

# Multiple Higgs models and the 125 GeV state: NMSSM and 2HDM perspectives

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NMSSM Collaborators: G. Belanger, U. Ellwanger, Y. Jiang, S. Kraml, J. Schwarz

1. “*Higgs Bosons at 98 and 125 GeV at LEP and the LHC*” G. Belanger, U. Ellwanger, J. F. Gunion, Y. Jiang, S. Kraml and J. H. Schwarz. arXiv:1210.1976 [hep-ph]
2. “*Two Higgs Bosons at the Tevatron and the LHC?*” G. Belanger, U. Ellwanger, J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1208.4952 [hep-ph]
3. “*Diagnosing Degenerate Higgs Bosons at 125 GeV*” J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1208.1817 [hep-ph]
4. “*Could two NMSSM Higgs bosons be present near 125 GeV?*” J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1207.1545 [hep-ph]
5. “*The Constrained NMSSM and Higgs near 125 GeV*” J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1201.0982 [hep-ph] Phys. Lett. B **710**, 454 (2012)

2HDM Collaborators: Alexandra Drozd, Bohdan Grzadkowski, Yun Jiang

1. “*Two-Higgs-Doublet Models and Enhanced Rates for a 125 GeV Higgs*” A. Drozd, B. Grzadkowski, J. F. Gunion and Y. Jiang. arXiv:1211.3580 [hep-ph]

# Higgs-like LHC Excesses at 125 GeV

- **Experimental Higgs-like excesses: define**

$$R_Y^h(X) = \frac{\sigma(pp \rightarrow Y \rightarrow h)\text{BR}(h \rightarrow X)}{\sigma(pp \rightarrow Y \rightarrow h_{SM})\text{BR}(h_{SM} \rightarrow X)}, \quad R^h(X) = \sum_Y R_Y^h, \quad (1)$$

where  $Y = gg, VV, Vh$  or  $t\bar{t}h$ . The notation  $\mu \equiv R$  is sometimes employed.

Experimental results are now available for many channels, where the experimental channel is usually a mixture of the theoretical channels.

$$\mu_k = \sum T_k^i \hat{\mu}_i \quad (2)$$

where the  $T_k^i$  give the amount of contribution to the experimental channel  $k$  coming from the theoretically defined channel  $i$  and  $\hat{\mu}_i$  is the prediction for a given theoretical channel. The observed  $\mu_k$  values and  $T_k^i$  values are summarized in the following tables.

Channel	Signal strength $\mu$	$m_H$ (GeV)	Production mode			
			ggF	VBF	VH	ttH
$H \rightarrow \gamma\gamma$ (4.8 fb <sup>-1</sup> at 7 TeV + 13.0 fb <sup>-1</sup> at 8 TeV) [?]						
$\mu(\text{ggF} + \text{ttH}, \gamma\gamma)$	$1.85 \pm 0.52$	126.6	100%	–	–	–
$\mu(\text{VBF} + \text{VH}, \gamma\gamma)$	$2.01 \pm 1.23$	126.6	–	60%	40%	–
$H \rightarrow ZZ$ (4.6 fb <sup>-1</sup> at 7 TeV + 13.0 fb <sup>-1</sup> at 8 TeV) [?, ?]						
Inclusive	$1.01^{+0.45}_{-0.40} \rightarrow 0.97^{+0.45}_{-0.40}$	125	87%	7%	5%	1%
$H \rightarrow WW$ (13.0 fb <sup>-1</sup> at 8 TeV) [?, ?]						
$e\nu\mu\nu$	$1.42^{+0.58}_{-0.54}$	125.5	95%	3%	2%	–
$H \rightarrow b\bar{b}$ (4.7 fb <sup>-1</sup> at 7 TeV + 13.0 fb <sup>-1</sup> at 8 TeV) [?, ?]						
VH tag	$-0.39 \pm 1.02$	125.5	–	–	100%	–
$H \rightarrow \tau\tau$ (4.6 fb <sup>-1</sup> at 7 TeV + 13.0 fb <sup>-1</sup> at 8 TeV) [?]						
$\mu(\text{ggF}, \tau\tau)$	$2.41 \pm 1.57$	125	100%	–	–	–
$\mu(\text{VBF} + \text{VH}, \tau\tau)$	$-0.26 \pm 1.02$	125	–	60%	40%	–

Table 1: ATLAS results as employed in this analysis. The correlations included in the fits are  $\rho = -0.37$  for the  $\gamma\gamma$  and  $\rho = -0.50$  for the  $\tau\tau$  channels.

Channel	Signal strength $\mu$	$m_H$ (GeV)	Production mode			
			ggF	VBF	VH	ttH
$H \rightarrow \gamma\gamma$ (5.1 fb <sup>-1</sup> at 7 TeV + 5.3 fb <sup>-1</sup> at 8 TeV) [?, ?, ?]						
$\mu(\text{ggF} + \text{ttH}, \gamma\gamma)$	$0.95 \pm 0.65$	125.8	100%	–	–	–
$\mu(\text{VBF} + \text{VH}, \gamma\gamma)$	$3.77 \pm 1.75$	125.8	–	60%	40%	–
$H \rightarrow ZZ$ (5.1 fb <sup>-1</sup> at 7 TeV + 12.2 fb <sup>-1</sup> at 8 TeV) [?, ?]						
Inclusive	$0.81^{+0.35}_{-0.28}$	125.8	87%	7%	5%	1%
$H \rightarrow WW$ (up to 4.9 fb <sup>-1</sup> at 7 TeV + 12.1 fb <sup>-1</sup> at 8 TeV) [?, ?, ?]						
0/1 jet	$0.77^{+0.27}_{-0.25}$	125.8	97%	3%	–	–
VBF tag	$-0.05^{+0.74}_{-0.55}$	125.8	17%	83%	–	–
VH tag	$-0.31^{+2.22}_{-1.94}$	125.8	–	–	100%	–
$H \rightarrow b\bar{b}$ (up to 5.0 fb <sup>-1</sup> at 7 TeV + 12.1 fb <sup>-1</sup> at 8 TeV) [?, ?, ?]						
VH tag	$1.31^{+0.65}_{-0.60}$	125.8	–	–	100%	–
ttH tag	$-0.80^{+2.10}_{-1.84}$	125.8	–	–	–	100%
$H \rightarrow \tau\tau$ (up to 5.0 fb <sup>-1</sup> at 7 TeV + 12.1 fb <sup>-1</sup> at 8 TeV) [?, ?, ?]						
0/1 jet	$0.85^{+0.68}_{-0.66}$	125.8	76%	16%	7%	1%
VBF tag	$0.82^{+0.82}_{-0.75}$	125.8	19%	81%	–	–
VH tag	$0.86^{+1.92}_{-1.68}$	125.8	–	–	100%	–

Table 2: CMS results as employed in this analysis. The correlation included for the  $\gamma\gamma$  channel is  $\rho = -0.54$ .

Channel	Signal strength $\mu$	$m_H$ (GeV)	Production mode			
			ggF	VBF	VH	ttH
$H \rightarrow \gamma\gamma$ [?]						
Combined	$6.14^{+3.25}_{-3.19}$	125	78%	5%	17%	–
$H \rightarrow WW$ [?]						
Combined	$0.85^{+0.88}_{-0.81}$	125	78%	5%	17%	–
$H \rightarrow b\bar{b}$ [?]						
VH tag	$1.56^{+0.72}_{-0.73}$	125	–	–	100%	–

Table 3: Tevatron results for up to  $10 \text{ fb}^{-1}$  at  $\sqrt{s} = 1.96 \text{ TeV}$ , as employed in this analysis.

Note: general enhancement of  $\gamma\gamma$  final states in both ggF (not CMS) and especially VBF.

Note:  $R(ZZ, WW) \gtrsim 1$  for ATLAS, whereas  $R(ZZ, WW) < 1$  for CMS.

- **The big questions:**

1. if the deviations from a single SM Higgs survive what is the model?
2. If they do survive, how far beyond the "standard" model must we go to describe them?

**Here, I focus on a a number of amusing possibilities in the NMSSM and summarize some recent pure 2HDM results.**

# Enhanced Higgs signals in the NMSSM

- NMSSM=MSSM+ $\widehat{S}$ .
- The extra complex  $S$  component of  $\widehat{S} \Rightarrow$  the NMSSM has  $h_1, h_2, h_2, a_1, a_2$ .
- The new NMSSM parameters of the superpotential ( $\lambda$  and  $\kappa$ ) and scalar potential ( $A_\lambda$  and  $A_\kappa$ ) appear as:

$$W \ni \lambda \widehat{S} \widehat{H}_u \widehat{H}_d + \frac{\kappa}{3} \widehat{S}^3, \quad V_{\text{soft}} \ni \lambda A_\lambda S H_u H_d + \frac{\kappa}{3} A_\kappa S^3 \quad (3)$$

- $\langle S \rangle \neq 0$  is generated by SUSY breaking and solves  $\mu$  problem:  $\mu_{\text{eff}} = \lambda \langle S \rangle$ .
- First question: Can the NMSSM give a Higgs mass as large as 125 GeV?

**Answer: Yes**, so long as it is not a highly unified model. For our studies, we employed universal  $m_0$ , except for NUHM ( $m_{H_u}^2, m_{H_d}^2, m_S^2$  free), universal  $A_t = A_b = A_\tau = A_0$  but allow  $A_\lambda$  and  $A_\kappa$  to vary freely. Of course,  $\lambda > 0$  and  $\kappa$  are scanned demanding perturbativity up to the GUT scale.

- Can this model achieve rates in  $\gamma\gamma$  and  $4\ell$  that are  $>SM$ ?

Answer: **it depends on whether or not we insist on getting good  $a_\mu$ .**

- The possible mechanism (arXiv:1112.3548, Ellwanger) is to reduce the  $b\bar{b}$  width of the mainly SM-like Higgs by giving it some singlet component. The  $gg$  and  $\gamma\gamma$  couplings are less affected.
- Typically, this requires  $m_{h_1}$  and  $m_{h_2}$  to have similar masses (for singlet-doublet mixing) and large  $\lambda$  (to enhance Higgs mass).

Large  $\lambda$  (by which we mean  $\lambda > 0.1$ ) is only possible while retaining perturbativity up to  $m_{Pl}$  if  $\tan\beta$  is modest in size.

**In the semi-unified model we employ, enhanced rates and/or large  $\lambda$  cannot be made consistent with decent  $\delta a_\mu$ . (J. F. Gunion, Y. Jiang and S. Kraml.arXiv:1201.0982 [hep-ph])**

- The "enhanced" SM-like Higgs can be either  $h_1$  or  $h_2$ .

$$R_{gg}^{h_i}(X) \equiv (C_{gg}^{h_i})^2 \frac{\text{BR}(h_i \rightarrow X)}{\text{BR}(h_{SM} \rightarrow X)}, \quad R_{\text{VBF}}^{h_i}(X) \equiv (C_{\text{VV}}^{h_i})^2 \frac{\text{BR}(h_i \rightarrow X)}{\text{BR}(h_{SM} \rightarrow X)}, \quad (4)$$

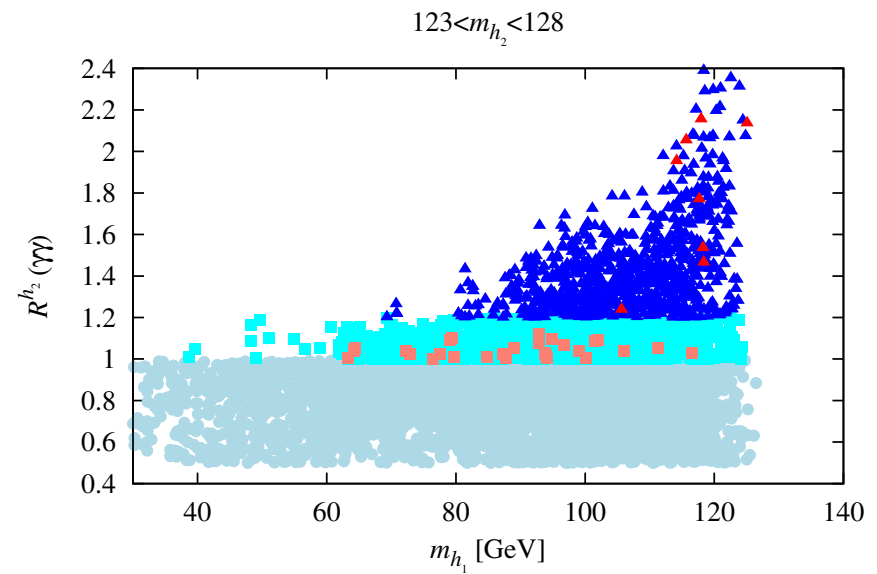
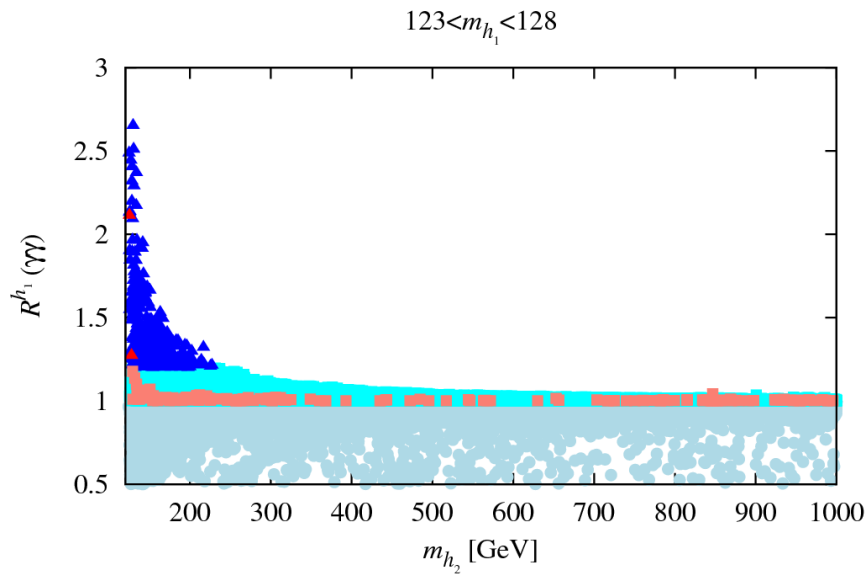
where  $h_i$  is the  $i^{\text{th}}$  NMSSM scalar Higgs, and  $h_{SM}$  is the SM Higgs boson.  $C_Y^{h_i} = g_{Yh_i}/g_{Yh_{SM}}$  and  $R_{Vh}$  for  $V^* \rightarrow Vh_i$  ( $V = W, Z$ ) with  $h_i \rightarrow X$  is equal to  $R_{\text{VBF}}^{h_i}(X)$  in doublets + singlets models.



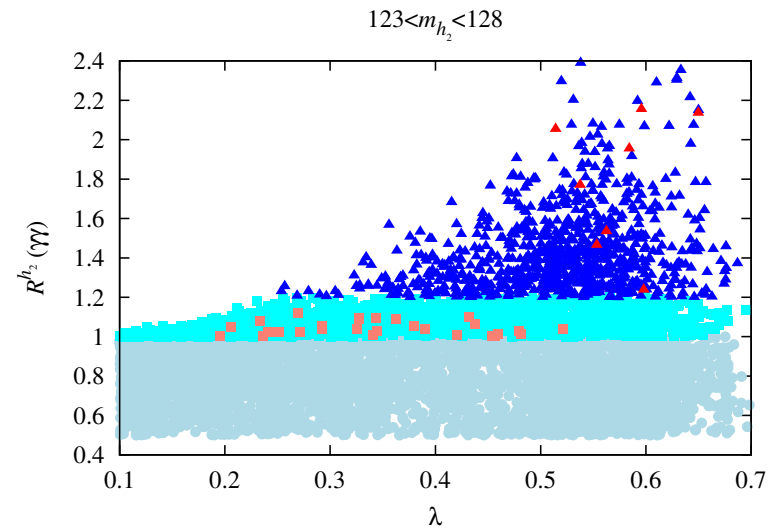
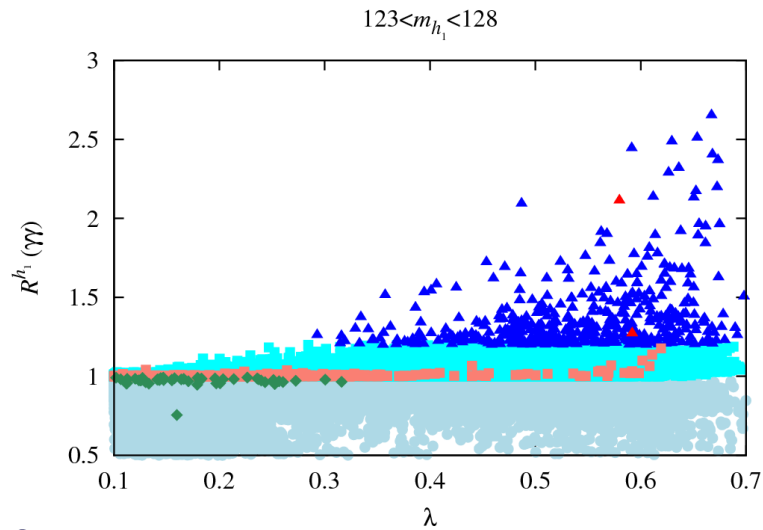
# Some illustrative $R_{gg}$ results from (J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1207.1545):

Figure Legend

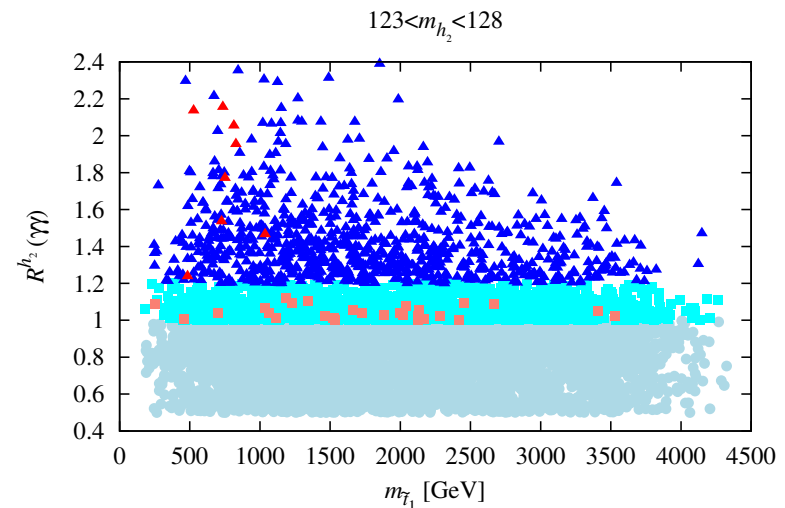
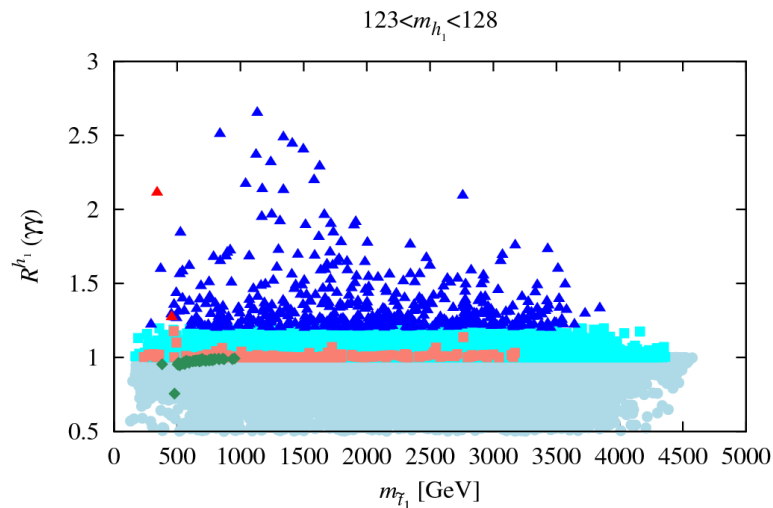
	LEP/Teva	B-physics	$\Omega h^2 > 0$	$\delta a_\mu (\times 10^{10})$	XENON100	$R^{h_1/h_2}(\gamma\gamma)$
●	✓	✓	0 – 0.136	×	✓	[0.5, 1]
■	✓	✓	0 – 0.094	×	✓	(1, 1.2]
▲	✓	✓	0 – 0.094	×	✓	> 1.2
■	✓	✓	0.094-0.136	×	✓	(1, 1.2]
▲	✓	✓	0.094-0.136	×	✓	> 1.2
◆	✓	✓	0.094 – 0.136	4.27-49.1	✓	$\sim 1$



**Figure 1:** The plot shows  $R_{gg}(\gamma\gamma)$  for the cases of  $123 < m_{h_1} < 128$  GeV and  $123 < m_{h_2} < 128$  GeV. Note: red triangle (orange square) is for WMAP window with  $R_{gg}(\gamma\gamma) > 1.2$  ( $R_{gg}(\gamma\gamma) = [1, 1.2]$ ).



**Figure 2:** Observe the clear general increase in maximum  $R_{gg}(\gamma\gamma)$  with increasing  $\lambda$ . Green points have good  $\delta a_\mu$ ,  $m_{h_2} > 1$  TeV **BUT**  $R_{gg}(\gamma\gamma) \sim 1$ .



**Figure 3:** The lightest stop has mass  $\sim 300 - 700$  GeV for red-triangle points.

- **If we ignore  $\delta a_\mu$** , then  $R_{gg}(\gamma\gamma) > 1.2$  (even  $> 2$ ) is possible while satisfying all other constraints provided  $h_1$  and  $h_2$  are close in mass, especially in the case where  $m_{h_2} \in [123, 128]$  GeV window.
  - This raises the issue of scenarios in which *both*  $m_{h_1}$  and  $m_{h_2}$  are in the  $[123, 128]$  GeV window where the experiments see the Higgs signal.
  - If  $h_1$  and  $h_2$  are sufficiently degenerate, the experimentalists might not have resolved the two distinct peaks, even in the  $\gamma\gamma$  channel.
  - The rates for the  $h_1$  and  $h_2$  could then add together to give an enhanced  $\gamma\gamma$ , for example, signal.
  - The apparent width or shape of the  $\gamma\gamma$  mass distribution could be altered.
  - There is more room for an apparent mismatch between the  $\gamma\gamma$  channel and other channels, such as  $b\bar{b}$  or  $4\ell$ , than in non-degenerate situation.
- In particular, the  $h_1$  and  $h_2$  will generally have different  $gg$  and  $VV$  production rates and branching ratios.

# Degenerate NMSSM Higgs Scenarios:

(arXiv:1207.1545, JFG, Jiang, Kraml)

- For the numerical analysis, we use NMSSMTools version 3.2.0, which has improved convergence of RGEs in the case of large Yukawa couplings.
- The precise constraints imposed are the following.
  1. Basic constraints: proper RGE solution, no Landau pole, neutralino LSP, Higgs and SUSY mass limits as implemented in NMSSMTools-3.2.0.
  2.  $B$  physics:  $\text{BR}(B_s \rightarrow X_s \gamma)$ ,  $\Delta M_s$ ,  $\Delta M_d$ ,  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$  (old upper limit),  $\text{BR}(B^+ \rightarrow \tau^+ \nu_\tau)$  and  $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$  at  $2\sigma$  as encoded in NMSSMTools-3.2.0, plus updates.
  3. Dark Matter:  $\Omega h^2 < 0.136$ , thus allowing for scenarios in which the relic density arises at least in part from some other source.  
However, we single out points with  $0.094 \leq \Omega h^2 \leq 0.136$ , which is the ‘WMAP window’ defined in NMSSMTools-3.2.0.

4. 2011 XENON 100: spin-independent LSP–proton scattering cross section bounds implied by the neutralino-mass-dependent XENON100 bound. (For points with  $\Omega h^2 < 0.094$ , we rescale these bounds by a factor of  $0.11/\Omega h^2$ .) (2012 XENON 100 has little additional impact.)
5.  $\delta a_\mu$  ignored: impossible to satisfy for scenarios we study here.

- Compute the effective Higgs mass in given production and final decay channels  $Y$  and  $X$ , respectively, and  $R_{gg}^h$  as

$$m_h^Y(X) \equiv \frac{R_Y^{h_1}(X)m_{h_1} + R_Y^{h_2}(X)m_{h_2}}{R_Y^{h_1}(X) + R_Y^{h_2}(X)} \quad R_Y^h(X) = R_Y^{h_1}(X) + R_Y^{h_2}(X). \quad (5)$$

- The extent to which it is appropriate to combine the rates from the  $h_1$  and  $h_2$  depends upon the degree of degeneracy and the experimental resolution.

Very roughly, one should probably think of  $\sigma_{\text{res}} \sim 1.5$  GeV or larger. **The widths of the  $h_1$  and  $h_2$  are very much smaller than this resolution.**

- We perform scans covering the following parameter ranges:

$$0 \leq m_0 \leq 3000; \quad 100 \leq m_{1/2} \leq 3000; \quad 1 \leq \tan \beta \leq 40;$$

$$\begin{aligned}
& -6000 \leq A_0 \leq 6000; \quad 0.1 \leq \lambda \leq 0.7; \quad 0.05 \leq \kappa \leq 0.5; \\
& -1000 \leq A_\lambda \leq 1000; \quad -1000 \leq A_\kappa \leq 1000; \quad 100 \leq \mu_{eff} \leq 500. \quad (6)
\end{aligned}$$

We only display points which pass the basic constraints, satisfy  $B$ -physics constraints, have  $\Omega h^2 < 0.136$ , obey the 2011 XENON100 limit on the LSP scattering cross-section off protons *and* have *both*  $h_1$  and  $h_2$  in the desired mass range:  $123 \text{ GeV} < m_{h_1}, m_{h_2} < 128 \text{ GeV}$ .

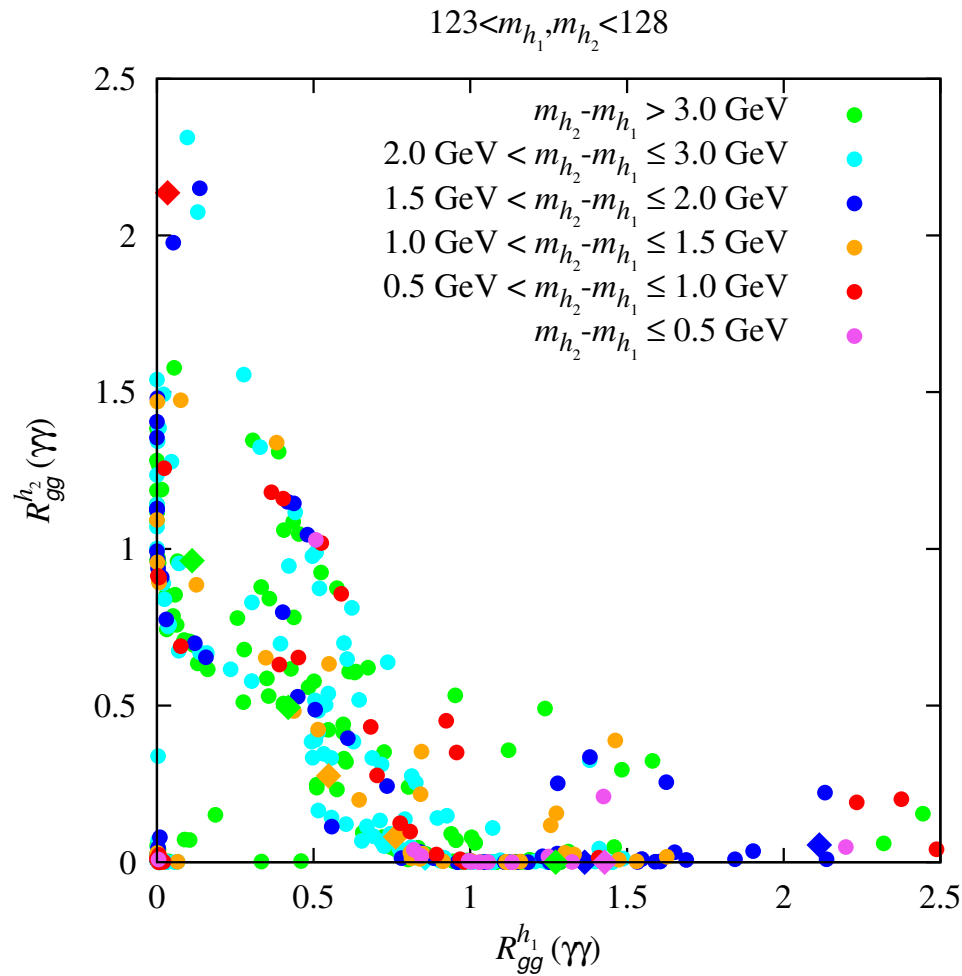
- In Fig. 4, points are color coded according to  $m_{h_2} - m_{h_1}$ .

**Circular points** have  $\Omega h^2 < 0.094$ , while **diamond points** have  $0.094 \leq \Omega h^2 \leq 0.136$  (*i.e.* lie within the WMAP window).

- Many of the displayed points are such that  $R_{gg}^{h_1}(\gamma\gamma) + R_{gg}^{h_2}(\gamma\gamma) > 1$ .
- A few such points have  $\Omega h^2$  in the WMAP window.

These points are such that either  $R_{gg}^{h_1}(\gamma\gamma) > 2$  or  $R_{gg}^{h_2}(\gamma\gamma) > 2$ , with the  $R_{gg}^h(\gamma\gamma)$  for the other Higgs being small.

- However, the majority of the points with  $R_{gg}^{h_1}(\gamma\gamma) + R_{gg}^{h_2}(\gamma\gamma) > 1$  have  $\Omega h^2 < 0.094$  and the  $\gamma\gamma$  signal is often shared between the  $h_1$  and the  $h_2$ .

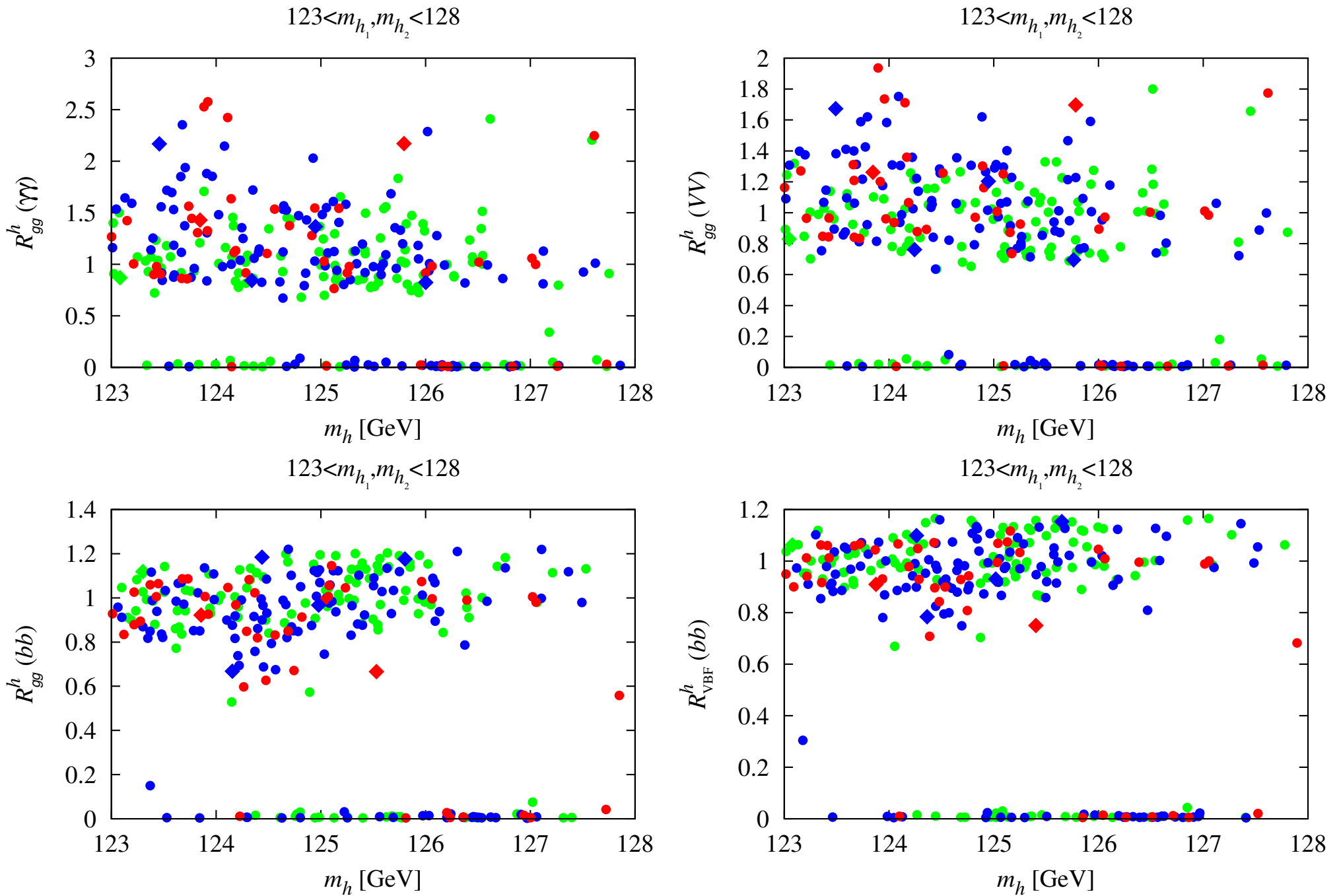


**Figure 4:** Correlation of  $gg \rightarrow (h_1, h_2) \rightarrow \gamma\gamma$  signal strengths when both  $h_1$  and  $h_2$  lie in the 123–128 GeV mass range. The circular points have  $\Omega h^2 < 0.094$ , while diamond points have  $0.094 \leq \Omega h^2 \leq 0.136$ . Points are color coded according to  $m_{h_2} - m_{h_1}$ . Probably green and cyan points can be resolved in mass.

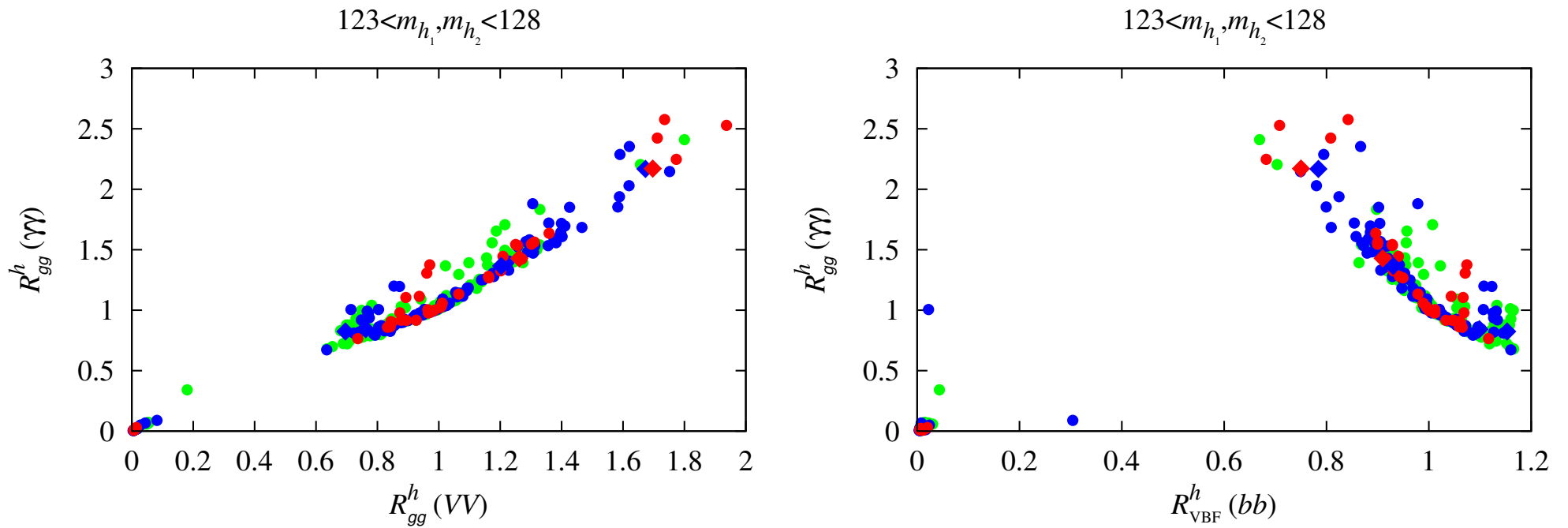
Now combine the  $h_1$  and  $h_2$  signals as described above. Recall: circular (diamond) points have  $\Omega h^2 < 0.094$  ( $0.094 \leq \Omega h^2 \leq 0.136$ ). Color code:

1. **red** for  $m_{h_2} - m_{h_1} \leq 1$  GeV;
  2. **blue** for  $1 \text{ GeV} < m_{h_2} - m_{h_1} \leq 2$  GeV;
  3. **green** for  $2 \text{ GeV} < m_{h_2} - m_{h_1} \leq 3$  GeV.
- For current statistics and  $\sigma_{\text{res}} \gtrsim 1.5$  GeV we estimate that the  $h_1$  and  $h_2$  signals will not be seen separately for  $m_{h_2} - m_{h_1} \leq 2$  GeV.
  - In Fig. 5, we show results for  $R_{gg}^h(X)$  for  $X = \gamma\gamma, VV, b\bar{b}$ . Enhanced  $\gamma\gamma$  and  $VV$  rates from gluon fusion are very common.
  - The bottom-right plot shows that enhancement in the  $Vh$  with  $h \rightarrow b\bar{b}$  rate is also natural, though not as large as the best fit value suggested by the new Tevatron analysis.
  - Diamond points (*i.e.* those in the WMAP window) are rare, but typically show enhanced rates.





**Figure 5:**  $R_{gg}^h(X)$  for  $X = \gamma\gamma, VV, b\bar{b}$ , and  $R_{VBF}^h(b\bar{b})$  versus  $m_h$ . For application to the Tevatron, note that  $R_{VBF}^h(b\bar{b}) = R_{V^* \rightarrow Vh}^h(b\bar{b})$ .



**Figure 6:** Left: correlation between the gluon fusion induced  $\gamma\gamma$  and  $VV$  rates relative to the SM. Right: correlation between the gluon fusion induced  $\gamma\gamma$  rate and the  $VV$  fusion induced  $b\bar{b}$  rates relative to the SM; the relative rate for  $V^* \rightarrow Vh$  with  $h \rightarrow b\bar{b}$  (relevant for the Tevatron) is equal to the latter.

- **Comments on Fig. 6:**

1. Left-hand plot shows the strong correlation between  $R_{gg}^h(\gamma\gamma)$  and  $R_{gg}^h(VV)$ .

Note that if  $R_{gg}^h(\gamma\gamma) \sim 1.5$ , as suggested by current experimental results, then in this model  $R_{gg}^h(VV) \geq 1.2$ .

2. The right-hand plot shows the (anti) correlation between  $R_{gg}^h(\gamma\gamma)$  and  $R_{V^* \rightarrow Vh}^h(b\bar{b}) = R_{VBF}^h(b\bar{b})$ .

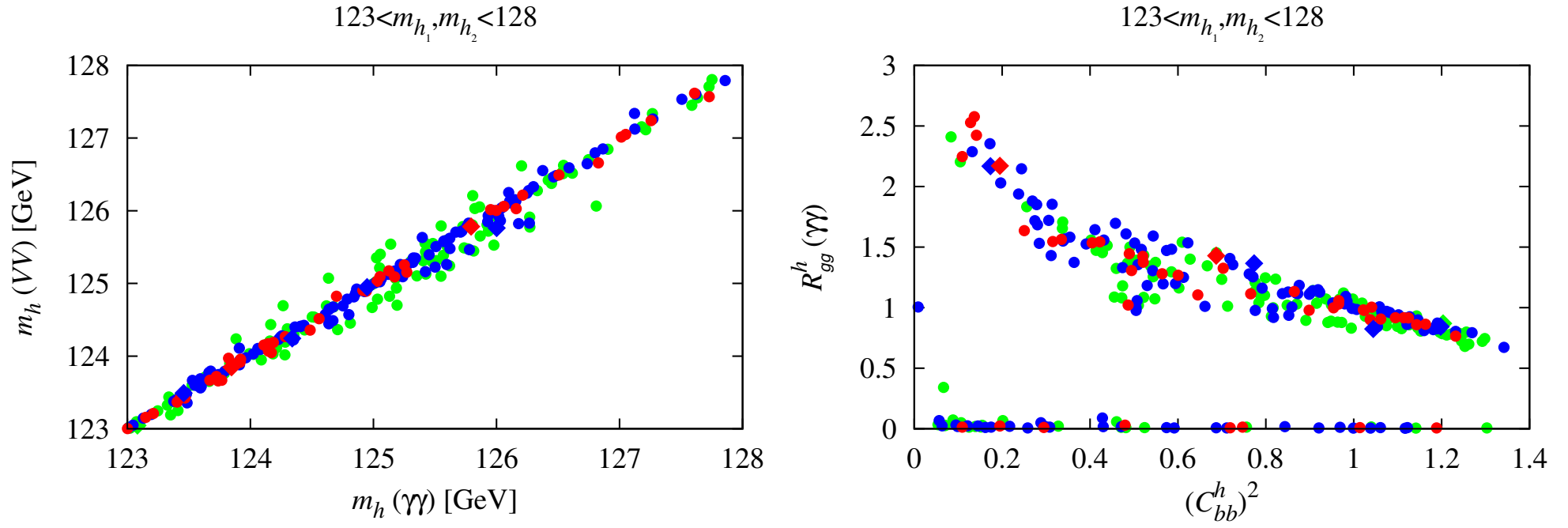
In general, the larger  $R_{gg}^h(\gamma\gamma)$  is, the smaller the value of  $R_{V^* \rightarrow Vh}^h(b\bar{b})$ .

However, this latter plot shows that there *are* parameter choices for which both the  $\gamma\gamma$  rate at the LHC and the  $V^* \rightarrow Vh(\rightarrow b\bar{b})$  rate at the Tevatron (and LHC) can be enhanced relative to the SM as a result of there being contributions to these rates from both the  $h_1$  and  $h_2$ .

3. It is often the case that one of the  $h_1$  or  $h_2$  dominates  $R_{gg}^h(\gamma\gamma)$  while the other dominates  $R_{V^* \rightarrow Vh}^h(b\bar{b})$ . This is typical of the diamond WMAP-window points.

However, a significant number of the circular  $\Omega h^2 < 0.094$  points are such that either the  $\gamma\gamma$  or the  $b\bar{b}$  signal receives substantial contributions from both the  $h_1$  and the  $h_2$ .

We did not find points where the  $\gamma\gamma$  and  $b\bar{b}$  final states *both* receive substantial contributions from *both* the  $h_1$  and  $h_2$ .



**Figure 7:** Left: effective Higgs masses obtained from different channels:  $m_h^{gg}(\gamma\gamma)$  versus  $m_h^{gg}(VV)$ . Right:  $\gamma\gamma$  signal strength  $R_{gg}^h(\gamma\gamma)$  versus effective coupling to  $b\bar{b}$  quarks  $(C_{b\bar{b}}^h)^2$ . Here,  $C_{b\bar{b}}^h \equiv [R_{gg}^{h_1}(\gamma\gamma)C_{b\bar{b}}^{h_1} + R_{gg}^{h_2}(\gamma\gamma)C_{b\bar{b}}^{h_2}] / [R_{gg}^{h_1}(\gamma\gamma) + R_{gg}^{h_2}(\gamma\gamma)]$ .

### Comments on Fig. 7

1. The  $m_h$  values for the gluon fusion induced  $\gamma\gamma$  and  $VV$  cases are also strongly correlated — in fact, they differ by no more than a fraction of a

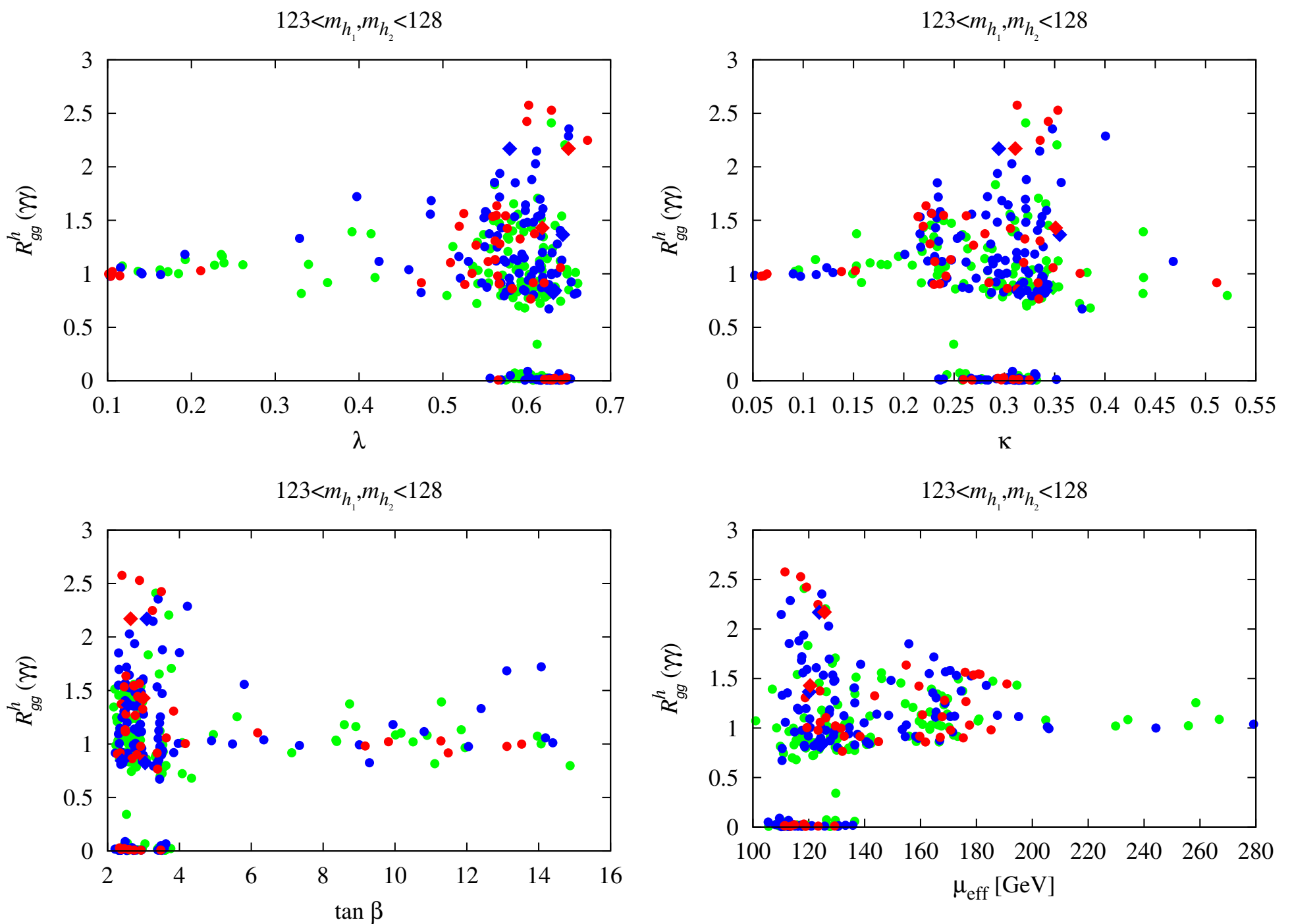
GeV and are most often much closer, see the left plot of Fig. 7.

2. The right plot of Fig. 7 illustrates the mechanism behind enhanced rates, namely that large net  $\gamma\gamma$  branching ratio is achieved by reducing the average total width by reducing the average  $b\bar{b}$  coupling strength.

- The dependence of  $R_{gg}^h(\gamma\gamma)$  on  $\lambda$ ,  $\kappa$ ,  $\tan\beta$  and  $\mu_{\text{eff}}$  is illustrated in Fig. 8.

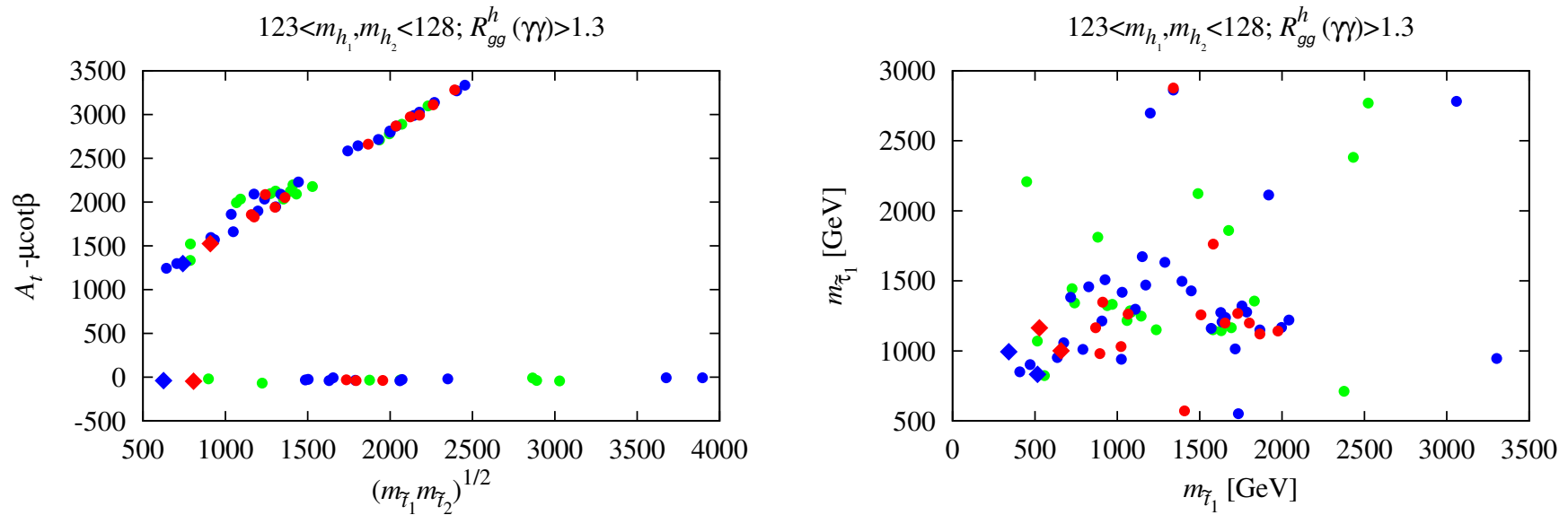
We observe that the largest  $R_{gg}^h(\gamma\gamma)$  values arise at large  $\lambda$ , moderate  $\kappa$ , small  $\tan\beta < 5$  (but note that  $R_{gg}^h(\gamma\gamma) > 1.5$  is possible even for  $\tan\beta = 15$ ) and small  $\mu_{\text{eff}} < 150$  GeV.

Such low values of  $\mu_{\text{eff}}$  are very favorable in point of view of fine-tuning, in particular if stops are also light.



**Figure 8:** Dependence of  $R_{gg}^h(\gamma\gamma)$  on  $\lambda$ ,  $\kappa$ ,  $\tan \beta$  and  $\mu_{\text{eff}}$ .

**Fig. 9** shows that the stop mixing is typically large in these cases,  $(A_t - \mu_{\text{eff}} \cot \beta) / M_{\text{SUSY}} \approx 1.5\text{--}2$ . Moreover, the few points which we found in the WMAP window always have  $m_{\tilde{t}_1} < 700$  GeV.

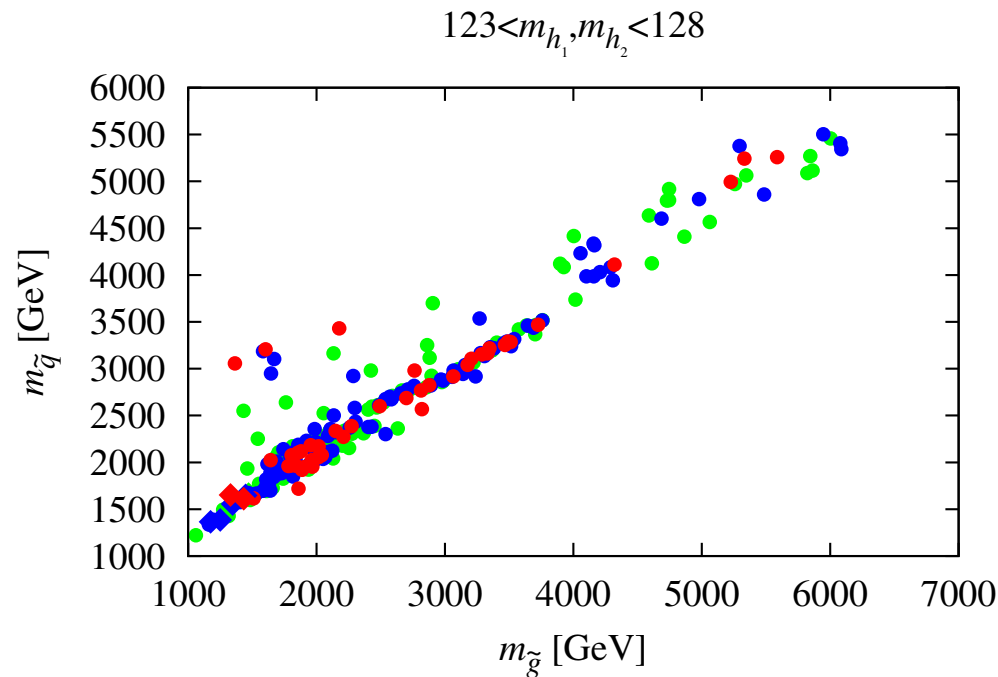


**Figure 9:** Left: Stop mixing parameter vs.  $M_{\text{SUSY}} \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$ . Right:  $m_{\tilde{\tau}_1}$  vs.  $m_{\tilde{t}_1}$ . Points plotted have  $R_{gg}^h(\gamma\gamma) > 1.3$ .

- Implications of the enhanced  $\gamma\gamma$  rate scenarios for other observables are also quite interesting.

First, let us observe from Fig. 10 that these scenarios have squark and gluino masses that are above about 1.25 TeV ranging up to as high as 6 TeV (where our scanning more or less ended).

The WMAP-window points with large  $R_{gg}^h(\gamma\gamma)$  are located at low masses of  $m_{\tilde{g}} \sim 1.3$  TeV and  $m_{\tilde{q}} \sim 1.6$  TeV.



**Figure 10:** Average light-flavor squark mass,  $m_{\tilde{q}}$ , versus gluino mass,  $m_{\tilde{g}}$ , for the points plotted in the previous figures.



- The value of  $R_{gg}^h(\gamma\gamma)$  as a function of the masses of the other Higgs bosons is illustrated in Fig. 11.

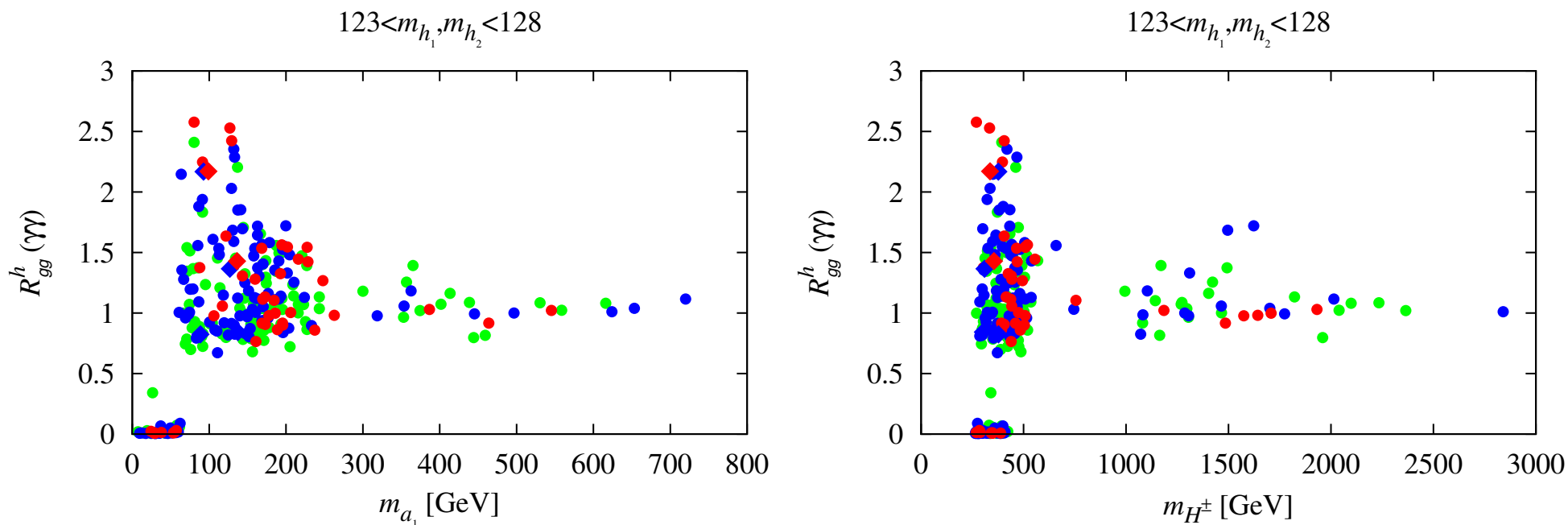


Figure 11:  $R_{gg}^h(\gamma\gamma)$  versus the masses of  $m_{a_1}$  and  $m_{H^\pm}$  (note that  $m_{H^\pm} \simeq m_{a_2} \simeq m_{h_3}$ ).

### Comments on Fig. 11:

1. We see that values above of  $R^h(\gamma\gamma) > 1.7$  are associated with masses

for the  $a_2$ ,  $h_3$  and  $H^\pm$  of order  $\lesssim 500$  GeV and for the  $a_1$  of order  $\lesssim 150$  GeV.

(Note that  $m_{a_2} \simeq m_{h_3} \simeq m_{H^\pm}$ )

Although these states have moderate masses, their detectability requires further study.

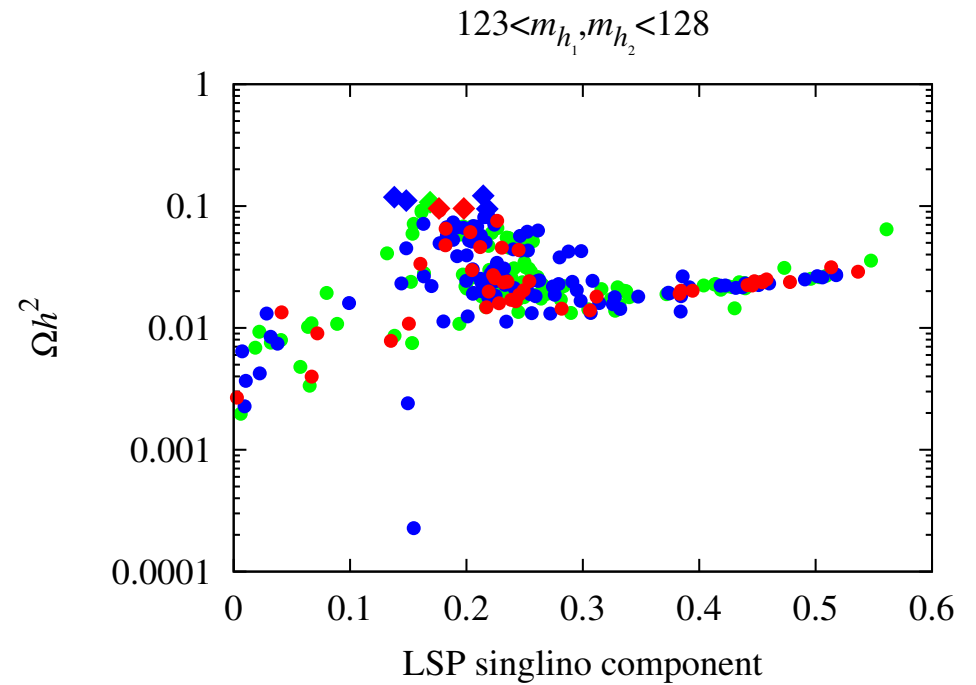
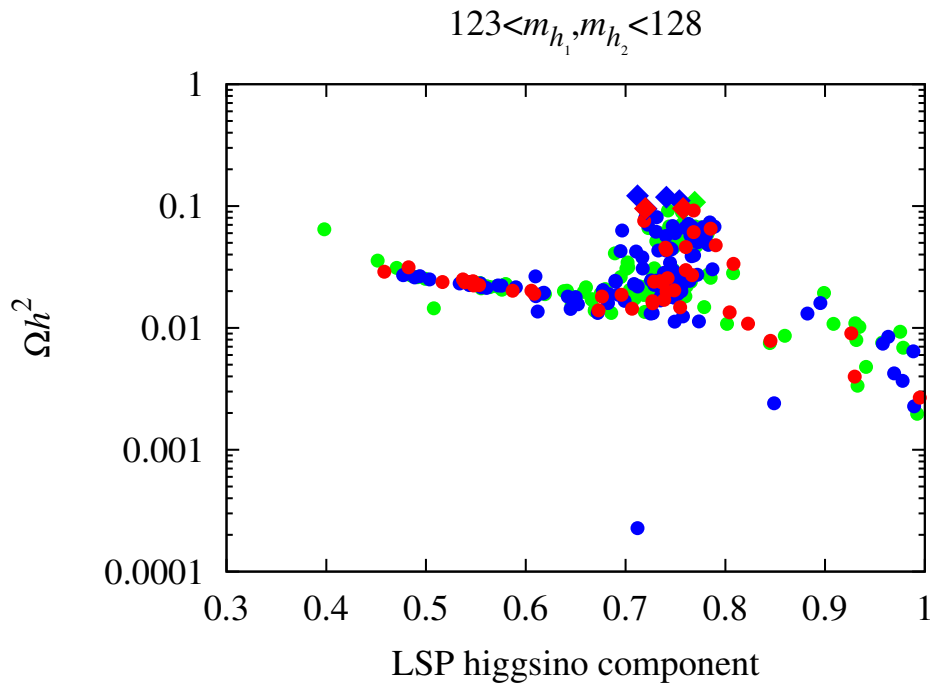
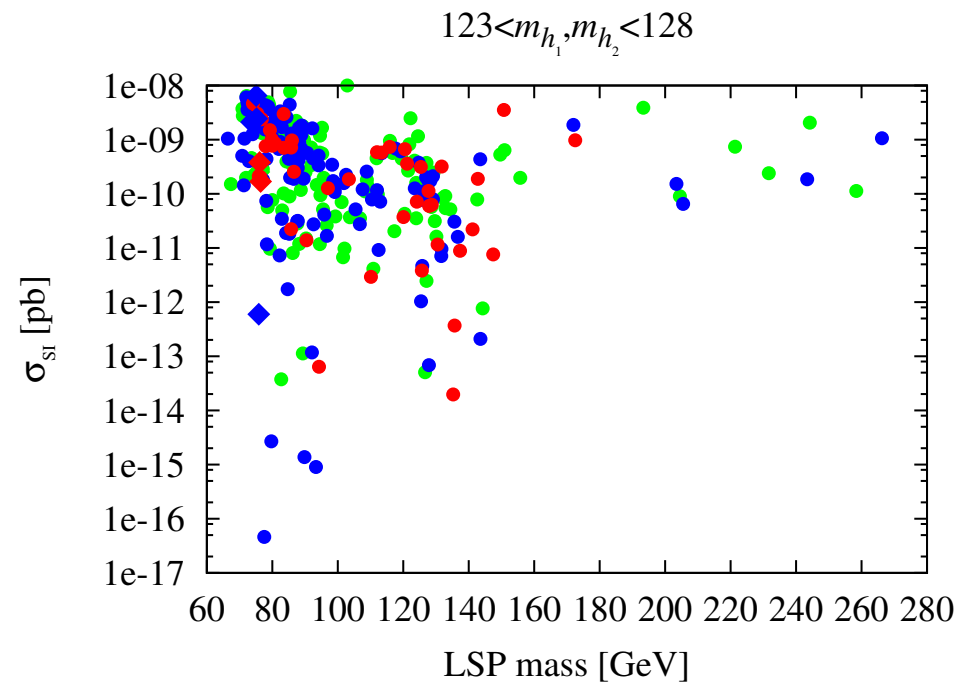
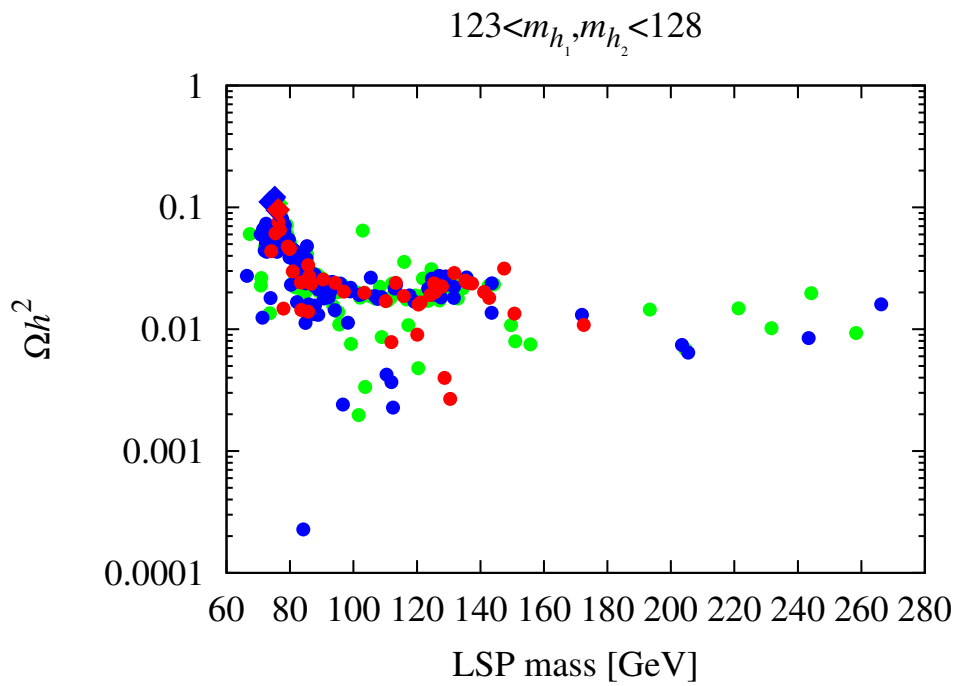
2. One interesting point is that  $m_{a_1} \sim 125$  GeV is common for points with  $R_{gg}^h(\gamma\gamma) > 1$  points.

We have checked that  $R_{gg}^{a_1}(\gamma\gamma)$  is quite small for such points — typically  $\lesssim 0.01$ .

- In Fig. 12, we display  $\Omega h^2$  and the spin-independent cross section for LSP scattering on protons,  $\sigma_{SI}$ , for the points plotted in previous figures.

Comments on Fig. 12:

1. Very limited range of LSP masses consistent with the WMAP window, roughly  $m_{\tilde{\chi}_1^0} \in [60, 80]$  GeV.
2. Corresponding  $\sigma_{SI}$  values range from *few*  $\times 10^{-9}$  pb to as low as *few*  $\times 10^{-11}$  pb.



**Figure 12:** Top row:  $\Omega h^2$  and spin-independent cross section on protons versus LSP mass for the points plotted in previous figures. Bottom row:  $\Omega h^2$  versus LSP higgsino (left) and singlino (right) components.

3. Owing to the small  $\mu_{\text{eff}}$ , the LSP is dominantly higgsino, which is also the reason for  $\Omega h^2$  typically being too low.

The points with  $\Omega h^2$  within the WMAP window are mixed higgsino–singlino, with a singlino component of the order of 20%, see the bottom-row plots of Fig. 12.

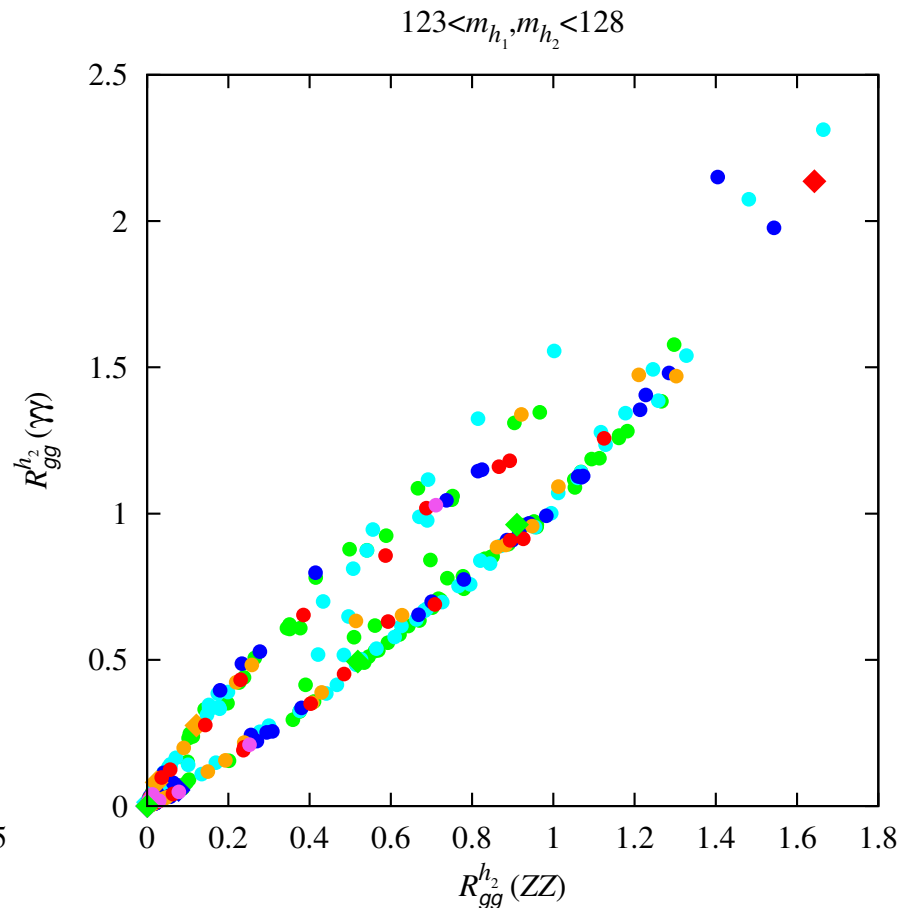
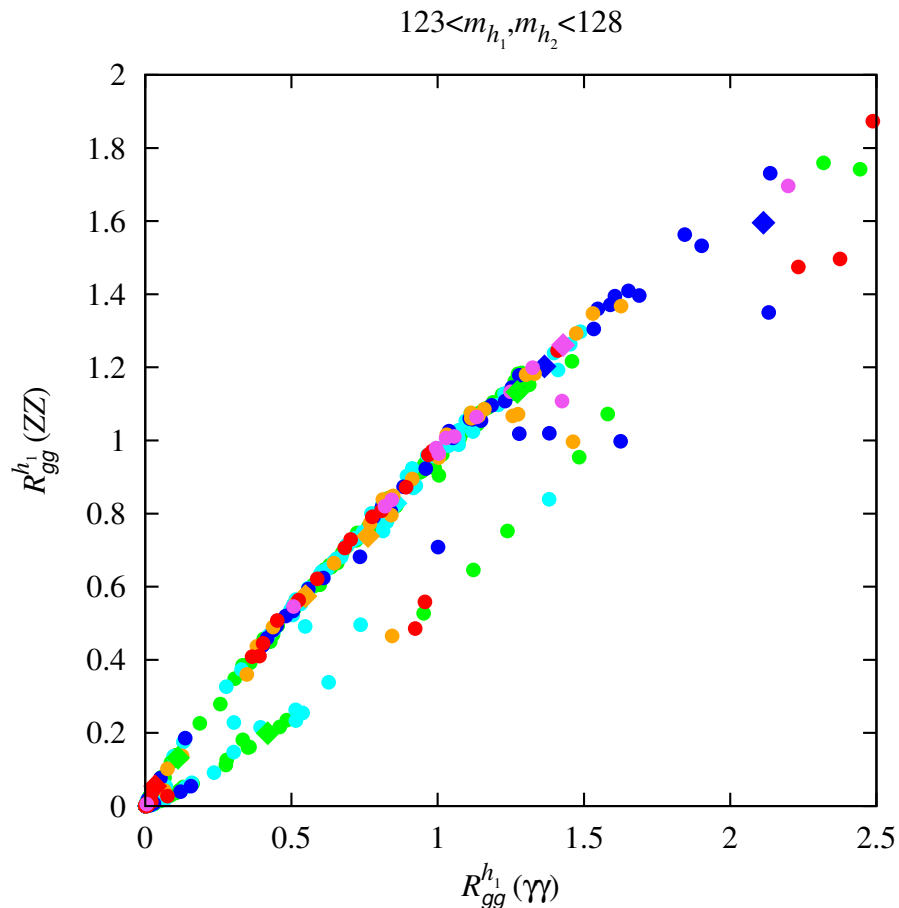
- It is interesting to note a few points regarding the parameters associated with the points plotted in previous figures.
  1. For the WMAP-window diamond points,  $\lambda \in [0.58, 0.65]$ ,  $\kappa \in [0.28, 0.35]$ , and  $\tan \beta \in [2.5, 3.5]$ .
  2. Points with  $R_{gg}^h(\gamma\gamma) > 1.3$  have  $\lambda \in [0.33, 0.67]$ ,  $\kappa \in [0.22, 0.36]$ , and  $\tan \beta \in [2, 14]$ .
- Can't find scenarios of this degenerate/enhanced type such that  $\delta a_\mu$  is consistent with that needed to explain the current discrepancy.

In particular, the very largest value of  $\delta a_\mu$  achieved is of order  $1.8 \times 10^{-10}$  and, further, the WMAP-window points with large  $R_{gg}^h(\gamma\gamma, VV)$  have  $\delta a_\mu < 6 \times 10^{-11}$ .

## Two Higgs separated by 3 GeV or so

- Return to scenarios of previous section and analyze more closely.
- $h_1$  should have  $ZZ$  rate not too much smaller than SM-like rate, but suppressed  $\gamma\gamma$  rate.
- $h_2$  should have enhanced  $\gamma\gamma$  and somewhat suppressed  $ZZ$  rate.

The basic issue is encapsulated in the following plots. The green and cyan points have  $m_{h_2} - m_{h_1} > 3$  GeV and  $m_{h_2} - m_{h_1} \in [2, 3]$  GeV, respectively. So, pay most attention to these colors.



- Left-hand figure shows that  $R^{h_1}(\gamma\gamma) \lesssim R^{h_1}(ZZ)$  along lower part of upper branch (the best branch).
- Right-hand figure shows that  $R^{h_2}(\gamma\gamma) > R^{h_2}(ZZ)$  by a substantial amount along the upper branch.
- Net result would be to shift  $ZZ$  mass lower and  $\gamma\gamma$  mass higher.
- Detailed fit needed to see if ATLAS mass discrepancy can be described.

# Diagnosing the presence of degenerate Higgses

(J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1208.1817)

- Given that enhanced  $R_{gg}^h$  is very natural if there are degenerate Higgs mass eigenstates, **how do we detect degeneracy?** Must look at correlations among different  $R^h$ 's.
- In the context of any doublets plus singlets model not all the  $R^{h_i}$ 's are independent; a complete independent set of  $R^h$ 's can be taken to be:

$$R_{gg}^h(VV), \quad R_{gg}^h(bb), \quad R_{gg}^h(\gamma\gamma), \quad R_{VBF}^h(VV), \quad R_{VBF}^h(bb), \quad R_{VBF}^h(\gamma\gamma). \quad (7)$$

Let us now look in more detail at a given  $R_Y^h(X)$ . It takes the form

$$R_Y^h(X) = \sum_{i=1,2} \frac{(C_Y^{h_i})^2 (C_X^{h_i})^2}{C_\Gamma^{h_i}} \quad (8)$$

where  $C_X^{h_i}$  for  $X = \gamma\gamma, WW, ZZ, \dots$  is the ratio of the  $h_i X$  to  $h_{SM} X$  coupling and  $C_\Gamma^{h_i}$  is the ratio of the total width of the  $h_i$  to the SM Higgs

total width. The diagnostic tools that can reveal the existence of a second, quasi-degenerate (but non-interfering in the small width approximation) Higgs state are the double ratios:

$$\text{I): } \frac{R_{VBF}^h(\gamma\gamma)/R_{gg}^h(\gamma\gamma)}{R_{VBF}^h(bb)/R_{gg}^h(bb)}, \quad \text{II): } \frac{R_{VBF}^h(\gamma\gamma)/R_{gg}^h(\gamma\gamma)}{R_{VBF}^h(VV)/R_{gg}^h(VV)}, \quad \text{III): } \frac{R_{VBF}^h(VV)/R_{gg}^h(VV)}{R_{VBF}^h(bb)/R_{gg}^h(bb)}, \quad (9)$$

each of which should be unity if only a single Higgs boson is present but, due to the non-factorizing nature of the sum in Eq. (8), are generally expected to deviate from 1 if two (or more) Higgs bosons are contributing to the net  $h$  signals.

In a doublets+singlets model all other double ratios that are equal to unity for single Higgs exchange are not independent of the above three.

Of course, the above three double ratios are not all independent.

Which will be most useful depends upon the precision with which the  $R^h$ 's for different initial/final states can be measured.

E.g measurements of  $R^h$  for the  $bb$  final state may continue to be somewhat imprecise and it is then double ratio II) that might prove most discriminating.



Or, it could be that one of the double ratios deviates from unity by a much larger amount than the others, in which case it might be most discriminating even if the  $R^h$ 's involved are not measured with great precision.

- In Fig. 13, we plot the numerator versus the denominator of the double ratios I) and II), [III) being very like I) due to the correlation between the  $R_{gg}^h(\gamma\gamma)$  and  $R_{gg}^h(VV)$  values discussed earlier].
- We observe that any one of these double ratios will often, but not always, deviate from unity (the diagonal dashed line in the figure).
- The probability of such deviation increases dramatically if we require (as apparently preferred by LHC data)  $R_{gg}^h(\gamma\gamma) > 1$ , see the solid (vs. open) symbols of Fig. 13.

This is further elucidated in Fig. 14 where we display the double ratios I) and II) as functions of  $R_{gg}^h(\gamma\gamma)$  (left plots).

For the NMSSM, it seems that the double ratio I) provides the greatest discrimination between degenerate vs. non-degenerate scenarios with values

very substantially different from unity (the dashed line) for the majority of the degenerate NMSSM scenarios explored in the earlier section of this talk that have enhanced  $\gamma\gamma$  rates.

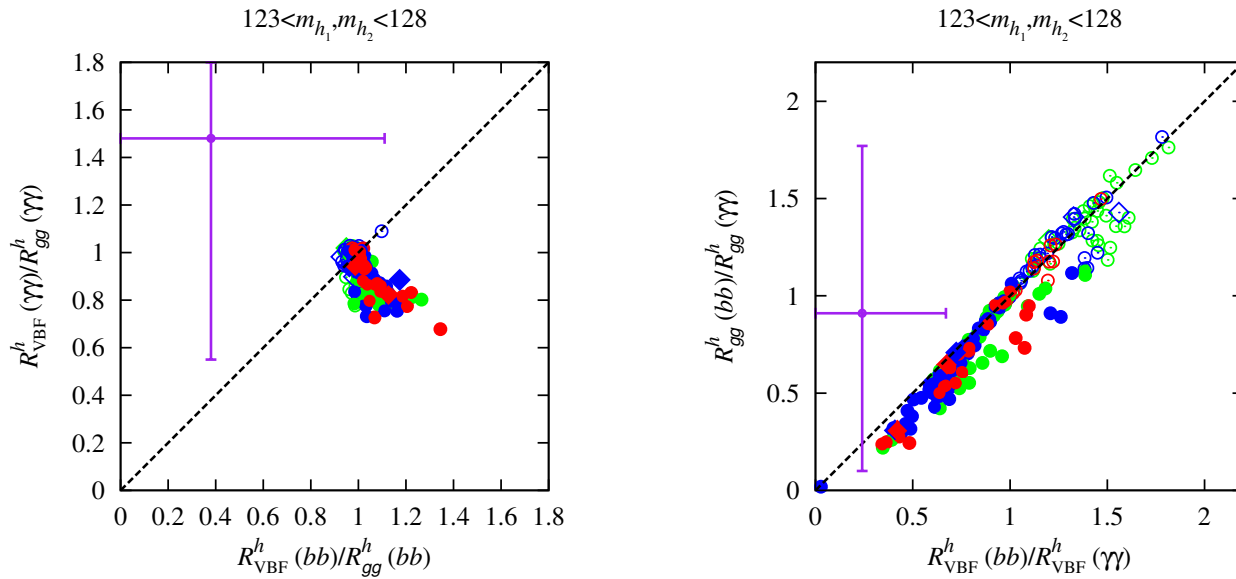
Note in particular that I), being sensitive to the  $b\bar{b}$  final state, singles out degenerate Higgs scenarios even when one or the other of  $h_1$  or  $h_2$  dominates the  $gg \rightarrow \gamma\gamma$  rate, see the top right plot of Fig. 14.

In comparison, double ratio II) is most useful for scenarios with  $R_{gg}^h(\gamma\gamma) \sim 1$ , as illustrated by the bottom left plot of Fig. 14.

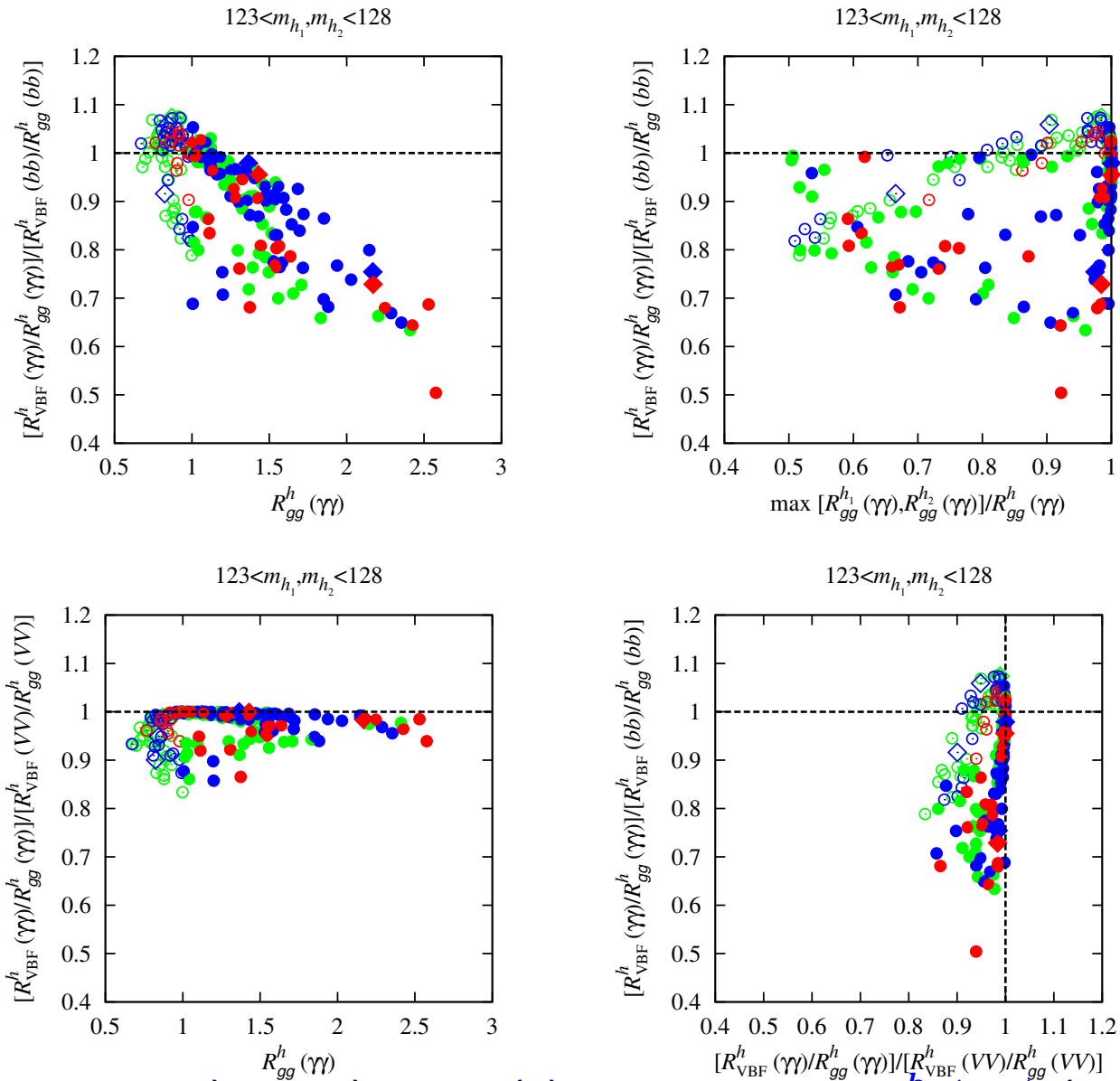
- Thus, as illustrated by the bottom right plot of Fig. 14, the greatest discriminating power is clearly obtained by measuring both double ratios.

In fact, a close examination reveals that there are no points for which *both* double ratios are exactly 1!

Of course, experimental errors may lead to a region containing a certain number of points in which both double ratios are merely consistent with 1 within the errors.



**Figure 13:** Comparisons of pairs of event rate ratios that should be equal if only a single Higgs boson is present. The color code is green for points with  $2 \text{ GeV} < m_{h_2} - m_{h_1} \leq 3 \text{ GeV}$ , blue for  $1 \text{ GeV} < m_{h_2} - m_{h_1} \leq 2 \text{ GeV}$ , and red for  $m_{h_2} - m_{h_1} \leq 1 \text{ GeV}$ . Large diamond points have  $\Omega h^2$  in the WMAP window of  $[0.094, 0.136]$ , while circular points have  $\Omega h^2 < 0.094$ . Solid points are those with  $R_{gg}^h(\gamma\gamma) > 1$  and open symbols have  $R_{gg}^h(\gamma\gamma) \leq 1$ . Current experimental values for the ratios from CMS data along with their  $1\sigma$  error bars are also shown.



**Figure 14:** Double ratios I) and II) of Eq. (9) as functions of  $R_{gg}^h(\gamma\gamma)$  (on the left). On the right we show (top) double ratio I) vs.  $\max [R_{gg}^{h_1}(\gamma\gamma), R_{gg}^{h_2}(\gamma\gamma)] / R_{gg}^h(\gamma\gamma)$  and (bottom) double ratio I) vs. double ratio II) for the points displayed in Fig. 16. Colors and symbols are the same as in Fig. 16.

- What does current LHC data say about these various double ratios?

The central values and  $1\sigma$  error bars for the numerator and denominator of double ratios I) and II) obtained from CMS data (CMS-PAS-HIG-12-020) are also shown in Fig. 16.

Obviously, current statistics are inadequate to discriminate whether or not the double ratios deviate from unity.

About 100 times increased statistics will be needed. This will not be achieved until the  $\sqrt{s} = 14$  TeV run with  $\geq 100 \text{ fb}^{-1}$  of accumulated luminosity.

Nonetheless, it is clear that the double-ratio diagnostic tools will ultimately prove viable and perhaps crucial for determining if the  $\sim 125$  GeV Higgs signal is really only due to a single Higgs-like resonance or if two resonances are contributing.

Degeneracy has significant probability in model contexts if enhanced  $\gamma\gamma$  rates are indeed confirmed at higher statistics.

# Higgs at 125 GeV for LHC and 136 GeV for the Tevatron (and LHC?):

(G. Belanger, U. Ellwanger, J. F. Gunion, Y. Jiang and S. Kraml. arXiv:1208.4952)

- Need to reexamine in light of HCP data.
- However, some salient points that appear to remain relevant are the following:
  1. There is a clear signal for an  $H_1$  at  $\sim 125$  GeV.
  2. CMS may have an  $H_2$  at  $\sim 136$  GeV in the  $\gamma\gamma$  final state.  
ATLAS so far does not see a corresponding  $\gamma\gamma$  peak.
  3. If  $R_{VBF}^1(\tau\tau)$  at CMS and ATLAS remains somewhat suppressed while  $R_{VH}(b\bar{b})$  measured at the Tevatron remains enhanced over a broad  $M_{b\bar{b}}$  mass range and above what can come from the  $H_1$ , then an  $H_2$  with  $M_{H_2} \sim 135\text{--}136$  GeV could provide the source of the extra  $b\bar{b}$  events.  
**This possibility is one of the main advantages of this 125+136 idea.**

4. Of course, the  $H_2$  should not appear in the  $ZZ^*$  final state with much strength, since neither CMS nor ATLAS sees a  $4\ell$  mass peak near 136 GeV.

(CMS appears to have something at  $\sim 144$  GeV, but ATLAS has only fluctuations in the relevant mass region.)

- The NMSSM is flexible enough to easily give a relevant scenario, but the precise model proposed in our original paper will need some adjustment.

And, of course, ATLAS would eventually need to see some signal in the  $\gamma\gamma$  final state at 135 GeV.

## Higgses at 98 GeV for LEP and 125 GeV for LHC:

( G. Belanger, U. Ellwanger, J. F. Gunion, Y. Jiang, S. Kraml and J. H. Schwarz.  
arXiv:1210.1976)

- We demonstrate that the two lightest CP-even Higgs bosons,  $h_1$  and  $h_2$ , of the NMSSM could have properties such that the  $h_1$  fits the LEP excess at  $\sim 98$  GeV while the  $h_2$  is reasonably consistent with the Higgs-like LHC signals at  $\sim 125$  GeV, including in particular the larger-than-SM signal in the  $\gamma\gamma$  channel.

To describe the LEP and LHC data the  $h_1$  must be largely singlet and the  $h_2$  primarily doublet (mainly  $H_u$  for the scenarios we consider).

An  $h_2$  with  $m_{h_2} \sim 125$  GeV and enhanced  $\gamma\gamma$  rate is obtained, as in previous cases, at large  $\lambda$  and moderate  $\tan\beta$ .

- In order to display the ability of the NMSSM to simultaneously explain the LEP and LHC Higgs-like signals, we (once again) turn to NMSSM scenarios with semi-unified GUT scale soft-SUSY-breaking.



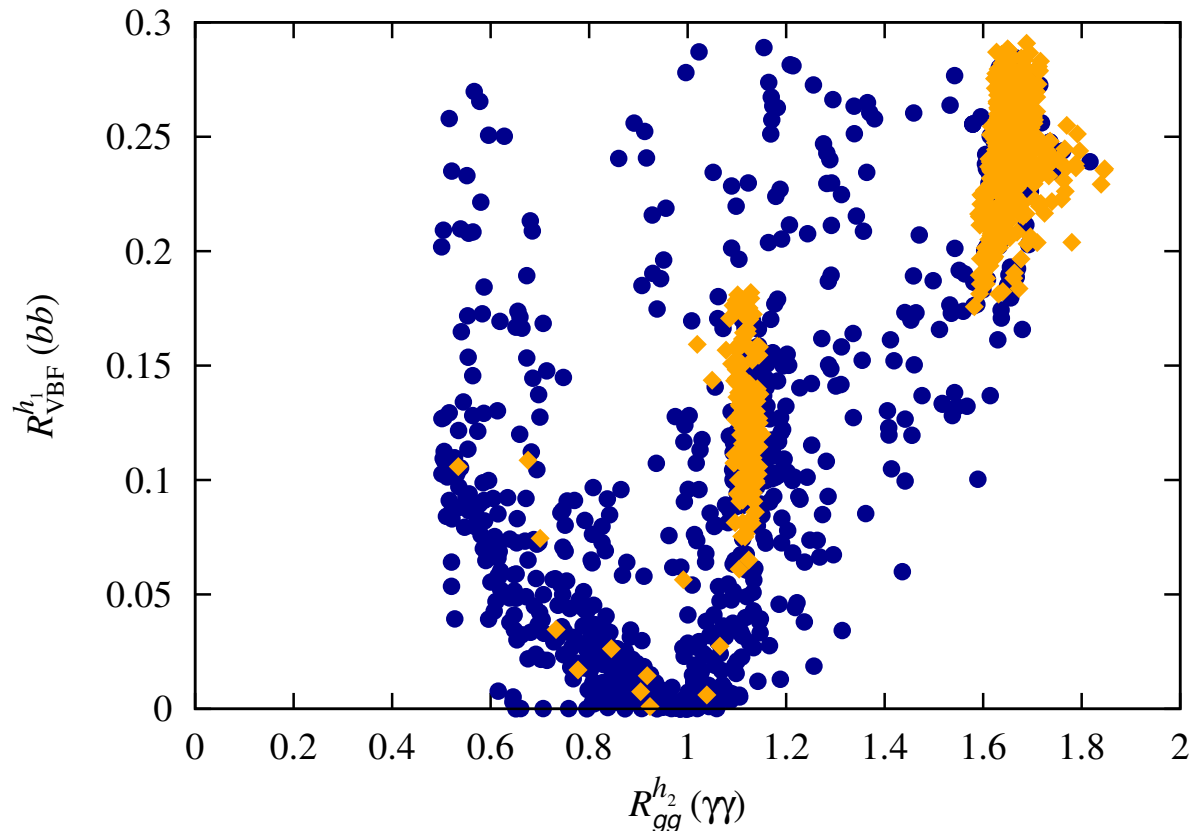
- All the accepted points correspond to scenarios that obey all experimental constraints (mass limits and flavor constraints as implemented in NMSSMTools,  $\Omega h^2 < 0.136$  and 2011 XENON100 constraints on the spin-independent scattering cross section) except that the SUSY contribution to the anomalous magnetic moment of the muon,  $\delta a_\mu$ , is too small to explain the discrepancy between the observed value of  $a_\mu$  and the SM prediction.
- Fig. 15, the crucial plot, shows  $R_{VBF}^{h_1}(bb)$  (which =  $R_{Z^* \rightarrow Zh_1}^{h_1}(bb)$  as for LEP) versus  $R_{gg}^{h_2}(\gamma\gamma)$  when  $m_{h_1} \in [96, 100]$  GeV and  $m_{h_2} \in [123, 128]$  GeV are imposed in addition to the above mentioned experimental constraints.<sup>1</sup>

(In this and all subsequent plots, points with  $\Omega h^2 < 0.094$  are represented by blue circles and points with  $\Omega h^2 \in [0.094, 0.136]$  (the "WMAP window") are represented by orange diamonds.)

Note that  $R_{VBF}^{h_1}(bb)$  values are required to be smaller than 0.3 by virtue of the fact that the LEP constraint on the  $e^+e^- \rightarrow Zb\bar{b}$  channel with  $M_{b\bar{b}} \sim 98$  GeV is included in the NMSSMTools program.

<sup>1</sup>Here the Higgs mass windows are designed to allow for theoretical errors in the computation of the Higgs masses.

Those points with  $R_{VBF}^{h_1}(bb)$  between about 0.1 and 0.25 would provide the best fit to the LEP excess.



**Figure 15:** Signal strengths (relative to SM)  $R_{VBF}^{h_1}(bb)$  versus  $R_{gg}^{h_2}(\gamma\gamma)$  for  $m_{h_1} \in [96, 100]$  GeV and  $m_{h_2} \in [123, 128]$  GeV. In this and all subsequent plots, points with  $\Omega h^2 < 0.094$  are represented by blue circles and points with  $\Omega h^2 \in [0.094, 0.136]$  (the "WMAP window") are represented by orange diamonds.

In all the remaining plots we will impose the additional requirements:  $R_{gg}^{h_2}(\gamma\gamma) > 1$  (for LHC enhancement) and  $0.1 \leq R_{VBF}^{h_1}(bb) \leq 0.25$  (for LEP fit).

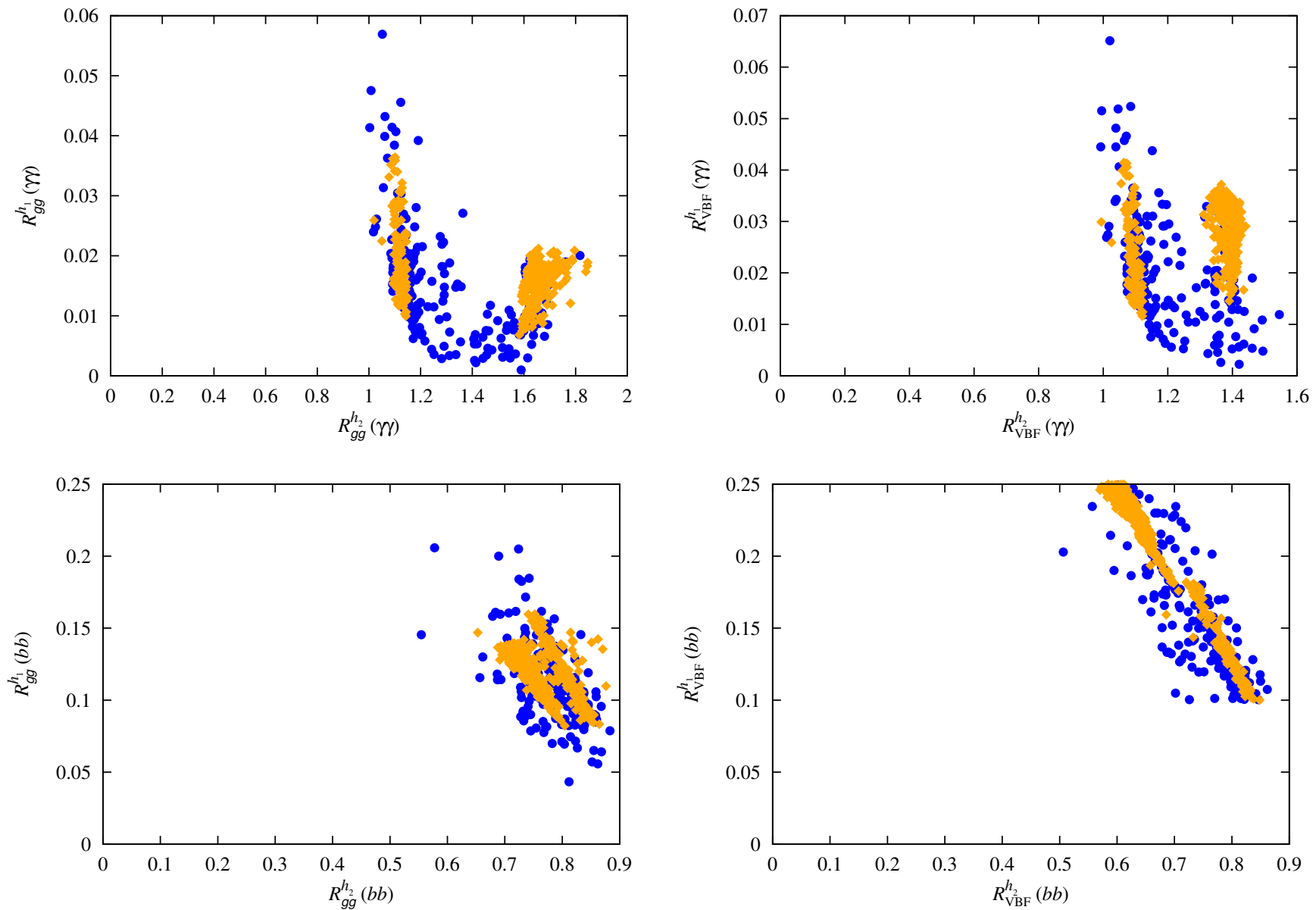
In the following, we will refer to these NMSSM scenarios as the “98 + 125 GeV Higgs scenarios” or “LEP-LHC scenarios”.

- Fig. 16 gives the essential results.

The upper plots show that the  $h_2$  can easily have an enhanced  $\gamma\gamma$  signal for both  $gg$  and VBF production whereas the  $\gamma\gamma$  signal arising from the  $h_1$  for both production mechanisms is quite small and unlikely to be observable.

Note the two different  $R_{gg}^{h_2}(\gamma\gamma)$  regions with orange diamonds (for which  $\Omega h^2$  lies in the WMAP window), one with  $R_{gg}^{h_2}(\gamma\gamma) \sim 1.1$  and the other with  $R_{gg}^{h_2}(\gamma\gamma) \sim 1.6$ . These same 2 regions emerge in many later figures.

The first region corresponds to  $m_{\tilde{\chi}_1^0} > 93$  GeV and  $m_{\tilde{t}_1} > 1.8$  TeV while the second region corresponds to  $m_{\tilde{\chi}_1^0} \sim 77$  GeV and  $m_{\tilde{t}_1}$  between 197 GeV and 1 TeV. If  $R_{gg}^{h_2}(\gamma\gamma)$  ends up converging to a large value, then masses for all strongly interacting SUSY particles would be close to current limits.



**Figure 16:** For  $h = h_1$  and  $h = h_2$ , we plot (top)  $R_{gg}^h(\gamma\gamma)$  and  $R_{VBF}^h(\gamma\gamma)$  and (bottom)  $R_{gg}^h(bb)$  and  $R_{VBF}^h(bb)$  we show only points satisfying all the basic constraints as well as  $m_{h_1} \in [96, 100]$  GeV,  $m_{h_2} \in [123, 128]$  GeV,  $R_{gg}^{h_2}(\gamma\gamma) > 1$  and  $R_{VBF}^{h_1}(bb) \in [0.1, 0.25]$ , *i.e.* the “98 + 125 GeV Higgs scenarios”.

- The **bottom row** of the figure focuses on the  $b\bar{b}$  final state. We observe the reduced  $R_{gg}^{h_2}(bb)$  and  $R_{VBF}^{h_2}(bb)$  values associated with reduced  $b\bar{b}$  width (relative to the SM) needed for enhanced  $R_{gg}^{h_2}(\gamma\gamma)$  and  $R_{VBF}^{h_2}(\gamma\gamma)$ .

The  $R_{gg}^{h_1}(bb)$  and  $R_{VBF}^{h_1}(bb)$  values  $\Rightarrow$  the  $h_1$  could not have been seen at the Tevatron nor (yet) at the LHC. Sensitivity to  $R_{gg}^{h_1}(bb)$  ( $R_{VBF}^{h_1}(bb)$ ) values from 0.05 to 0.2 (0.1 to 0.25) will be needed at the LHC.

This compares to expected sensitivities after the  $\sqrt{s} = 8$  TeV run in these channels to  $R$  values of at best 0.8.<sup>2</sup>

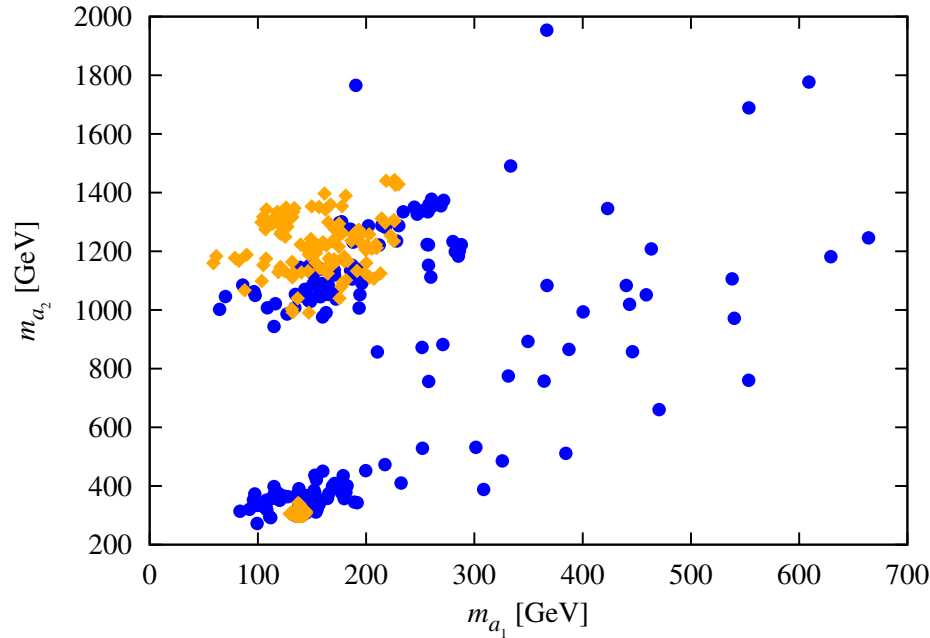
Statistically, a factor of 4 to 10 improvement requires integrated luminosity of order 16 to 100 times the current  $L = 10 \text{ fb}^{-1}$ . Such large  $L$  values will only be achieved after the LHC is upgraded to 14 TeV.

Finally, note that for WMAP-window points the largest  $R_{VBF}^{h_1}(bb)$  values occur for the light- $m_{\tilde{\chi}_1^0}$  point group described above for which supersymmetric particle masses are as small as possible.

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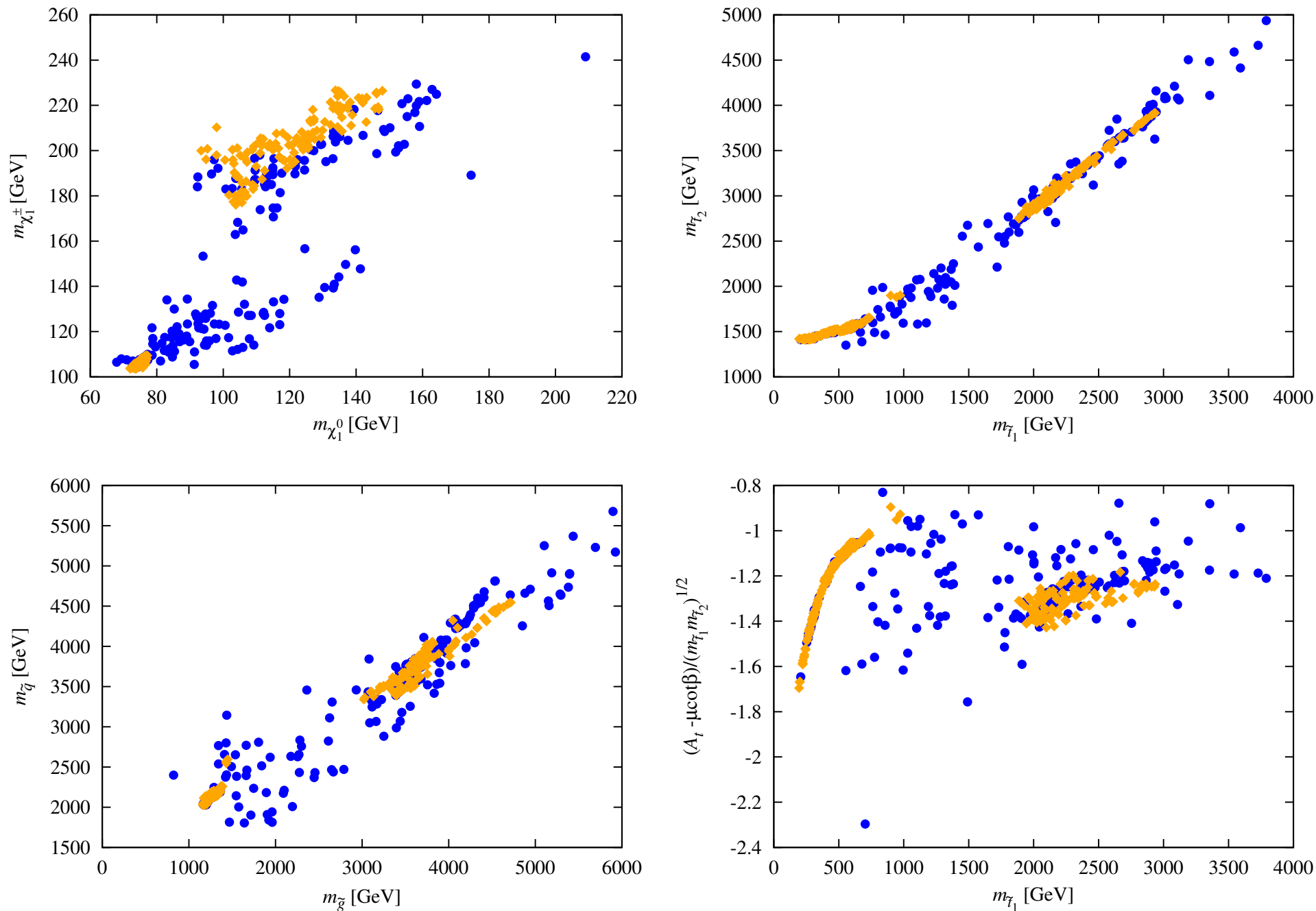
<sup>2</sup>Here, we have used Fig. 12 of cmshiggs extrapolated to a Higgs mass near 98 GeV and assumed  $L = 20 \text{ fb}^{-1}$  each for ATLAS and CMS.

- Other NMSSM particles, properties and parameters, including  $\tilde{\chi}_1^0$  and  $\tilde{\chi}_1^\pm$  compositions



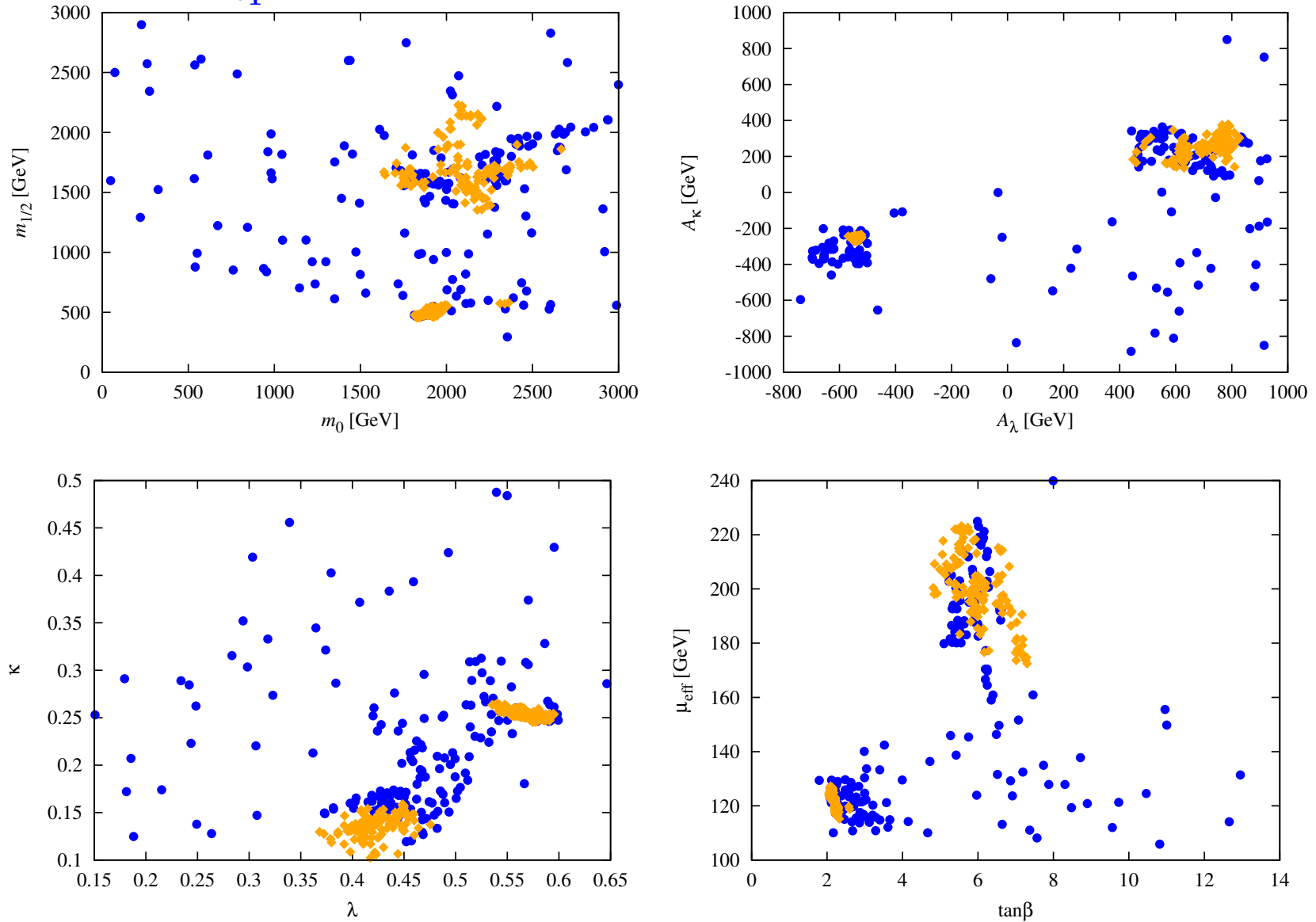
**Figure 17:** Scatter plot of  $m_{a_2}$  versus  $m_{a_1}$  for the 98+125 GeV scenario; note that  $m_{a_2} \simeq m_{h_3} \simeq m_{H^\pm}$ . Note that in this figure there is a dense region, located at  $(m_{a_1}, m_{a_2}) \sim (130, 330)$  GeV, of strongly overlapping orange diamond points. These are the points associated with the low- $m_{\tilde{\chi}_1^0}$  WMAP-window region of parameter space. Corresponding dense regions appear in other figures.

We note without a plot that the good  $\Omega h^2$  points all have  $m_{\tilde{\ell}_R}$ ,  $m_{\tilde{\nu}_\ell}$ ,  $m_{\tilde{\tau}_1}$  and  $m_{\tilde{\nu}_\tau}$  larger than 1.5 TeV.



**Figure 18:** Plots showing  $m_{\tilde{\chi}_1^0}$ ,  $m_{\tilde{\chi}_1^\pm}$ ,  $m_{\tilde{\tau}_1}$ ,  $m_{\tilde{\tau}_2}$ ,  $m_{\tilde{q}}$ ,  $m_{\tilde{g}}$ , and the mixing parameter  $(A_t - \mu \cot \beta) / \sqrt{m_{\tilde{\tau}_1} m_{\tilde{\tau}_2}}$ .

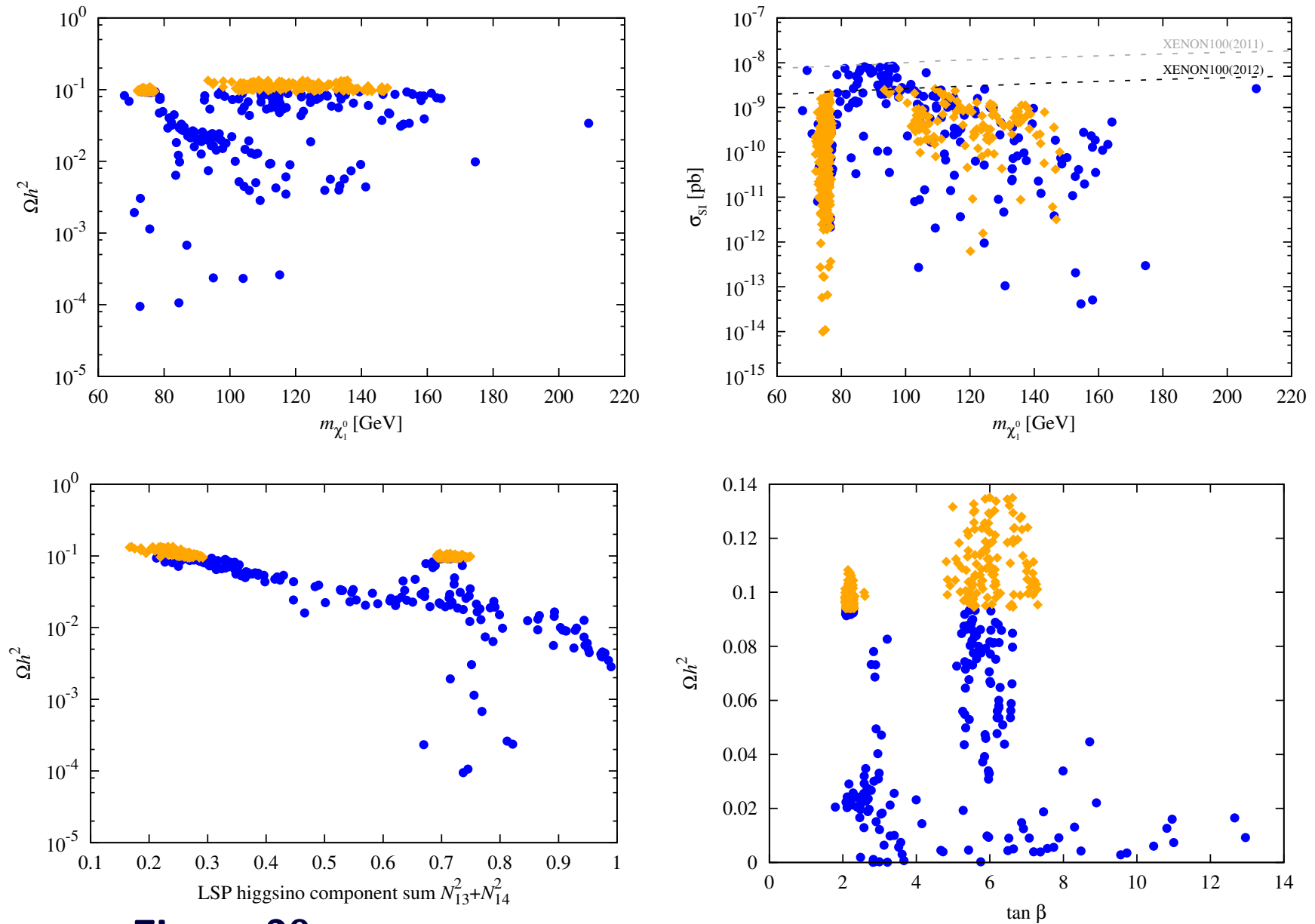
- **Input parameters** Note that the low- $m_{\tilde{\chi}_1^0}$  WMAP-window scenarios have not only low  $m_{\tilde{t}_1}$  but also low  $\mu_{\text{eff}}$ , implying not much fine-tuning.



**Figure 19:** GUT scale and SUSY scale parameters leading to the LEP–LHC scenarios.



## ● Dark Matter Issues



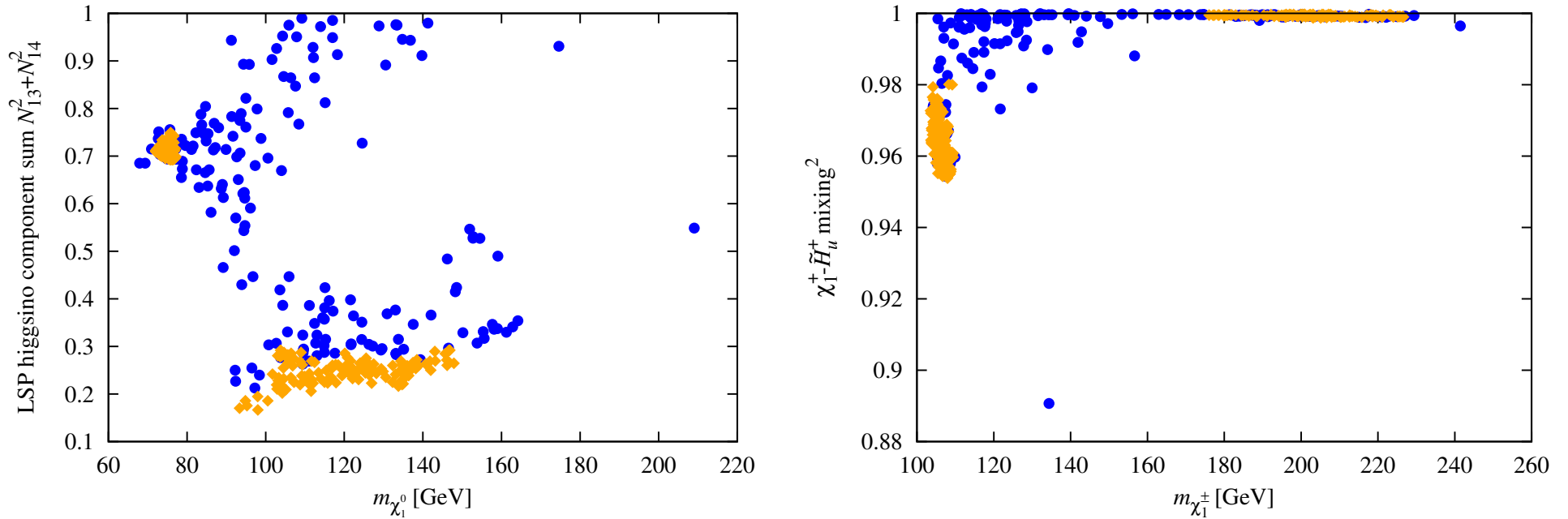
**Figure 20: Dark matter properties for the LEP-LHC scenarios.**

Dark matter (DM) properties for the surviving NMSSM parameter points are summarized in Fig. 20. Referring to the figure, we see a mixture of blue circle points (those with  $\Omega h^2 < 0.094$ ) and orange diamond points (those with  $0.094 \leq \Omega h^2 \leq 0.136$ , *i.e.* in the WMAP window).

The main mechanism at work to make  $\Omega h^2$  too small for many points is rapid  $\tilde{\chi}_1^0 \tilde{\chi}_1^0$  annihilation to  $W^+ W^-$  due to a substantial higgsino component of the  $\tilde{\chi}_1^0$  (see third plot of Fig. 20). Indeed, the relic density of a higgsino LSP is typically of order  $\Omega h^2 \approx 10^{-3} - 10^{-2}$ .

To avoid this, need  $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow W^+ W^-$  below threshold as for the light  $\tilde{\chi}_1^0$  point group (the strongly overlapping points with  $m_{\tilde{\chi}_1^0} < m_W$ )

As the higgsino component declines  $\Omega h^2$  increases it is the points for which the LSP is dominantly singlino that have large enough  $\Omega h^2$  to fall in the WMAP window. This kind of point appears in the large- $m_{\tilde{\chi}_1^0}$  point group.



**Figure 21:** Neutralino and chargino compositions for the LEP–LHC scenarios.

Also plotted in Fig. 20 is the spin-independent direct detection cross section,  $\sigma_{SI}$ , as a function of  $m_{\tilde{\chi}_1^0}$ . Experiments will reach sensitivities that will probe some of the predicted  $\sigma_{SI}$  values relatively soon, especially the  $m_{\tilde{\chi}_1^0} > 93$  GeV points that are in the WMAP window.

However, it is also noteworthy that the  $m_{\tilde{\chi}_1^0} \sim 75$  GeV WMAP-window points can have very small  $\sigma_{SI}$ .

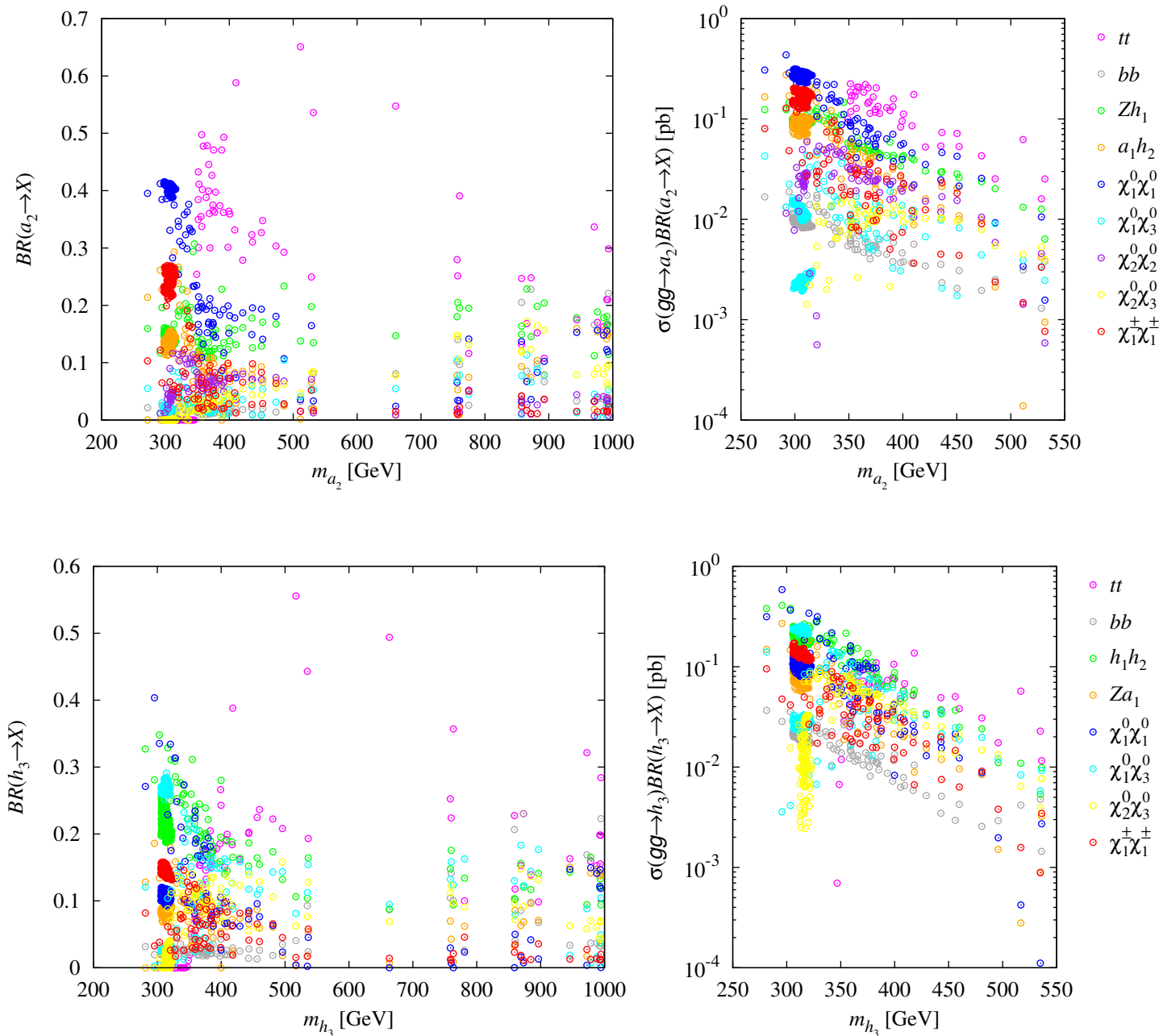
- **Direct Higgs production and decay at the LHC**

We have already noted in the discussion of Fig. 16 that  $gg$  and VBF production of the  $h_1$  with  $h_1 \rightarrow b\bar{b}$  provide event rates that might eventually be observable at the LHC once much higher integrated luminosity is attained. Other possibilities include production and decay of the  $a_1$ ,  $a_2$ , and  $h_3$ .

Since the  $a_1$  is dominantly singlet in nature, its production rates at the LHC are rather small.

Since the  $a_2$  and  $h_3$  are dominantly doublet they provide better discovery prospects.

Decay branching ratios and LHC cross sections in the  $gg$  fusion mode for  $a_2$  and  $h_3$  are shown in Fig. 22.



**Figure 22:** Decay branching ratios and LHC cross sections in the  $gg$  fusion mode (at  $\sqrt{s} = 8$  TeV) for  $a_2$  and  $h_3$

- If  $m_{a_2} > 2m_t$ , the  $t\bar{t}$  final state has  $\sigma(gg \rightarrow a_2)\text{BR}(a_2 \rightarrow t\bar{t}) > 0.01$  pb for  $m_{a_2} < 550$  GeV, implying  $> 200$  events for  $L = 20$  fb $^{-1}$ .

A study is needed to determine if this would be observable in the presence of the  $t\bar{t}$  continuum background.

No doubt, efficient  $b$  tagging and reconstruction of the  $t\bar{t}$  invariant mass in, say, the single lepton final state would be needed.

- For  $m_{a_2} < 2m_t$ , the  $X = a_1 h_2$  final state with both  $a_1$  and  $h_2$  decaying to  $b\bar{b}$  might be visible above backgrounds.

However, a dedicated study of this particular decay mode is still lacking.

Similar remarks apply in the case of the  $h_3$  where the possibly visible final states are  $t\bar{t}$  for  $m_{h_3} > 2m_t$  and  $h_1 h_2$  for  $m_{h_3} < 2m_t$ .

For both the  $a_2$  and  $h_3$ ,  $\sigma\text{BR}(X)$  is substantial for  $X = \tilde{\chi}_1^0 \tilde{\chi}_1^0$ , but to isolate this invisible final state would require an additional photon or jet tag which would reduce the cross section from the level shown.

Well, the story goes, with complicated decays of neutralinos and charginos to the various lighter Higgs bosons.

No time to go into it all here.

We do think this scenario is an intriguing one and hope experimentalists will educate themselves about some of its peculiarities.

It is possible, but far from guaranteed (in the low- $m_{\tilde{\chi}_1^0}$  region), that  $\sigma_{SI}$  is large enough to be detectable soon.

## The pure 2HDM

- “*Two-Higgs-Doublet Models and Enhanced Rates for a 125 GeV Higgs*” A. Drozd, B. Grzadkowski, J. F. Gunion and Y. Jiang. arXiv:1211.3580 [hep-ph]
- see also, “*Mass-degenerate Higgs bosons at 125 GeV in the Two-Higgs-Doublet Model*” P. M. Ferreira, H. E. Haber, R. Santos and J. P. Silva. arXiv:1211.3131 [hep-ph]
- There are some differences.
- We employ the 2HDMC code.<sup>3</sup> It implements:
  1. Precision electroweak constraints (denoted STU)
  2. Limits coming from requiring vacuum stability, unitarity and coupling-constant perturbativity (denoted jointly as SUP).

The SUP constraints are particularly crucial in limiting the level of enhancement of the  $gg \rightarrow h \rightarrow \gamma\gamma$  channel, our main focus.
- For all our scans, we have supplemented the 2HDMC code by including the B/LEP constraints.

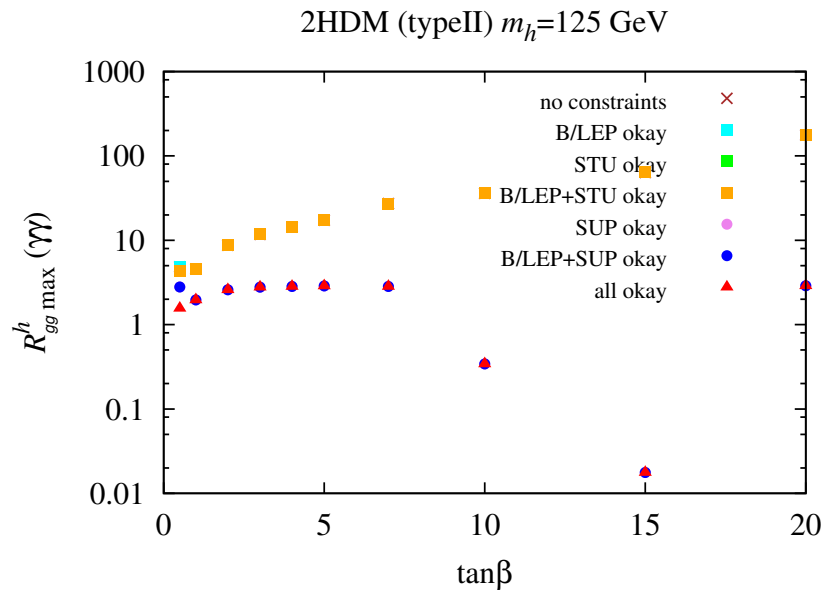
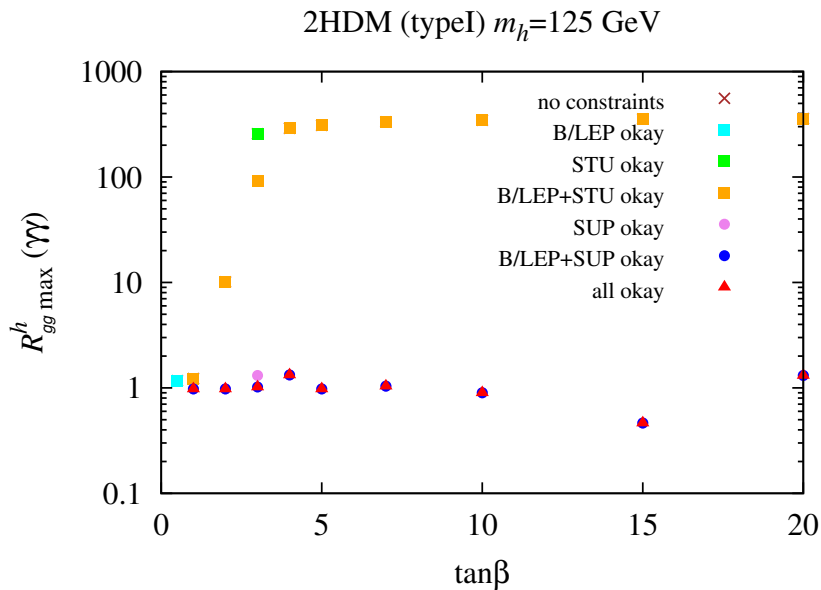
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<sup>3</sup>We have modified the subroutine in 2HDMC that calculates the Higgs boson decays to  $\gamma\gamma$  and also the part of the code relevant for QCD corrections to the  $q\bar{q}$  final state.



1. For the LEP data we adopt upper limits on  $\sigma(e^+e^- \rightarrow Zh/H)$  and  $\sigma(e^+e^- \rightarrow Ah/H)$  from Abbiendi:2002qp and Abbiendi:2004gn, respectively.
2. Regarding  $B$  physics, the constraints imposed are those from  $\text{BR}(B_s \rightarrow X_s \gamma)$ ,  $R_b$ ,  $\Delta M_{B_s}$ ,  $\epsilon_K$ ,  $\text{BR}(B^+ \rightarrow \tau^+ \nu_\tau)$  and  $\text{BR}(B^+ \rightarrow D \tau^+ \nu_\tau)$ .  
The most important implications of these results are to place a lower bound on  $m_{H^\pm}$  as a function of  $\tan \beta$  as shown in Fig. 15 of Branco:2011iw in the case of the Type II model and to place a lower bound on  $\tan \beta$  as a function of  $m_{H^\pm}$  as shown in Fig. 18 of Branco:2011iw.

- We scan and find results illustrated by the following plot.



The top two plots show the maximum  $R_{gg}^h(\gamma\gamma)$  values in the Type I (left) and Type II (right) models for  $m_h = 125$  GeV as a function of  $\tan\beta$  after imposing various constraints — see figure legend.

Disappearance of a point after imposing a given constraint set means that the point did not satisfy that set of constraints.

For boxes and circles, if a given point satisfies subsequent constraints then the resulting color is chosen according to the color ordering shown in the legend.

- Corresponding  $R_{gg}^h(ZZ)$  and  $R_{gg}^h(bb)$  are shown in Fig. 23.

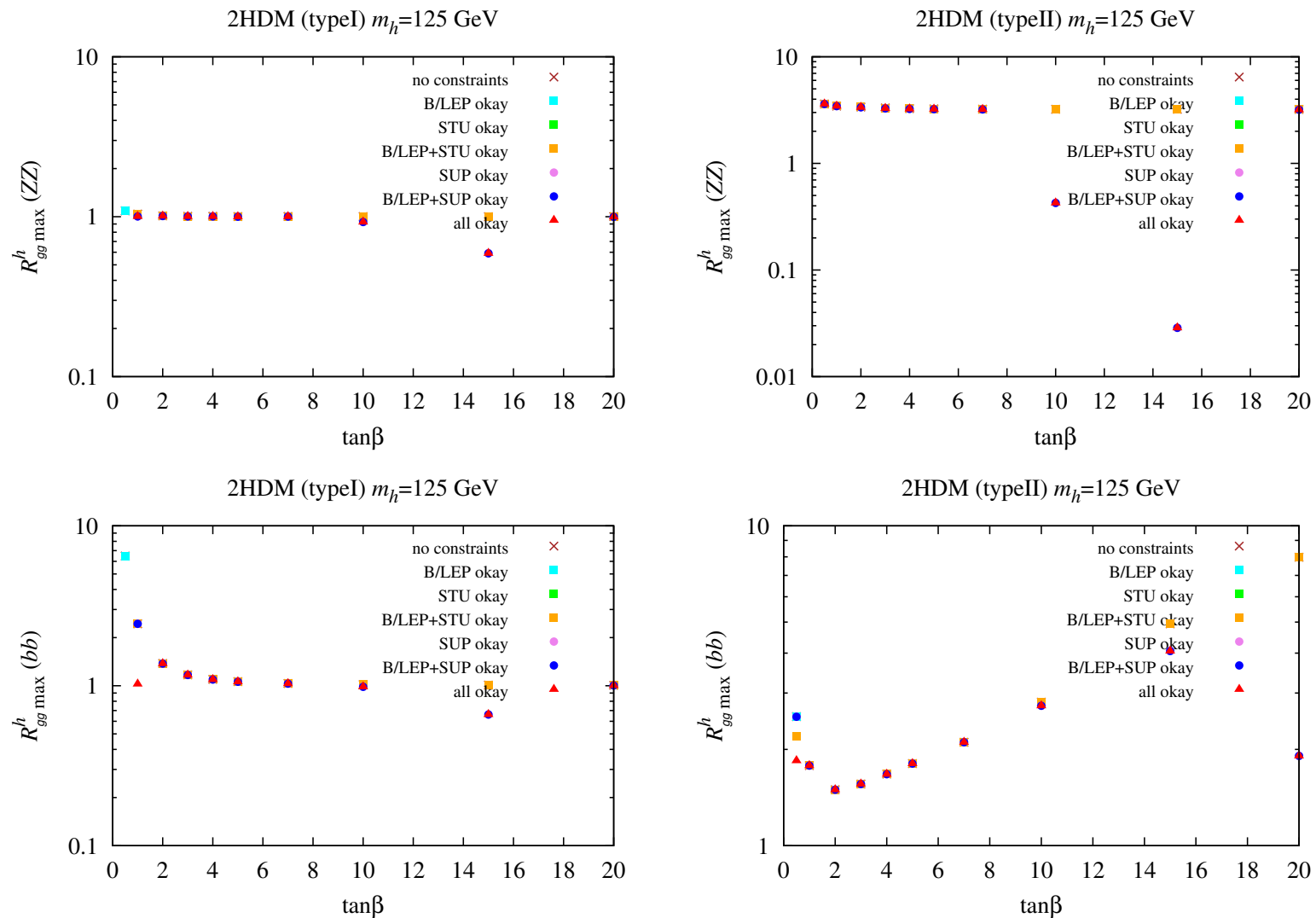


Figure 23:  $ZZ$  and  $b\bar{b}$  final states for parameters with maximum  $R_{gg}^h(\gamma\gamma)$ .

## Summary of results:

- Type II model:

1. For only  $h$  at 125 GeV, the parameters that give  $R_{gg}^h(\gamma\gamma) > 1.3$  are characterized by  $R_{gg}^h(ZZ) > R_{gg}^h(\gamma\gamma)$ , a result that is inconsistent with experimental results in the  $gg \rightarrow h \rightarrow ZZ \rightarrow 4\ell$  channel.

Thus, if  $R_{gg}^h(\gamma\gamma) > 1.3$  and  $R_{gg}^h(ZZ) < 1.3$  both persist experimentally, the Type II model cannot describe the data if only the  $h$  resides at 125 GeV.

2. Similar statements apply to the case of the heavier  $H$  having a mass of 125 GeV.

3. For approximately degenerate  $h$  and  $A$  Higgs bosons at 125 GeV there exist theoretically consistent parameter choices for Type II models for which  $R_{gg}^{h+A}(\gamma\gamma) > 1.3$  while  $R_{gg}^{h+A}(ZZ) < 1.3$ , but in these cases  $R_{gg}^{h+A}(b\bar{b}) > 3.75$ , a value far above that observed.

Thus, the Type II 2HDMs cannot yield  $R_{gg}^{h+A}(\gamma\gamma) > 1.3$  without conflicting with other observables.

In short, the Type II model is unable to give a significantly enhanced  $gg \rightarrow h \rightarrow \gamma\gamma$  signal while maintaining consistency with other channels.

- Type I model:

1. The maximal  $R_{gg}^h(\gamma\gamma)$  is of order of 1.3, as found if  $\tan\beta = 4$  or 20.
2. In these cases,  $R_{gg}^h(ZZ)$  and  $R_{gg}^h(b\bar{b})$  are of order 1 as fairly consistent with current data.
3. For these scenarios, the charged Higgs is light,  $m_{H^\pm} = 90$  GeV.
4. Despite this small mass, there is no conflict with LHC data due to the fact that  $BR(t \rightarrow H^+b) \sim 1/\tan^2\beta$  is small enough to be below current limits.

Thus, Type I models could provide a consistent picture if the LHC results converge to only a modest enhancement for  $R_{gg}^h(\gamma\gamma) \lesssim 1.3$ .

But, if  $R_{gg}^h(\gamma\gamma)$  is definitively measured to have a value much above 1.3 while the  $ZZ$  and  $b\bar{b}$  channels show little enhancement then there is no consistent 2HDM description.

- Perhaps the pure 2HDM is too limiting and one must go beyond the 2HDM to include new physics such as supersymmetry.

# Higgs fitting

*Collaboration: G. Belanger, B. Dumont, S. Kraml, U. Elwanger, J. Gunion*

- The structure we will test is

$$\mathcal{L} = g \left[ C_V \left( m_W W_\mu W^\mu + \frac{m_Z}{\cos \theta_W} Z_\mu Z^\mu \right) - C_U \frac{m_t}{2m_W} \bar{t}t - C_D \frac{m_b}{2m_W} \bar{b}b - C_D \frac{m_\tau}{2m_W} \bar{\tau}\tau \right] H. \quad (10)$$

In general, the  $C_I$  can take on negative as well as positive values; there is one overall sign ambiguity which we fix by taking  $C_V > 0$ .

- We will be fitting the data given earlier.
- In addition to the tree-level couplings given above, the  $H$  has couplings to  $gg$  and  $\gamma\gamma$  that are first induced at one loop and are completely

computable in terms of  $C_U$ ,  $C_D$  and  $C_V$  if only loops containing SM particles are present.

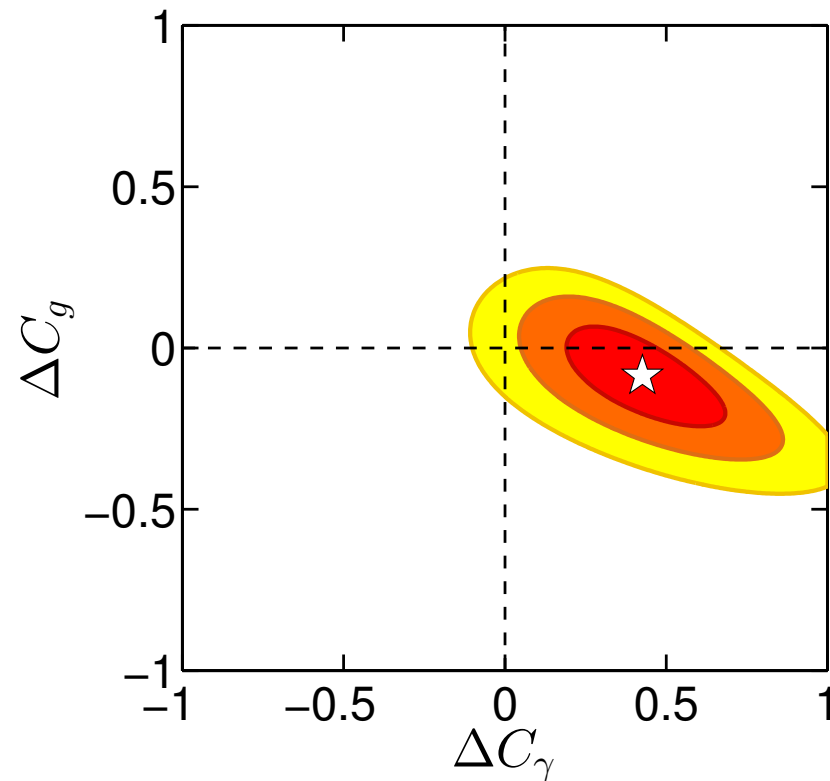
We define  $\bar{C}_g$  and  $\bar{C}_\gamma$  to be the ratio of these couplings so computed to the SM (*i.e.*  $C_U = C_D = C_V = 1$ ) values.

- However, in some of our fits we will also allow for additional loop contributions  $\Delta C_g$  and  $\Delta C_\gamma$  from new particles; in this case  $C_g = \bar{C}_g + \Delta C_g$  and  $C_\gamma = \bar{C}_\gamma + \Delta C_\gamma$ .
- The largest set of independent parameters in our fits is thus

$$C_U, C_D, C_V, \Delta C_g, \Delta C_\gamma. \quad (11)$$

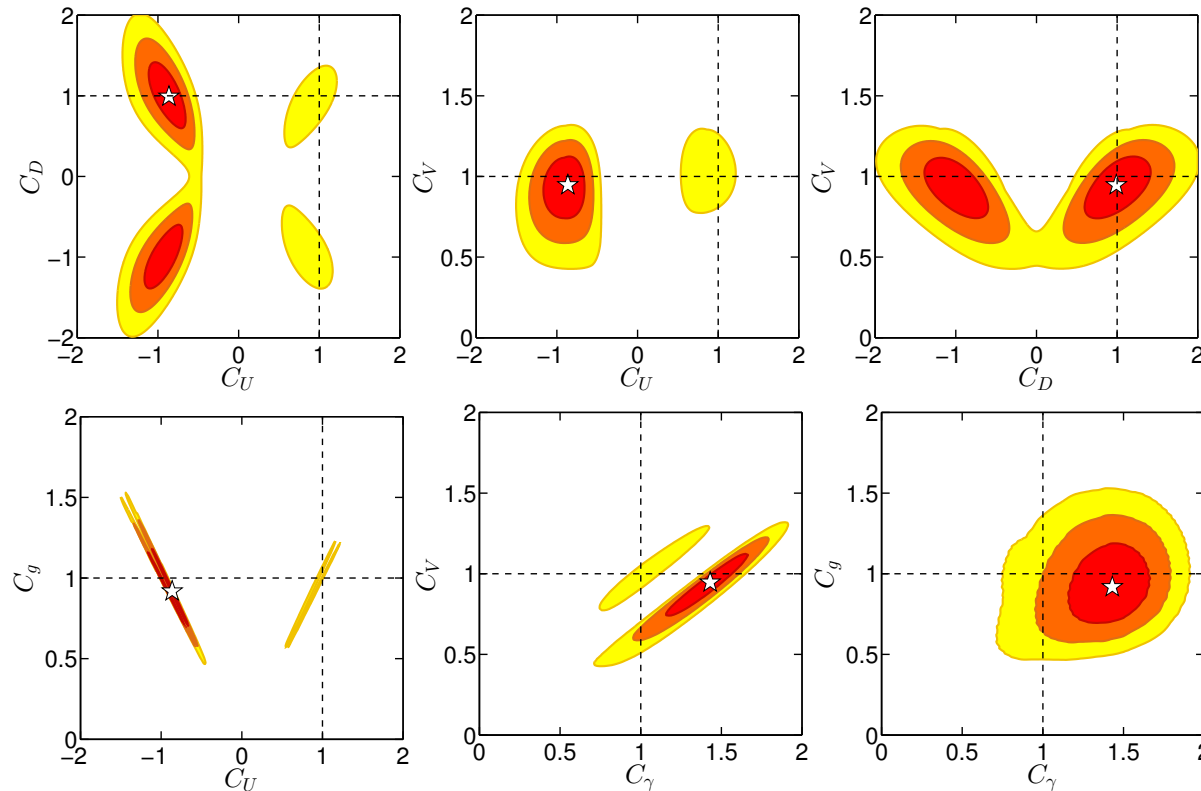


- **Fit I:  $C_U = C_D = C_V = 1$ ,  $\Delta C_g$  and  $\Delta C_\gamma$  free.**



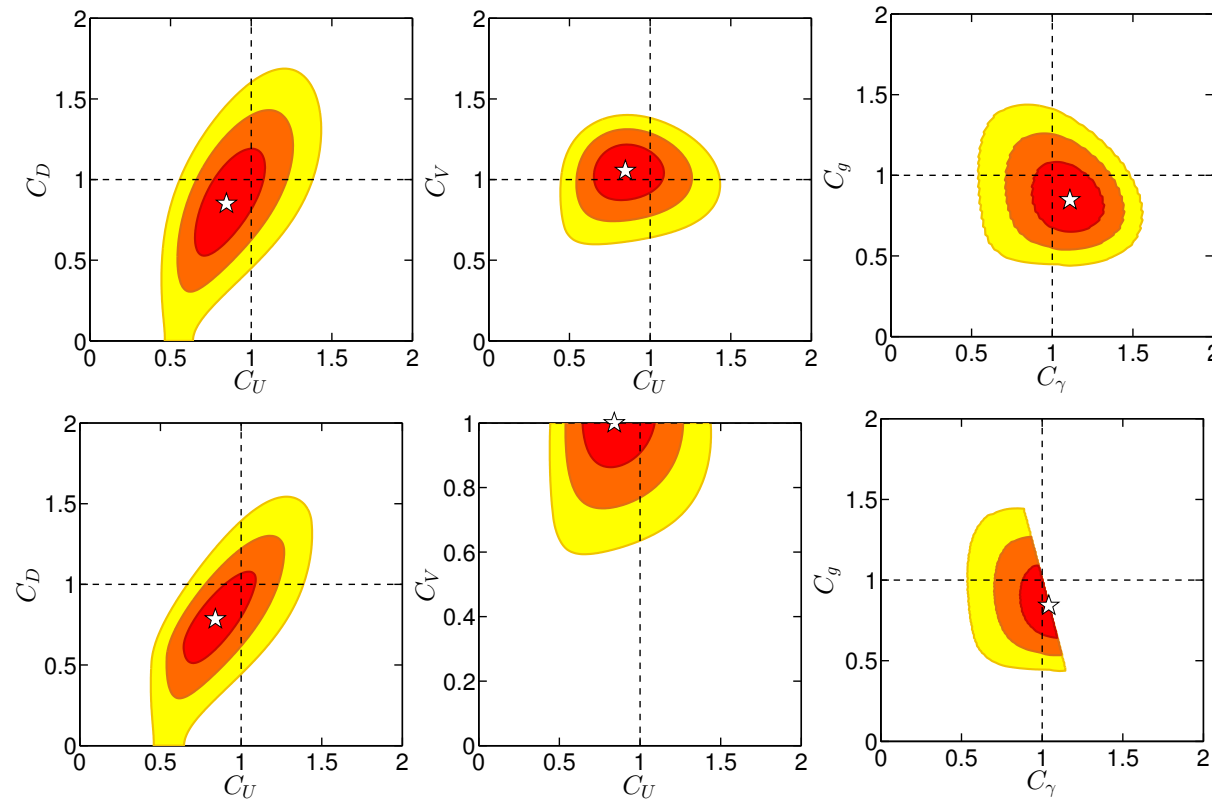
**Figure 24:** Two parameter fit of  $\Delta C_\gamma$  and  $\Delta C_g$ , assuming  $C_U = C_D = C_V = 1$  (Fit I). The red, orange and yellow ellipses show the 68%, 95% and 99.7% CL regions, respectively. The white star marks the best-fit point  $\Delta C_\gamma = 0.426$ ,  $\Delta C_g = -0.086$ . It has  $\chi^2 = 12.3$  vs. SM  $\chi^2 = 20.2$ . i.e. SM is  $\sim 2\sigma$  worse.

- **Fit II: varying  $C_U$ ,  $C_D$  and  $C_V$  ( $\Delta C_\gamma = \Delta C_g = 0$ )**



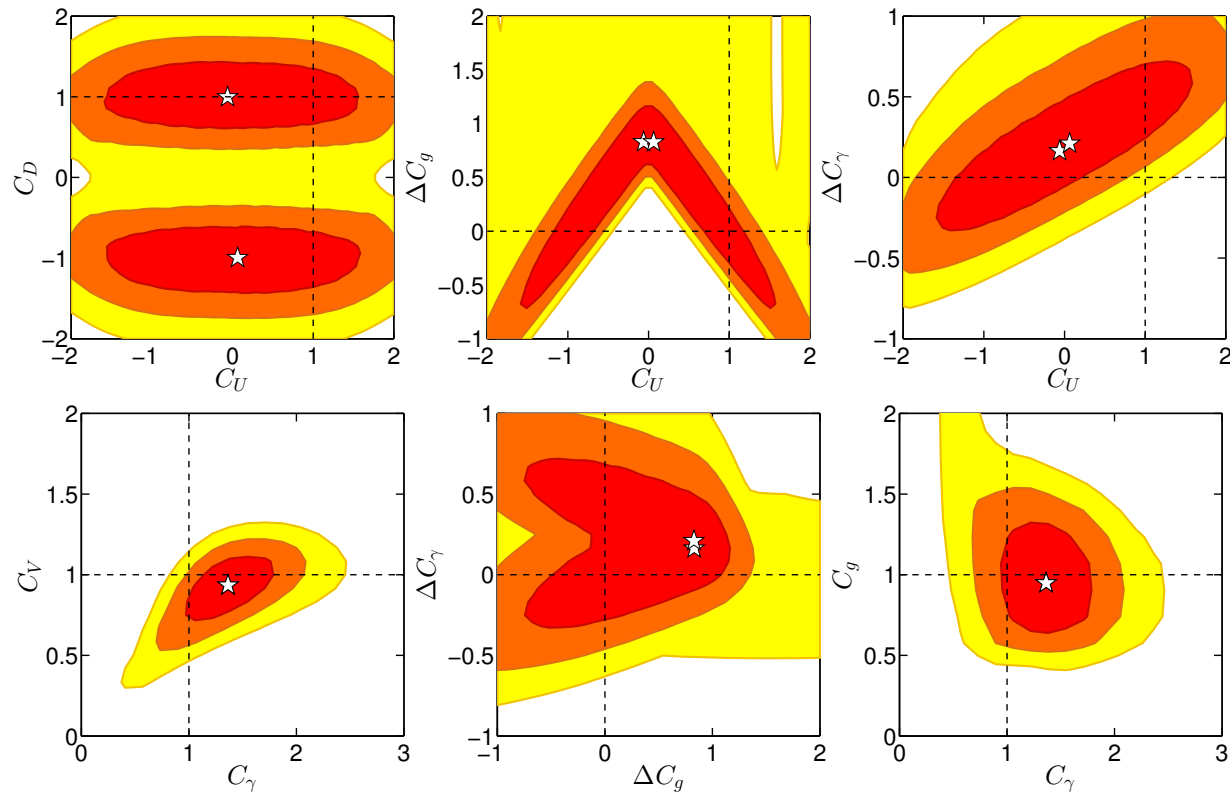
**Figure 25:** Two-dimensional  $\chi^2$  distributions for the three parameter fit, Fit II, of  $C_U$ ,  $C_D$ ,  $C_V$  with  $C_\gamma = \bar{C}_\gamma$  and  $C_g = \bar{C}_g$  as computed in terms of  $C_U, C_D, C_V$ . Details on the minima in different sectors of the  $(C_U, C_D)$  plane can be found in Table 5. Note strong preference for negative  $C_U = -1$  ( $\gamma\gamma$   $t$ -loop adds to  $W$  loop). Negative  $C_U$  is hard in most models. But,  $\chi^2 = 11.6$  is much better than for SM.

- **Fit II: varying  $C_U$ ,  $C_D$  and  $C_V$  ( $\Delta C_\gamma = \Delta C_g = 0$ ) requiring  $C_U, C_D > 0$  (and  $C_V > 0$  by convention)**



**Figure 26:** Two-dimensional  $\chi^2$  distributions for the three parameter fit, Fit II, as in Fig. 25 but with  $C_U > 0$ ,  $C_D > 0$ ,  $C_V > 0$ . The upper row of plots allows for  $C_V > 1$ , while in the lower row of plots  $C_V \leq 1$  is imposed.  $\chi^2 = 18.66$  is not much lower than SM in this case.

- Fit III: varying  $C_U$ ,  $C_D$ ,  $C_V$ ,  $\Delta C_\gamma$  and  $\Delta C_g$



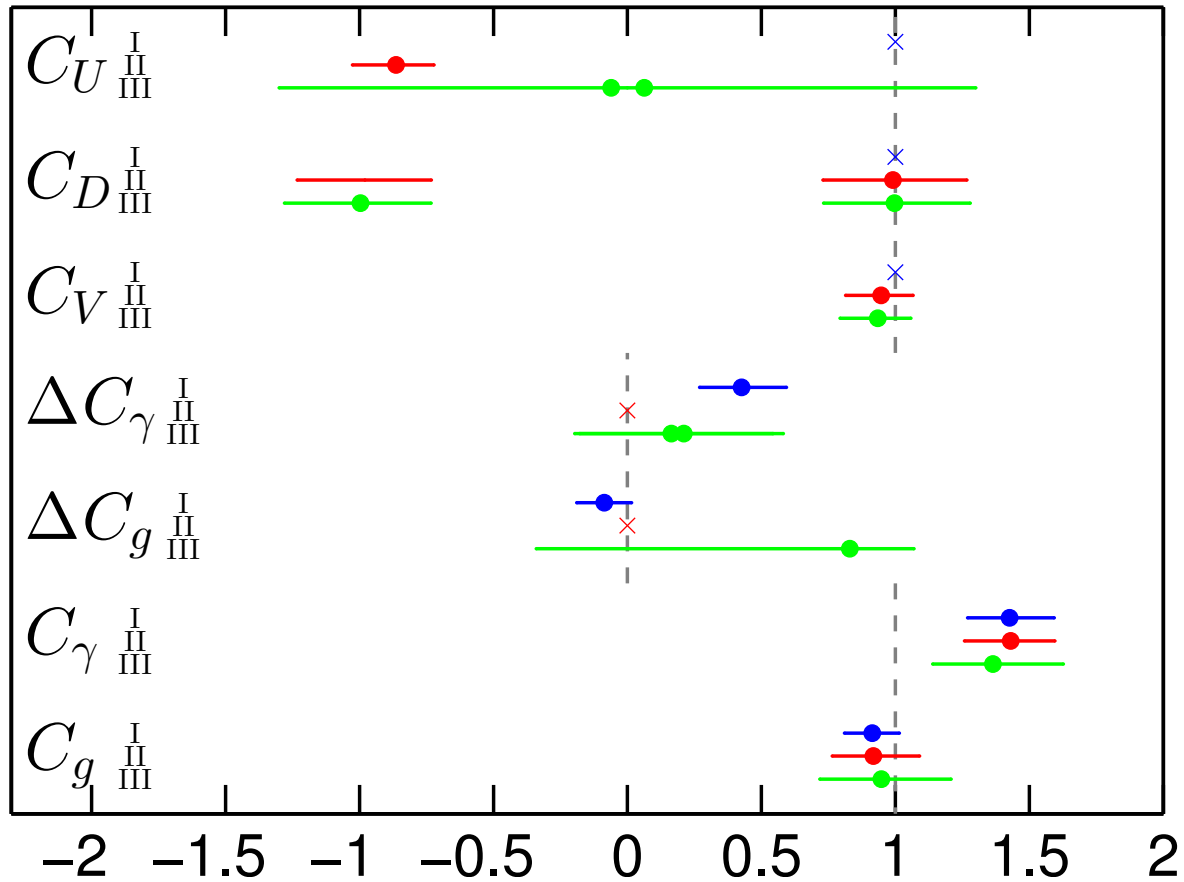
**Figure 27:** Two-dimensional distributions for the five parameter fit of  $C_U$ ,  $C_D$ ,  $C_V$ ,  $\Delta C_\gamma$  and  $\Delta C_g$  (Fit III). Details regarding the best fit point are given in Table 4. Note how  $\Delta C_g$  can be traded for  $C_U$ .

Fit	I	II	III, 1st min.	III, 2nd min.
$C_U$	1	$-0.864^{+0.142}_{-0.163}$	$-0.06 \pm 1.3$	$0.06 \pm 1.3$
$C_D$	1	$0.991^{+0.277}_{-0.261}$	$0.996^{+0.284}_{-0.264}$	$-0.996^{+0.263}_{-0.284}$
$C_V$	1	$0.947^{+0.119}_{-0.132}$	$0.934^{+0.124}_{-0.140}$	$0.934^{+0.124}_{-0.140}$
$\Delta C_\gamma$	$0.426^{+0.167}_{-0.157}$	–	$0.164^{+0.380}_{-0.360}$	$0.210^{+0.372}_{-0.389}$
$\Delta C_g$	$-0.086^{+0.102}_{-0.103}$	–	$0.830^{+0.24}_{-1.17}$	$0.828^{+0.24}_{-1.17}$
$C_\gamma$	$1.426^{+0.167}_{-0.157}$	$1.431^{+0.165}_{-0.173}$	$1.364^{+0.263}_{-0.225}$	$1.364^{+0.263}_{-0.225}$
$C_g$	$0.914^{+0.102}_{-0.103}$	$0.918^{+0.173}_{-0.153}$	$0.948^{+0.26}_{-0.23}$	$0.948^{+0.26}_{-0.23}$
$\chi^2_{\min}$	12.31	11.95	11.46	11.46
$\chi^2_{\min}/\text{d.o.f.}$	0.648	0.664	0.716	0.716

**Table 4:** Summary of results for Fits I–III. For Fit II, the tabulated results are from the best fit, cf. column 1 of Table 5.

Sector	$C_U < 0, C_D > 0$	$C_U, C_D < 0$	$C_U, C_D > 0$
$C_U$	$-0.864^{+0.142}_{-0.163}$	$-0.911^{+0.150}_{-0.171}$	$0.847^{+0.152}_{-0.133}$
$C_D$	$0.991^{+0.277}_{-0.261}$	$-0.980^{+0.258}_{-0.273}$	$0.851^{+0.221}_{-0.213}$
$C_V$	$0.947^{+0.120}_{-0.132}$	$0.943^{+0.119}_{-0.133}$	$1.055^{+0.109}_{-0.118}$
$C_\gamma$	$1.431^{+0.165}_{-0.173}$	$1.425^{+0.163}_{-0.173}$	$1.110^{+0.145}_{-0.159}$
$C_g$	$0.918^{+0.173}_{-0.153}$	$0.909^{+0.168}_{-0.150}$	$0.847^{+0.159}_{-0.128}$
$\chi^2_{\min}$	<b>11.95</b>	<b>12.06</b>	<b>18.66</b>
$\chi^2_{\min}/\text{d.o.f.}$	<b>0.66</b>	<b>0.67</b>	<b>1.04</b>

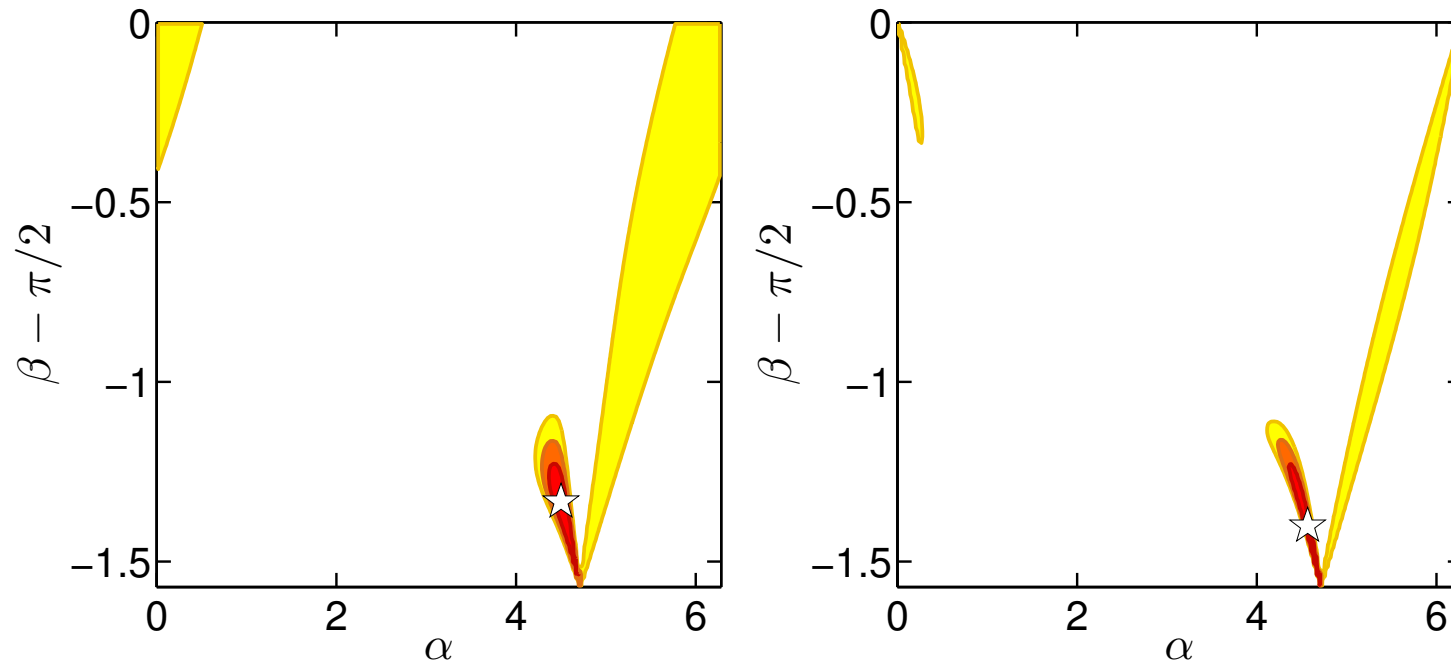
**Table 5:** Results for Fit II in different sectors of the  $(C_U, C_D)$  plane.



**Figure 28:** Graphical representation of the best fit values for  $C_U$ ,  $C_D$ ,  $C_V$ ,  $\Delta C_\gamma$  and  $\Delta C_g$  of Table 4. The labels refer to the fits discussed in the text. The dashed lines indicate the SM value for the given quantity. The  $\times$ 's indicate cases where the parameter in question was fixed to its SM value.

## Impact on Two-Higgs-Doublet Models

- Only  $\alpha$  and  $\beta$  needed to describe a single Higgs. So good fit is not exactly guaranteed.



**Figure 29:** 2HDM fits for the  $h$  in the Type I (left) and Type II (right) models. Note:  $\beta - \pi/2 = \alpha - 2\pi$  is SM limit. Fit is far from SM limit and requires small  $\tan \beta$ , the latter being problematical for perturbativity of top-quark coupling. If we require  $\tan \beta > 1$ , must move to ‘wedge’ which is near SM-like limit and has much higher  $\chi^2$ .



Fit	THDM-I	THDM-II	THDM-I, $\tan \beta > 1$	THDM-II, $\tan \beta > 1$
$\alpha$ [rad]	$4.5^{+0.093}_{-0.081}$	$4.56^{+0.148}_{-0.136}$	$5.374^{+1.113}_{-0.131}$	$6.275^{+0.165}_{-0.825}$
$\beta$ [rad]	$0.237^{+0.069}_{-0.097}$	$0.17^{+0.124}_{-0.170}$	$[\pi/4, \pi/2]$	$1.562^{+0.009}_{-0.776}$
$\cos \alpha$	$-0.211^{+0.092}_{-0.078}$	$-0.147^{+0.147}_{-0.133}$	$0.614^{+0.386}_{-0.108}$	$1.0_{-0.673}$
$\tan \beta$	$0.241^{+0.075}_{-0.101}$	$0.172^{+0.131}_{-0.172}$	$[1, +\infty]$	$[1, +\infty]$
$C_U$	$-0.899^{+0.166}_{-0.192}$	$-0.869^{+0.116}_{-0.134}$	$0.869^{+0.168}_{-0.154}$	$1.02^{+0.05}_{-0.07}$
$C_D$	$-0.899^{+0.166}_{-0.192}$	$1.004_{-0.01}$	$0.869^{+0.168}_{-0.154}$	$0.94^{+0.13}_{-0.11}$
$C_V$	$0.901^{+0.069}_{-0.073}$	$0.950^{+0.048}_{-0.115}$	$0.992^{+0.008}_{-0.040}$	$1.0_{-0.047}$
$C_\gamma$	$1.369^{+0.094}_{-0.097}$	$1.436^{+0.081}_{-0.130}$	$1.025_{-0.062}$	$1.005^{+0.009}_{-0.088}$
$C_g$	$0.899^{+0.188}_{-0.162}$	$0.924^{+0.132}_{-0.113}$	$0.869^{+0.164}_{-0.149}$	$0.99^{+0.08}_{-0.04}$
$\chi^2_{\min}$	12.20	11.95	19.43	19.88

Table 6: Summary of fit results for the  $h$  in 2HDMs of Type I and Type II.

## Summary of Fitting Results

Best  $\chi^2$ 's are achieved pretty far from SM limit and would have to involve exotic parameters. Only cure: light charged Higgs, but then other constraints become a problem.

## Conclusions

- It seems likely that the Higgs responsible for EWSB has emerged.
- Perhaps, other Higgs-like objects are emerging.
- Survival of enhanced signals for one or more Higgs boson would be one of the most exciting outcomes of the current LHC run and would guarantee years of theoretical and experimental exploration of BSM models with elementary scalars.
- $>$ SM signals would appear to guarantee the importance of a linear collider or LEP3 or muon collider in order to understand fully the responsible BSM physics.
- In any case, the current situation illustrates the fact that we must never assume we have uncovered all the Higgs.

**Certainly, I will continue watching and waiting**

