

“Condensation of pairs of fermionic lithium atoms”

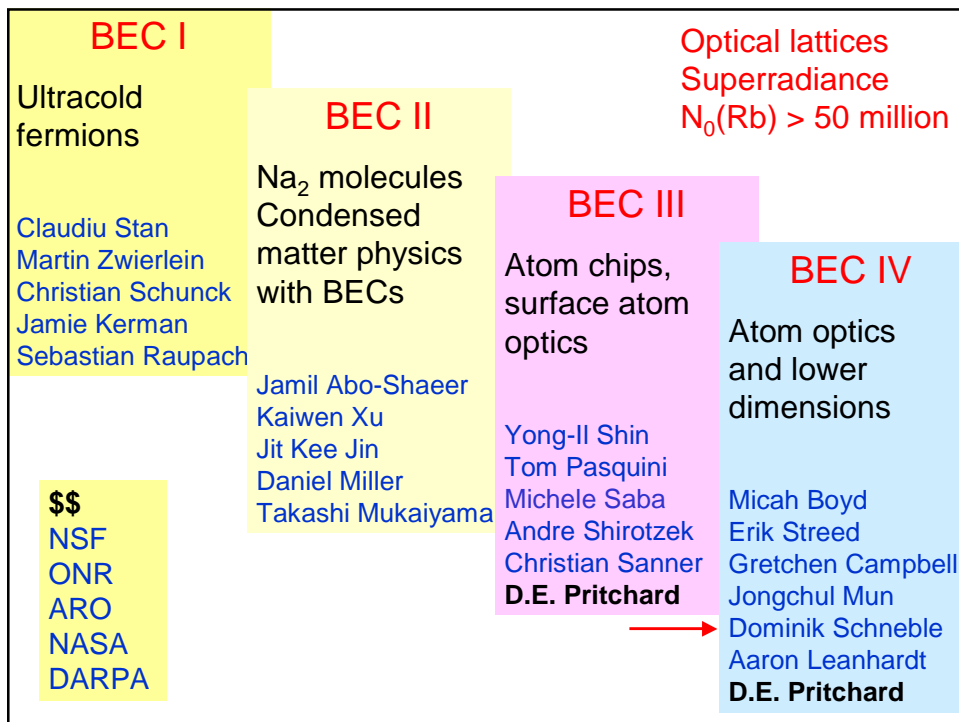
Wolfgang Ketterle

Massachusetts Institute of Technology
MIT-Harvard Center for Ultracold Atoms



5/10/04

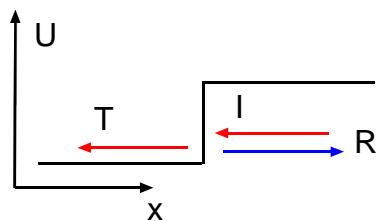
KITP workshop, Santa Barbara



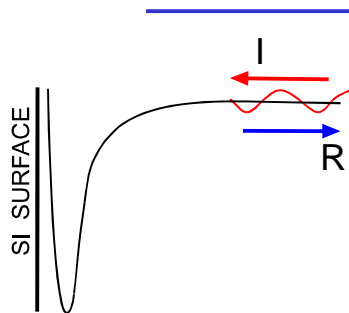
Quantum Reflection of Ultracold Atoms

T.A. Pasquini, Y. Shin, C. Sanner, M. Saba, A. Schirotzek,
D.E. Pritchard, W.K.

Quantum Reflection



- Quantum mechanical turning point without classical analogue.
- Reflection coefficient determined by matching condition.



- Long range, attractive Casimir-Polder potential.

$$U = -C_4 / r^4$$

- Reflection occurs far from surface at effective "step".

$$R \approx \sqrt{1 - 2\beta_4 k}$$

$$C_4 = \beta_4^2 \hbar^2 / 2m$$

Mody et. al., PRB 2001; Friedrich et. al. PRA 2002

Reflection of cold atoms from surfaces

Extremely weak interactions

Normal incidence: Hydrogen on helium 1 K
(Walraven 1986; Greytak/Kleppner 1991)

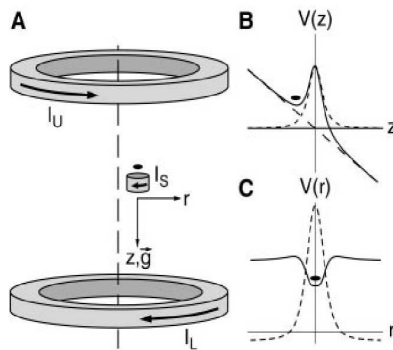
Grazing incidence: Helium on helium (Masuhara 1983)

All other atoms

Normal incidence 10 nK

Grazing incidence Cesium (Hinds 1986), Ne* (Shimizu 2001)

Gravito-magnetic Trap

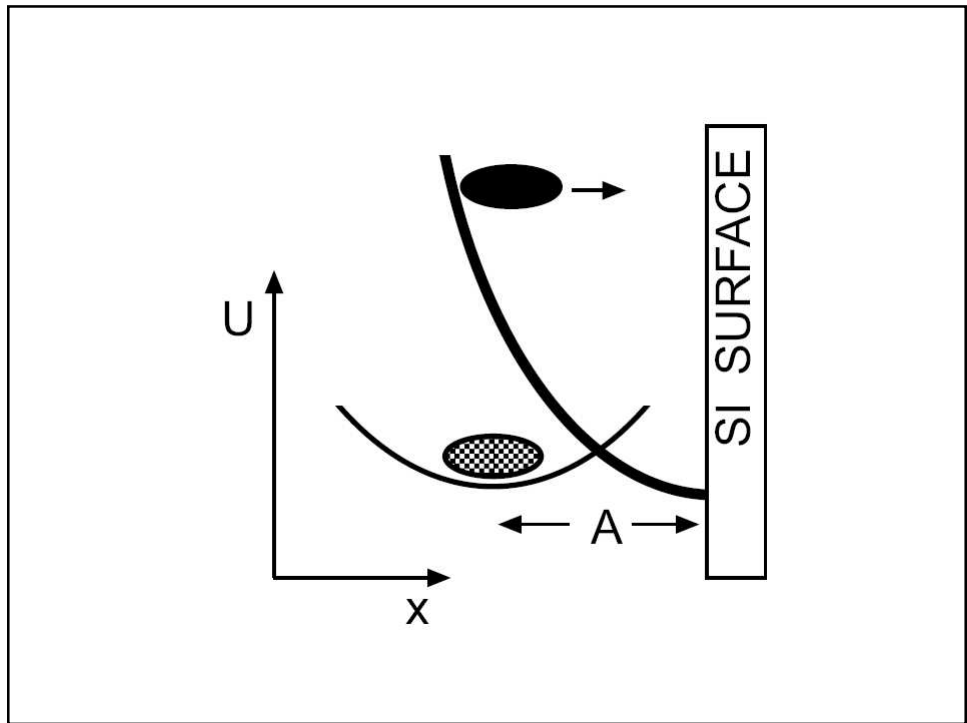
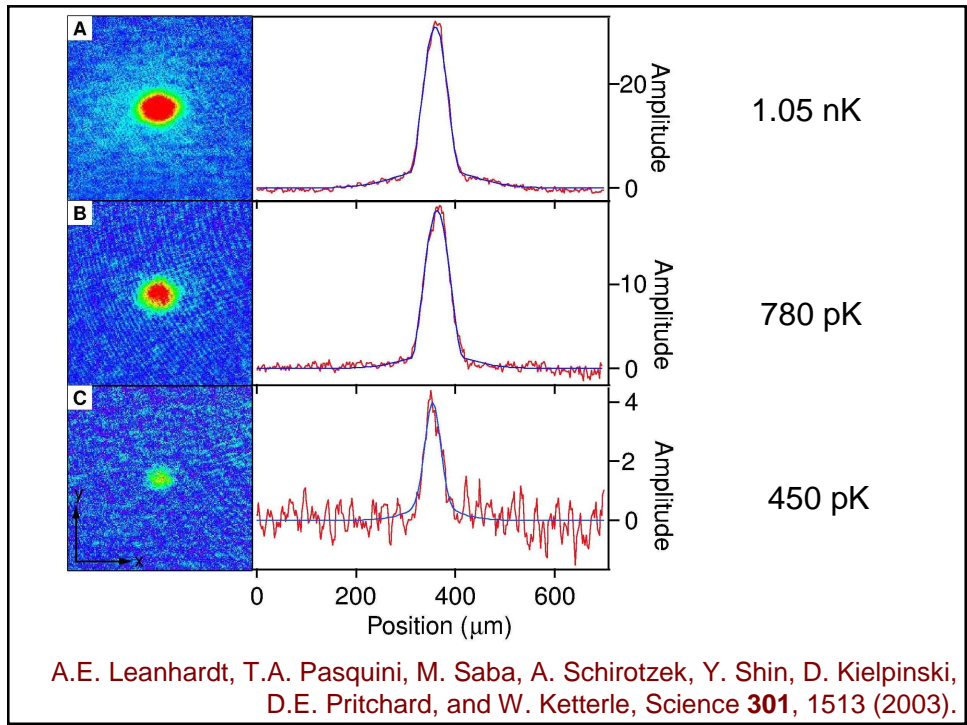


- Ultra-dilute condensates
- Easily adjustable trap position
- Long, slow dipole oscillation
- Very long lifetime

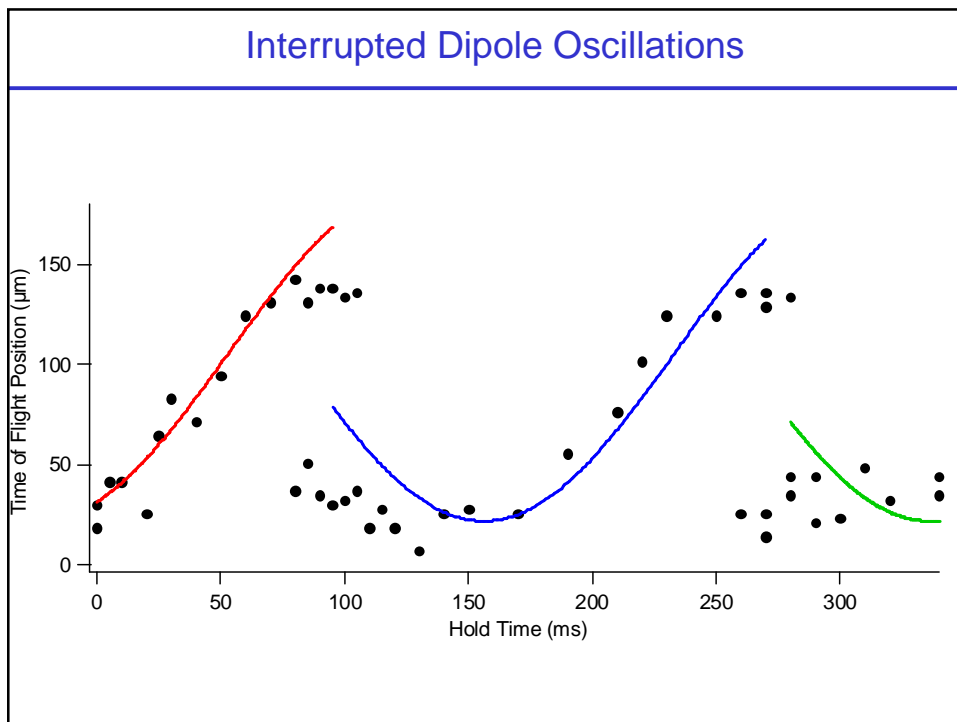
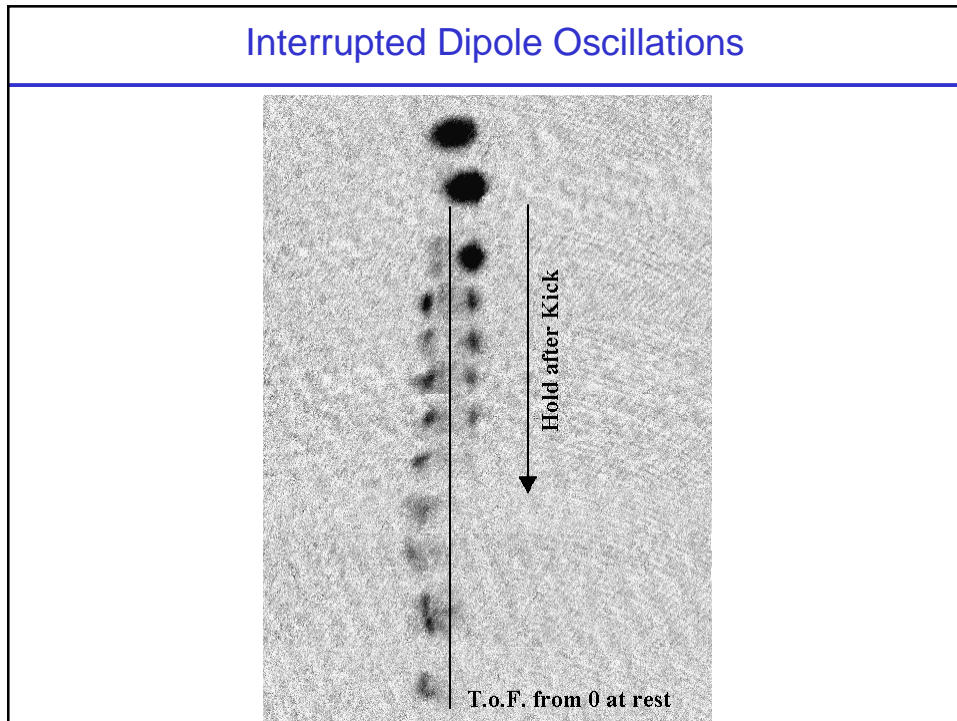
Trap Parameters:

$N = 10^4 - 10^5$ $n = 10^{11} \text{ cm}^{-3}$ $\diamond_{\text{HO}} = 1 - 10 \text{ Hz}$ $\diamond_{\text{LIFE}} \sim 1 \text{ min}$
 $T_C = 1 \text{ nK}$ $v_{\text{TH}} = 1 \text{ mm/s}$ $v_S = 1 \text{ mm/s}$

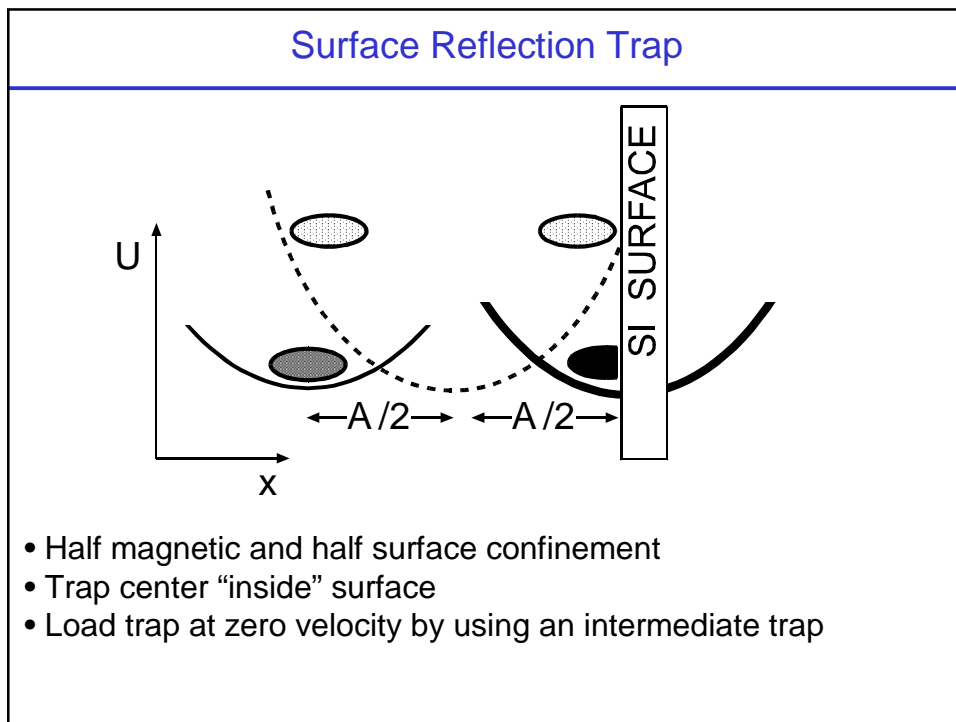
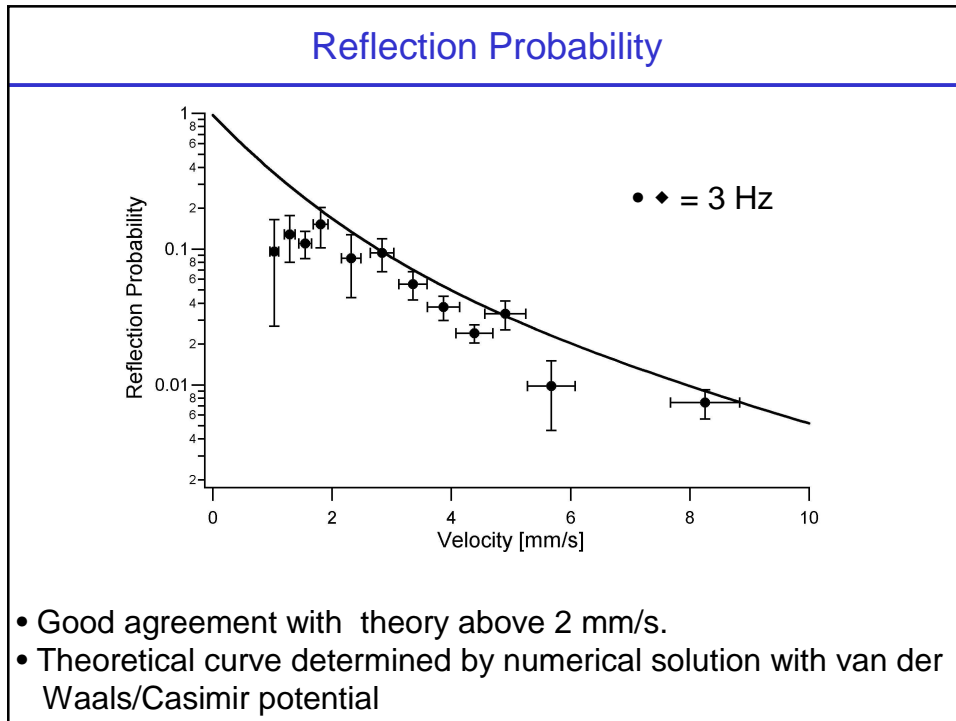
Condensation of pairs of fermionic lithium atoms



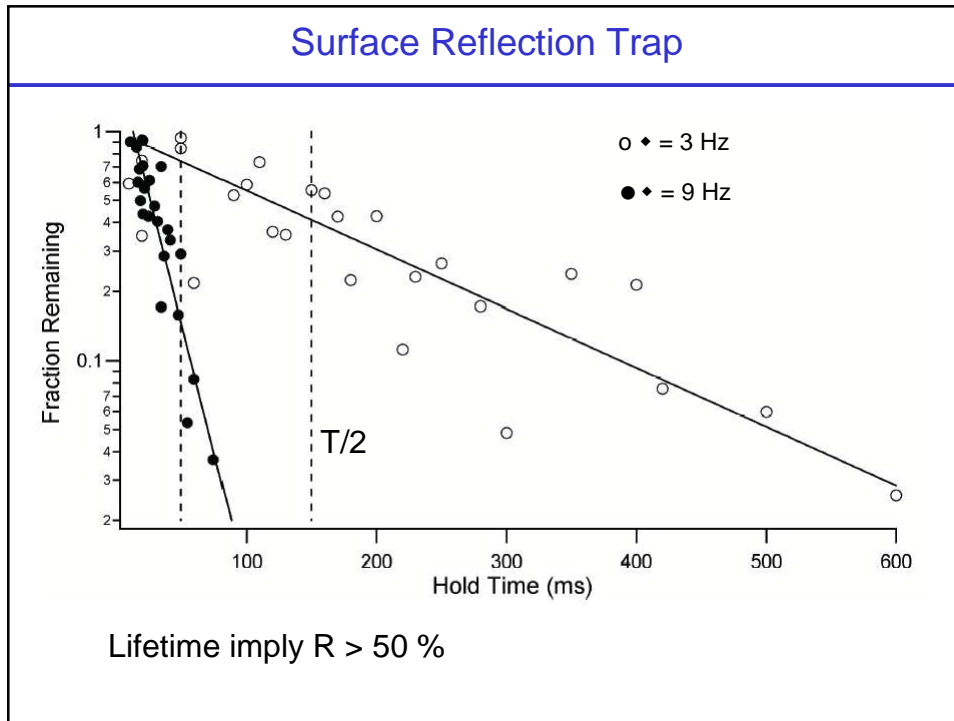
Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



- ### Outlook
- Enhance reflection coefficient
 - ▶ Membrane surfaces or spongy materials
 - New atomic mirrors and atom optics
 - Confinement in surface trap
 - ▶ Condensates in a “cup”
 - Study density dependent effects
 - ▶ Collective behavior

Pairs of
bosonic atoms

**Quantum degenerate
Na₂ molecules**

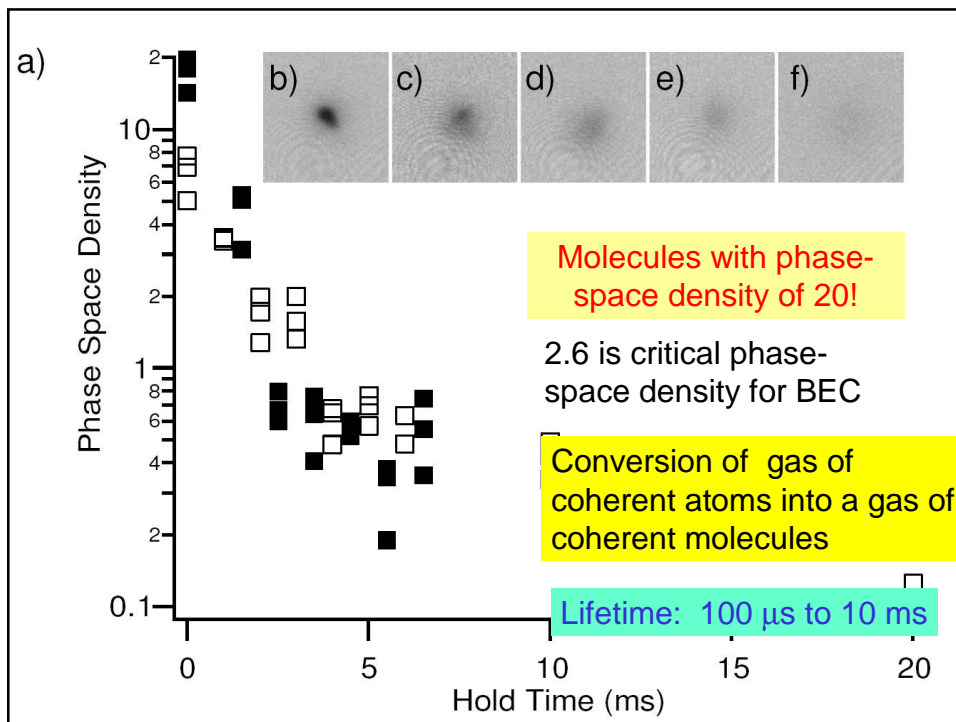
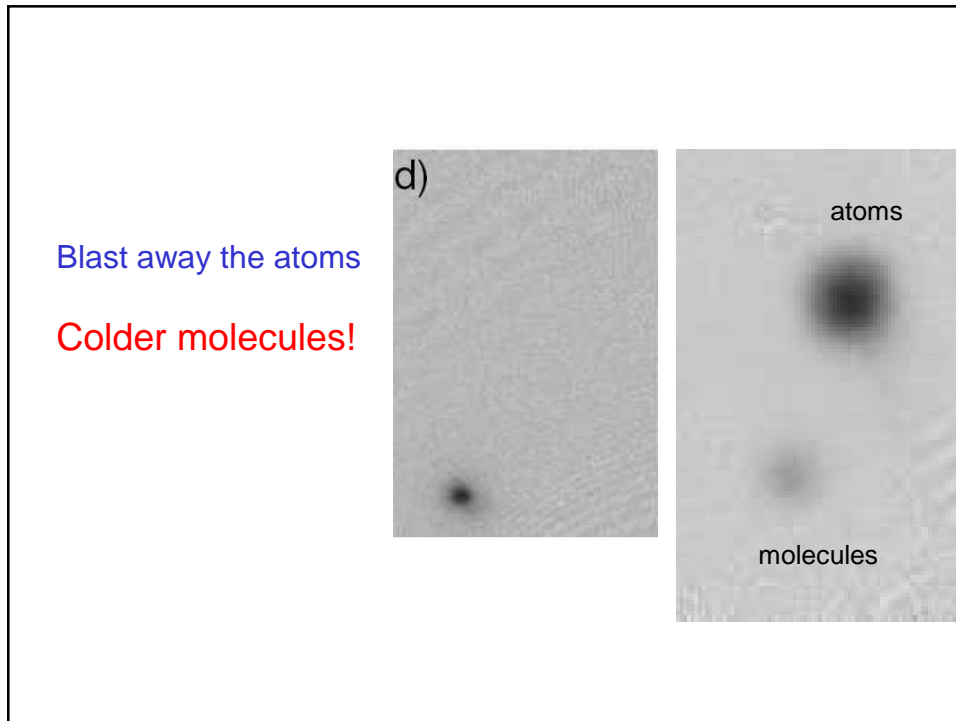
Takashi Mukaiyama, Kaiwen Xu, Jamil Abo-Shaeer, Jit Kee Chin,
Daniel Miller, W.K.
Phys. Rev. Lett. **91**, 210402 (2003)
Phys. Rev. Lett., in print; cond-mat/0311558.

The new cold frontier: molecules

The diagram shows energy levels (E) versus magnetic field. A vertical dashed line marks the Feshbach resonance. To the left of the resonance, two blue spheres represent a molecule. To the right, two blue spheres represent two atoms. A red arrow indicates the transition from the molecular state to the atomic state at the resonance. To the right of the diagram are two experimental images: the top one shows a dark spot labeled 'atoms', and the bottom one shows a dark spot labeled 'molecules'.

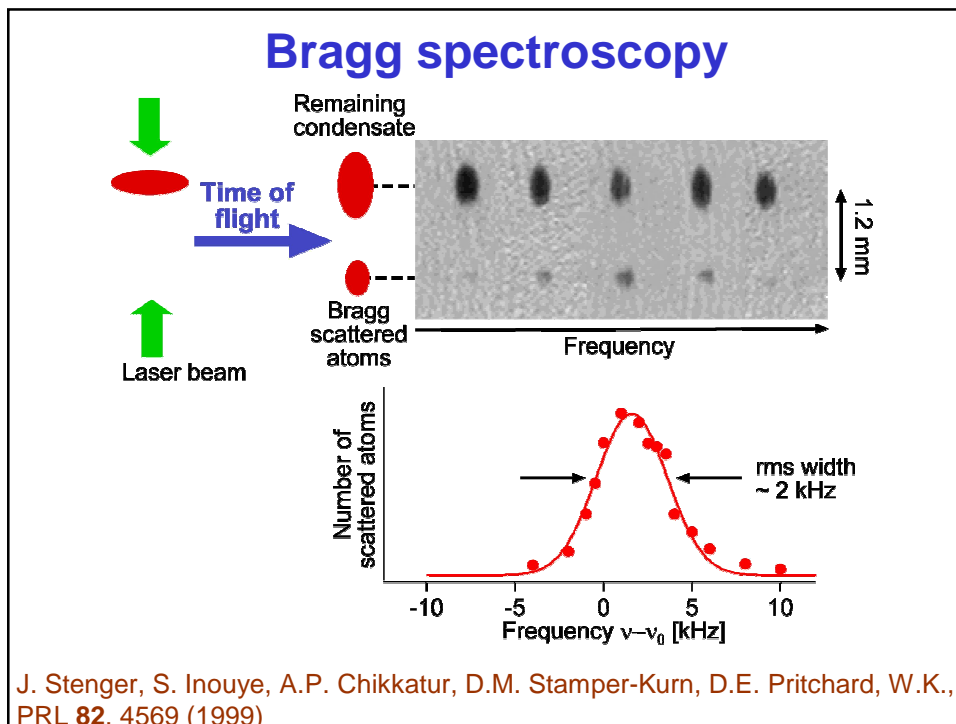
Bosons: Boulder, Garching, Innsbruck, MIT
Fermions: Boulder, Rice, Paris, Innsbruck, MIT

Condensation of pairs of fermionic lithium atoms



Frequency doubling of coherent matter waves

$$a_{2m}^+ a_m a_m$$
$$\hbar \omega = E = mc^2$$



Bragg resonance

transition $\mathbf{p}_i \rightarrow \mathbf{p}_f = \mathbf{p}_i + \mathbf{q}$

change of optical energy = change of kinetic energy

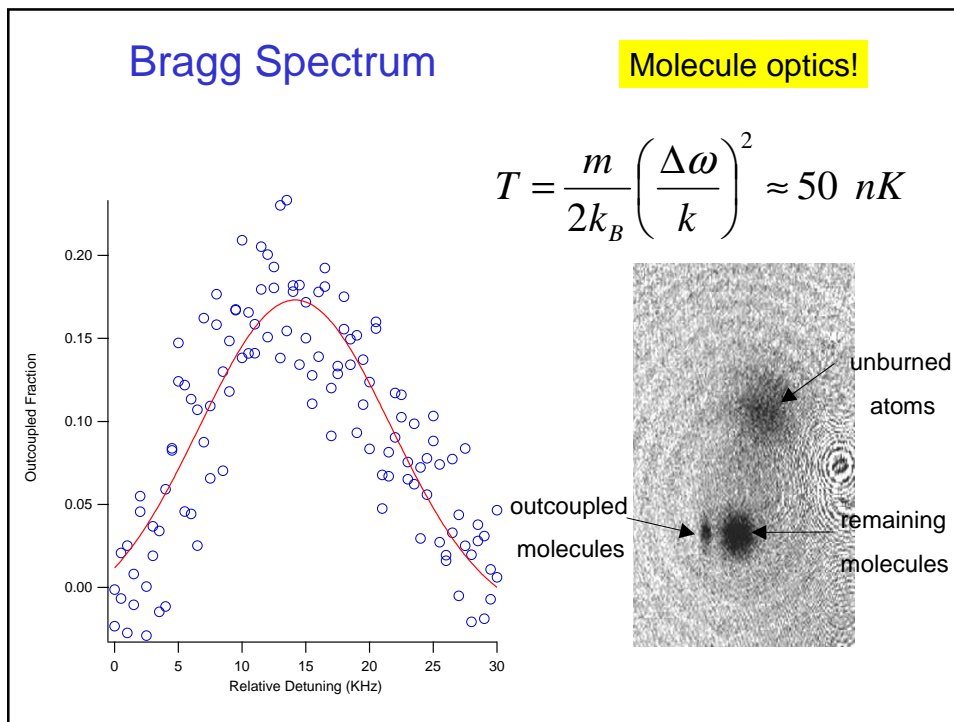
$$\hbar\omega_2 - \hbar\omega_1 = (\mathbf{q}^2/2m) + \mathbf{q} \cdot \mathbf{p}_i/m$$

recoil energy

Doppler shift $\mathbf{q} \cdot \mathbf{v}$

Coherence length \propto
(Doppler broadening)⁻¹

Doppler broadening
 \Rightarrow momentum distribution
of the condensate



Condensation of pairs of fermionic lithium atoms

Width of Bragg spectrum \propto (coherence length) $^{-1}$

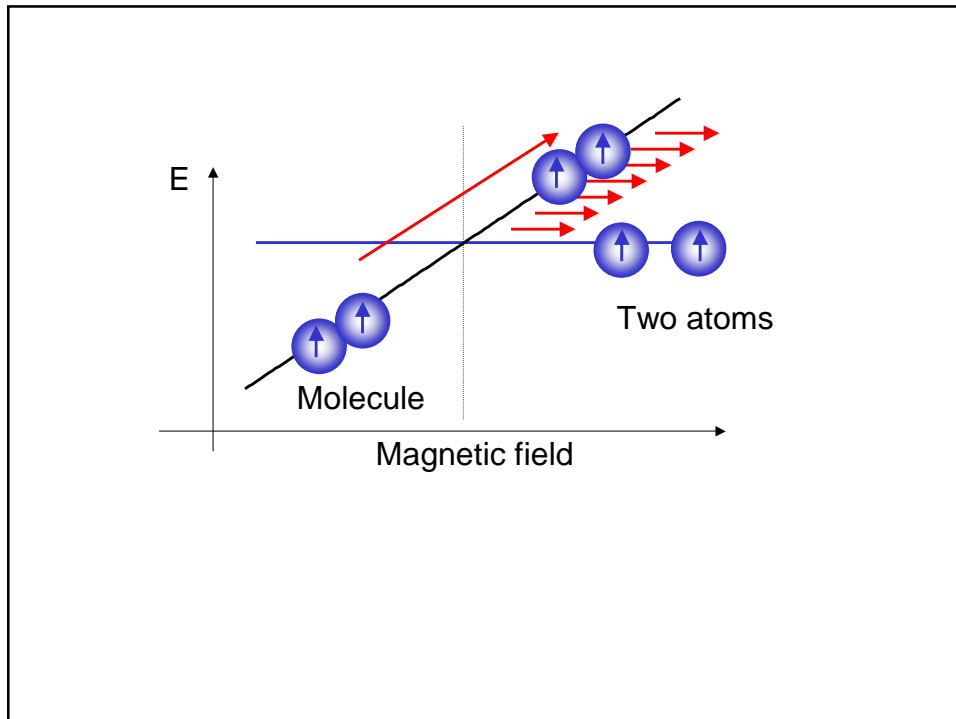
De Broglie Wavelength: 1.1 μm

Interparticle spacing: 0.86 μm

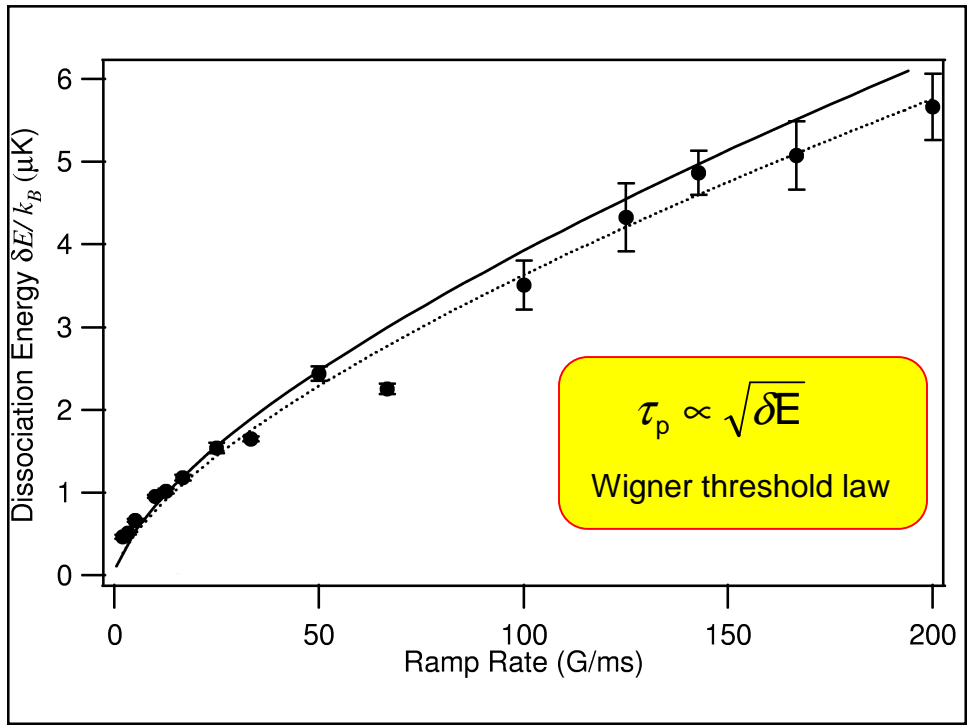
Phase space density: ~ 5

Possibly other contributions to the width:

- random motion
- excitations



Condensation of pairs of fermionic lithium atoms



Quantum degeneracy in fermions

Evaporative cooling of fermions

No s-wave collisions in single-component fermionic cloud

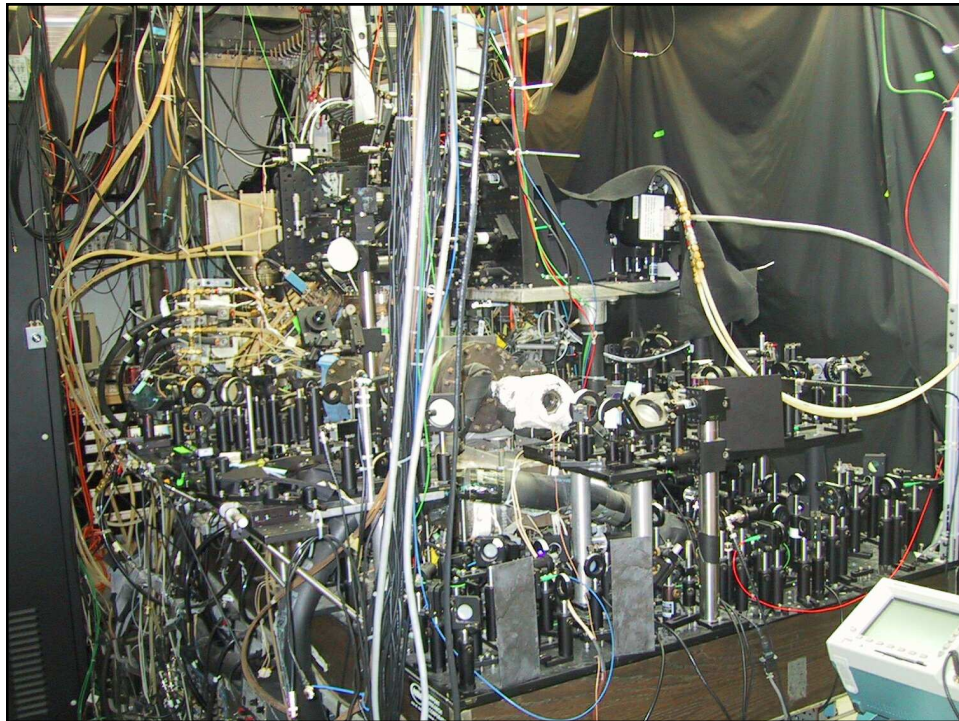
⇒ use mixtures

Fermion-Fermion

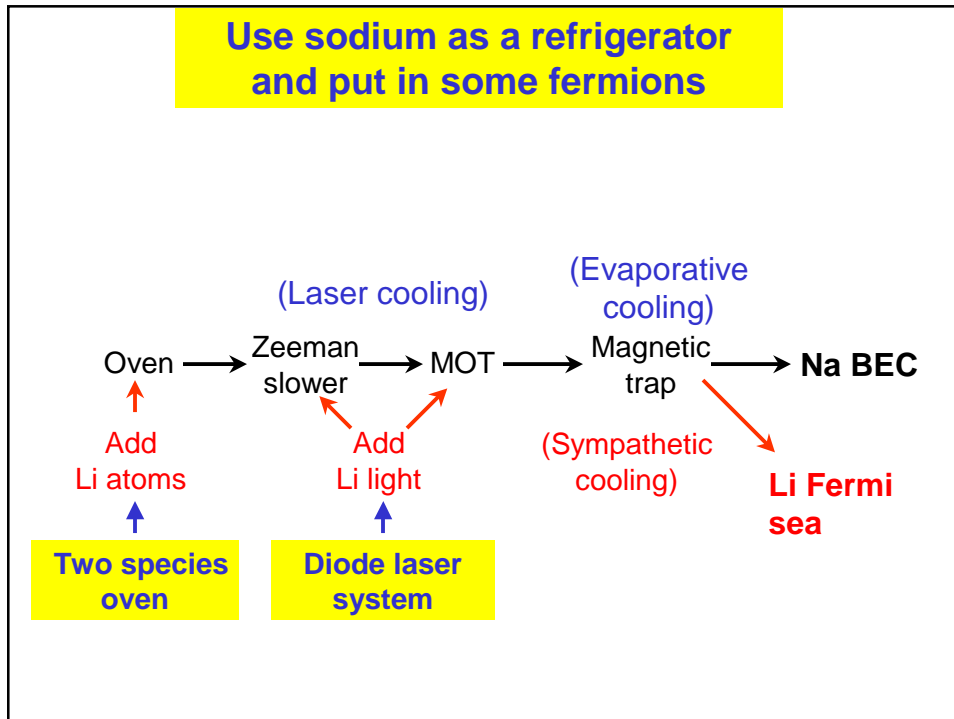
- Two hyperfine states of ^{40}K (Boulder, 1999)
- Two HFS of ^6Li (Duke, 2001; Innsbruck 2003)

Fermion-Boson

- ^6Li - ^7Li (Rice, 2001; Paris, 2001)
- ^6Li - ^{23}Na (MIT, 2001)
- ^{40}K - ^{87}Rb (Florence, 2002; Boulder, 2002; Zürich, 2004)

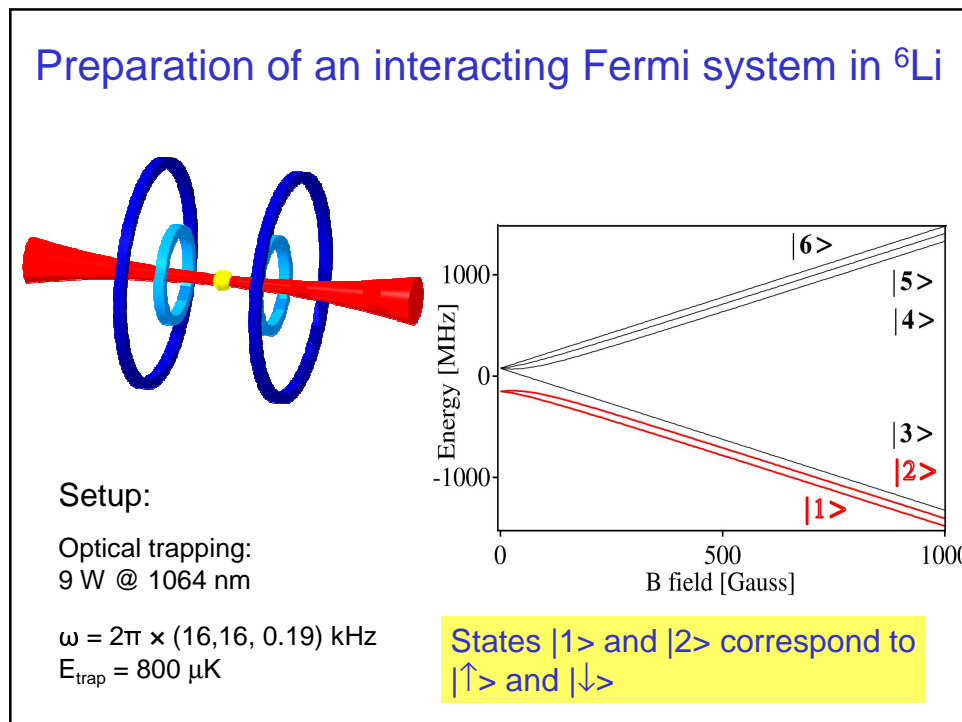
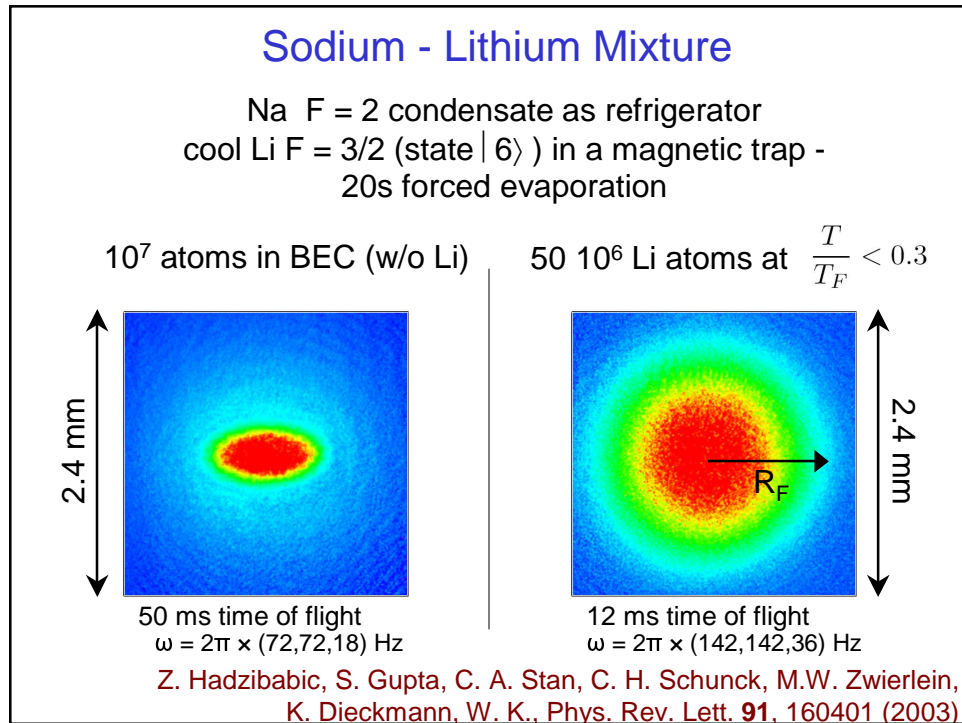


Condensation of pairs of fermionic lithium atoms

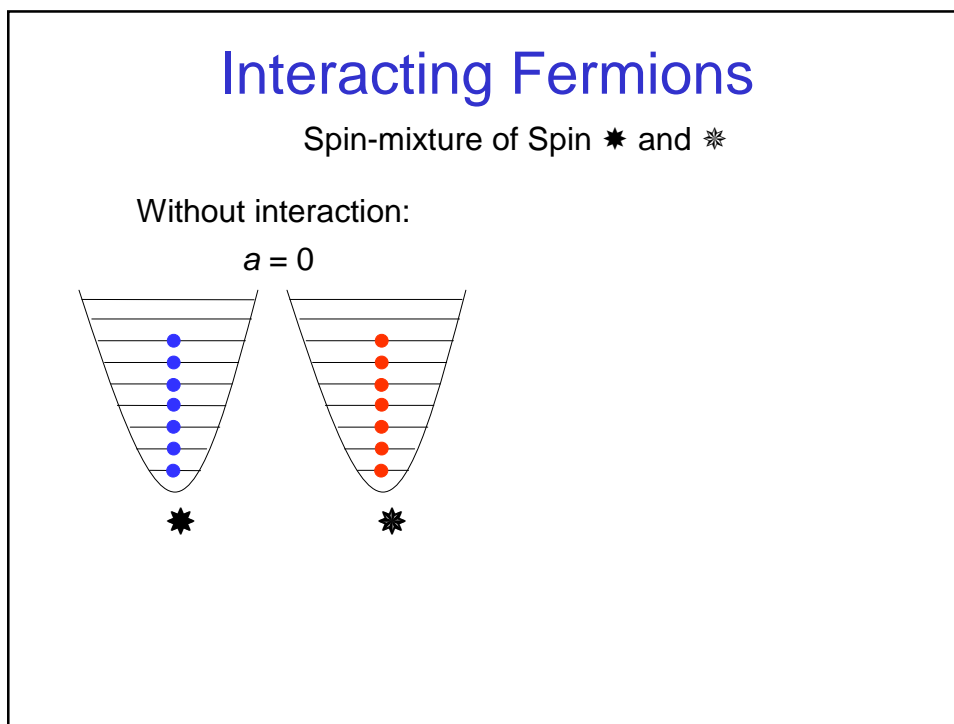
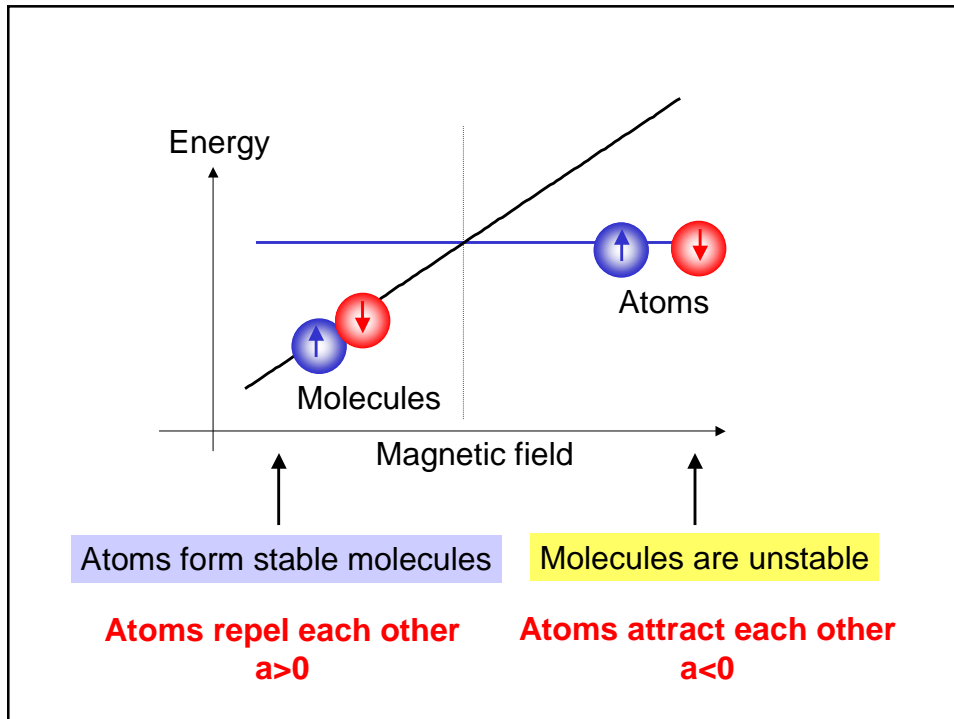


Quantum degenerate fermion-boson mixture: ${}^6\text{Li-Na}$

Z. Hadzibabic, C. Stan, S. Gupta, K. Dieckmann, M. Zwierlein, A. Görlitz, W. Ketterle, PRL **88**, 160401(2002).



Condensation of pairs of fermionic lithium atoms



Interacting Fermions

Spin-mixture of Spin \uparrow and \downarrow

With attractive interaction:
 $a < 0$

BCS-Transition
Condensation of
long-range Cooper pairs

$$T_C \approx 0.5 T_F e^{-\frac{\pi}{2k_F |a|}}$$

\uparrow We want a large and negative scattering length
 T_C/T_F is predicted to be as high as 0.2

Many theorists: Eagles, Nozières, Schmitt-Rink, Holland, Zwerger, Timmermans, Levin, Strinati, Combescot, Griffin, Stoof, Randeira

Interacting Fermions

Spin-mixture of Spin \uparrow and \downarrow

With repulsive interaction:
 $a > 0$

BEC-Transition
Condensation of
tightly bound Fermion pairs

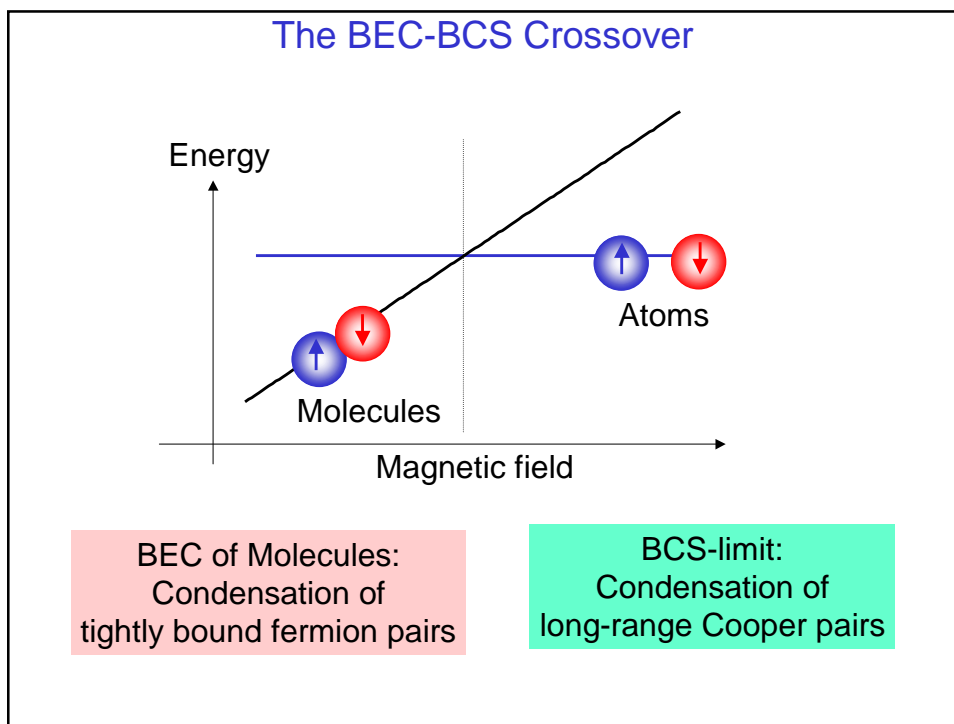
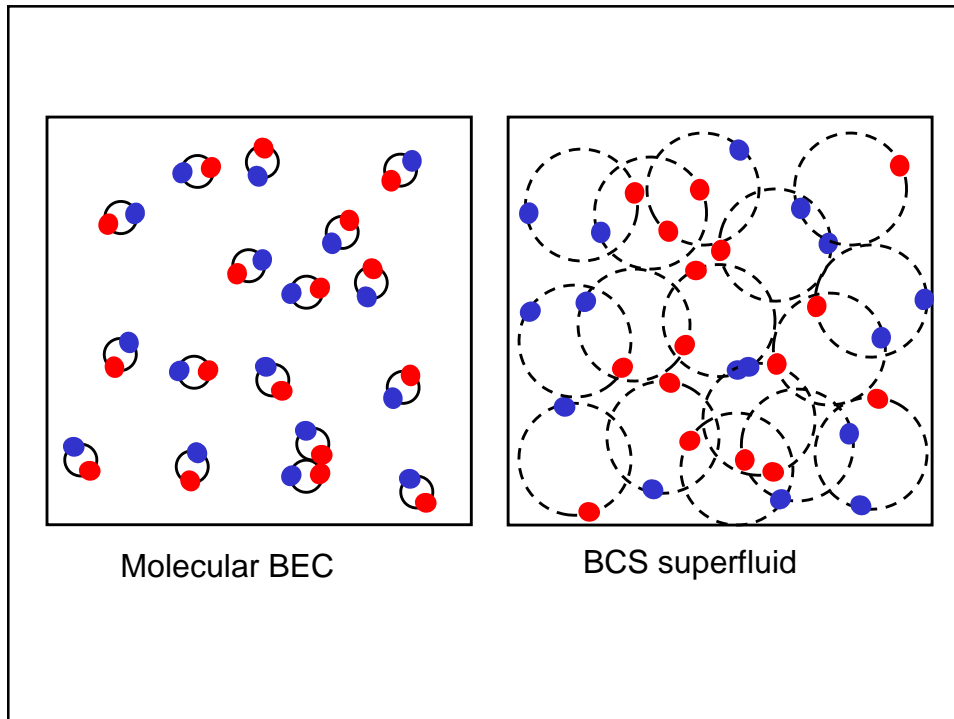
$$T_C = 0.91 \hbar \bar{\omega} N_{\text{mol}}^{1/3}$$

$$= 0.5 T_F$$

$$E_B = -\frac{\hbar^2}{2ma^2}$$

A bound state appears! per atom

Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms

BCS

$$\frac{\text{Binding energy of pairs}}{\text{Fermi energy}} \approx \frac{\text{Transition temperature}}{\text{Fermi temperature}} \approx$$


| | | |
|---|-------------------------|----------------------------|
| { | $10^{-5} \dots 10^{-4}$ | normal superconductors |
| | 10^{-3} | superfluid ^3He |
| | 10^{-2} | high T_c superconductors |

BEC

$$\frac{\text{Binding energy of bosons}}{k_B \text{ BEC transition temperature}} \approx$$

| | | |
|---|-----------|--------------------------|
| { | 10^5 | superfluid ^4He |
| | 10^{10} | alkali BEC |

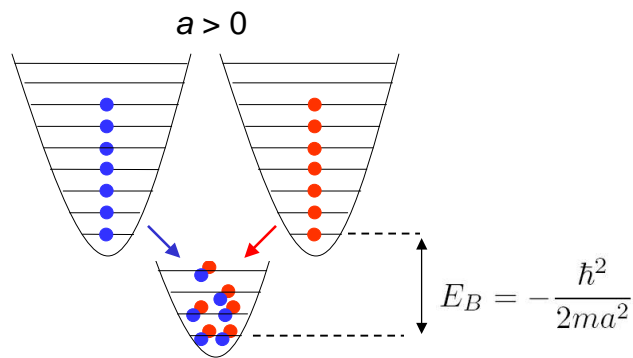
$$\frac{\text{Binding energy of composite boson}}{k_B \text{ degeneracy temperature}} \approx$$

| | | | |
|----------|--------------------------|----------------------------|---|
| { | $10^{-5} \dots 10^{-4}$ | normal superconductors |  |
| | 10^{-3} | superfluid ^3He | |
| | 10^{-2} | high T_c superconductors | |
| 1 | BEC-BCS crossover | | |
| { | 10^5 | superfluid ^4He | |
| | 10^{10} | alkali BEC | |

Direct evaporation of ${}^6\text{Li}$ molecules

Long lifetime of Lithium molecules! (ENS, Rice)

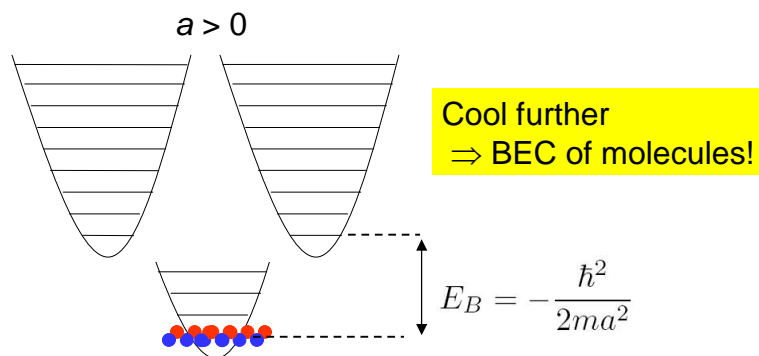
- ↳ Directly evaporate at large and positive a
- ↳ Form molecules by three-body recombination when $kT \ll E_B$



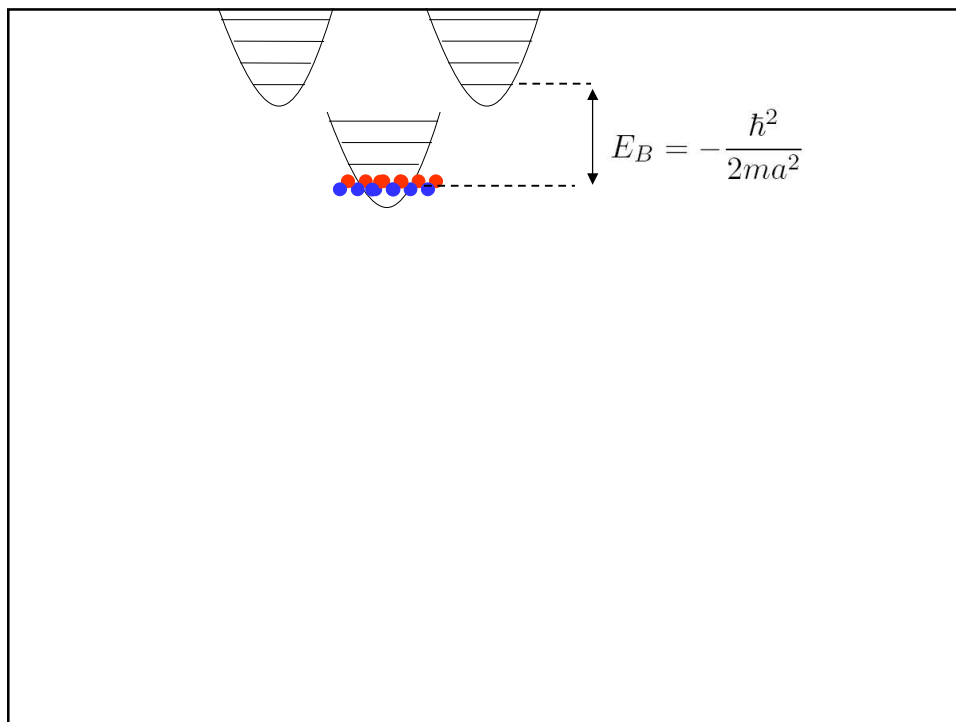
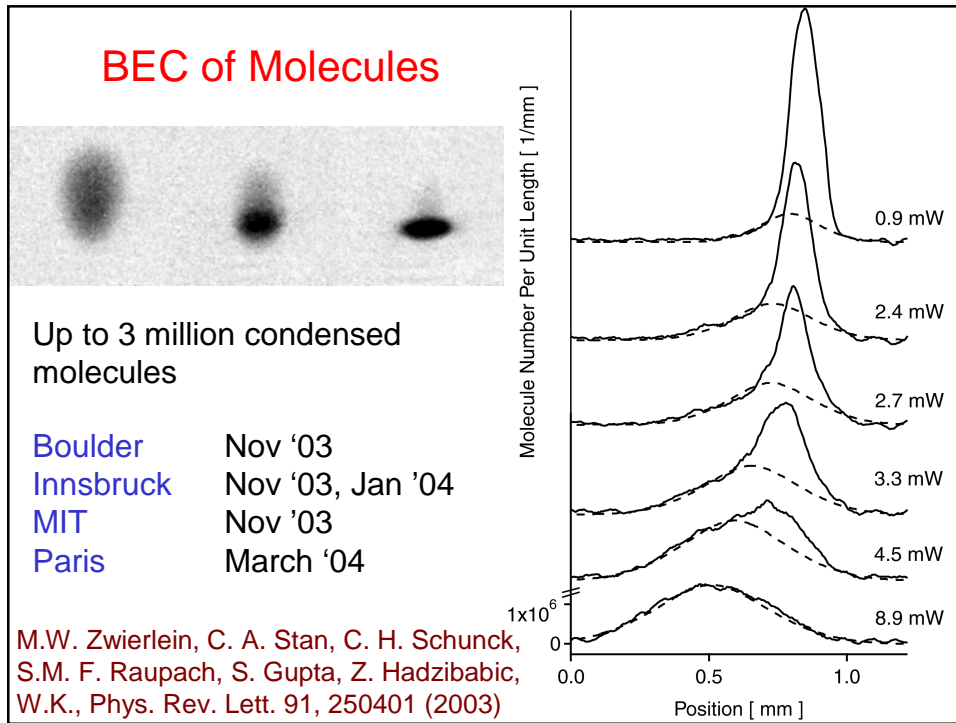
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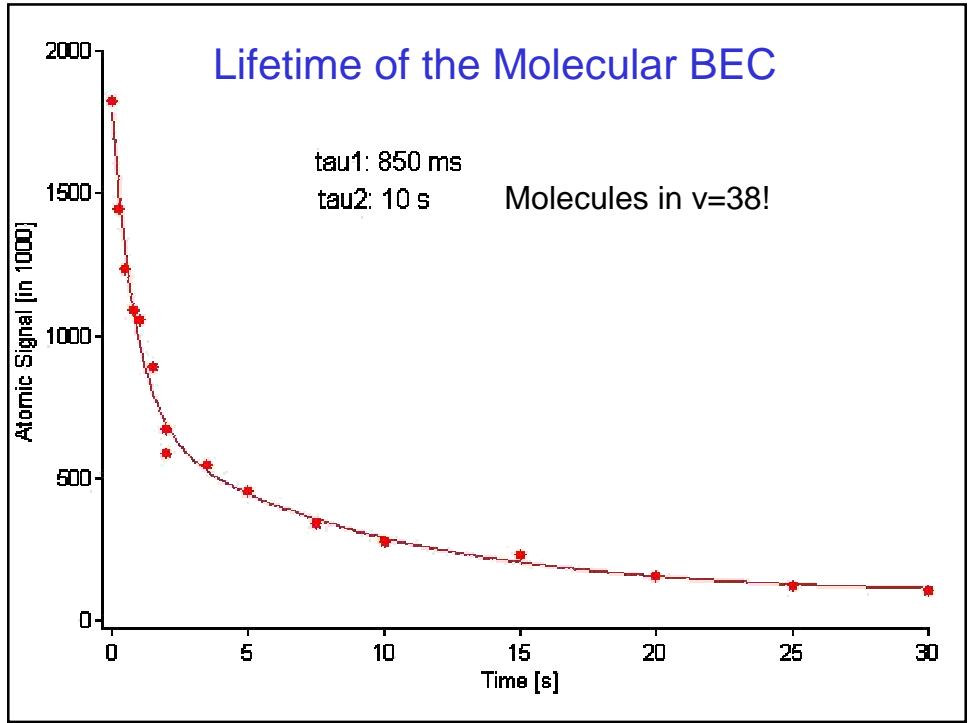
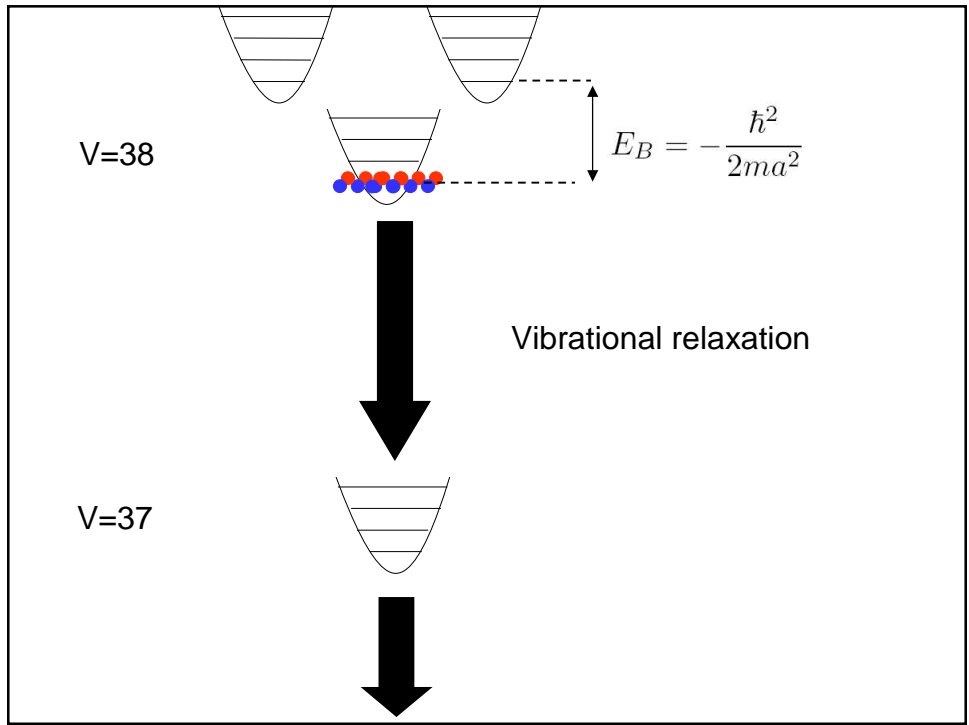
- ↳ Directly evaporate at large and positive a
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Condensation of pairs of fermionic lithium atoms



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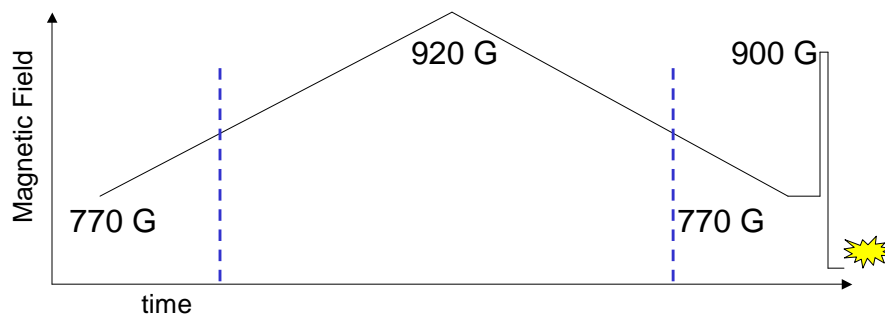
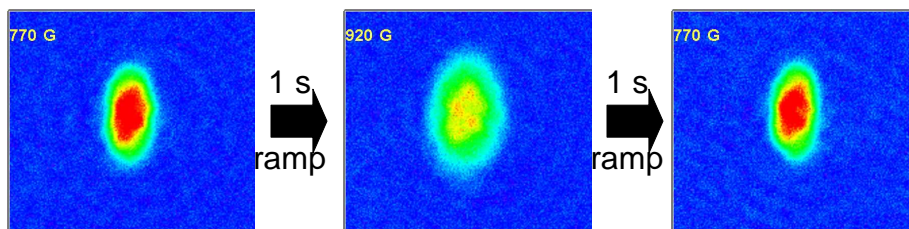


Crossover from a Degenerate Fermi Gas to a BEC of molecules

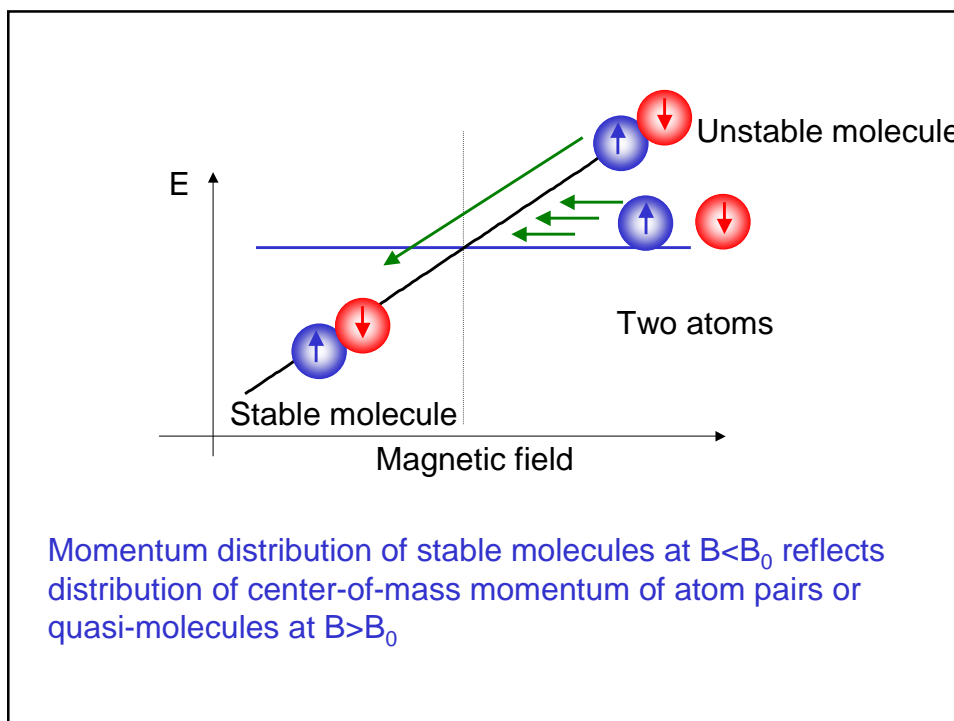
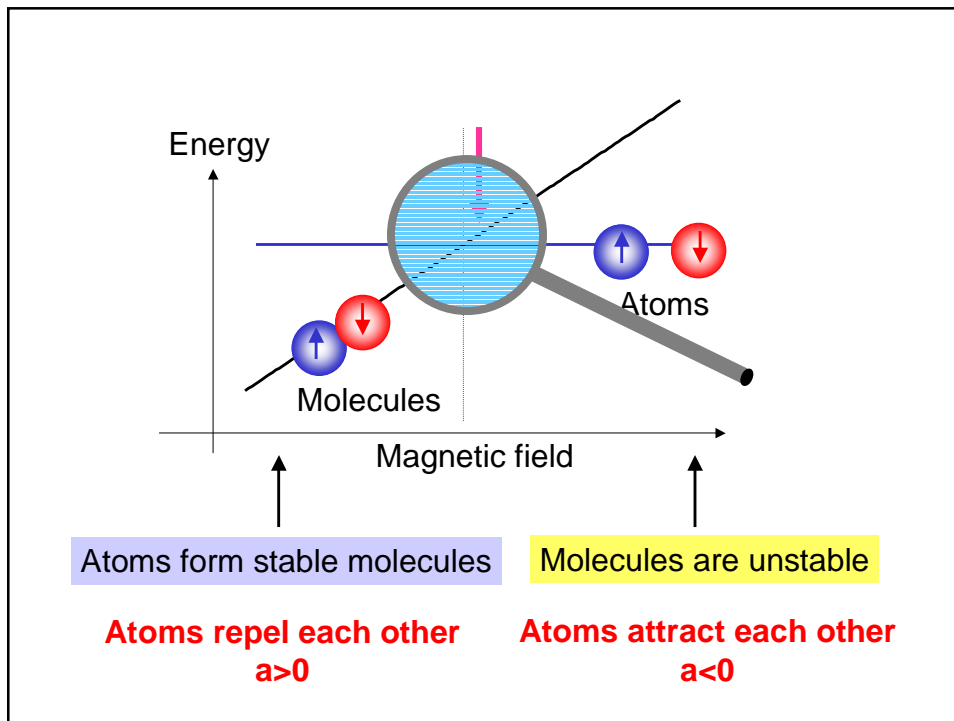
Recent results of the last few months:

- Innsbruck
- Boulder
- MIT
- Paris
- Duke

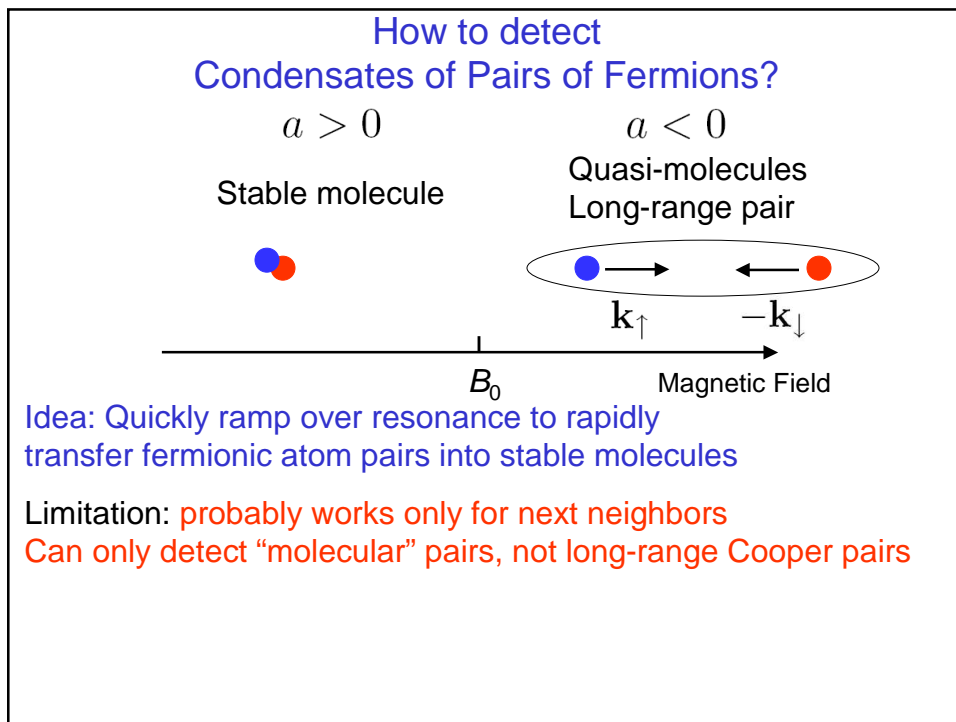
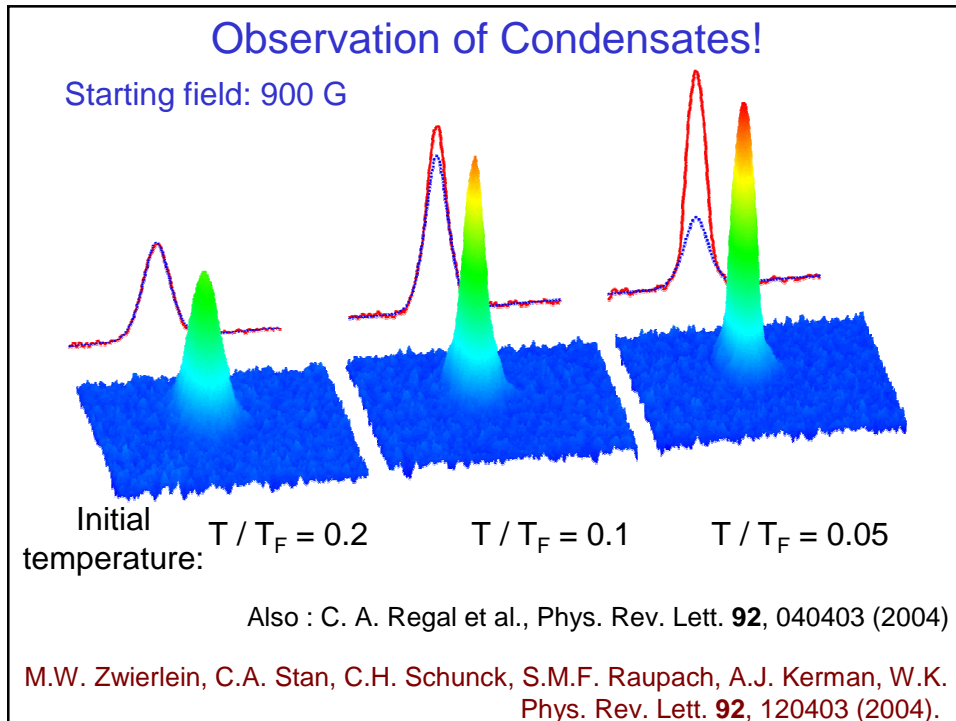
Crossover from a BEC to a Degenerate Fermi Gas ...and back



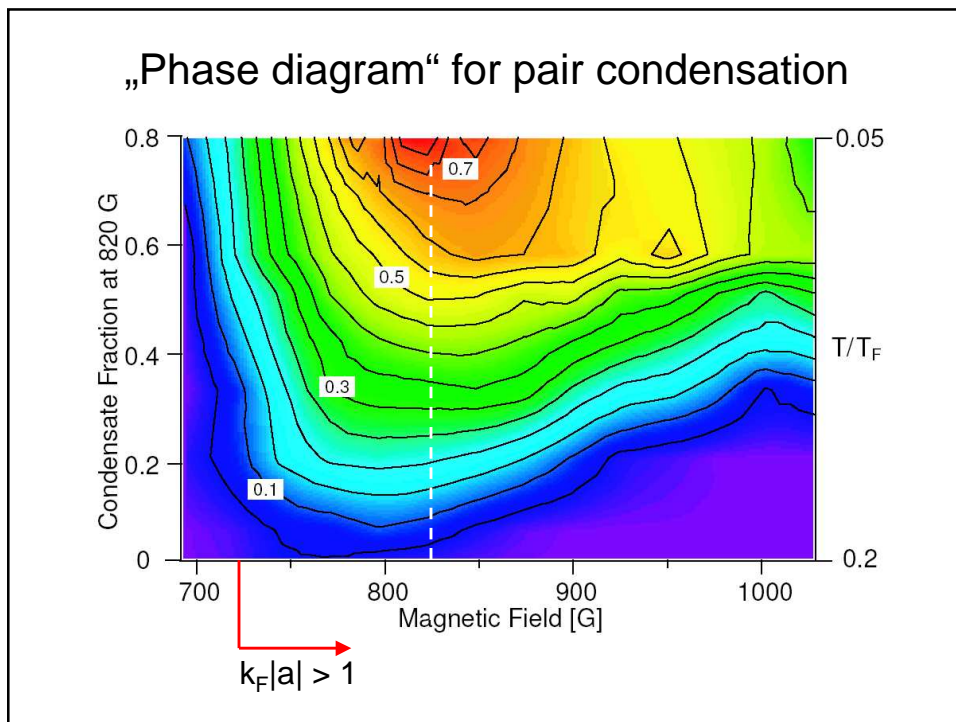
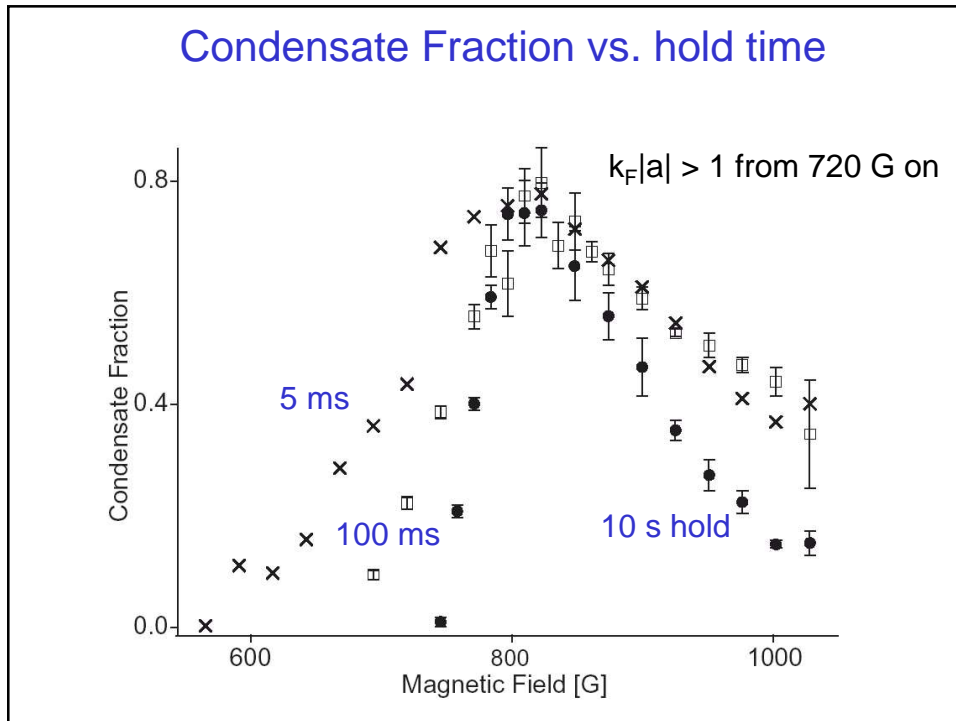
Condensation of pairs of fermionic lithium atoms



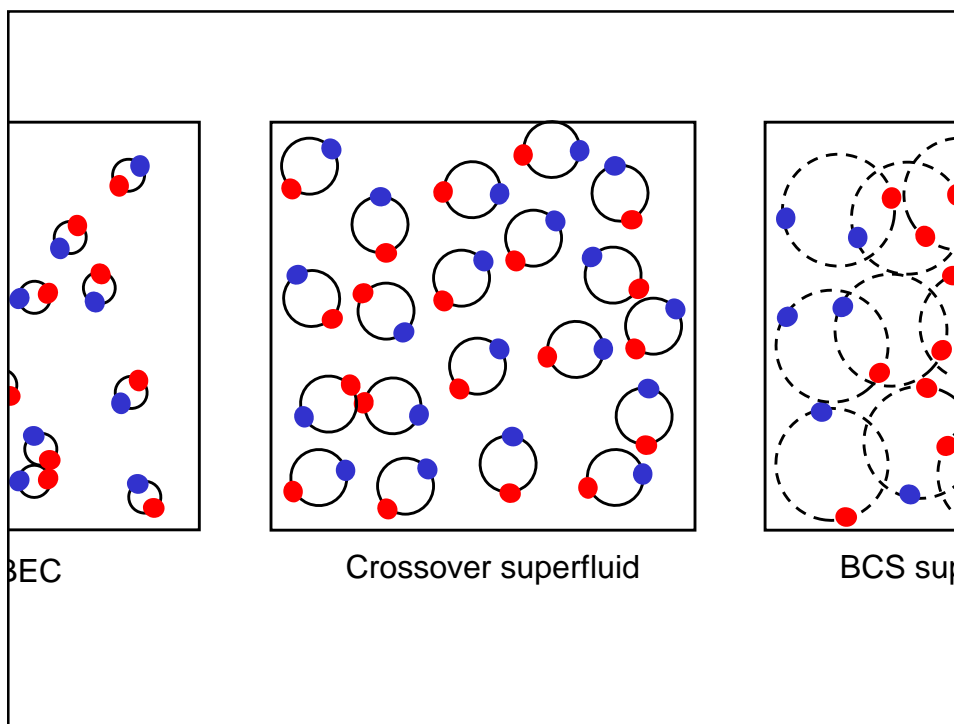
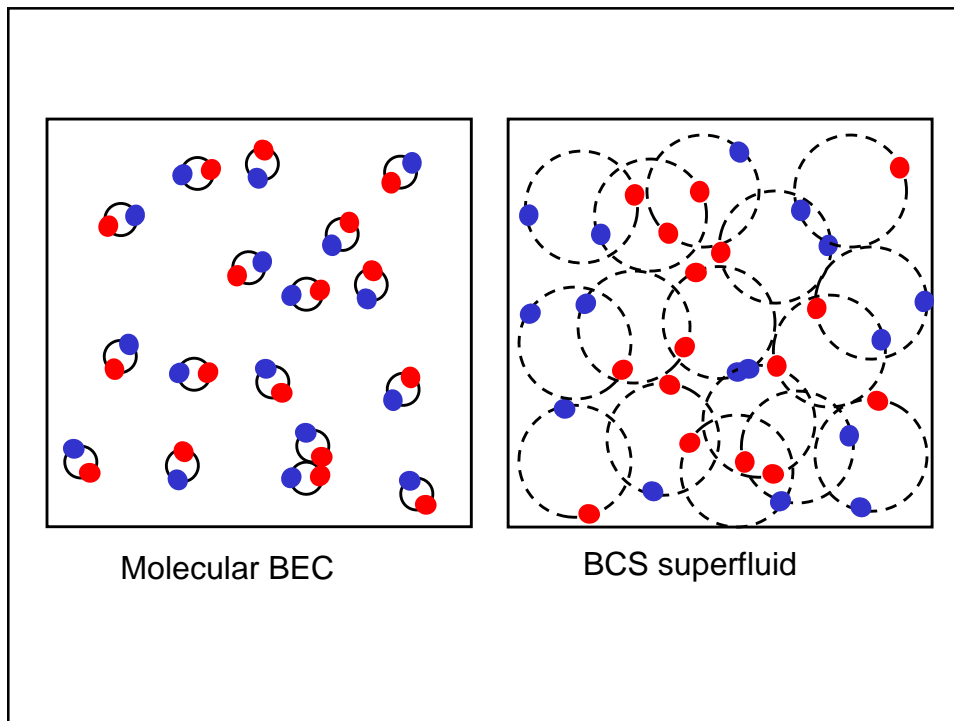
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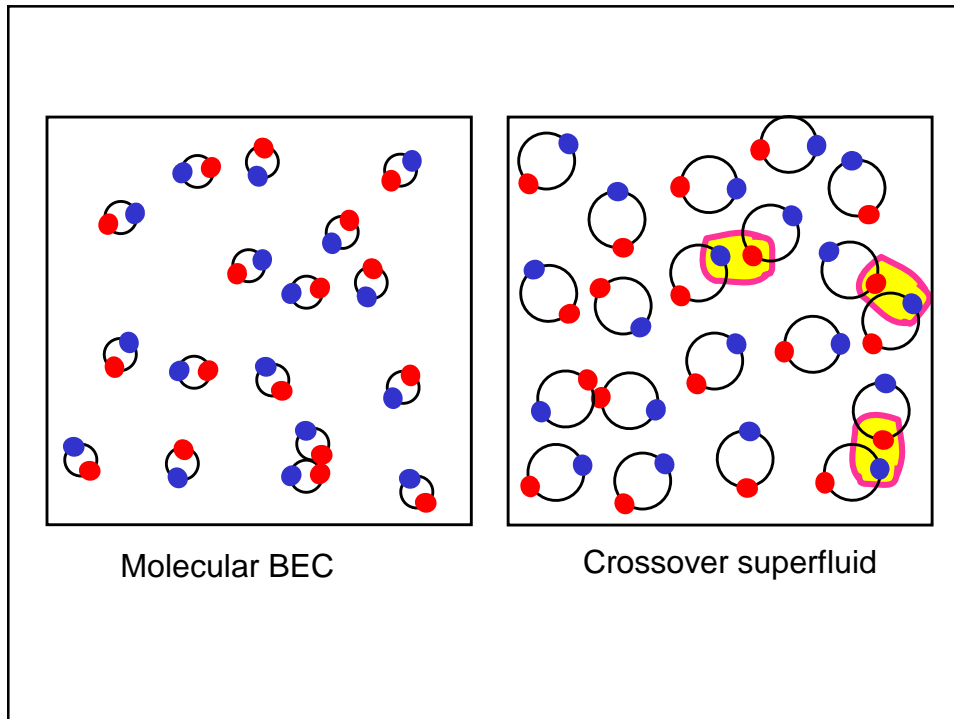
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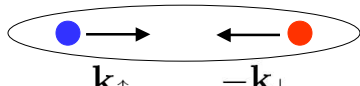
Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



**How to detect
Condensates of Pairs of Fermions?**

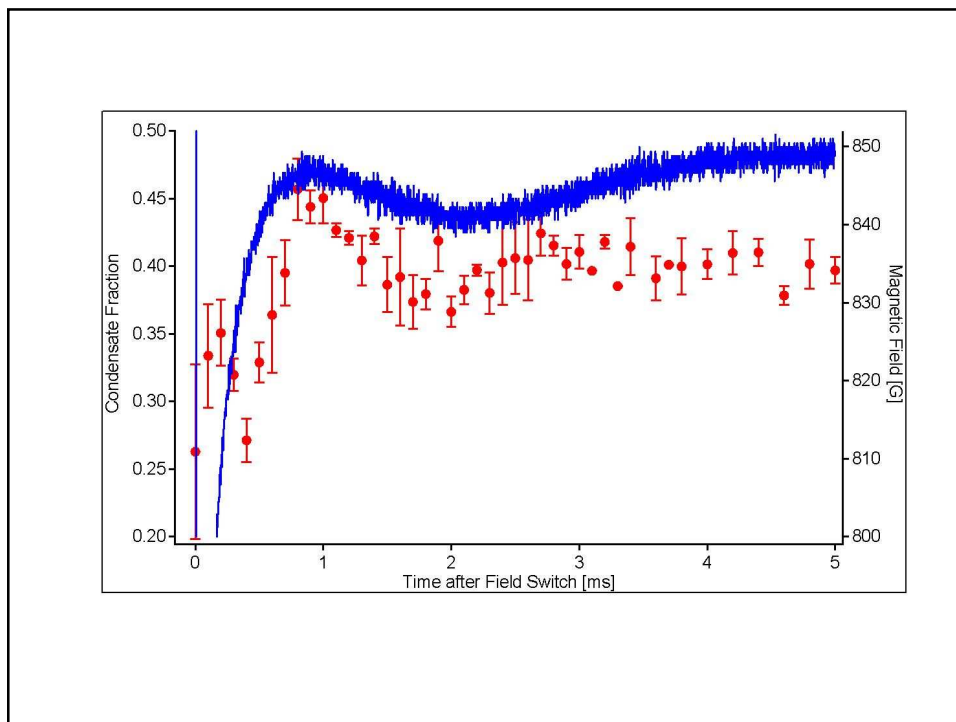
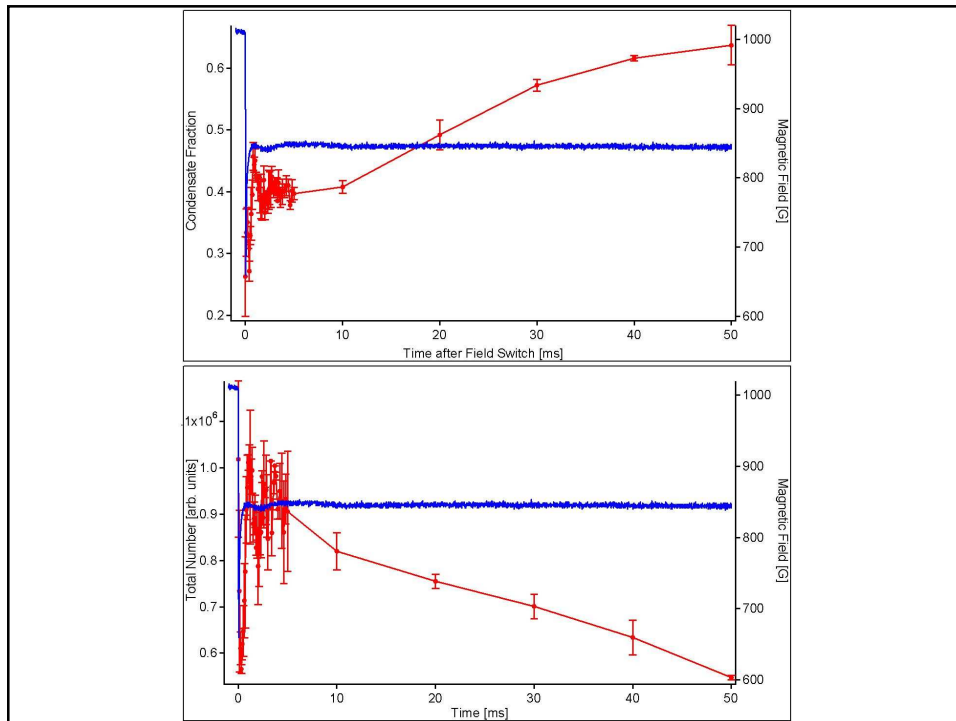
| | |
|---|--|
| <p>$a > 0$</p> <p>Stable molecule</p>  | <p>$a < 0$</p> <p>Quasi-molecules Long-range pair</p>  |
| <p>————— —————→ Magnetic Field</p> <p style="margin-left: 100px;">B_0</p> | |

Idea: Quickly ramp over resonance to rapidly transfer fermionic atom pairs into stable molecules

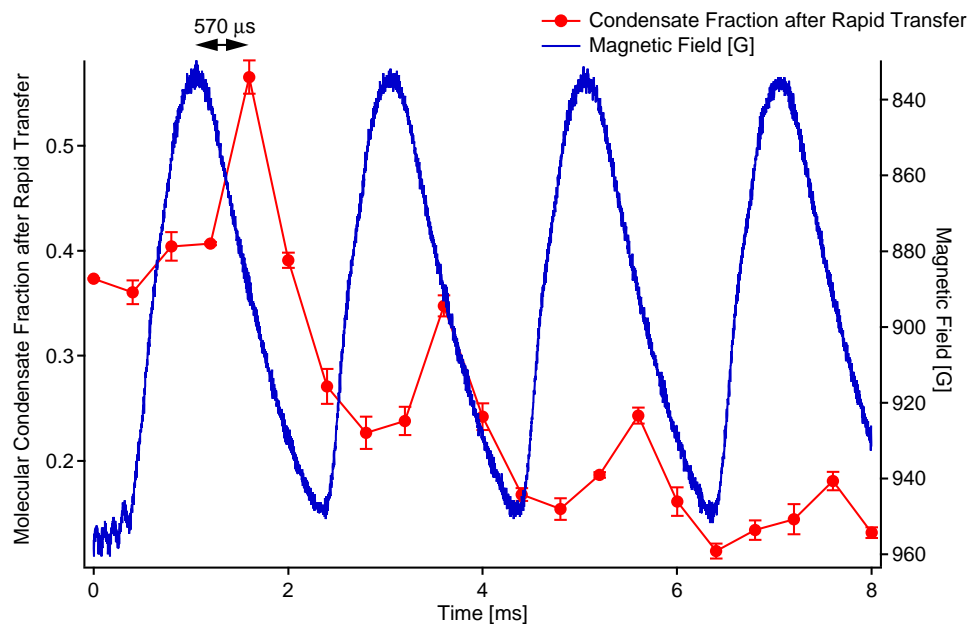
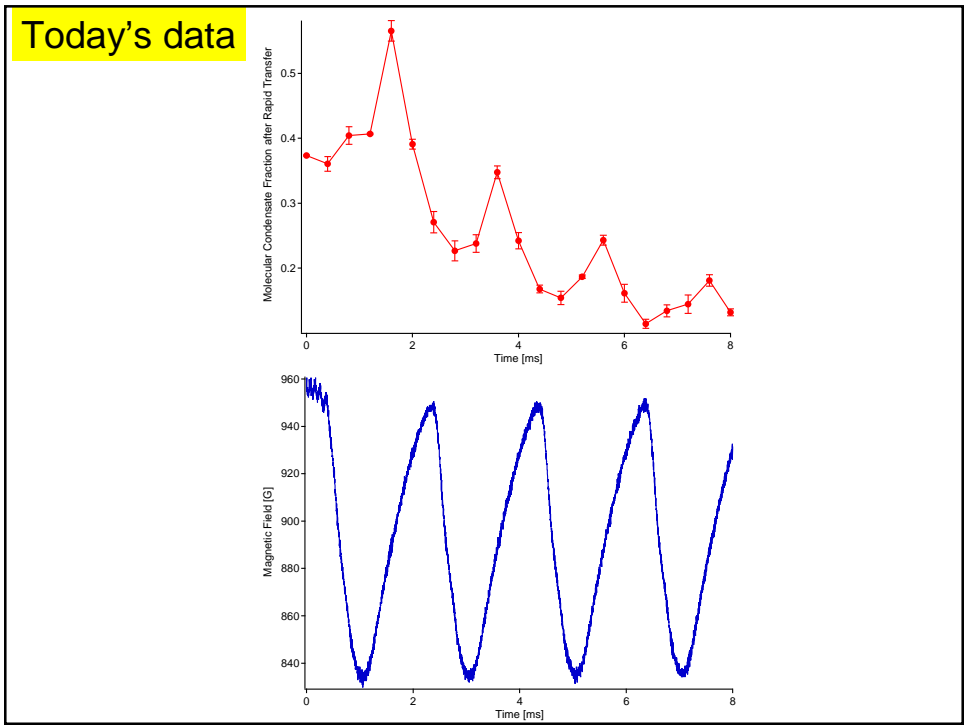
Limitation: probably works only for next neighbors
Can only detect “molecular” pairs, not long-range Cooper pairs

Is the ramp fast enough to neglect collisions or other dynamics?

Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



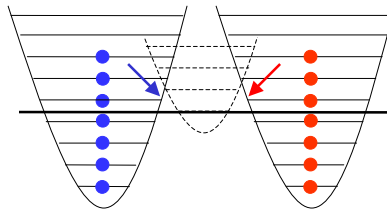
Condensation of pairs of fermionic lithium atoms

What's going on?

Tentative interpretation:

High condensate fraction implies pre-existing molecules above the two-body resonance position – stabilized by the Fermi sea

Simple model, neglecting interactions

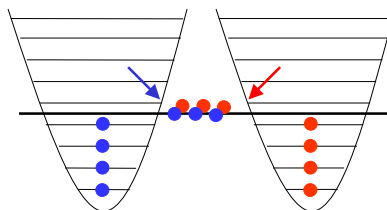


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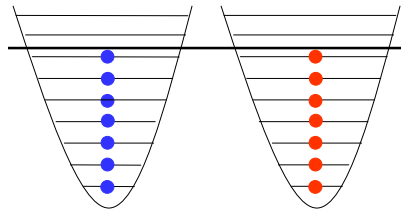
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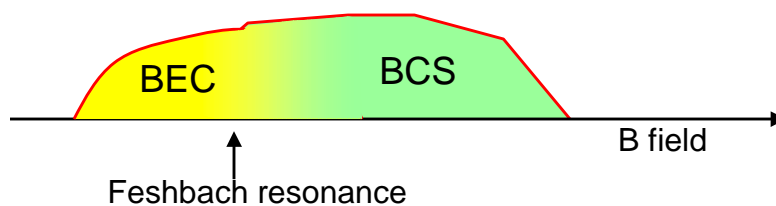
High condensate fraction implies pre-existing molecules above the two-body resonance position – stabilized by the Fermi sea

„Cooper pairs“ become delocalized only when $E_{\text{Mol}} \ll 2 E_F$ or equivalently $k_F |a| \gg 1$

Simple model, neglecting interactions



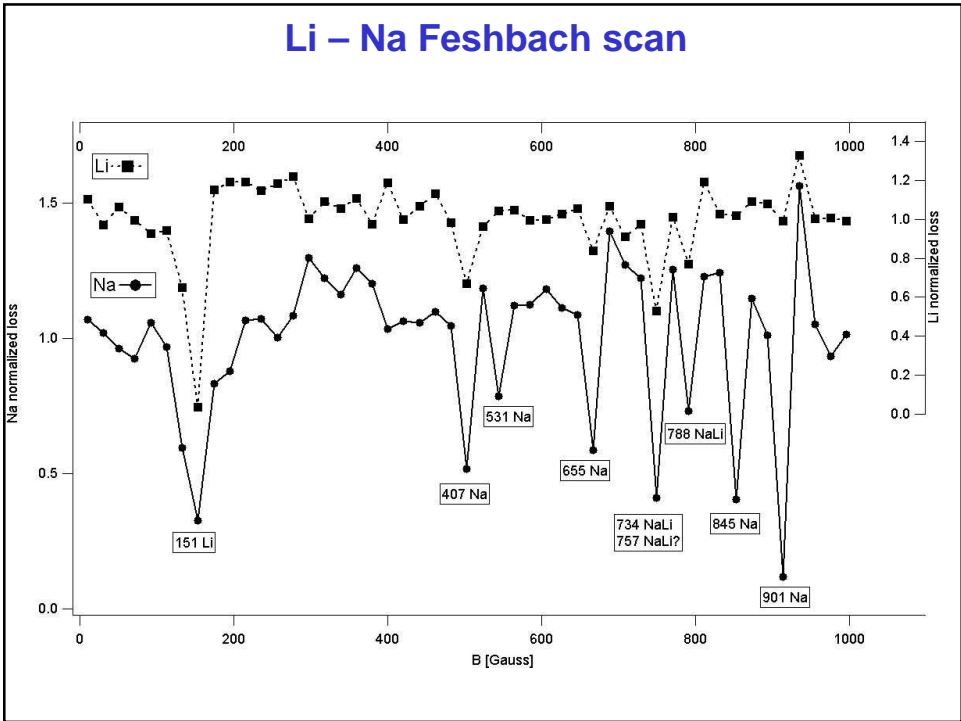
Also: H. T. C. Stoof, preprint cond-mat/0402xxx



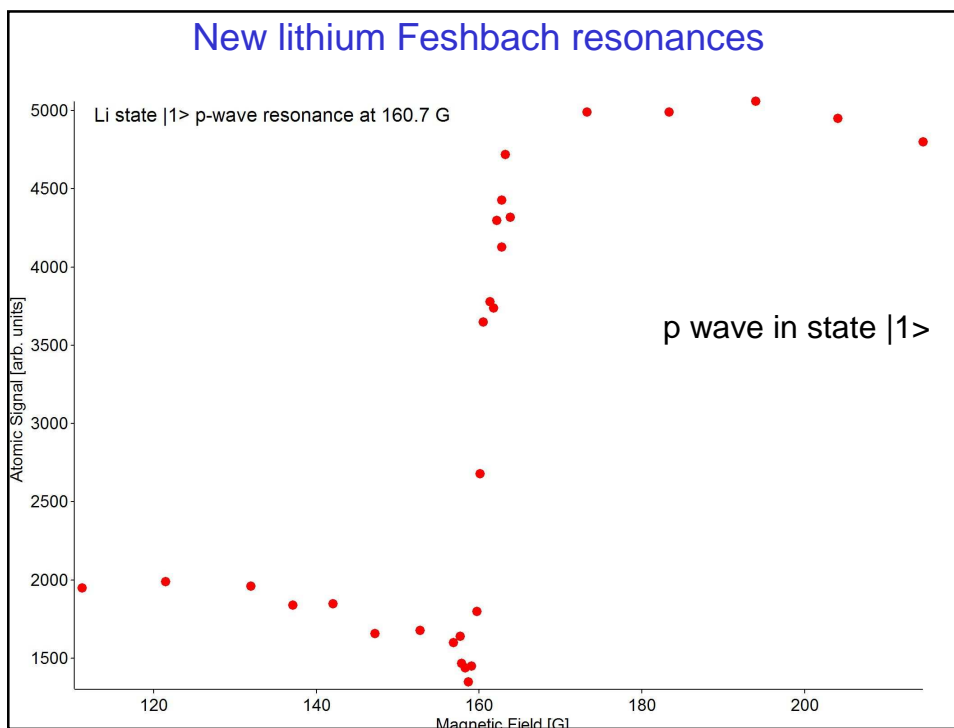
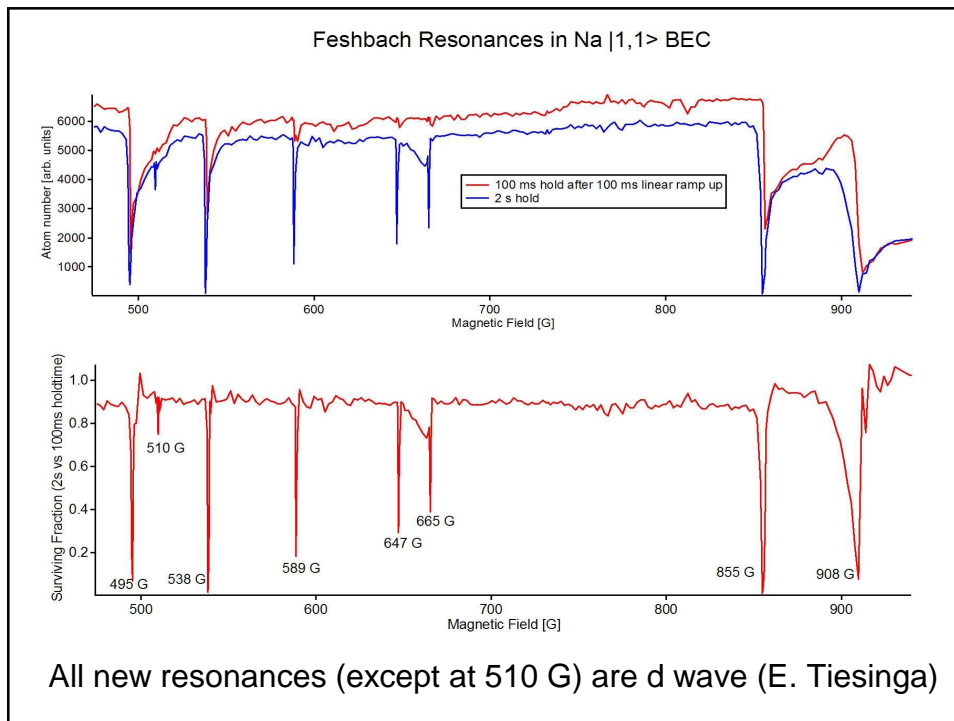
All experimental results are consistent with the existence of a molecular condensate above the Feshbach resonance

Molecules above the Feshbach resonance and tightly bound Cooper pairs are probably the same

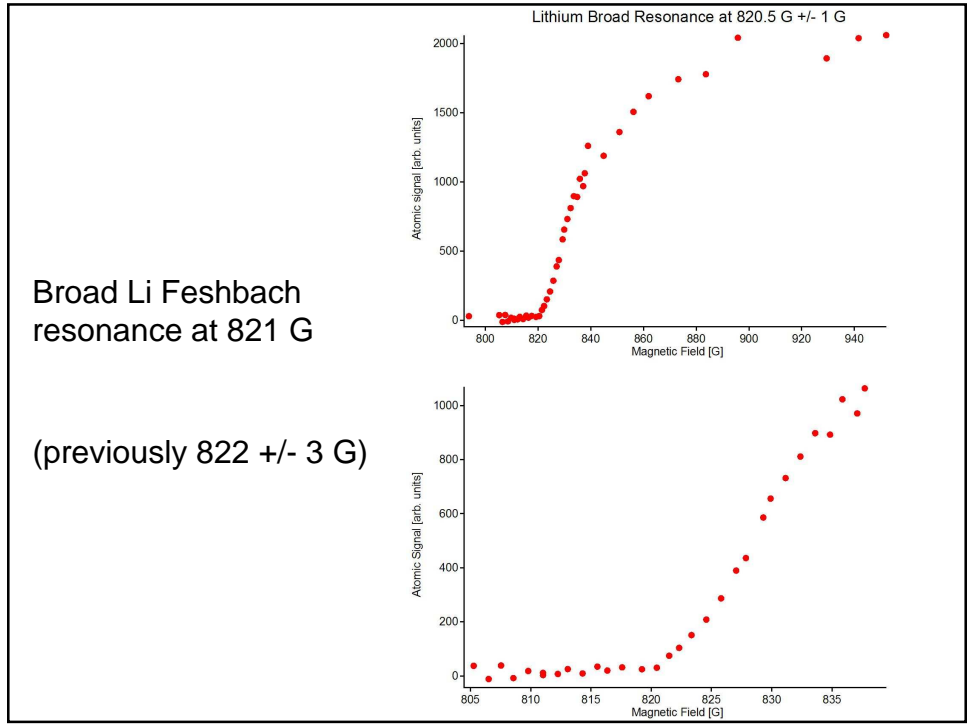
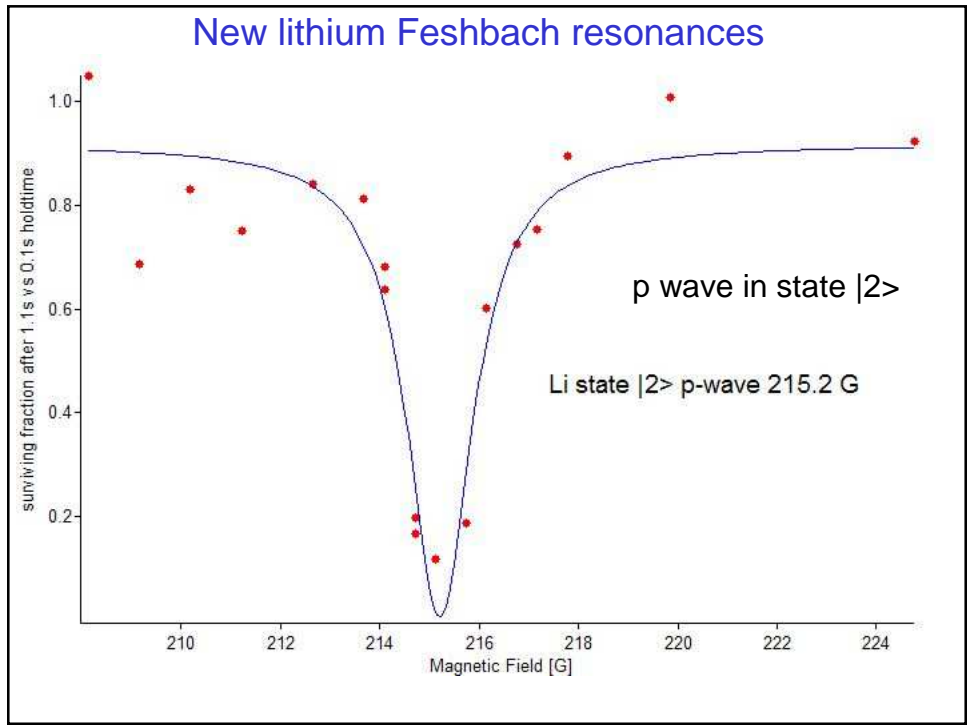
Heteronuclear fermionic molecules



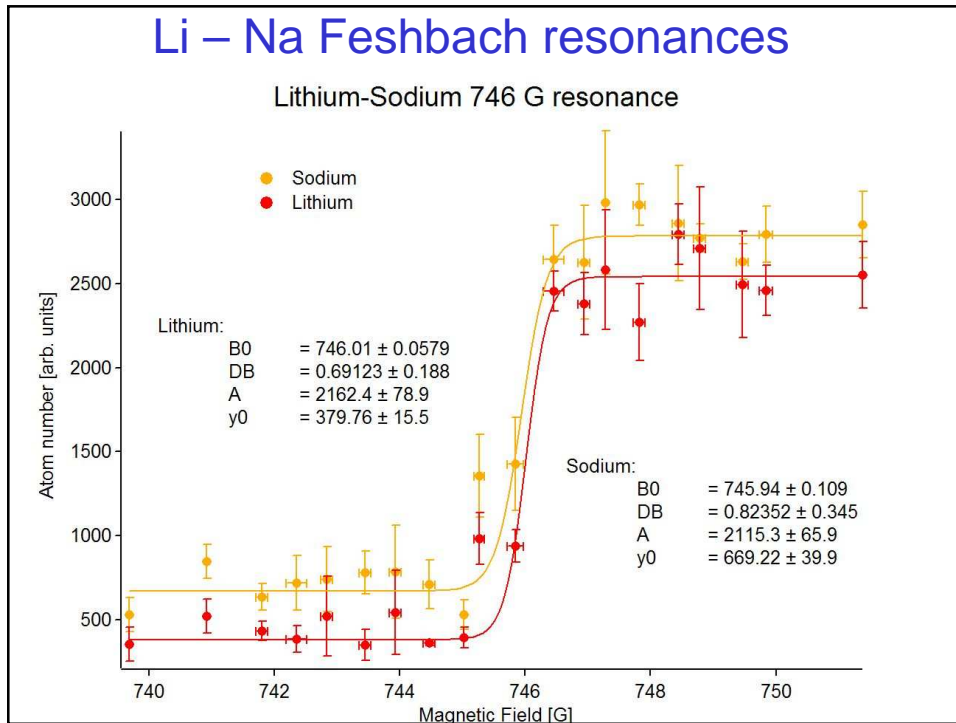
Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



Condensation of pairs of fermionic lithium atoms



Li – Na Feshbach resonances

at 746, 760, 795 G

Stable LiNa molecules?

Should be stable after blasting Li and Na away
and outside the Feshbach resonance, when fermionic nature
suppresses collisions

Condensation of pairs of fermionic lithium atoms

The Lithium Team



Claudiu A. Stan, Sebastian M.F. Raupach, W.K.,
Christian H. Schunck, Martin W. Zwierlein, Andrew J. Kerman

Not shown: Subhadeep Gupta, Zoran Hadzibabic