

QCD effects in exclusive Higgs production

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Higgs Identification at KITP
December 12, 2012



Outline

- Theory errors in experimental searches
- Brief discussion of inclusive cross sections, for purposes of comparison when cuts added
- Jet vetoes in VH, gluon-fusion

Effects of theory uncertainties

- CMS PAS HIG-11-024: (WW channel) “The overall signal efficiency uncertainty... is dominated by the theoretical uncertainty due to missing higher-order corrections”
- ATLAS CERN-PH-EP-2012-013 ($\gamma\gamma$): uncertainties due to QCD scale variation one of the two dominant systematic effects (along with photon reconstruction+ID efficiency)

Source	Affected Processes	Typical uncertainty
PDFs+ α_s (cross sections)	$gg \rightarrow H, t\bar{t}H, gg \rightarrow VV$ VBF $H, VH, VV@NLO$	$\pm 8\%$ $\pm 4\%$
Higher-order uncertainties on cross sections	total inclusive $gg \rightarrow H$ inclusive “ gg ” $\rightarrow H + \geq 1$ jets inclusive “ gg ” $\rightarrow H + \geq 2$ jets VBF H associated VH $t\bar{t}H$ uncertainties specific to high mass Higgs boson, see Section 2.1 V VV up to NLO $gg \rightarrow VV$ $t\bar{t}$, incl. single top productions for simplicity	$+12\%$ -7% $\pm 20\%$ $\pm 20\%$ (NLO), $\pm 70\%$ (LO) $\pm 1\%$ $\pm 1\%$ $+4\%$ -10% $\pm 30\%$ $\pm 1\%$ $\pm 5\%$ $\pm 30\%$ $\pm 6\%$
acceptance	acceptance for $H \rightarrow WW \rightarrow l\nu l\nu$ events	$\pm 2\%$
phenomenology	modelling of underlying event and parton showering fake lepton probability ($W + jets \rightarrow ll^{fake}$)	$\pm 10\%$ $\pm 40\%$
luminosities	ATLAS and CMS uncertainties on their luminosity measurements	$\pm 3.7\%$, $\pm 4.5\%$

from G. Rolandi,
HCP 2011

Effects of theory uncertainties

Source (0-jet)	Signal (%)	Bkg. (%)
Inclusive ggF signal ren./fact. scale	13	-
1-jet incl. ggF signal ren./fact. scale	10	-
PDF model (signal only)	8	-
QCD scale (acceptance)	4	-
Jet energy scale and resolution	4	2
<i>W</i> +jets fake factor	-	5
<i>WW</i> theoretical model	-	5
Source (1-jet)	Signal (%)	Bkg. (%)
1-jet incl. ggF signal ren./fact. scale	26	-
2-jet incl. ggF signal ren./fact. scale	15	-
Parton shower/ U.E. model (signal only)	10	-
<i>b</i> -tagging efficiency	-	11
PDF model (signal only)	7	-
QCD scale (acceptance)	4	2
Jet energy scale and resolution	1	3
<i>W</i> +jets fake factor	-	5
<i>WW</i> theoretical model	-	3

systematics in the *WW* channel, from J. Qian

Inclusive cross sections

- How well do we know the inclusive gluon-fusion cross section? Receives several large corrections at higher orders

NLO in the EFT:

analytic continuation to
time-like form factor

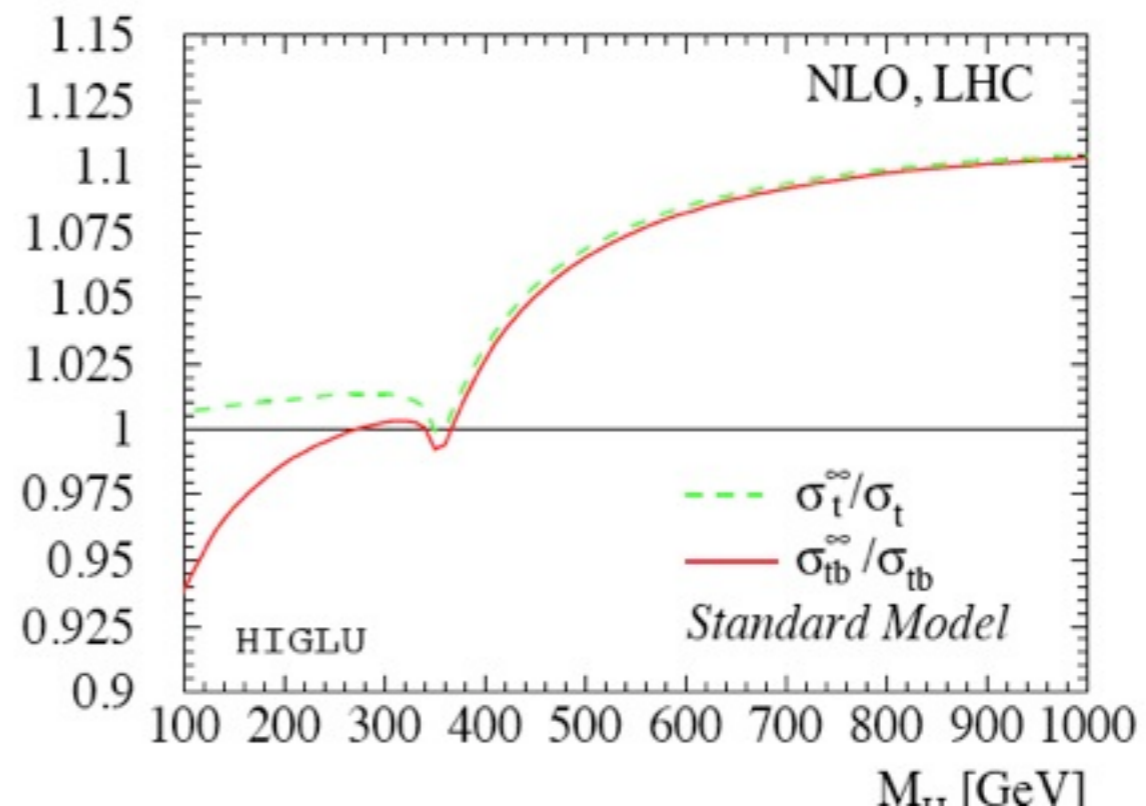
$$z = M_H^2 / (x_1 x_2 s)$$

$$\Delta\sigma = \sigma_0 \frac{\alpha_s}{\pi} \left\{ \left(\frac{11}{2} + \pi^2 \right) \delta(1-z) + 12 \left[\frac{\ln(1-z)}{1-z} \right]_+ - 12z(-z + z^2 + 2)\ln(1-z) - 6 \frac{(z^2 + 1 - z)^2}{1-z} \ln(z) - \frac{11}{2} (1-z)^3 \right\}$$

eikonal emission of soft gluons

Identical factors in full theory with $\sigma_0 \rightarrow \sigma_{LO, \text{full theory}}$

$$\sigma_{NLO}^{approx} = \left(\frac{\sigma_{NLO}^{EFT}}{\sigma_{LO}^{EFT}} \right) \sigma_{LO}^{QCD}$$



Gluon-fusion: inclusive

Effects of soft-gluon resummation at Next-to-next-to leading logarithmic (NNLL) accuracy (about 6-15%)

S. Catani, D. De Florian,
P. Nason, Grazzini (2003)

Partial N³LO corrections known (considerably reduced scale dependence)

Moch, Vogt (2005)

Resummation of π^2 factors through appropriate matching condition

Ahrens, Becher, Neubert, Yang (2008)

Two-loop EW corrections are also known (effect is about $O(5\%)$)

U. Aglietti et al. (2004)
G. Degrossi, F. Maltoni (2004)
G. Passarino et al. (2008)

Mixed QCD-EW effects evaluated in EFT approach

Anastasiou, Boughezal, FP (2008)

EW effects for real radiation

W. Keung, FP, (2009)

Inclusive cross sections

m_H (GeV)	Cross Section (pb)	+Total %	-Total %	+Scale %	-Scale %	+(PDF+ α_s) %	-(PDF+ α_s) %
123.0	20.15	+14.7	-14.8	+7.2	-7.9	+7.5	-6.9
123.5	19.99	+14.7	-14.8	+7.2	-7.9	+7.5	-6.9
124.0	19.83	+14.7	-14.8	+7.2	-7.9	+7.5	-6.9
124.5	19.68	+14.7	-14.8	+7.2	-7.9	+7.5	-6.9
125.0	19.52	+14.7	-14.7	+7.2	-7.8	+7.5	-6.9
125.5	19.37	+14.7	-14.7	+7.2	-7.8	+7.5	-6.9
126.0	19.22	+14.7	-14.7	+7.2	-7.8	+7.5	-6.9
126.5	19.07	+14.7	-14.7	+7.2	-7.8	+7.5	-6.9
127.0	18.92	+14.6	-14.7	+7.1	-7.8	+7.5	-6.9

LHC Higgs XS working group

More in talk of M. Neubert

Imposing cuts: VH

- The difficulty comes when typical experimental cuts are imposed. Consider the VH channel as an example, and compare inclusive to exclusive

Inclusive NLO QCD: +30% (Han, Willenbrock 1990)

NLO EW: +5-10% (Ciccolini, Dittmaier, Denner 2003)

NNLO QCD: 1-2% (Ferrera, Grazzini, Tramontano 2011)

However:

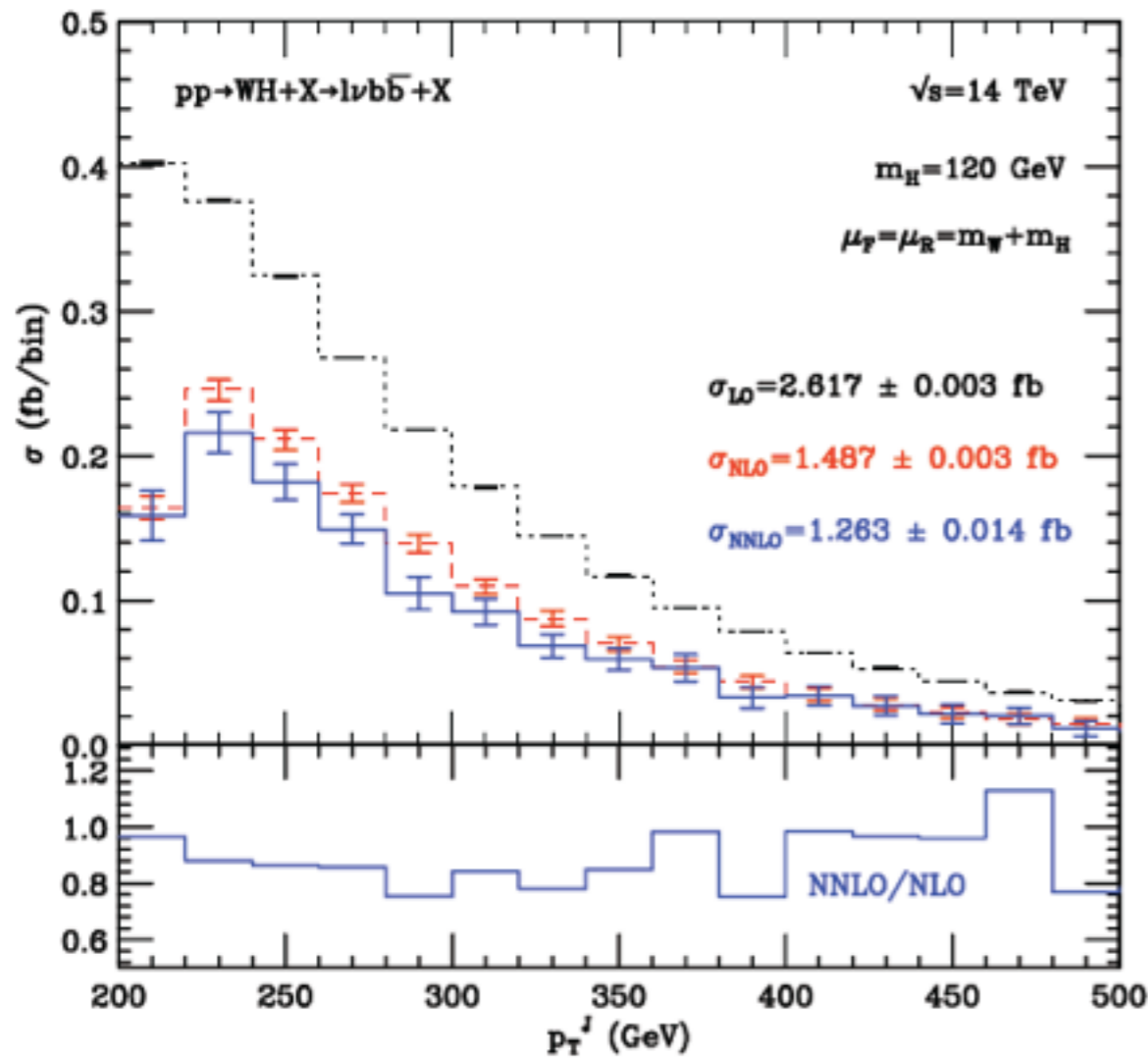
Categorization to take advantage of different S/B ratios:

- 3 E_T^{miss} categories for $ZH \rightarrow \nu b \bar{b}$: 120–160, 160–200, >200 GeV
- 4 p_T^W categories for $WH \rightarrow \ell \nu b \bar{b}$: 0–50, 50–100, 100–200, >200 GeV;
- 4 p_T^Z categories for $ZH \rightarrow \ell \ell b \bar{b}$: 0–50, 50–100, 100–200, >200 GeV;

from J. Qian

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Ferrera, Grazzini, Tramontano 2011

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A 30% increase turns into a decrease of more than a factor of 2!

Imposing cuts: $\tau\tau$

- The difficulty comes when typical experimental cuts are imposed. Consider the CMS $\tau\tau$ channel

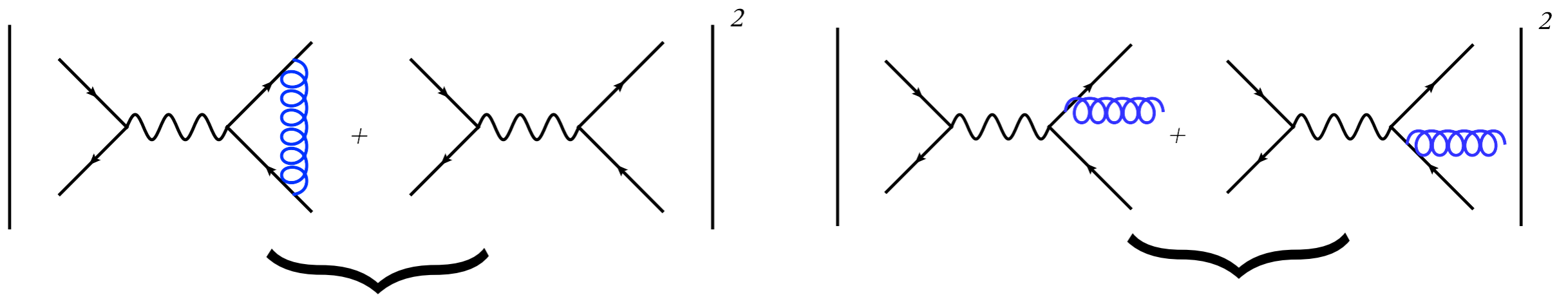
- Categorization ($\mu\tau, e\tau, e\mu, \mu\mu$)

- **VBF**: Require 2 jets above 30 GeV, $|\eta| < 4.7$. The jets must have $\Delta\eta > 3.5$ and $M_{jj} > 500$ GeV. Jet veto in the gap between the jets and the tau products
- **1 jet**: Requires at least one jet > 30 GeV. Veto events accepted by VBF category.

from M. Bachtis

Why are jet vetoes dangerous?

- Illustrate with simple example of $e^+e^- \rightarrow \text{jets}$
- Infrared safety: must sum both virtual and real corrections

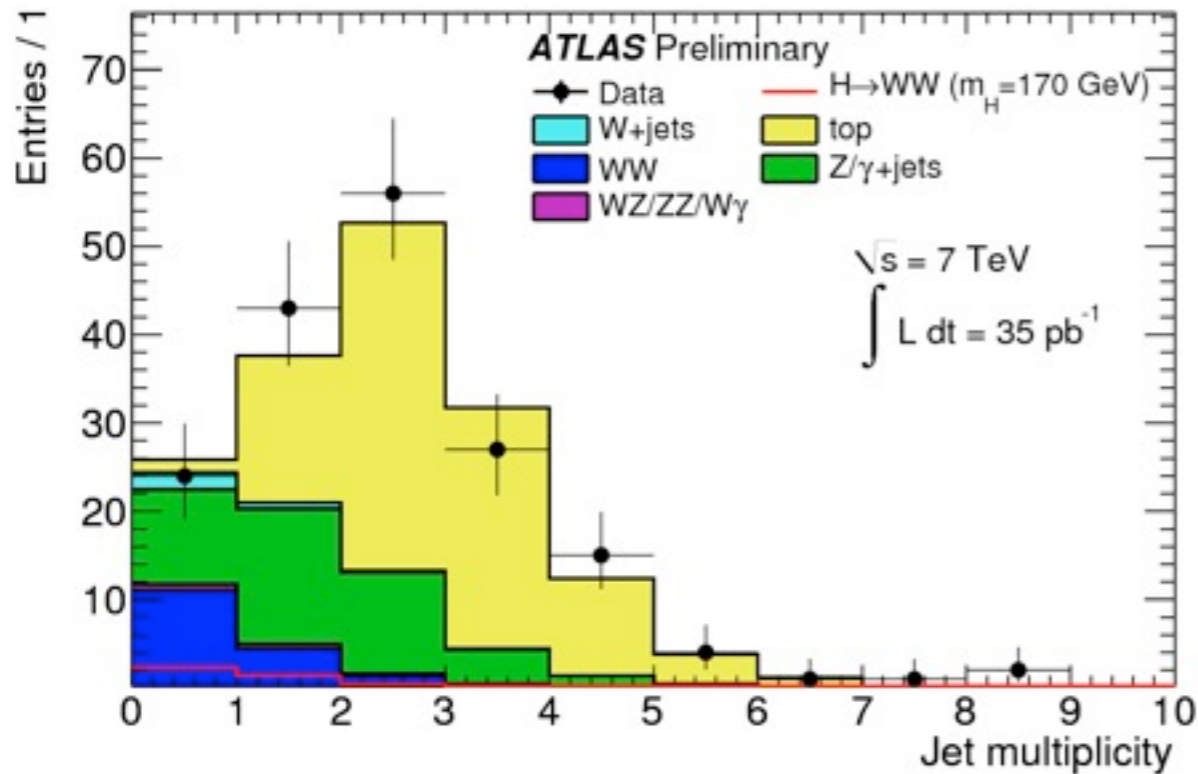


Virtual corrections: $-1/\epsilon_{\text{IR}}^2$

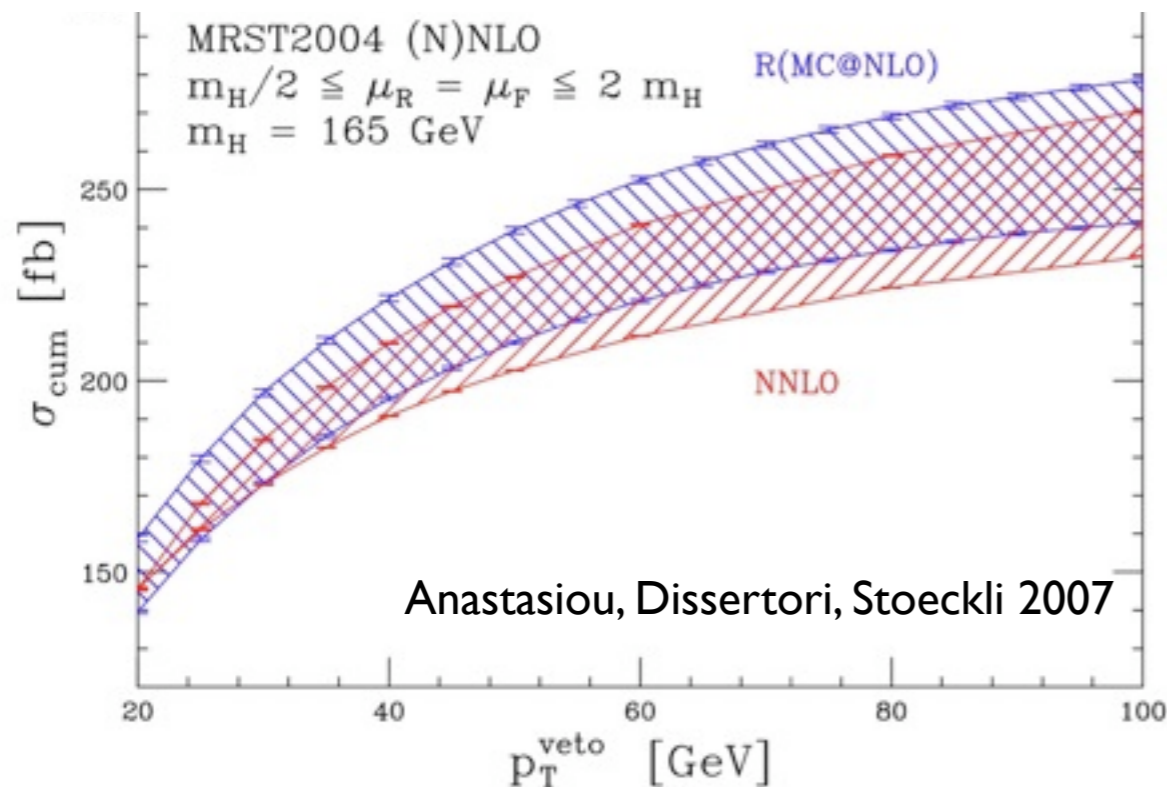
Real corrections: $1/\epsilon_{\text{IR}}^2 - a \times \ln^2(Q/p_{\text{T,cut}})$

- Incomplete cancellation of IR divergences in presence of final state restrictions gives large logarithms of restricted kinematic variable
- Relevant log term for gluon-fusion Higgs searches: $6(\alpha_s/\pi)\ln^2(M_H/p_{\text{T,veto}}) \sim 1/2 \Rightarrow$ potentially a large correction

The jet-veto in gluon fusion

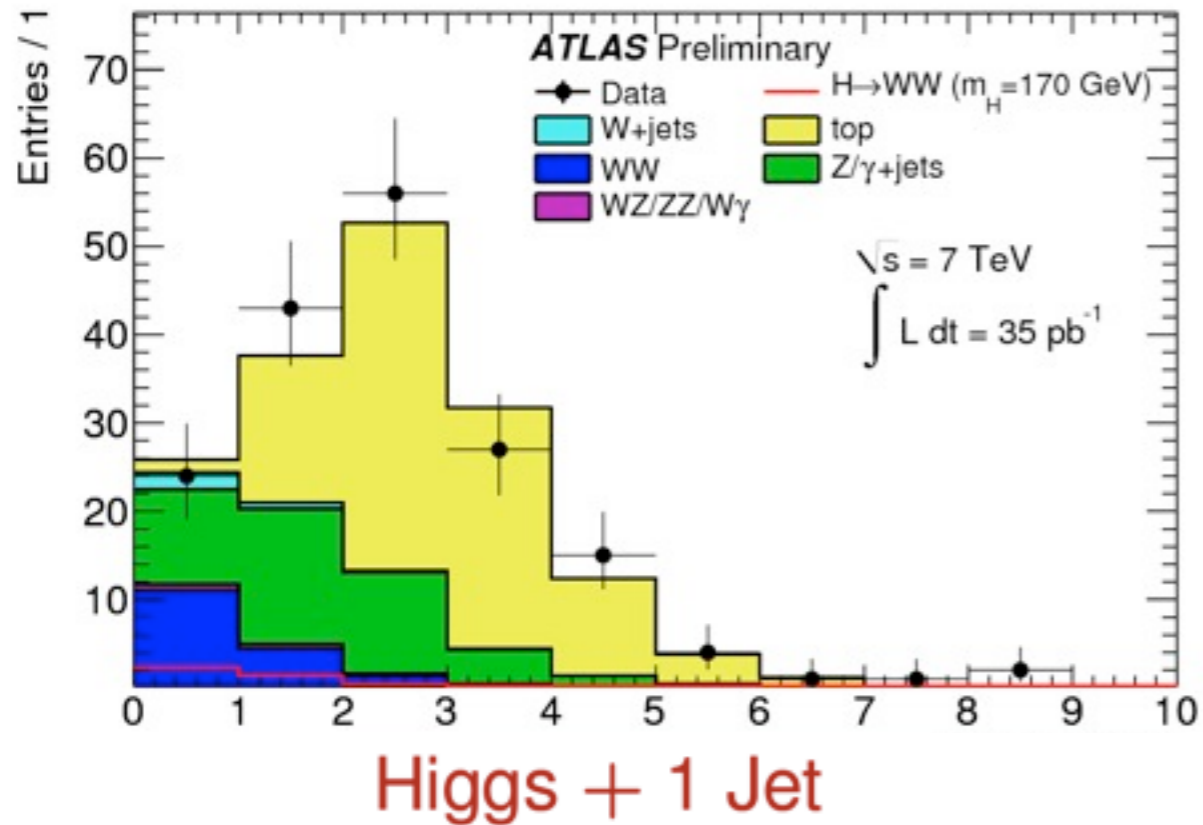


- Required in WW channel due to background composition; used in other channels also ($\gamma\gamma$, $\tau\tau$)
- 25-30 GeV jet cut used; restriction of radiation leads to large logs

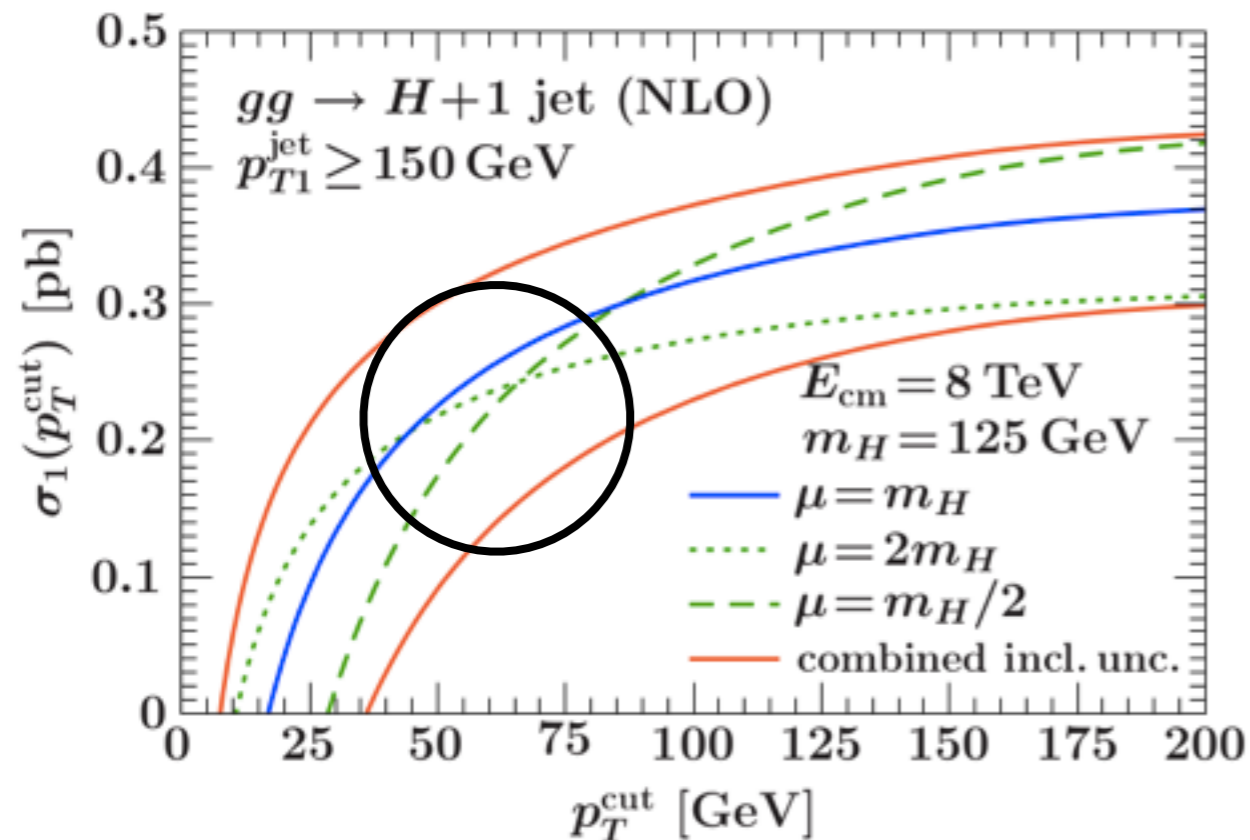


- Inclusive scale variation 10%; with a 25 GeV jet veto, 5-6%!
- Having $\Delta\sigma_{\text{veto}} < \Delta\sigma_{\text{tot}}$ doesn't seem correct; σ_{veto} has a more complicated structure and a larger expansion parameter, $\alpha_s \ln^2(m_H/p_{T,\text{cut}})$ rather than α_s

The jet-veto in gluon fusion



- Required in WW channel due to background composition; used in other channels also ($\gamma\gamma$, $\tau\tau$)
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- Similar issue affects the H+1 jet bin; cross-over of scale variation bands near the experimental cut value

Cancellations

- Study of cross section structure (Stewart, Tackmann 2011)

$$\begin{aligned}\sigma_0(p^{\text{cut}}) &= \sigma_{\text{total}} - \sigma_{\geq 1}(p^{\text{cut}}) \\ &\simeq \sigma_B \left\{ [1 + \alpha_s + \alpha_s^2 + \mathcal{O}(\alpha_s^3)] - [\alpha_s(L^2 + L + 1) + \alpha_s^2(L^4 + L^3 + L^2 + L + 1) + \mathcal{O}(\alpha_s^3 L^6)] \right\}\end{aligned}$$

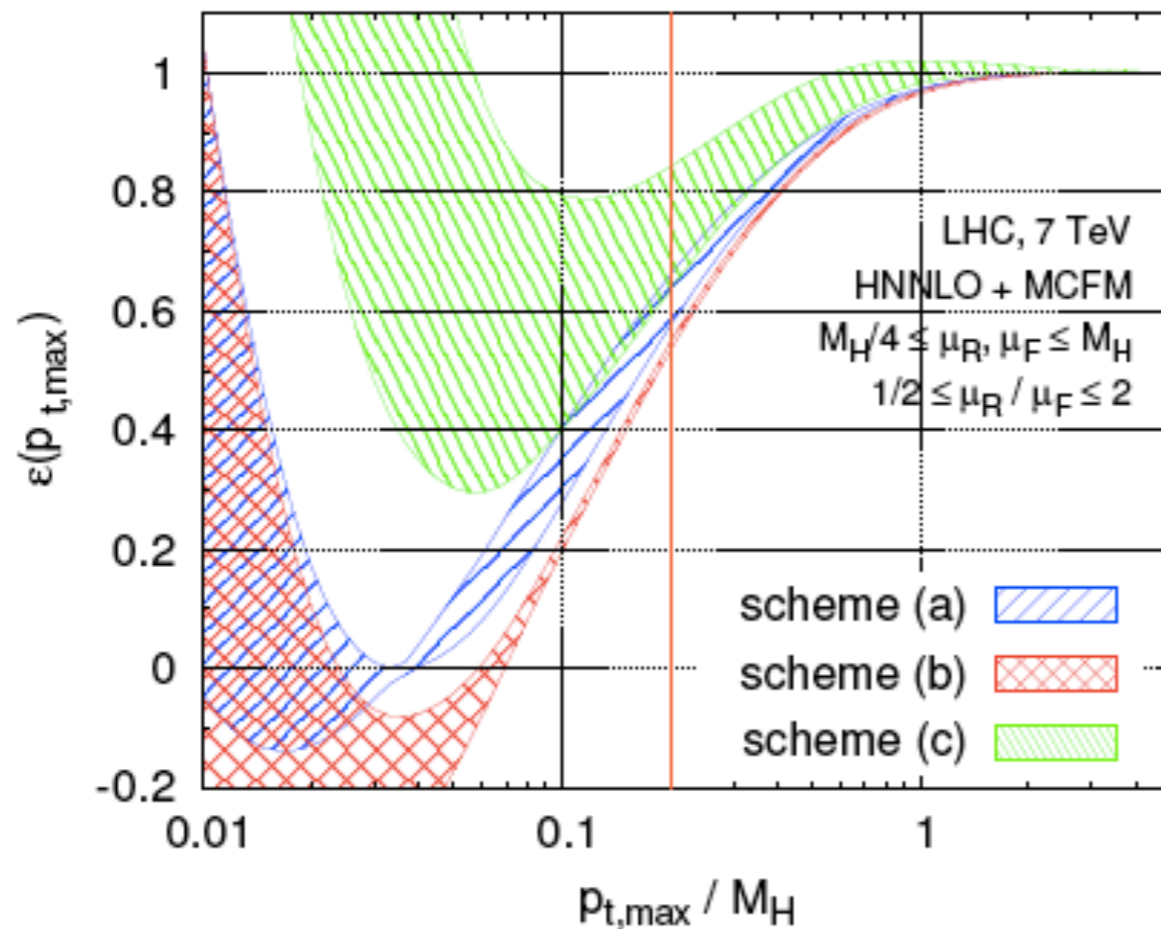
$$\sigma_{\text{total}} = (3.32 \text{ pb}) [1 + 9.5 \alpha_s + 35 \alpha_s^2 + \mathcal{O}(\alpha_s^3)] ,$$

$$\sigma_{\geq 1}(p_T^{\text{jet}} \geq 30 \text{ GeV}, |\eta^{\text{jet}}| \leq 3.0) = (3.32 \text{ pb}) [4.7 \alpha_s + 26 \alpha_s^2 + \mathcal{O}(\alpha_s^3)] .$$

- Accidental cancellation between large corrections to total cross section and logarithms, leading to reduced scale error. No reason to persist at higher orders

Explicit demonstration

- First further evidence: three ways of extending the calculation of the 0-jet event fraction that differ by $O(\alpha_s^3)$ w.r.t. leading order



Banfi, Salam, Zanderighi 2012

$$f_0^{(a)}(p_T^{\text{cut}}) \equiv \frac{\Sigma^{(0)}(p_T^{\text{cut}}) + \Sigma^{(1)}(p_T^{\text{cut}}) + \Sigma^{(2)}(p_T^{\text{cut}})}{\sigma^{(0)} + \sigma^{(1)} + \sigma^{(2)}}$$

$$f_0^{(b)}(p_T^{\text{cut}}) = 1 - \frac{\sigma_{1\text{-jet}}^{\text{NLO}}(p_T^{\text{cut}})}{\sigma^{(0)} + \sigma^{(1)}}.$$

$$f_0^{(c)}(p_T^{\text{cut}}) = 1 - \frac{\sigma_{1\text{-jet}}^{\text{NLO}}(p_T^{\text{cut}})}{\sigma^{(0)}} + \frac{\sigma^{(1)}}{(\sigma^{(0)})^2} \sigma_{1\text{-jet}}^{\text{LO}}(p_T^{\text{cut}})$$

- Gives results differing from 0.5 to 0.85 for a 30 GeV veto

Error prescription

- A solution using fixed-order results pointed out (Stewart, Tackmann 2011)

- In the limit of $\ln(m_H/p_{T,cut})$ large, σ_{tot} and $\sigma_{\geq 1}$ have independent expansions

- Gives expected result, that $\Delta\sigma_{veto} > \Delta\sigma_{tot}$

- The current prescription used in LHC analyses (phrased in terms of jet fractions)

- Leads to large uncertainties which limit experimental studies; any way to improve?

First consider *inclusive* jet cross sections

$$\sigma_{total}, \sigma_{\geq 1}, \sigma_{\geq 2} \Rightarrow C = \begin{pmatrix} \Delta_{total}^2 & 0 & 0 \\ 0 & \Delta_{\geq 1}^2 & 0 \\ 0 & 0 & \Delta_{\geq 2}^2 \end{pmatrix}$$

Transform to *exclusive* jet cross sections

$$\sigma_0 = \sigma_{total} - \sigma_{\geq 1}, \quad \sigma_1 = \sigma_{\geq 1} - \sigma_{\geq 2}, \quad \sigma_{\geq 2}$$

$$\Rightarrow C = \begin{pmatrix} \Delta_{total}^2 + \Delta_{\geq 1}^2 & -\Delta_{\geq 1}^2 & 0 \\ \Delta_{\geq 1}^2 & \Delta_{\geq 1}^2 + \Delta_{\geq 2}^2 & -\Delta_{\geq 2}^2 \\ 0 & -\Delta_{\geq 1}^2 & \Delta_{\geq 2}^2 \end{pmatrix}$$

cut	$\frac{\Delta\sigma_{total}}{\sigma_{total}}$	$\frac{\Delta\sigma_{\geq 1}}{\sigma_{\geq 1}}$	$\frac{\Delta\sigma_{\geq 2}}{\sigma_{\geq 2}}$	$\frac{\Delta\sigma_0}{\sigma_0}$	$\frac{\Delta\sigma_1}{\sigma_1}$
$p_T^{cut} = 30 \text{ GeV}, \eta^{cut} = 3$	10%	21%	45%	17%	29%

Resummation

- Significant recent efforts toward resumming logarithms associated with the jet veto

H+0 jets through NNLL Banfi, Salam, Zanderighi, Monni; Becher, Neubert 2012

‘Clustering log’ effects on H+0 jets Tackmann, Walsh, Zuberi 2012

H+1 jet through NLL X. Liu, FP 2012

$$\begin{aligned} \sigma(p_T^{\text{cut}}) &\sim 1 \\ &+ \alpha_s L^2 + \alpha_s L + \alpha_s \text{ NLO} \\ &+ \alpha_s^2 L^4 + \alpha_s^2 L^3 + \alpha_s^2 L^2 + \alpha_s^2 L + \alpha_s^2 \text{ NNLO} \\ &+ \alpha_s^3 L^6 + \alpha_s^3 L^5 + \alpha_s^3 L^4 + \alpha_s^3 L^3 + \alpha_s^3 L^2 + \dots \\ &\quad \text{LL} \quad \text{NLL} \quad \text{NNLL} \end{aligned} \qquad L \equiv \ln \frac{p_T^{\text{cut}}}{m_H}$$

from S. Zuberi

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H+1 jet through NLL X. Liu, FP 2012

- Distance measures for H+1 jet, anti- k_T algorithm:

$$\rho_{ij} = \min(p_{T,i}^{-1}, p_{T,j}^{-1}) \Delta R_{ij} / R,$$

$$\rho_i = p_{T,i}^{-1}.$$

$$\rho_{JJ} \lesssim \rho_J \sim 1, \quad \rho_{Js} \sim R^{-1}, \quad \rho_{Ja} \sim \rho_{Jb} \sim R^{-1} \log \lambda^{-1},$$

$$\rho_{ss} \sim \rho_{aa} \sim \rho_{bb} \sim (\lambda R)^{-1}, \quad \rho_{sa} \sim \rho_{sb} \sim \rho_{ab} \sim (\lambda R)^{-1} \log \lambda^{-1},$$

$$\rho_s \sim \rho_a \sim \rho_b \sim \lambda^{-1}.$$

$$R \sim 0.4, \lambda \sim 0.2$$

EFT approach (Becher, Neubert)

$$\rho_s \sim m_H(\lambda, \lambda, \lambda)$$

$$\rho_{a,b} \sim m_H(\lambda^2, 1, \lambda)$$

$$\rho_J \sim m_H(\lambda^2, 1, \lambda) \text{ (along jet direction)}$$

Radiation along the jet direction is combined first into a single state; soft radiation insensitive to details of collinear radiation

Resummation

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$$\rho_s \sim \rho_a \sim \rho_b \sim \lambda^{-1}.$$

$$\lambda \equiv p_T^{\text{veto}} / \sqrt{\hat{s}} \ll 1$$

$$R \sim 0.4, \lambda \sim 0.2$$

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$$\rho_{a,b} \sim m_H(\lambda^2, 1, \lambda)$$

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Soft and collinear radiation clustered separately

Resummation

- Significant recent efforts toward resumming logarithms associated with the jet veto

H+0 jets through NNLL Banfi, Salam, Zanderighi, Monni; Becher, Neubert 2012

‘Clustering log’ effects on H+0 jets Tackmann, Walsh, Zuberi 2012

H+1 (or more) jets through NLL X. Liu, FP 2012

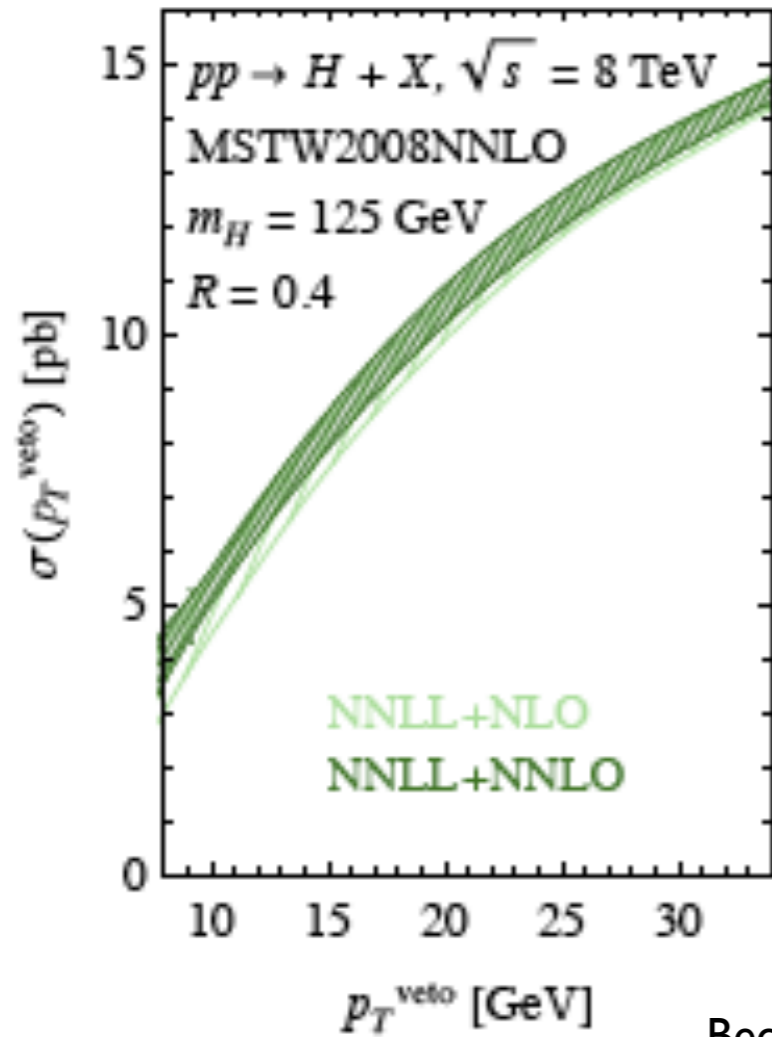
- Can factorize radiation from soft, collinear, beam directions to establish the result:

$$\sigma(p_T^{\text{cut}}) \sim H_{gg}(\mu) [B_a(\mu, \nu) \times B_b(\mu, \nu) \times S(\mu, \nu)] + \sigma_{ns} \quad (\text{0-jet})$$

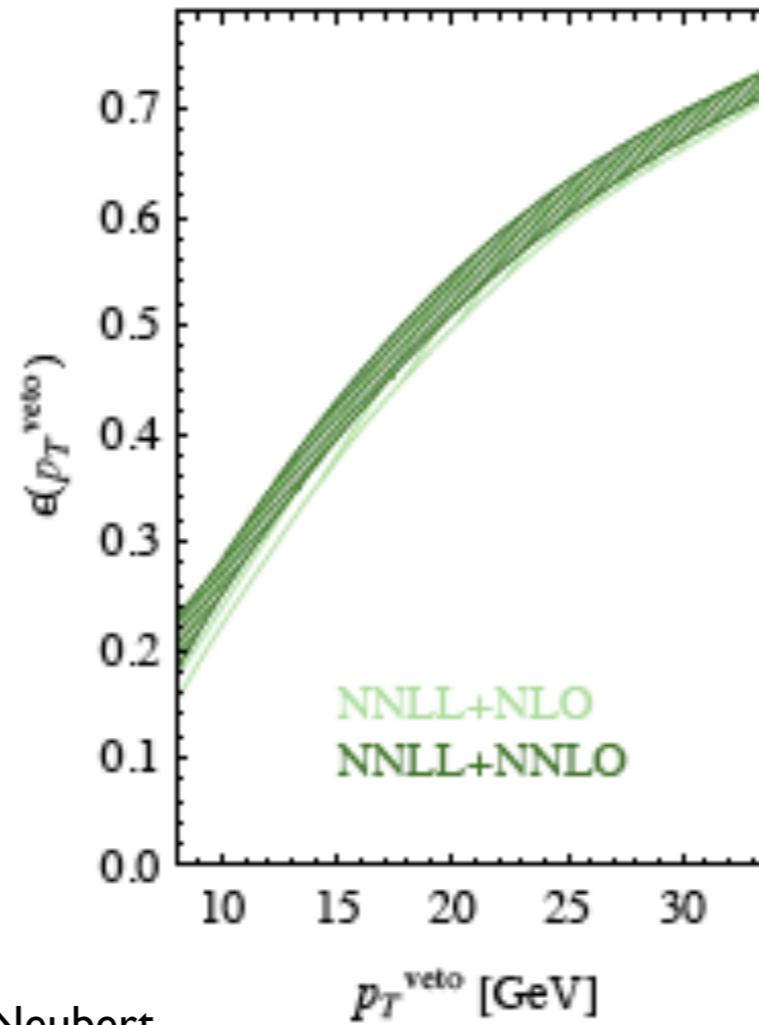
$$d\sigma = d\Phi_{H_c} d\Phi_{J_i} \mathcal{F}(\Phi_{H_c}, \Phi_{J_i}) \sum_{a,b} \int dx_a dx_b \frac{1}{2\hat{s}} (2\pi)^4 \delta^4 \left(q_a + q_b - \sum_i^n q_{J_i} - \sum_c q_{H_c} \right) \quad (\text{H+n-jets})$$

$$\times \sum_{\text{spin}} \sum_{\text{color}} \text{Tr}(H \cdot S) \mathcal{I}_{a,i_a j_a} \otimes f_{j_a}(x_a) \mathcal{I}_{b,i_b j_b} \otimes f_{j_b}(x_b) \prod_i^n J_{J_i}(R),$$

Numerical results, 0 jets



Becher, Neubert



Uncertainties from
varying all scales
separately and adding in
quadrature

Numerical results, 0 jets

- Central value: scheme (a) with

$$\mu_R = \mu_F = Q = M/2$$

- μ_R and μ_F variations

$$\frac{M}{4} \leq \mu_{R,F} \leq M \quad \frac{1}{2} \leq \frac{\mu_R}{\mu_F} \leq 2$$

- Resummation scale (Q) variation

i.e.

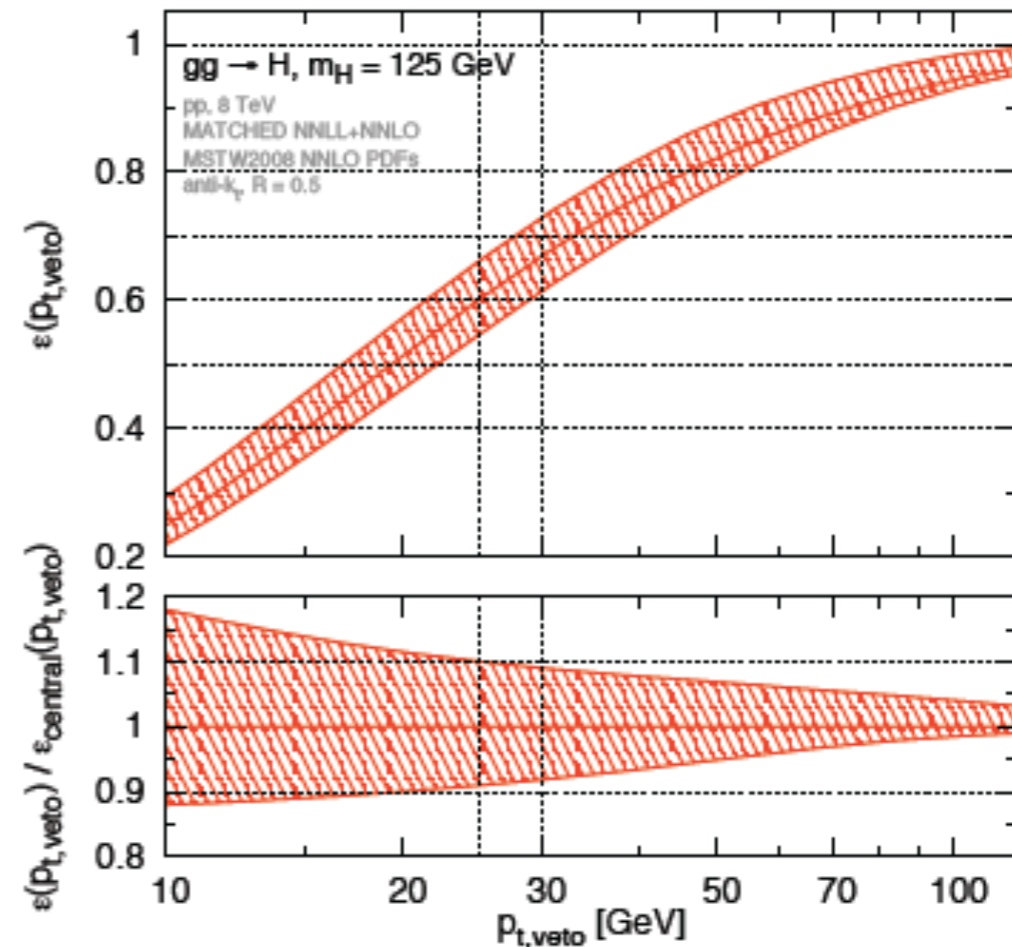
$$\ln \frac{M}{p_{t,veto}} \rightarrow \ln \frac{Q}{p_{t,veto}}$$

$$\frac{M}{4} \leq Q \leq M \quad \mu_{R,F} = M/2$$

- Scheme (b) and (c) with

$$\mu_R = \mu_F = Q = M/2$$

- Total uncertainty \longleftrightarrow envelope



From P. Monni

Banfi, Monni, Salam, Zanderighi

Numerical results, 0 jets

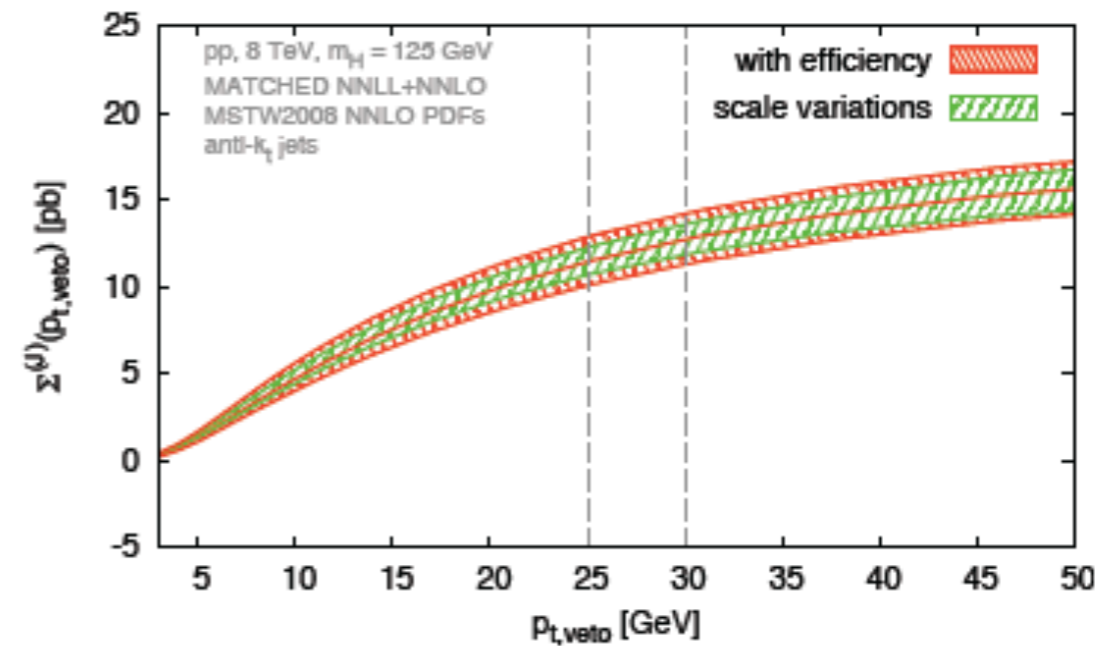
Using jet-veto efficiencies to estimate the uncertainty @ **NNLL+NNLO**

μ_R, μ_F and Q variations (green)

$$\delta_{\Sigma(J)} = 9\%$$

With efficiencies (red)

$$\delta_{\Sigma(J)} = 11.5\%$$



From P. Monni

Banfi, Monni, Salam, Zanderighi

At fixed-order:

$$\delta_{\Sigma(J)} = 16.2\%$$

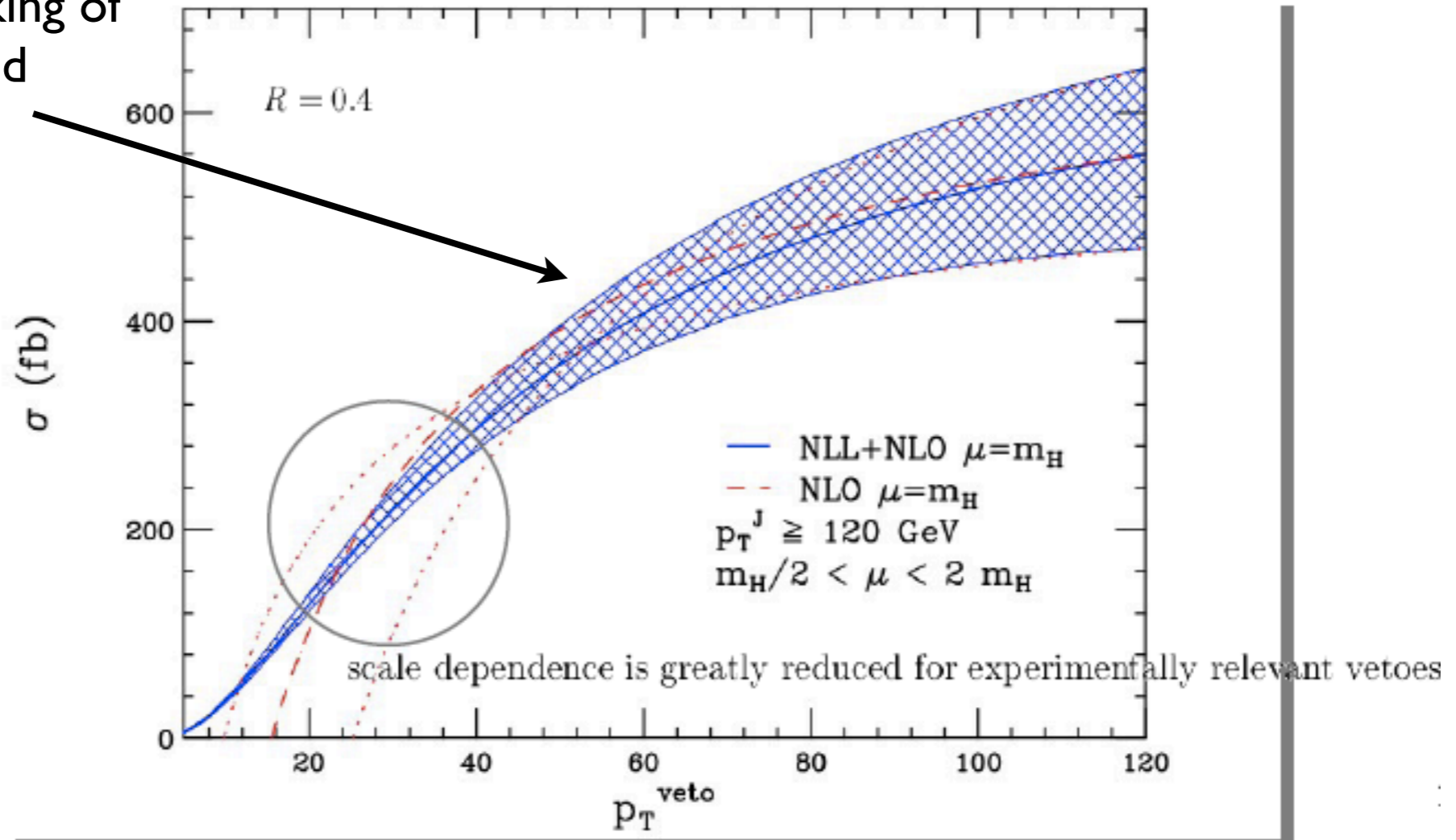
consistent with Stewart-Tackmann

in the region

$$25\text{GeV} \leq p_{t,\text{veto}} \leq 30\text{GeV}$$

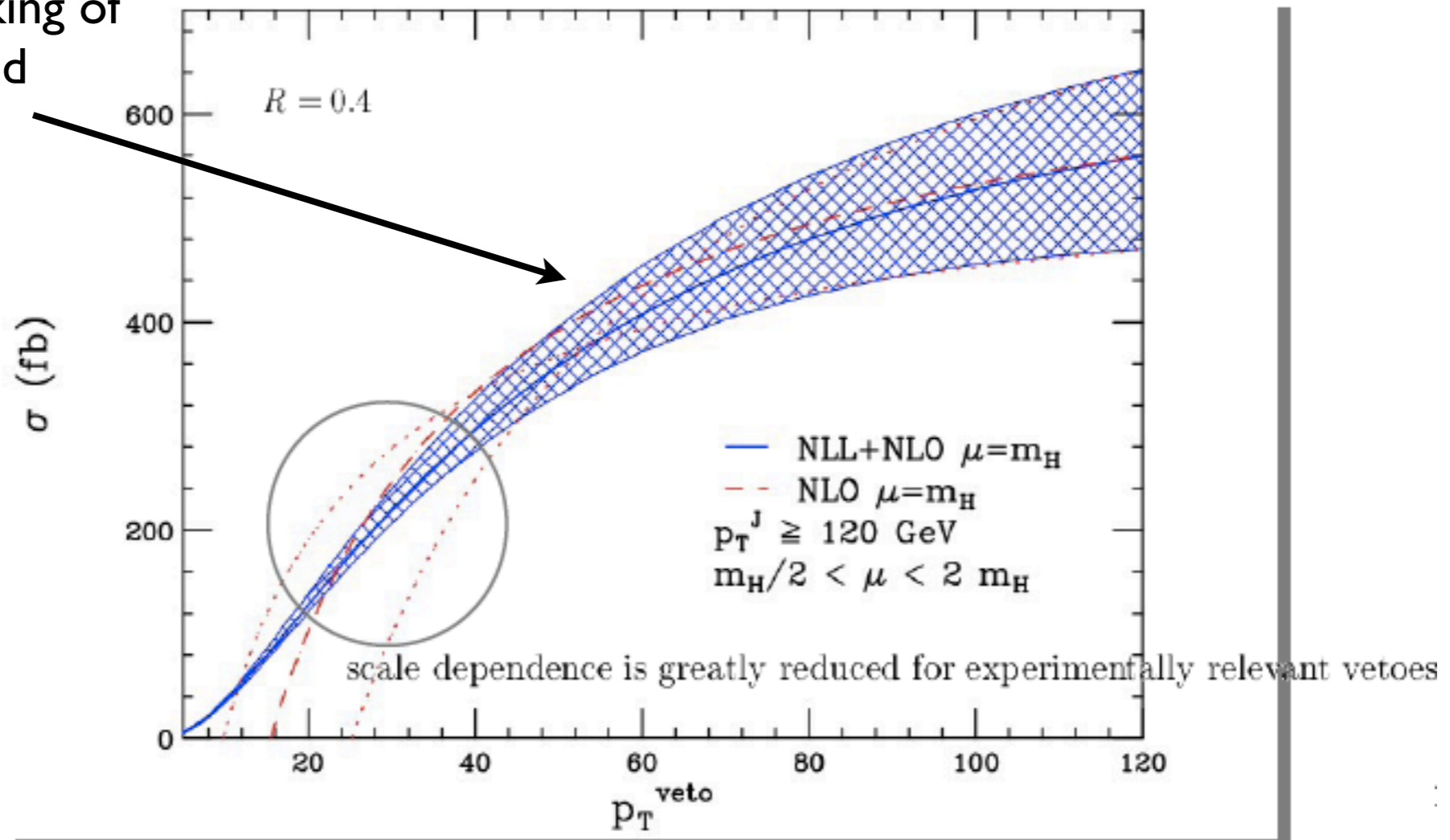
Numerical results, 1 jet

No artificial shrinking of scale-variation band



Numerical results, 1 jet

No artificial shrinking of scale-variation band



X. Liu, FP

- Region where $p_{TJ} \gg p_{T,\text{veto}}$ accounts for between 30-50% of the spectrum; for $p_{TJ} \sim p_{T,\text{veto}}$ need new EFT with only soft+beam emissions



R dependence



- There is only a narrow window of parameter space where the resummation holds

$$R \gg p_T^{\text{cut}}/m_H \quad \sigma \supset \alpha_s^n R^2$$

Soft-collinear mixing.

$$R \sim p_T^{\text{cut}}/m_H \quad \sigma \supset \alpha_s^n \ln^{n-1} R$$

Clustering logarithms.

R dependence



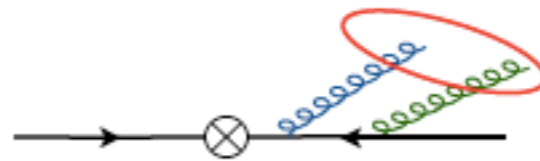
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Soft-collinear mixing.

Clustering logarithms.



$$\delta\sigma_{SC} = -\sigma_{LO} \left(\frac{\alpha_s C_A}{\pi} \right)^2 \frac{2\pi^2}{3} R^2 \ln \frac{m_H}{p_T^{\text{cut}}}$$

From S. Zuberi

Tackmann, Walsh, Zuberi

Phenomenologically, $R \sim 0.4$, $p_{T,\text{veto}}/m_H \sim 0.2 \rightarrow$ not the relevant limit

R dependence



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Soft-collinear mixing.

$$R \sim p_T^{\text{cut}}/m_H \quad \sigma \supset \alpha_s^n \ln^{n-1} R$$

Clustering logarithms.

$$\frac{1}{\epsilon} - \frac{1}{\epsilon} R^{-2\epsilon} \sim \ln R$$

From S. Zuberi

Tackmann, Walsh, Zuberi

R dependence



- There is not a large window of parameter space where the resummation holds

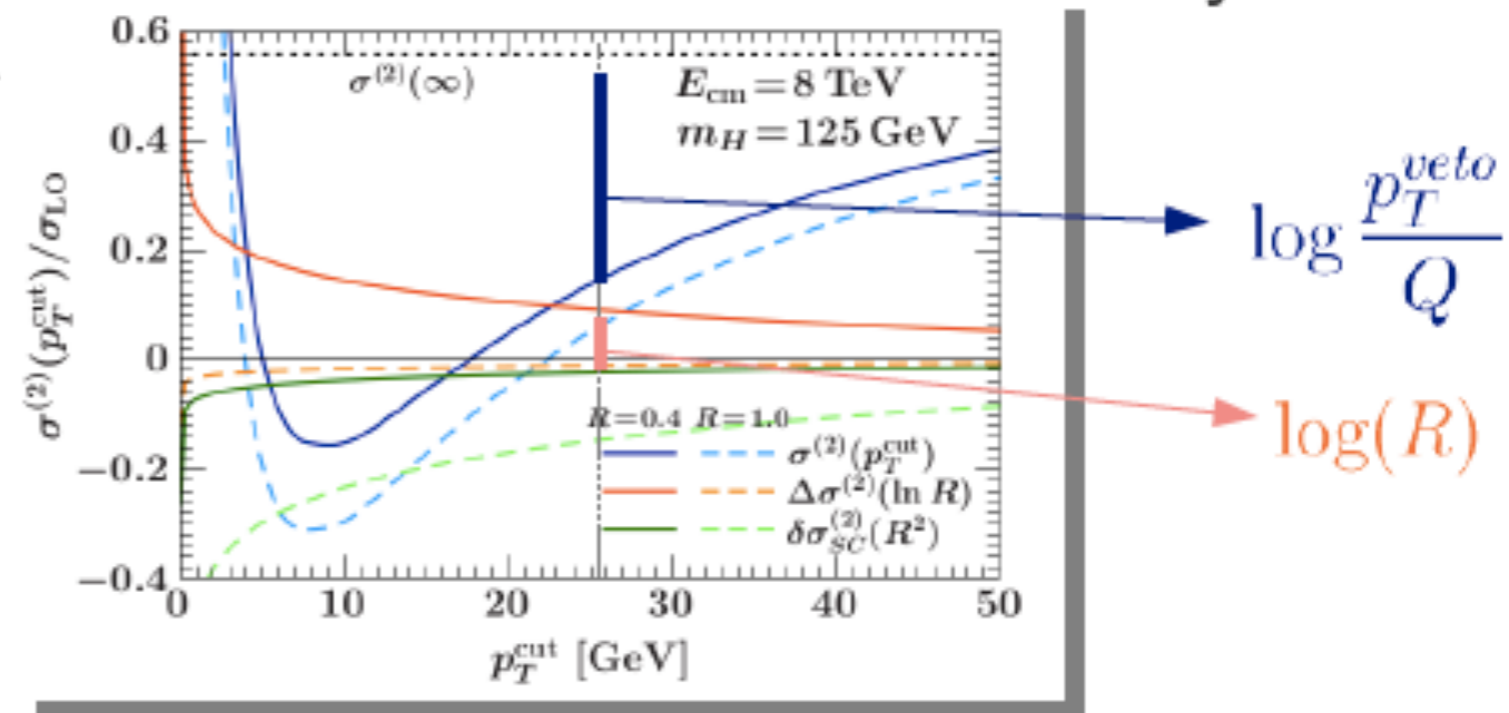
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Soft-collinear mixing.

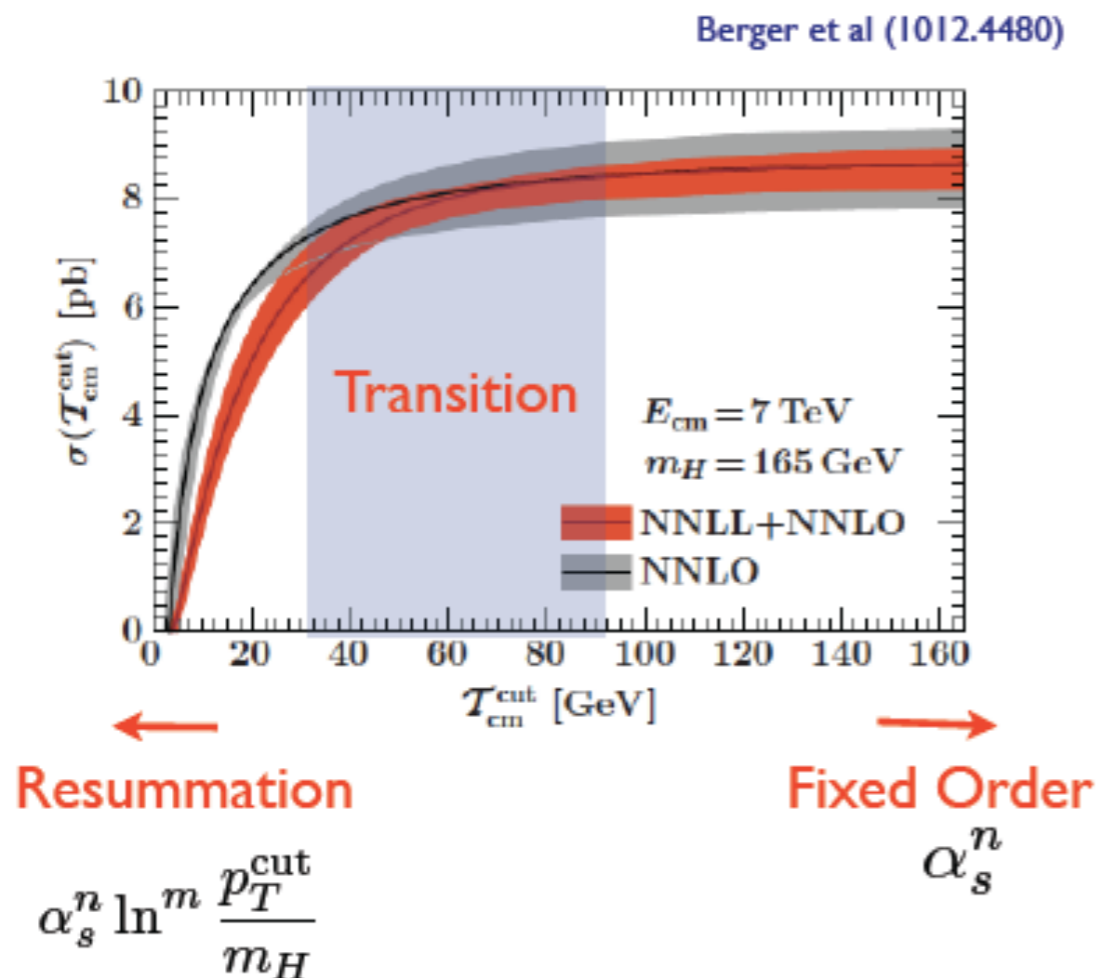
Clustering logarithms.

Moderate and well controlled for experimentally interesting R



Status

- Formalism well established for H+0 jet, 1-jet cross sections; some differences in how uncertainties are estimated by the various groups, more EFT development for the entire 1-jet bin spectrum
- A reduction of uncertainty from the current fixed-order estimates used, and experimentalists should stay tuned for updates



- The interesting region isn't dominated by either the resummation or the fixed-order results... progress on extending both frameworks needed
- Next steps: $\alpha_s^3 \ln^2 R$ In λ clustering terms
Tackmann, Walsh, Zuberi
- H+1 jet at NNLO Boughezal, Caola, Melnikov, FP, Schulze