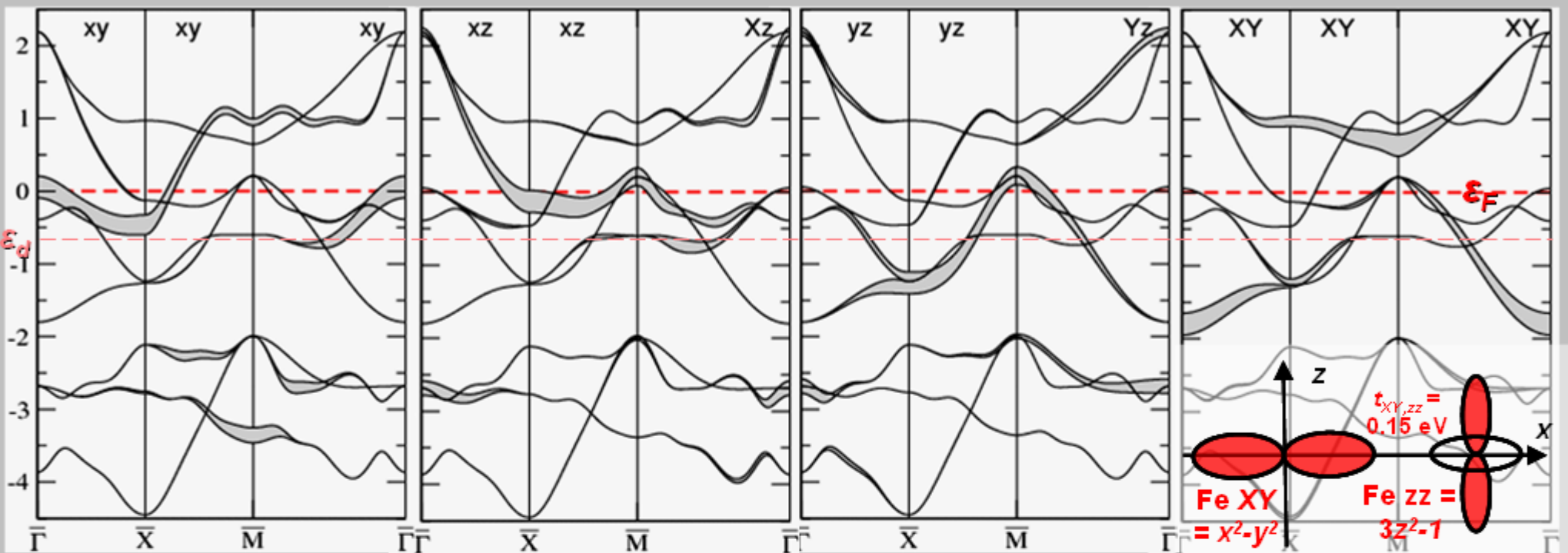


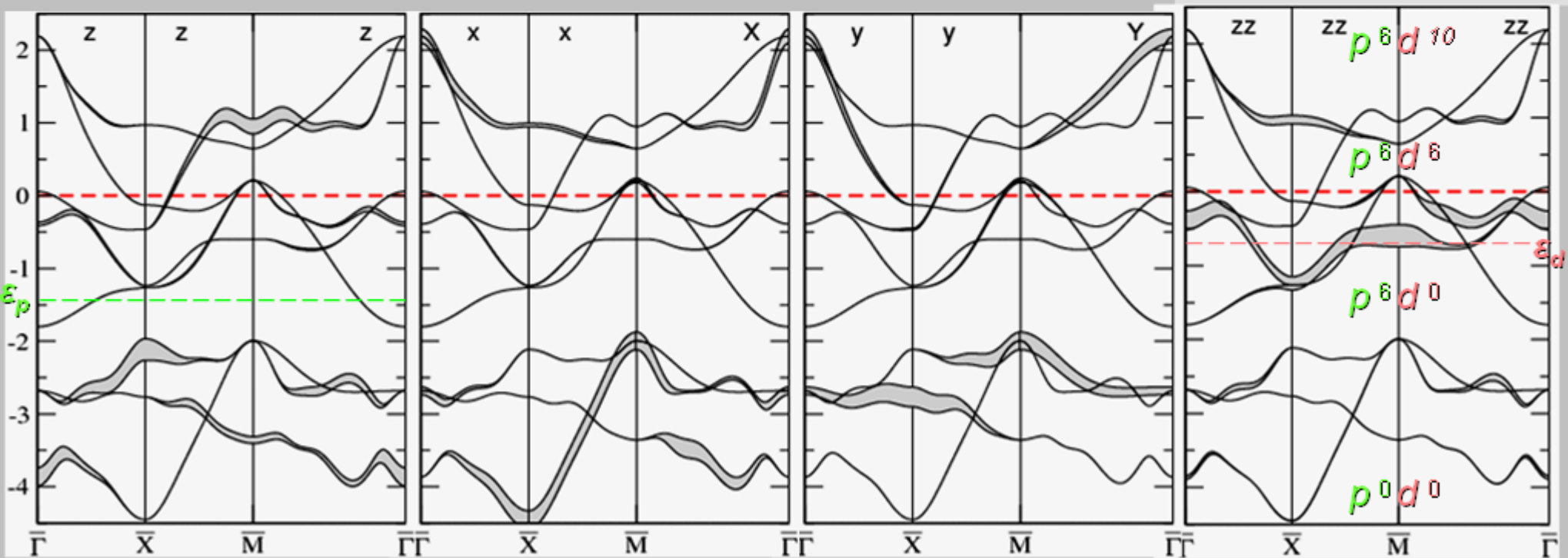
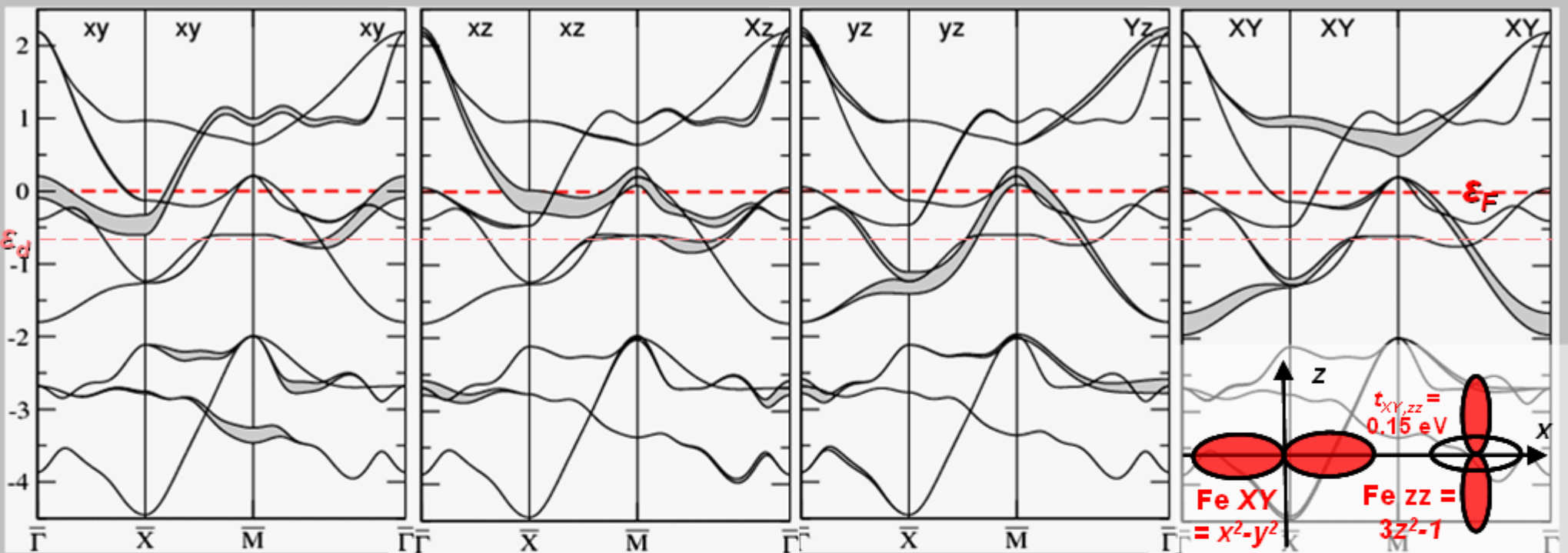


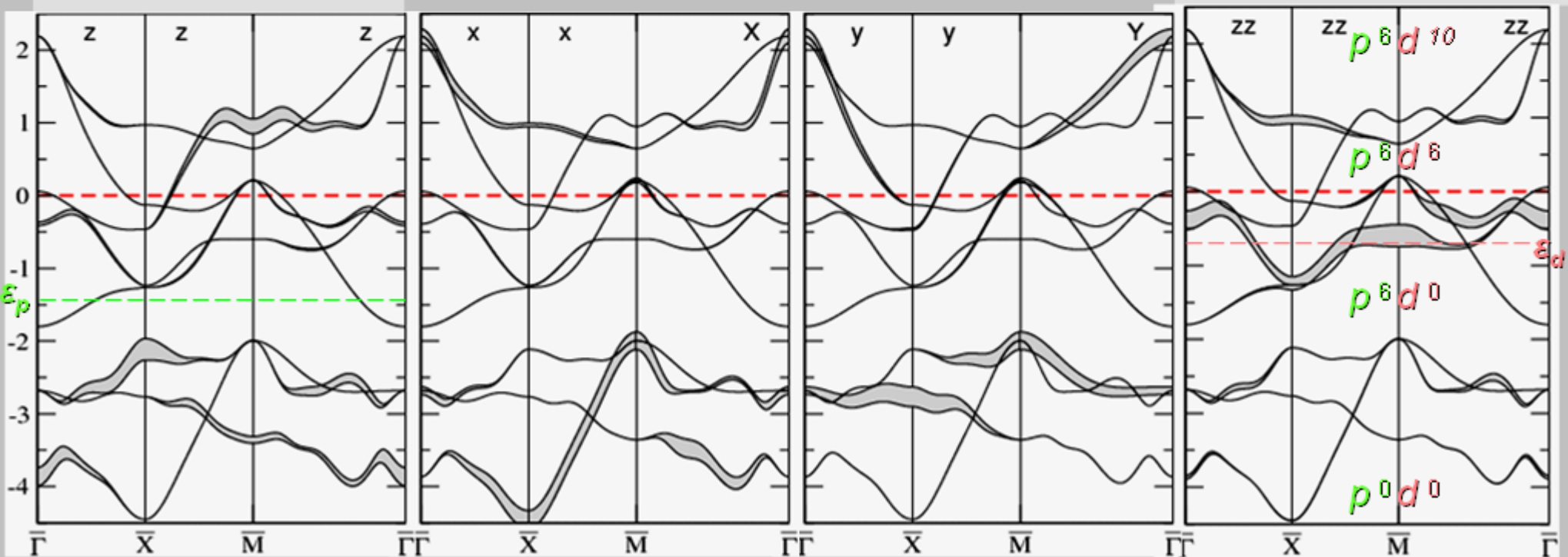
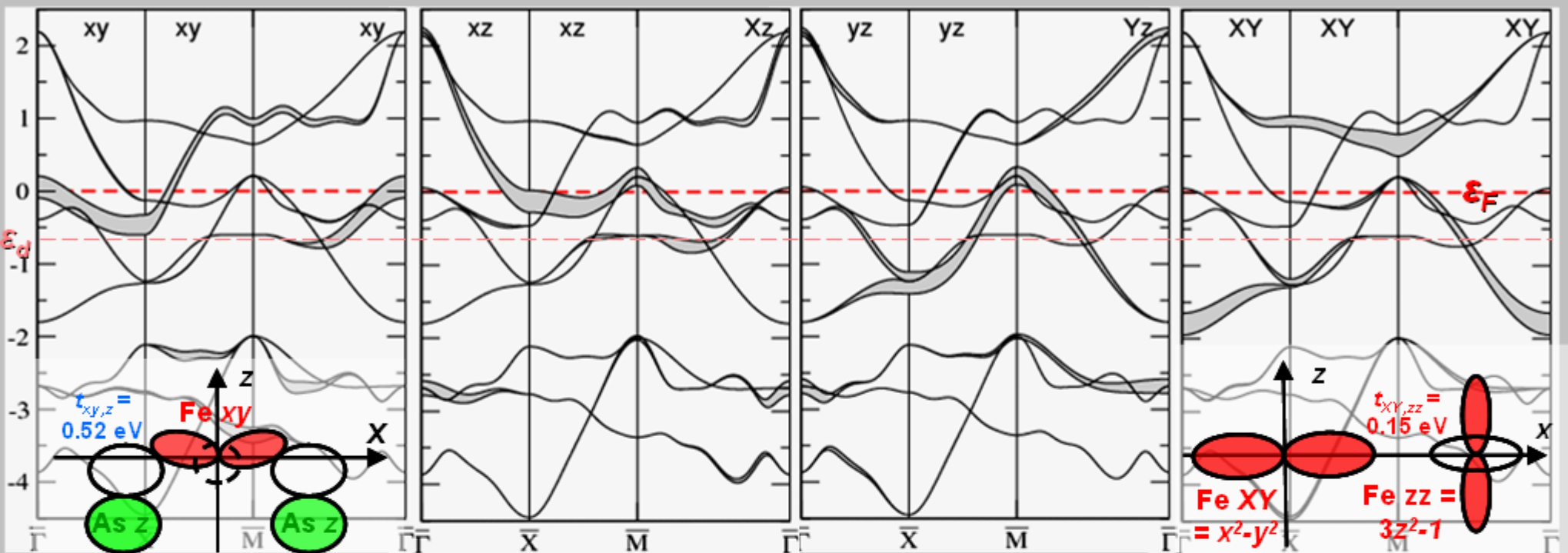


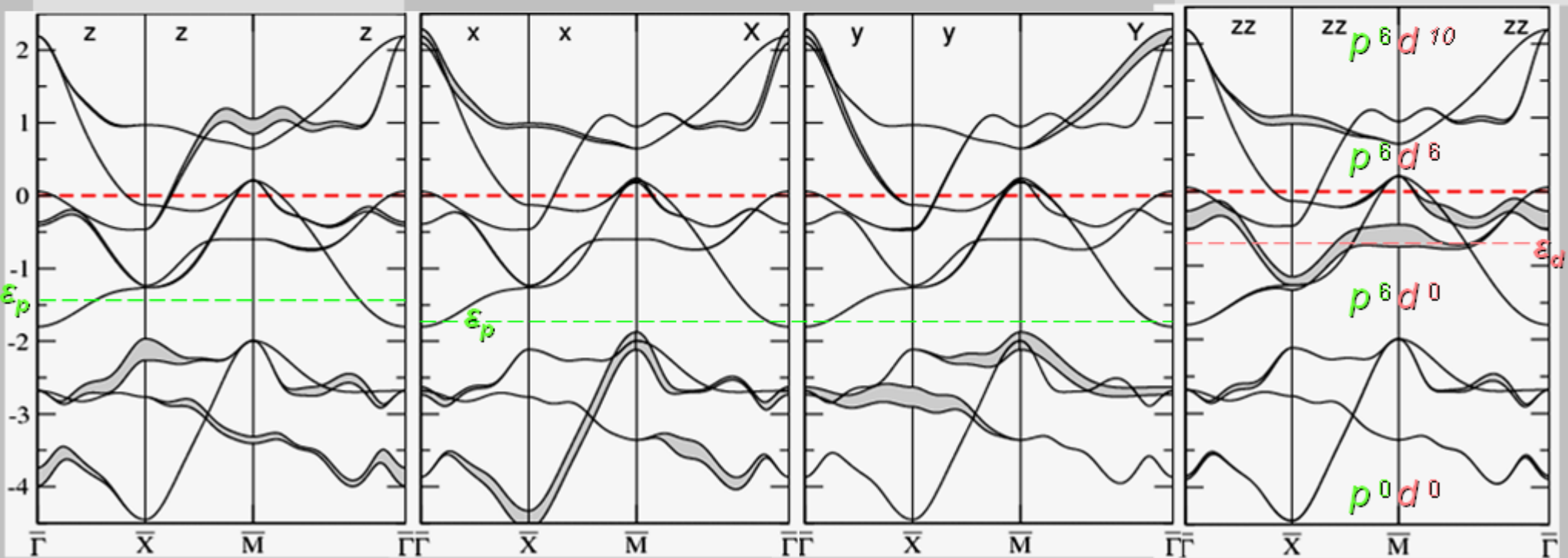
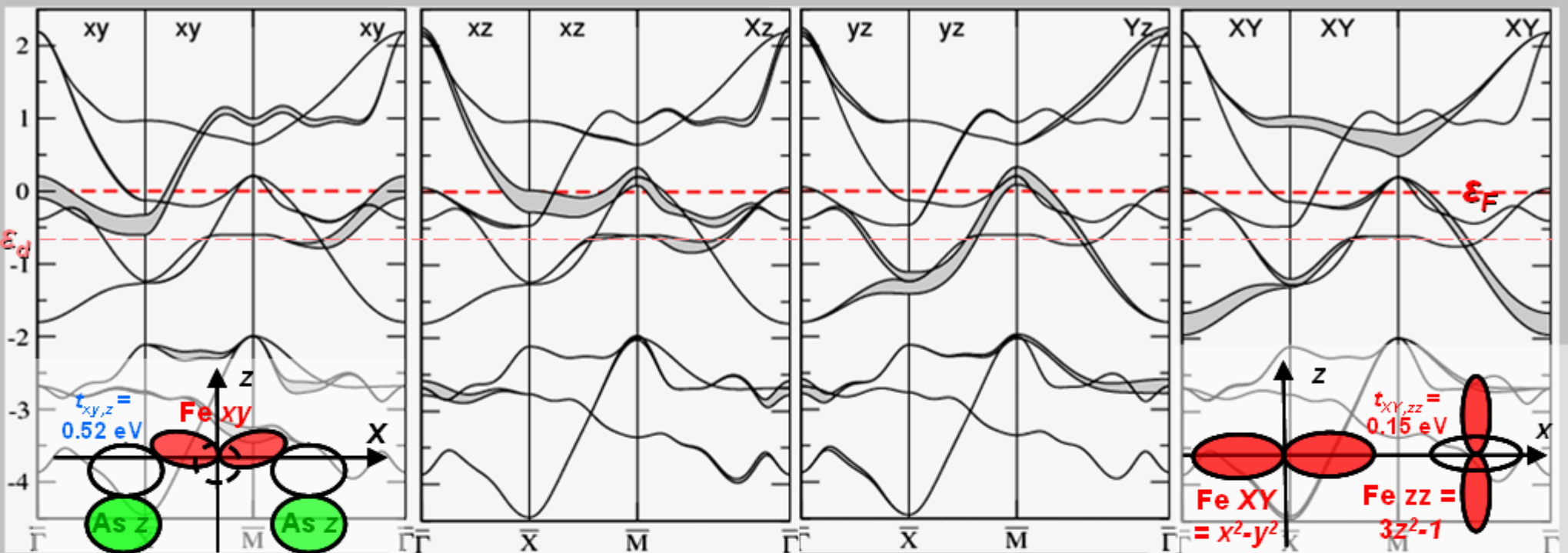


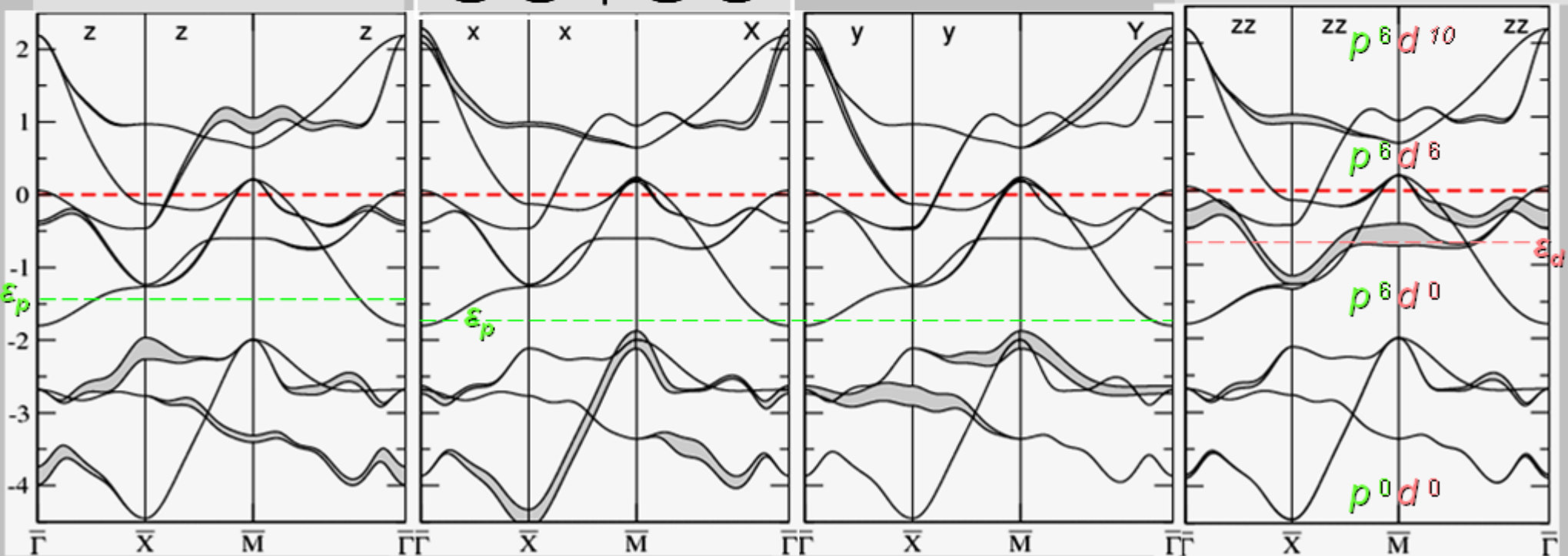
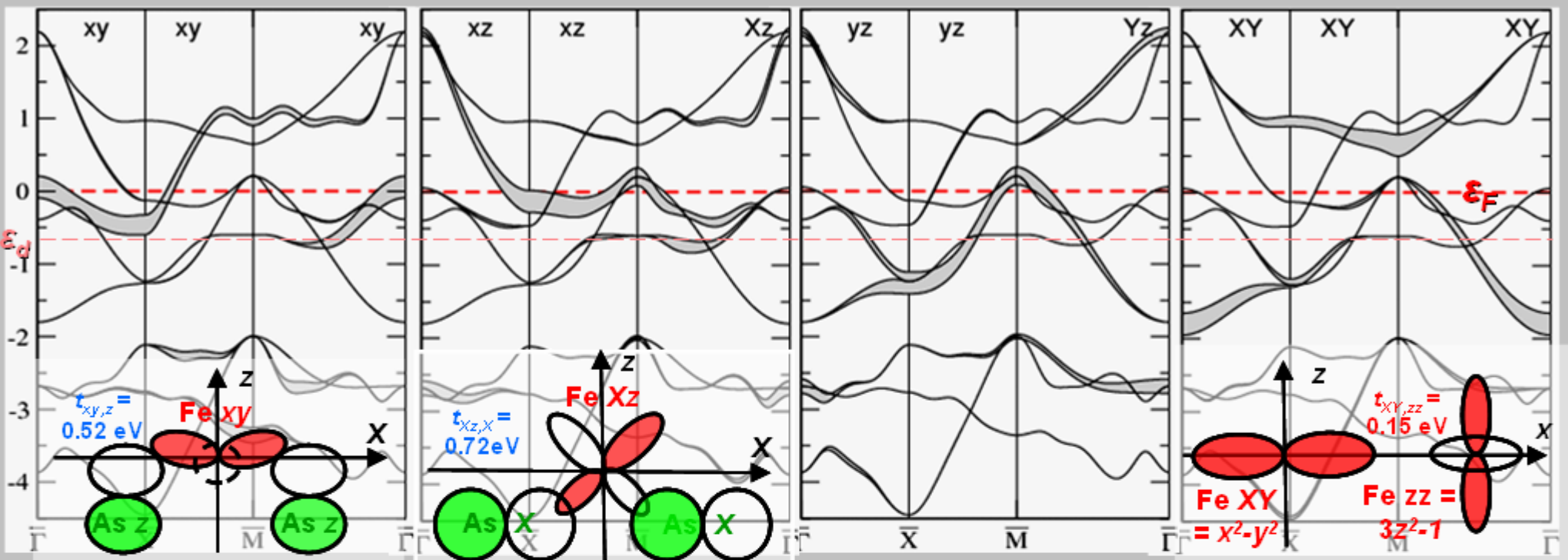


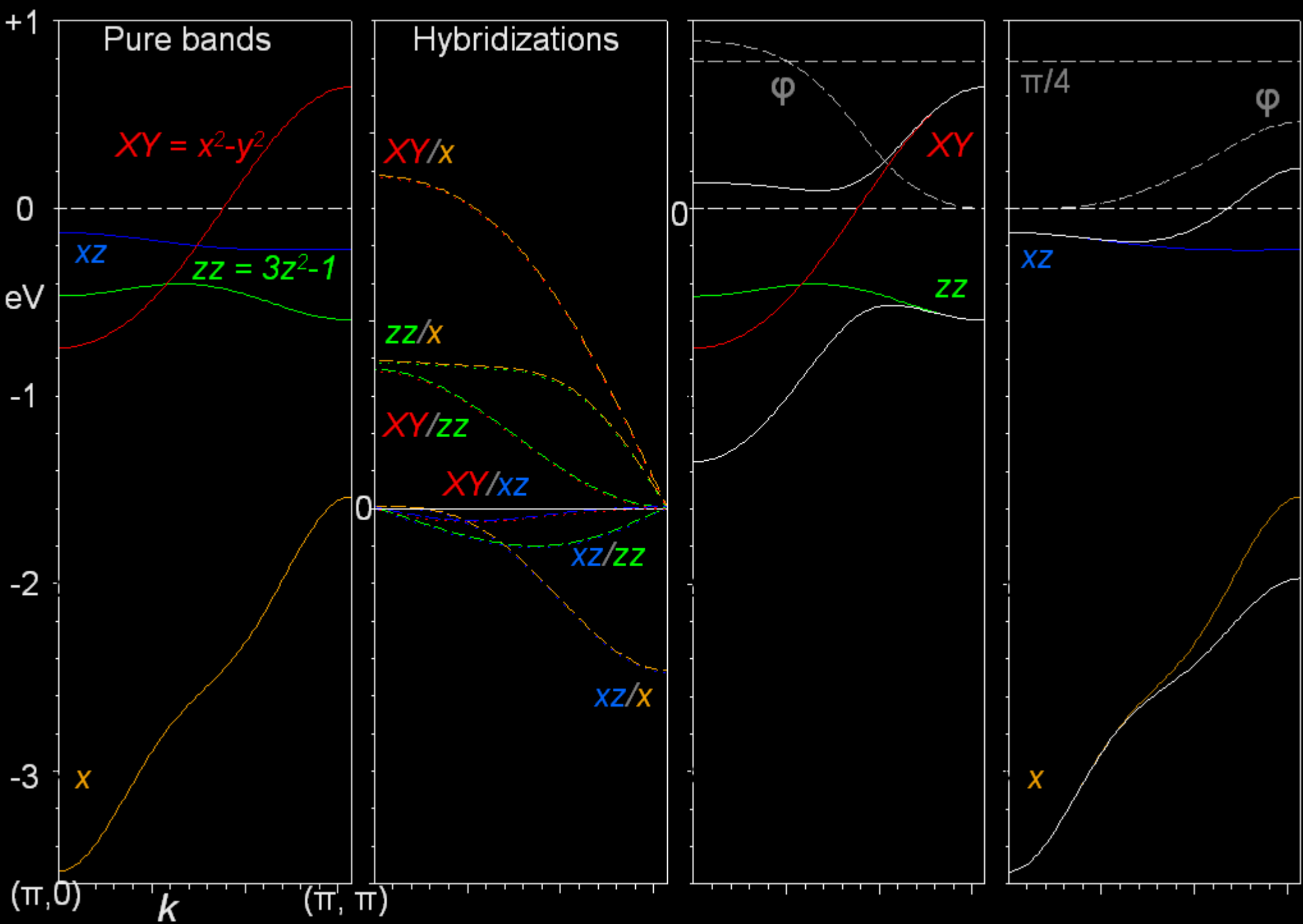


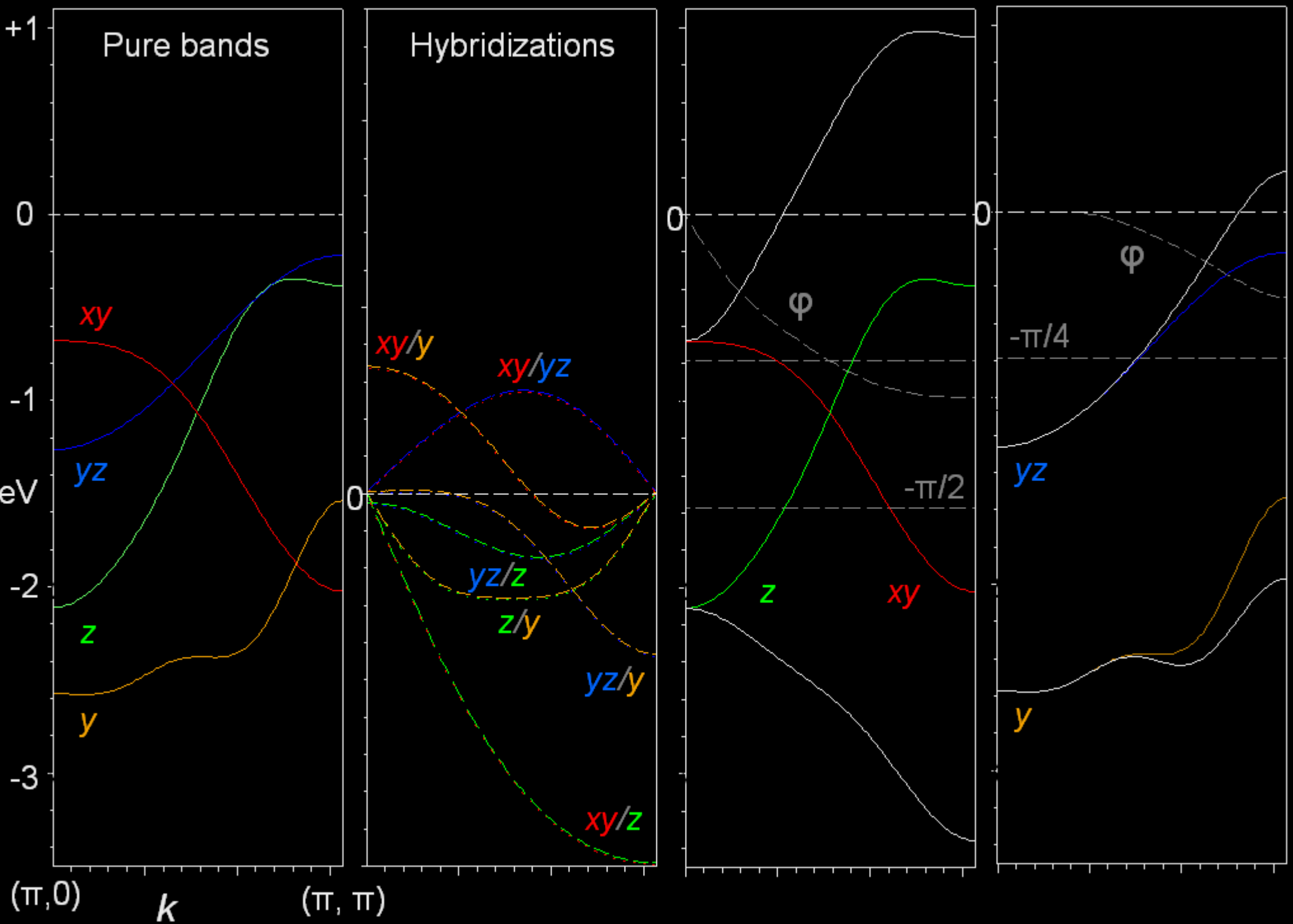


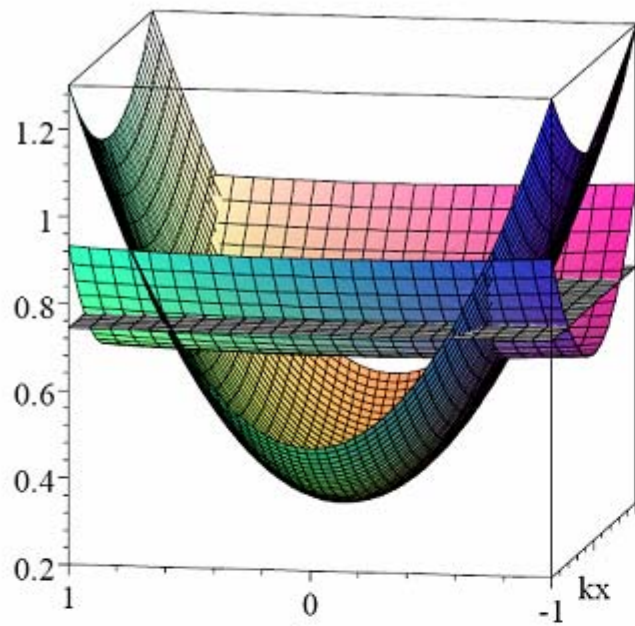




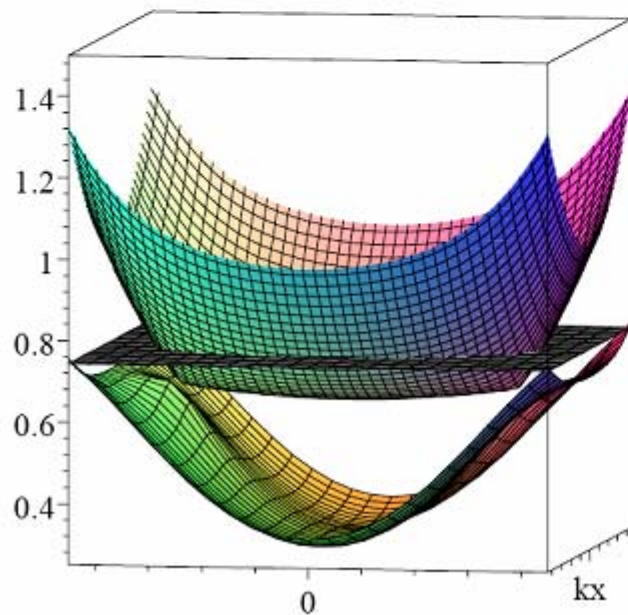
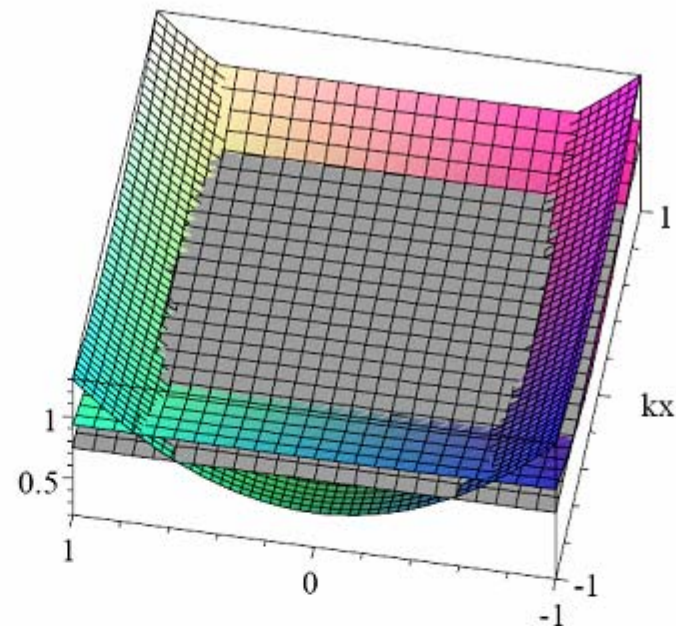




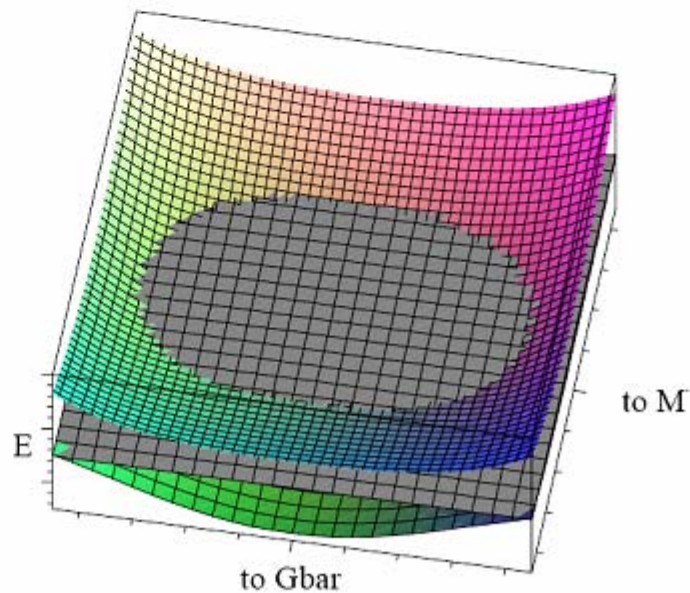




Non-hybridized xy - z and xz - y like bands near \underline{X}

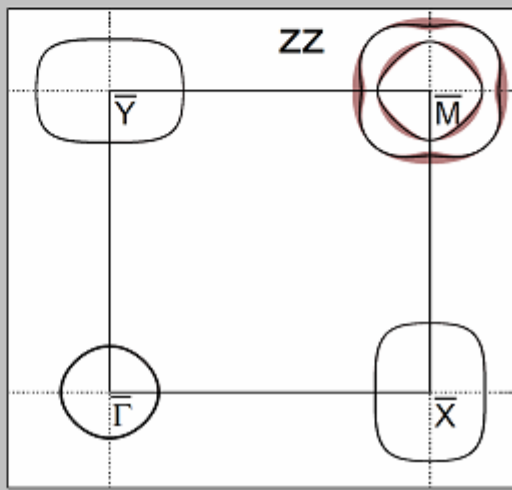
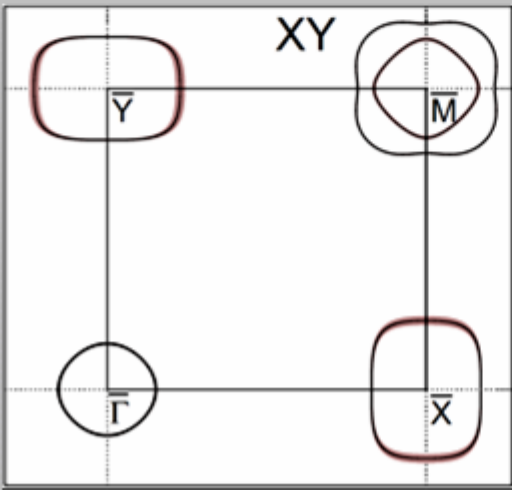
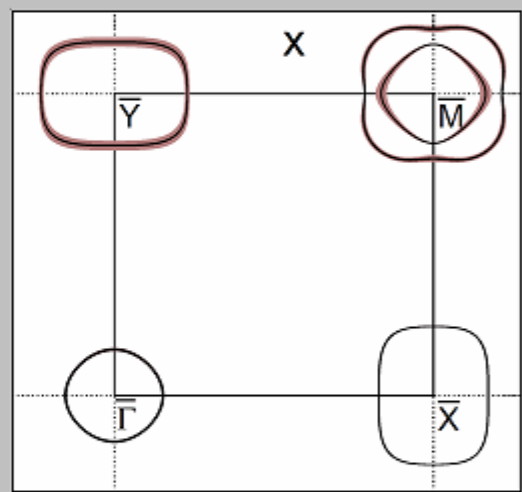
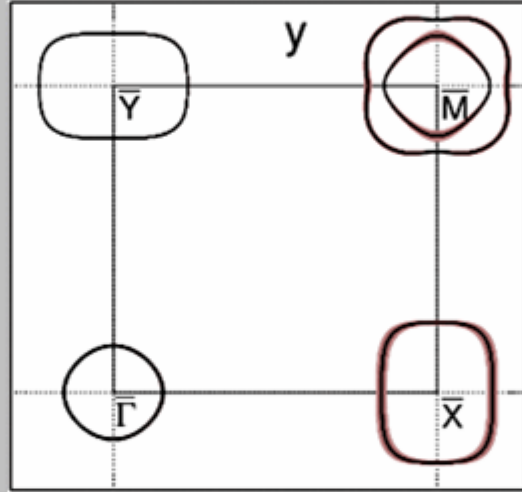
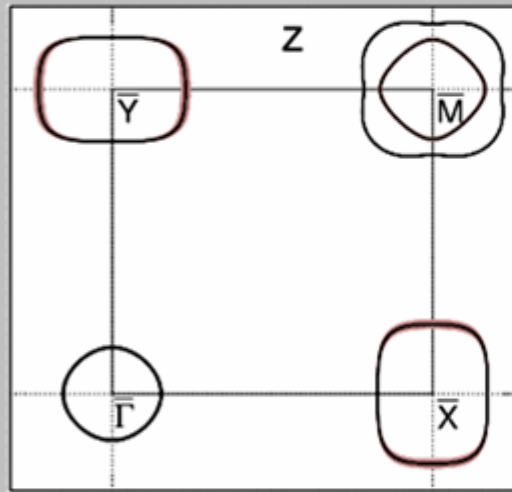
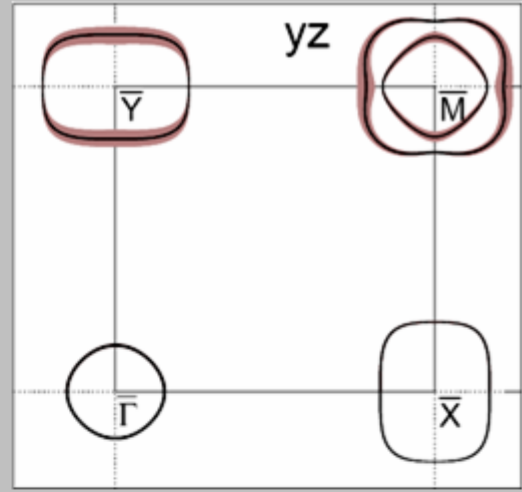
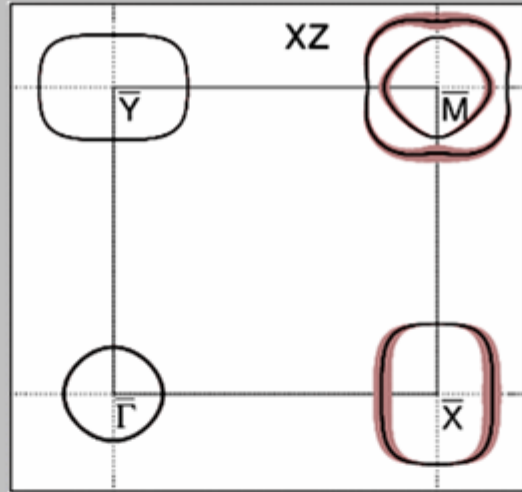
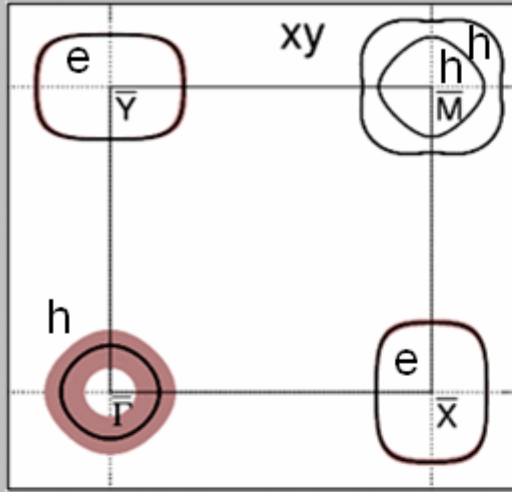


Hybridized xy - z and xz - y like bands near \underline{X}



This super-ellipsoidal electron pocket points towards the doubly degenerate hole pockets at \underline{M}

1/5 x

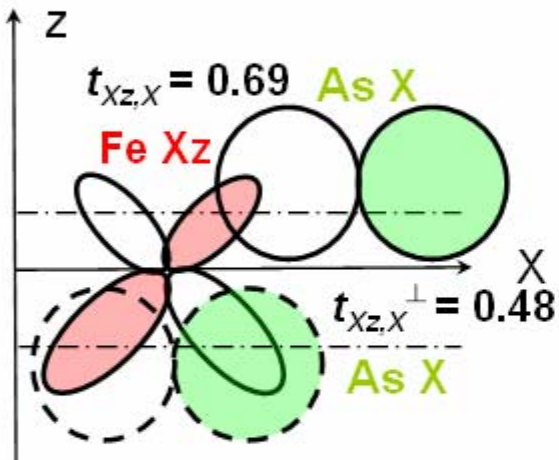


One reason for the small mass ($\sim 1m_0$) of the inner, M-centered hole pocket

Hybridized Xz - X band

Pure Xz band

thin line: (1,0) hops only



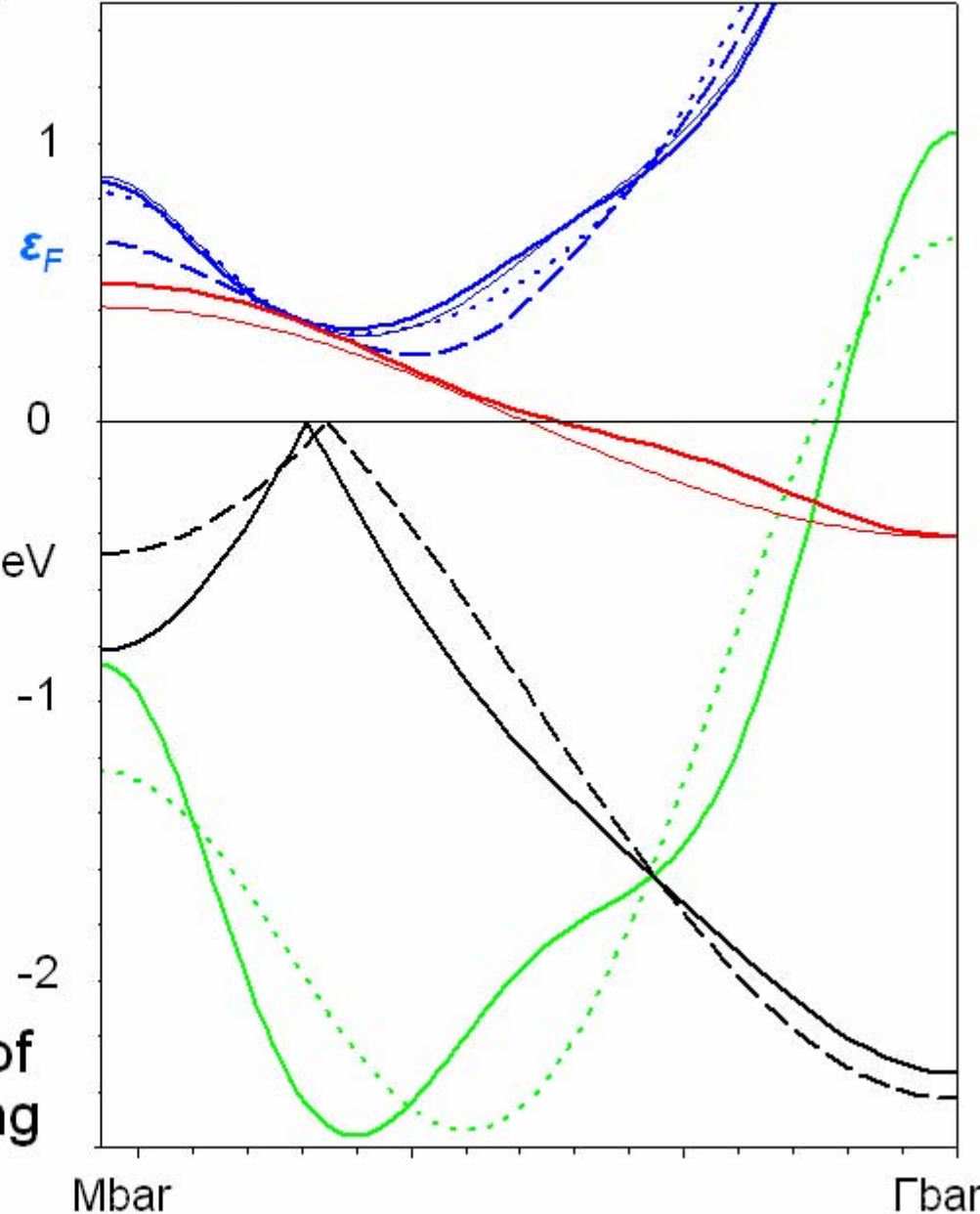
Xz - X hybridization (- abs. value)

dashed line: $(\frac{1}{2}, \frac{1}{2})$ hops only

Pure X band

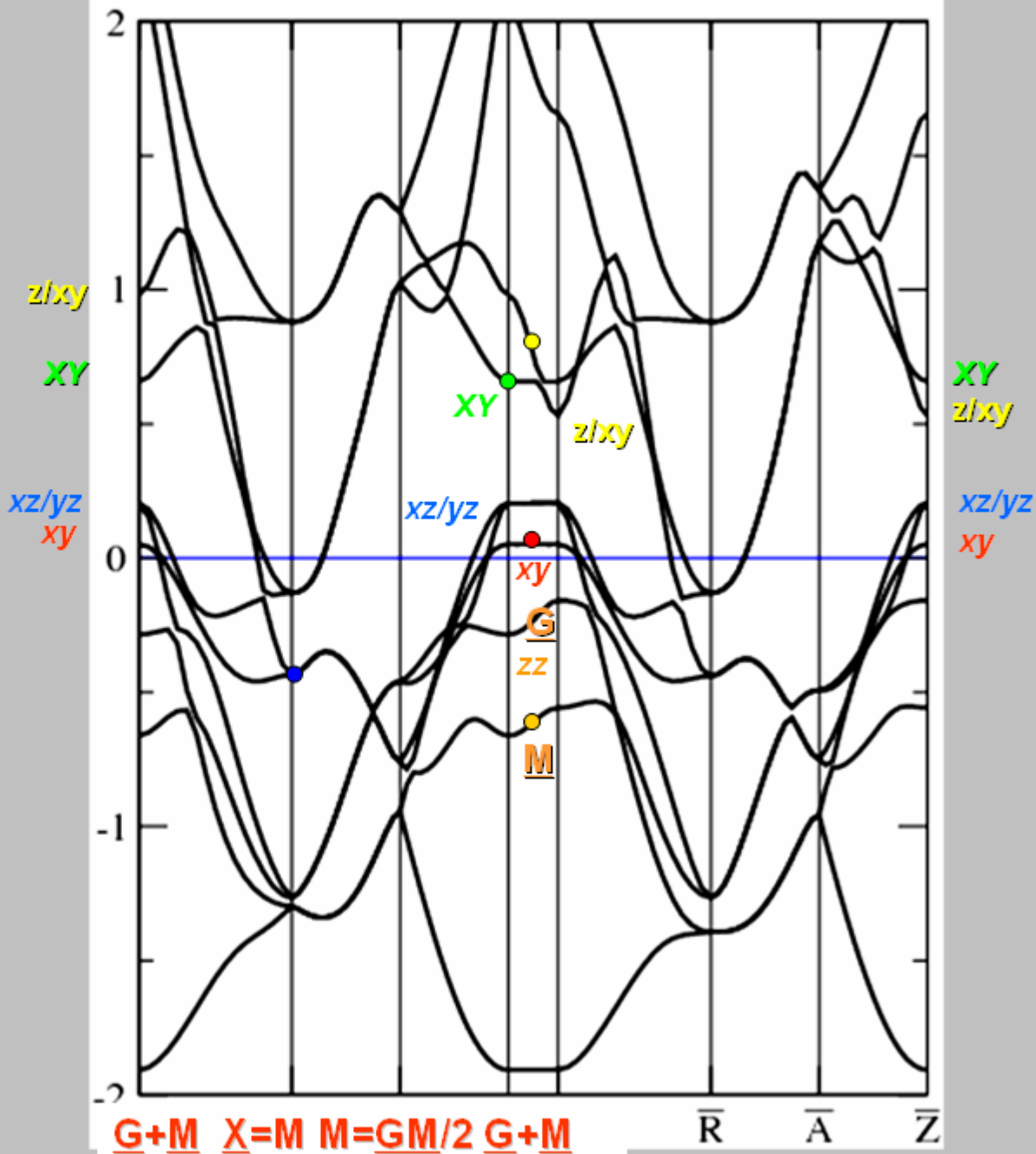
dotted line: (1,0) and (1,1) hops only

For the small band mass ($\sim 1m_0$) of the Fe d -like hole pockets, the long range of the As p - Fe d hybridization is crucial.



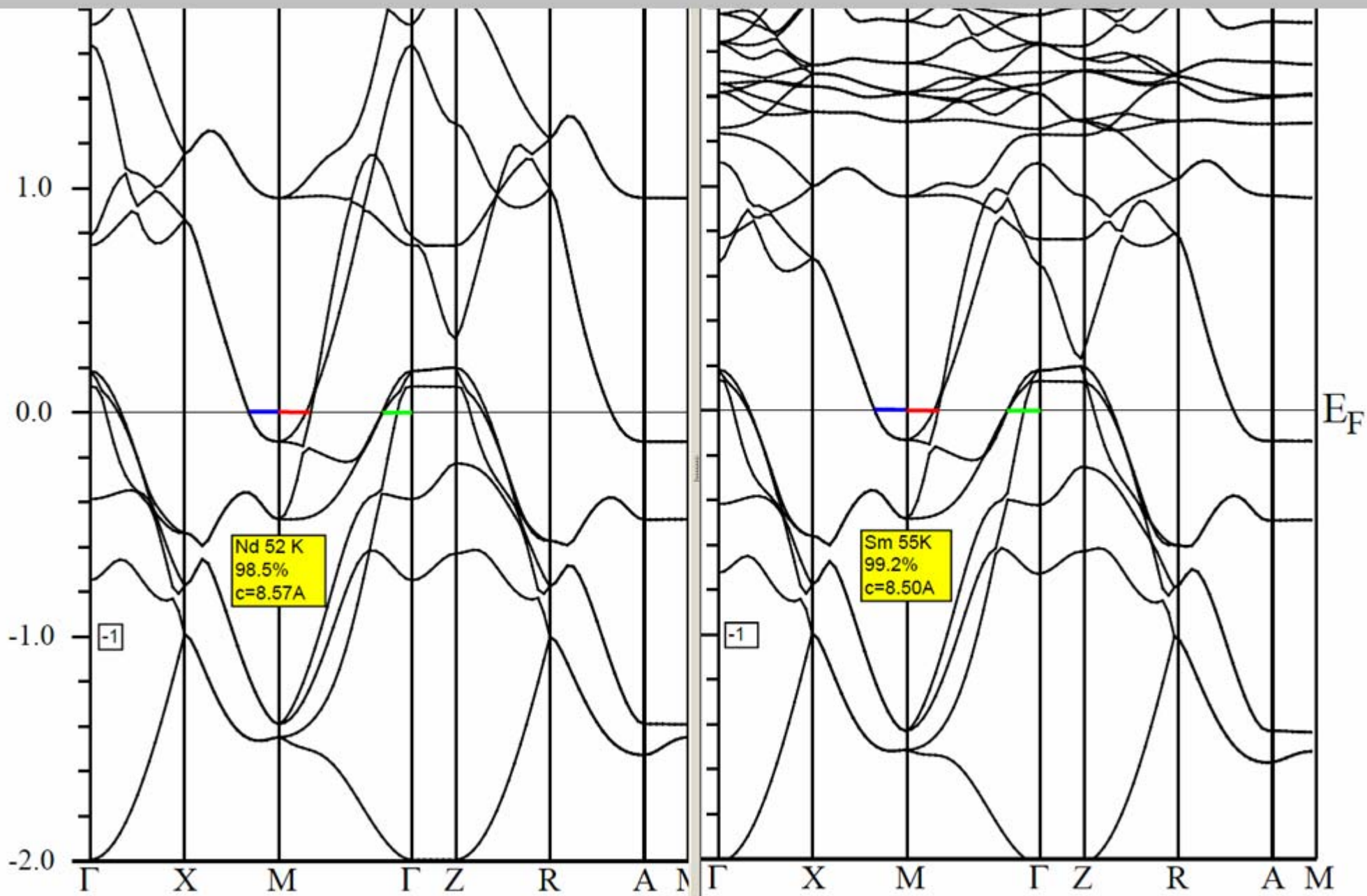
LAPW, exp coord

Another -more interesting- reason, causing the materials' trend

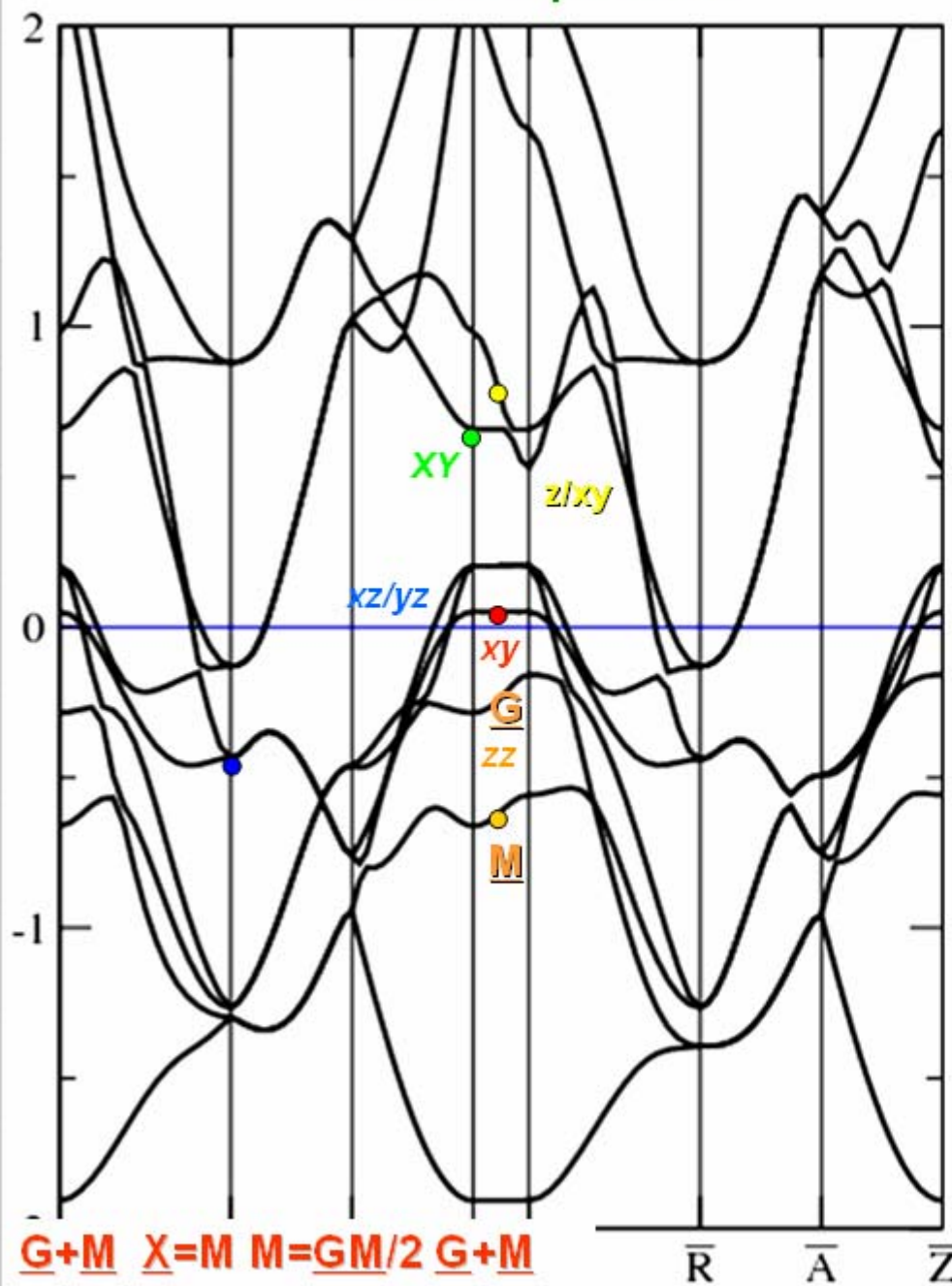


NdOFeAs

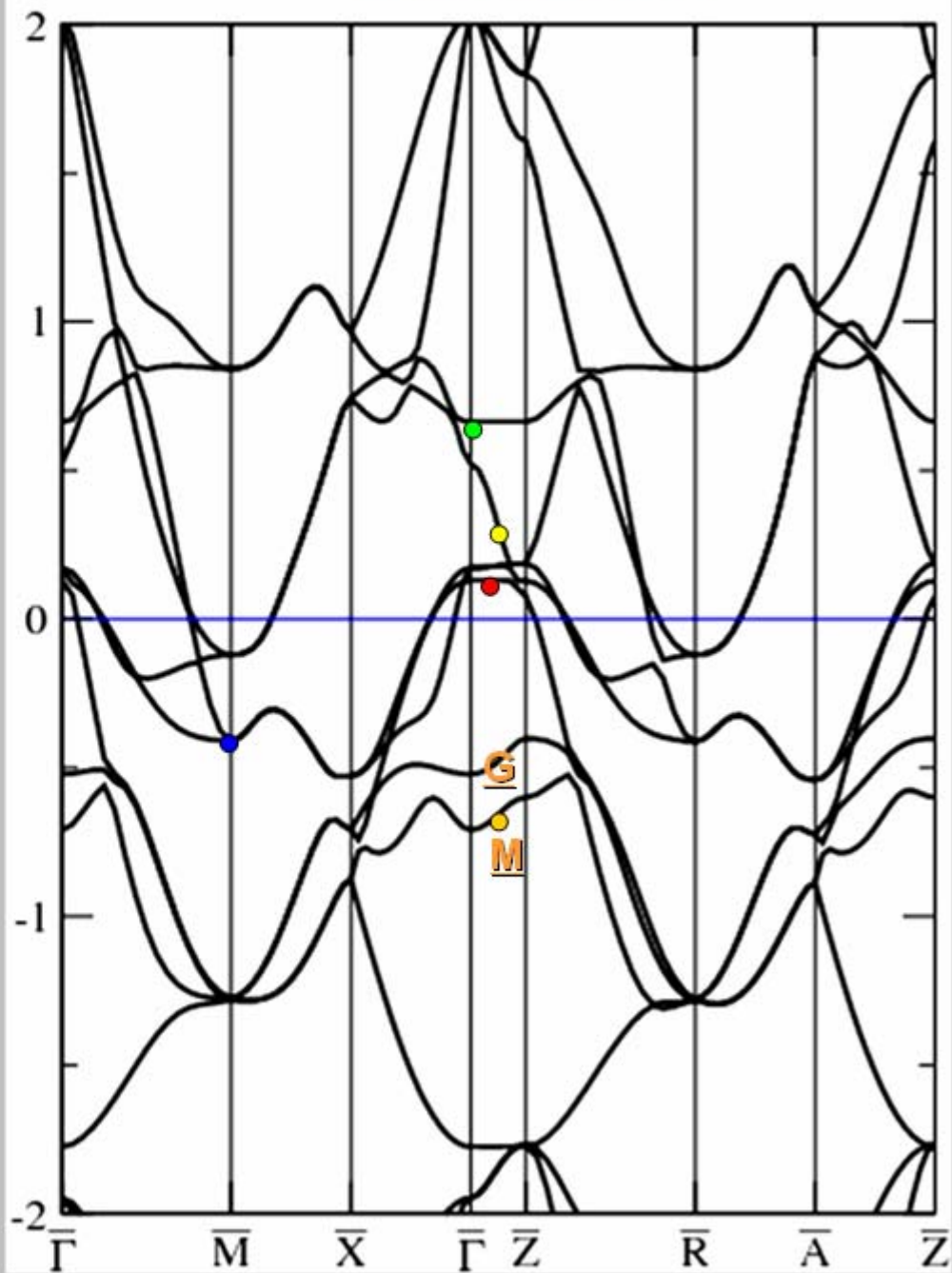
SmOFeAs

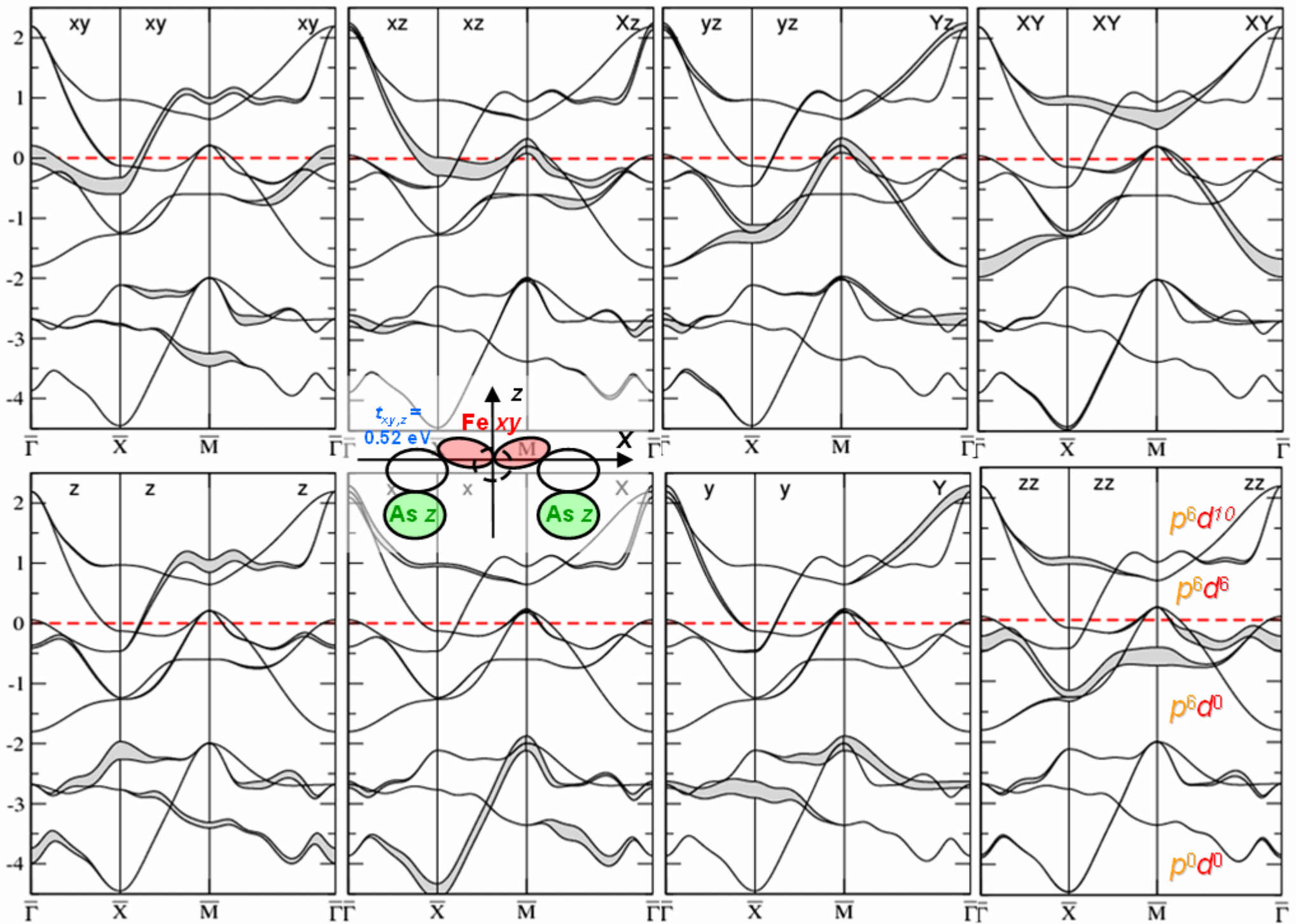


LAPW, exp coord
96% compression

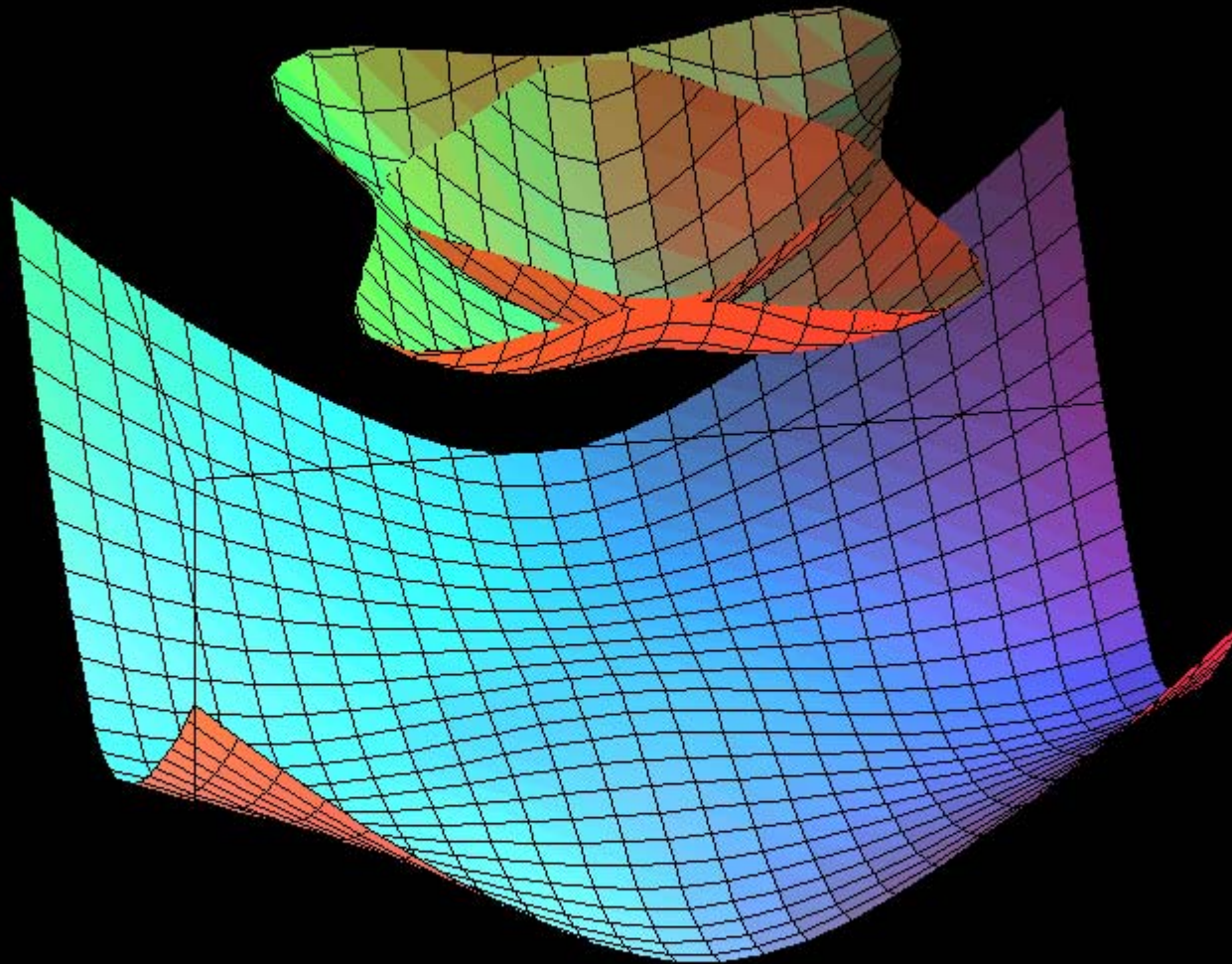


LAPW, elongated tetrahedron
102% elongation



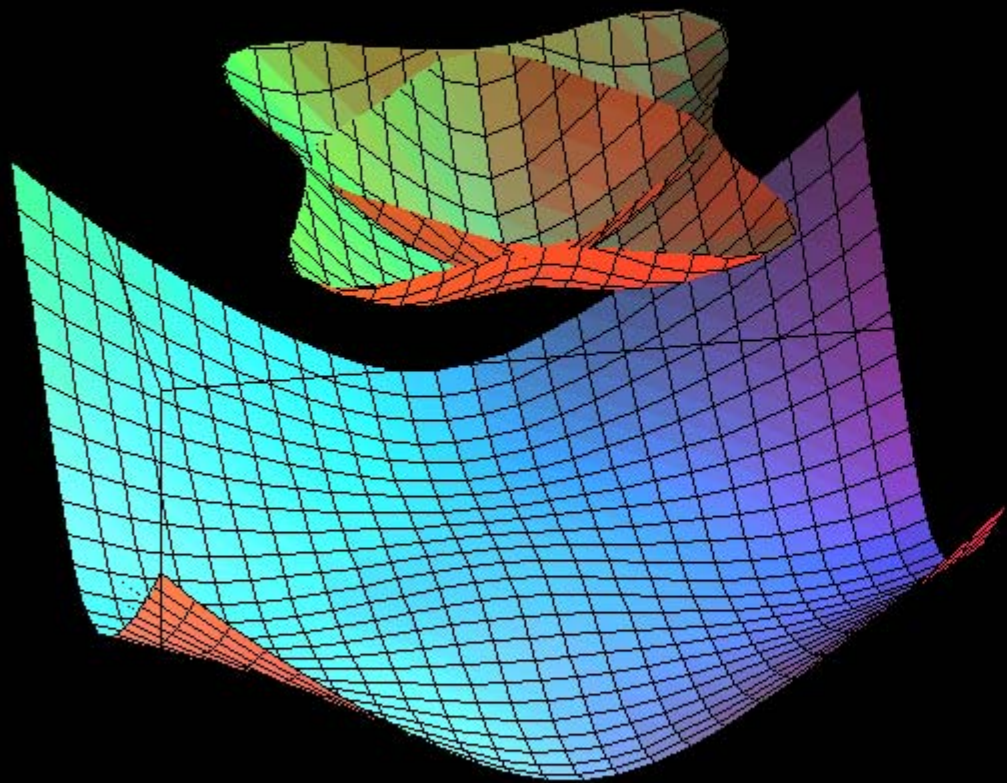


Hybridized xz/yz -like hole bands near M



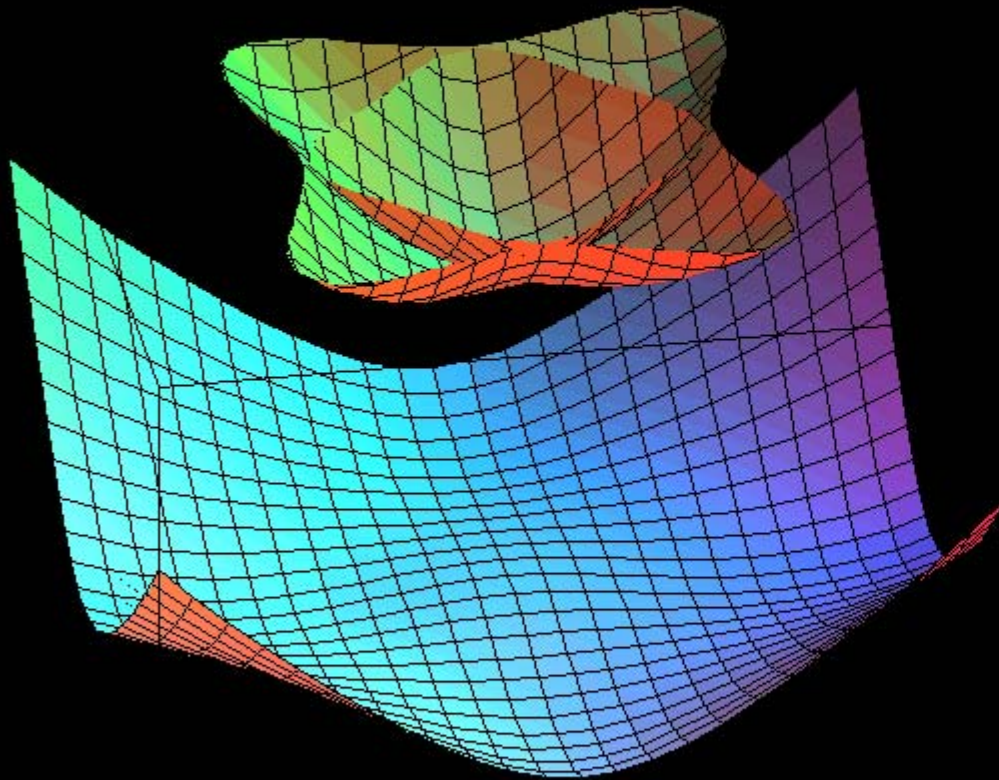
Antibonding z/xy band

Hybridized xz/yz -like
hole bands near M



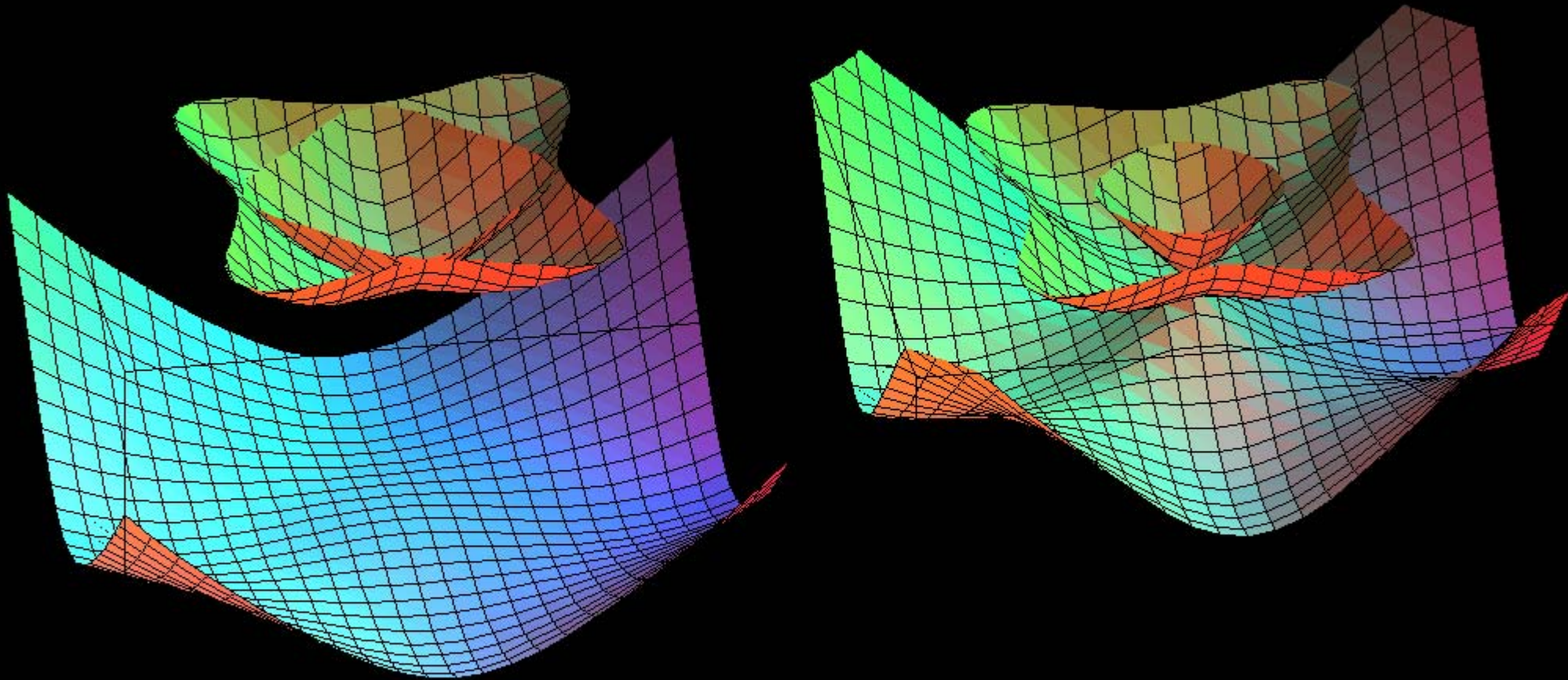
Hybridized xz/yz -like
hole bands near \underline{M}

The z/xy band cannot hybridize with xz/yz
at \underline{M} . But it can away from \underline{M} , where the
hybridization increases linearly with k_{\perp} .



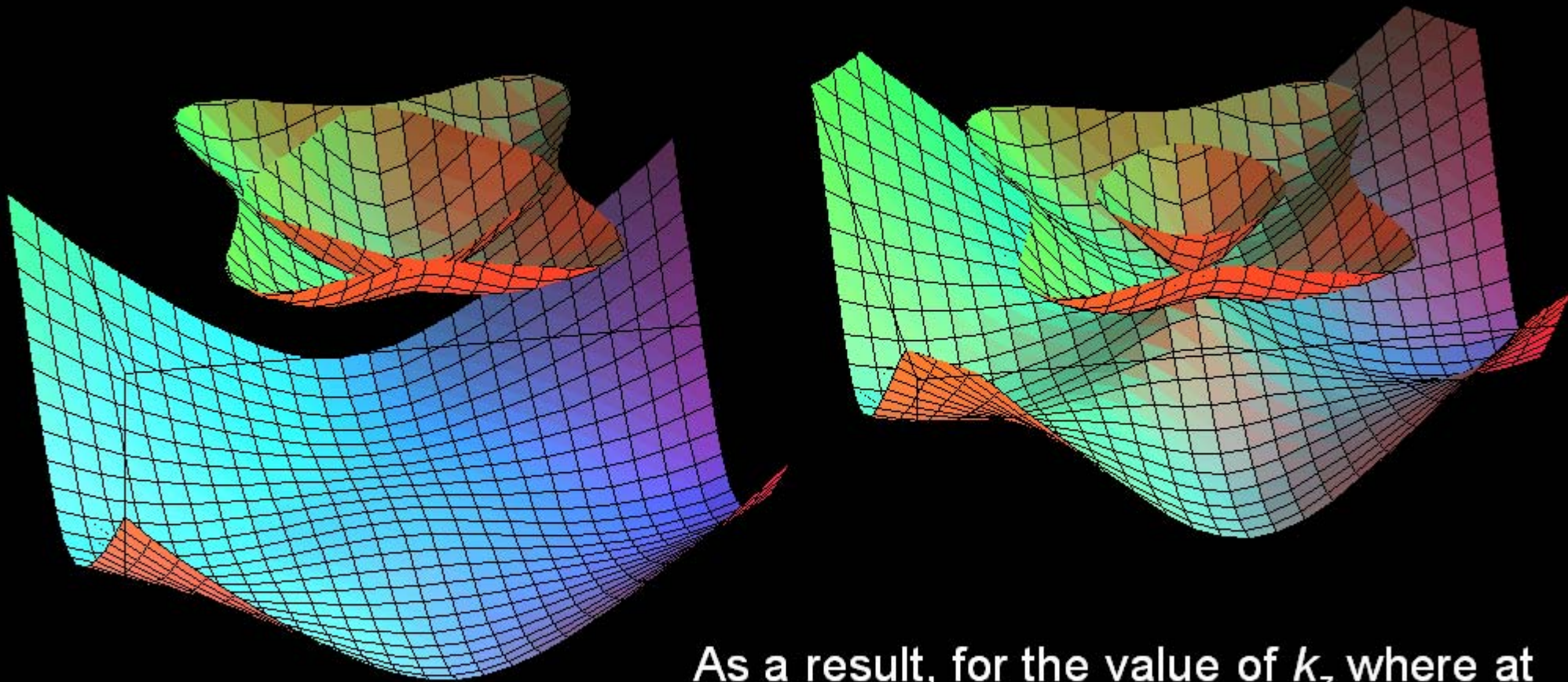
Hybridized xz/yz -like
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The z/xy band cannot hybridize with xz/yz
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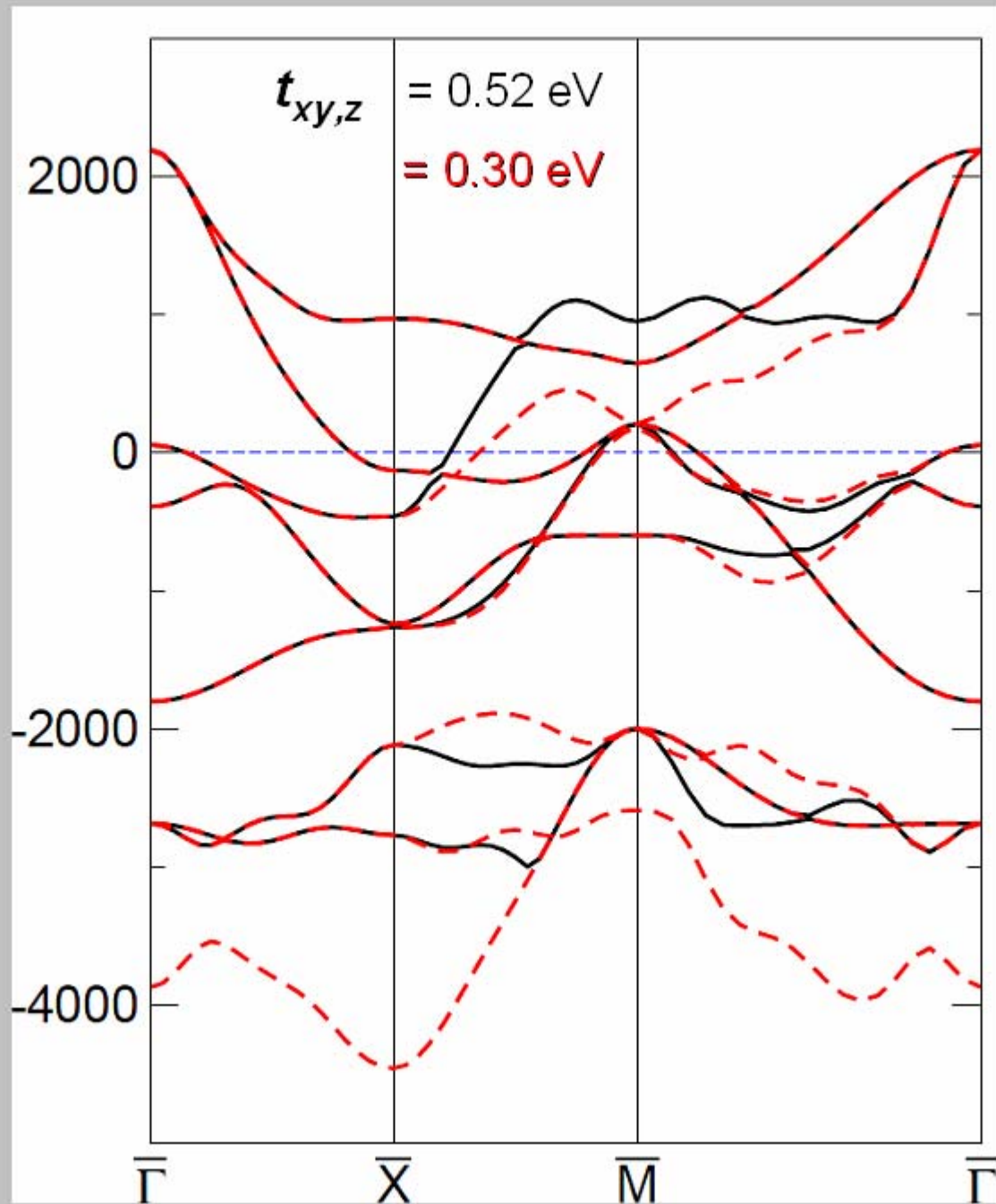
Hybridized xz/yz -like
hole bands near \underline{M}

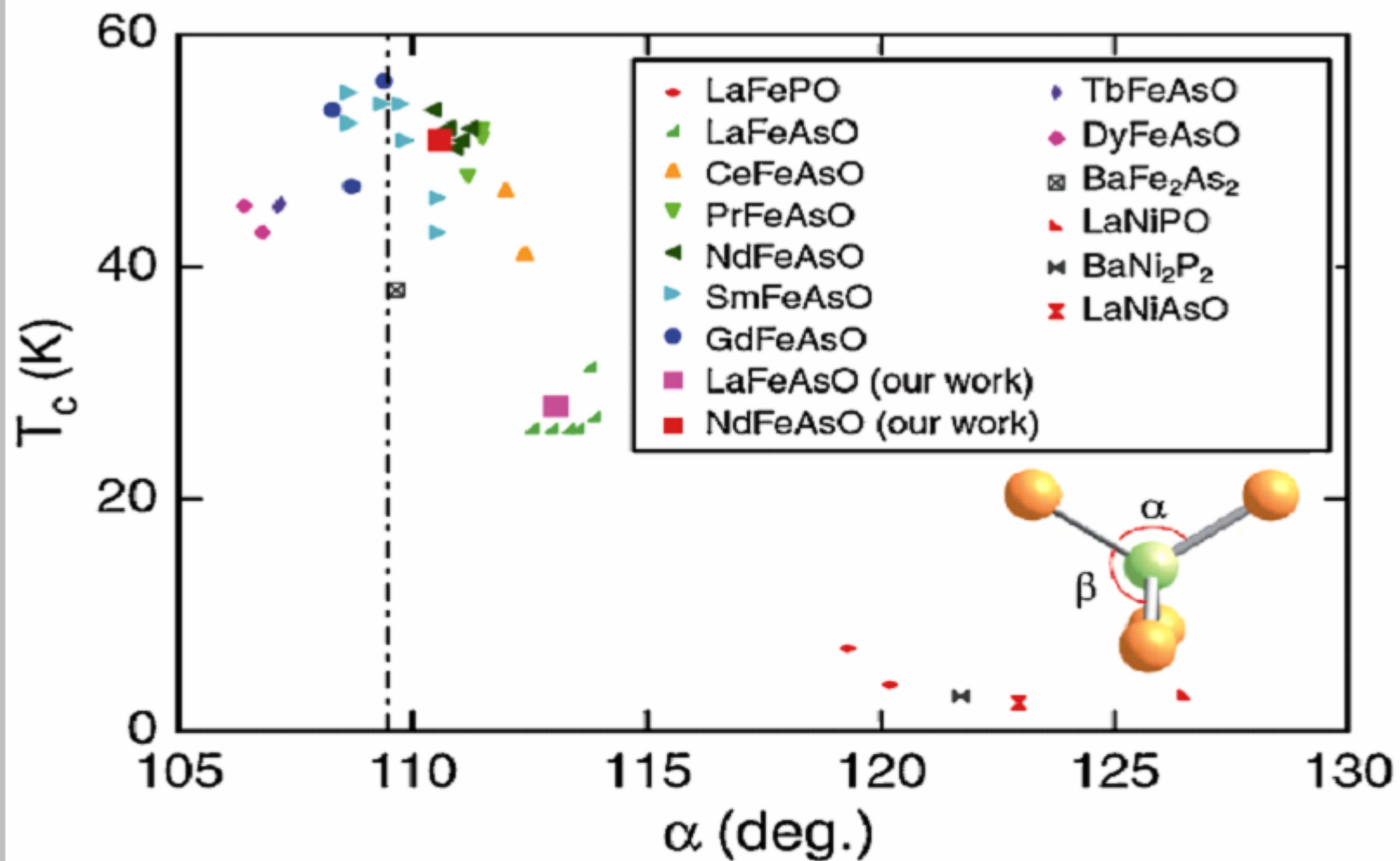
The z/xy band cannot hybridize with xz/yz
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hybridization increases linearly with k_{\perp} .



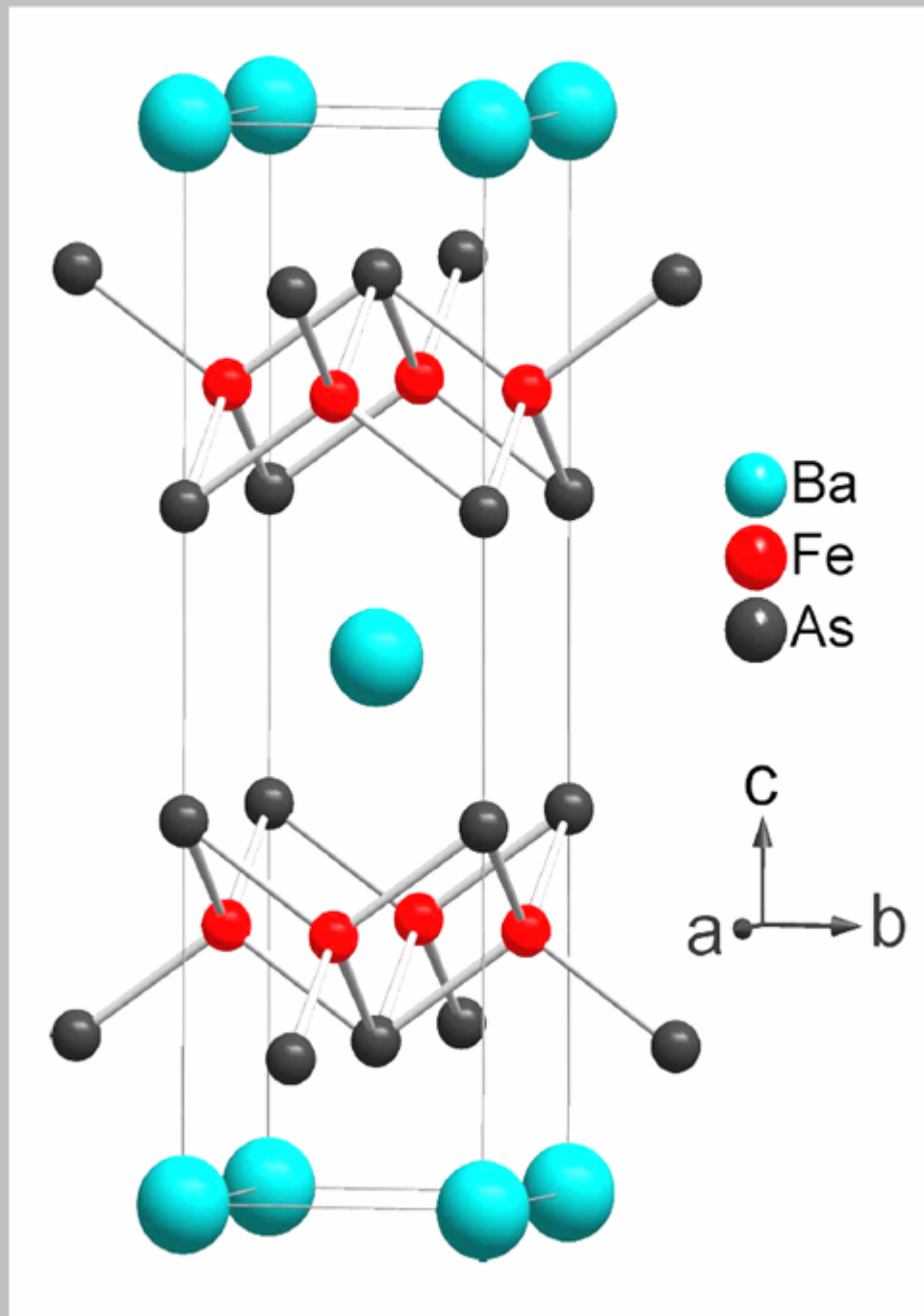
As a result, for the value of k_z where at
 \underline{M} the z/xy and xz/yz bands become
degenerate, the z/xy band and the
inner xz/yz band form a *Dirac cone*
with linear dispersion in k_{\perp} .

Main effect of tetraheder elongation





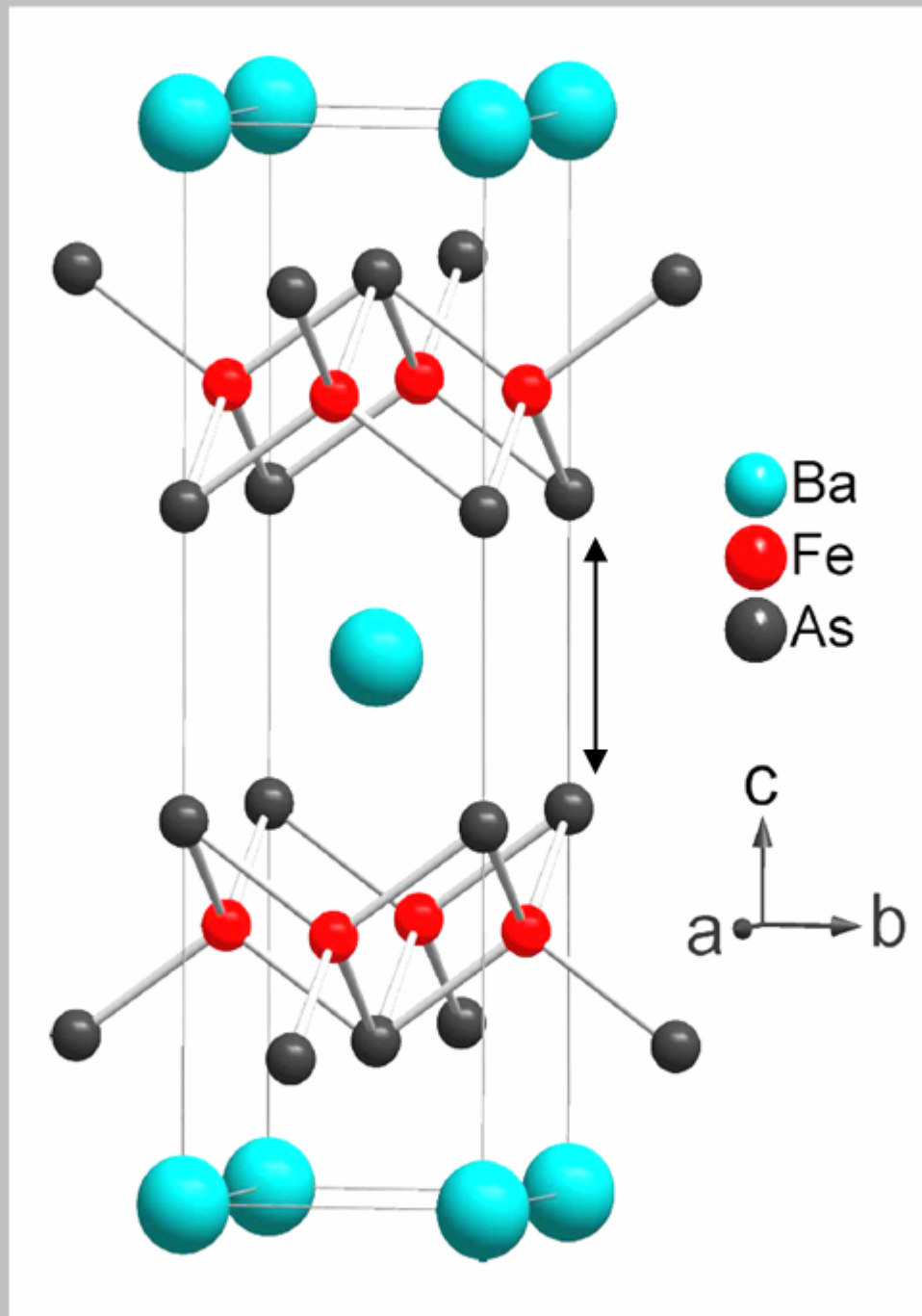
g. 31. (Color online) T_c vs As–Fe–As bond angle α for various pnictide superconductors. The formulas of parent compositions of superconductors are depicted in the inset. The crystal structure parameters of samples showing almost maximum T_c in each system are selected. The vertical dashed line indicates the bond angle of a regular tetrahedron ($\alpha = 109.4^\circ$).¹²¹⁾ Figure reprinted from C.-H. Lee *et al.*: *J. Phys. Soc. Jpn.* **77** (2008) 083704. Copyright 2009 by the Physical Society of Japan.



Fe chalcogenides have the same structure, but without Ba.

In all compounds, the Fe layers are stacked on top.

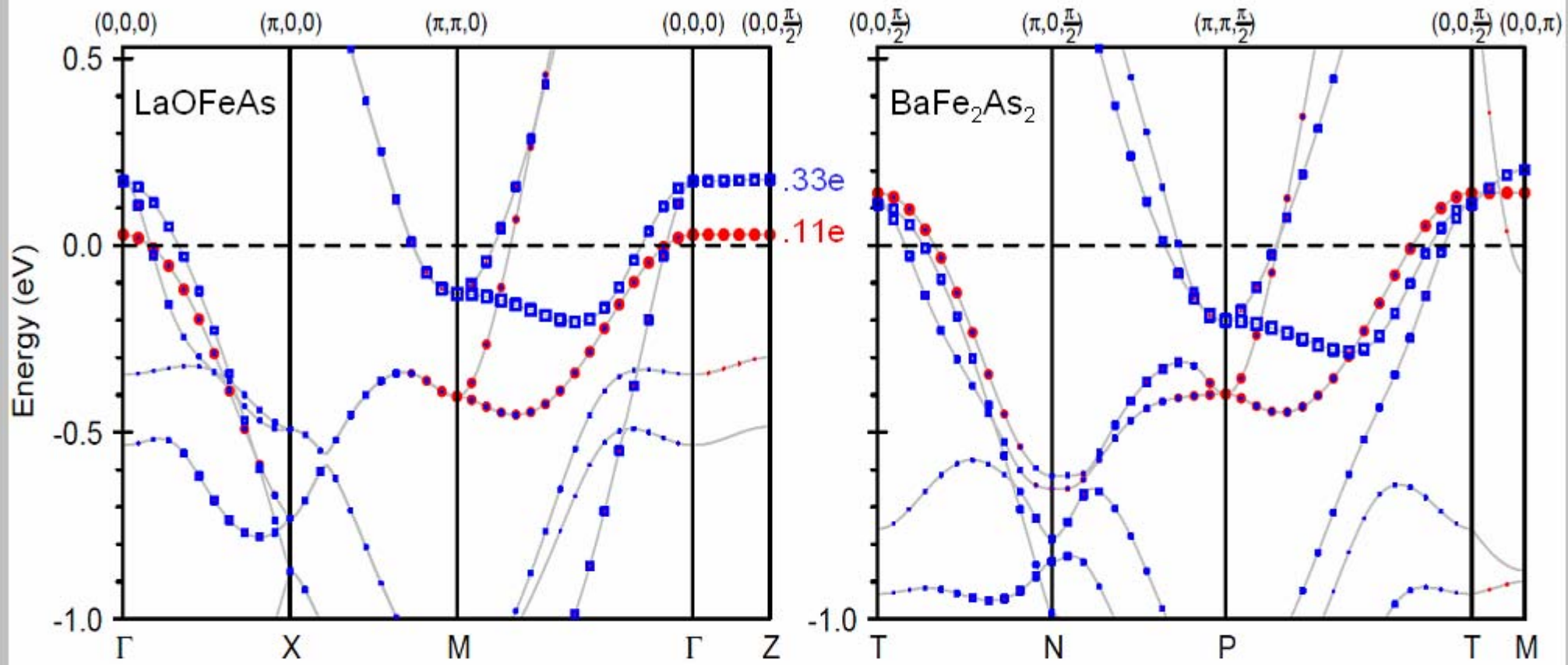
A primitive translation along c should be associated with mirroring in the Ba and chalcogenides compounds but not in the LnO.



Fe chalcogenides have the same structure, but without Ba.

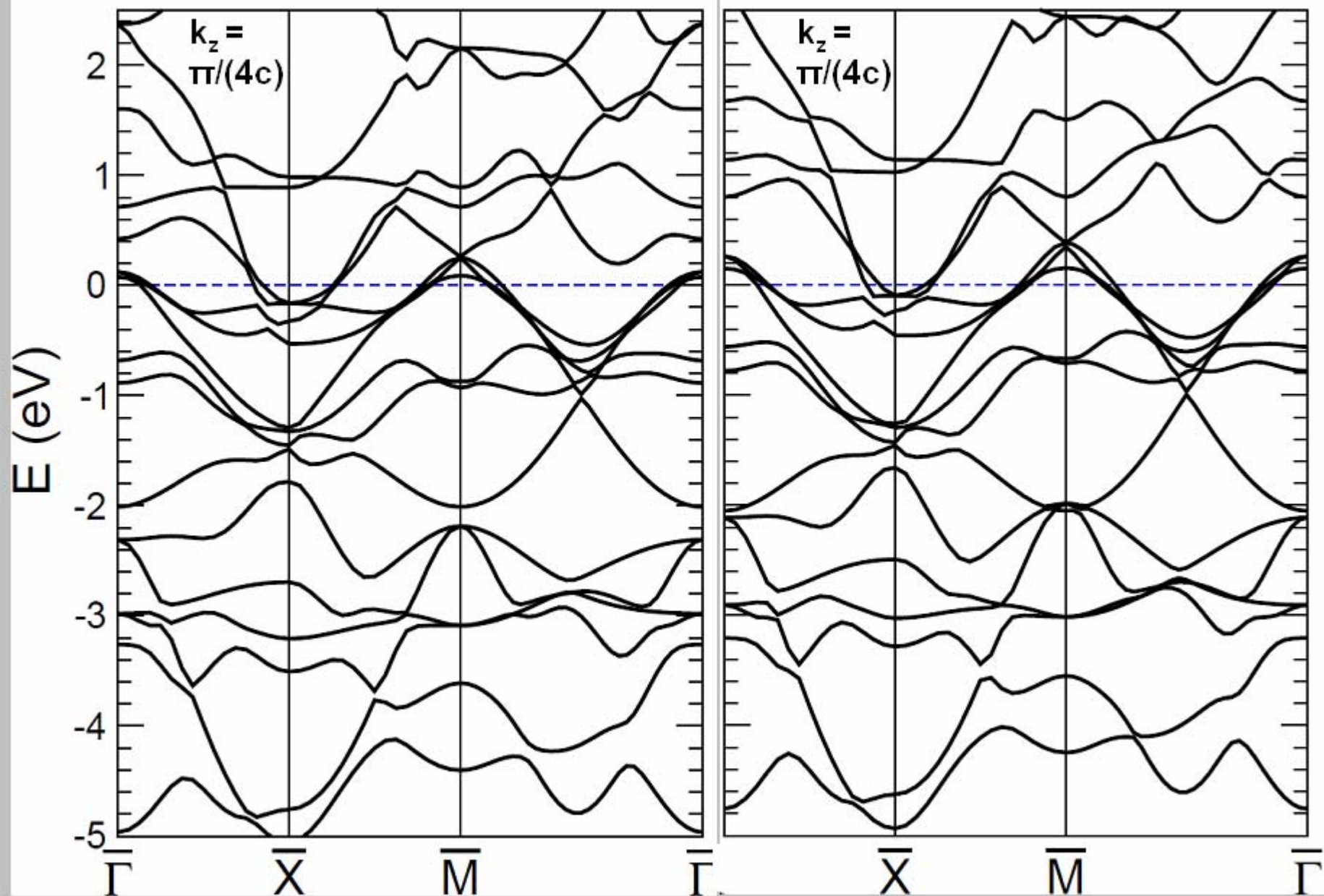
In all compounds, the Fe layers are stacked on top.

A primitive translation along c should be associated with mirroring in the Ba and chalcogenides compounds but not in the LnO.



BaFeAs, undoped,
Dirac point above E_F and at $k_z = \pi/(4c)$

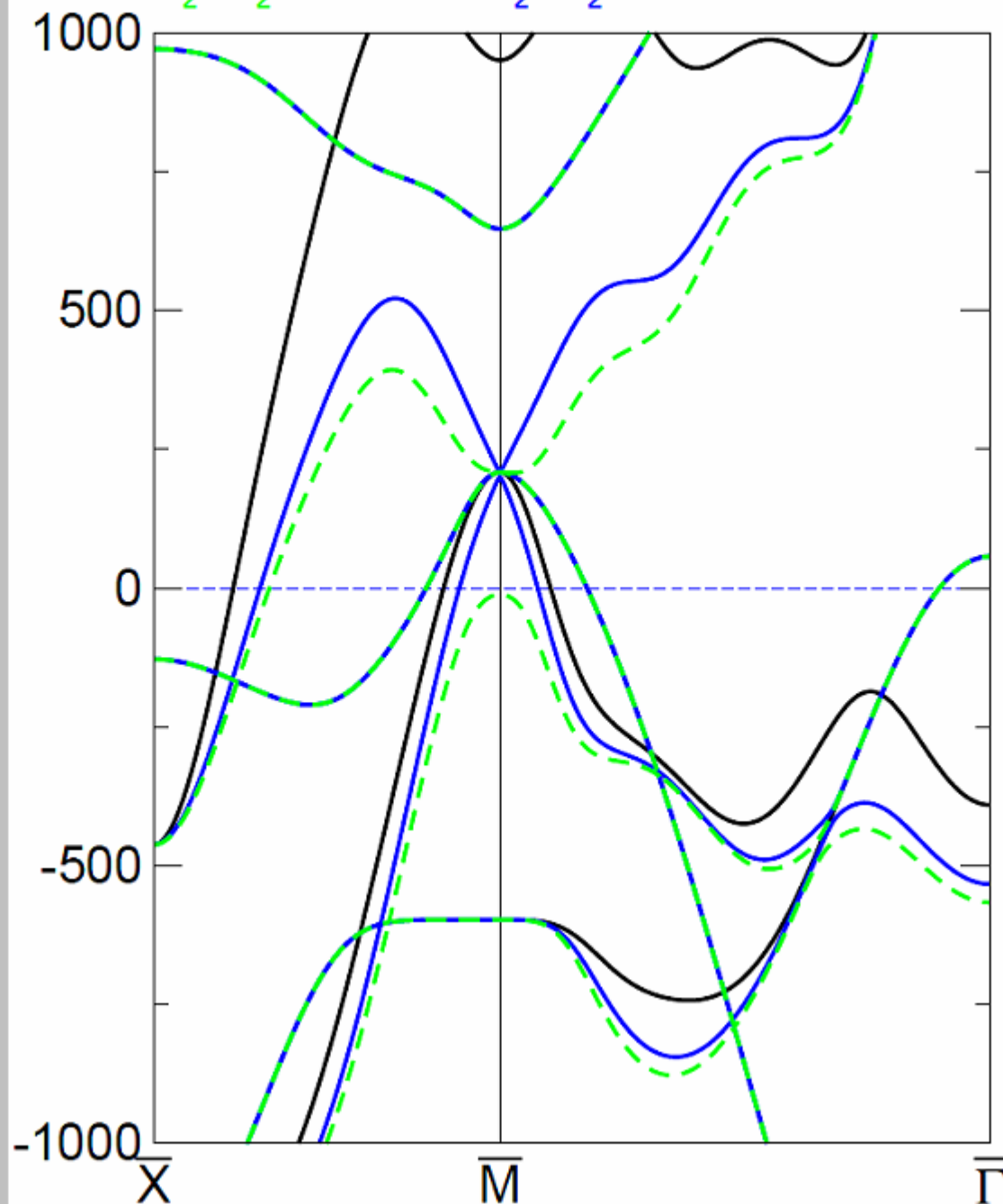
0.2 hole/Fe



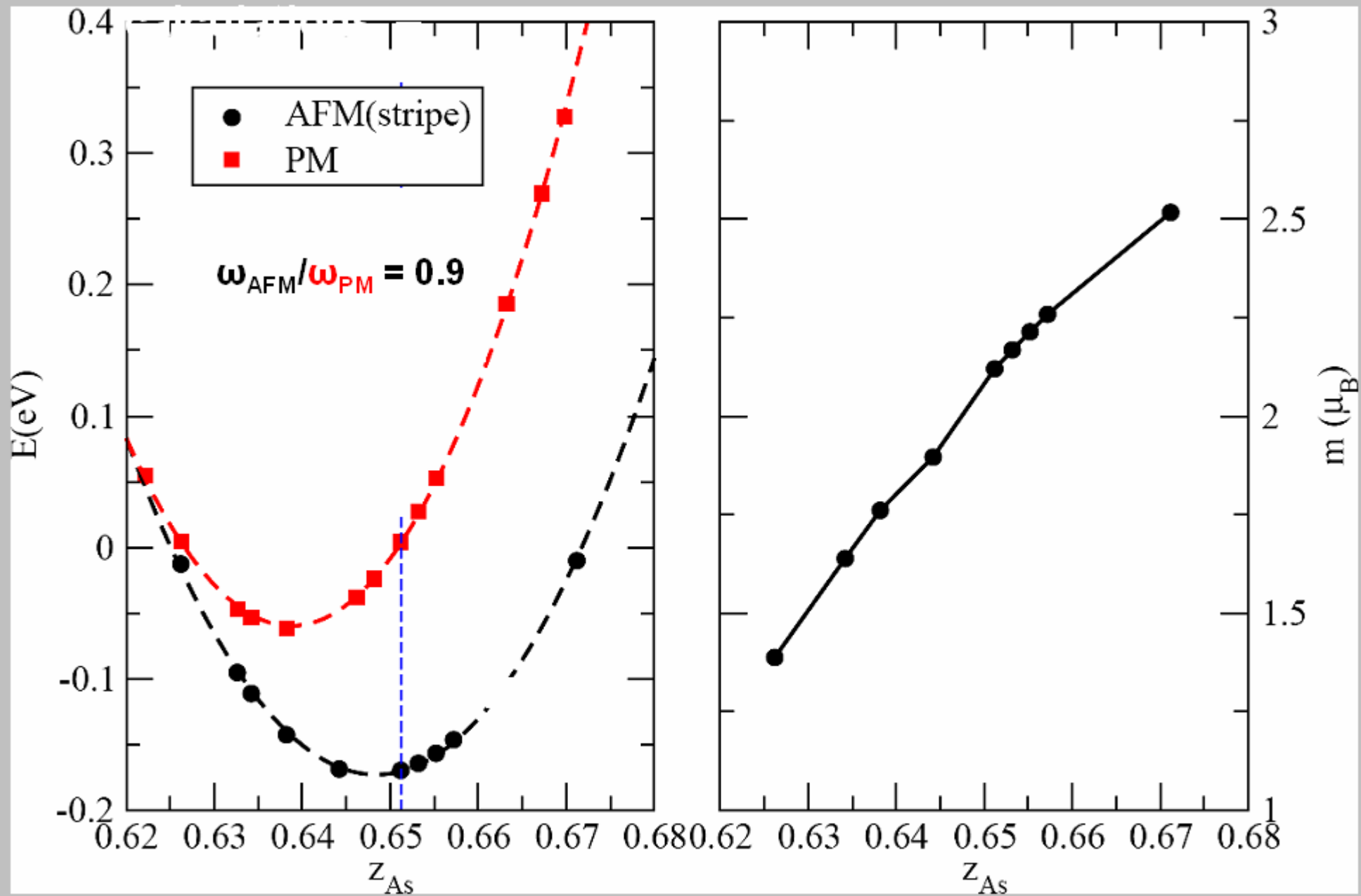
TB (2b) bands in the big zone $kz=\pi/2c$

$xy,z: =519$, shift p_z (simulate 3d dispersion)

$e_z=e_z^0-1600$ meV $e_z=e_z^0-1200$ meV



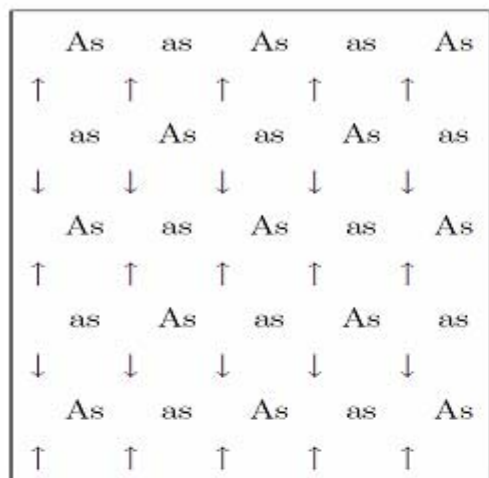
Results of LAPW **LDA** and **LSDA** total energy



Exp value of the elongation of the $FeAs_4$ tetrahedron

As a first application of our pd model we have studied magnetism.

Striped AFM order corresponds to a SDW with $\mathbf{q} = (0, \pi) = \underline{\gamma}$.



$$\mathbf{H}_{stripe} = \begin{pmatrix} \mathbf{H}(k_x, k_y) & \frac{1}{2}\Delta \\ \frac{1}{2}\Delta & \mathbf{H}(k_x, k_y + \pi) \end{pmatrix}$$

SDW
Hamiltonian

with $\Delta = \Delta \times$

Exchange
splitting

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

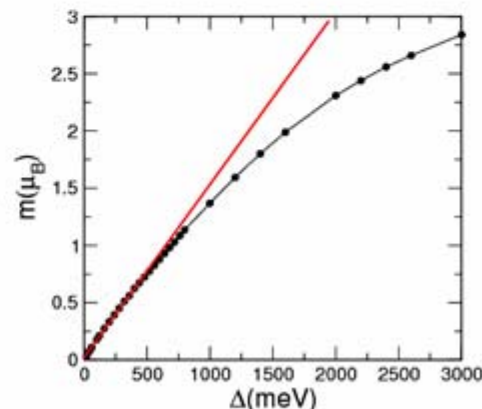
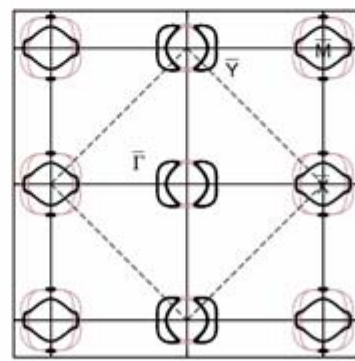
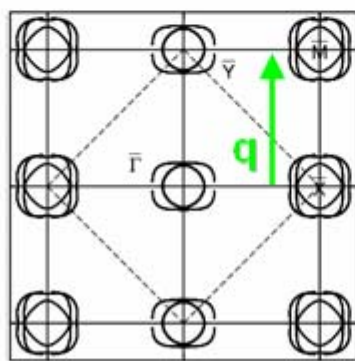
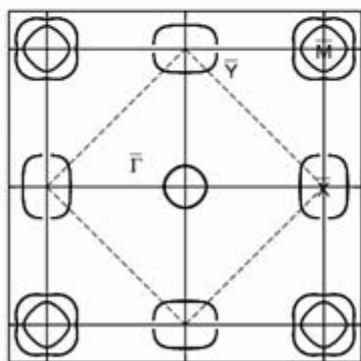
$$m(\Delta) = \sum_{\alpha=1}^5 m_{\alpha}(\Delta) = \sum_{\alpha=1}^5 \sum_{i\mathbf{k}} c_{\alpha, i\mathbf{k}} c_{\alpha, i\mathbf{k}+\mathbf{Q}}^*$$

Magnetic moment

$$\Delta = m(\Delta) I$$

Self-consistency
condition

I is the Stoner- or
Hund's-rule exchange
coupling constant for Fe



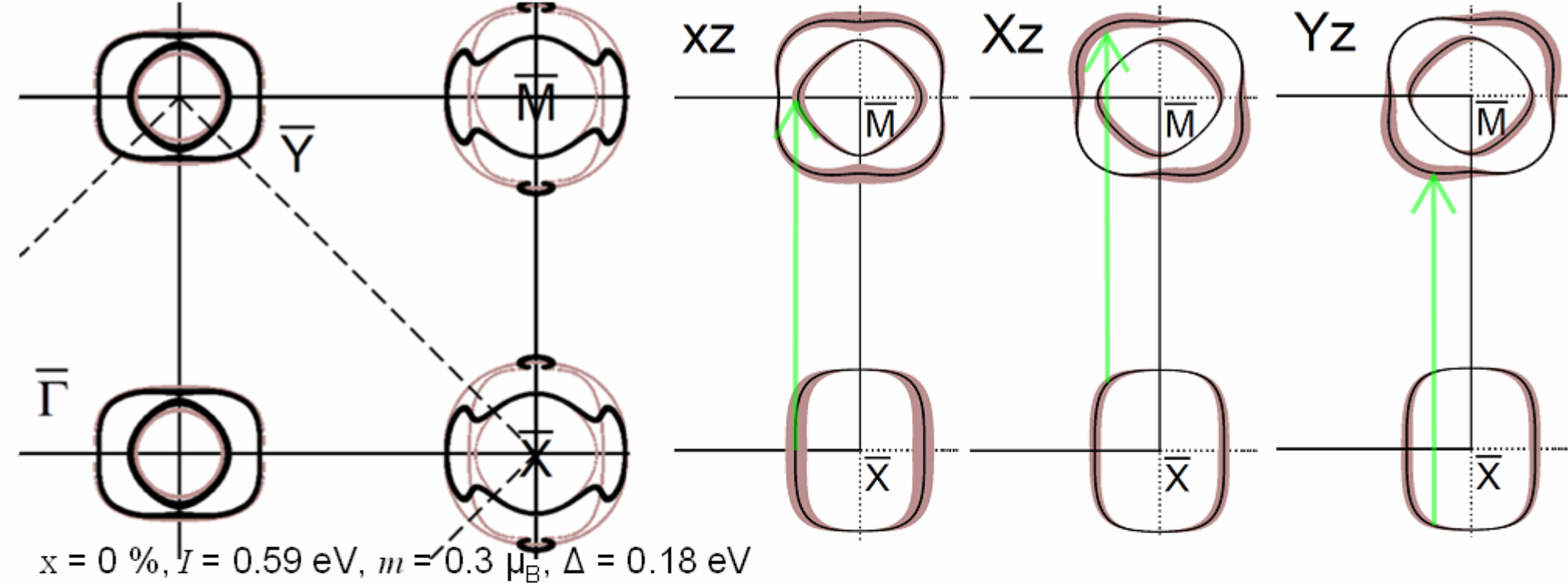
1) Start from PM bands

2) Fold in ...

3) Couple with Δ ...

4) Compute $m(\Delta)$

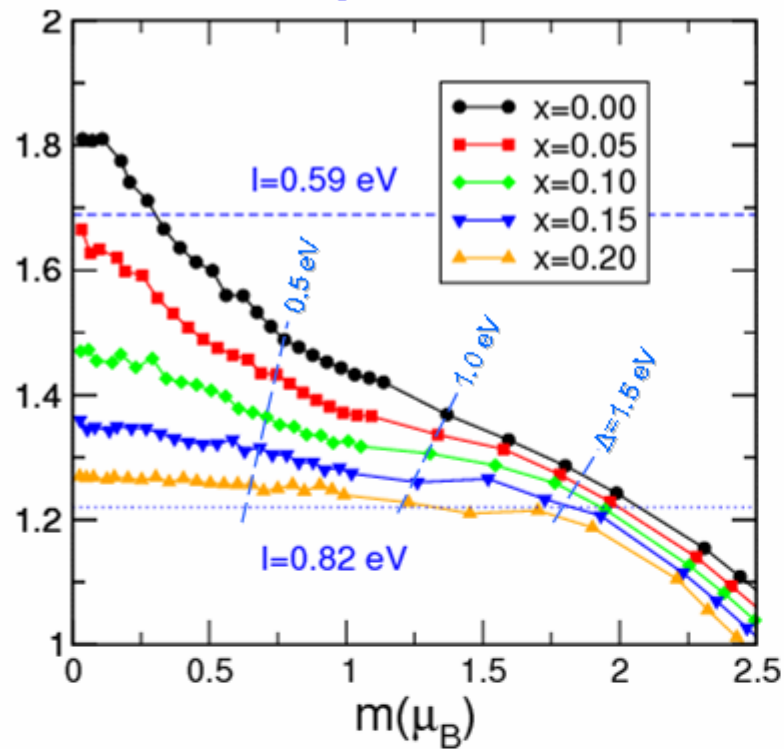
5) Solve $m(\Delta) = \Delta/I$



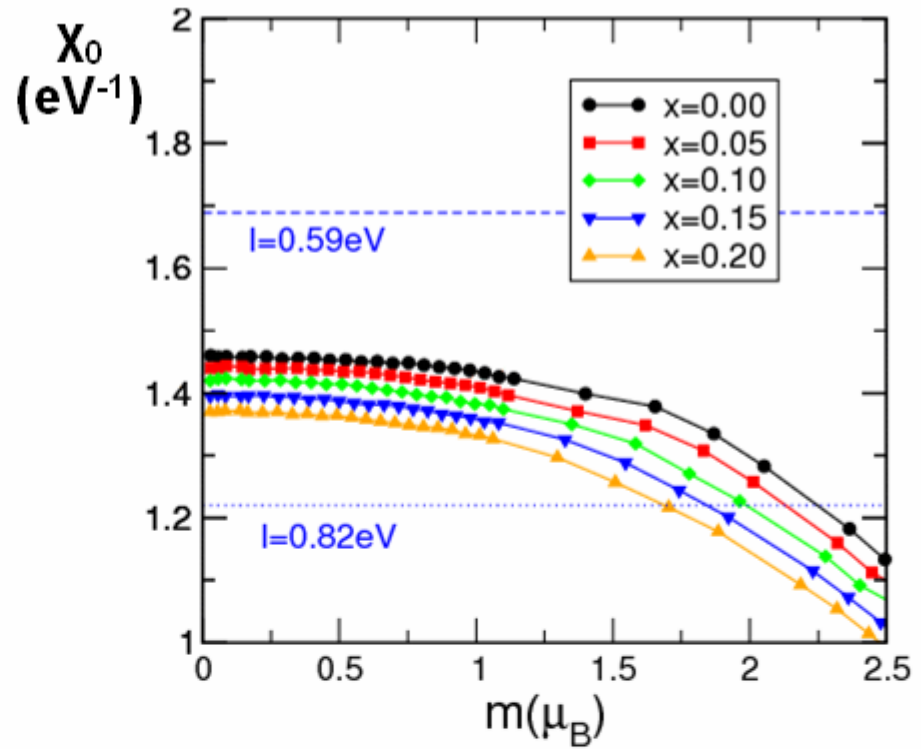
The exchange-coupling matrix, $\mathbf{\Delta}$, is diagonal (to a good approximation) so that only Fermi-surface sheets with similar Fe characters couple. Below, to the right, we show the paramagnetic \bar{M} -centered hole pockets and the \bar{X} -centered electron pocket, decorated with the common Wannier-function characters, which are xz , Xz , and Yz . The stripe translation \bar{Y} , brings those sheets on top of each other and, as seen on step to the left, those parts with good nesting and a common character do gap. The gapped Fermi surface has "propeller" shape, as was recently observed with ARPES by Borisenko et al.. The gapping of the xz , Xz , and Yz characters leads to "bonds" with those characters and hence, to a SDW-induced contraction along x , i.e. in the F -ordered direction. We believe that this is the observed orthorhombic distortion.

How does Doug's pairing compare with this (Maier et al 09)?

Stripe Y

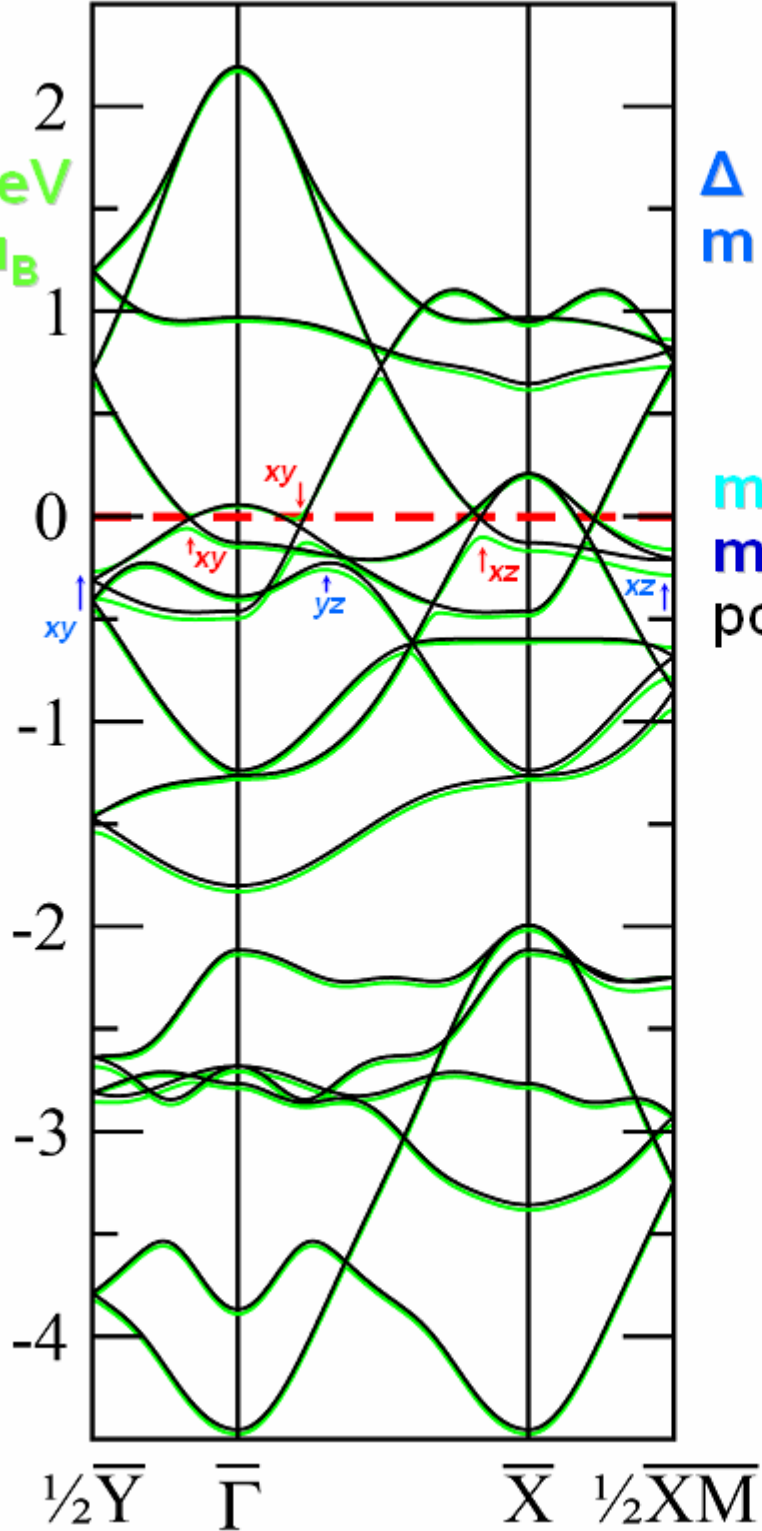


Checkerboard M



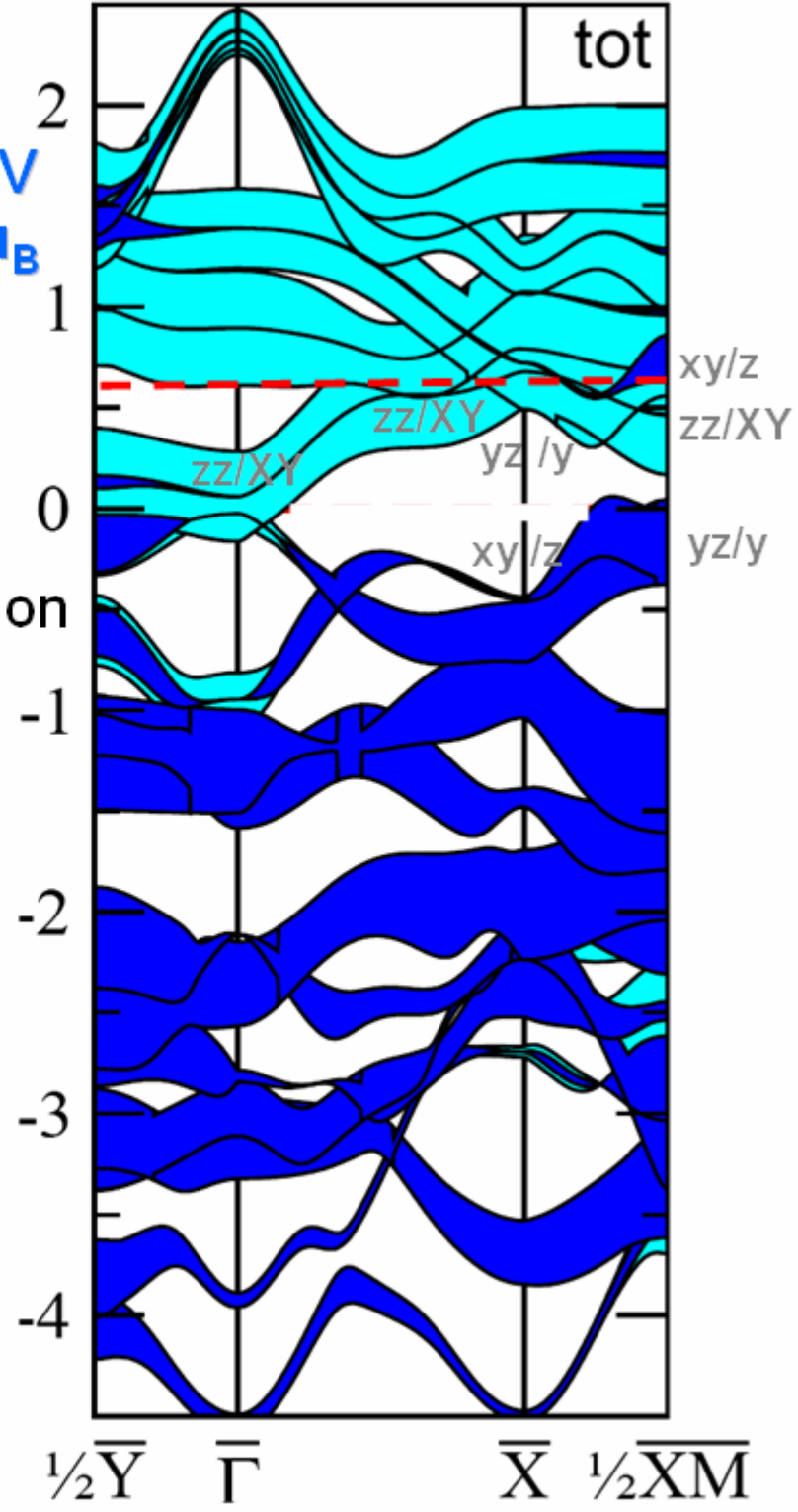
The curves below show for $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$ the bare susceptibility, $\chi_0(m) = m(\Delta)/\Delta$, as a function of the induced moment, $m(\Delta)$, for striped (Y) and checkerboard (M) AFM order and various values of the electron doping x . For a given value of l , the stable moment is the solution of: $\chi_0(m) = 1/l$. The LSDA value $l = 0.82$ eV, predicts that both Y and M orders are stable and with moments $m \sim 2 \mu_B$. Experimentally, only Y order is stable and $m \sim 0.3 \mu_B$. This is consistent with the LDA bands and $l = 0.59$ eV; a reduction presumably due to the strong As p character. With this value of l , our bands also reproduce the disappearance of the moment for $x > 5\%$ in accord with experiments.

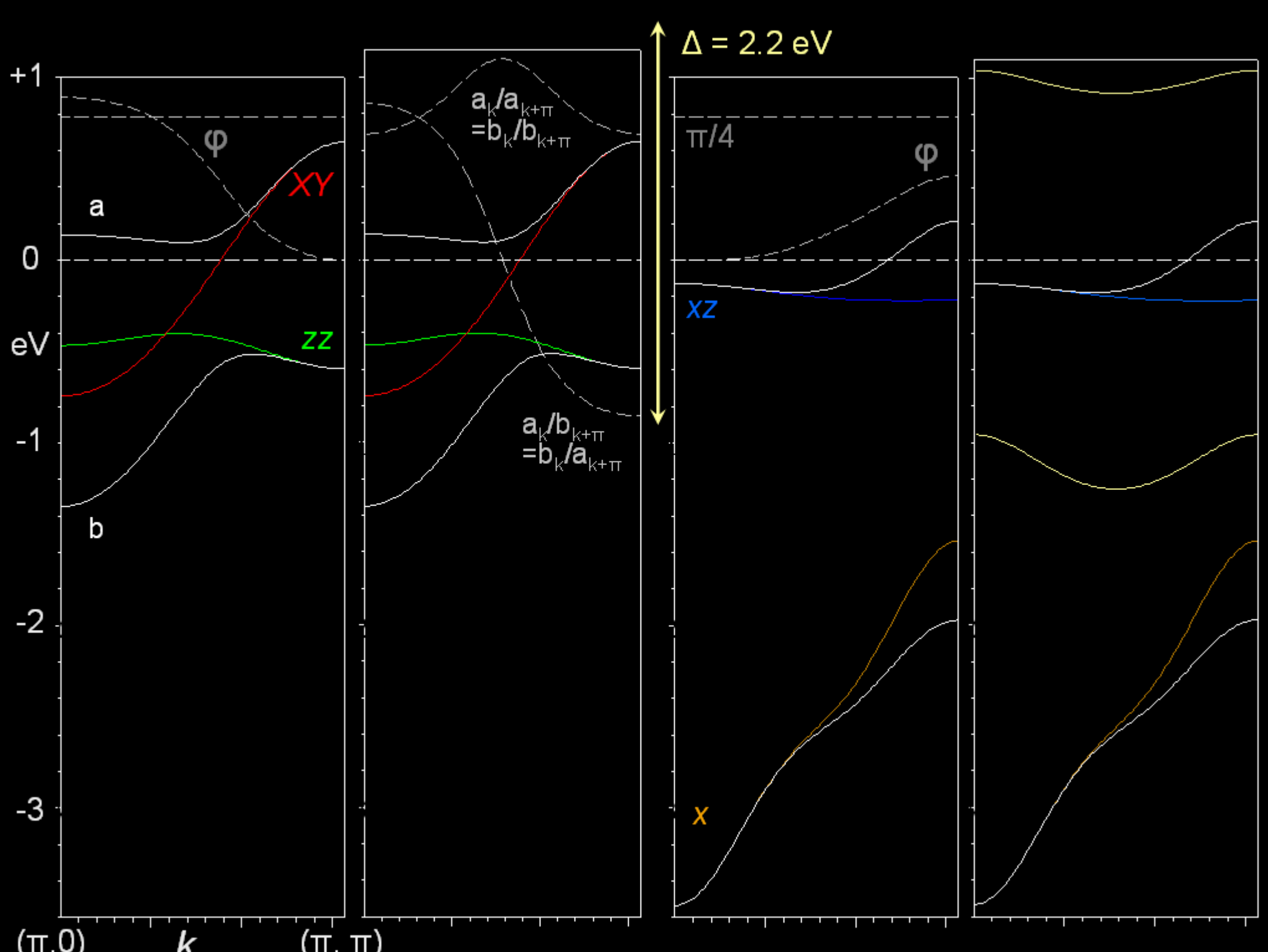
$\Delta = 0.18 \text{ eV}$
 $m = 0.3 \mu_B$

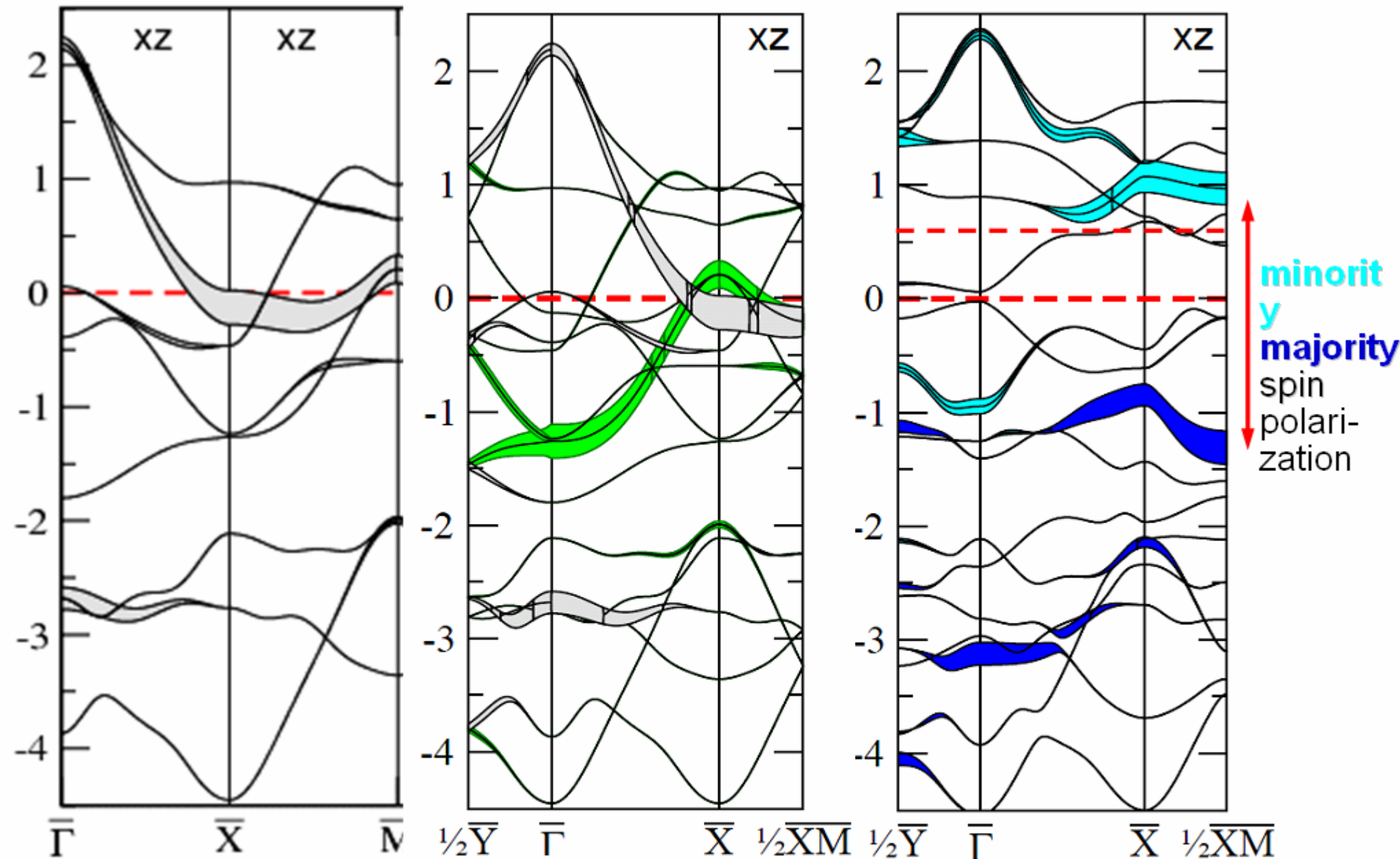


$\Delta = 2.2 \text{ eV}$
 $m = 2.4 \mu_B$

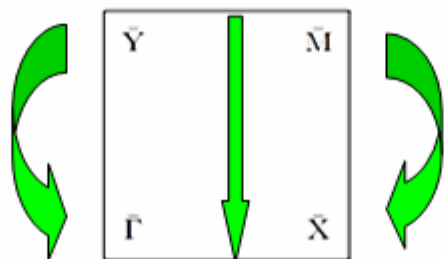
minority
majority
polarization



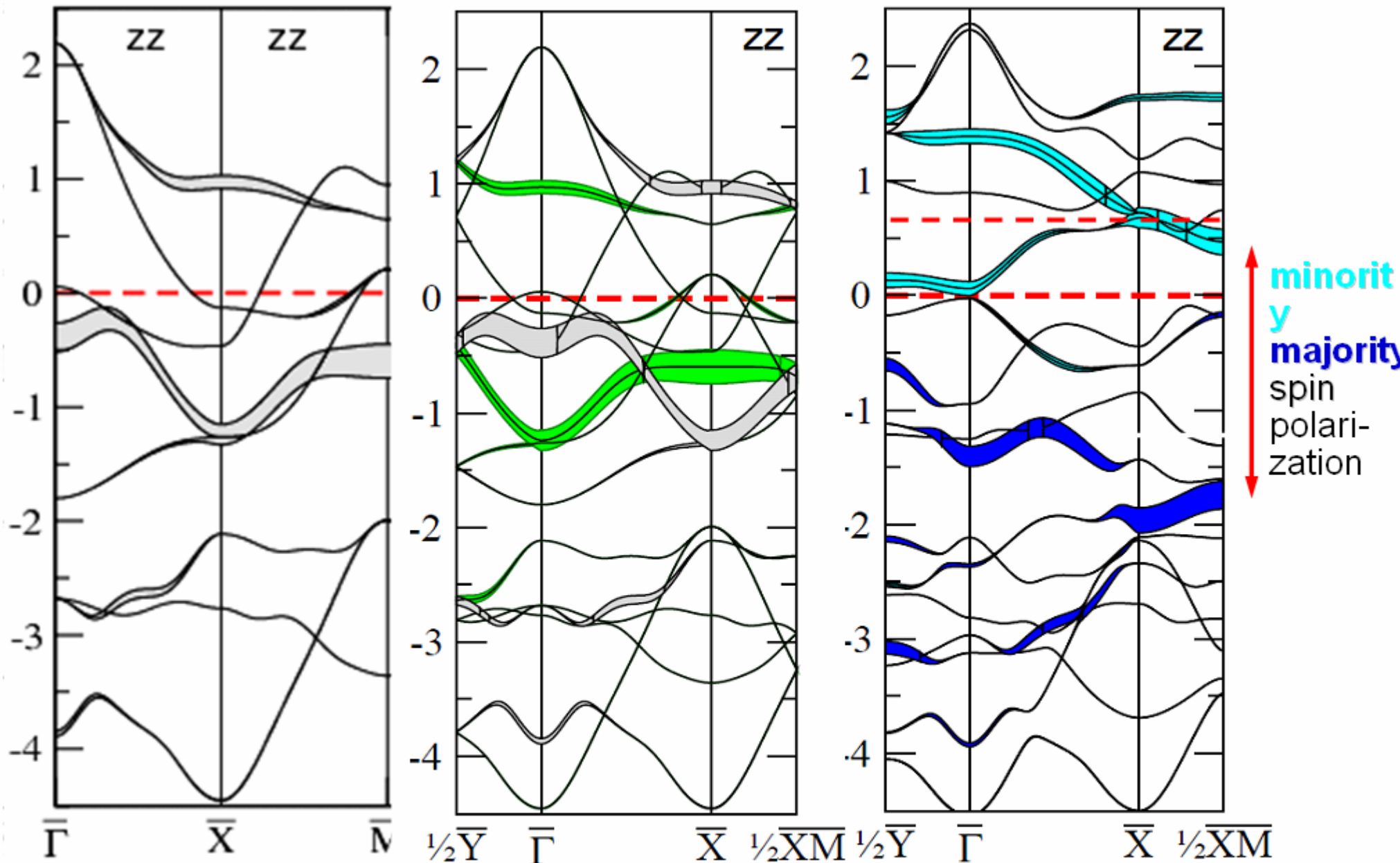




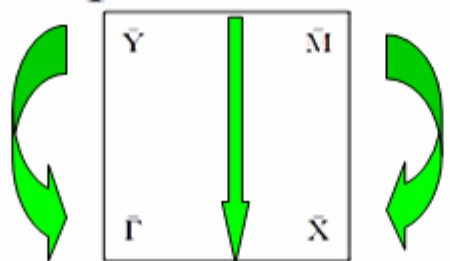
Preparing for the $q=(0,\pi)$ stripes (folding into the small zone):



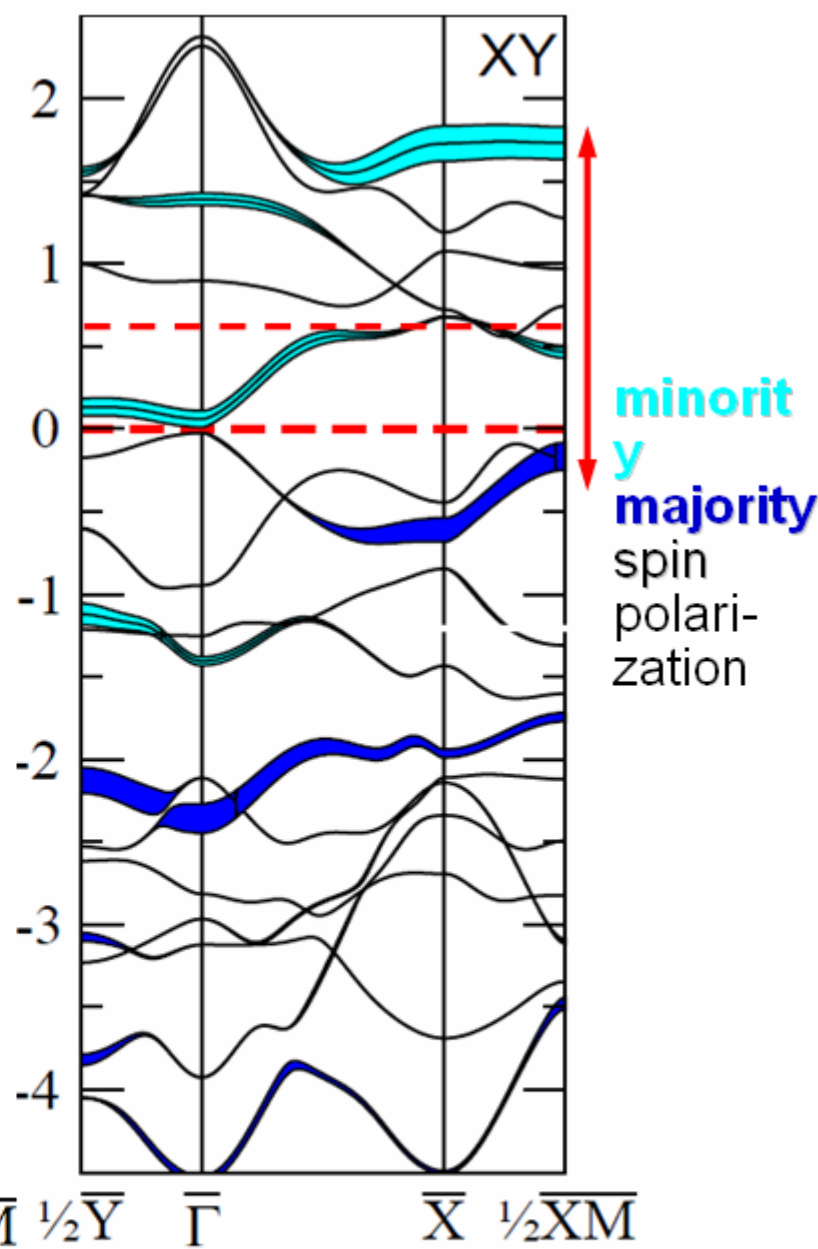
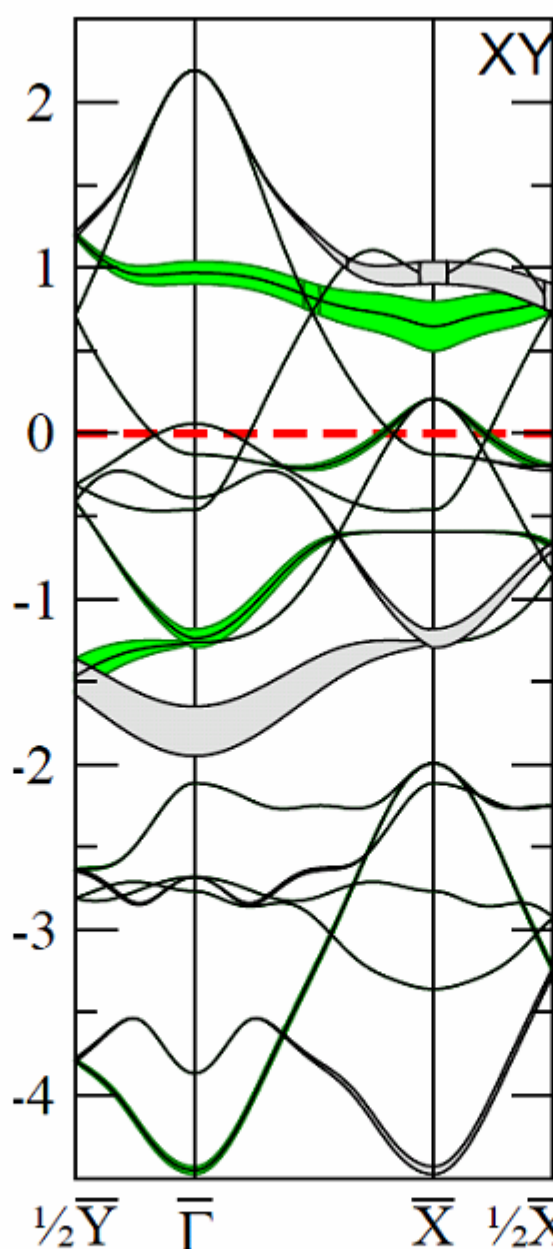
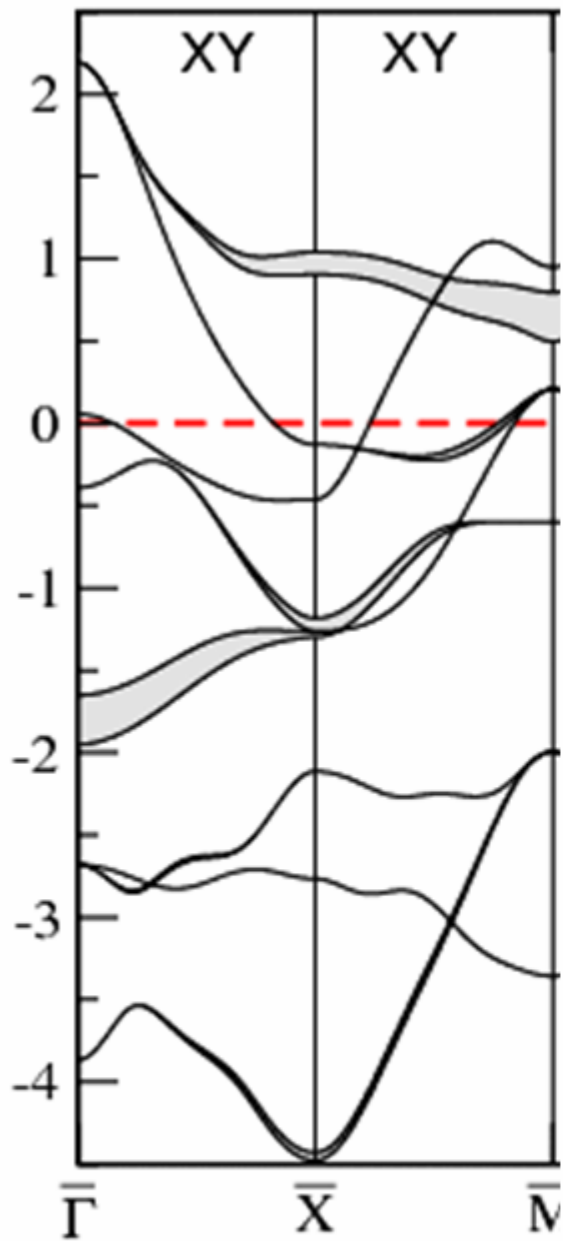
Coupling with $\Delta = mI = 2.2 \text{ eV}$



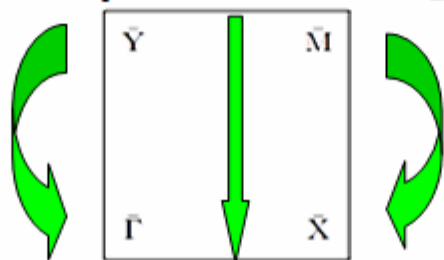
Preparing for the $q=(0,\pi)$ stripes (folding into the small zone):



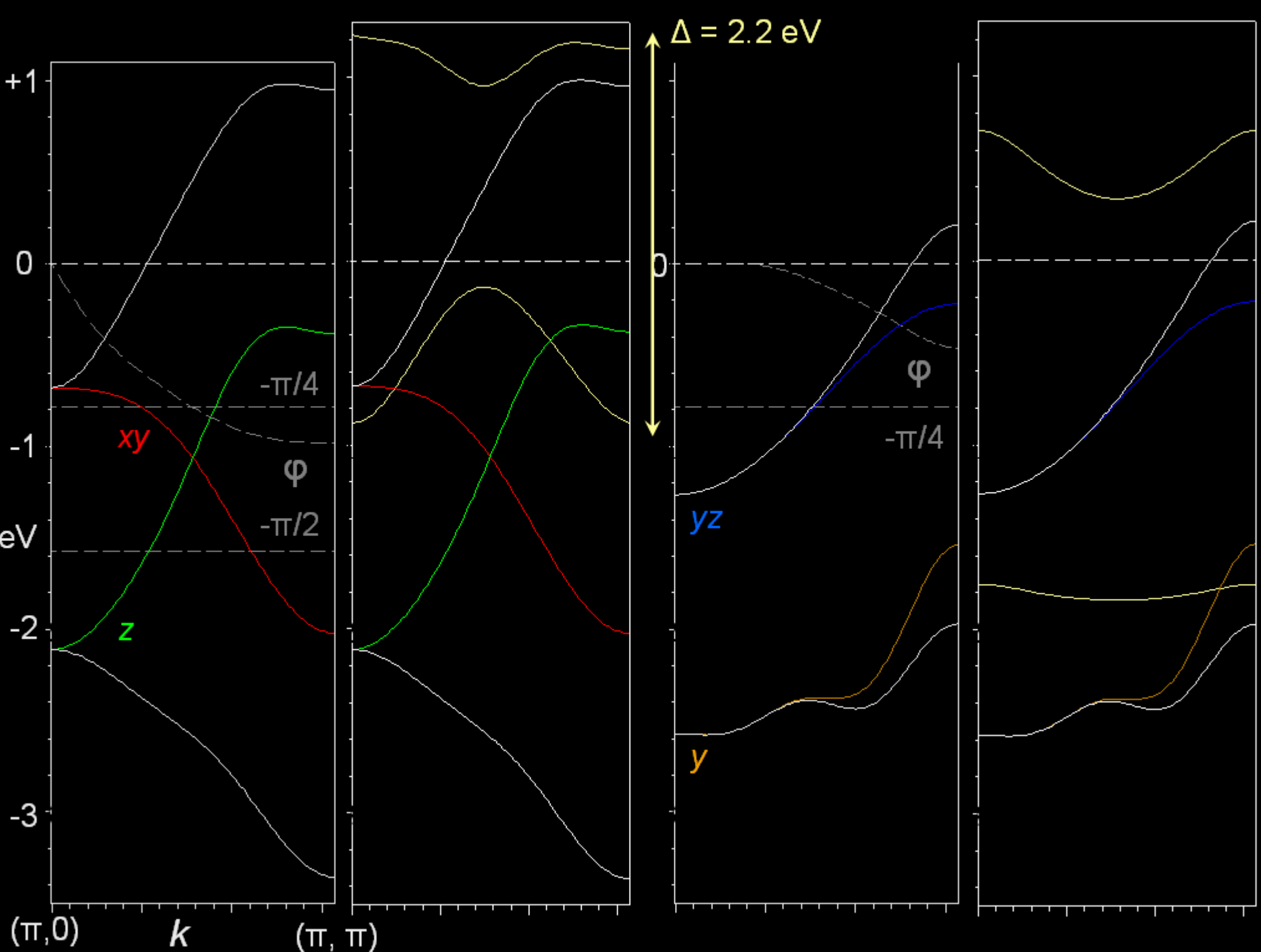
Coupling with $\Delta = mI = 2.2 \text{ eV}$

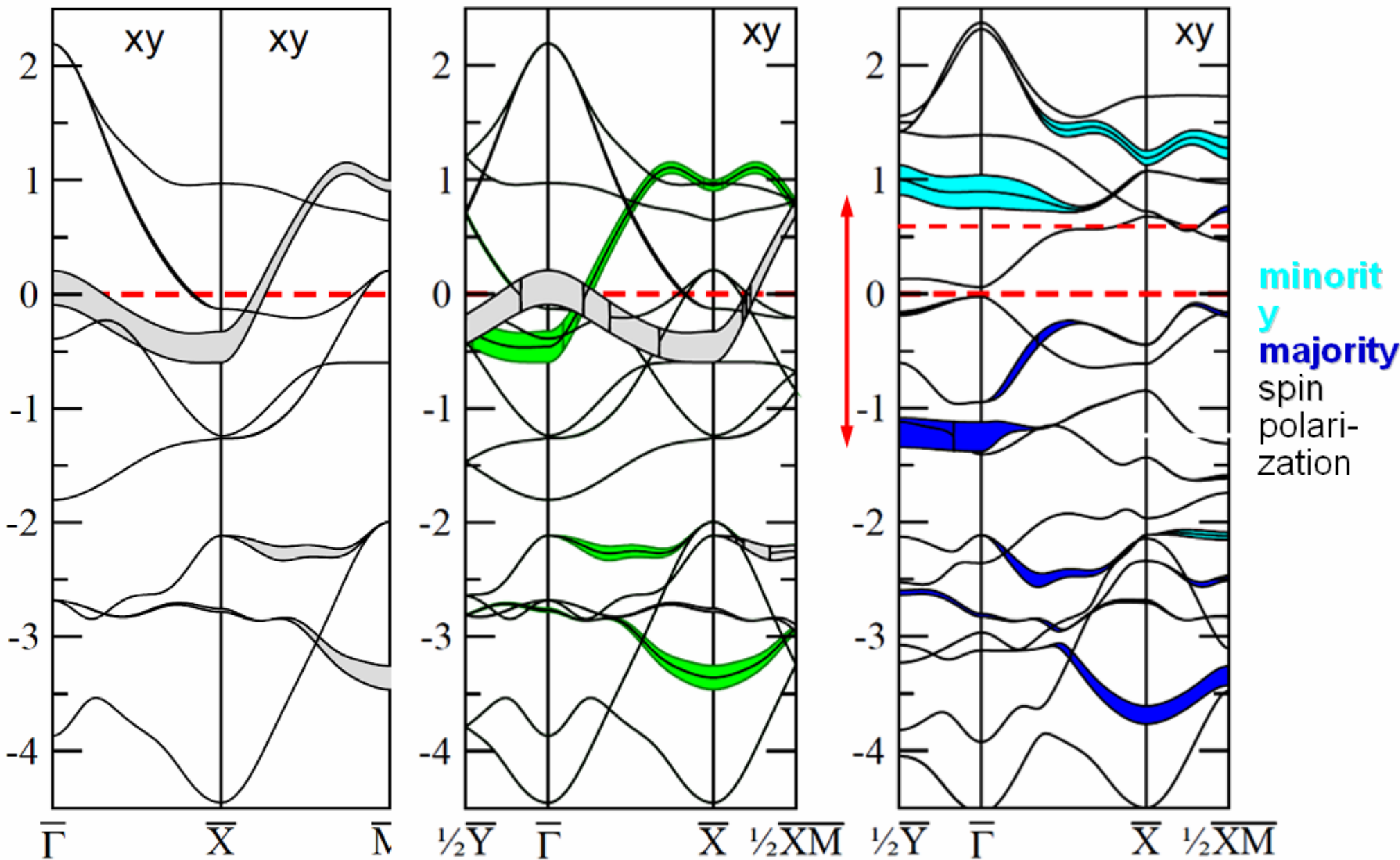


Preparing for the $q=(0,\pi)$ stripes (folding into the small zone):

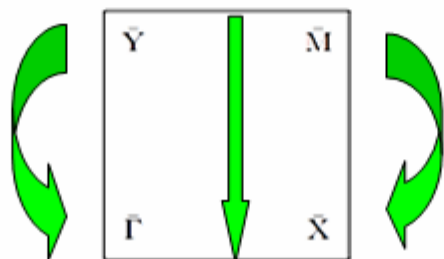


Coupling with $\Delta = mI = 2.2$ eV

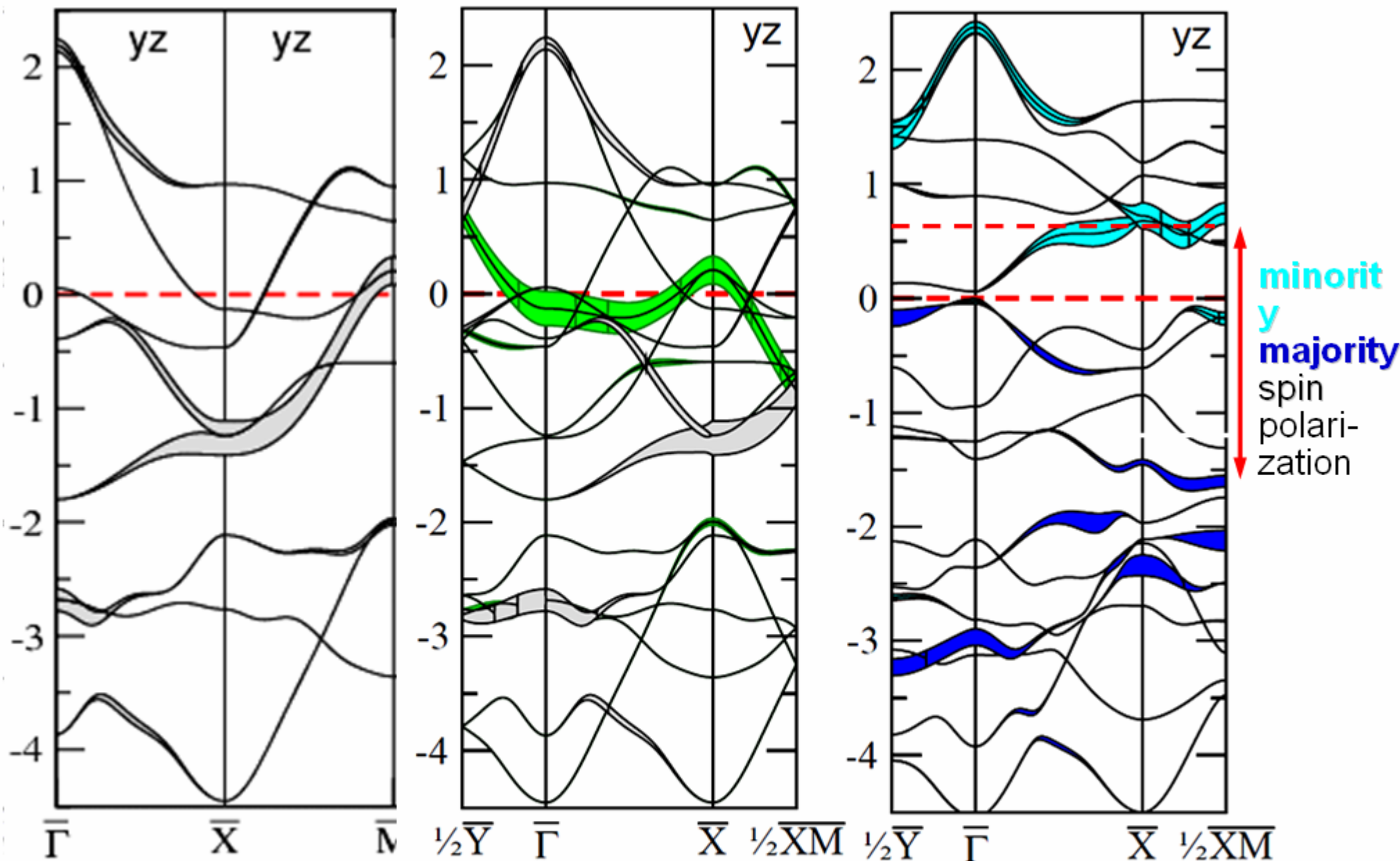




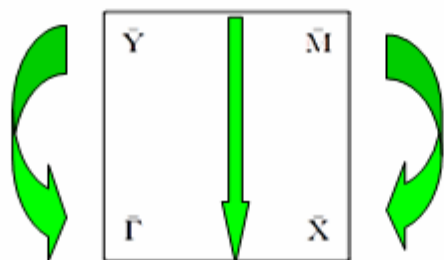
Preparing for the $q=(0,\pi)$ stripes (folding into the small zone):



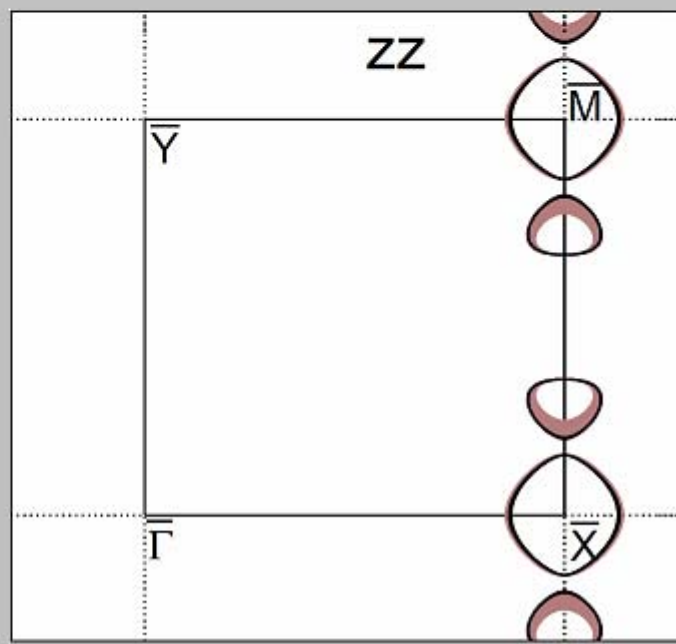
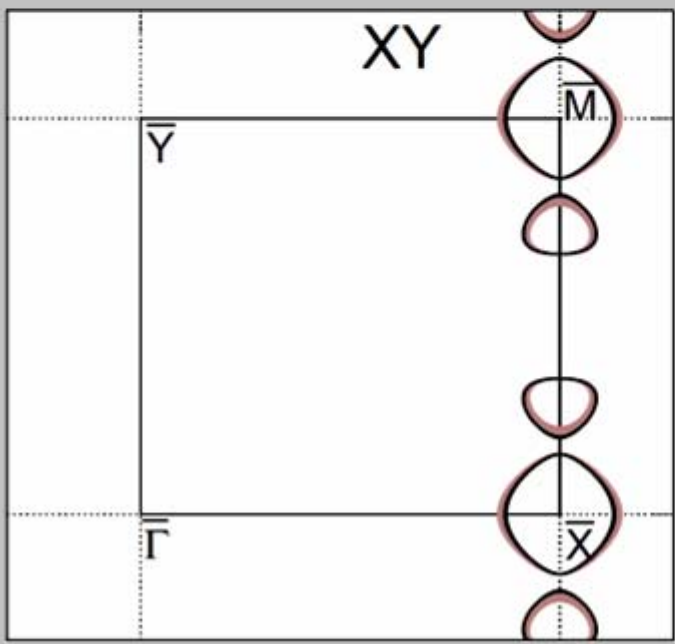
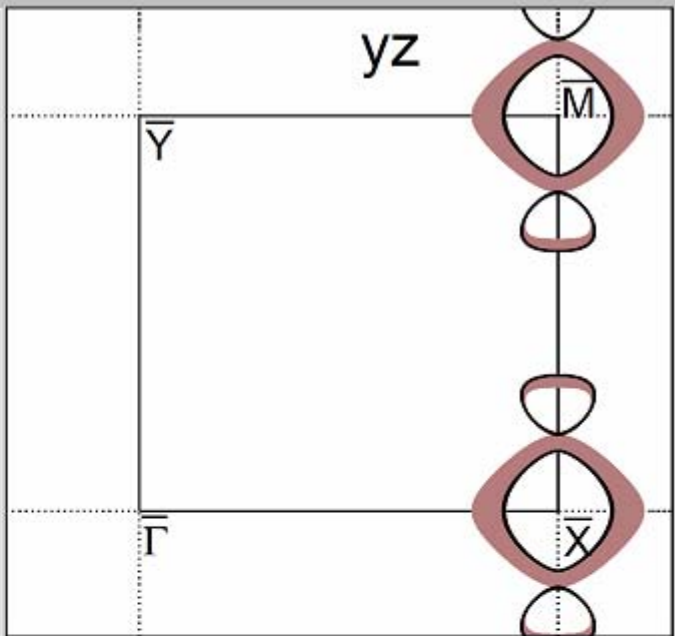
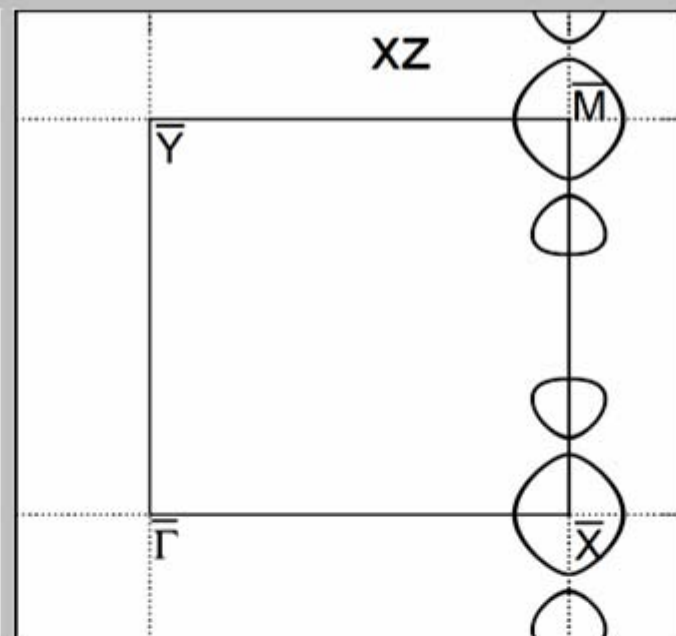
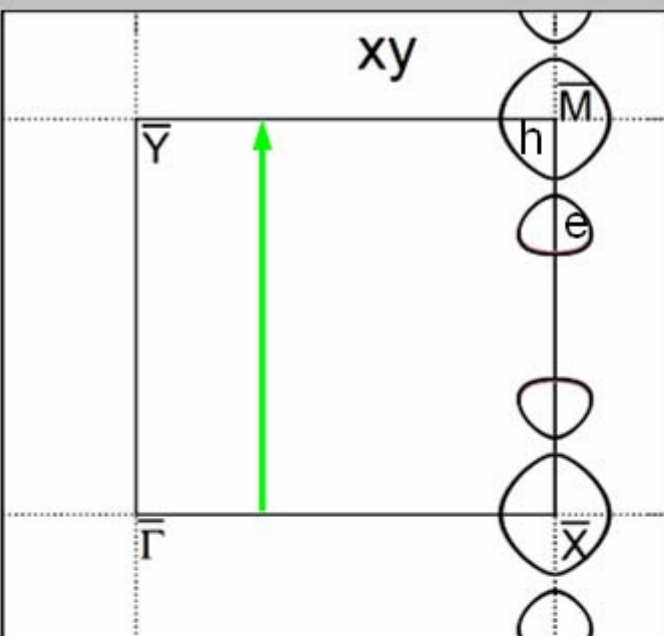
Coupling with $\Delta = mI = 2.2 \text{ eV}$



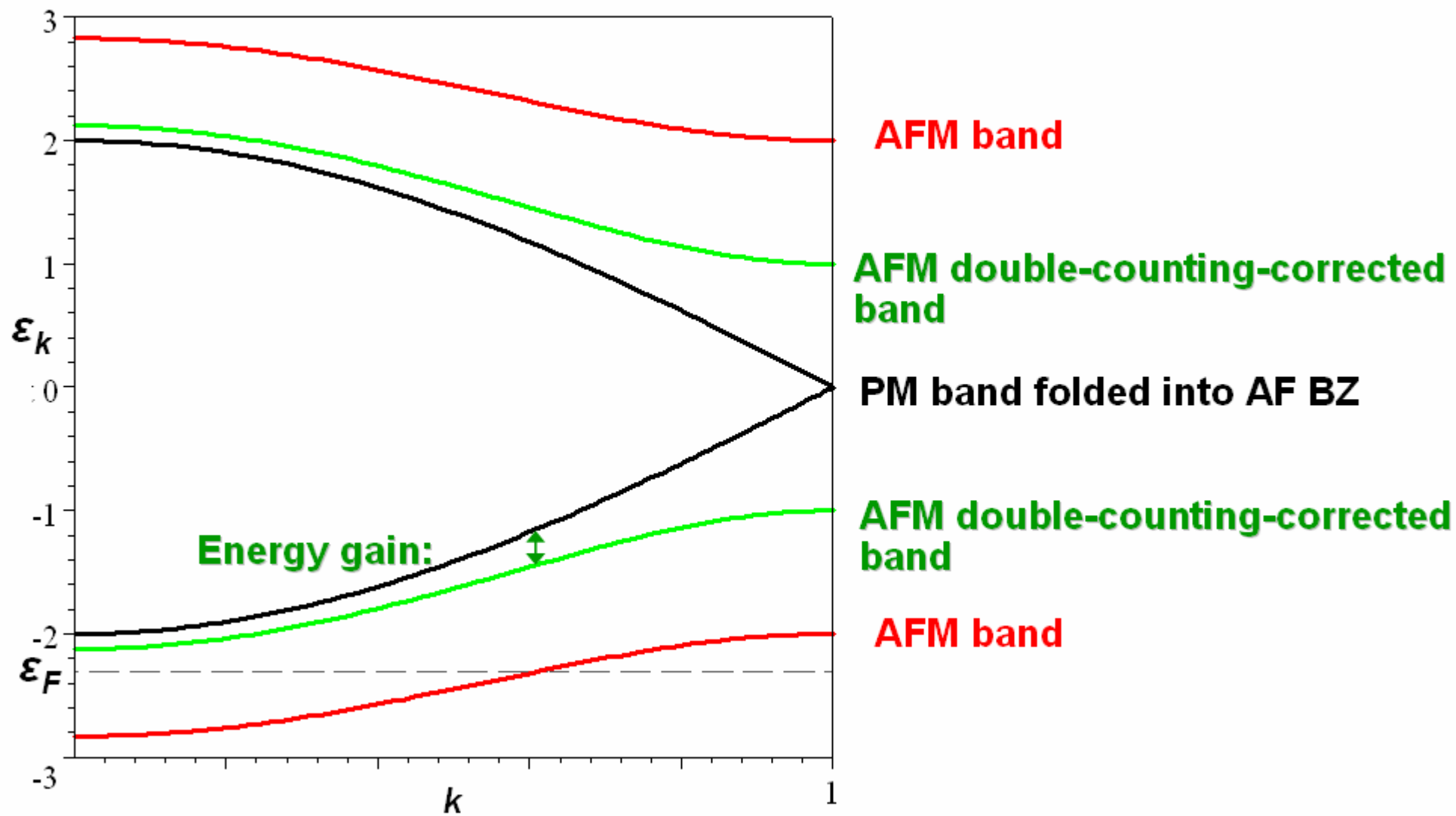
Preparing for the $q=(0,\pi)$ stripes (folding into the small zone):

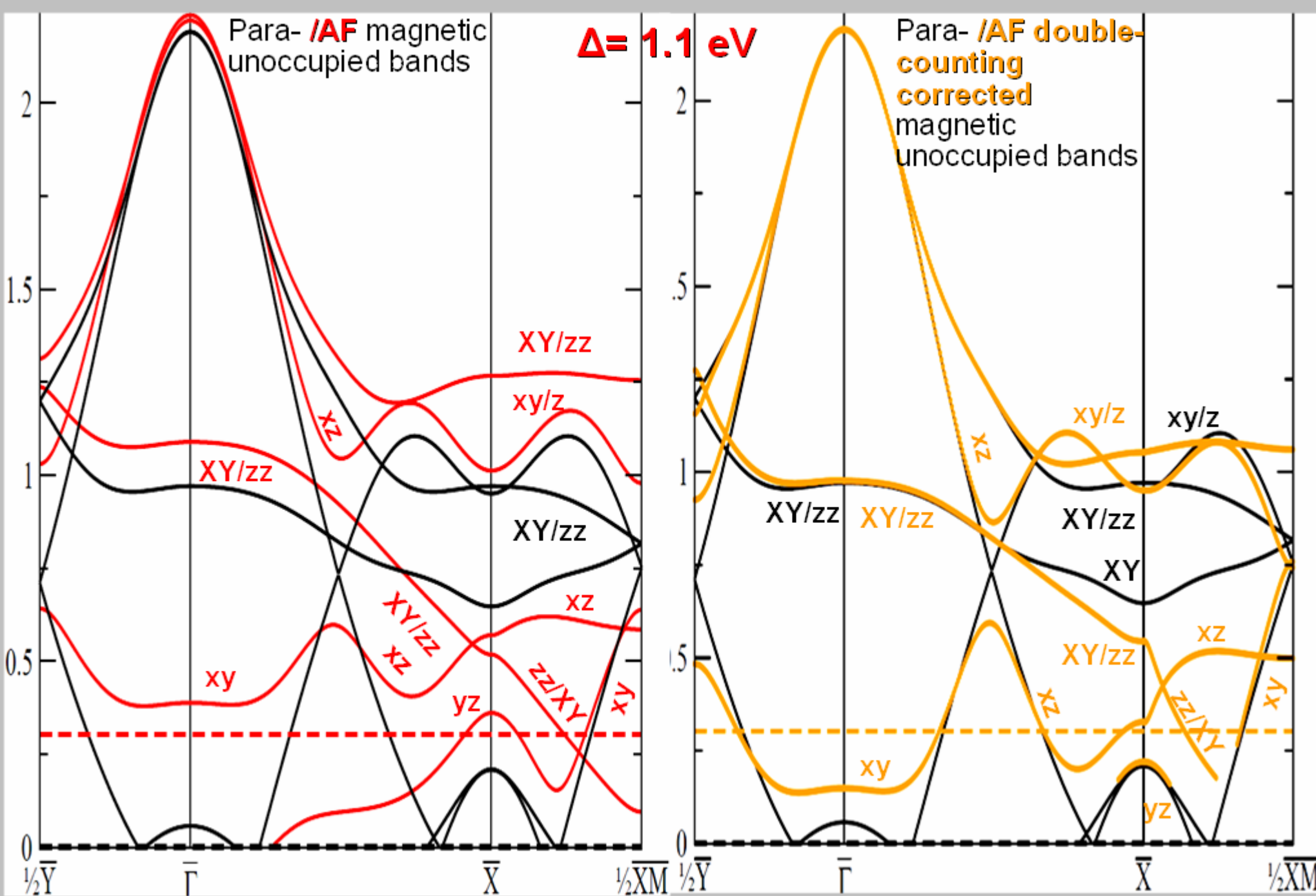


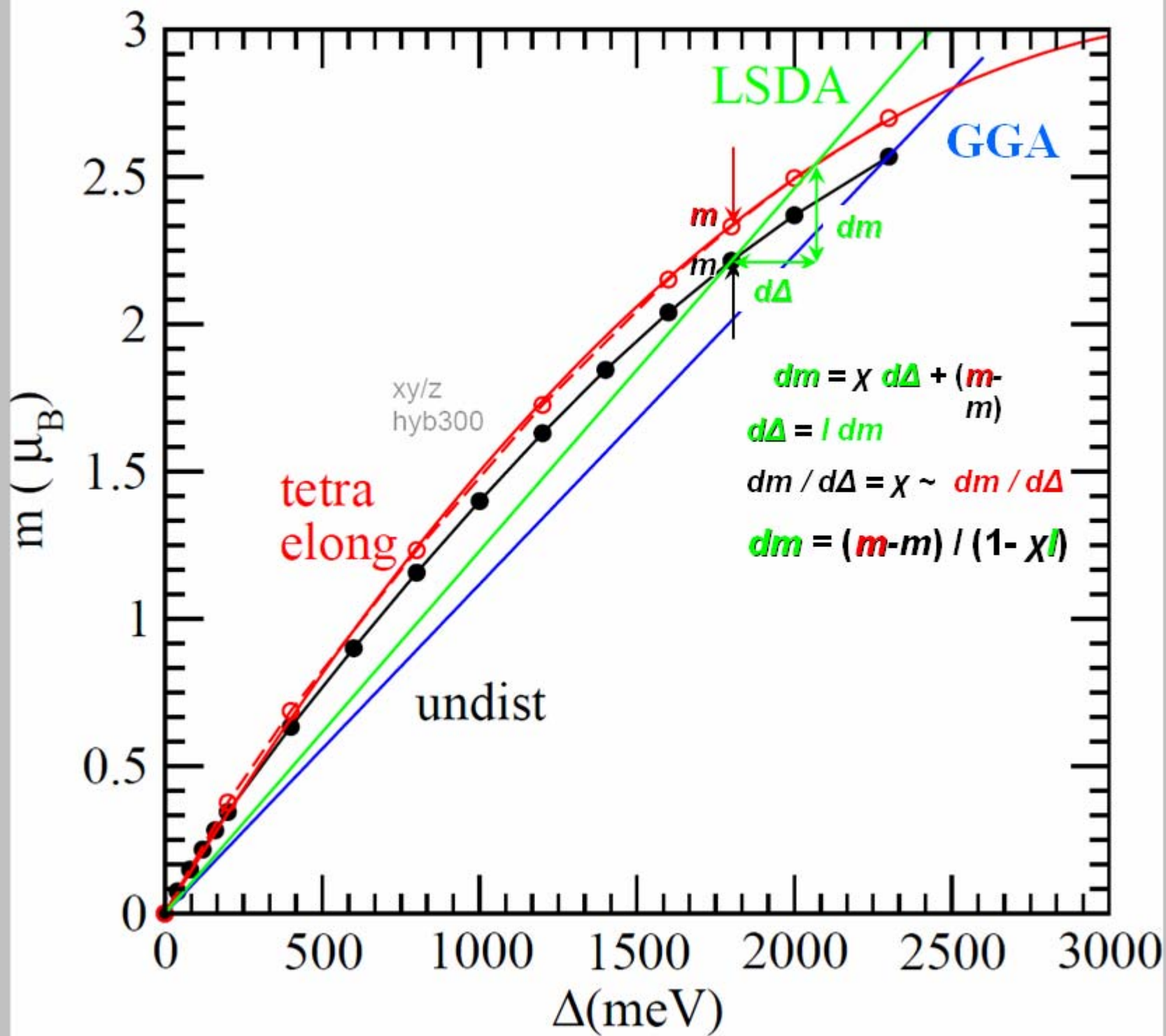
Coupling with $\Delta = mI = 2.2$ eV



**2 μ_B
propeller.
Mostly
minority
spins**

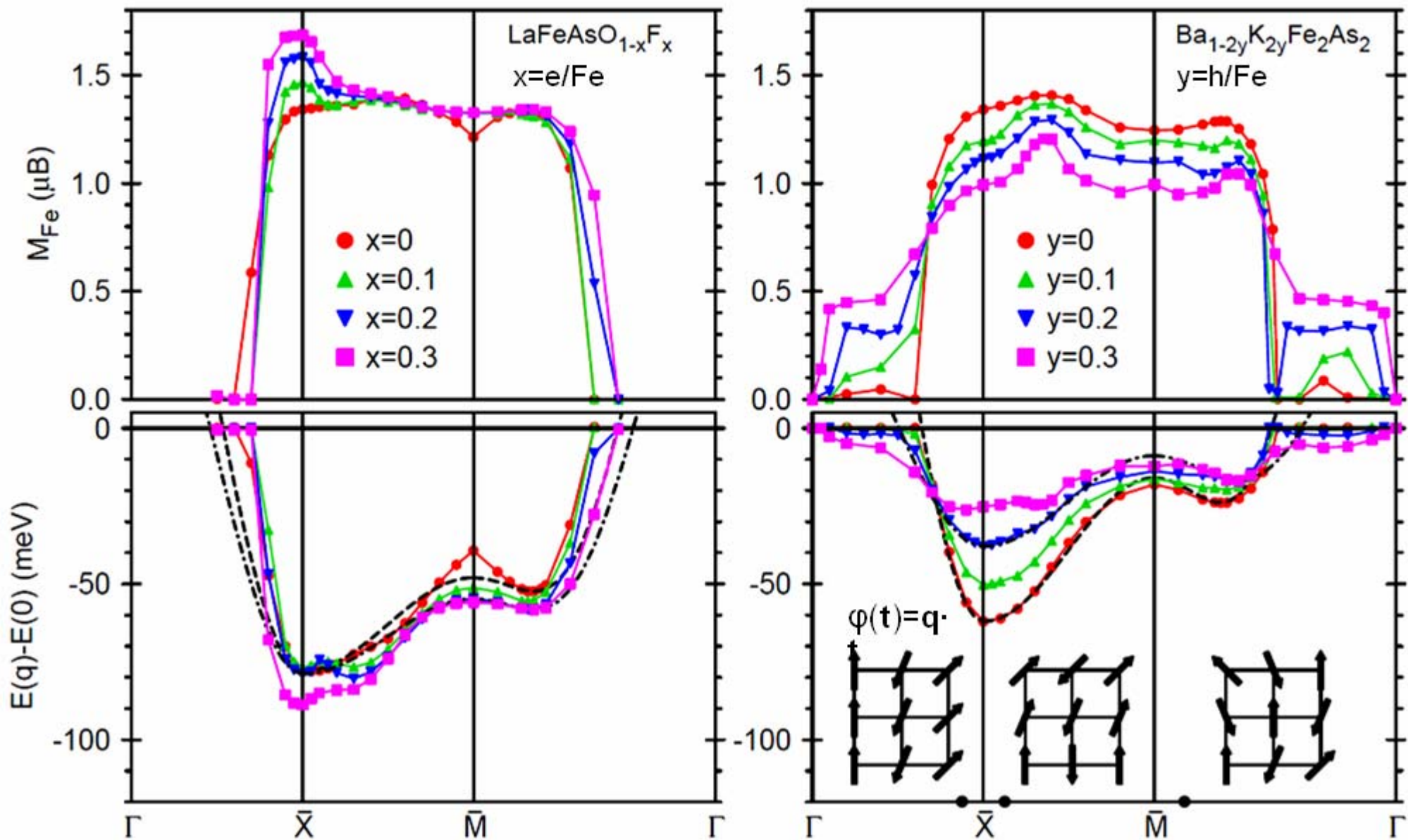




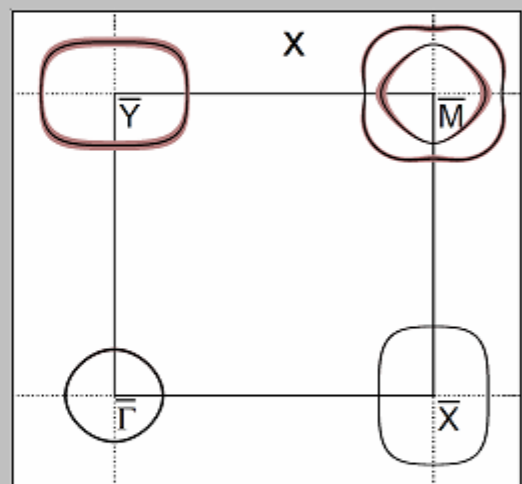
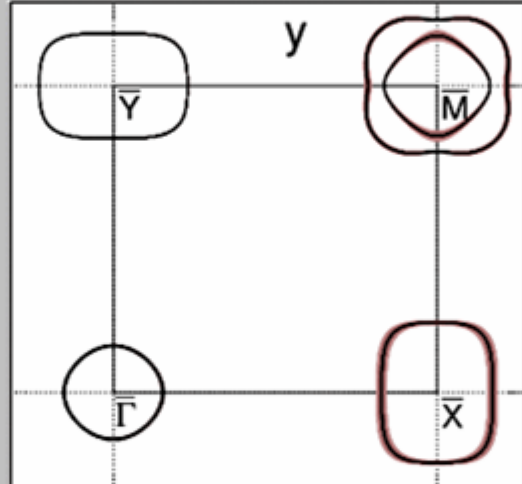
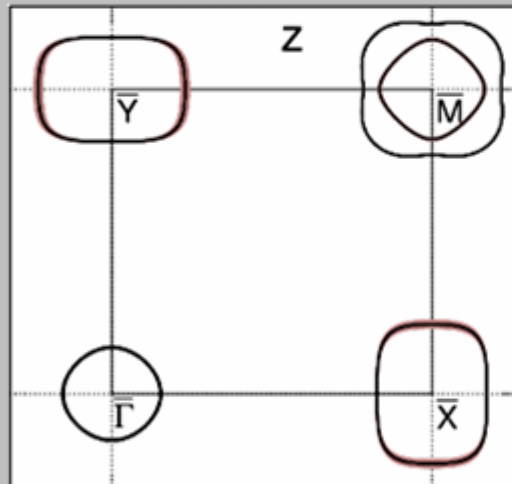
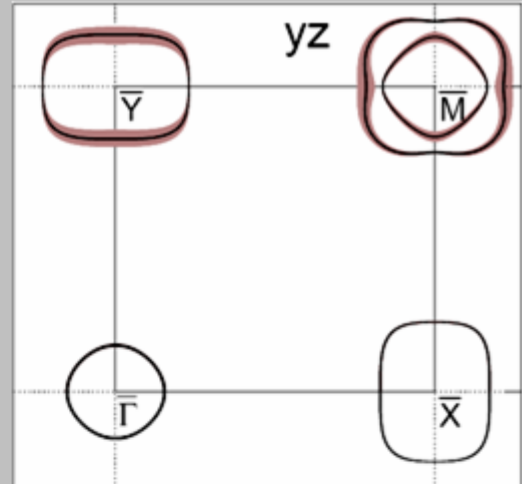
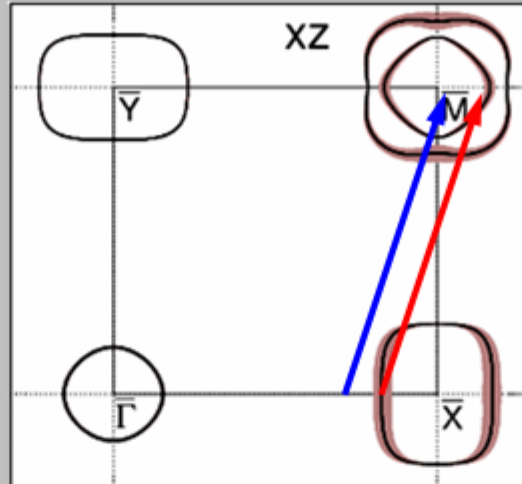
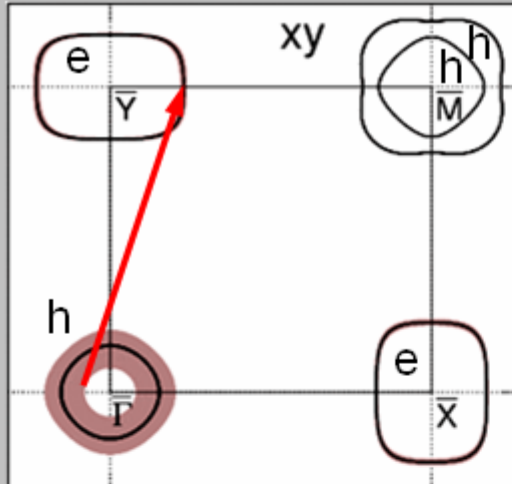


Fe sublattice magnetizations and magnetic energies of spin spirals calculated by LMTO-LSDA for the experimental structure.

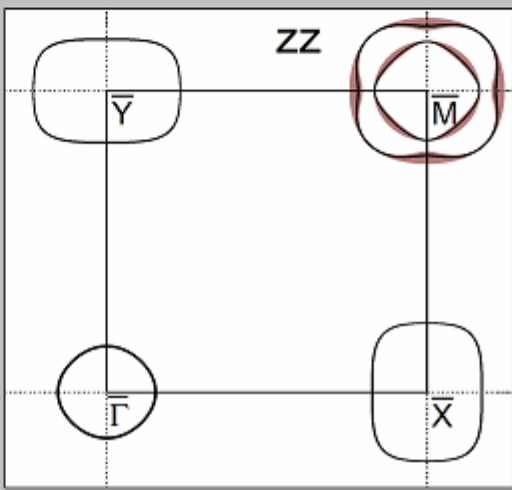
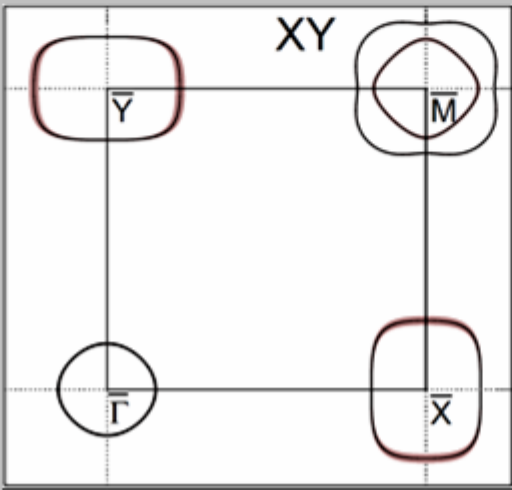
A. Yaresko et al. PR B 79, 114503 (2009)



$1/5 \times$

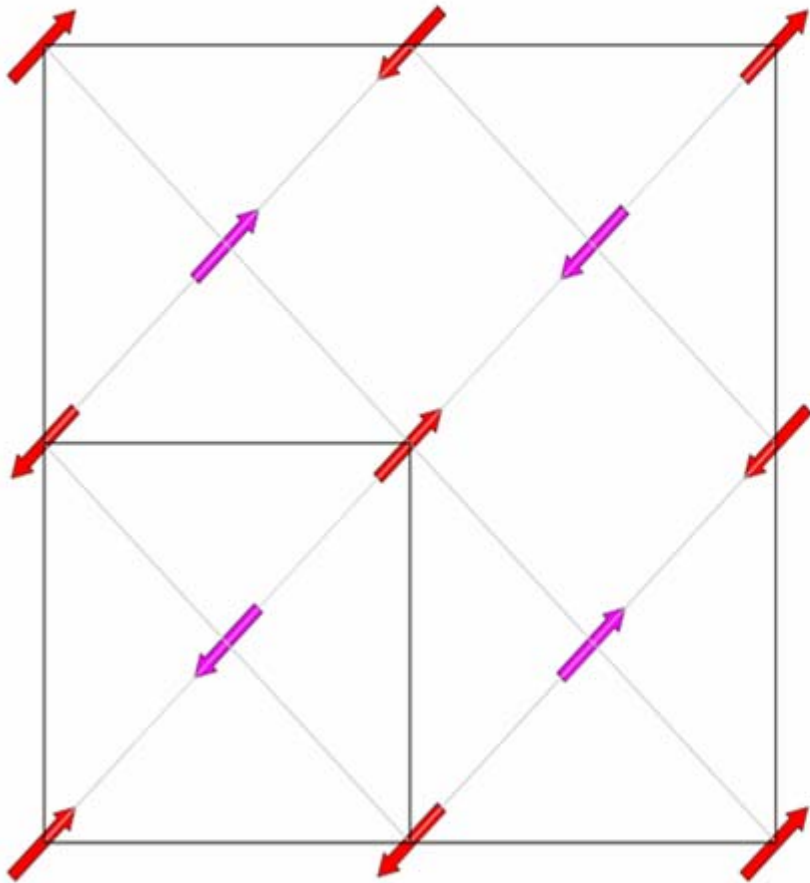


End of region of flat SDW energy for undoped LaOFeAs.



Second minimum for electron doping

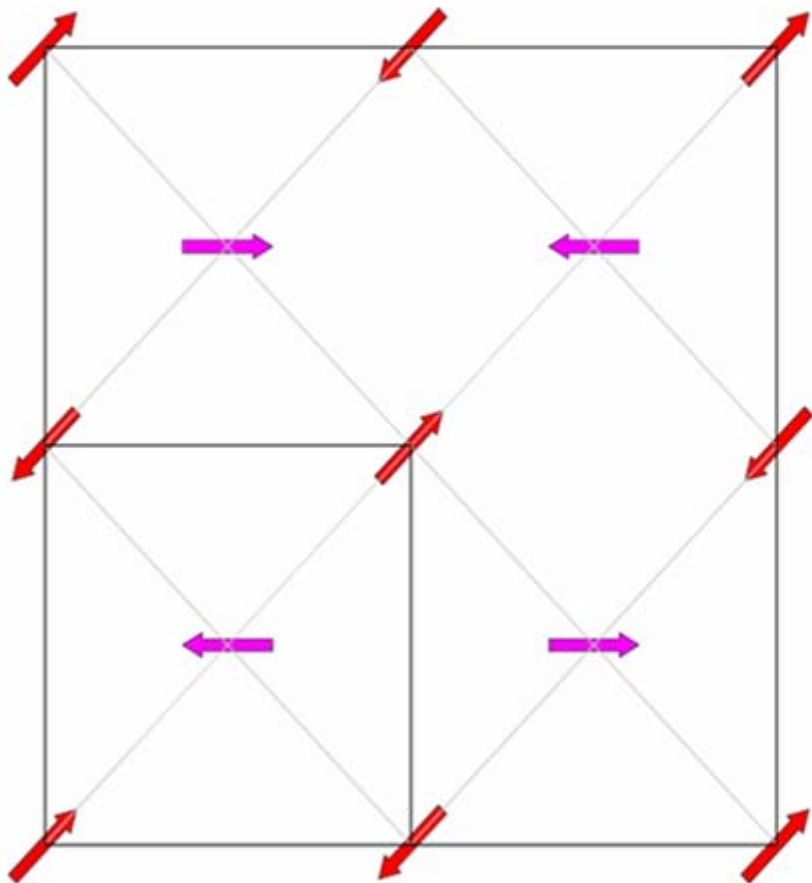
does the Heisenberg model work for undoped compounds?



two AFM sublattices at $\mathbf{q}=(\pi,0)$
each Fe has two FM and two AFM
n.n.:

$$\begin{aligned} E_H &= j_1[\cos \alpha + \cos(\pi - \alpha)] - 2j_2 \\ &= -2j_2 \end{aligned}$$

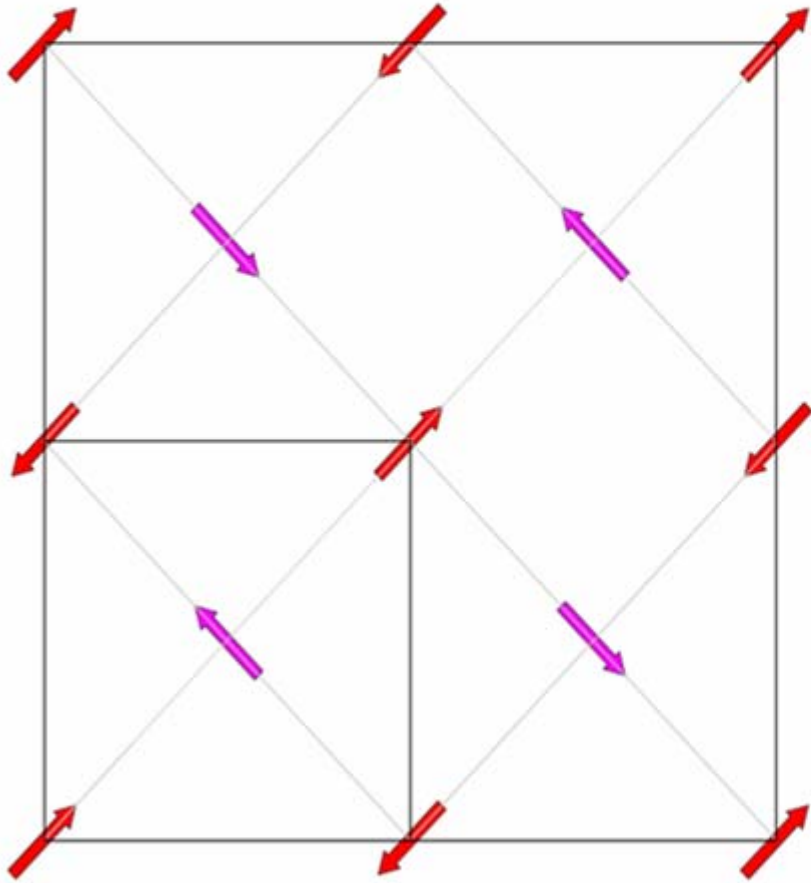
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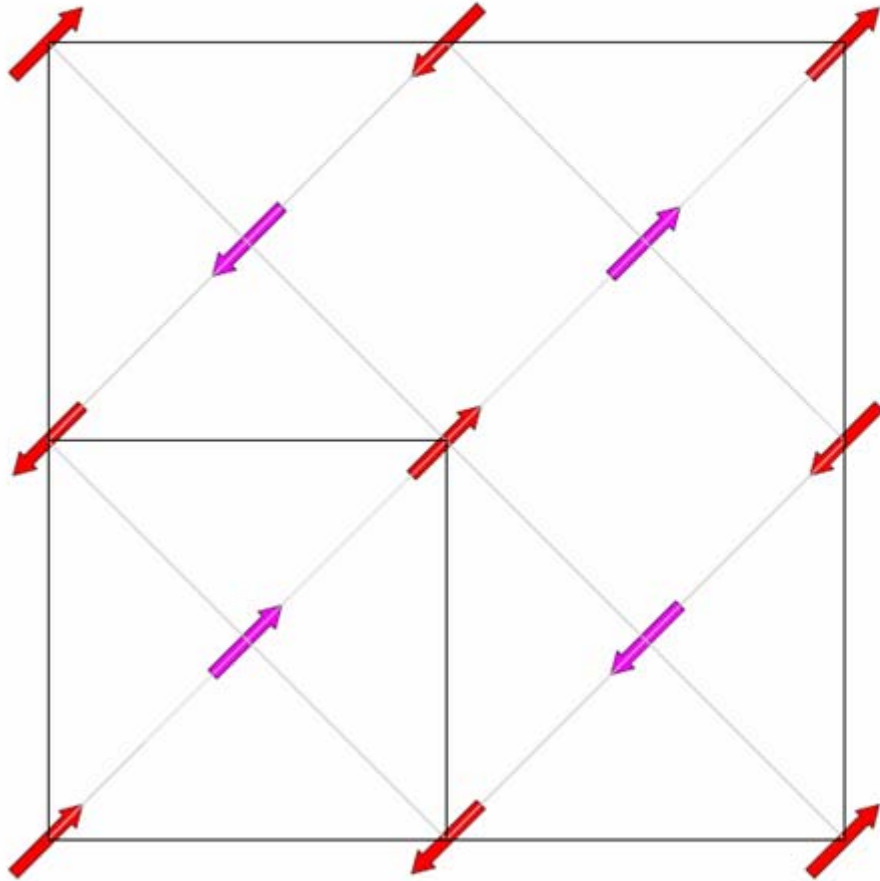
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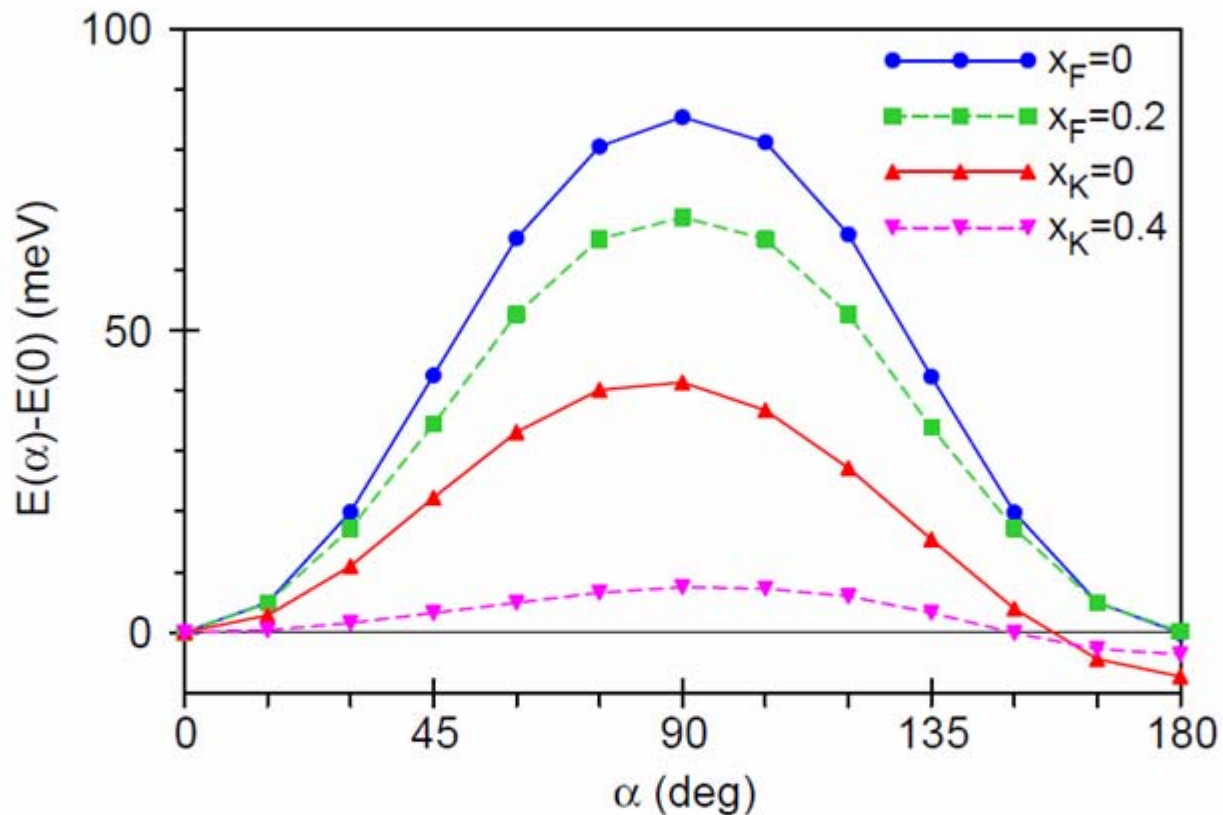
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each Fe has two FM and two AFM
n.n.:

$$\begin{aligned} E_H &= j_1[\cos \alpha + \cos(\pi - \alpha)] - 2j_2 \\ &= -2j_2 \end{aligned}$$

NO!



- collinear stripe AFM order is preferable
- $E(\alpha) \sim \sin^2 \alpha \sim -(\mathbf{S}_i \cdot \mathbf{S}_j)^2$
- the energy variation is suppressed by doping, especially in BaFe_2As_2 .

The End