

*(Lucas et al. 1977)*



# Is there a Tatooine?

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*Prof. Kaitlin M. Kratter  
University of Arizona  
March 14th, 2017, KITP*

# From 18th century problems to exotic exoplanets

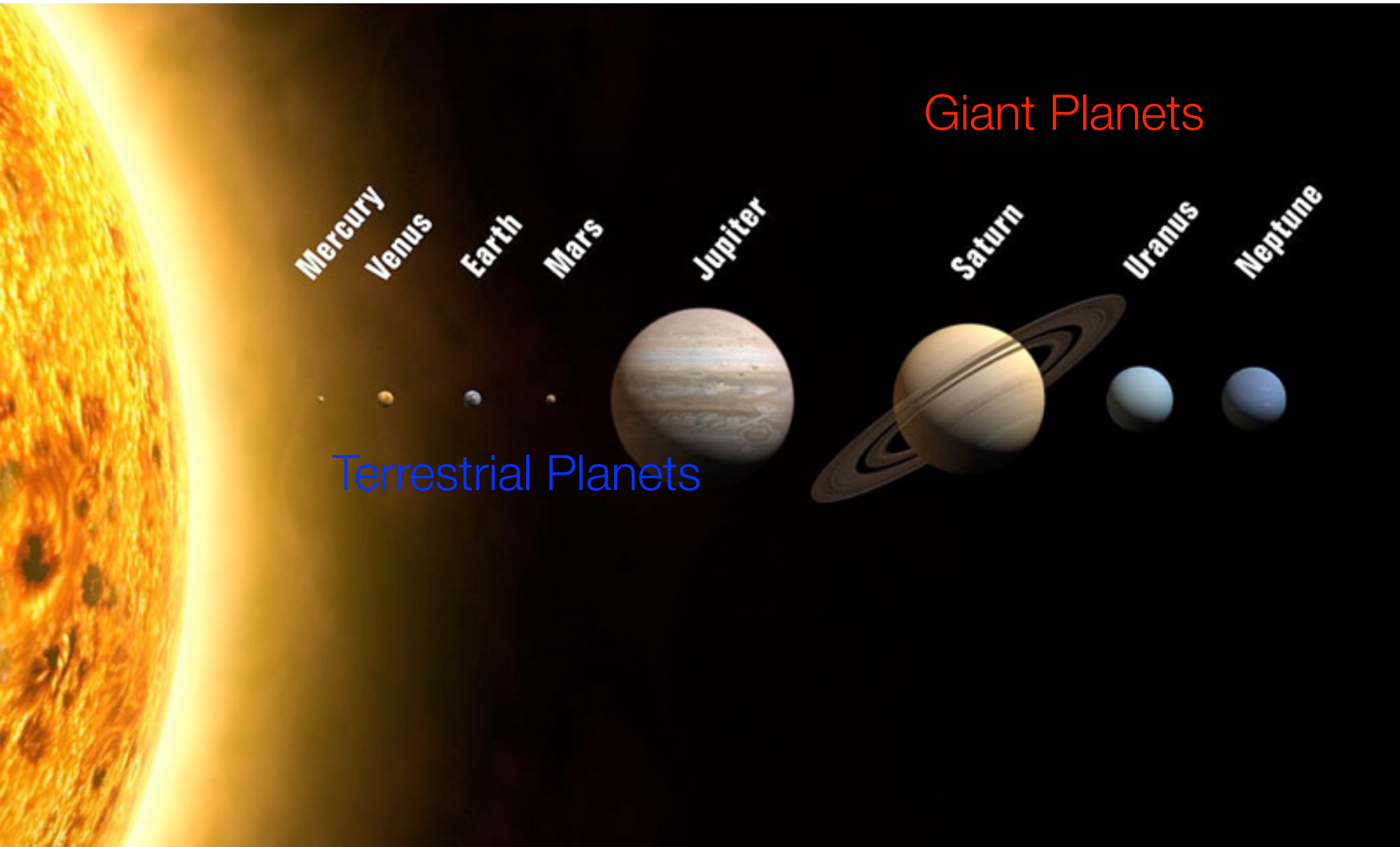
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- The observational **exoplanet revolution**
- How do we model the **gravitational interactions** of systems containing more than two massive bodies?
- How can we use **celestial mechanics** to gain new insight into the mysteries of planet formation?



Pierre-Simon Laplace (1749–1827). Posthumous portrait by Jean-Baptiste Paulin Guérin, 1838.

# Our Solar System



Giant Planets

Mercury

Venus

Earth

Mars

Jupiter

Saturn

Uranus

Neptune

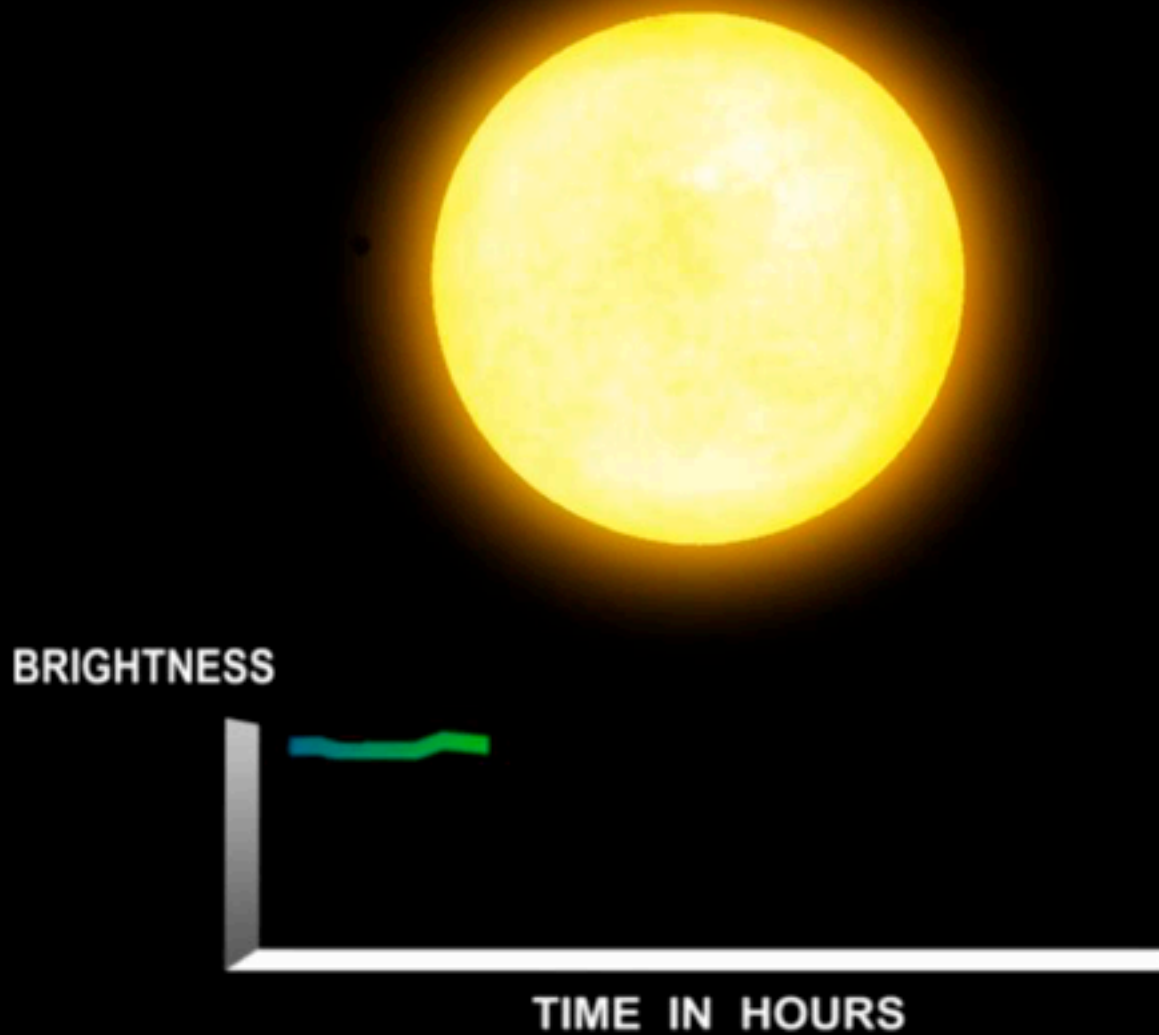
Terrestrial Planets

# Kepler Space Telescope

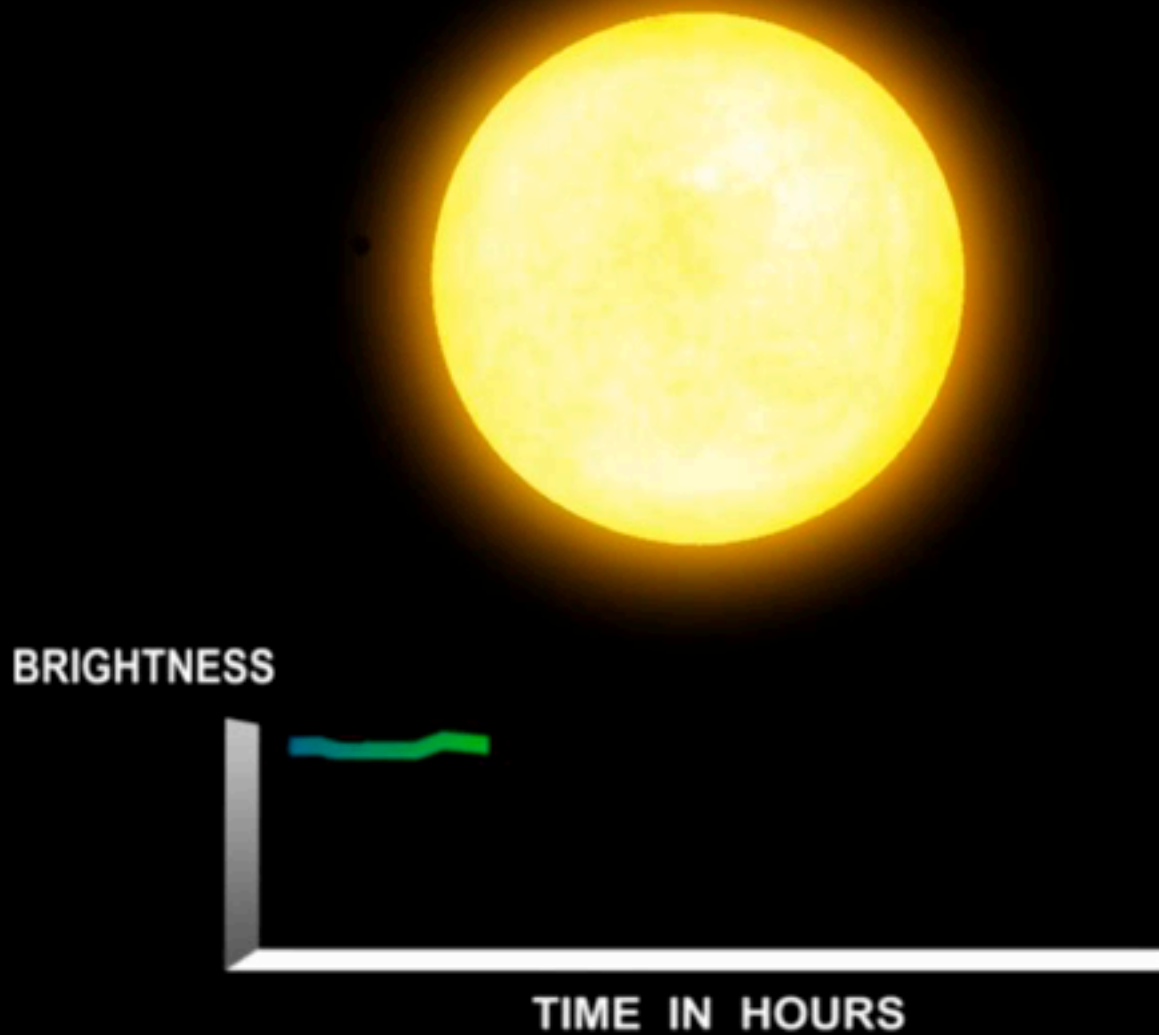


Image Credit: NASA

# Exoplanet Detection: Transits



# Exoplanet Detection: Transits



# The Exoplanet Revolution

Movie by Alex Parker



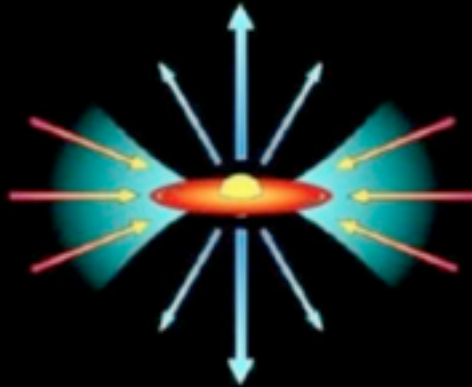


How do we extract meaning from all of this data?

*Shu et al. 1987 (updated)*



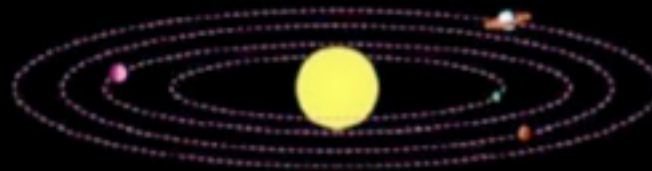
$10^4$  yrs;  $10-10^4$  AU;  $10-300$  K



$10^{5-6}$  yrs;  $1-1000$  AU;  $100-3000$  K

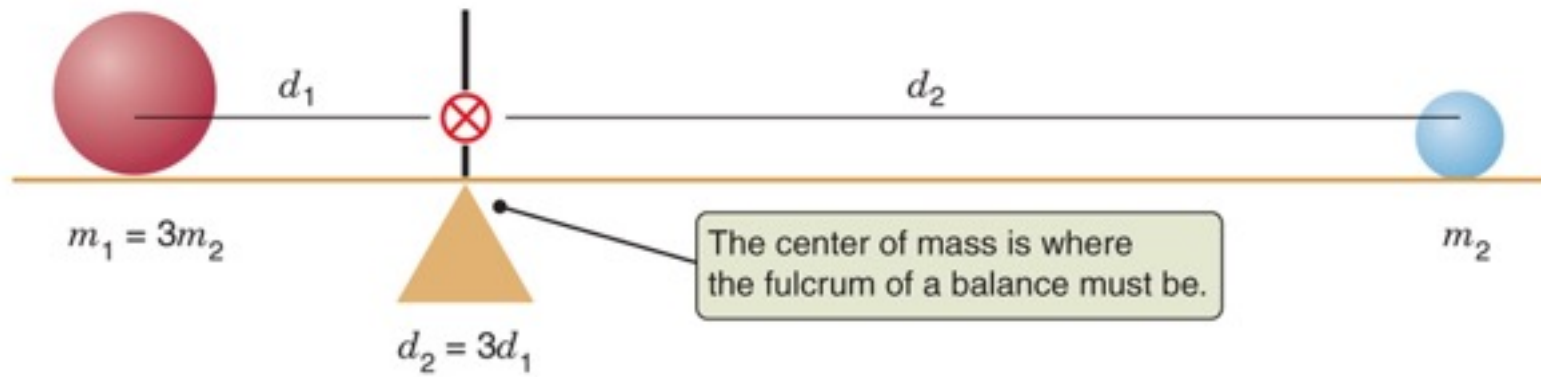


$10^{6-7}$  yrs;  $1-100$  AU;  $100-3000$  K



$10^{7-9}$  yrs;  $1-100$  AU;  $200-3000$  K

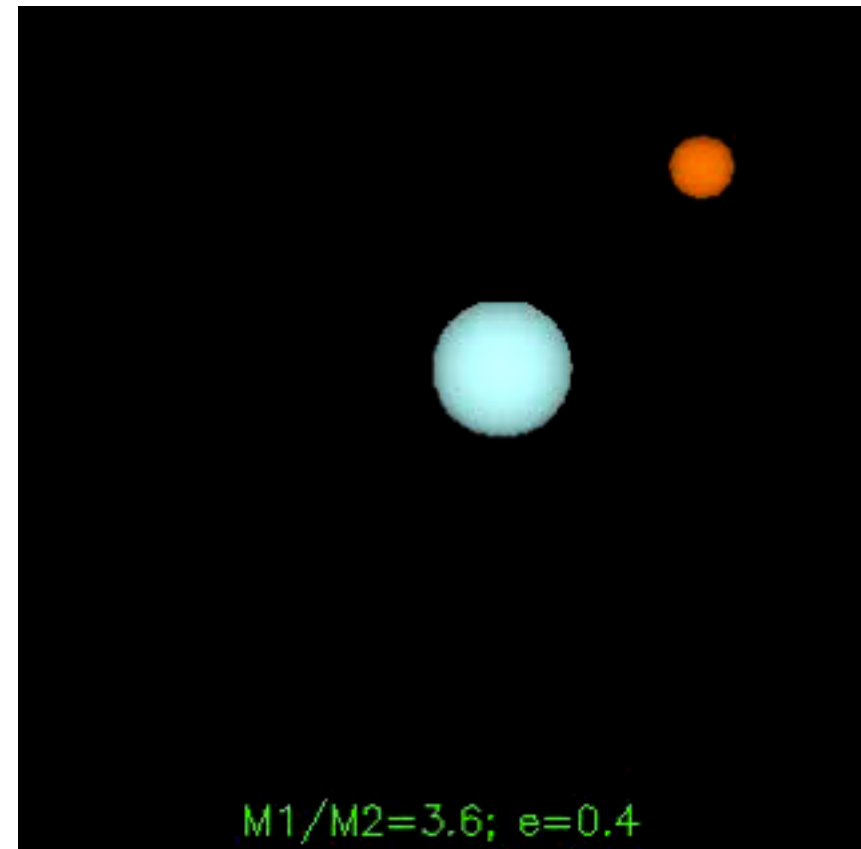
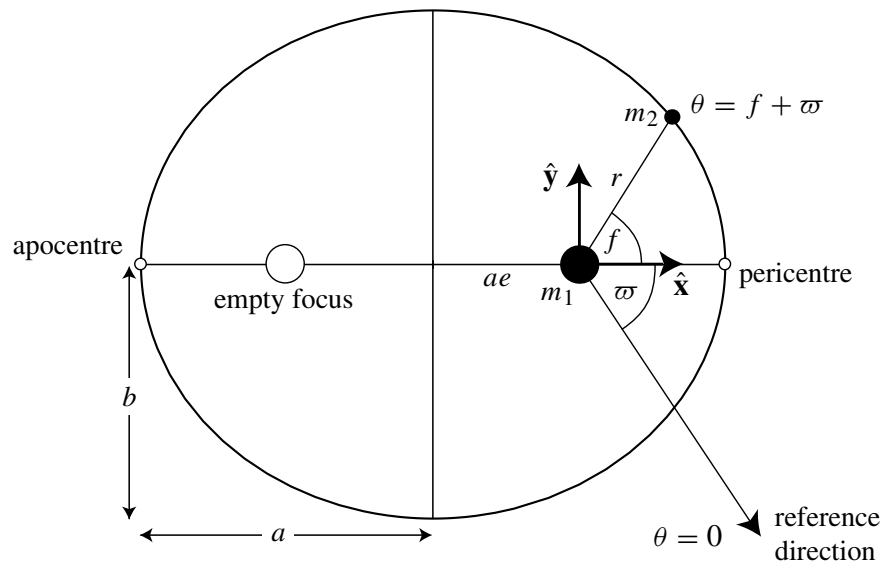
An end-to-end model for planet formation is still out of reach. We can make progress by trying to model orbital evolution and dynamics

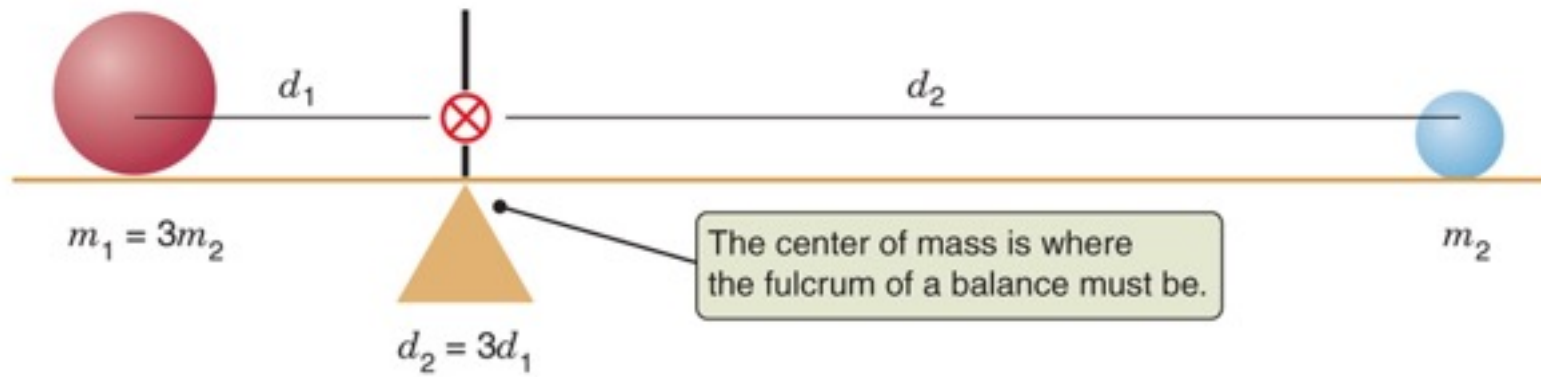


## The two-body problem

There exists an **analytic orbital solution** for any two massive bodies.

Given the positions and velocities at any instant in time, we know the future (and past) behavior

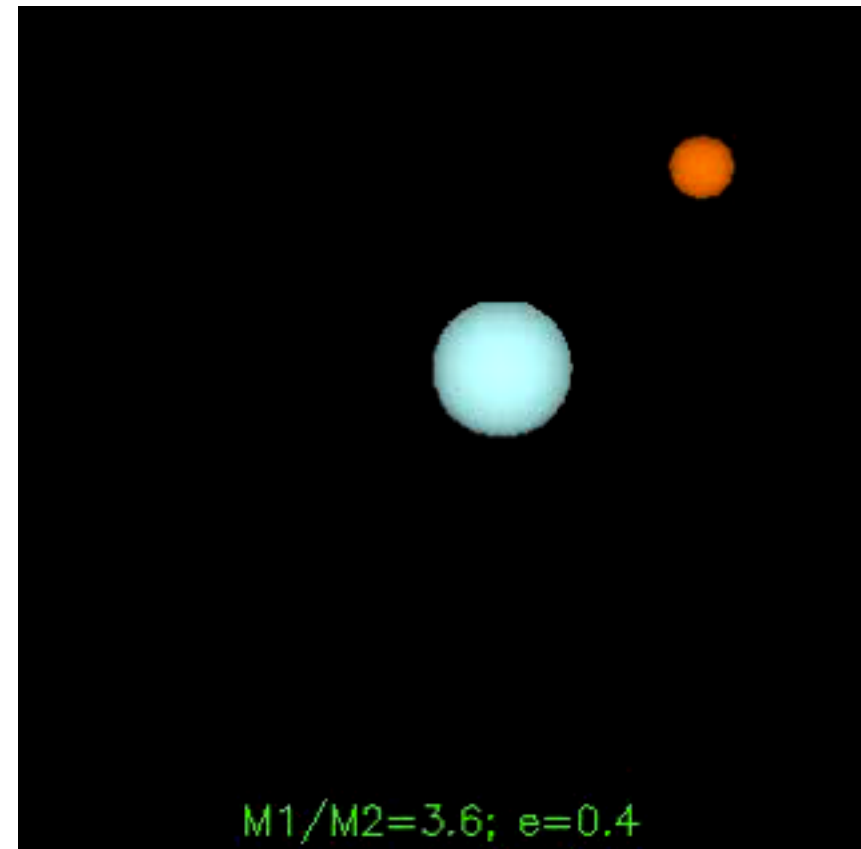
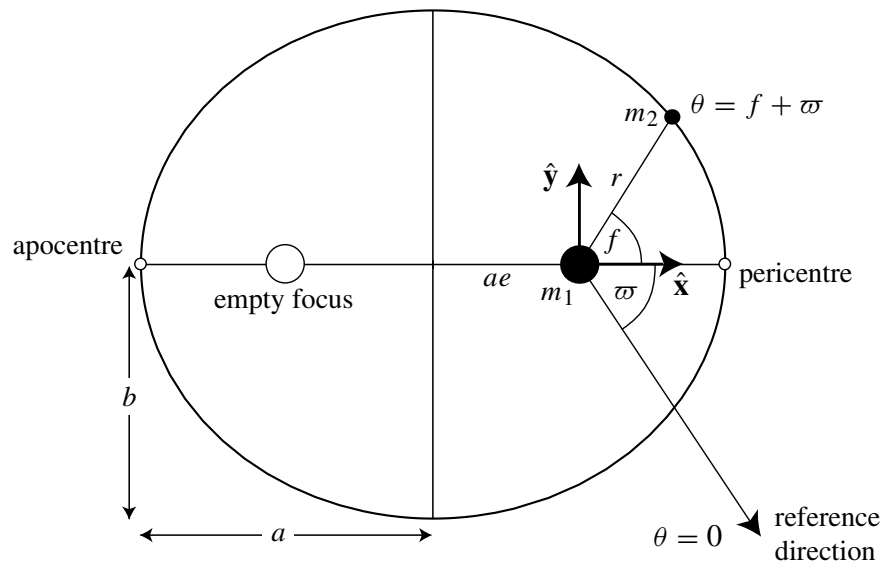




## The two-body problem

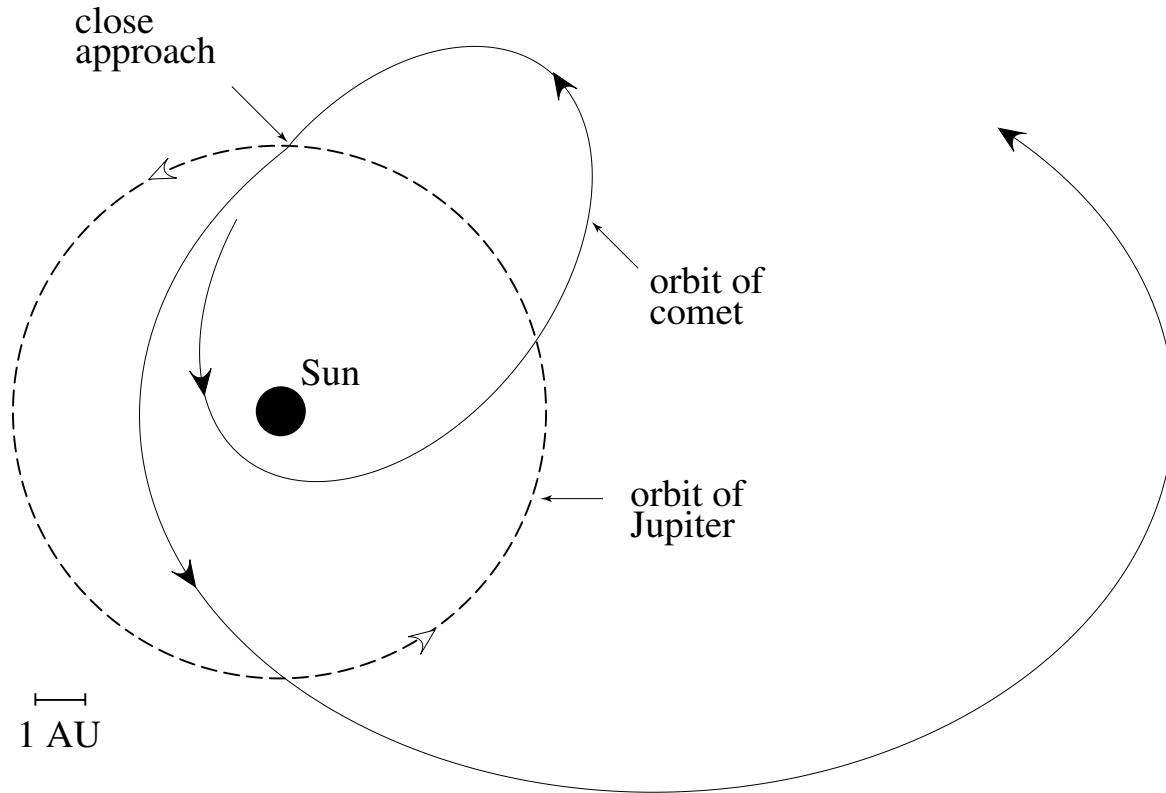
There exists an **analytic orbital solution** for any two massive bodies.

Given the positions and velocities at any instant in time, we know the future (and past) behavior



# Next step up: the restricted three body problem

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- Three bodies, but we only count the mass of two. The third is a so-called “test particle”
- Like the two body problem, we can make some statements about how the objects orbit each other with a few simple equations
- Classic example is the **Sun**, **Jupiter** and an **asteroid**, moon, or comet

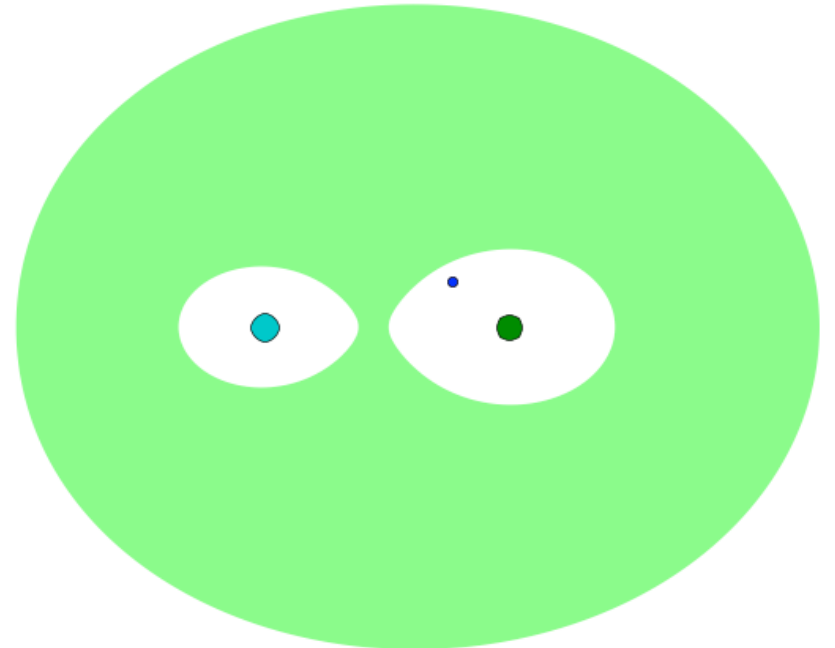
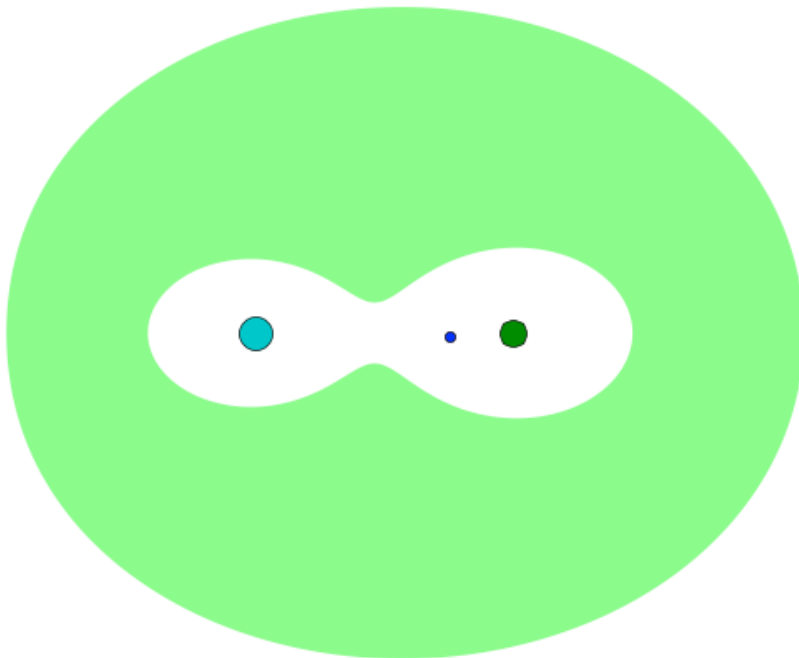
# The circular restricted 3-body problem

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$$\begin{bmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} \end{bmatrix} = \begin{bmatrix} x + 2\dot{y} - \frac{1-\mu}{r_1^3}[x + \mu] - \frac{\mu}{r_2^3}[x - (1-\mu)] \\ y - 2\dot{x} - \frac{1-\mu}{r_1^3}y - \frac{\mu}{r_2^3}y \\ -\frac{1-\mu}{r_1^3}z - \frac{\mu}{r_2^3}z \end{bmatrix}$$

$$r_1 = \sqrt{(x + \mu)^2 + y^2 + z^2} \quad r_2 = \sqrt{(x - (1 - \mu))^2 + y^2 + z^2}$$

$$C_J = n^2(x^2 + y^2) + 2\left(\frac{\mu_1}{r_1} + \frac{\mu_2}{r_2}\right) - (\dot{x}^2 + \dot{y}^2 + \dot{z}^2)$$





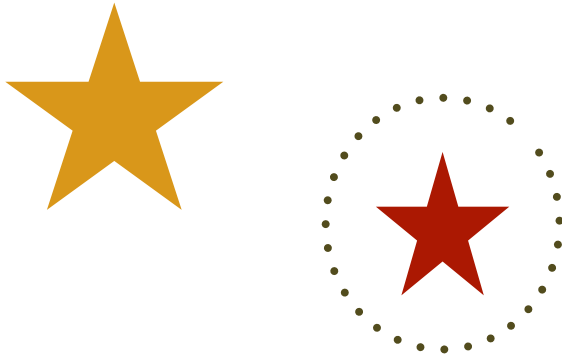
Credit: Zarmeen Shahzad

Many stars are in pairs  
(or triples!)

Planets are found at a  
range of distances and  
masses in these systems

# A modern example, planets in binaries

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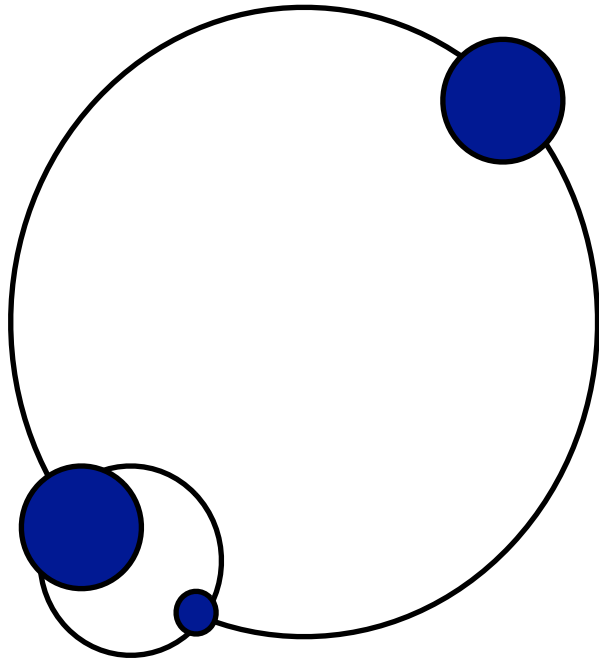
Satellite-Type

Planetary-Type  
“Tatooines”

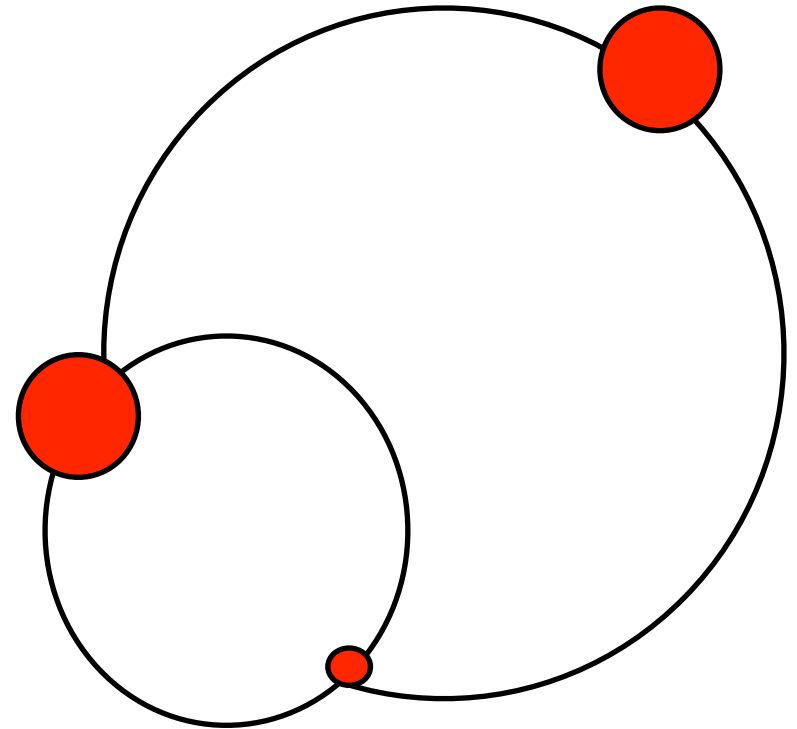


# Planet stability requires well separated orbits

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$$a_{\text{in}} \ll a_{\text{out}}$$

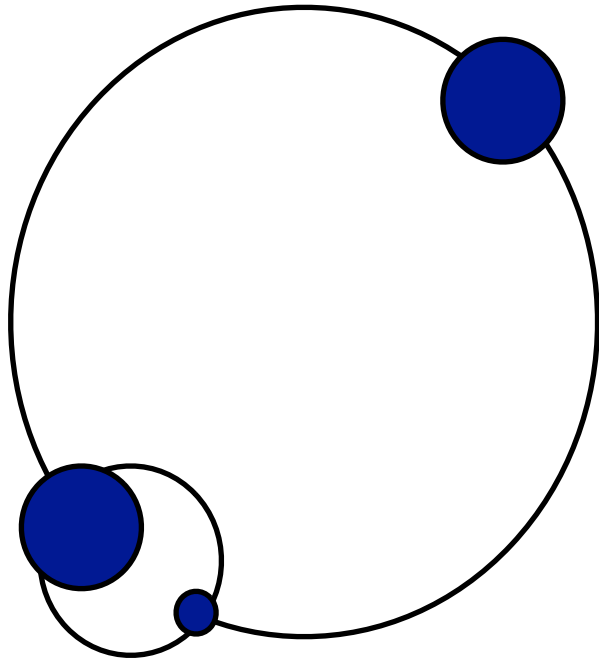


$$a_{\text{in}} \leq a_{\text{out}}$$

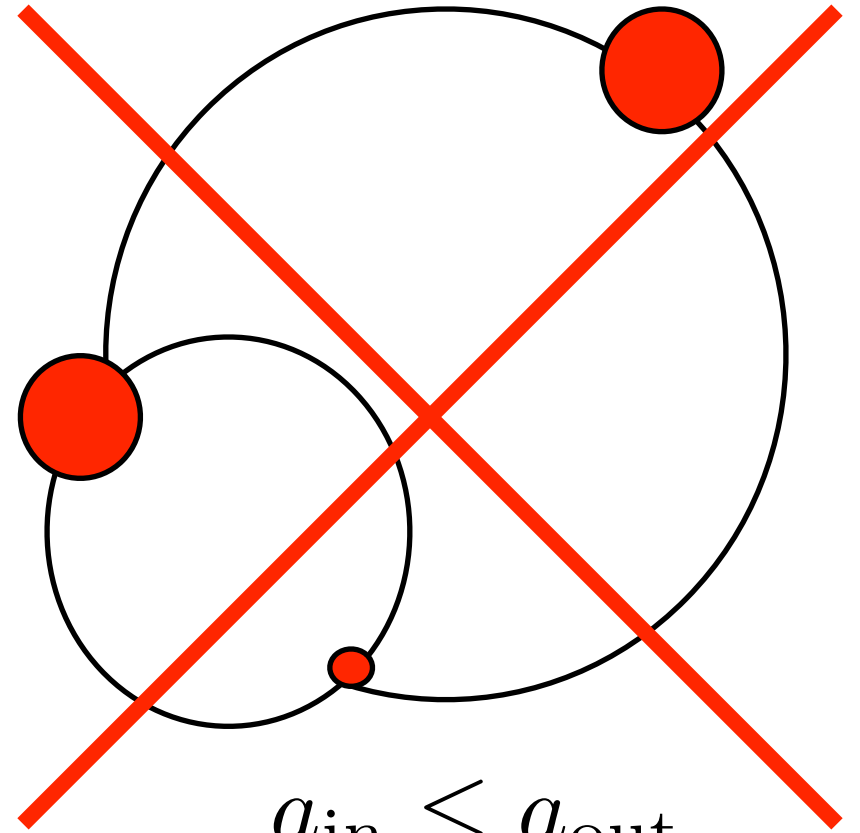


# Planet stability requires well separated orbits

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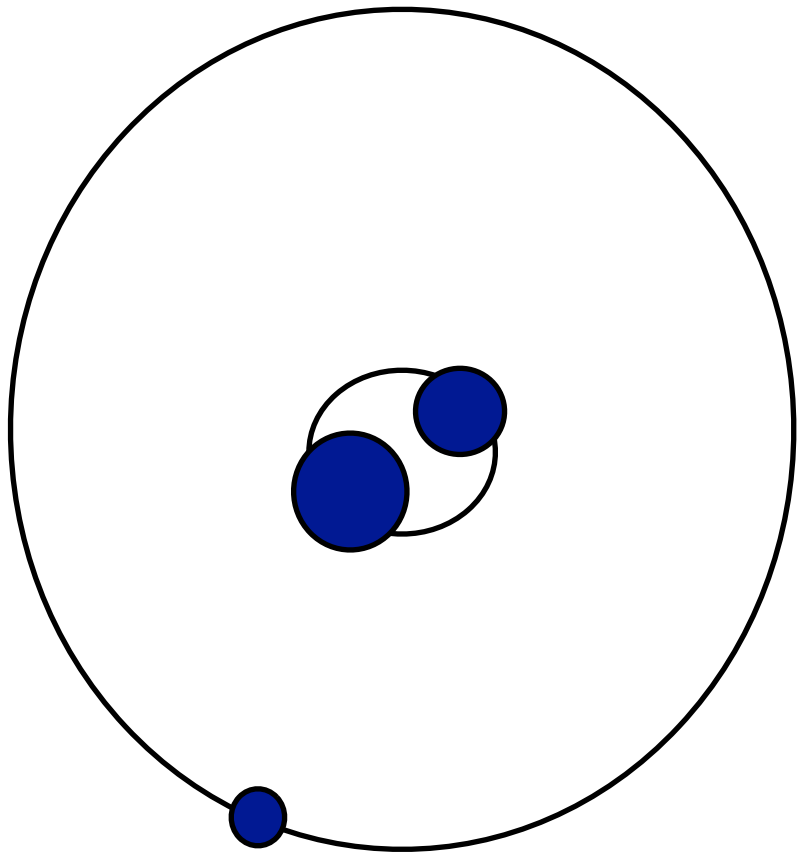
$$a_{in} \ll a_{out}$$



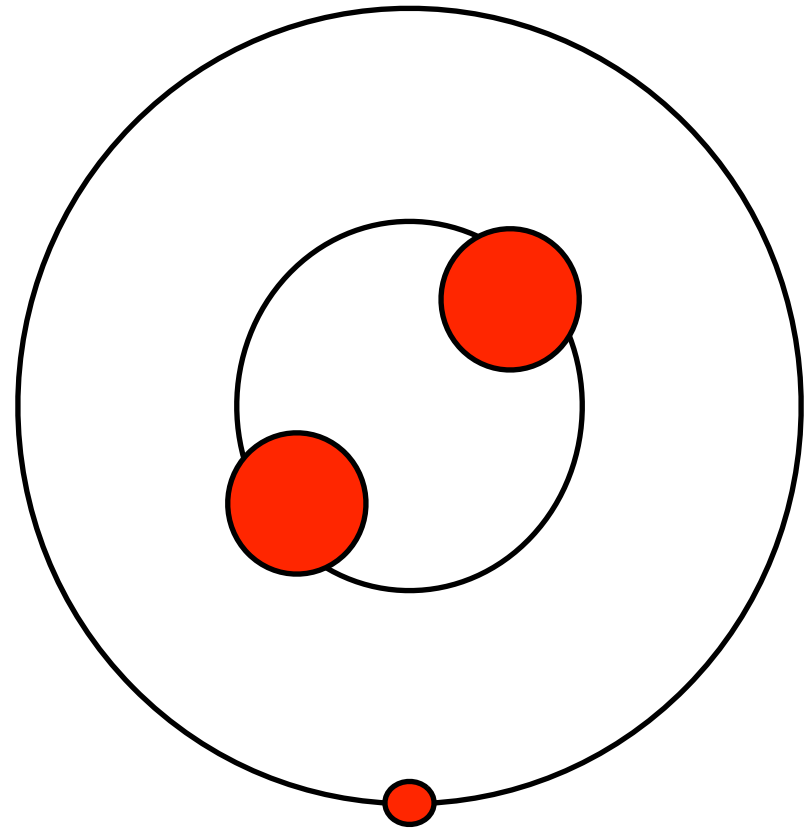
$$a_{in} \leq a_{out}$$

# Planet stability requires well separated orbits

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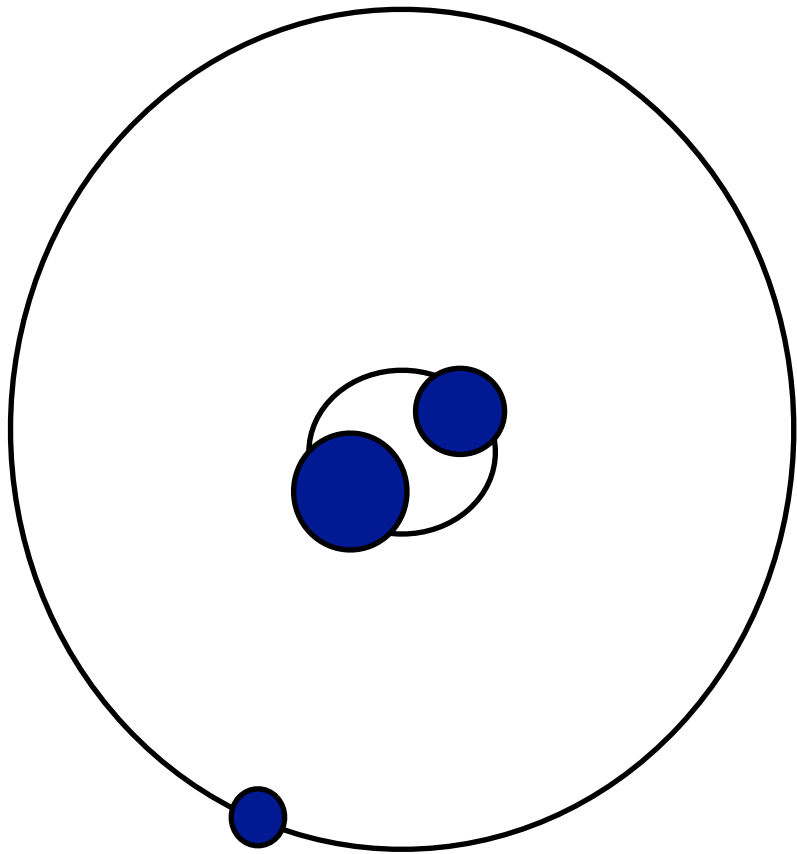
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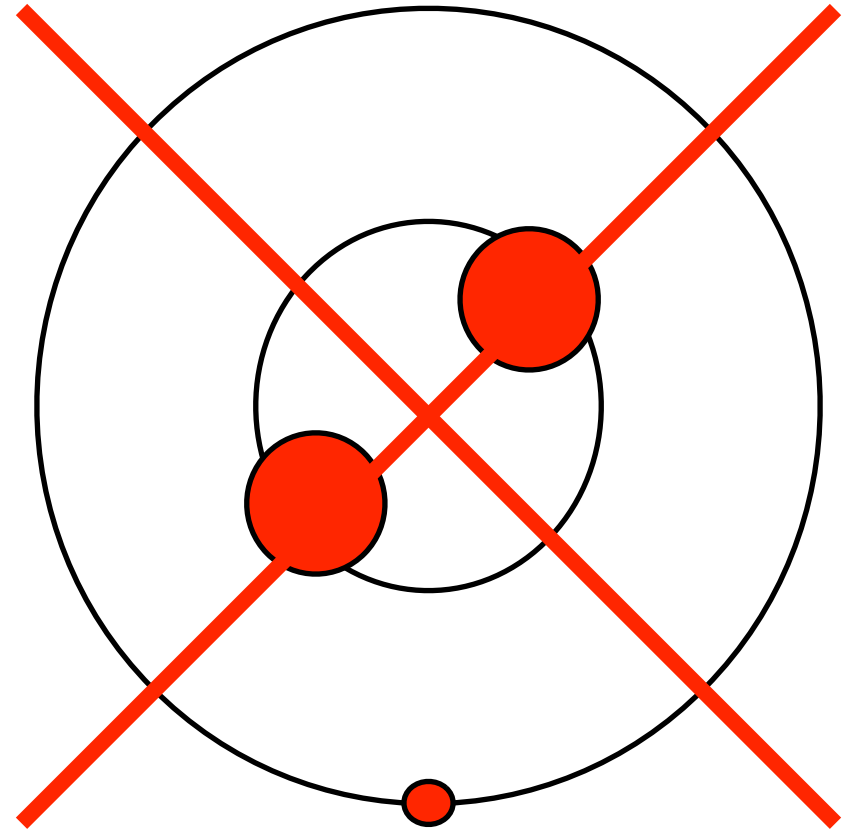
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# Planet stability requires well separated orbits

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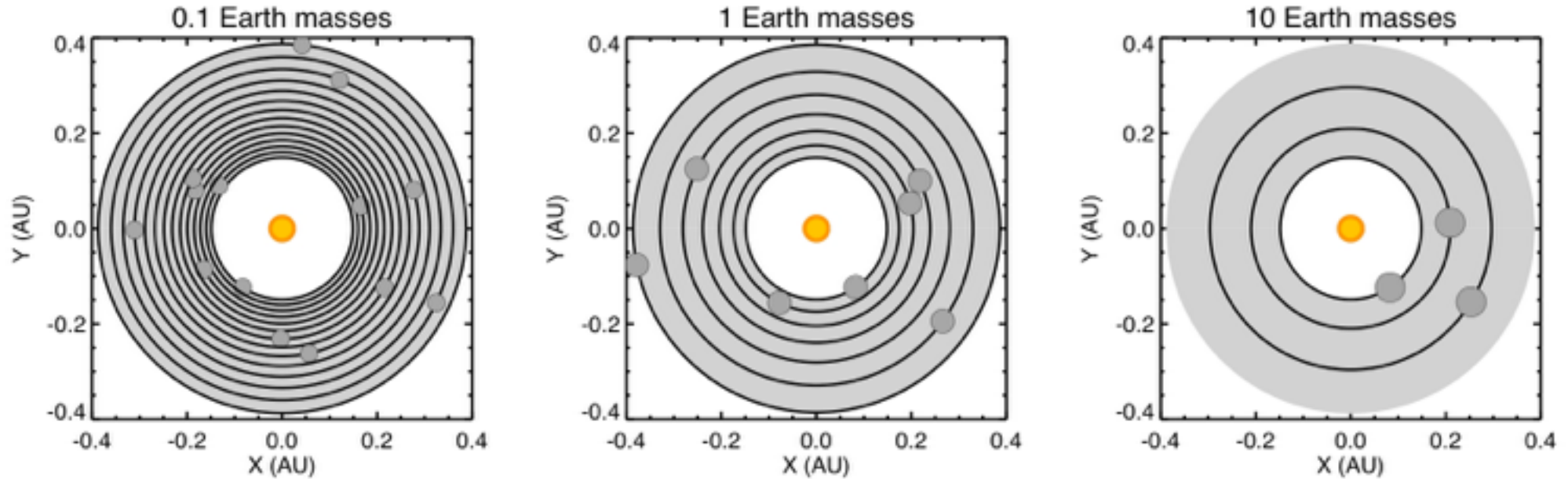
$$a_{\text{in}} \ll a_{\text{out}}$$



$$a_{\text{in}} \leq a_{\text{out}}$$

# Stability is an issue even in systems with only 1 sun

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- Minimum planet spacing depends on distance from the sun and planet mass.
- More massive, or more tightly packed planets exert stronger gravitational tugs on each other, readily causing instabilities
- When they are closer to the star, its gravity dominates more, making the planet tugs less important

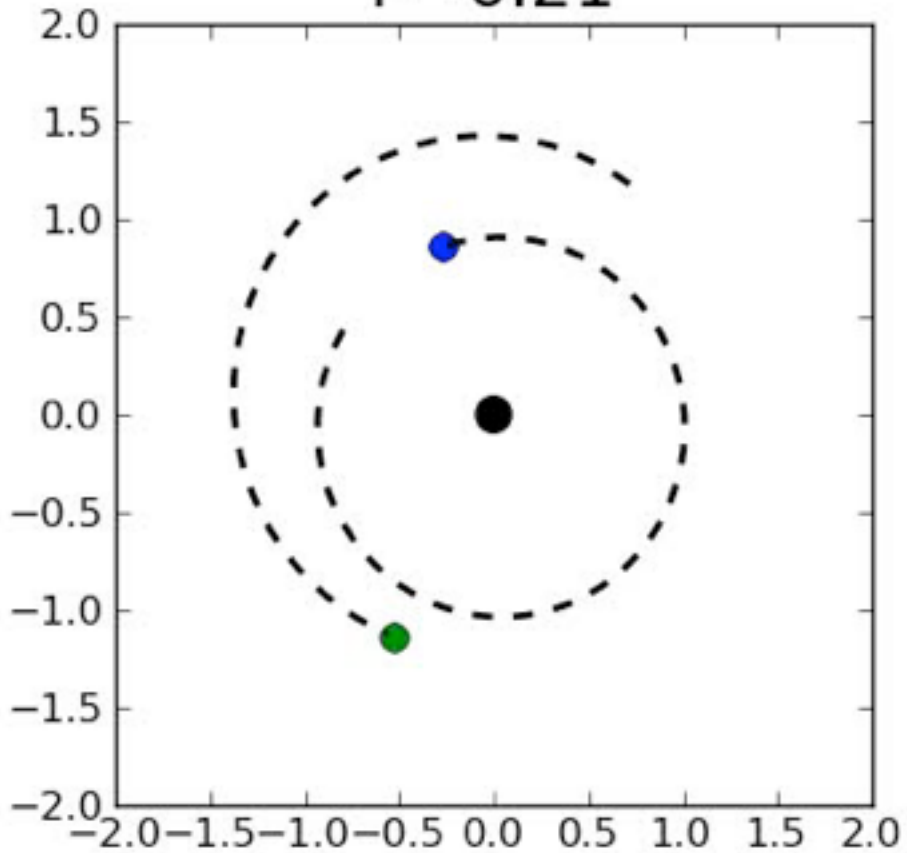
# Chaos vs Stability?

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System 1:

1.0 AU, 1.067 AU

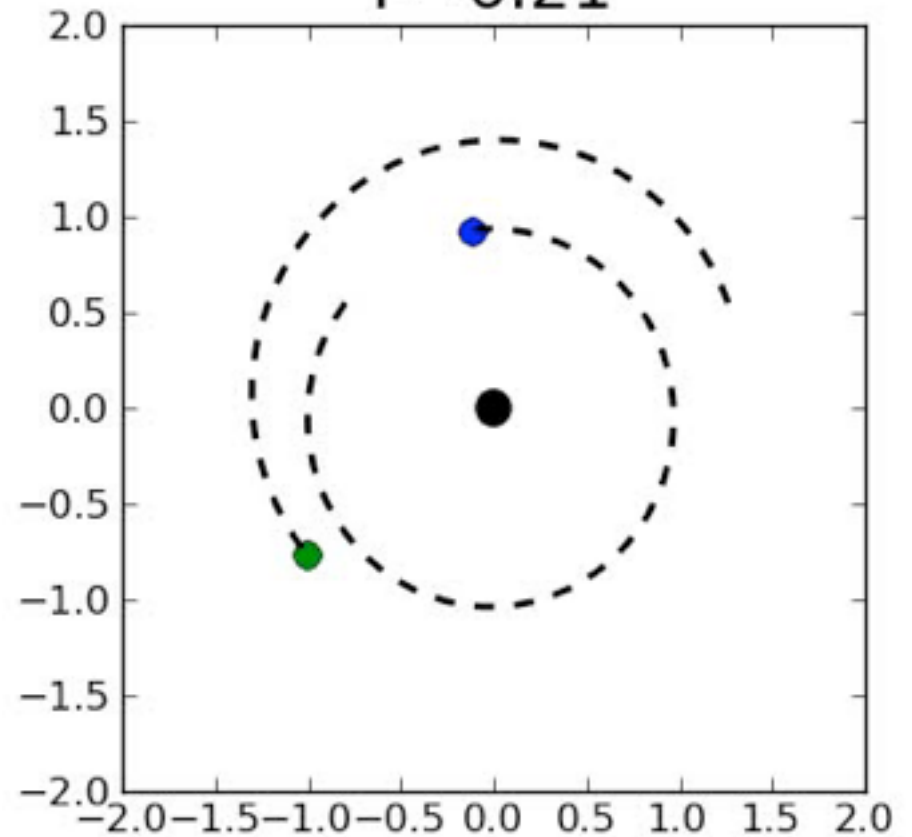
$P=6.21$



System 2:

1.0 AU, 1.073 AU

$P=6.21$



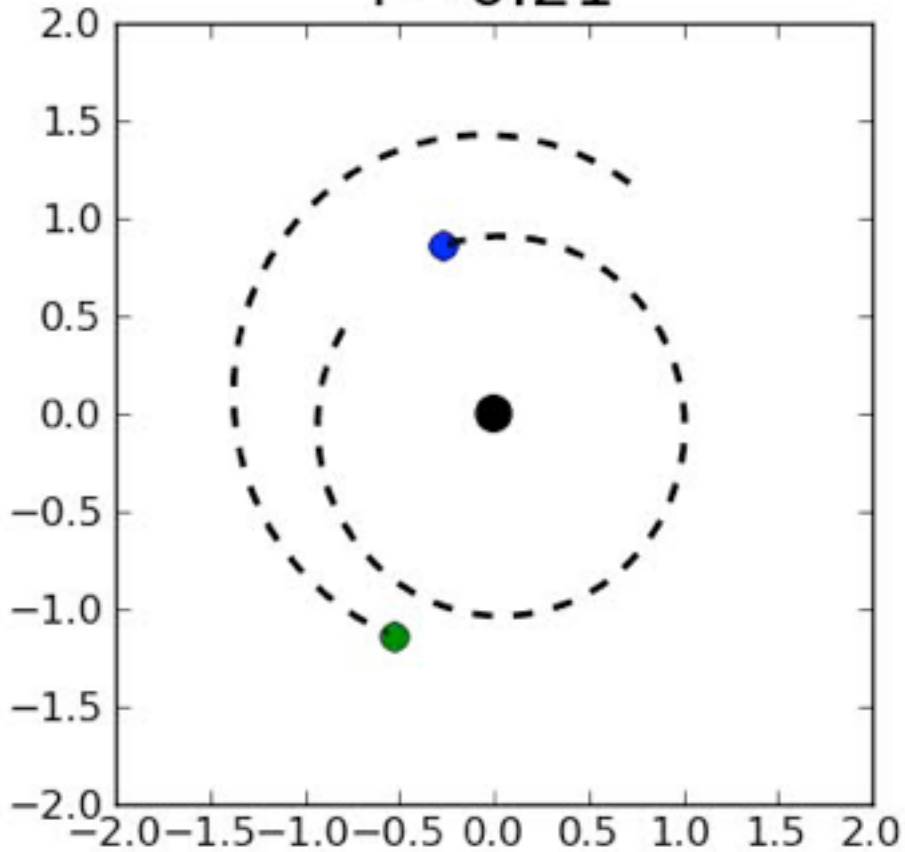
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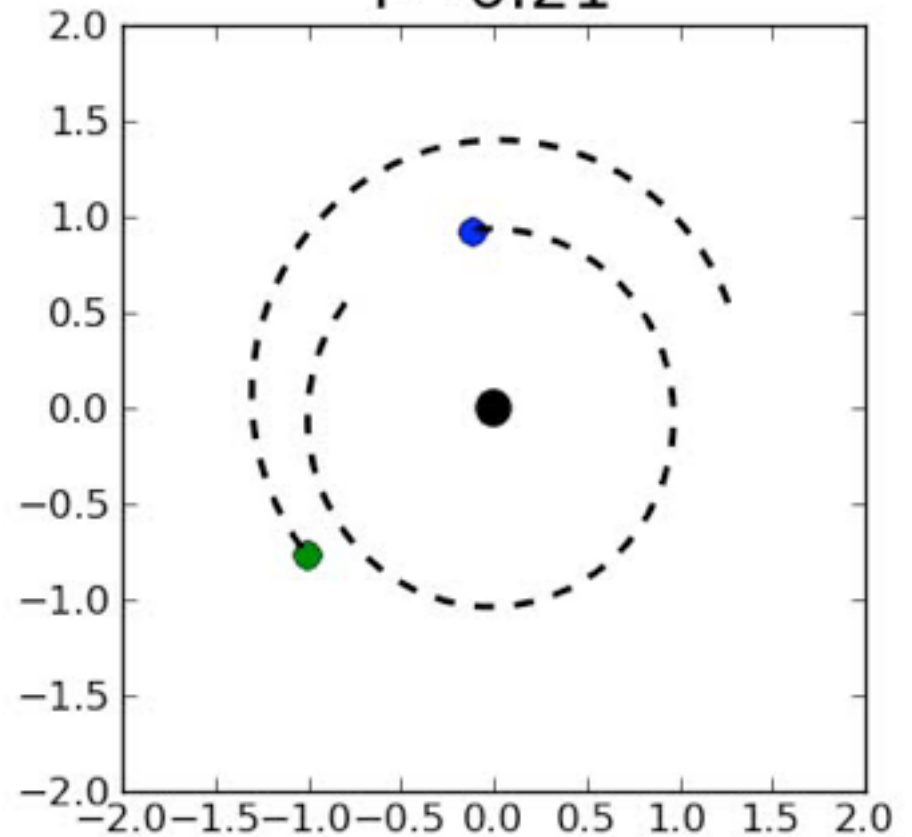
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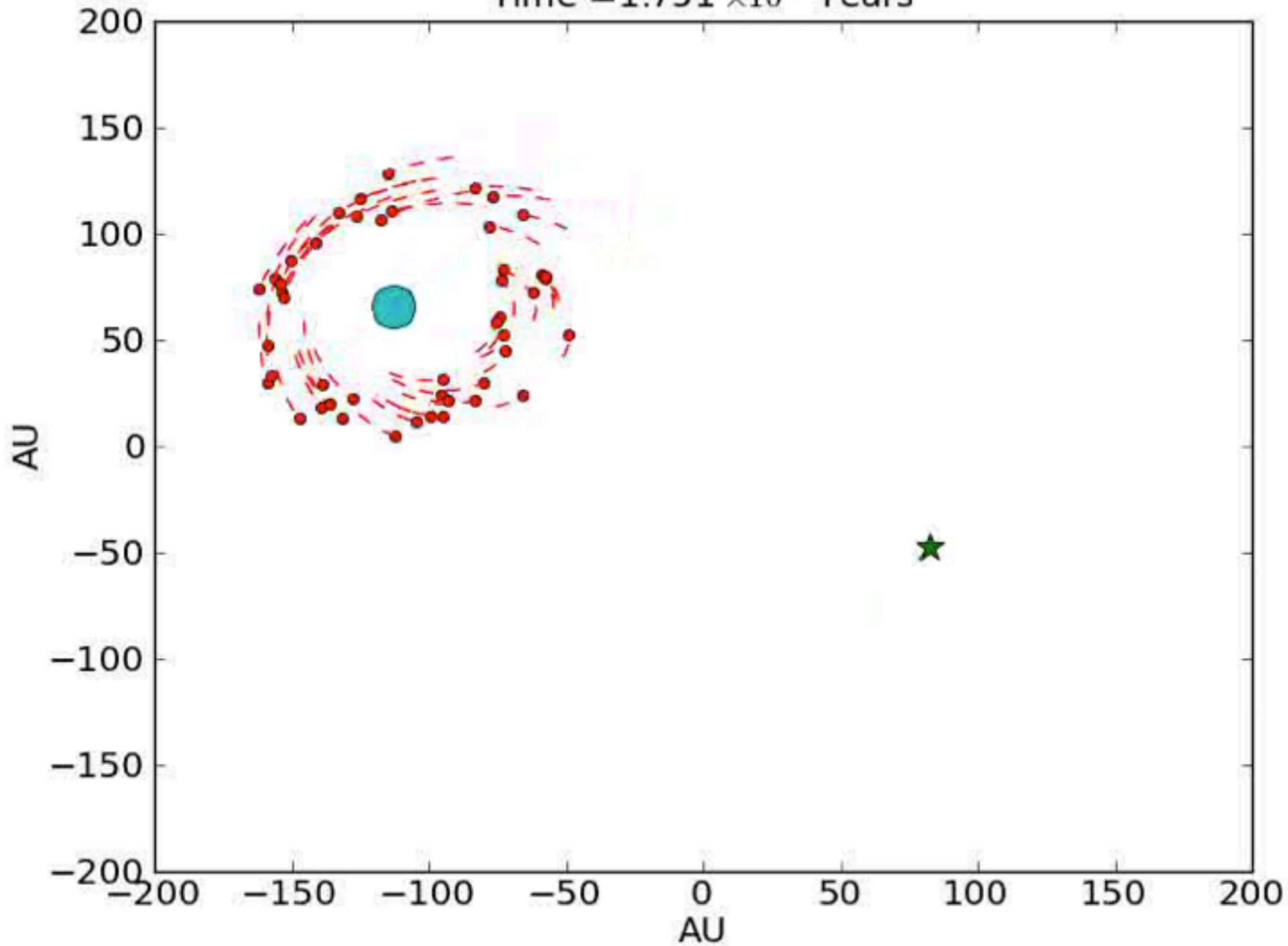
System 2:

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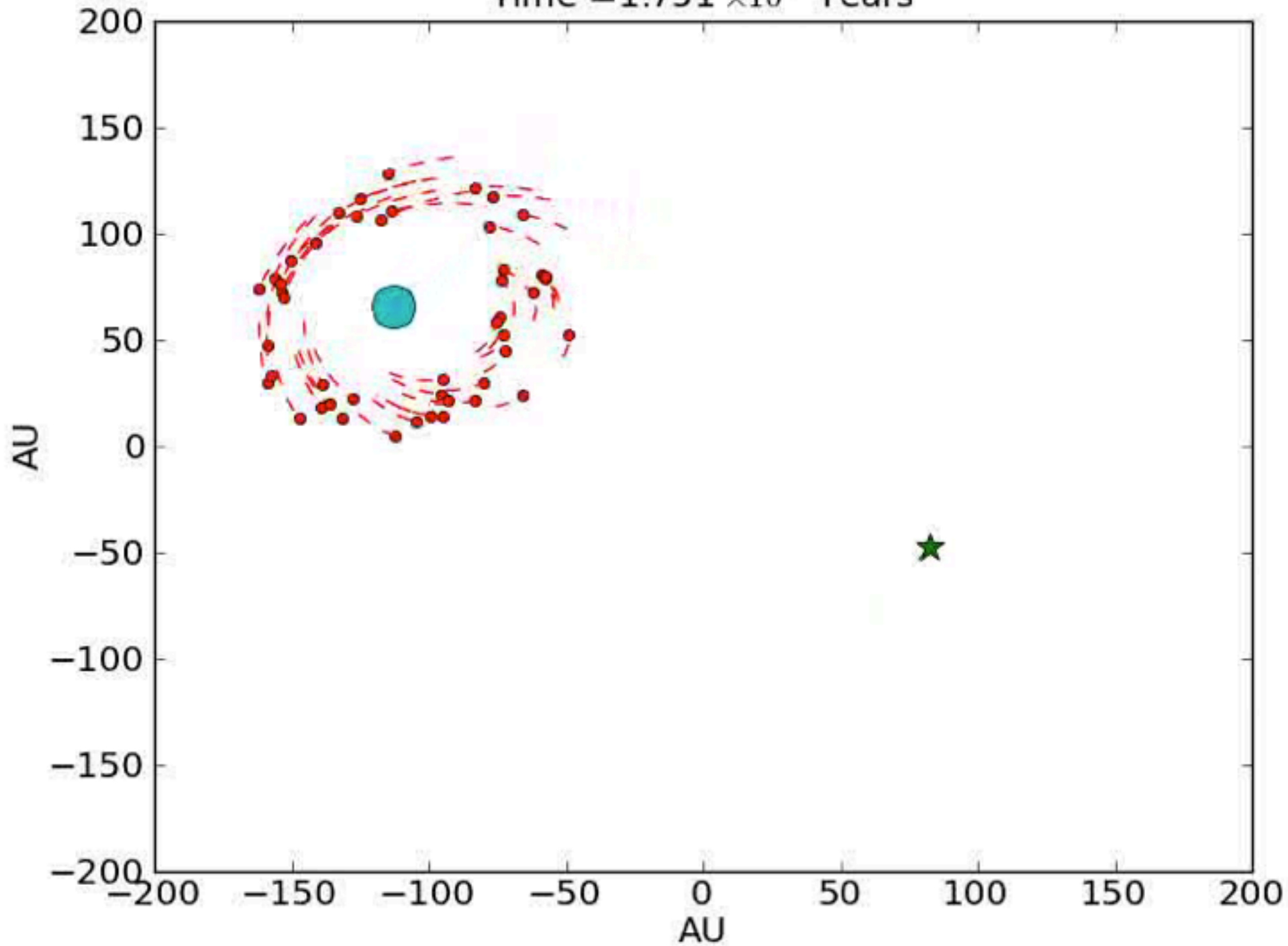
$P=6.21$



Time =  $1.751 \times 10^6$  Years

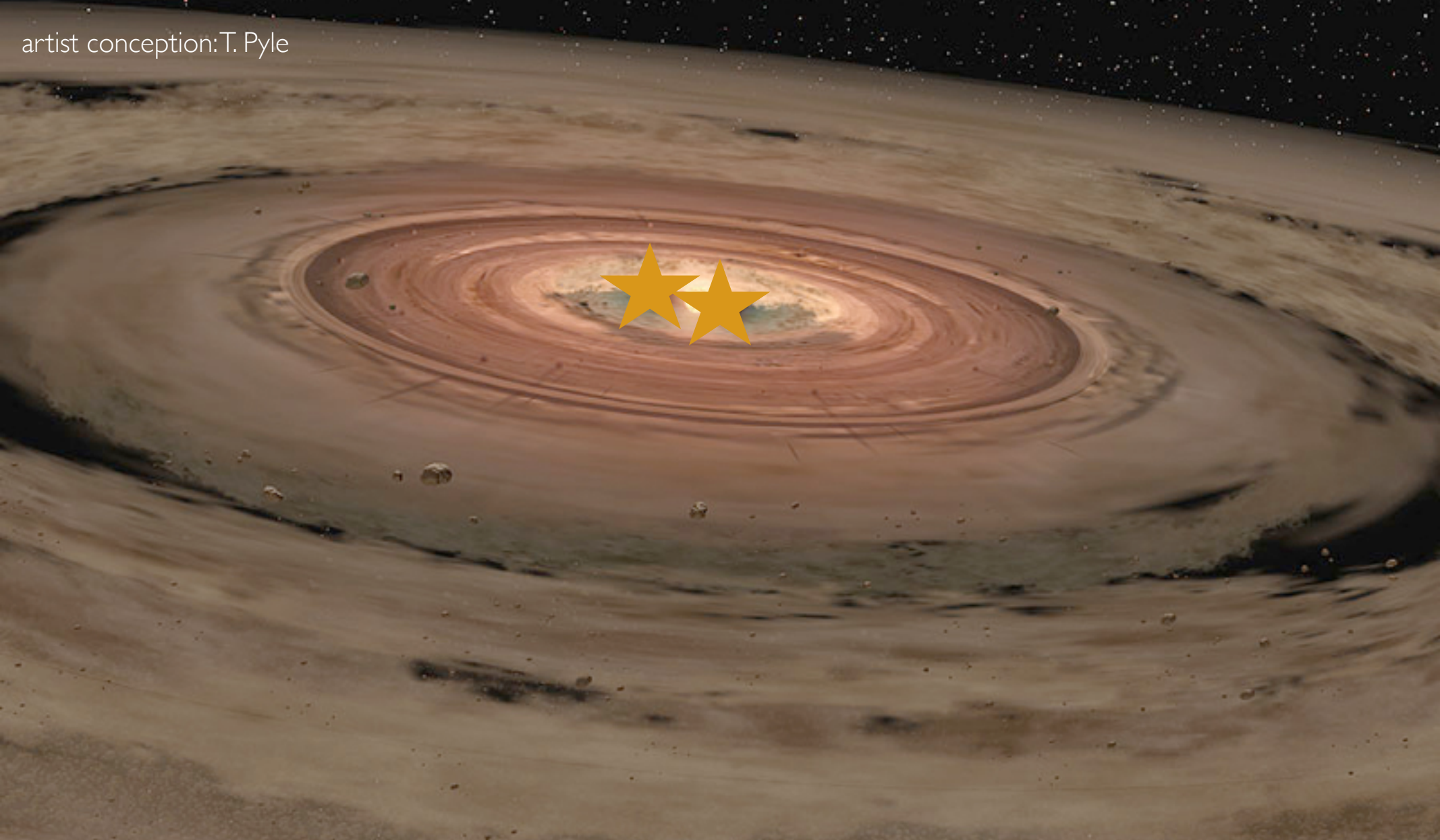


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artist conception:T. Pyle



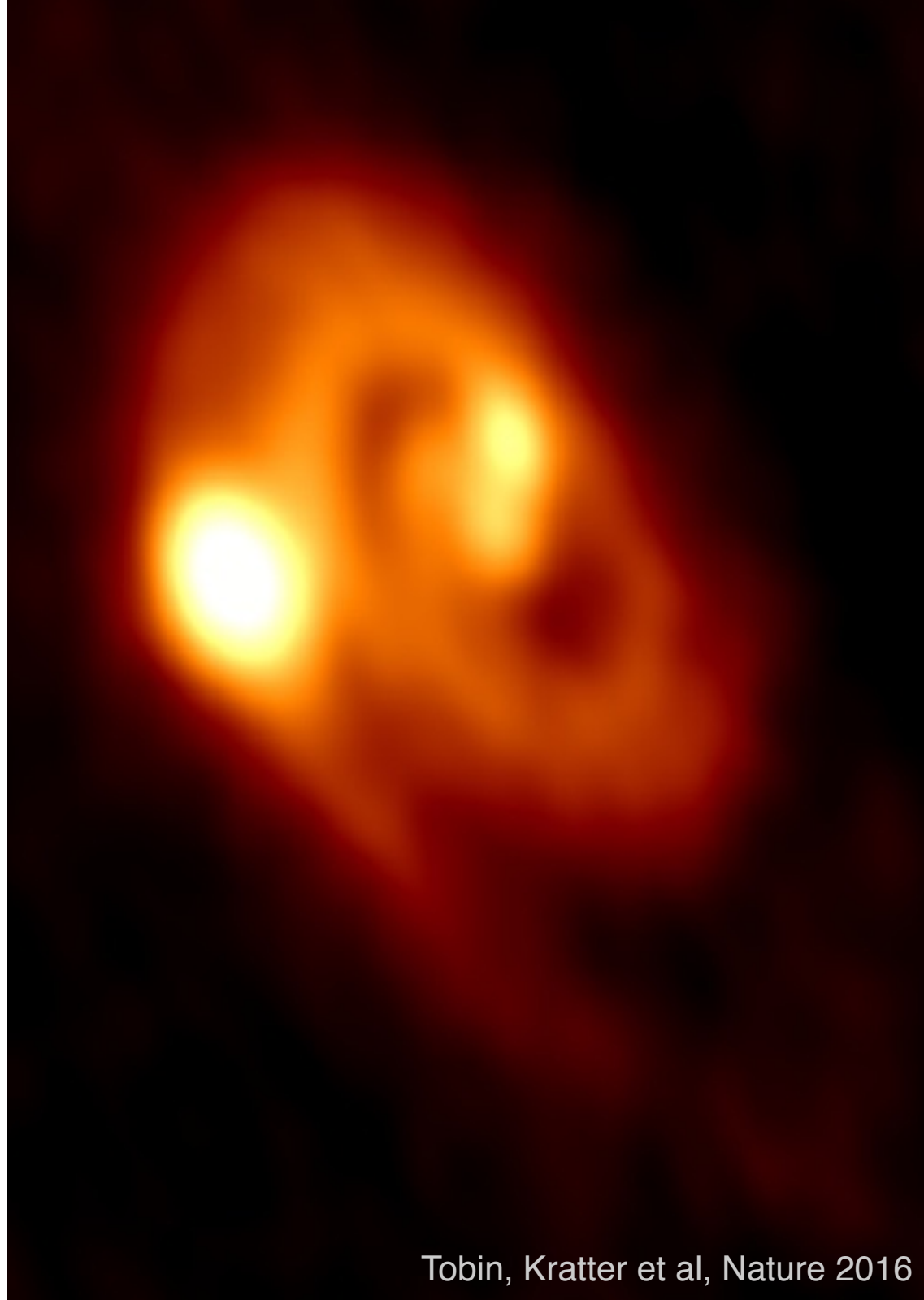
Why study planets  
in binaries?

We learn about the stars  
and planets!

# The Planet Clock!

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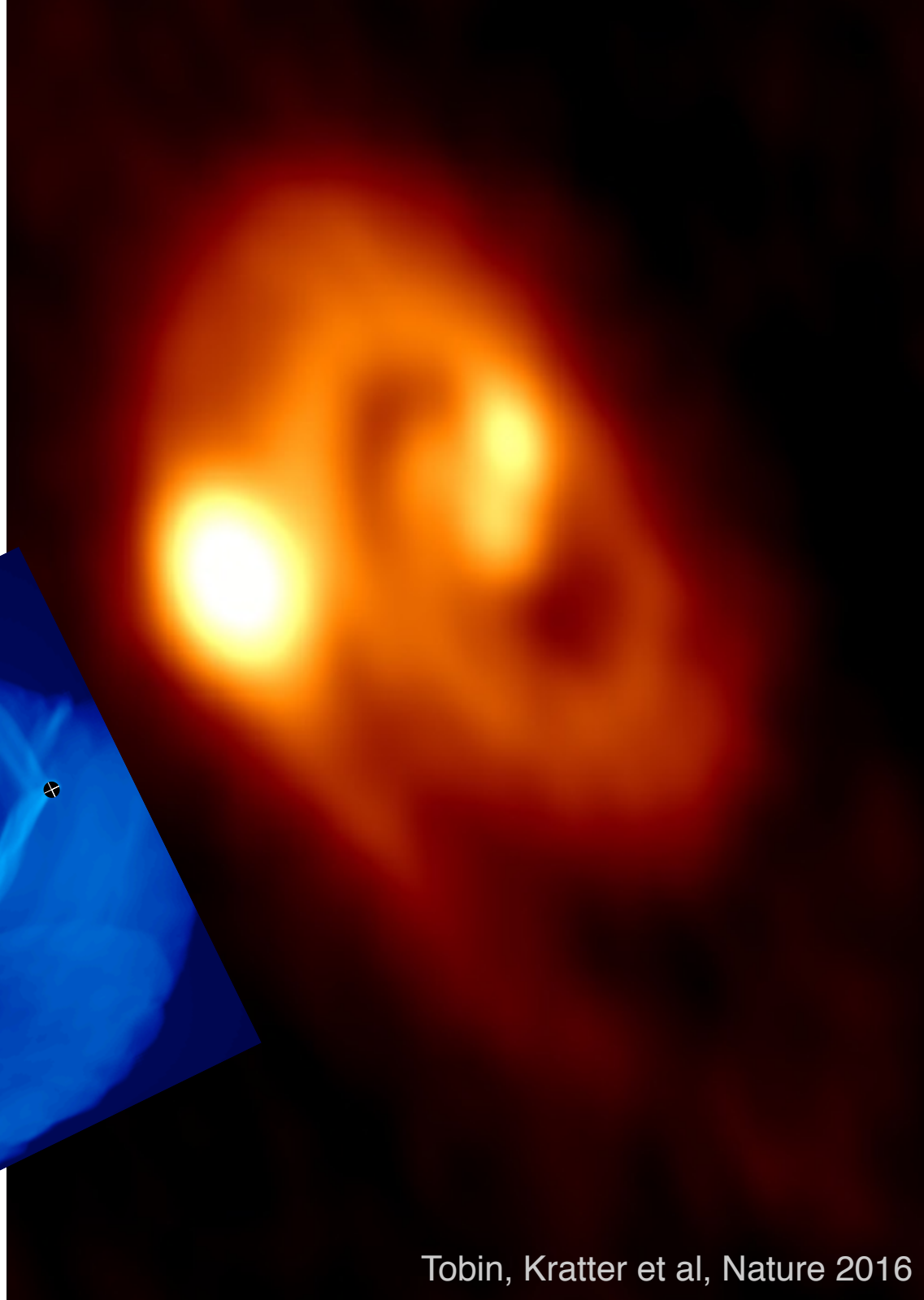
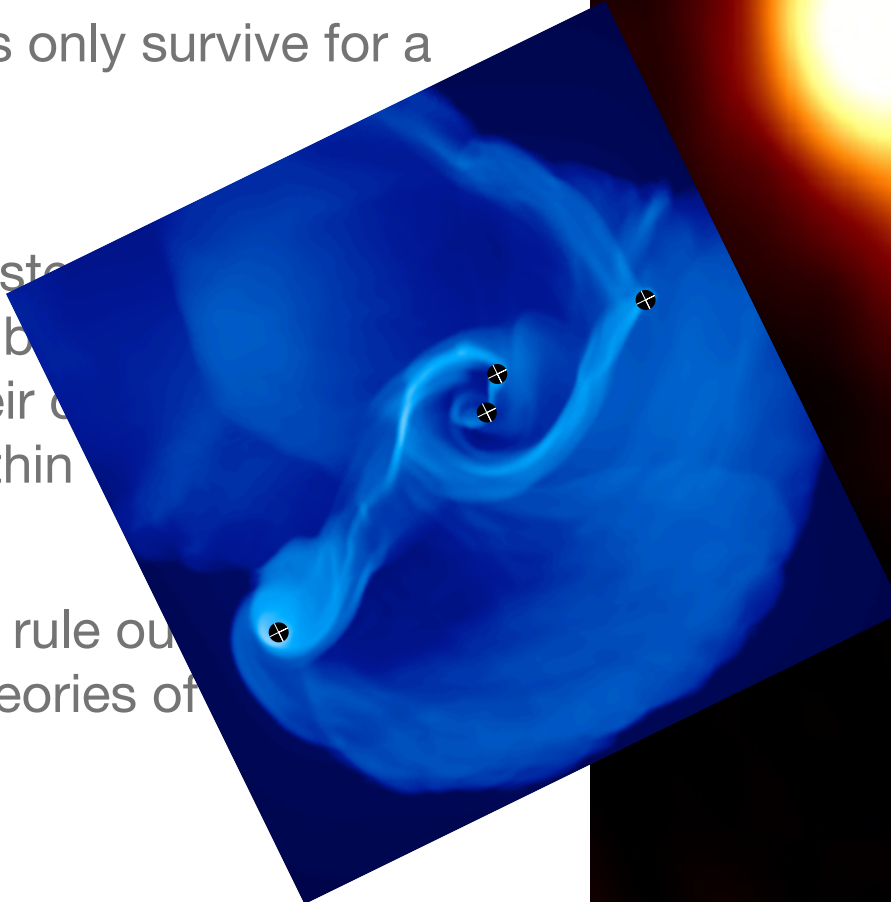
- Planets form in the disks of gas and dust out of which stars are born
- These disks only survive for a few Myr
- Tatooine systems tell us that at least some binary stars must assume their current system position within  $\sim$ Myr
- This lets us rule out many previous theories of binary formation!



# The Planet Clock!

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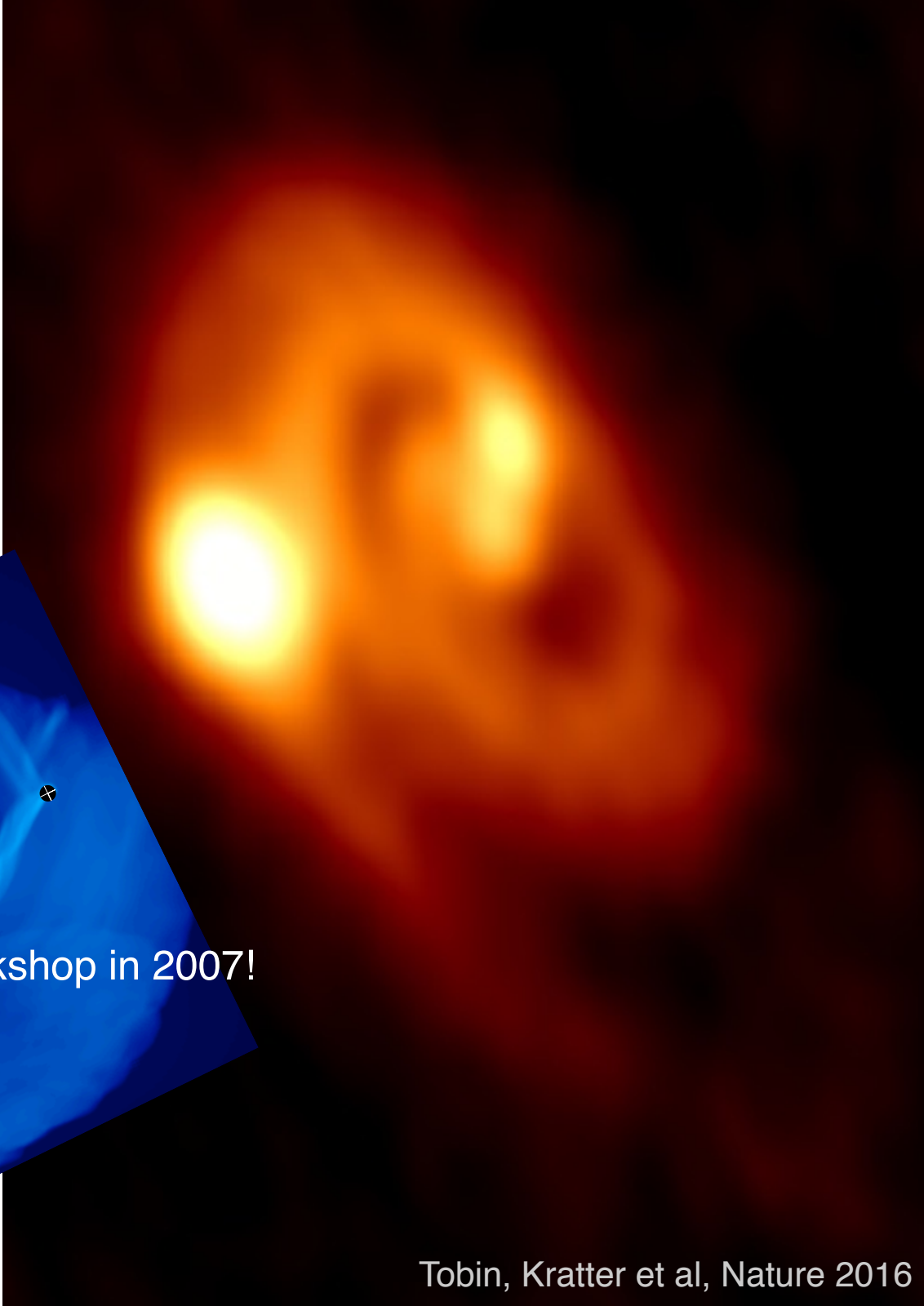


# The Planet Clock!

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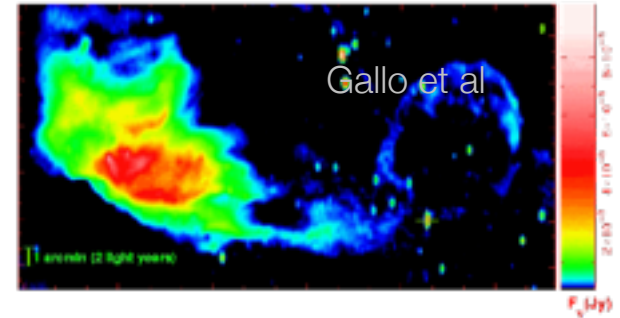
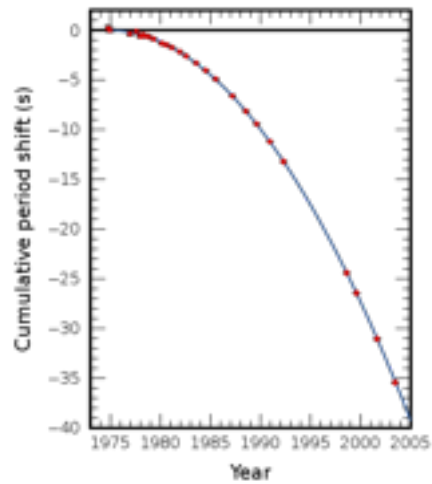
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Started at KITP workshop in 2007!



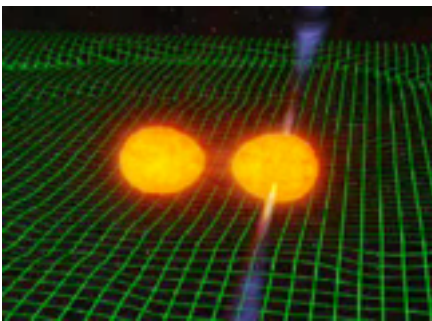
# Binaries are fundamental to all of astrophysics

Type Ia supernovae / dark energy



Confirmed BH

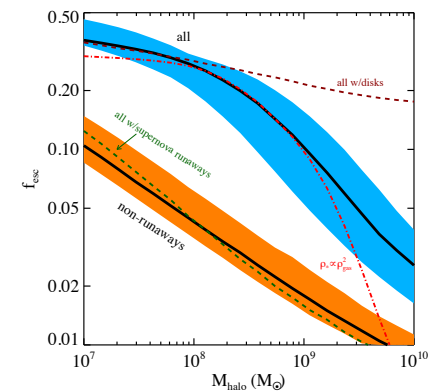
GR confirmation



GW signal



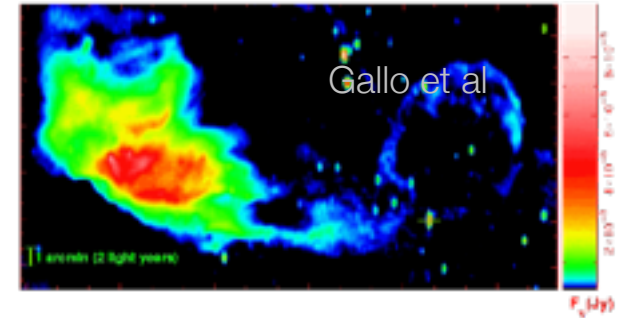
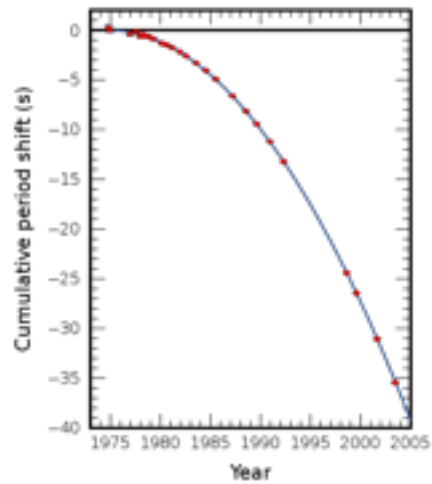
Exoplanet characterization



Reionization

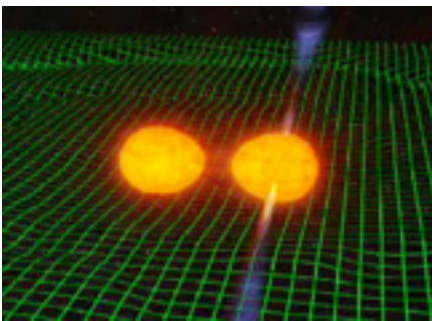
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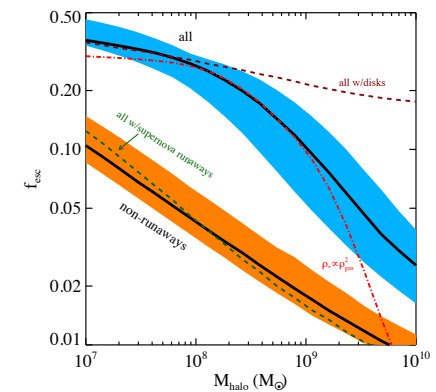
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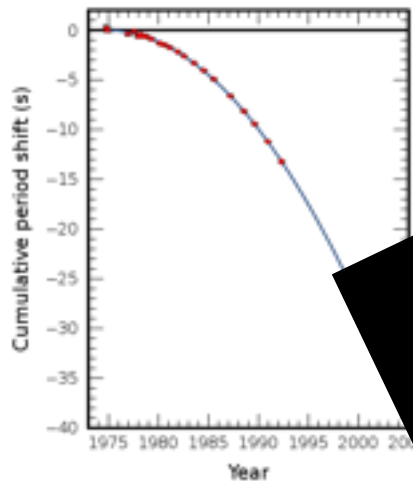


Exoplanet characterization



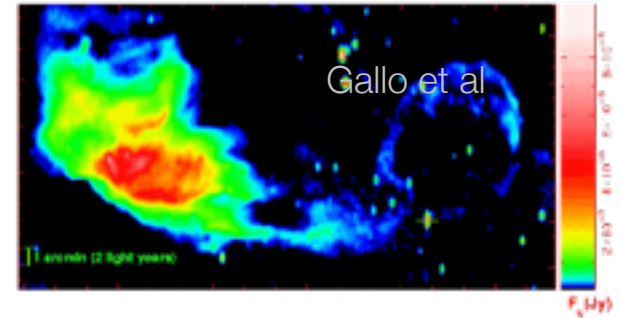
Reionization

# Binaries are fundamental to all of astrophysics



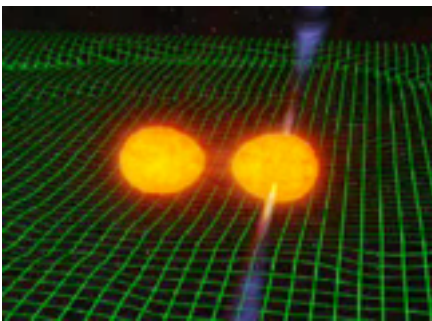
Type Ia supernovae / dark energy

**NOBEL PRIZES!**



Confirmed BH

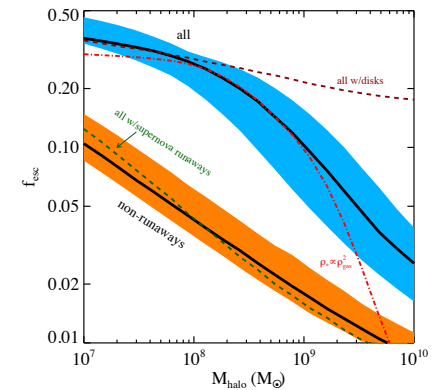
GR confirmation



GW signal

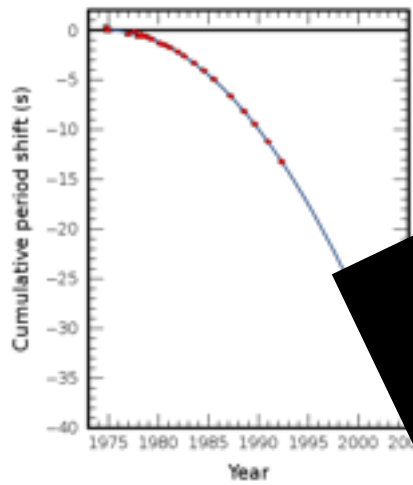


Exoplanet characterization



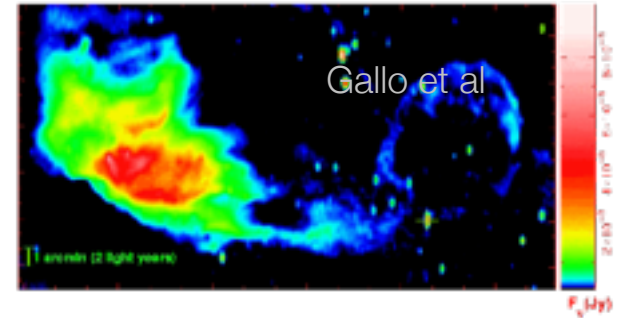
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# Binaries are fundamental to all of astrophysics



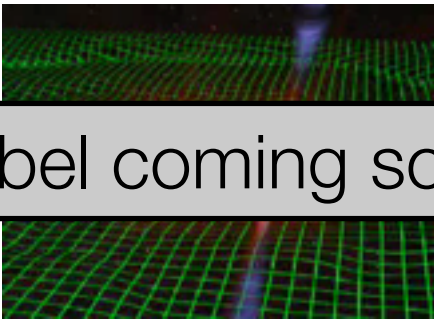
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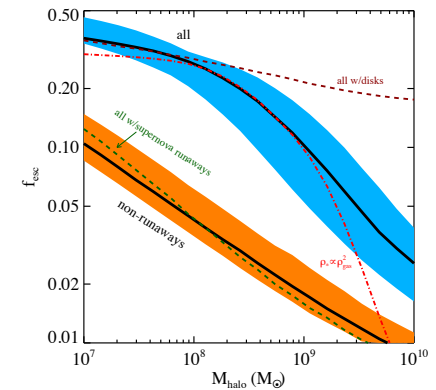
GR confirmation



Nobel coming soon?!



Exoplanet characterization



Reionization

GW signal



# Formation Extremes

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- Planets around binaries are subject to extra kicks and tugs
- The properties of the natal disk can be highly constrained
- Serve as excellent mode to falsify planet formation models

A triple star system containing a super-Jupiter on a nearly unstable orbit

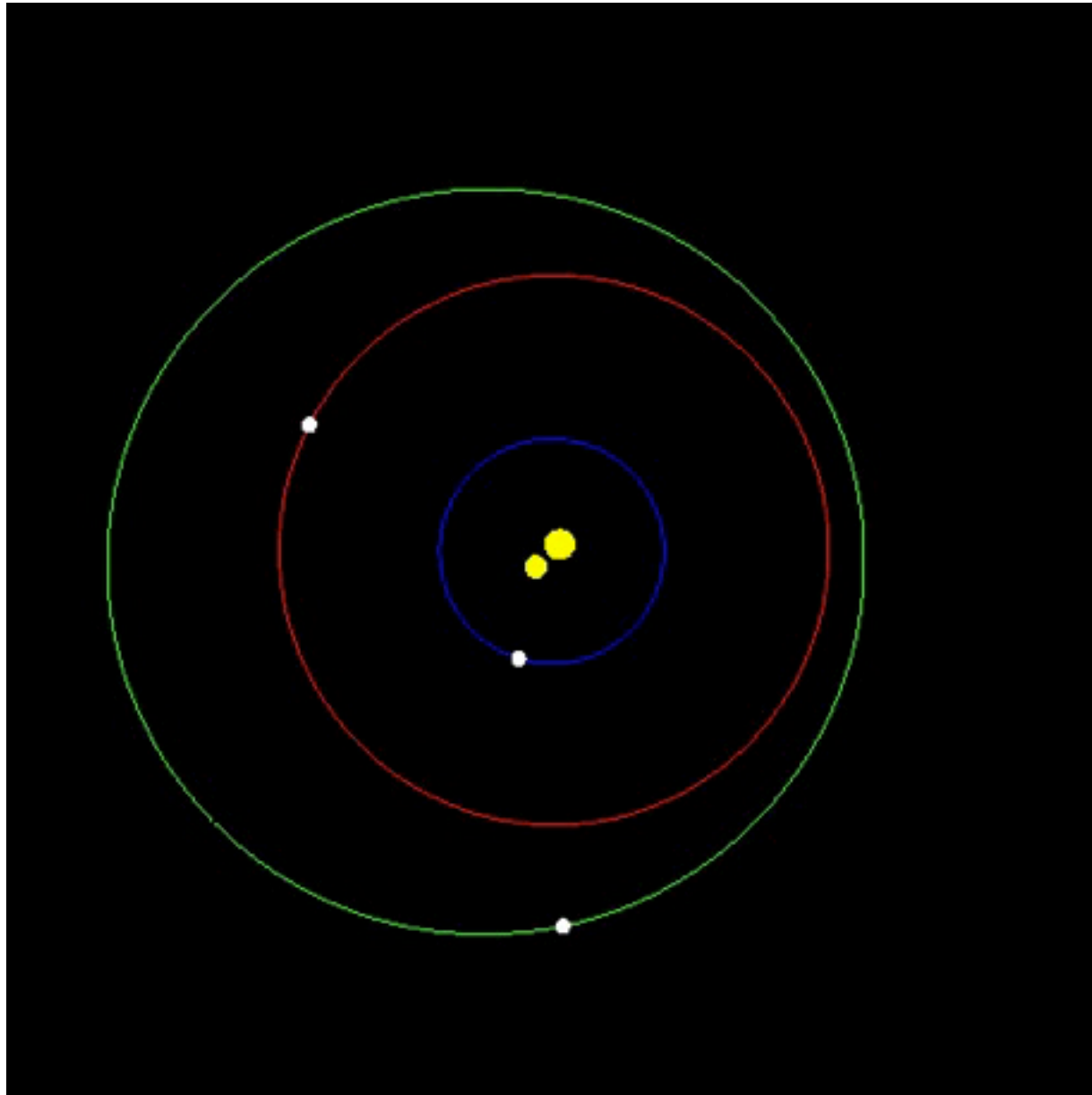
HD 131399

Wagner, Apai, Kasper, Kratter et al, 2016, Science



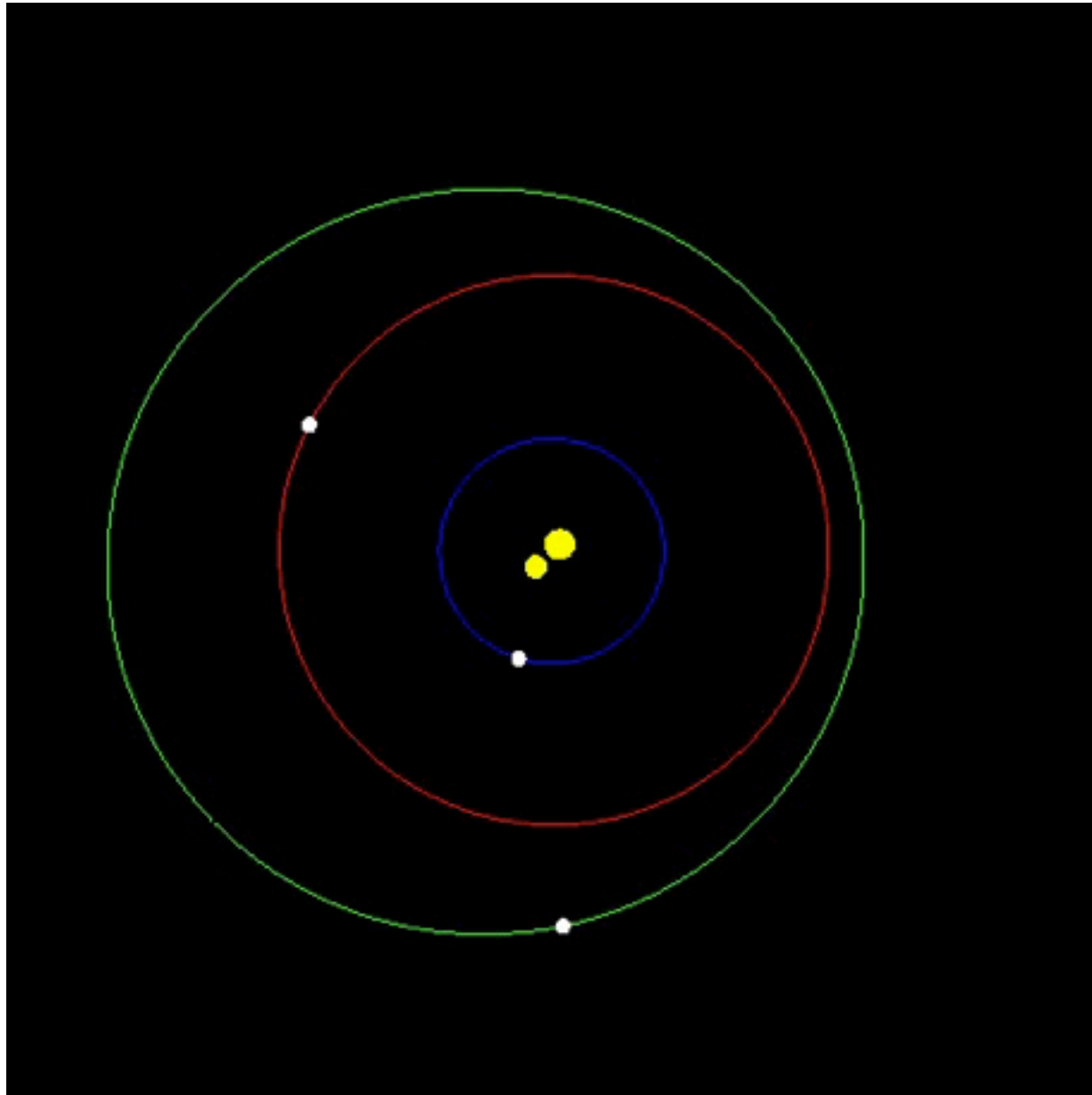
# Kepler 47: a (stable) Tatooine type system

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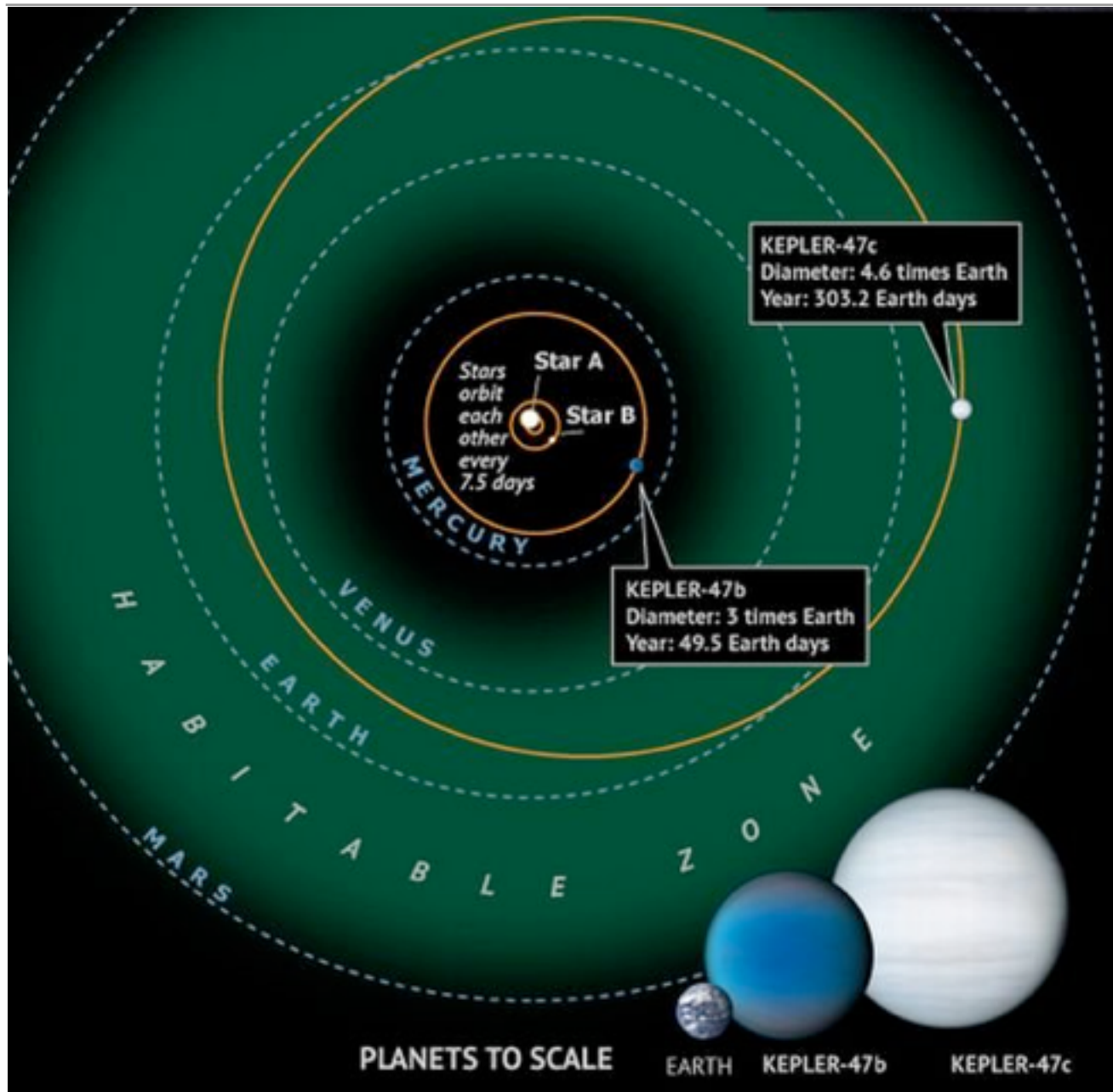


# Kepler 47: a (stable) Tatooine type system

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# Circumbinary planets are easier to find in “habitable zone”

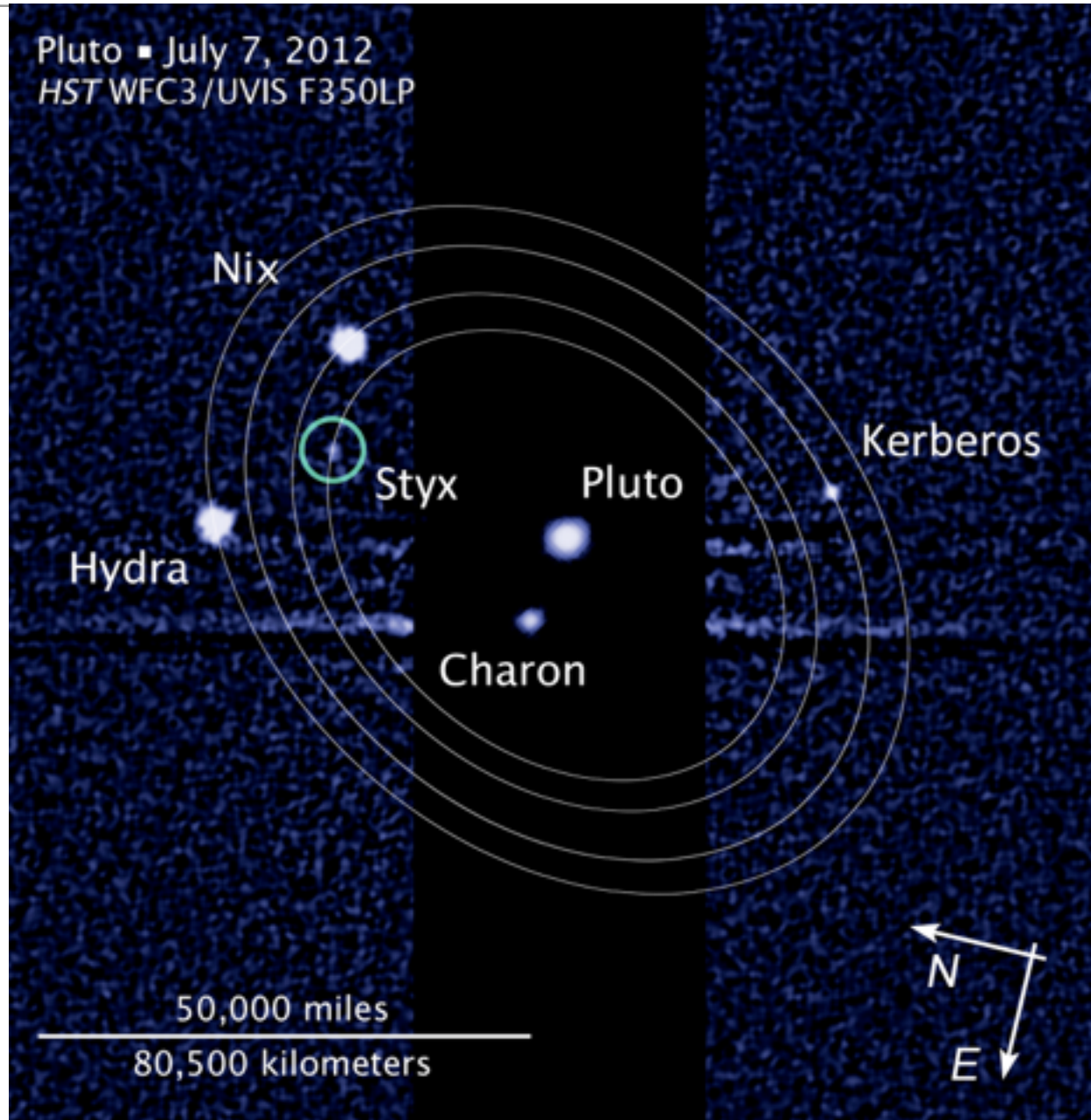


In theory, this bodes well for finding Tatooines.

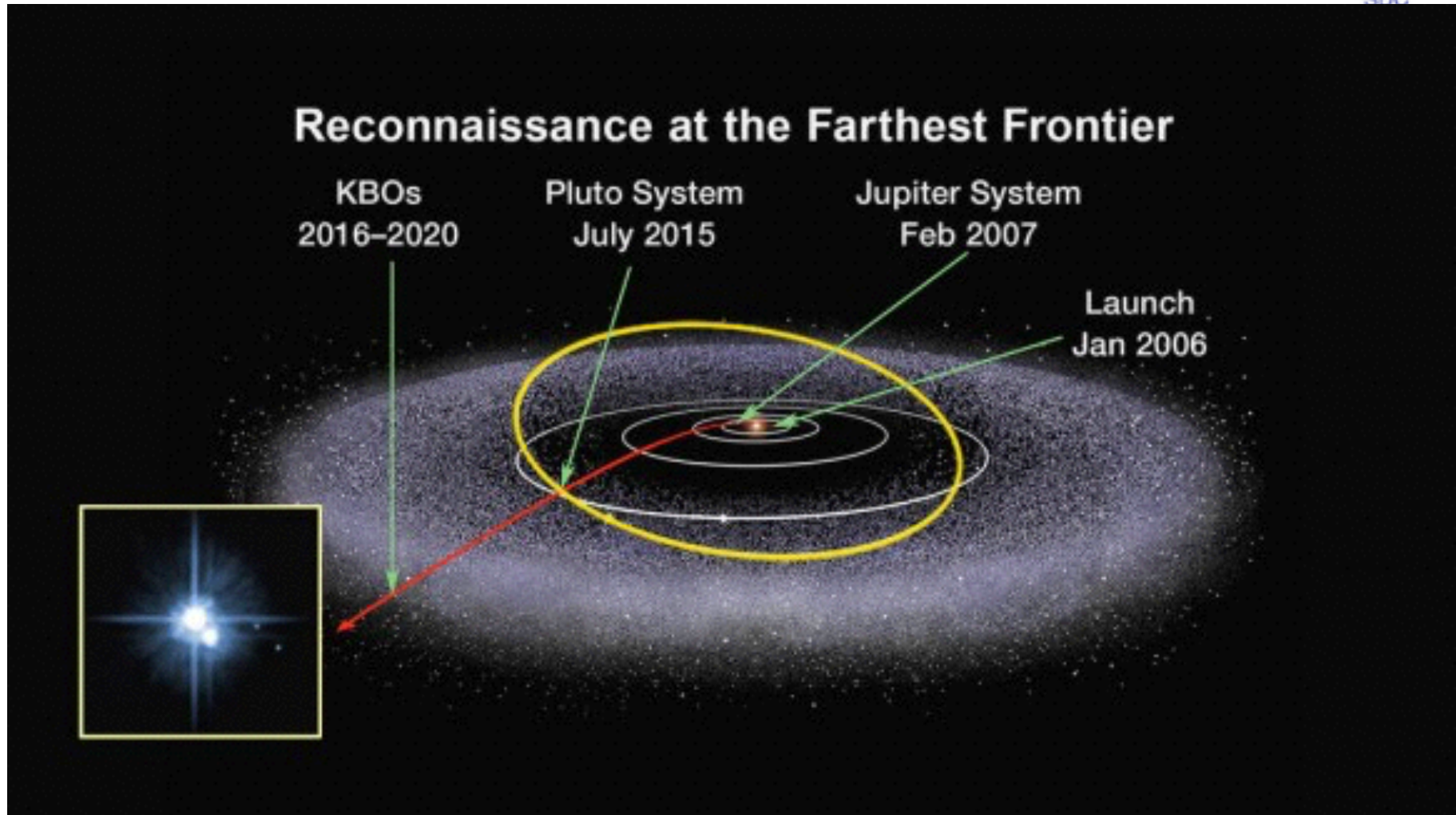
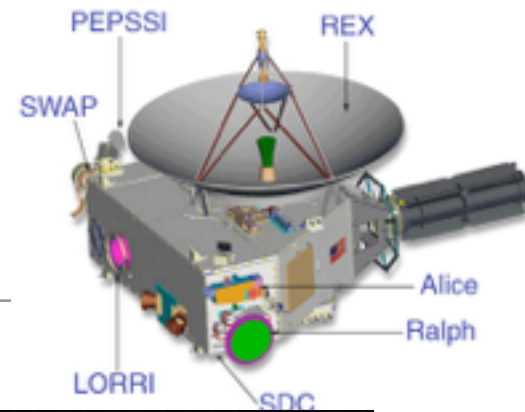
So far, all of the circumbinary planets are massive gas giants.

Kepler 47 b,c  
(*Orosz et al. 2012*)

# Local Example: Pluto not a Planet ... a Mini Circumbinary Multi-Planet System!

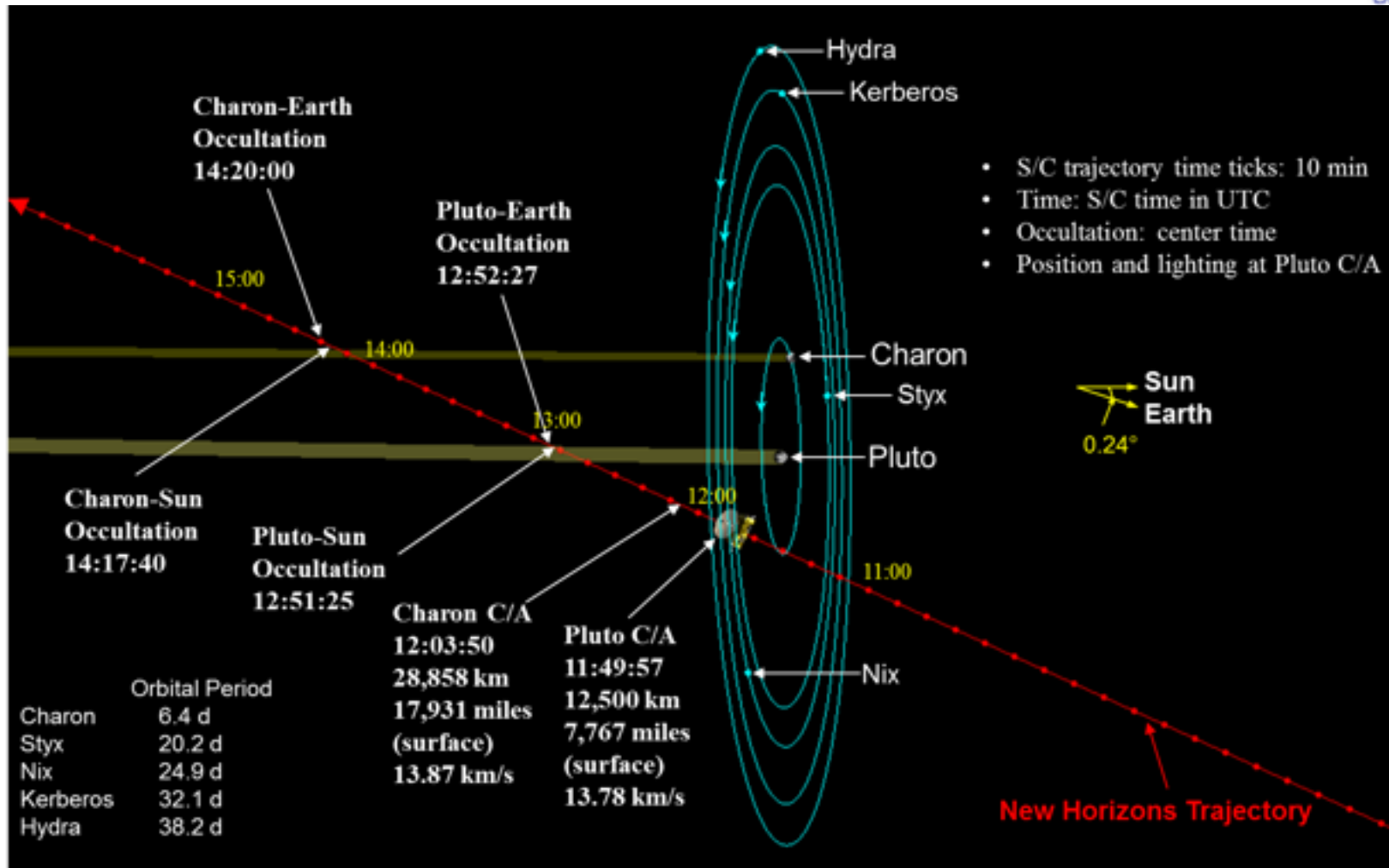
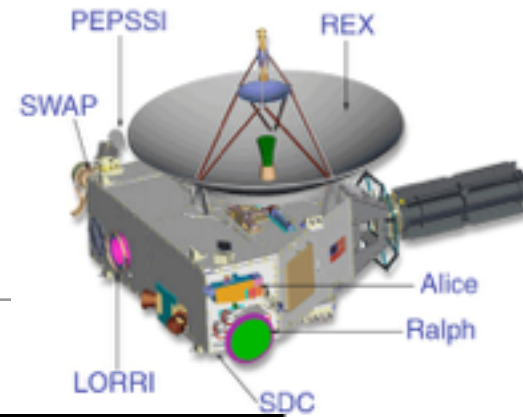


# Local Example: Pluto not a Planet ... a Mini Circumbinary Multi-Planet System!

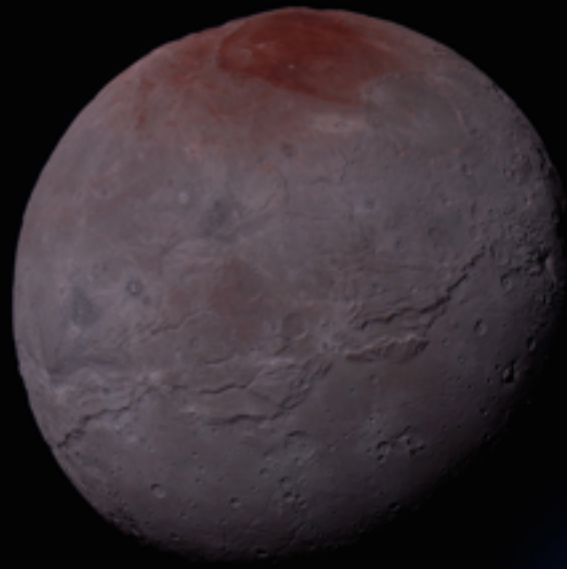


New Horizons Mission

# Local Example: Pluto not a Planet ... a Mini Circumbinary Multi-Planet System!

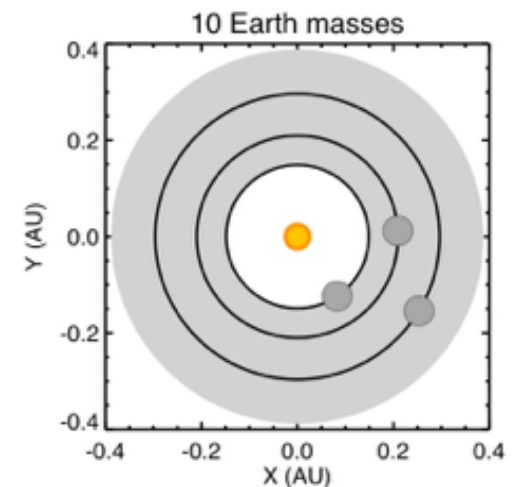
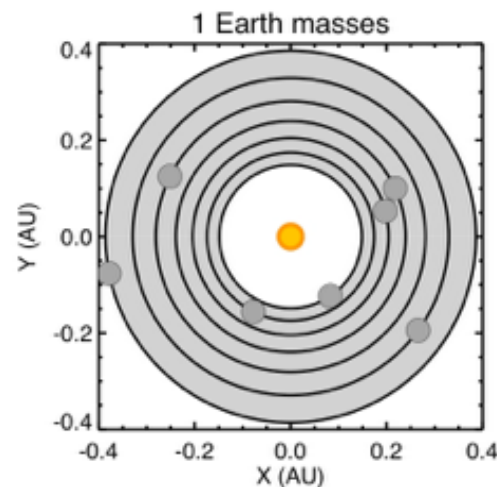
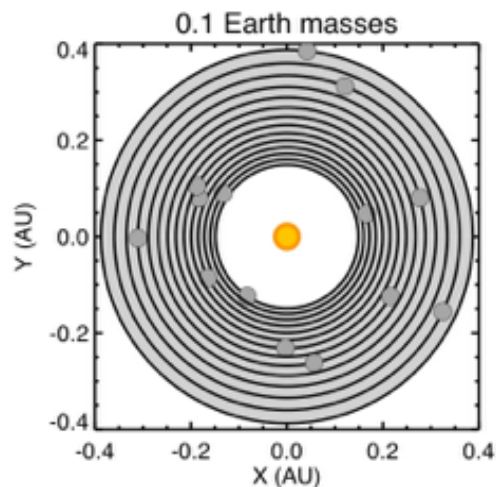
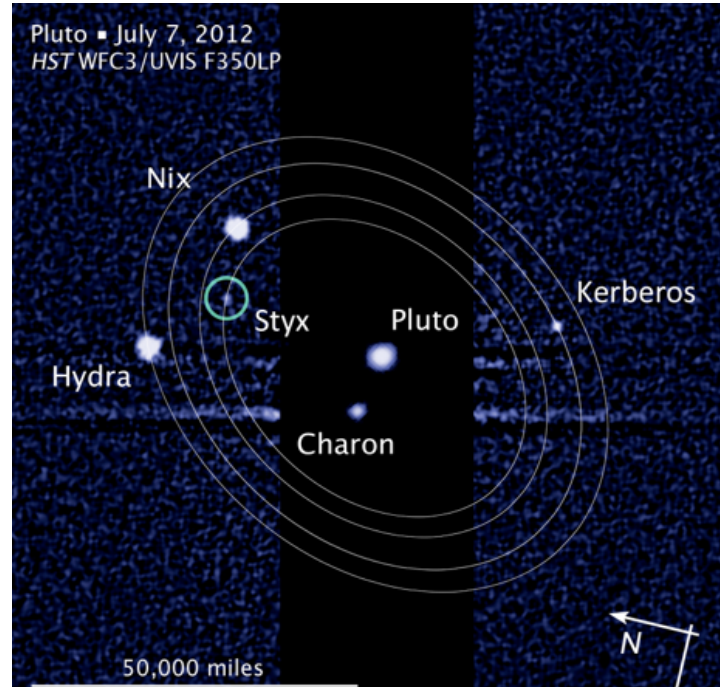


New Horizons Mission



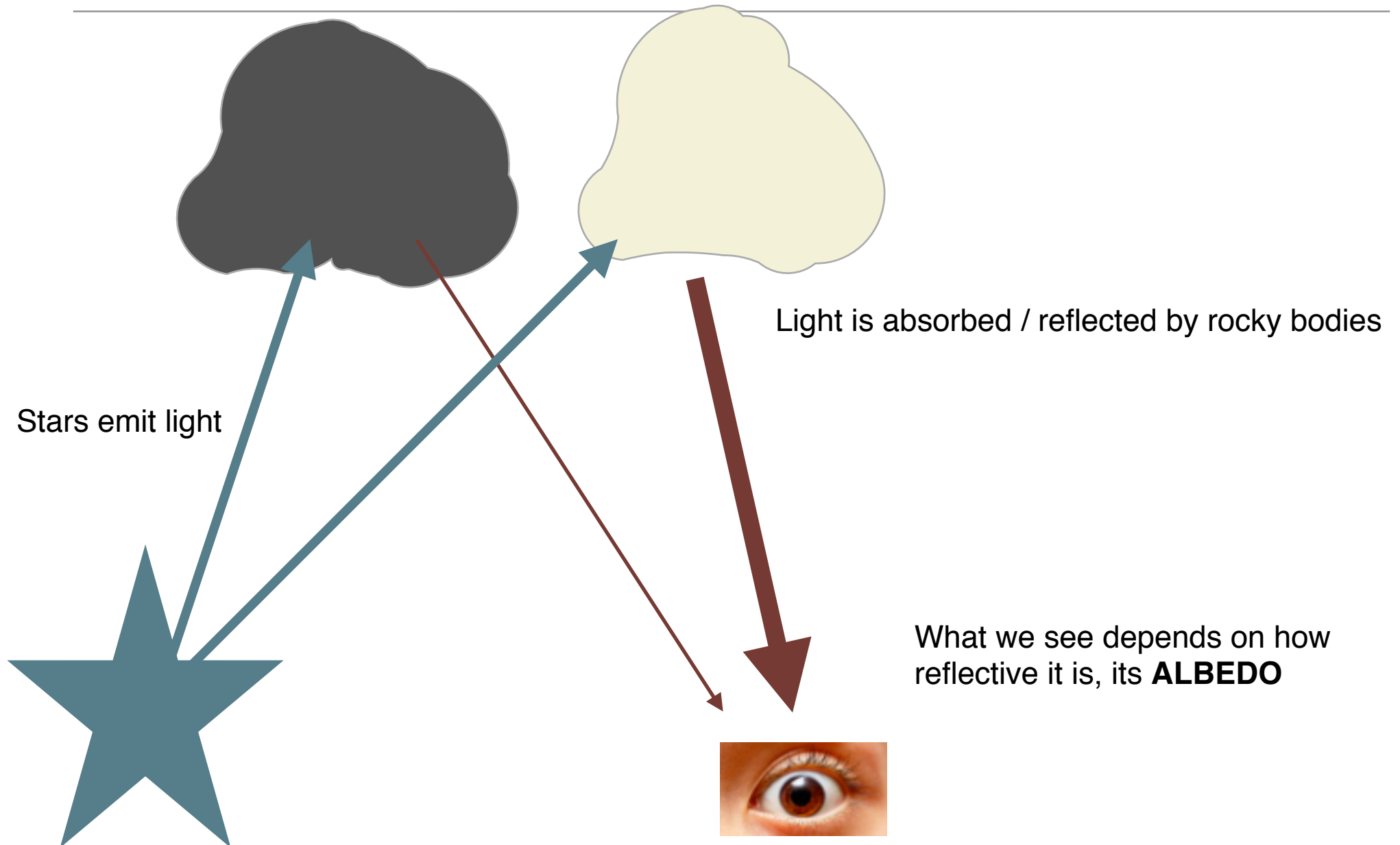


# We can discern the properties of the system using dynamical stability



# Observing “Rocks” vs “Stars”

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# Observing “Rocks” vs “Stars”

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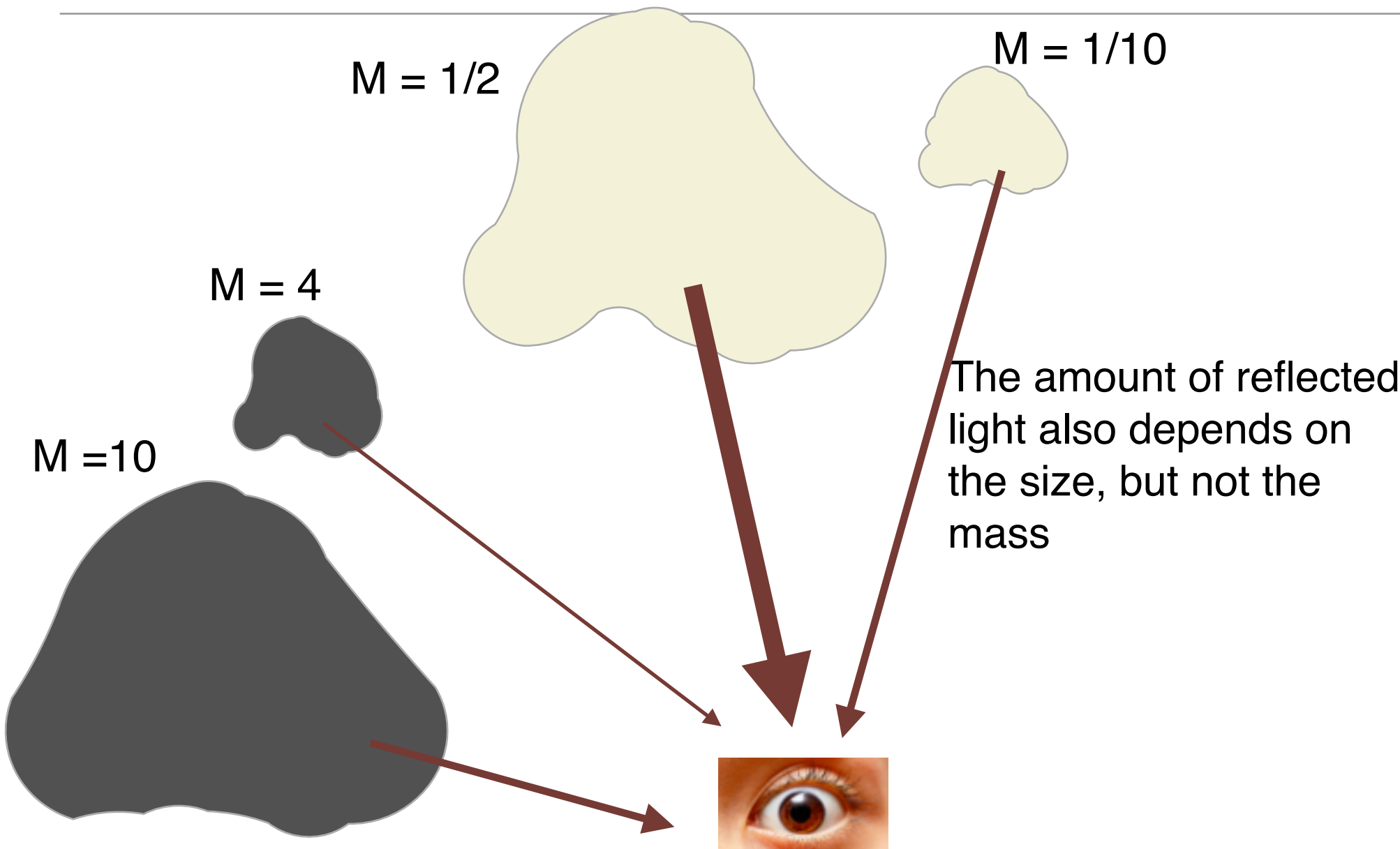
$M = 1/2$

$M = 1/10$

$M = 4$

$M = 10$

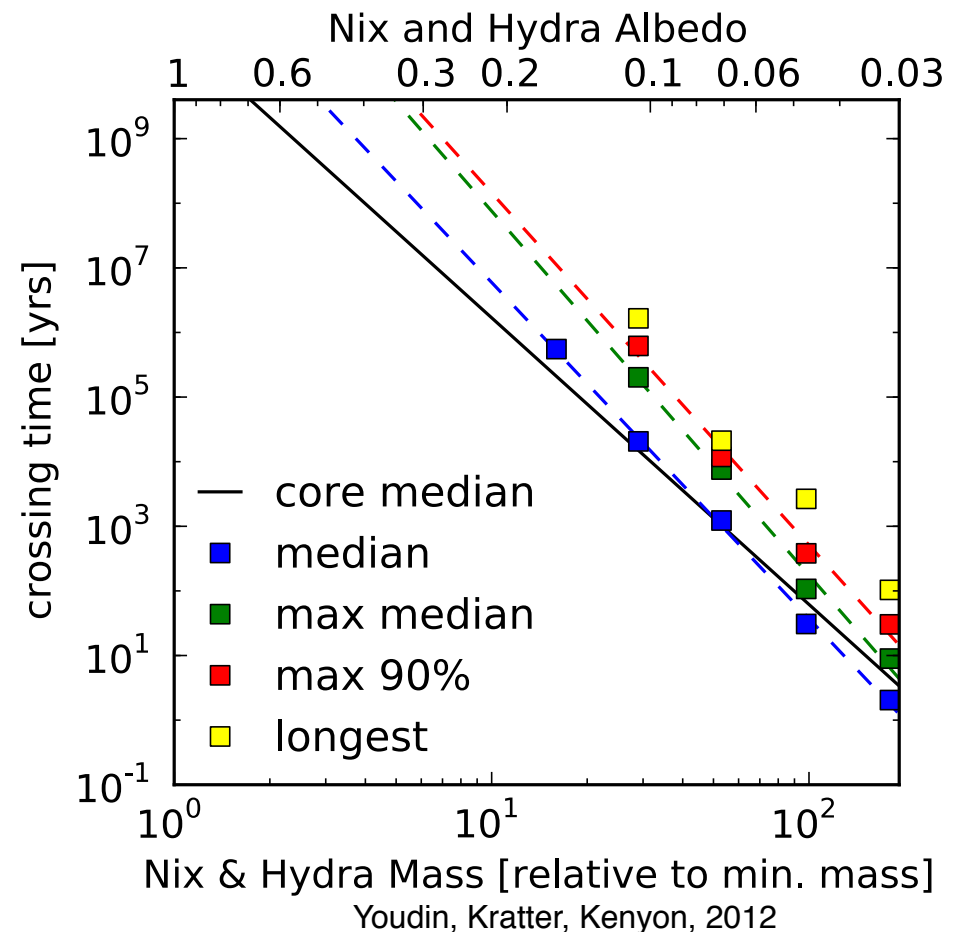
The amount of reflected light also depends on the size, but not the mass



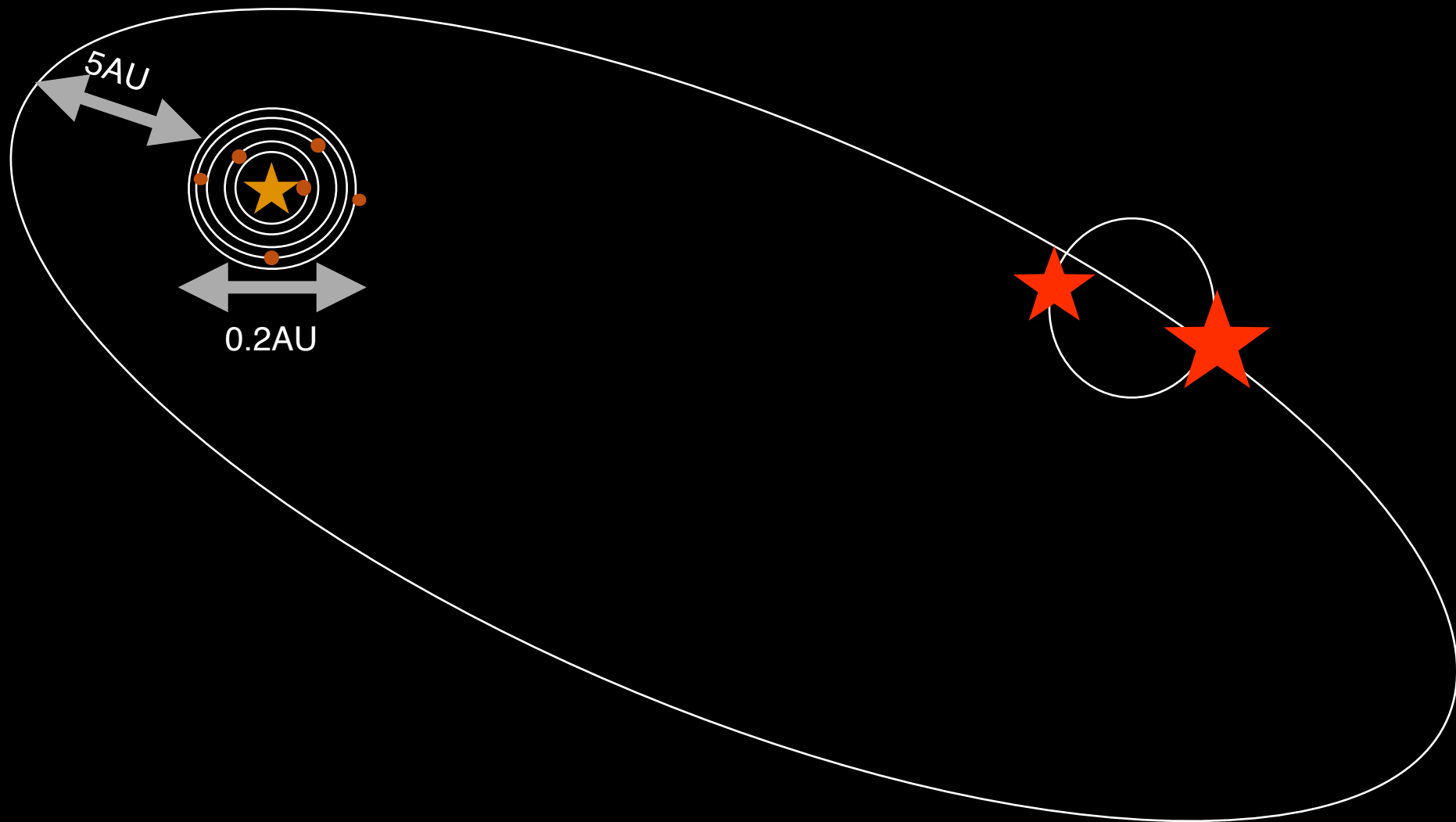
# We can conclude that Pluto's moons are icy!

- Our dynamical estimates of the masses and albedos have been validated by New Horizons
- This shows the strength of this method for systems we can't go visit

Fresh asphalt	0.04
Worn asphalt	0.12
Bare soil	0.17
Green grass	0.25
Desert sand	0.40
New concrete	0.55
Ocean Ice	0.5–0.7
Fresh snow	0.80–0.90
Enceladus	0.9
Pluto	0.49-0.66
Charon	0.36-0.39

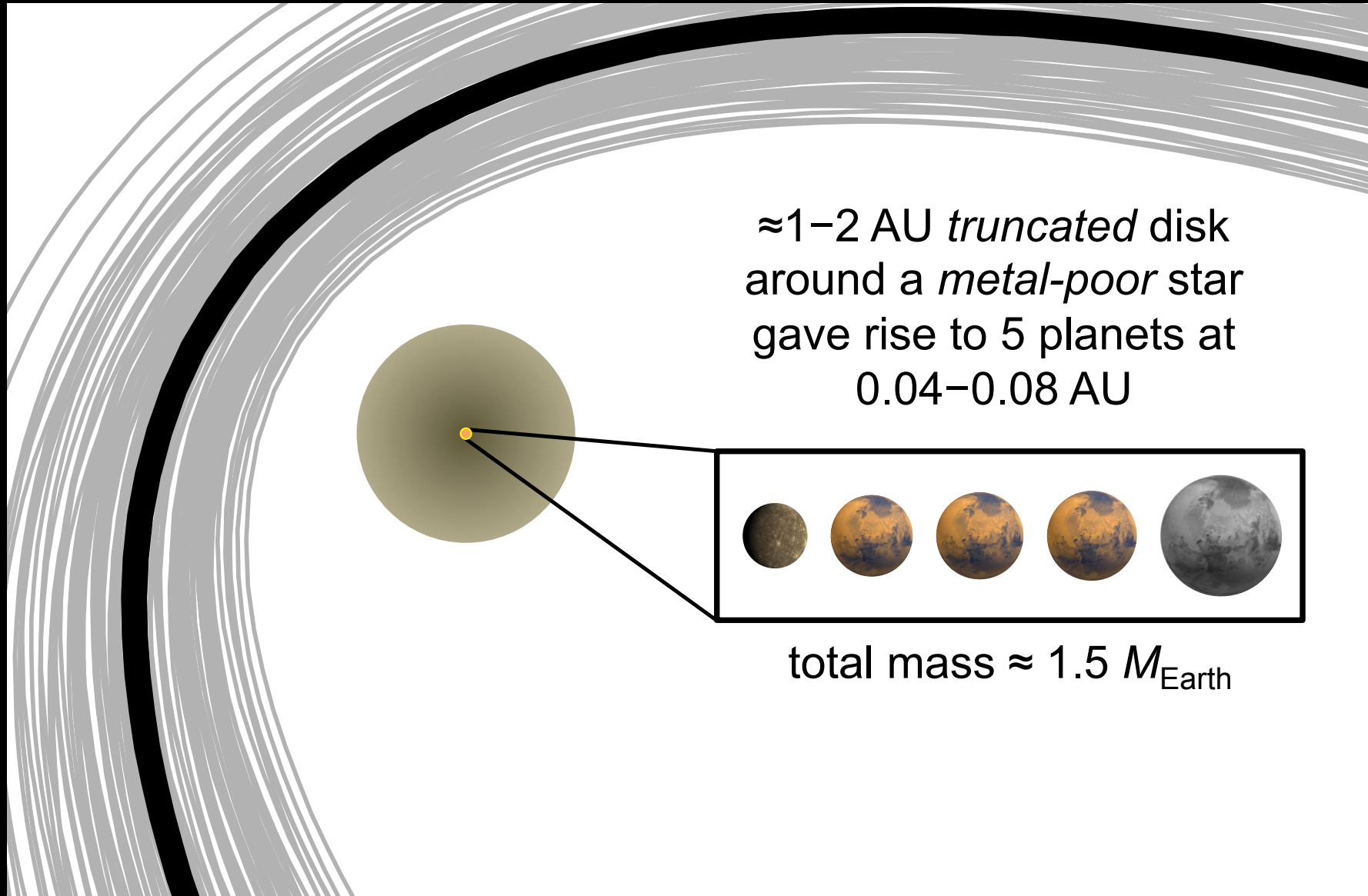


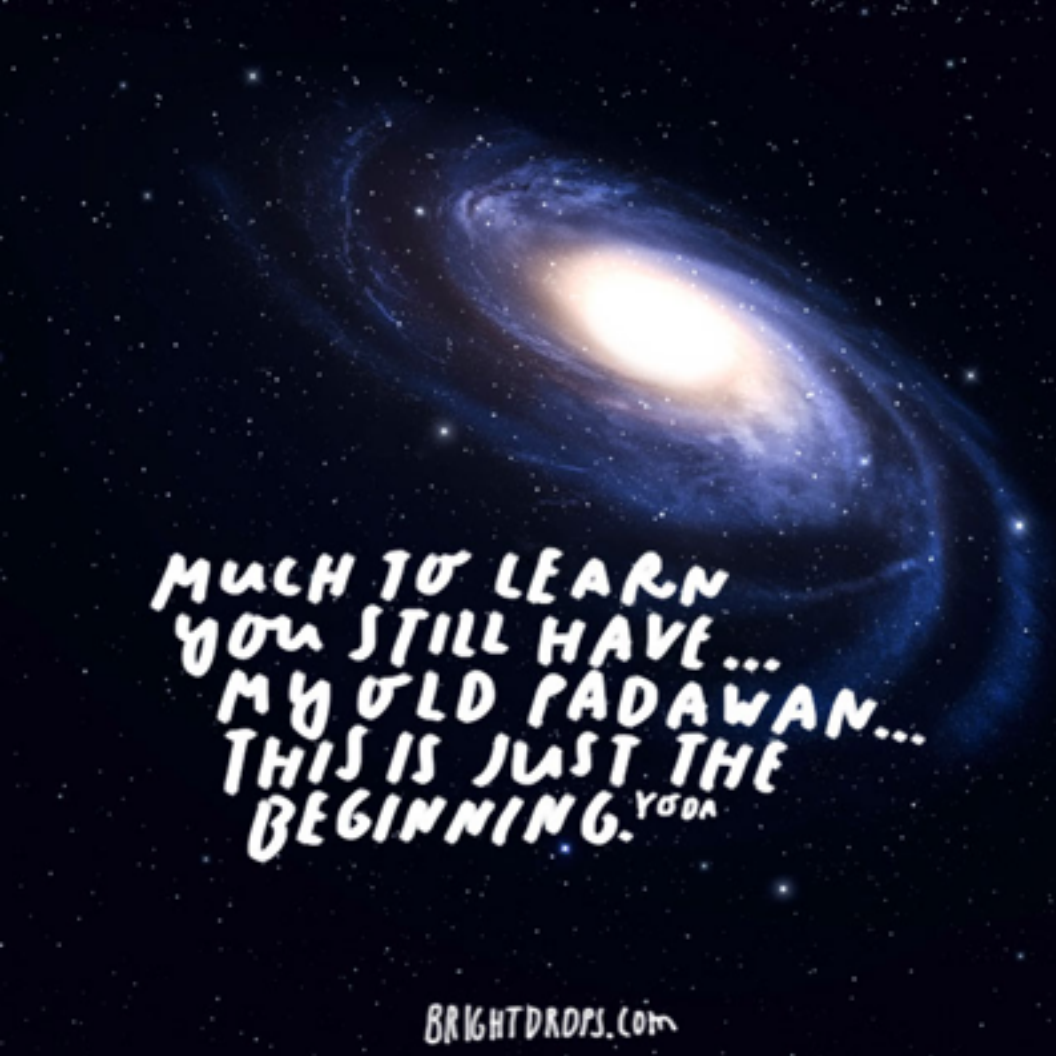
# KEPLER 444: 5 SUB-EARTH PLANETS IN A TRIPLE STAR SYSTEM



Another extreme system that constraints planet formation

# PLANET FORMATION MUST BE VERY EFFICIENT IN SOME SYSTEMS





MUCH TO LEARN  
YOU STILL HAVE...  
MY OLD PADAWAN...  
THIS IS JUST THE  
BEGINNING. YODA

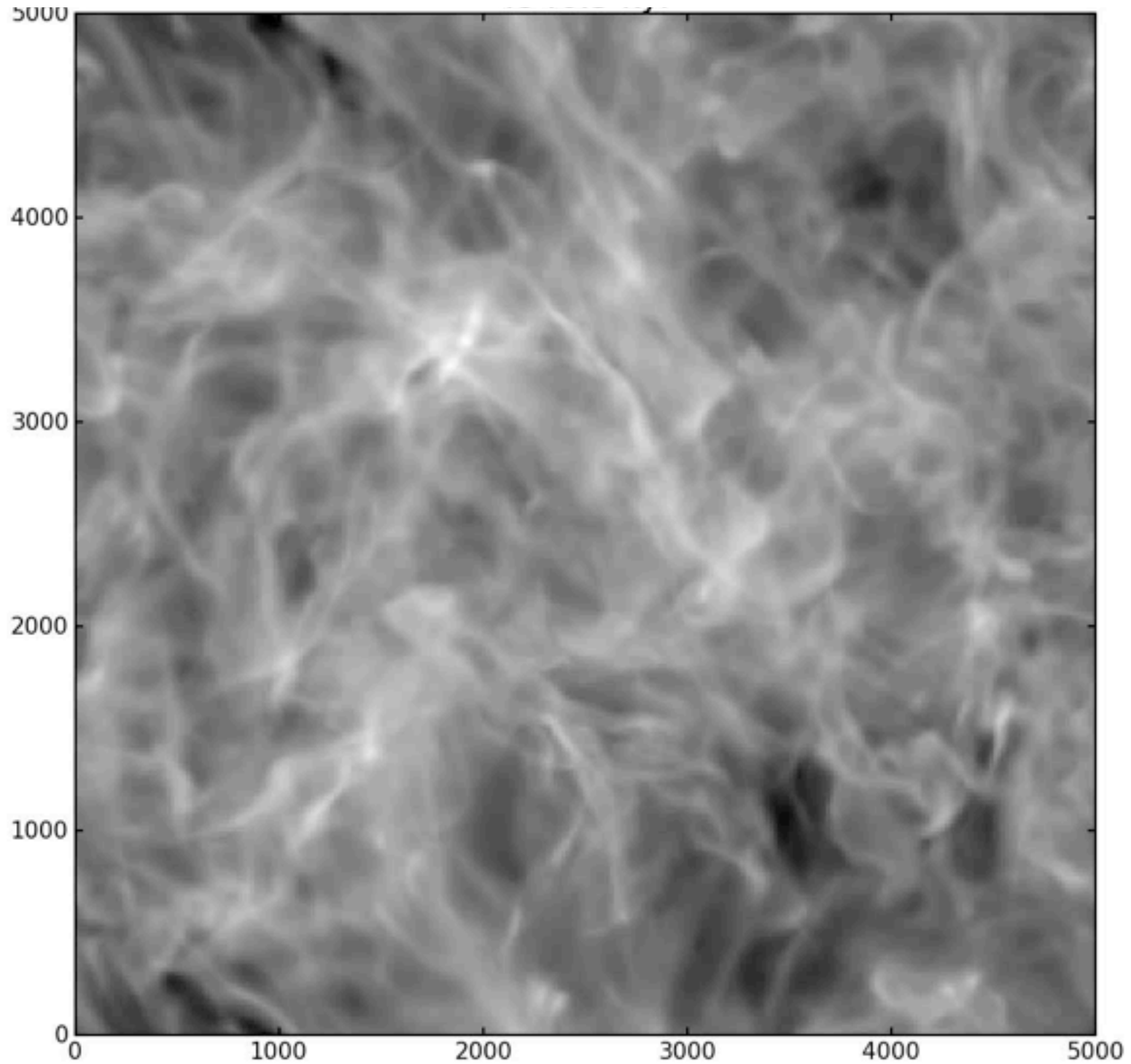
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ALWAYS PASS ON  
WHAT YOU HAVE  
LEARNED. YODA

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Thank you





Thank you

