



New Perspectives on London Dispersion Interactions and Hamaker Coefficients: Dispersion Energy Of Graded Interfaces And Dispersion Driven RE Segregation

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- R. Podgornik (Slovenia)

Electronic Structure Calculations

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Si₃N₄

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PS, P(S-MMA), PMMA, PET

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Polysilanes

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History of The London Dispersion Interaction

T. Young (1805)

- **An Essay on the Cohesion of Fluids**

J. W. Gibbs (1875)

J. D. van der Waals (1893)

- Theory of Capillarity

Sellmeier (1872)

- **Regarding the Sympathetic Oscillations Excited in Particles by Oscillations of the Ether and Their Feedback to the Latter, Particularly as a Means of Explaining Dispersion and its Anomalies**

Maxwell's Equations

- Oliver Heaviside

R. de L. Kronig, (1926)

- On The Theory of Dispersion of X-Rays

F. London (1930)

- General Theory of Mol. Forces
- Induced Dipoles

Hamaker (1937)

- Hamaker Constant

Casimir (1948)

- Attraction of 2 Conducting Plates
- QED - Casimir Force

Lifshitz (1956)

- QED - General Theory
- With Retardation Effects

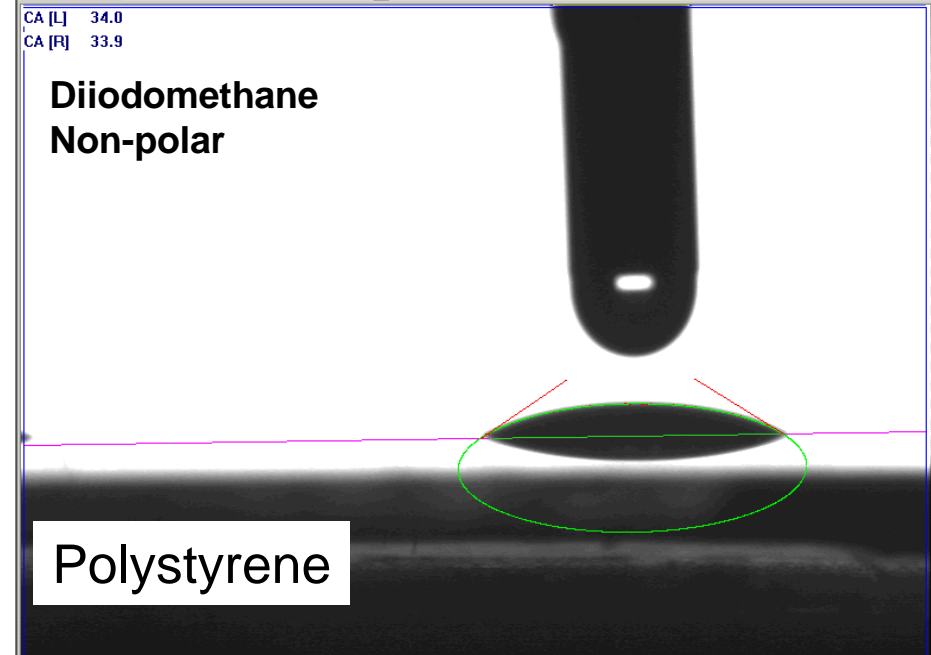
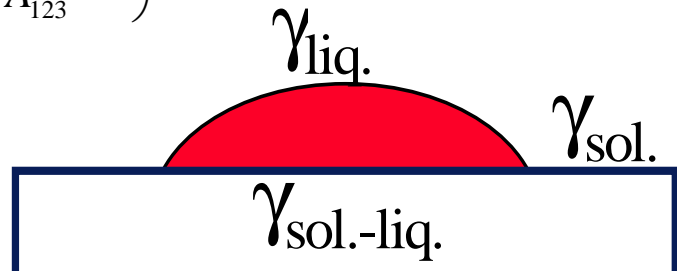
R. H. French, Journal of the American Ceramic Society, 83, 9, 2117-46 (2000).

Dispersion Contribution to Surface Free Energy

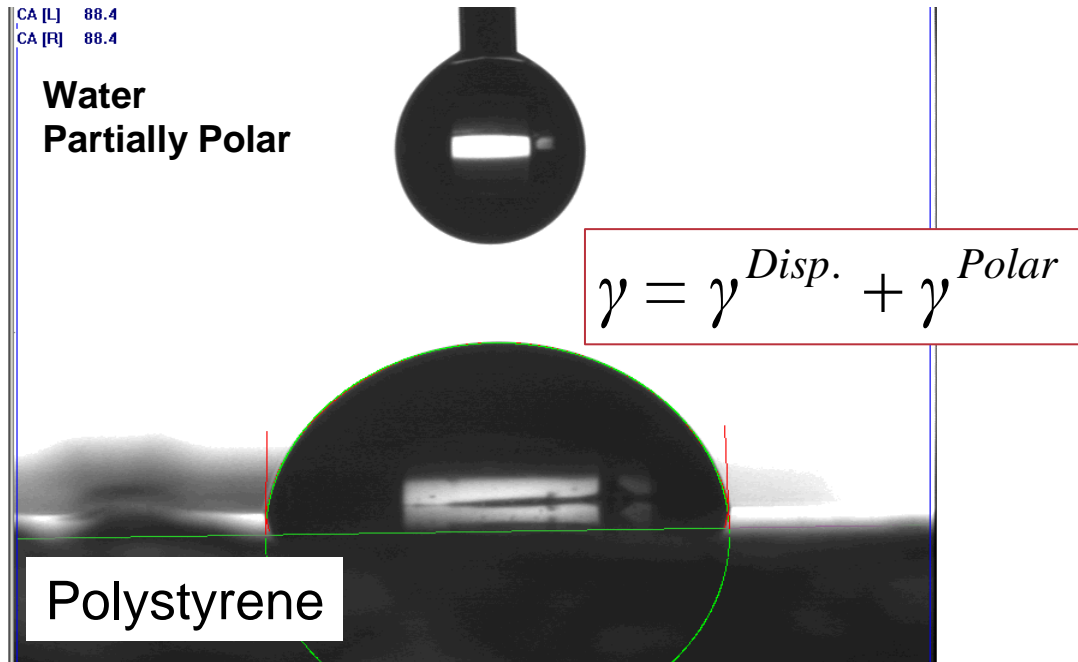
vdW - London Dispersion Energy

- Thermodynamic Free Energy Arising From
 - London Dispersion Interaction
- Dispersive Component Of Surface Free Energy

$$\theta = \arccos\left(\frac{A_{121}}{A_{123}} - 1\right)$$



Electrodynamic (vdW-LD) & Polar Interactions

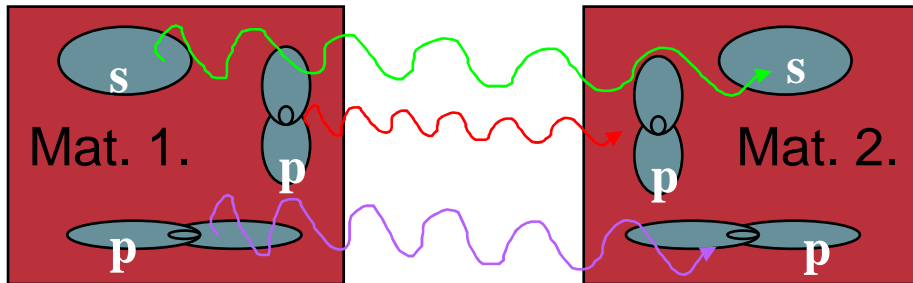


R. H. French, K. I. Winey, M. K. Yang,
W. Qiu, *Aust. J. Chem.*, **60**, 251-63,

Introduction

van der Waals-London Dispersion Interactions

- Thermodynamic Free Energy



Arises From Oscillating Dipoles

- Interatomic Bonds of Elect. Struc.

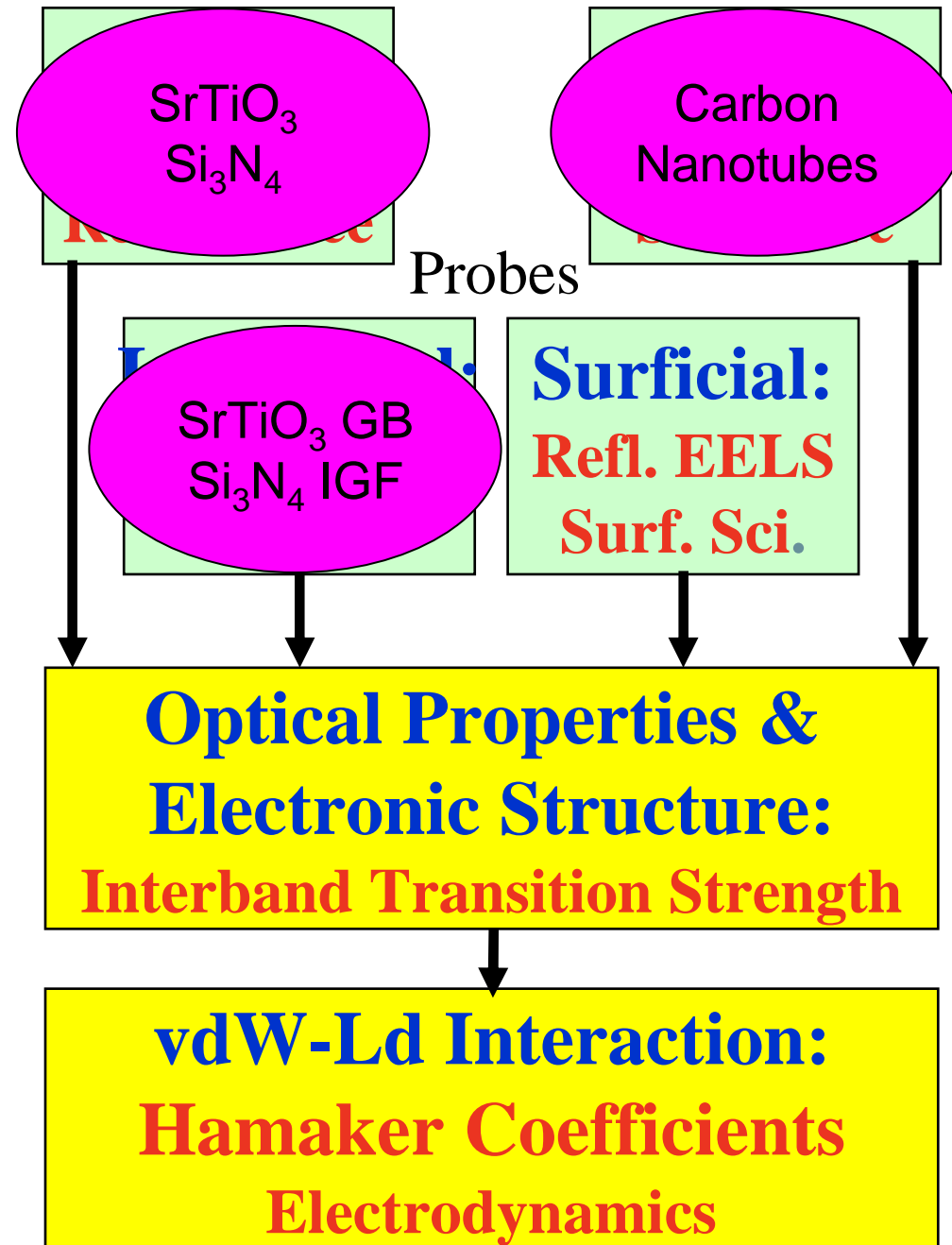
$\mathbf{J}_{cv}, \epsilon'' \Rightarrow$ London Disp. Spectra

A - Hamaker Constant

- Interaction Scaling Constant

\mathbf{F}_{disp} - Dispersion Force

$$E_{London\ Dispersion} = -\frac{A(l)}{12\pi l^2}$$



Outline

Interfaces In Ceramics And vdW-Ld Interactions

Optical Properties And Electronic Structure

van der Waals – London Dispersion Interactions

1. vdW-Ld Energies Of Grain Boundaries in SrTiO₃

2. Role Of Retardation In Novel Wetting Phenomena

3. vdW-Ld Driven Rare Earth Segregation In RE-M-SiON: Si₃N₄

Conclusions

Interfaces In Ceramics

And The vdW-Ld Interaction

Atomically Structured Grain Boundaries

Nanostructured Amorphous Films



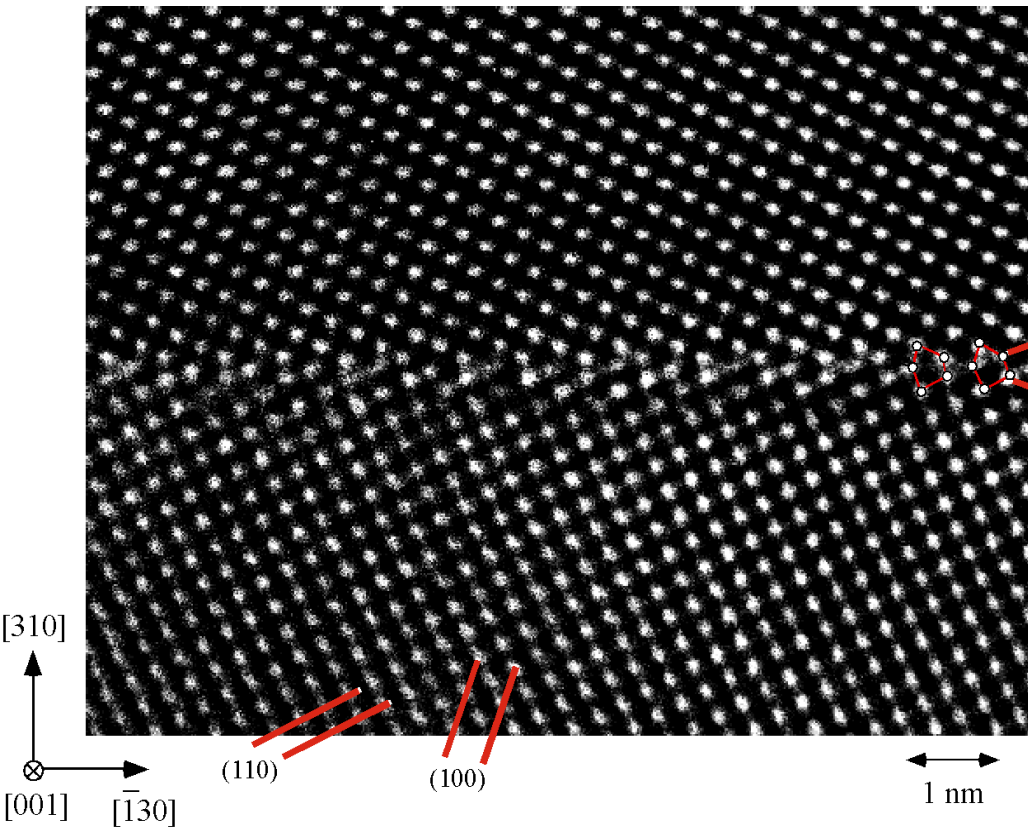
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SrTiO₃:Fe Bi-crystals

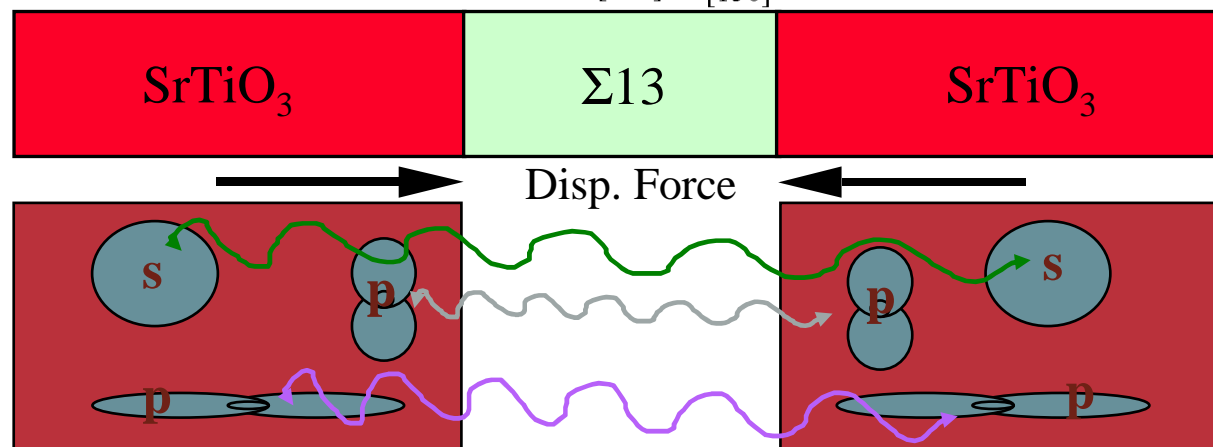
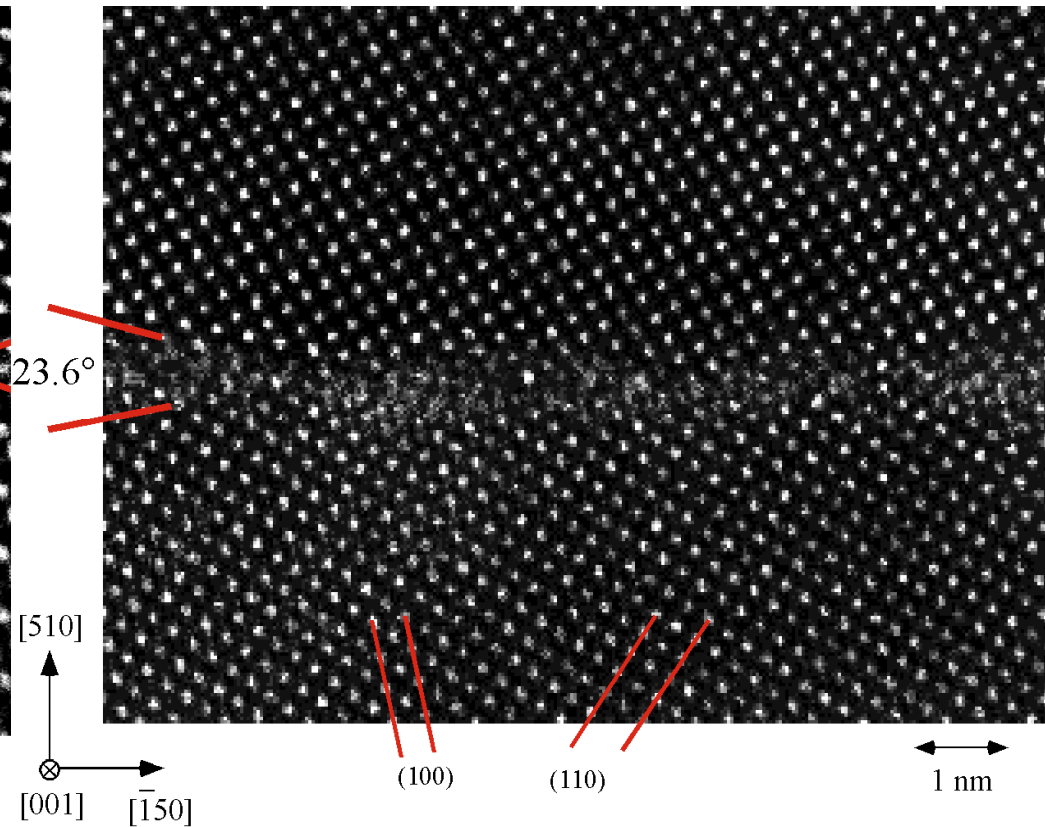
$\Sigma 5$ Boundary

- Atomically Structured



$n\Sigma 13$ Boundary

- Atomically Structured



IGF's in Thick Film Resistors

**Pb₂Ru₂O₇ Conductor Particles
Separated by PbAl-Silicate
Intergranular Glass Films**

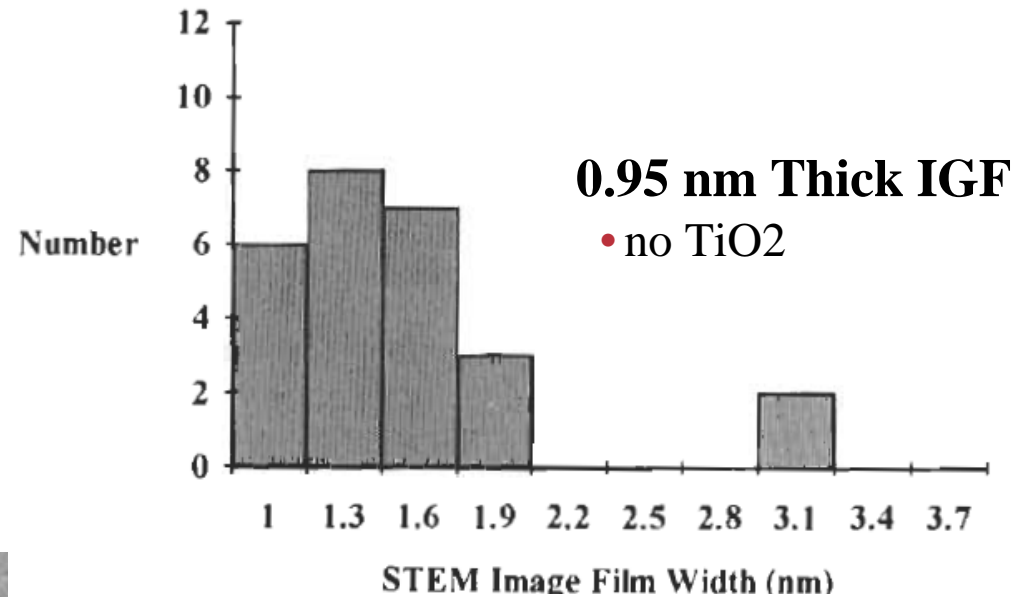
This TiO₂ Effect Arises From

- Ti Segregation To Grain Surfaces
- A 5 Layer Hamaker Configuration

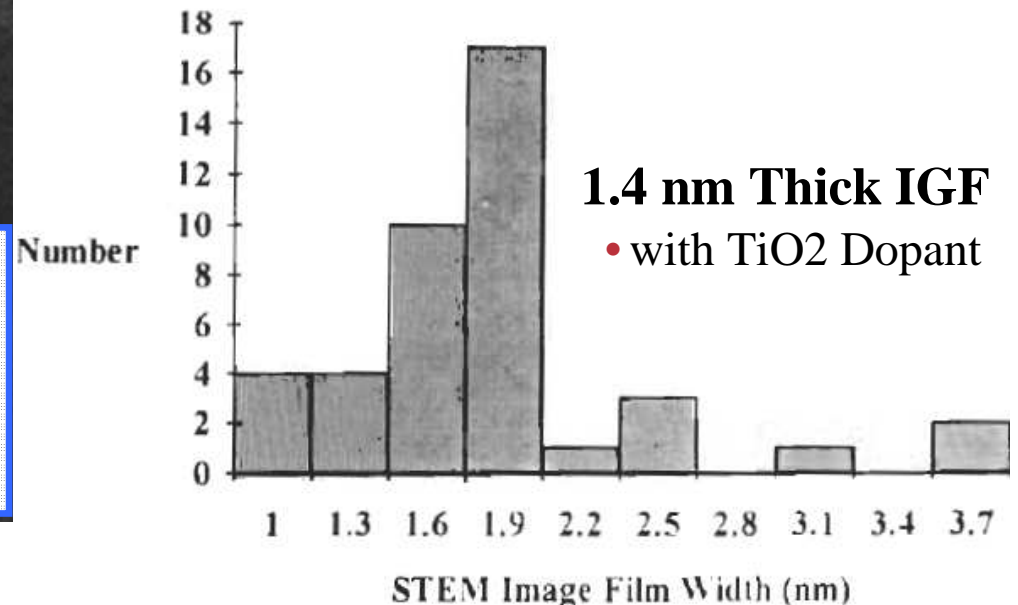


**Compositional Manipulation Of
Nanoscale Intergranular Films
Using vdW-Ld Interactions
Already In Common Use**

Sample A (no TiO₂)



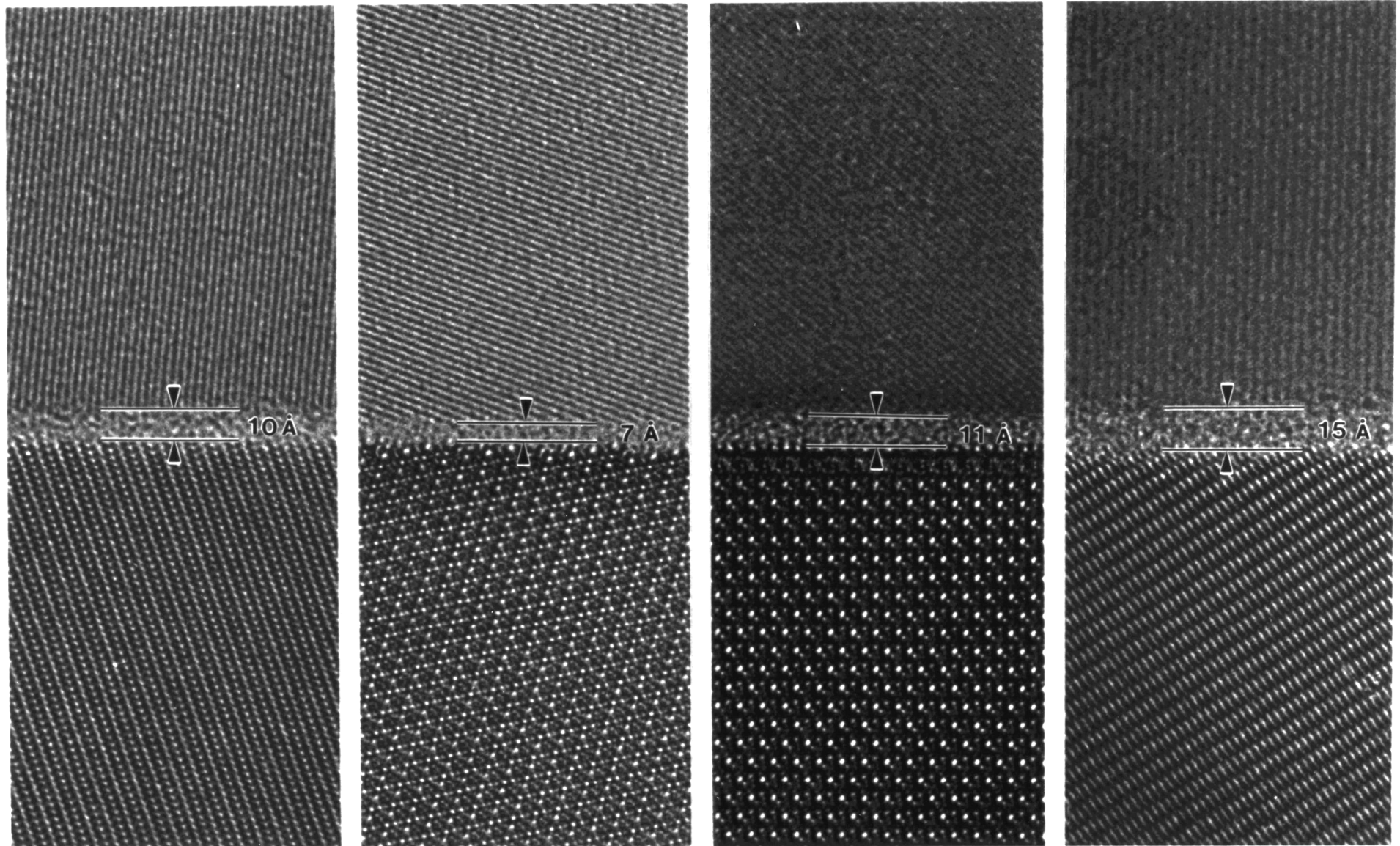
Sample C (8.44 mole% TiO₂)



Y. M. Chiang, L. E. Silverman, R. H. French, R. M. Cannon, J. Am. Ceram. Soc., 77, 1143-52. (1994).

Si₃N₄ : Nanostructured Amorphous Films

Equilibrium Intergranular Glassy Films



Tanaka

undoped

1.0 nm

80 ppm Ca

0.7 nm

220 ppm Ca

1.1 nm

450 ppm Ca

1.5 nm

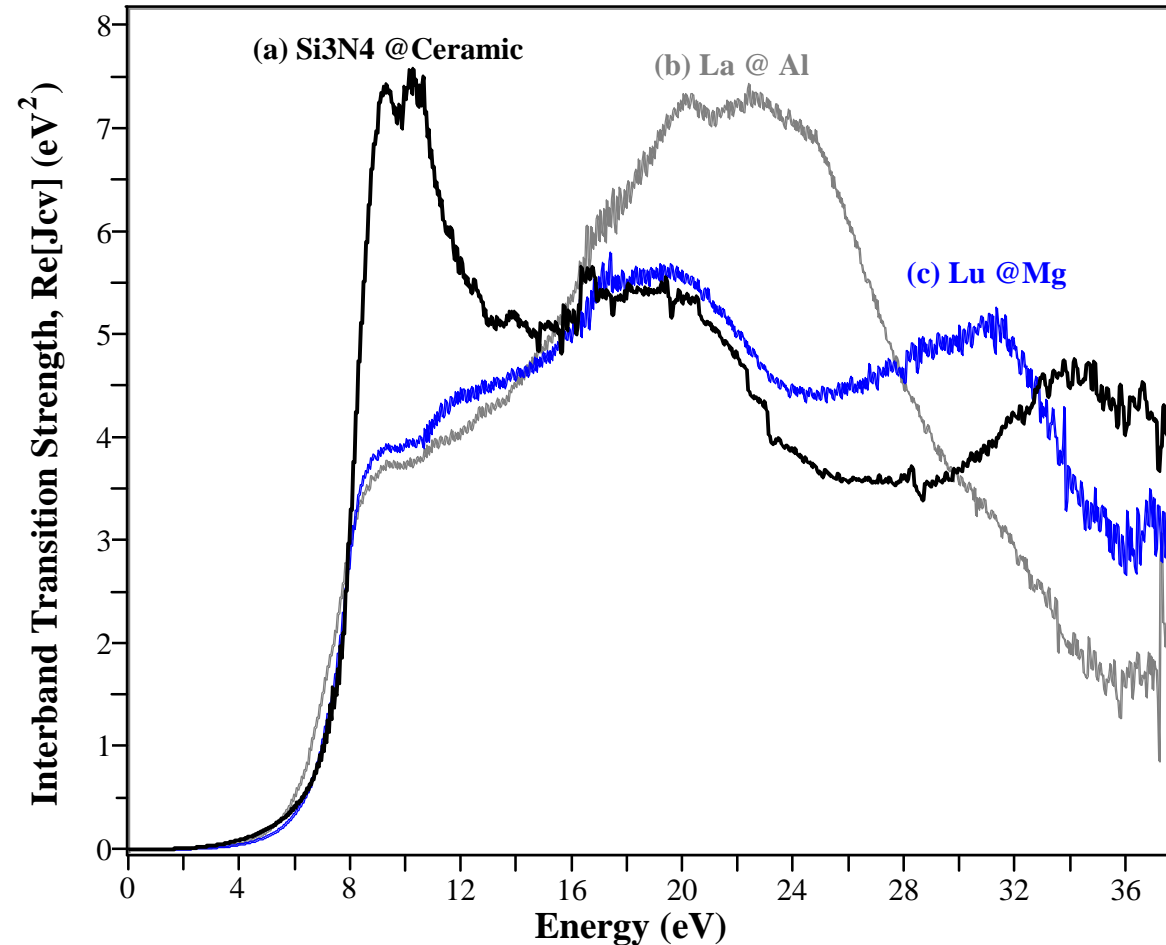
Properties Of Rare Earth-M-SiON:

Bulk SiON Glasses

- Al or Mg Family
- RE Dopants: Y, Lu, La, Gd

Jcv: Interband Transitions

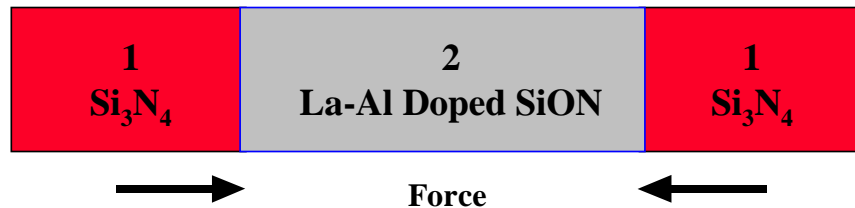
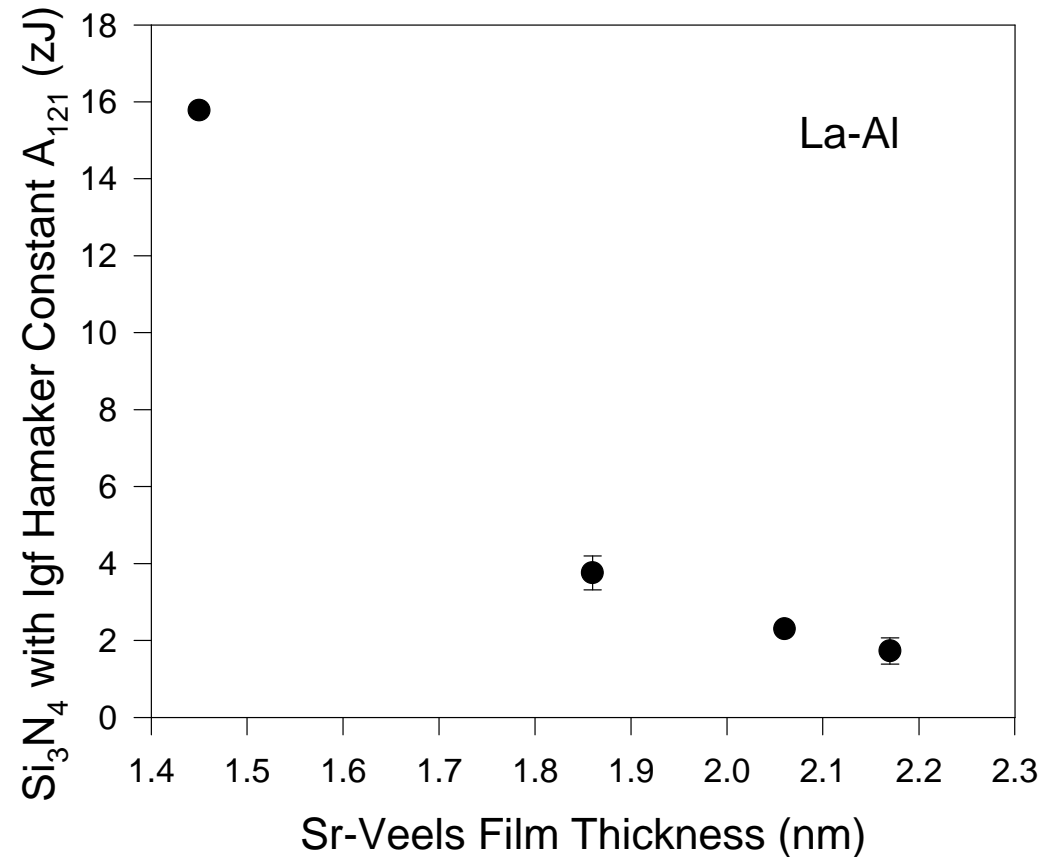
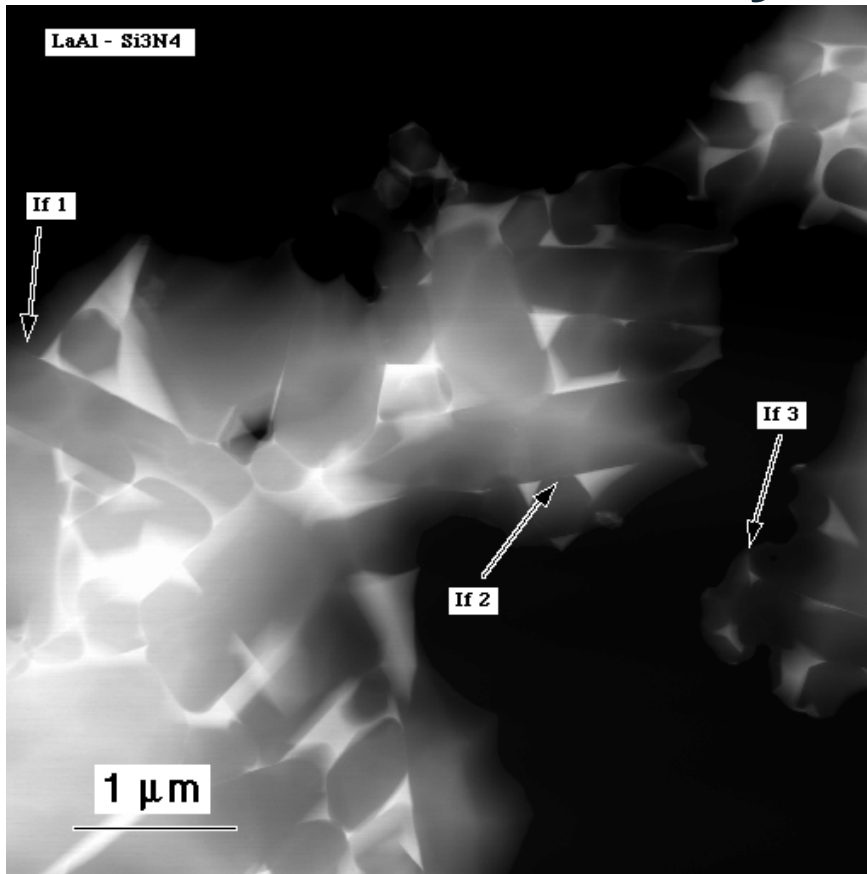
- VUV Spectroscopy



Index of Refraction		
SiON	Mg Glass	Al Glass
Y	1.78 1.71	
Lu	1.70	1.776
La		1.832
Gd		1.826
Si_3N_4 Bulk	1.96	

A_{121} Hamaker Constant (zJ)		
SiON	Mg Glass	Al Glass
Y	4.54 6.50	
Lu	7.86	5.06
La		2.72
Gd		4.64
Si_3N_4 Bulk	180.8	

IG Film Thickness Vary With Dispersion Force



Thickness of Equilibrium Intergranular Films

- In Silicon Nitride

Vary With Magnitude of the London Dispersion Force at the Interface

R. H. French, H. Müllejans, D. J. Jones, G. Duscher, R. M. Cannon, M. Rühle, *Acta Materialia*, **46**, 7, 2271-87 (1998).

Interfacial Segregation of RE in Si_3N_4

From Periodically Averaged
HAADF-STEM Images

RE Segregation To Interface

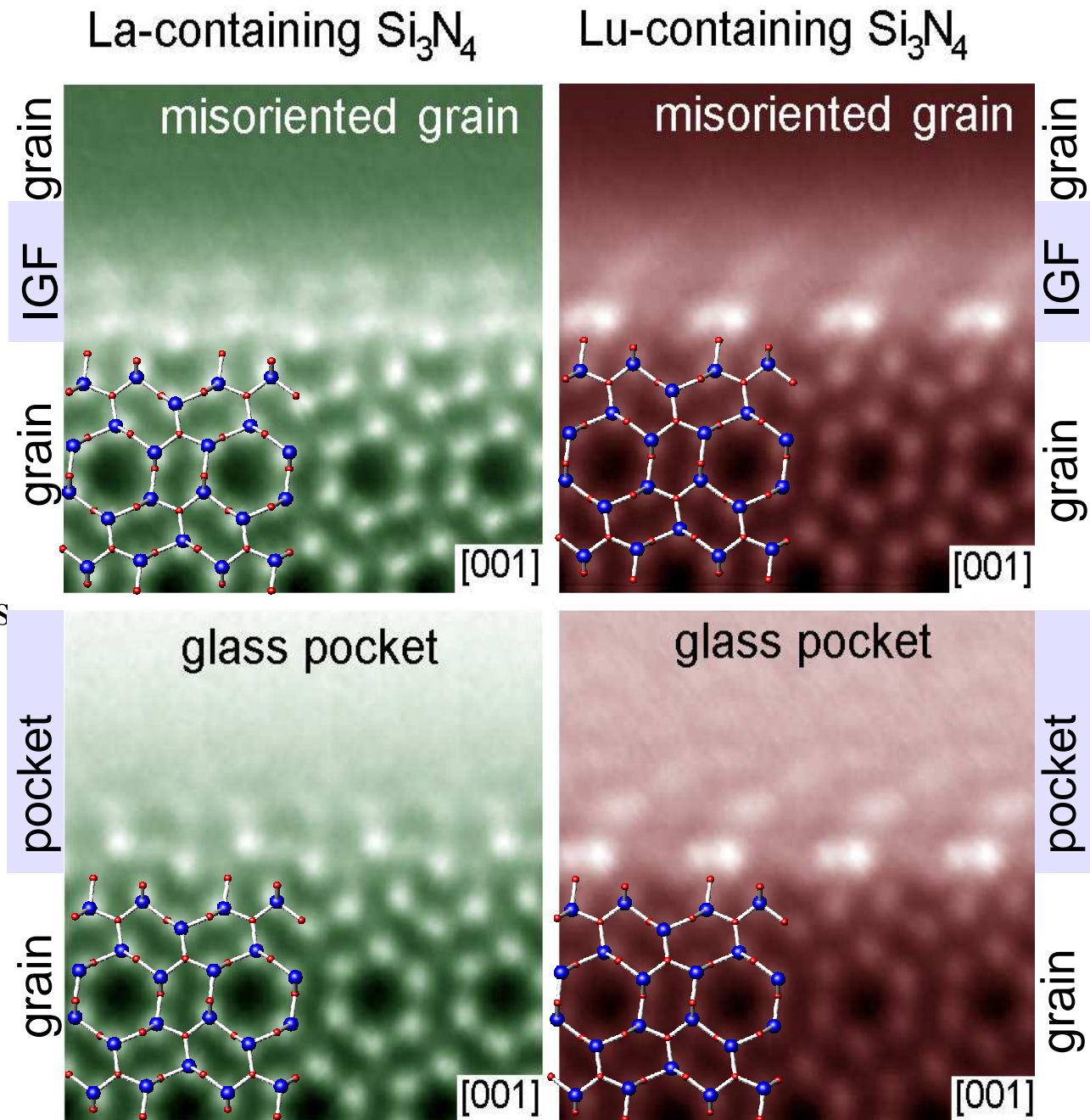
At Grain/Film Interface

And At Grain/Triple Pocket Interfaces

Different Average Atomic
Arrangement Of La & Lu

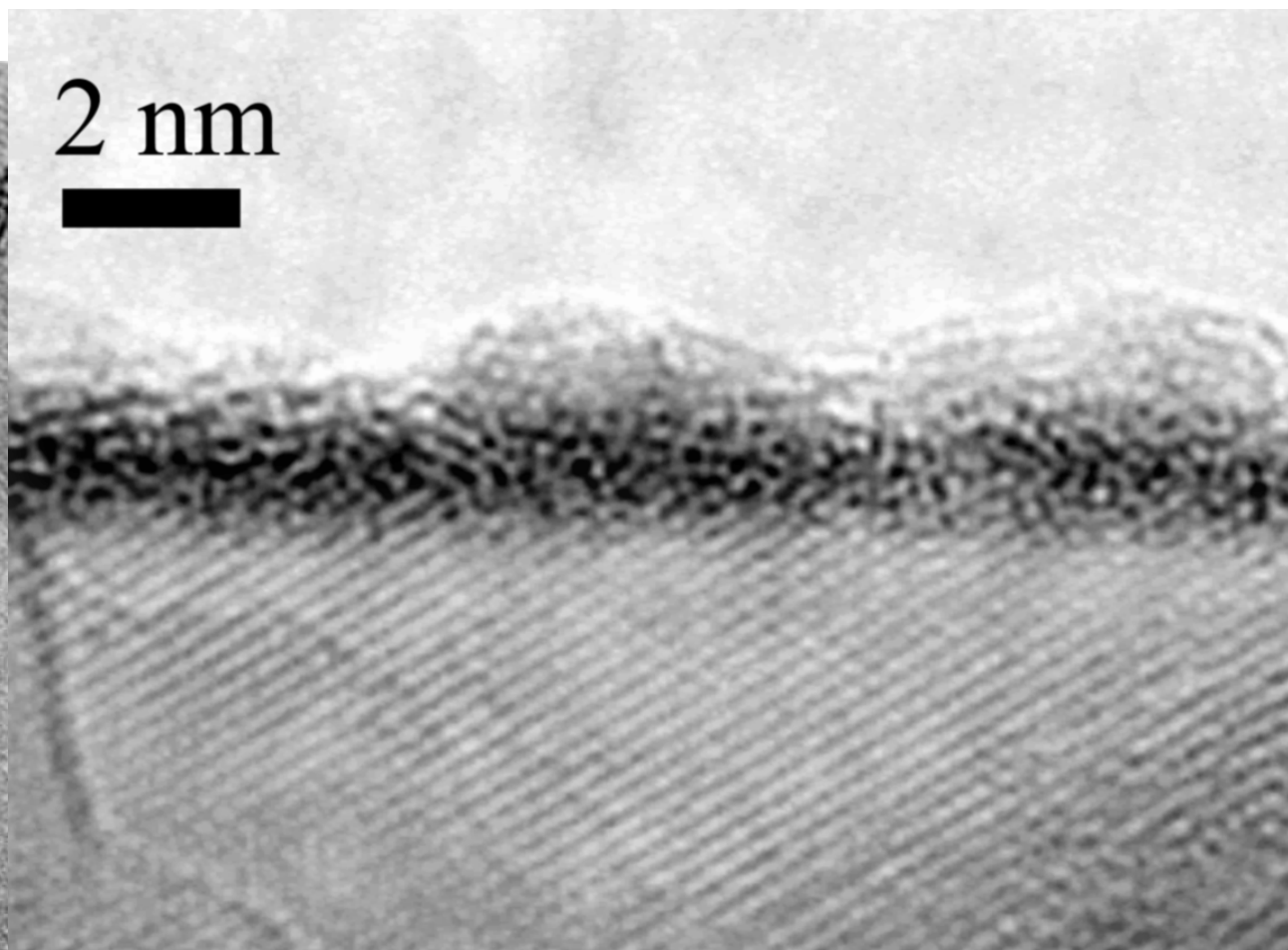
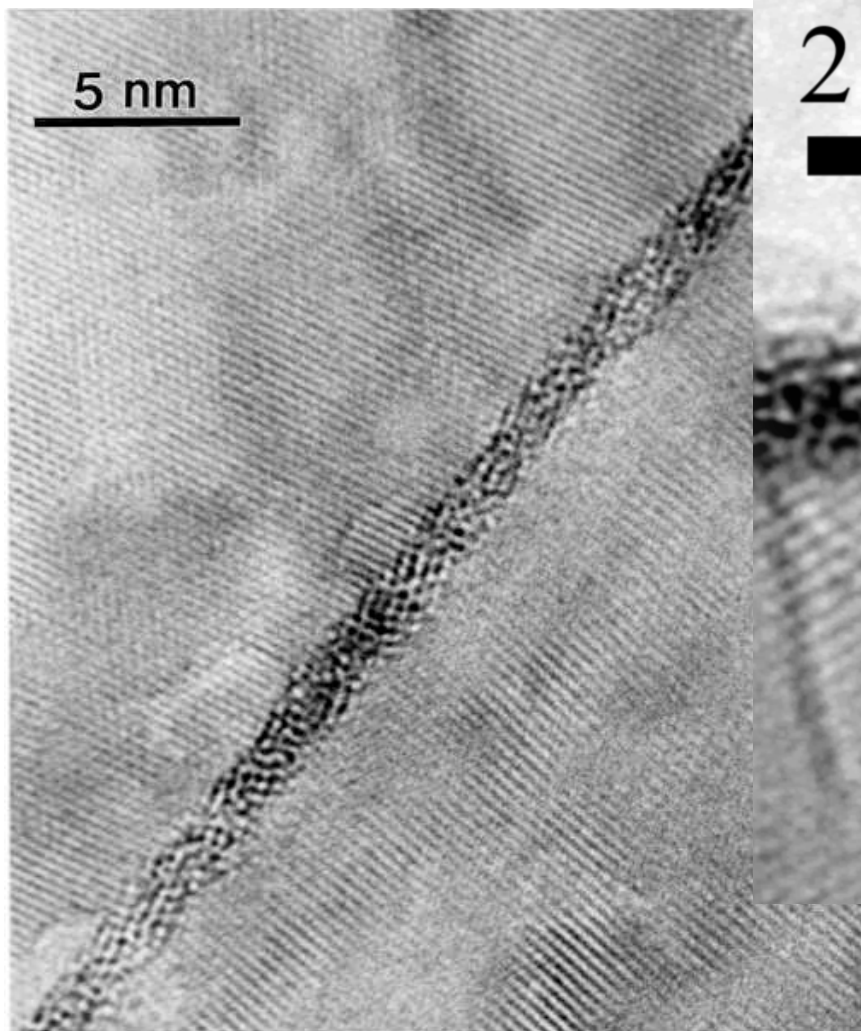
In RE-M-SiON: Si_3N_4

- M = Mg
- RE = La, Lu



G.B. Winkelman, C. Dwyer, D.J.H. Cockayne, 1Department of Materials, University of Oxford

Bi₂O₃-doped ZnO: Interfacial & Surficial Films



Equilibrium Films Determined By Detailed Balance

- Of Dispersion Forces
- And Other Forces

J. Luo, H. Wang, and Y.-M. Chiang, "Origin of Solid-State Activated Sintering in ZnO-Bi₂O₃," *J. Am. Ceram. Soc.*, **82**[4] 916-20 (1999).

Optical Properties And Electronic Structure



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Bulk: VUV- LPLS Spectrophotometer

Laser Plasma Light Source

- Samarium

Spectral Range

- 1.5 to 44 eV
- 700 to 28 nm

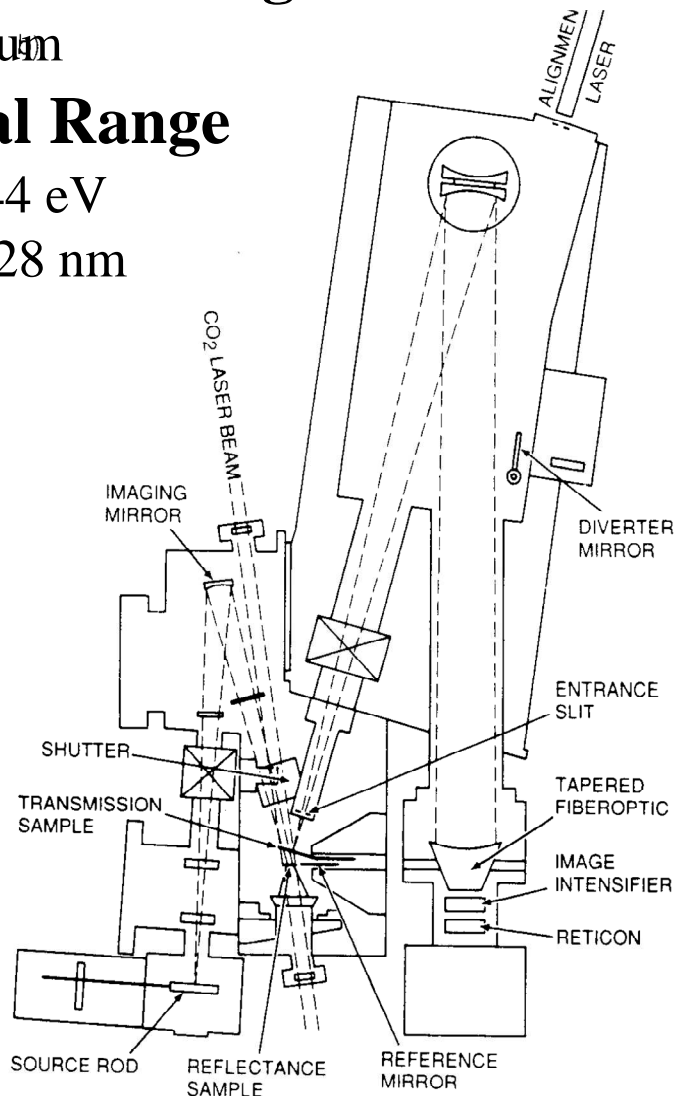
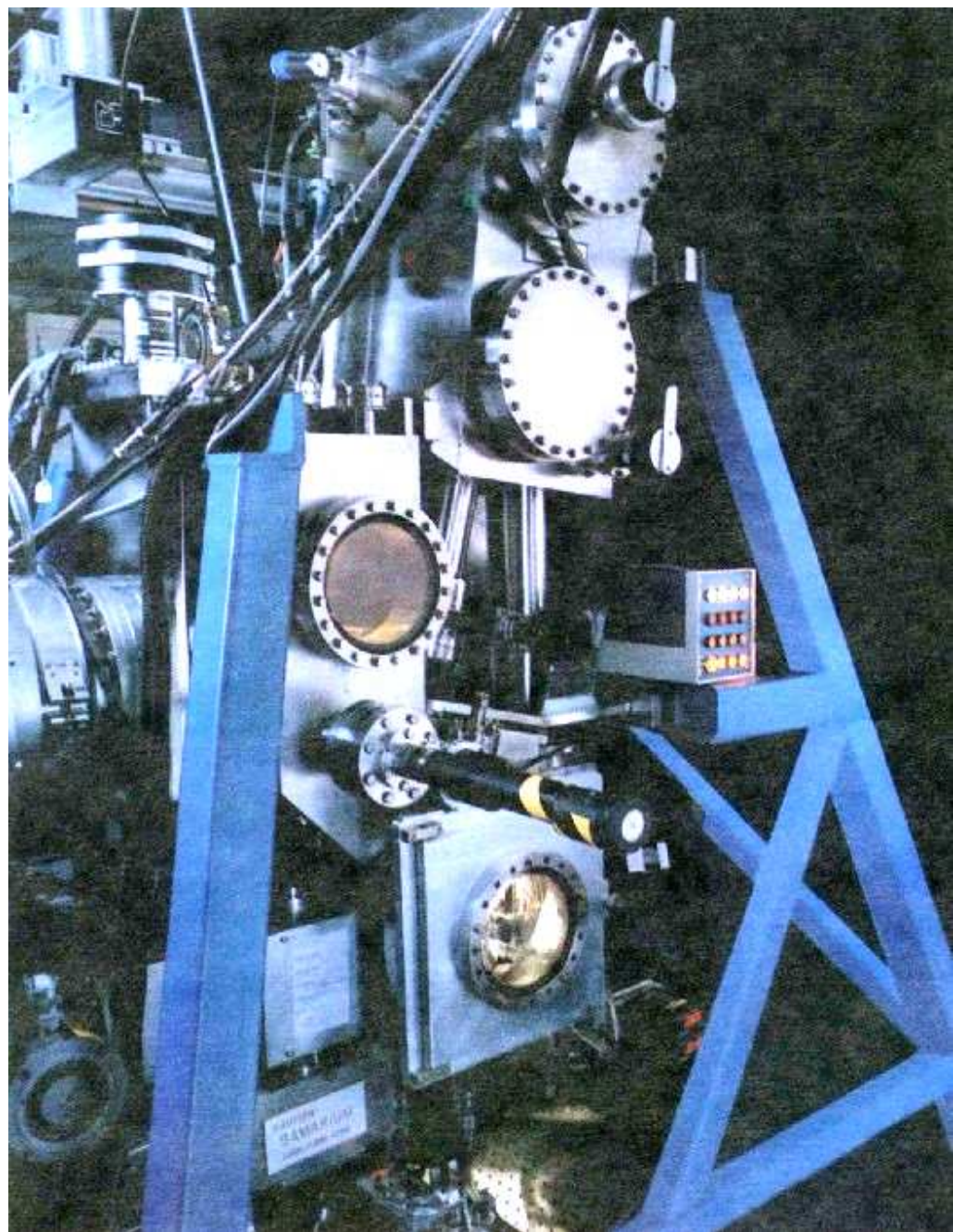


Fig. 1. (q) Block diagram of the major elements of the LPLS spectrophotometer. (b) schematic representations of the LPLS spectrophotometer.



M. L. Bortz, R. H. French, *Applied Physics Letters*, **55**, 19, 1955-7, Nov. 8, (1989).
R. H. French, *Physica Scripta*, **41**, 4, 404-8, (1990).

VUV Reflectance and Interband Transitions

VUV Reflectance

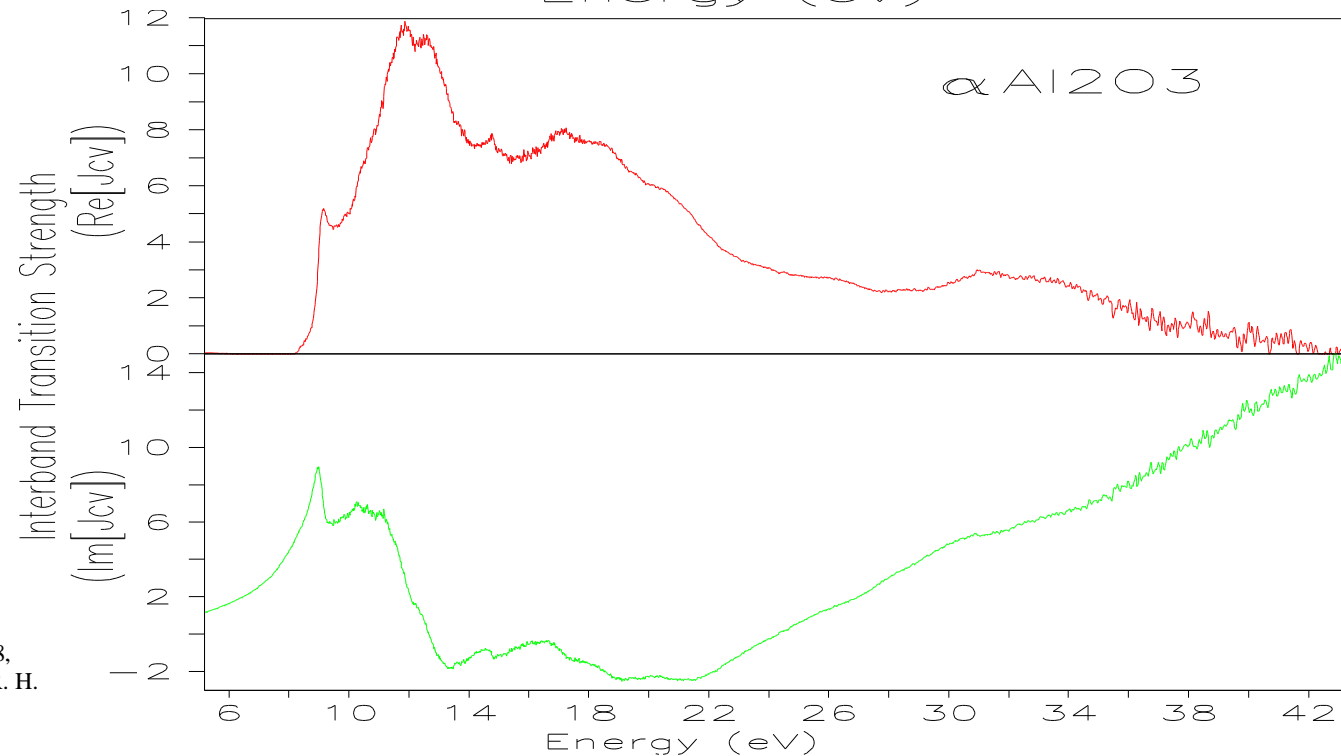
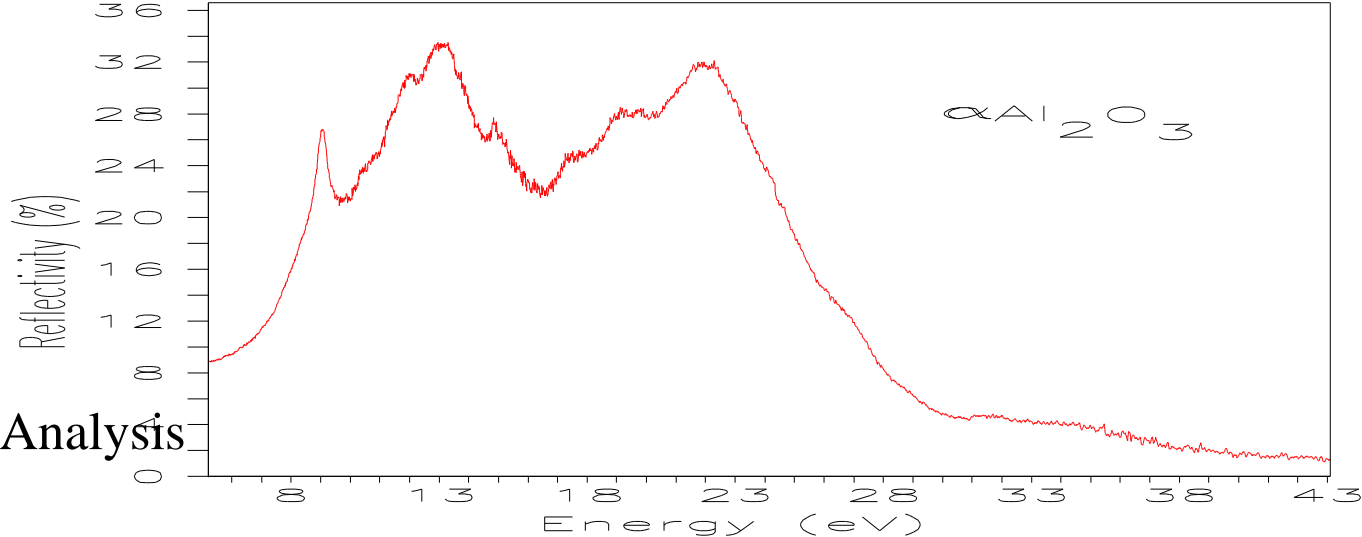
- Linear Response Func.

$$\theta(E) = -\frac{2E}{\pi} \text{P} \int_0^{\infty} \frac{\ln\{\rho(E')\}}{E'^2 - E^2} dE'$$

Kramers Kronig Dispersion Analysis

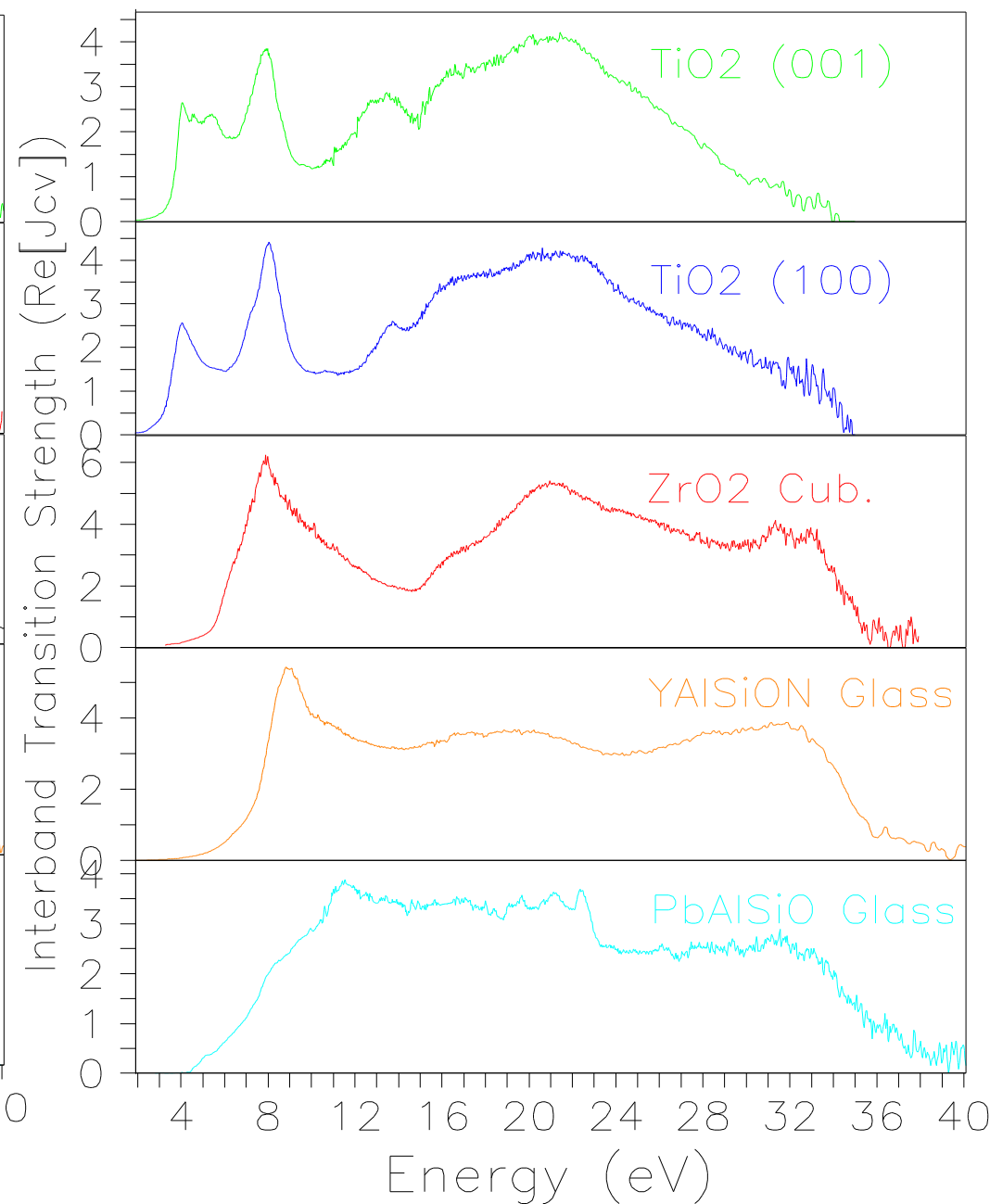
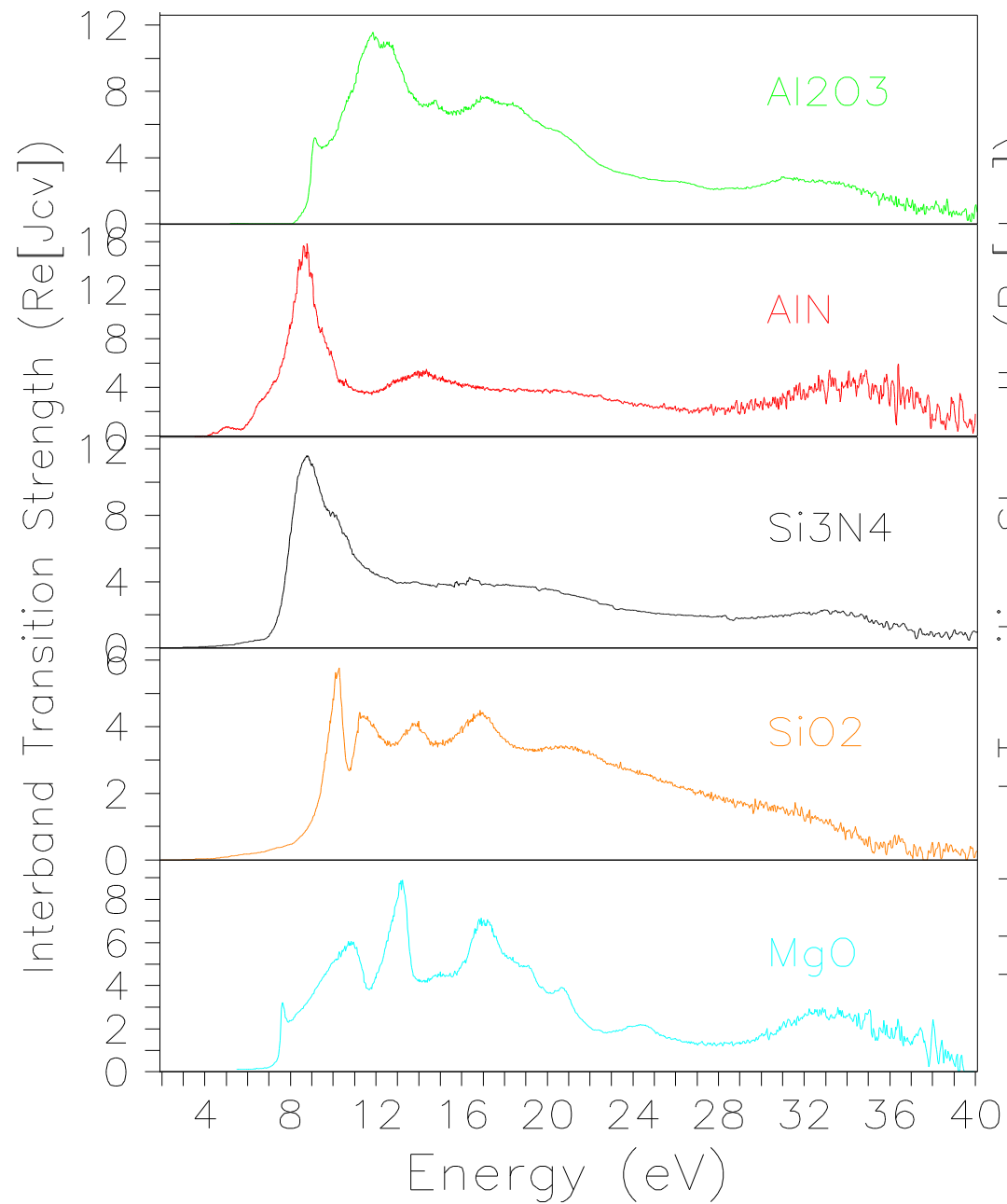
Interband Transition Strength

$$J_{cv} = i \frac{E^2}{8\pi^2} (\epsilon_1 + i\epsilon_2)^*$$



M. L. Bortz, R. H. French, Applied Physics Letters, 55, 19, 1955-7, Nov. 8, (1989). R. H. French, Physica Scripta, 41, 4, 404-8, (1990). M. L. Bortz, R. H. French, Applied Spectroscopy, 43, 8, 1498-1501, (1989).

Electronic Structure of Ceramics



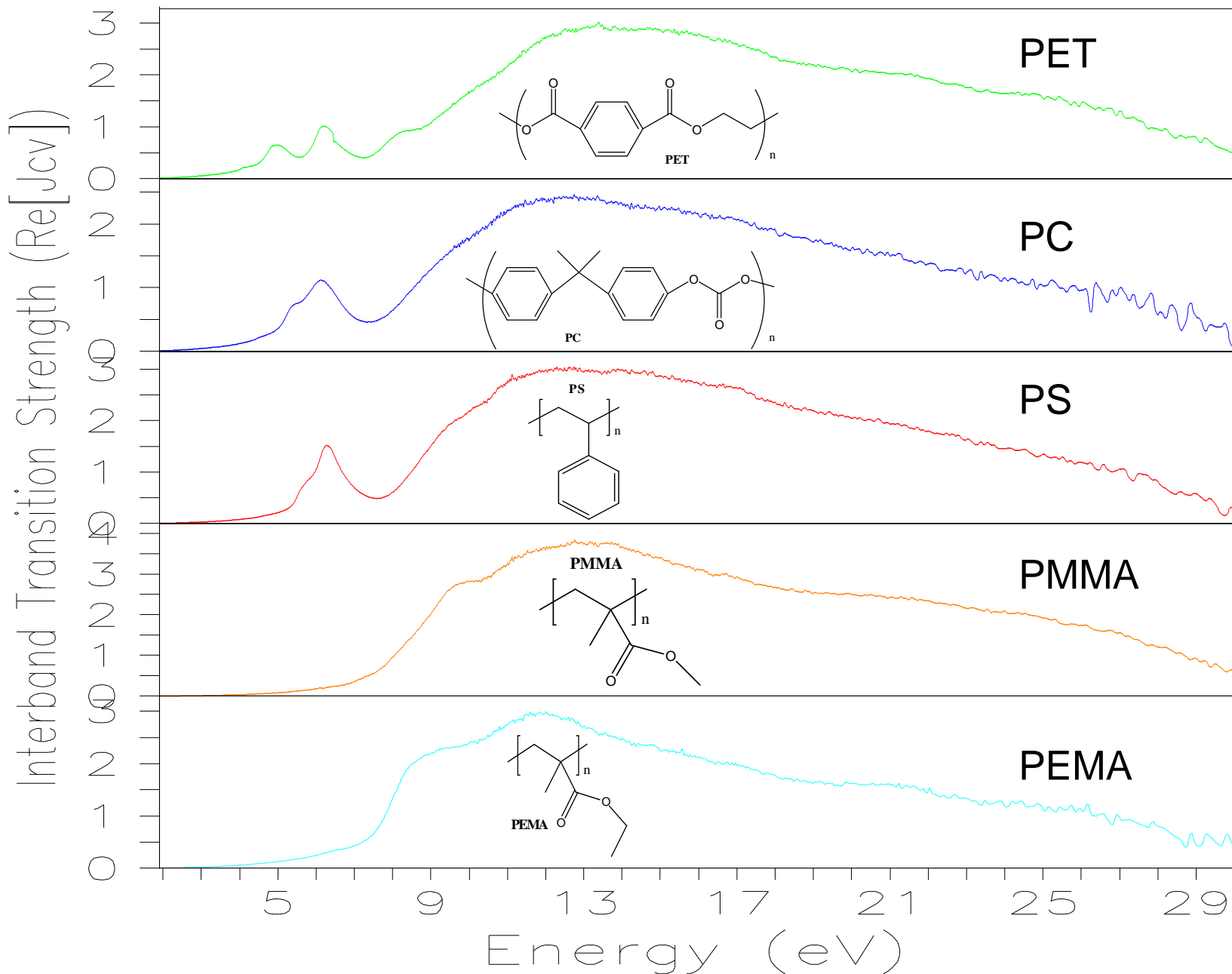
Electronic Structure of Polymers

Hierarchy Of Transitions

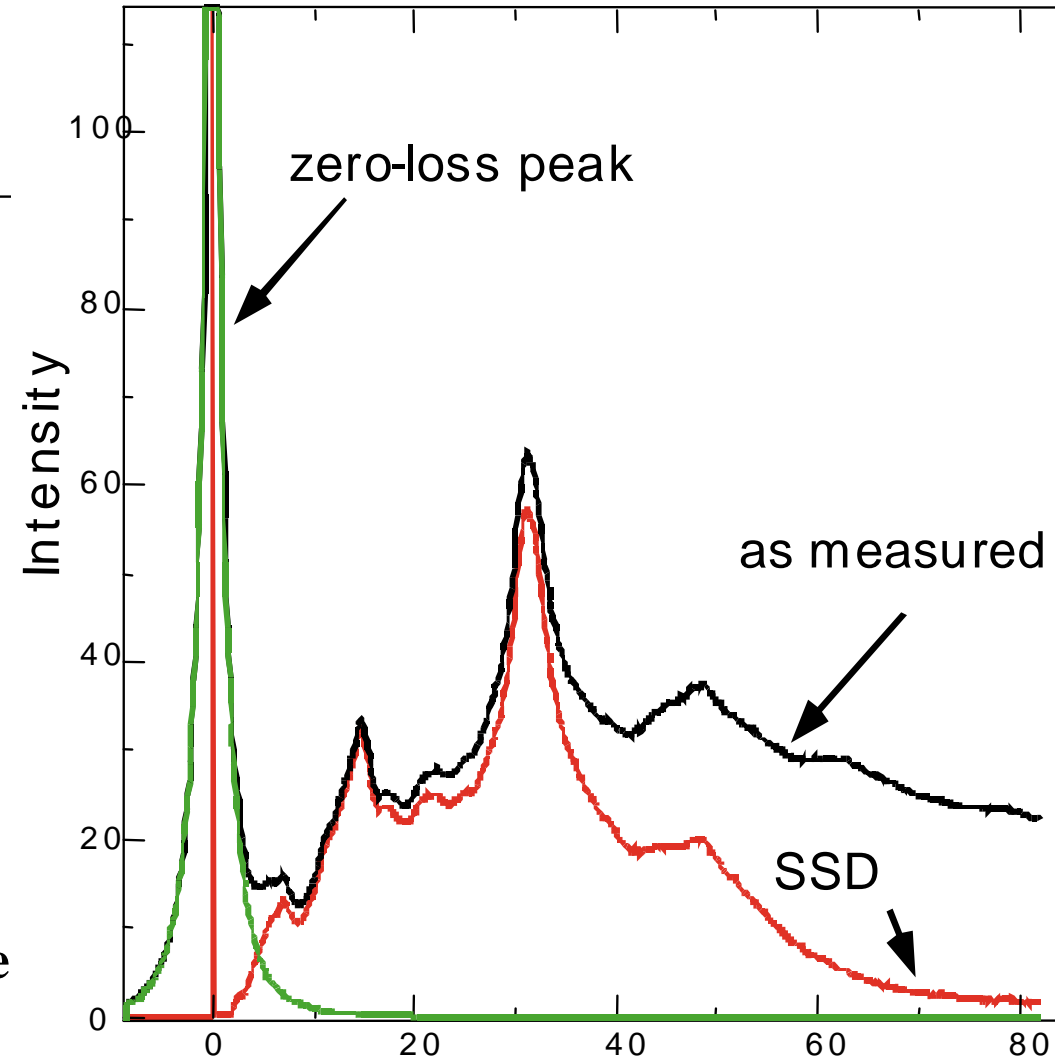
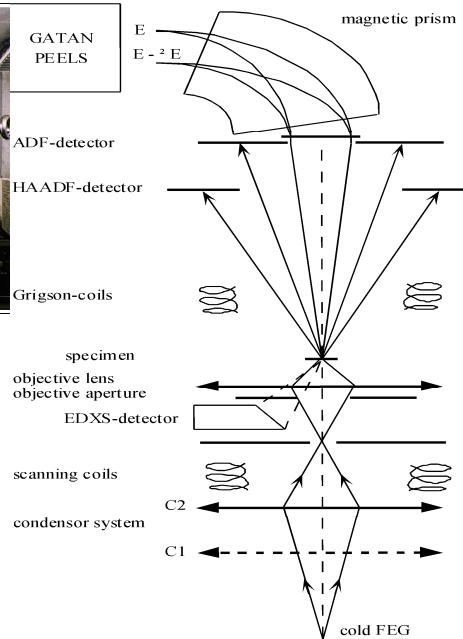
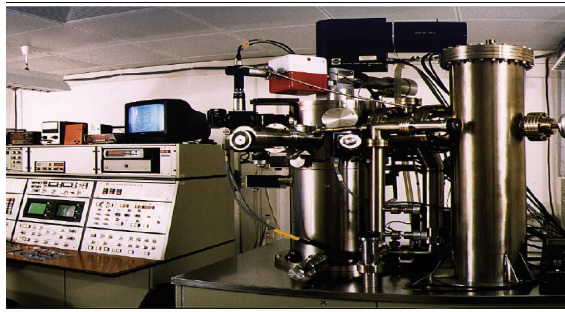
- Aromatic:
 - $\pi \rightarrow \pi^*$
- Carbonyl:
 - $n \rightarrow \sigma^*$,
- C-C Backbone:
 - $\sigma \rightarrow \sigma^*$

Dimensionality Of Transitions

- Critical Points
- Or Spectral Lineshapes



Interfaces: Valence Electron Energy Loss Spectroscopy



Energy Loss (eV)
 Single Scattering Deconvolution
 Kramers Kronig Analysis
 London Dispersion Transform

Energy Loss Function

- An Optical Property

Energy Loss Regimes

- Core EELS:
- Near Edge EELS:
- **Valence EELS:**
 - Interband Electronic Structure
 - Too Complex To Analyze?

Scanning Transmission Electron Microscope Spatially Resolved Microscopy

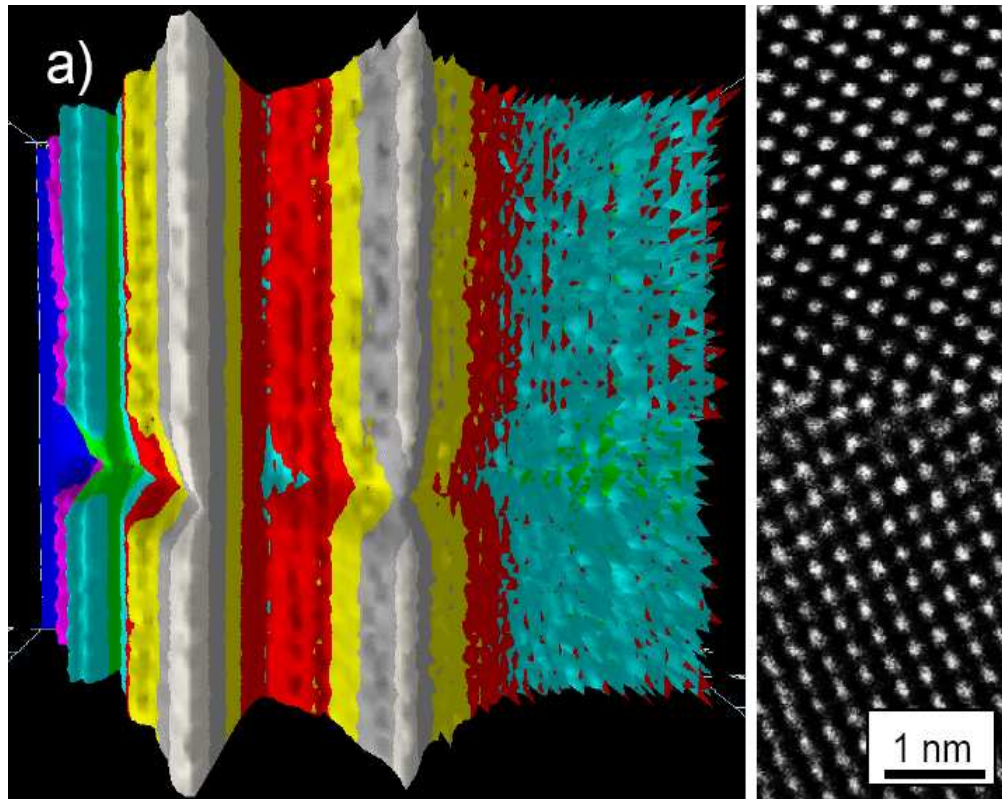
- Probe Size: ~1.0 nm
- Energy Resolution: 0.6 eV
- Linescans (100 Spectra in 40 nm)

R. H. French, et. al., *Acta Materialia*, **46**, 7, 2271-87, (1998). A. D. Dorneich, et. al., *J. Microscopy*, **191**, 3, 286-96 (1998).

SrTiO₃:Fe Bicrystals

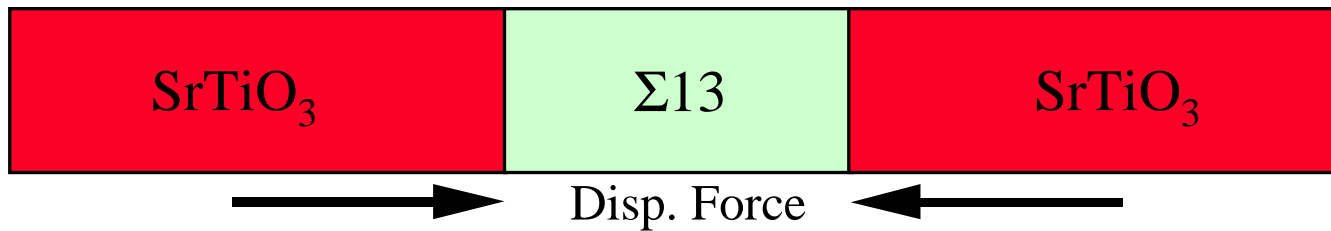
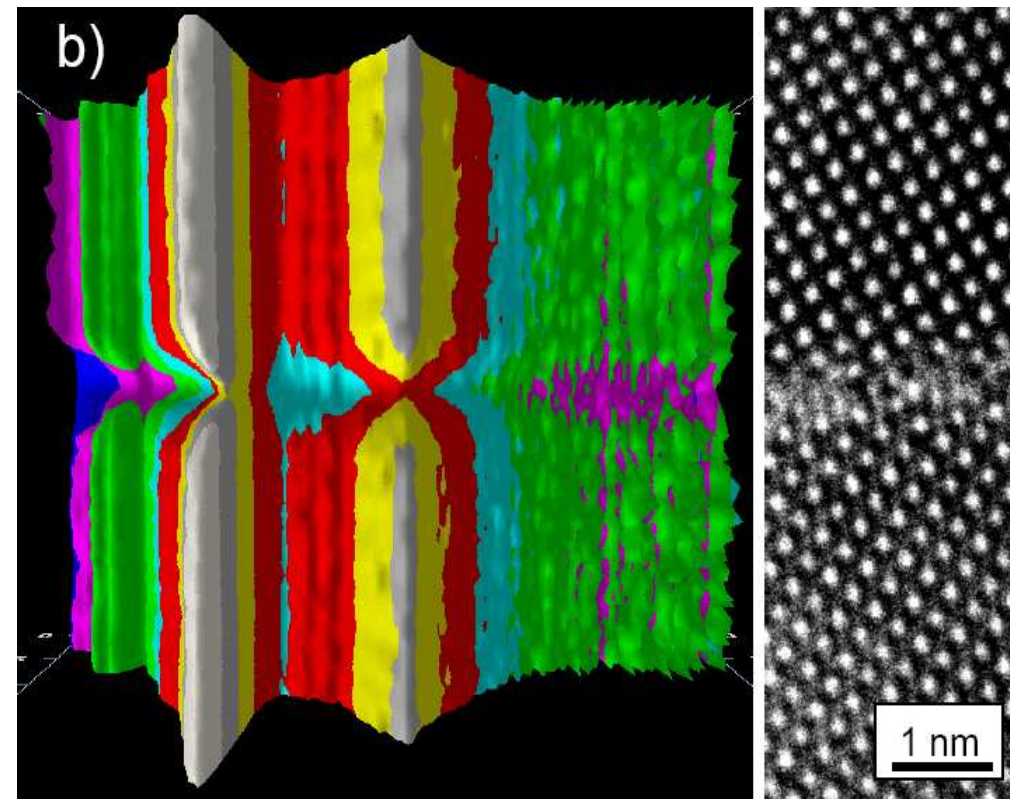
Σ 5 Boundary

- Atomically Structured



$n\Sigma$ 13 Boundary

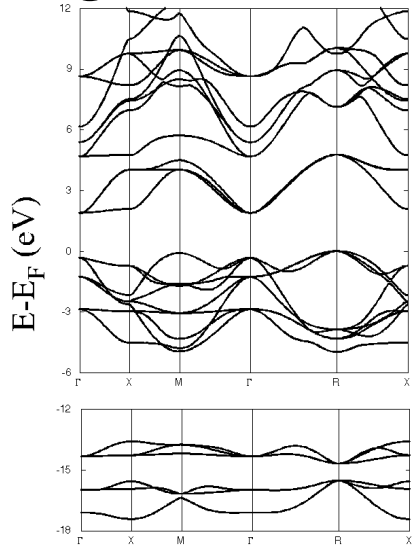
- Atomically Structured



K. van Benthem, G. L. Tan, L. K. Denoyer, R. H. French, M. Rühle, **Phys. Rev. Lett.**, **93**, 227201, (2004),
 K. van Benthem, G. Tan, R. H. French, L. K. Denoyer, R. Podgornik, V. A. Parsegian, **Phys. Rev. B**, **74**, (2006).

SrTiO₃ $\Sigma 5$ & $\Sigma 13$ Interfacial Electronic Structure

Assignments: LDA Band Structure Calc.



Loss of Transitions

- From O2p
- To Ti3d

Removal of Ti

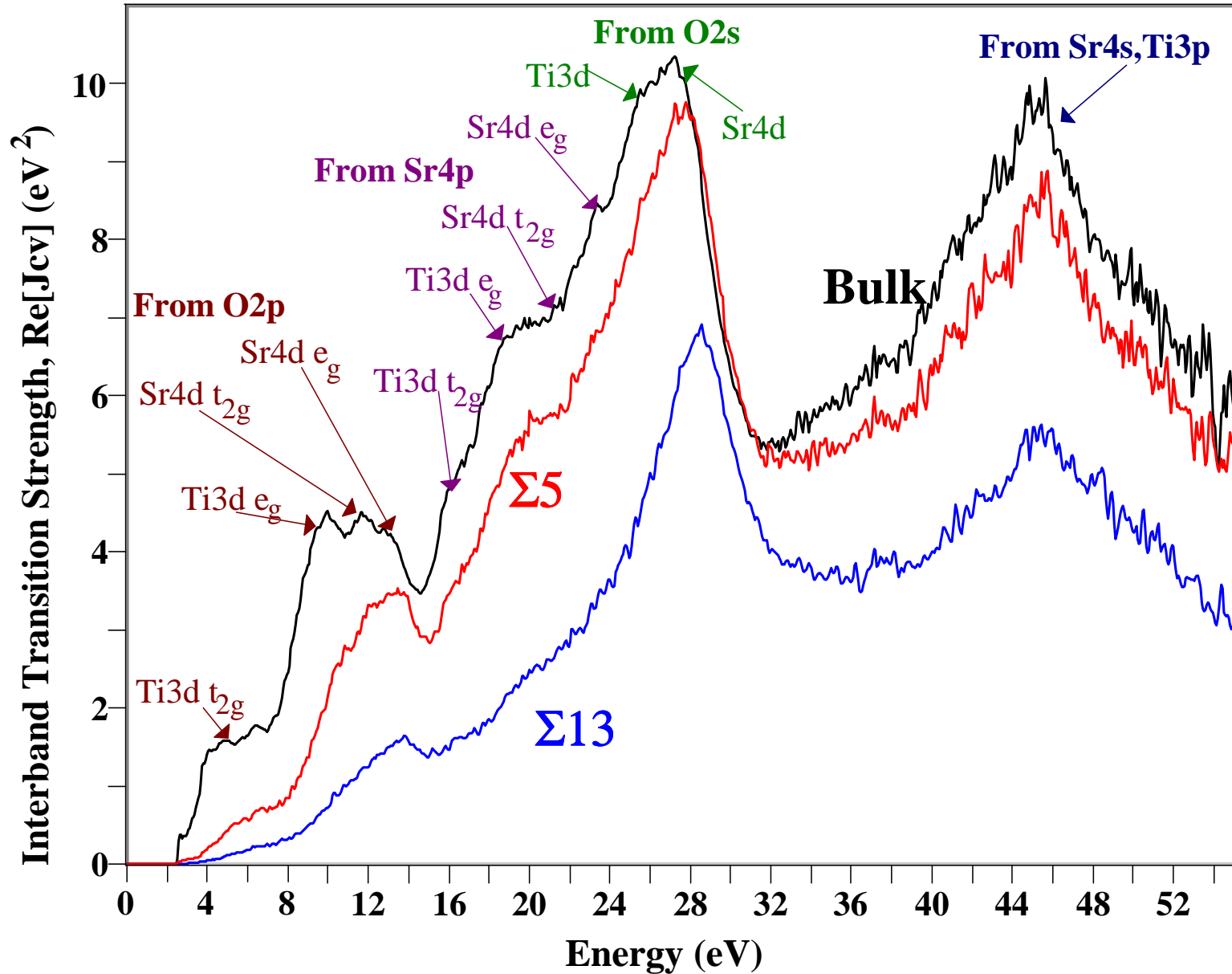
- In Boundary

$\Sigma 5$ GB

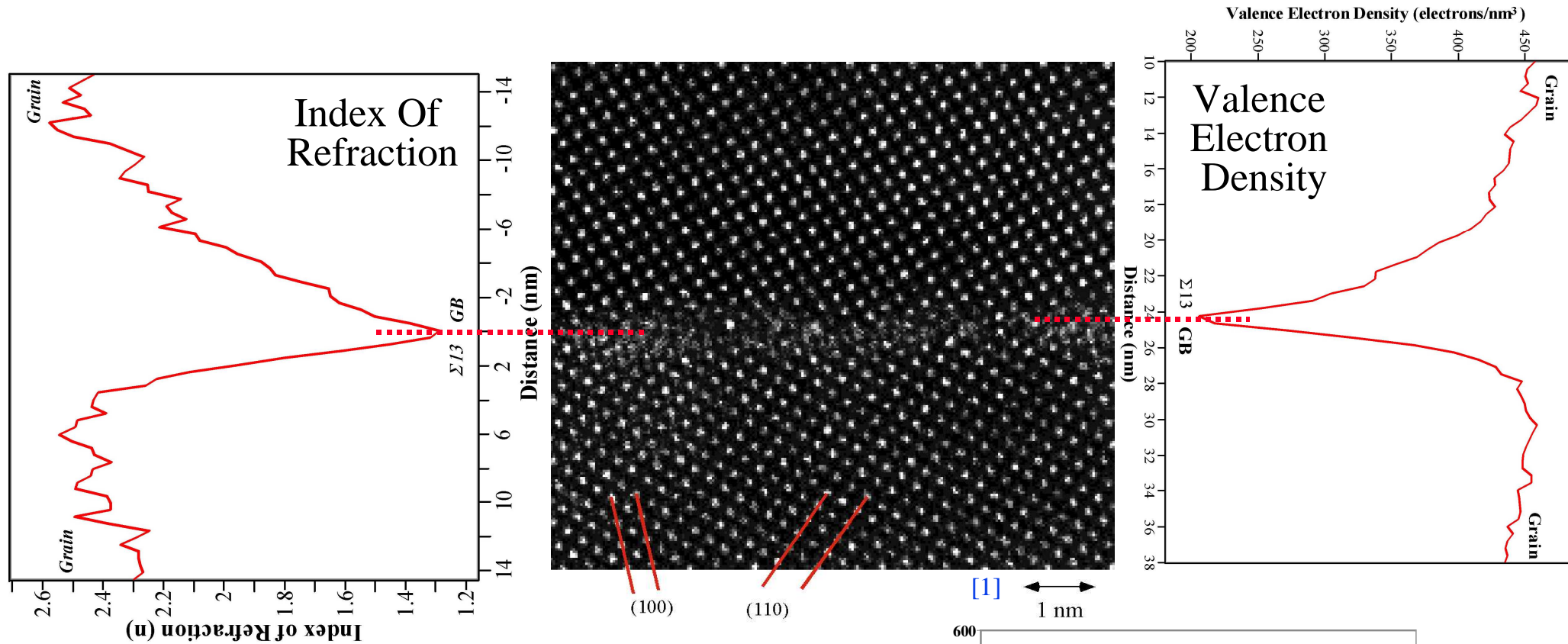
- Ti3d t_{2g} Reduced
- Sr Present

$\Sigma 13$ GB

- Ti3d t_{2g} Reduced
- Sr Present



Measured Properties Gradients At Grain Bndry

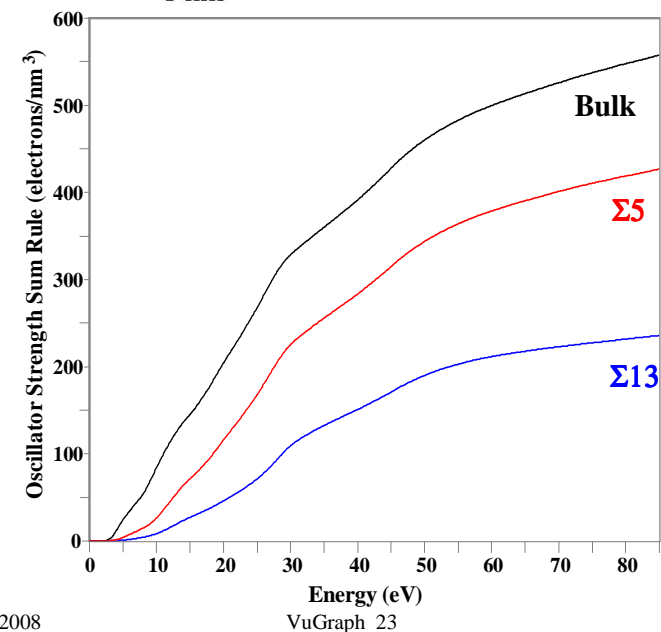


$n\Sigma13$ Grain Boundary In SrTiO_3

- Valence EELS in STEM

Measure GB Core

- Index Of Refraction
- Electron Density / nm^3



van der Waals – London

Dispersion Interactions



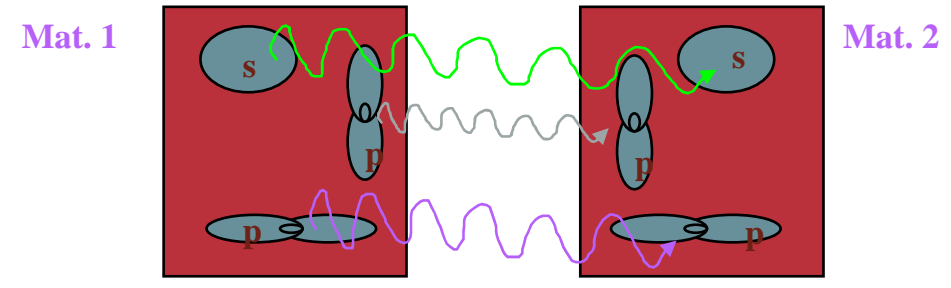
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Origin of The London Dispersion Interaction

van der Waals-London Dispersion Interactions

- Thermodynamic Free Energy



Arise From Oscillating Dipoles

- Interatomic Bonds of Elect. Struc.

J_{cv} , $\epsilon'' \Rightarrow$ London Disp. Spectra

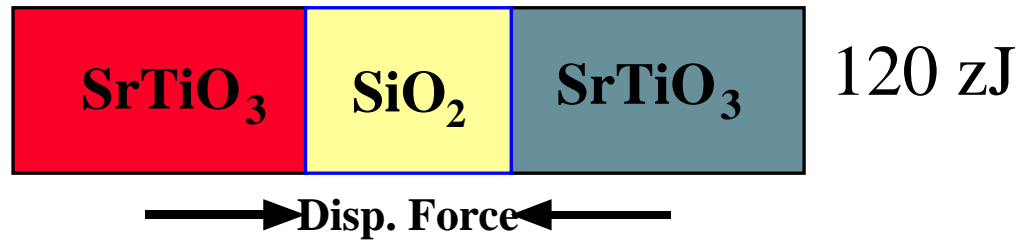
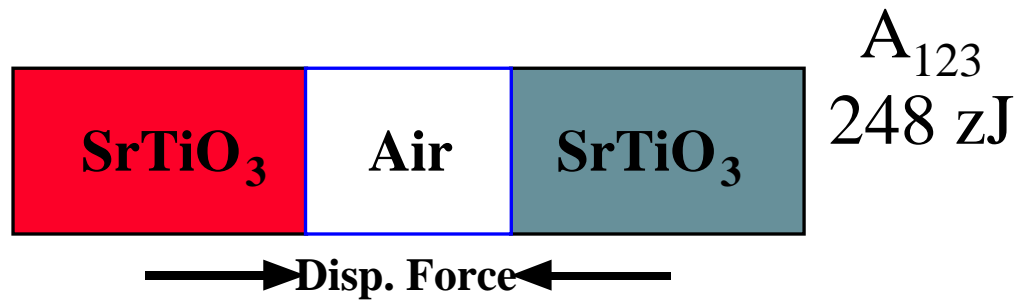
A - Hamaker Constant

- F_{disp} - Dispersion Force

$$E_{London\ Dispersion} = -\frac{A(l)}{12\pi l^2}$$

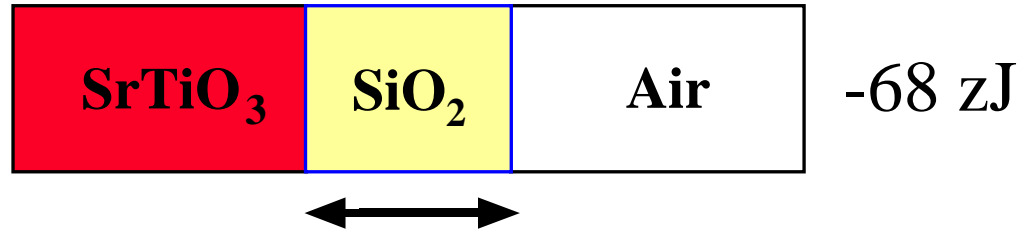
Attractive Force: Nonwetting

- Positive Hamaker Constant



Repulsive Force: Wetting

- Negative Hamaker Constant



Full Spectral Hamaker Constants

Using Lifshitz Theory, QED

- Acquire Exp. Spectra
- Calc. London Disp. Spectrum
 - Kramers Kronig Transform

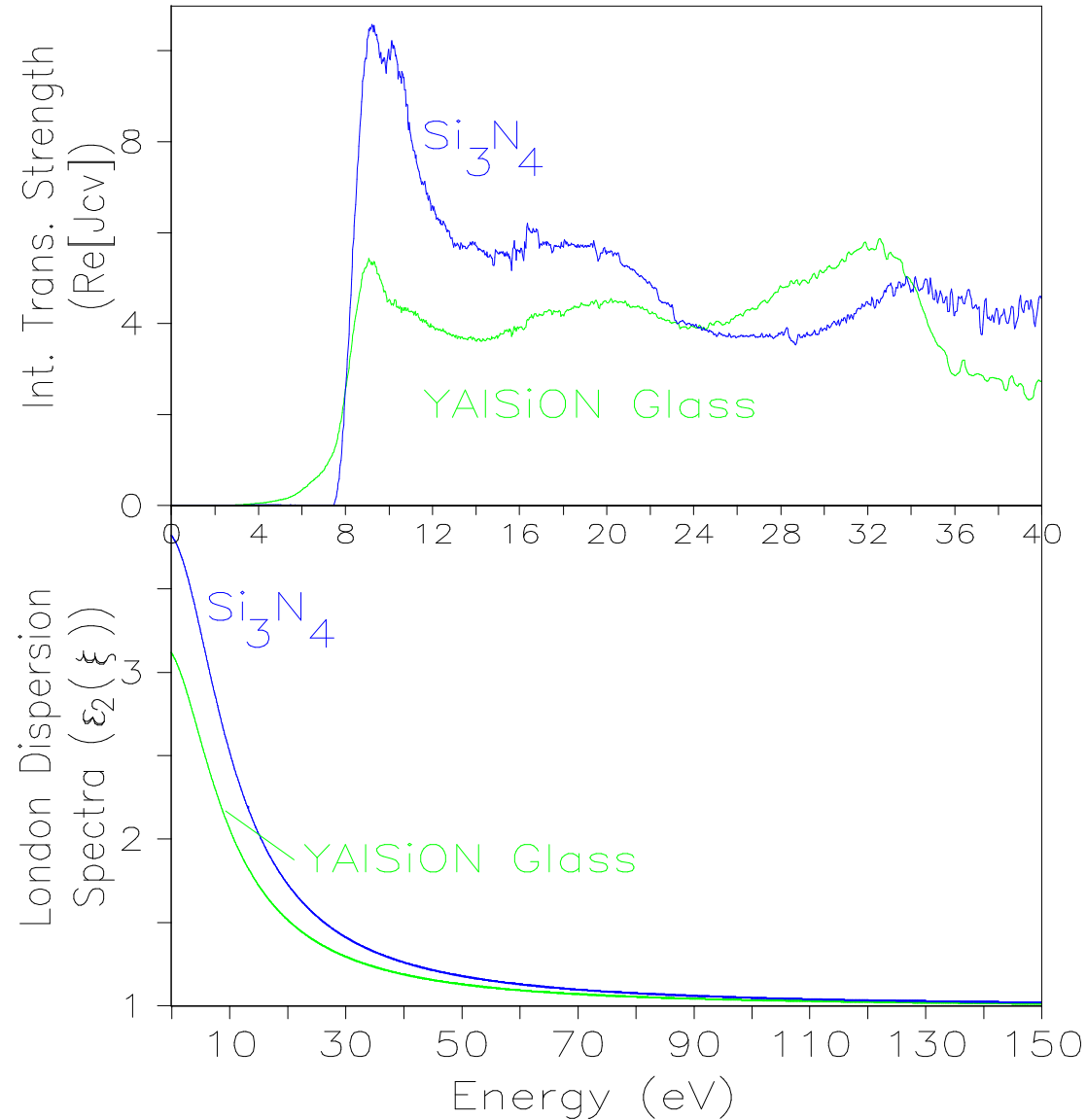
$$\epsilon_2(\xi) = 1 + \frac{2}{\pi} \int_0^{\infty} \frac{\omega \epsilon_2(\omega)}{\omega^2 + \xi^2} d\omega$$

- Then Hamaker Constant
 - Calc'd by Spectral Differences
 - of London Disp. Spectra

$$A = \frac{-3\eta L^2}{\pi} \int_0^{\infty} \rho d\rho \int_0^{\infty} \ln G(\xi) d\xi$$

$$G_{121}^{NR}(\xi) = 1 - \Delta_{12}^2 e^{-2a\rho}$$

$$\Delta_{kj} = \frac{\epsilon_{2,k}(\xi) - \epsilon_{2,j}(\xi)}{\epsilon_{2,k}(\xi) + \epsilon_{2,j}(\xi)}$$



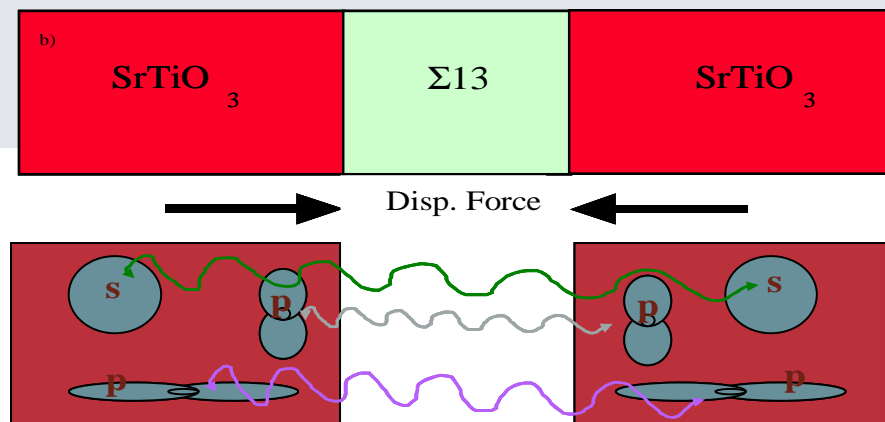
$$A(\text{Si}_3\text{N}_4 | \text{Vac.} | \text{Si}_3\text{N}_4) = 192 \text{ zJ}$$

$$A(\text{Si}_3\text{N}_4 | \text{YAlSiON} | \text{Si}_3\text{N}_4) = 9.3 \text{ zJ}$$

$$\text{zJ} = 10^{-21} \text{ Joules}$$

vdW-Ld Energies of Grain Boundaries

Atomically Structured $\Sigma 5$ and $n\Sigma 13$ SrTiO_3 Grain Boundaries

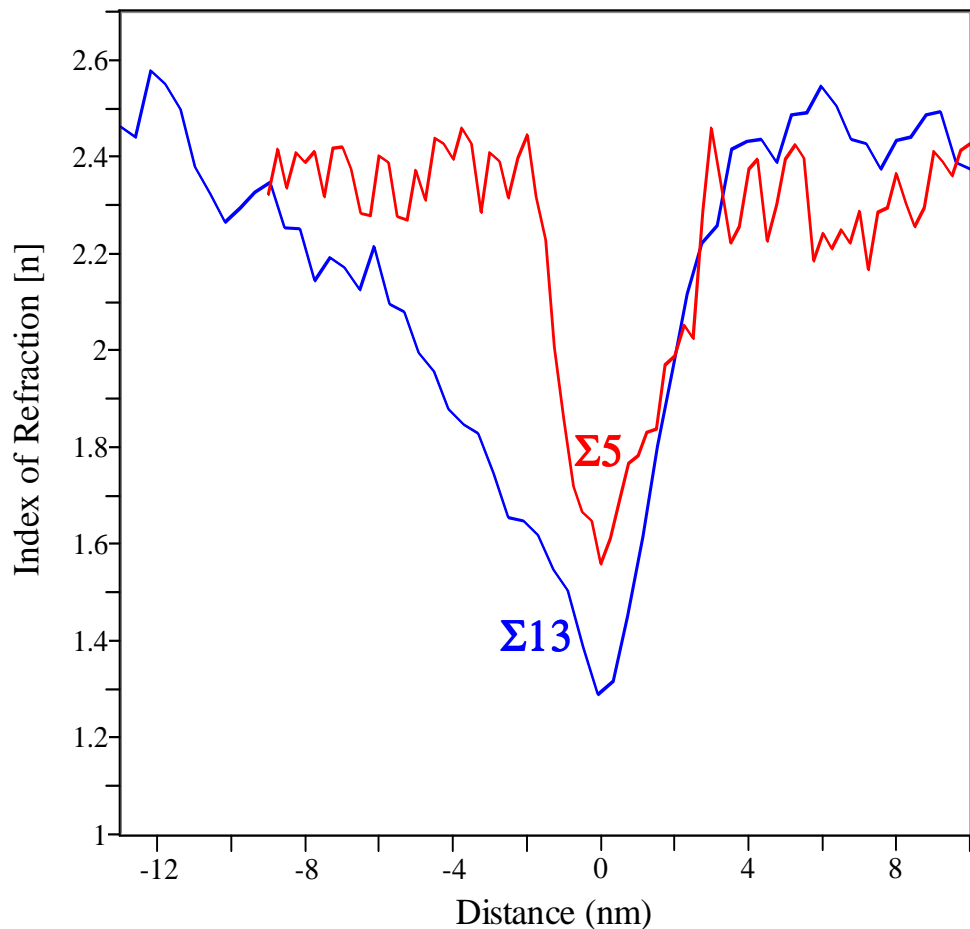


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K. van Benthem, G. L. Tan, L. K. Denoyer, R. H. French, M. Rühle, **Phys. Rev. Lett.**, **93**, 227201, (2004),
K. van Benthem, G. Tan, R. H. French, L. K. Denoyer, R. Podgornik, V. A. Parsegian, **Phys. Rev. B**, **74**, (2006).

Gradient Properties in Grain Boundaries of SrTiO₃

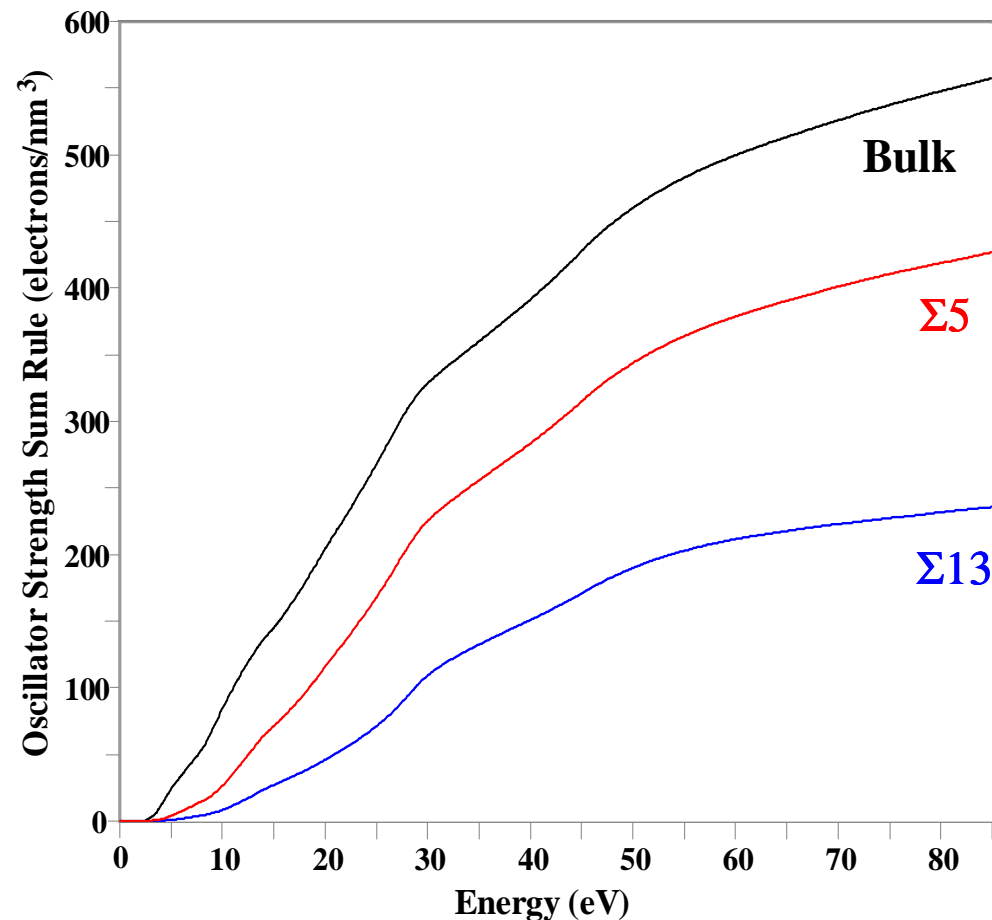


Index of Refraction

- $\Sigma 5$ Grain Boundary = 1.56
- $n\Sigma 13$ Grain Boundary = 1.29

$n=2.37$ for bulk SrTiO₃,

- Spectroscopic Ellipsometry.²²



Valence Electron Density Variations

- From Oscillator Strength Sum Rule

Units of Electrons Per nm³

- for bulk SrTiO₃ $\Sigma 5$ and $n\Sigma 13$ GB

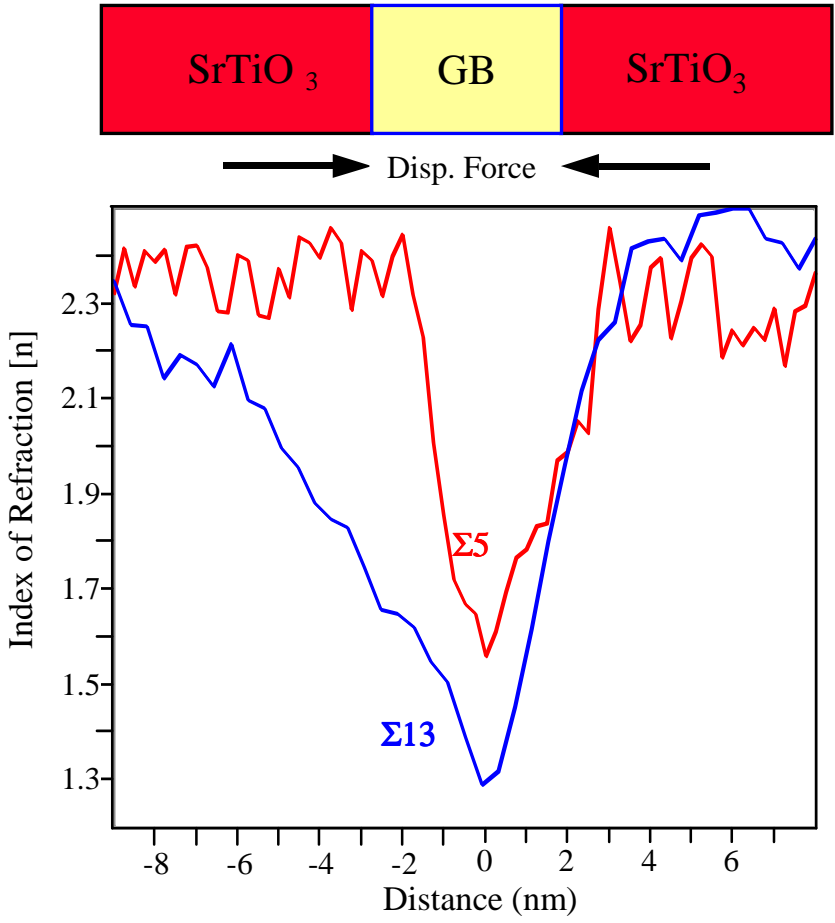
K. van Benthem, C. Elsässer, R. H. French, *J. Appl. Phys.*, **90**, 12, 6156-64, (2001), K. van Benthem, et al., *Phys. Rev. Lett.*, **93**, 227201, (2004), K. van Benthem, et al., *Phys. Rev. B*, **74**, 205110, (2006).

Grain Boundary Dispersion Interaction: A_{121}

A_{121} Hamaker Constants

- With Sharp Interfaces

Use Of “Bulk” Hamaker?



Interface	A_{121}^{NR} (zJ)
SrTiO ₃ vac. SrTiO ₃ $d_0=0.195$ nm	243.9
SrTiO ₃ $\Sigma 13$ SrTiO ₃ $d_0=0.195$ nm	105.5
SrTiO ₃ $\Sigma 5$ SrTiO ₃ $d_0=0.195$ nm	35.0
SiO ₂ vac. SiO ₂ $d_0=0.165$ nm	68.2

$$E_{London} = -\frac{A(l)}{12\pi l^2}$$

$\Sigma 13$ Grain Boundary: Larger Disp. Int.

- Than A (SrTiO₃ | Silica | SrTiO₃) = 71 zJ
- Than A (SiO₂ | Vacuum | SiO₂) = 68.2 zJ

$\Sigma 5$ Grain Boundary: Larger Disp. Int

- Than Most Intergranular Films

K. van Benthem , G. Tan, R. H. French, L. K. Denoyer, R. Podgornik, V. A. Parsegian, *Phys. Rev. B*, **74**, (2006).

A Graded Interface Approach

The Sharp Interfaces of a 1|2|1 Type Model

- Have Unrealistic Infinite Property Gradients

Are These Sharp Interface Results

- Applicable To Grain Boundaries?

Nanoscale Approach To Apply

- Bulk Continuum Dispersion Theory

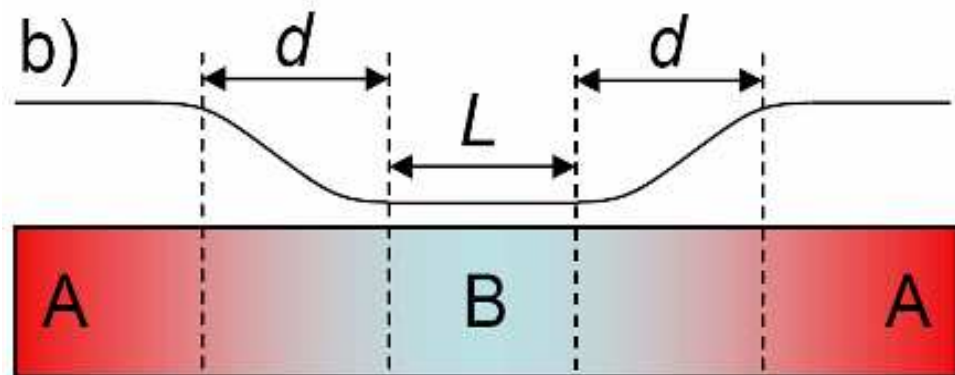
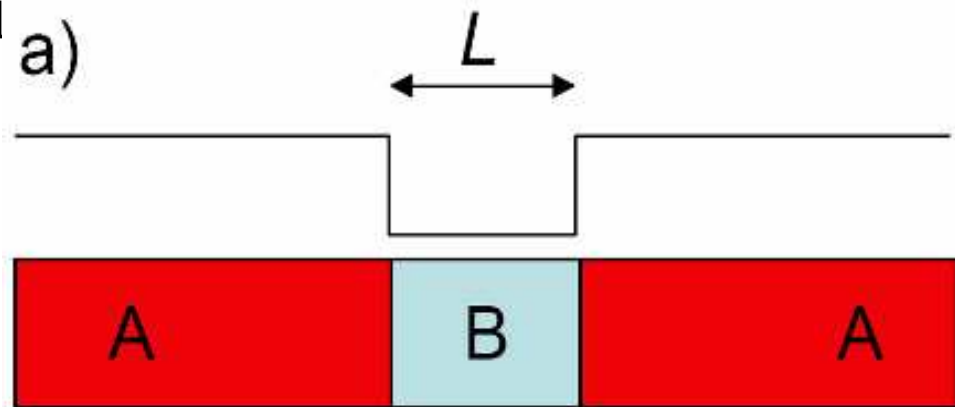
Use Graded Interface Model

- Interfaces With Finite Property Gradients
 - [1 | gradient | 2 | gradient | 1]

Define Finest Length Scale For Gradients

- Use A Characteristic Interatomic Bond Length
 - For SrTiO_3 Use $d_0 = 0.19525$
 - The Ti-O Bond Length in SrTiO_3

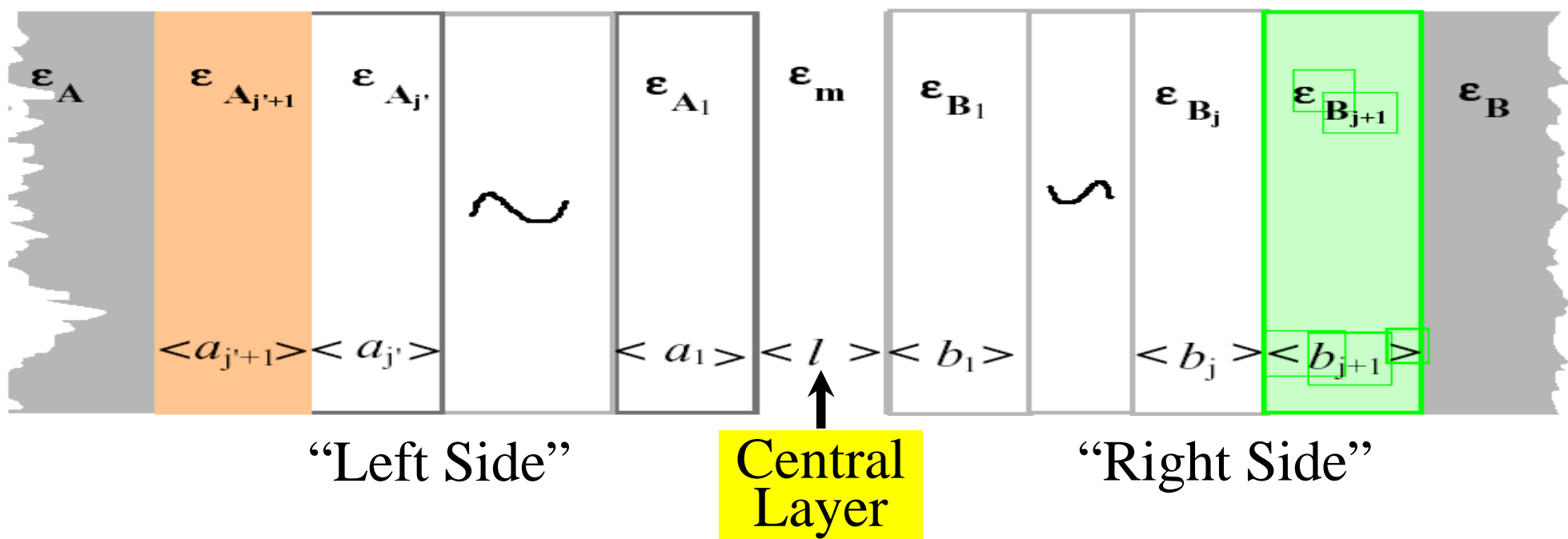
Finest Scale Property Gradients Are Interatomic



K. van Benthem , G. Tan, R. H. French, L. K. Denoyer, R. Podgornik, V. A. Parsegian, **Phys. Rev. B**, 74, (2006).

R. Podgornik, R. H. French, V.A. Parsegian, **J. Chem. Phys.**, 124, 044709, (2006)

Hamaker Coefficients For Arbitrary Multilayers



Previously Only 3 or 5 Layer Hamaker Coefficients Tractable

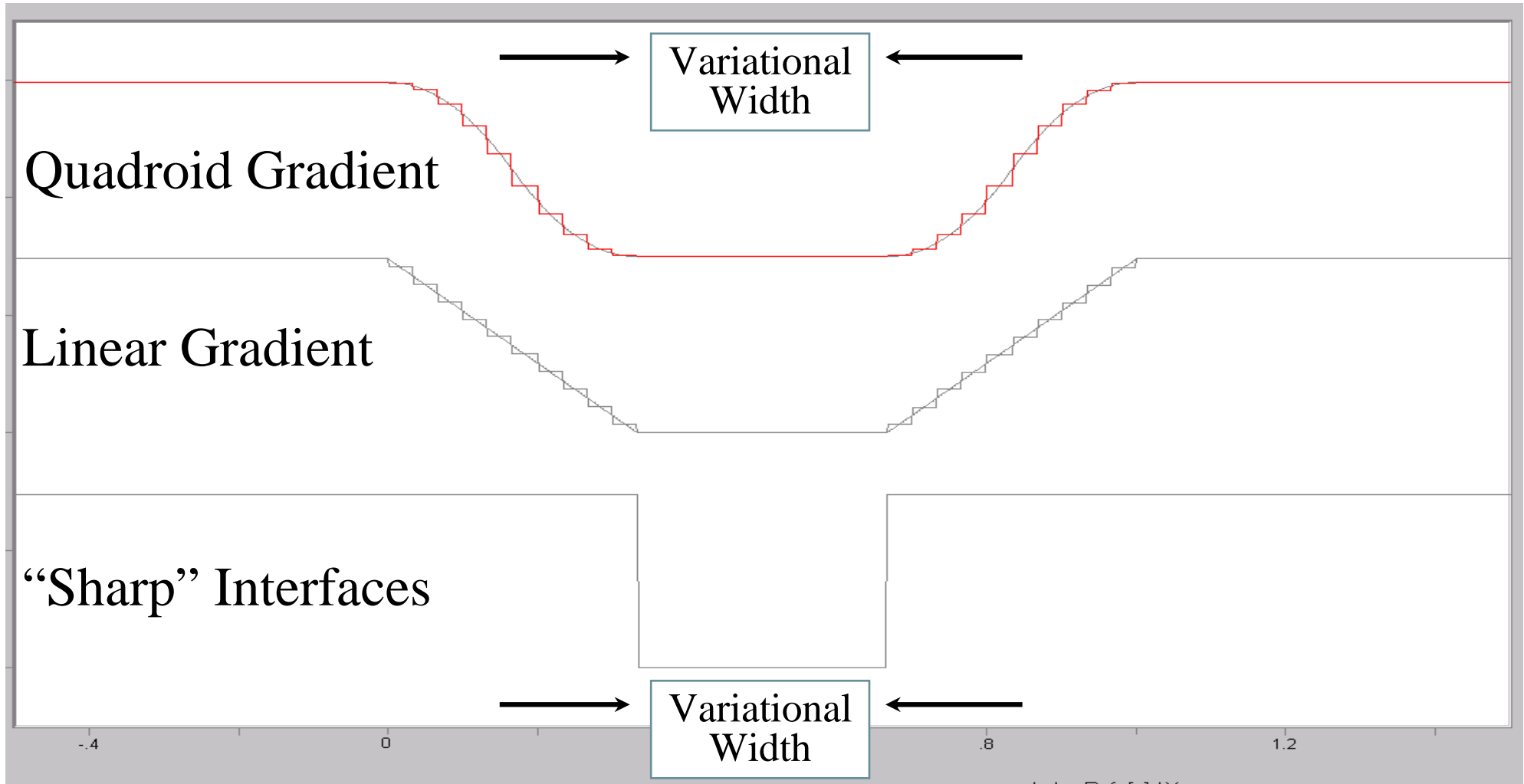
"Add A Layer" Approach

- Matrix Expansion Approach Of Left And Right Half Spaces
- Calculate Effective London Dispersion Spectra
 - For Left and Right Side Of Multilayer Stacks

Fully Retarded Calculations

- Any # of Layers, With A "Central" Layer

Add-A-Layer Method For Quadroid Gradients



vdW-L Dispersion Energies Of GBs

GB Stabilization Energy

- Due To Dispersion

Abrupt Model Results

- ΔE (n Σ 13) = 169 – 73 = **96** mJ/m²
- ΔE (n Σ 5) = 169 – 24 = **145** mJ/m²

Quadroid Graded Interface Model

- ΔE (n Σ 5) = 119 – 14 = **69** mJ/m²
- ΔE (n Σ 13) = 119 – 50 = **105** mJ/m²

Interface	Abrupt Gradient		Double-Quadratic Gradient ^a	
	A_{121}^{NR} (zJ)	E_{London} (mJ.m ⁻²)	A_{121}^R (zJ)	E_{London} (mJ.m ⁻²)
SrTiO ₃ vac. SrTiO ₃ $d_0=0.195$ nm	243.9	169	171.2 (L=0.9 nm)	119
SrTiO ₃ n Σ 13 SrTiO ₃ $d_0=0.195$ nm	105.5	73	72.5 (L=0.9 nm)	50
SrTiO ₃ Σ 5 SrTiO ₃ $d_0=0.195$ nm	35.0	24	20.7 (L=0.6 nm)	14
SiO ₂ vac. SiO ₂ $d_0=0.165$ nm	68.2	66	50.3	49

London Dispersion Stabilization Energies

For These Atomically Abrupt Grain Boundaries Are Appreciable

Compare To Chemical Energies

- Σ 3 GB = 520 mJ/m²
- Surface Energy ~ 1100/mJ/m²

The Role Of Retardation Of vdW-Ld Interactions In Novel Wetting Phenomena



The miracles of science™



Retarded Hamaker Coefficients

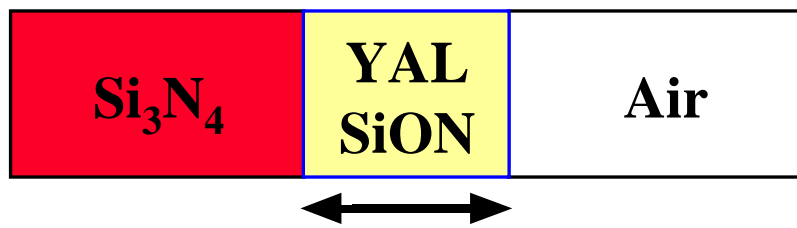
Nonwetting

- Attractive Dispersion Force



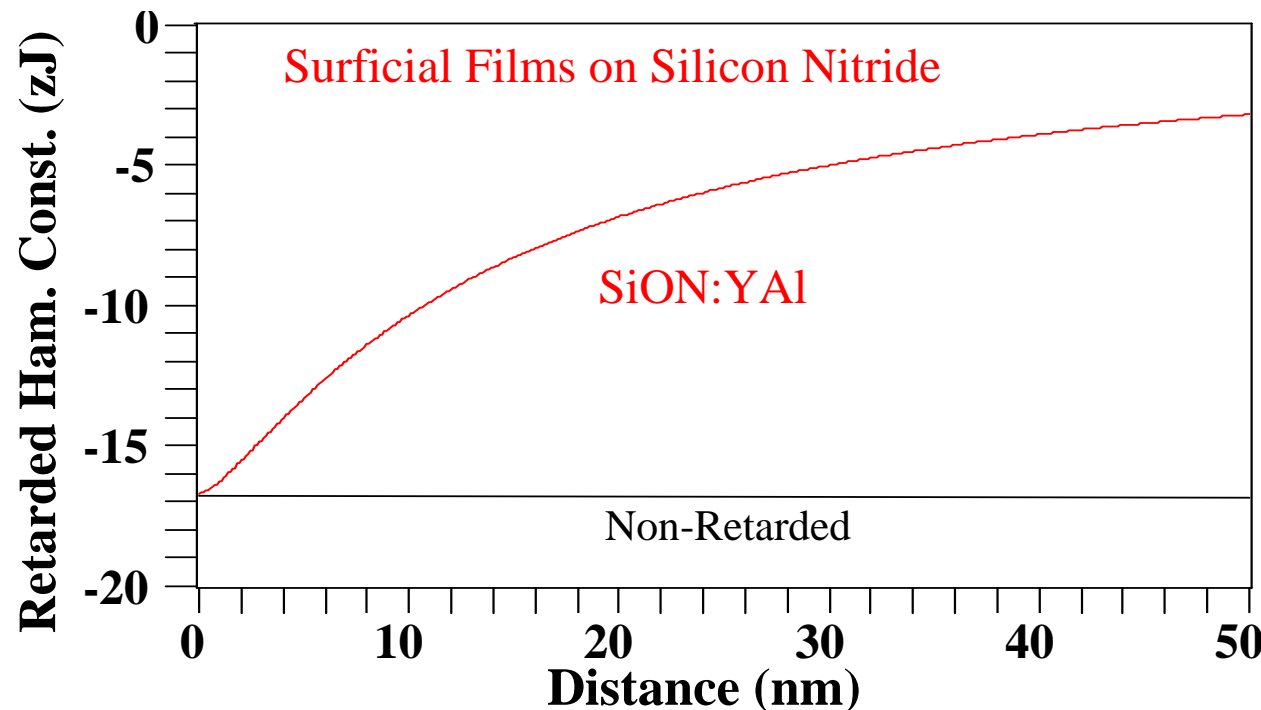
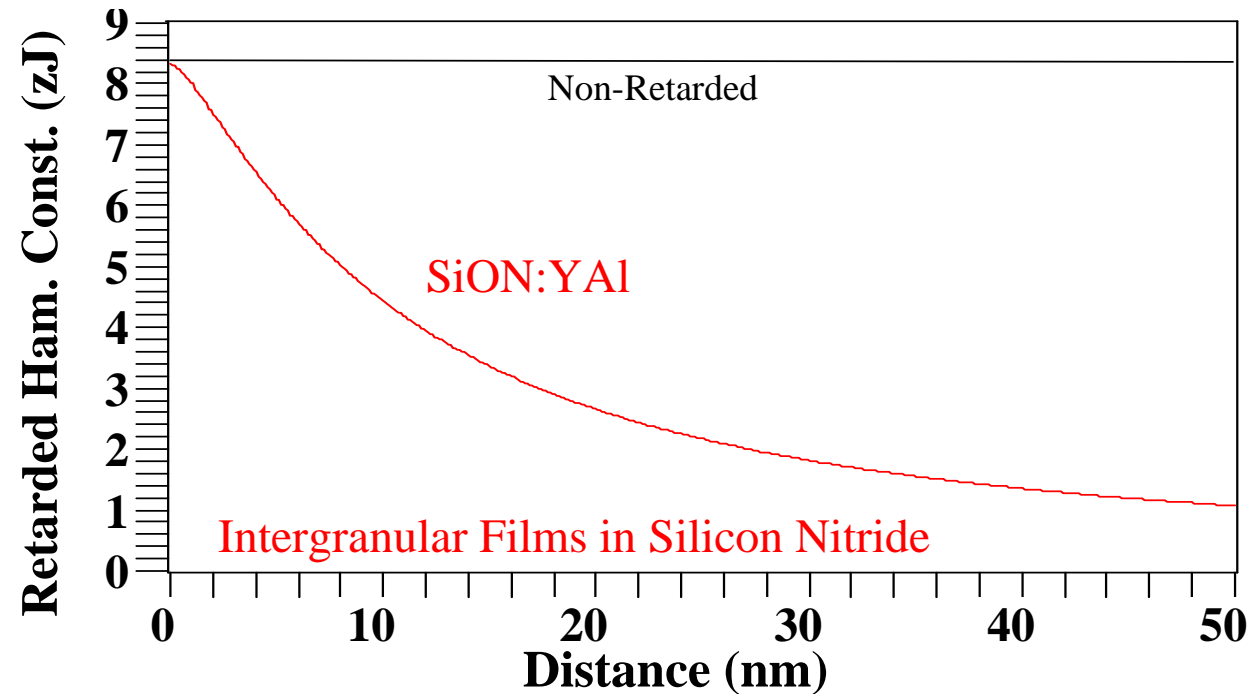
Wetting

- Repulsive Dispersion Force



Retardation Length

- Can Exceed 300 nm
- Depending On Details Of System



Equilibrium Surficial Films Of Water On Ice

Retardation of the London Dispersion Interaction

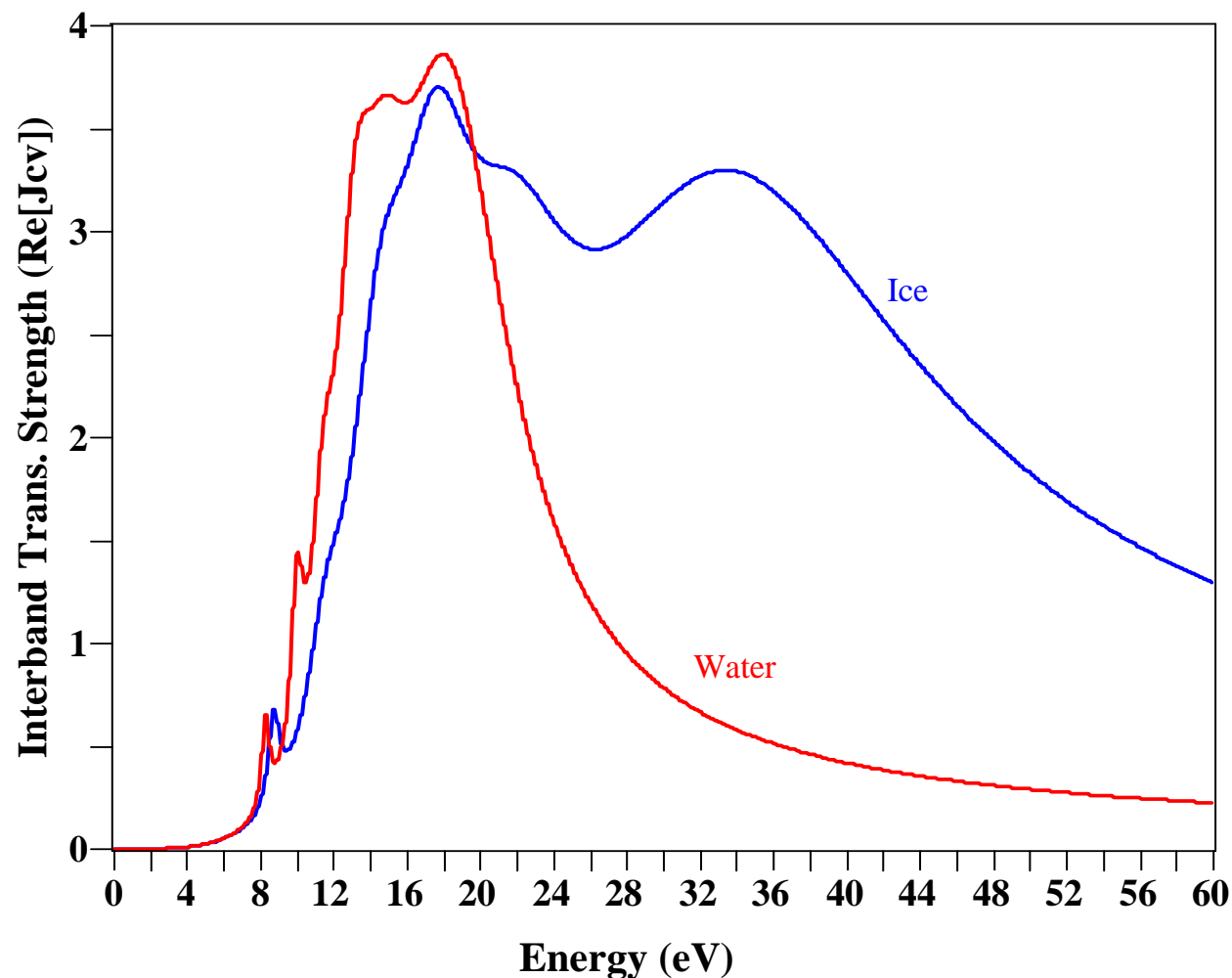
- Leads to Formation Of Surficial Films Of Water On Ice¹
- Surface Premelting

Equilibrium ~3 nm Water Film On Ice

- Persists to -40°C

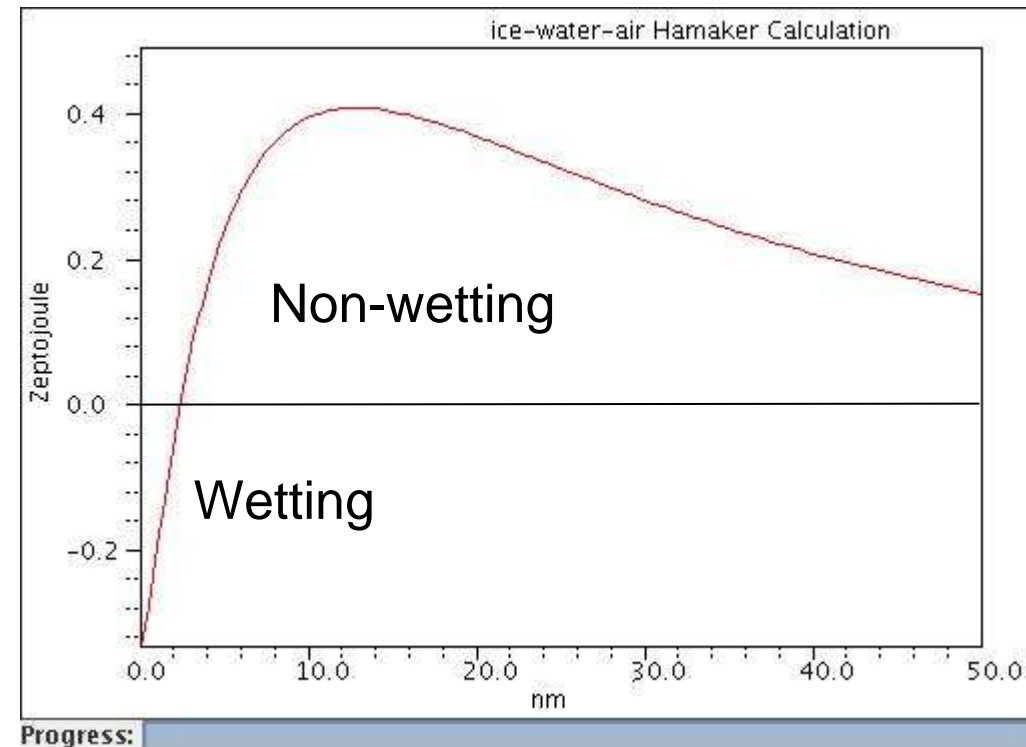
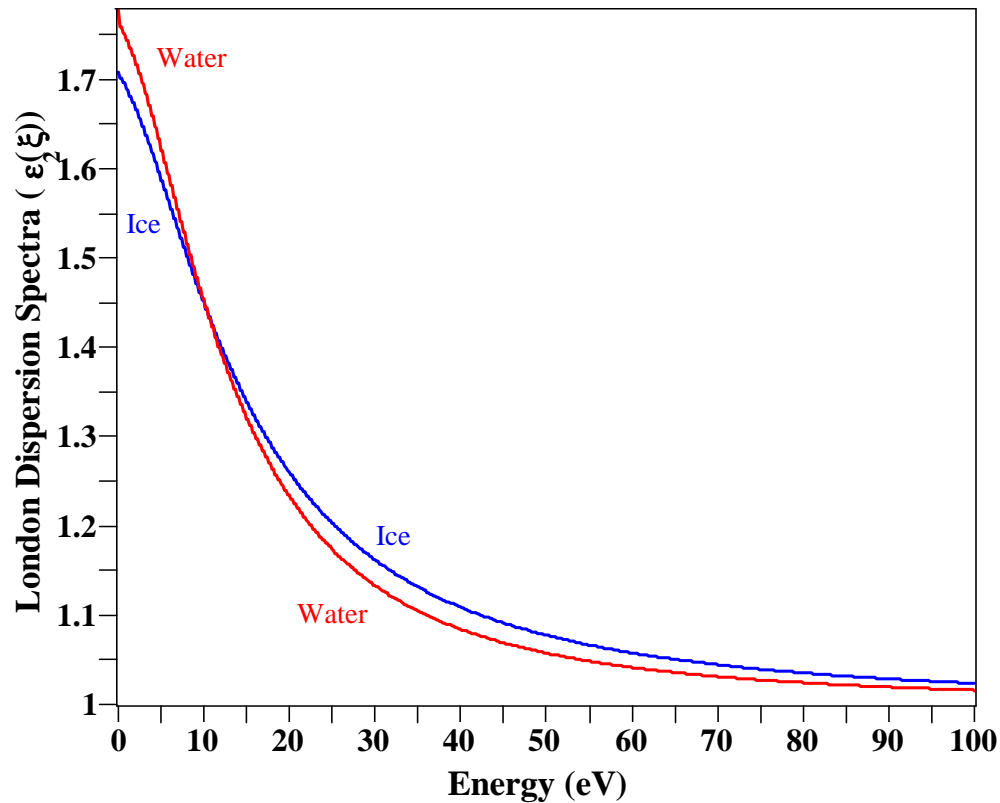
Interband Transitions

- $n(\text{Water}) = 1.33$
- $n(\text{Ice}) = 1.31$



1. M. Elbaum, M. Schick, *Phys. Rev. Lett.*, 66, 13, (1991); L. A. Wilen, J. S. Wettlaufer, M. Elbaum, M. Schick, *Phys. Rev. B*, 12426.

Equilibrium Surficial Film: Water on Ice



Equilibrium Surficial Film¹

- Stabilized by Retardation of Dispersion Interaction
- Important To
 - Friction Of Ice
 - Charge Transfer In Clouds

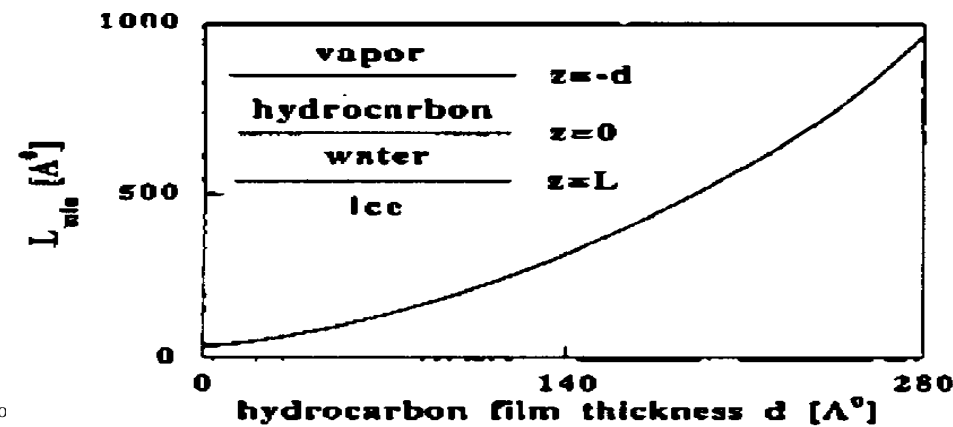
Wetting to Nonwetting Transition

- Multilayer Adsorbate of Water

Addition of Hydrocarbon Surfactant²

- For Water on Ice

Water Thickness Increases To 100 nm



1. M. Elbaum, M. Schick, **PRL**, 66, 13, (1991).
2. R. Bar-Ziv, S. A. Safran, **Langmuir**, 9, (1993).

Gecko Hamaker: Open Source Hamaker Program

Full Spectral, Retarded Hamaker, Coefficients:

<http://geckoproj.sourceforge.net/> Distributed With Optical Spectra Of Materials

File Database Material Project Admin About

Search: contains

Name	Pa...	SPC	Comments	nVis	N...	DSPEC
al2o3-teels...	T U	al2o3-teels#7,Al2O3, alpha, sscor@Stutt VEELS, KK		1.76		<input checked="" type="checkbox"/>
al2o3-vuv-p	T U	al2o3-vuv-Al2O3 Single Xtal Basal Plane VUV YO		1.75		<input checked="" type="checkbox"/>
aln-p	T U	aln-t #301, AlN Single Xtal, Slack, w Ellips.		2.14		<input checked="" type="checkbox"/>
au-palik-p	T U	au-palik-t au palik		19....		<input checked="" type="checkbox"/>
CIRCULOID	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
EMA	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
ice-d	T U	icedT :-Los (.01,.08,.00)(.11,.05,.00)(.40,		1.55		<input checked="" type="checkbox"/>
LINEAR	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
mgal2o4-g...	T U	mgal2o4-g#7,MgAl2O4 Spinel Geological, Burma,		1.67		<input checked="" type="checkbox"/>
mgal2o4-v...	T U	mgo-veels#7,MgO, HM16-04-97-1, p0862o ref.		1.72		<input checked="" type="checkbox"/>
mgo-veels-p	T U	mgo-veels#7,MgO, HM16-04-97-1, p0862o ref.		1.72		<input checked="" type="checkbox"/>
MIXTURE3	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
pd-palik-p	T U	pd-palik-t Pd Palik, ref. = S C Fain et al, Nanotech		16....		<input checked="" type="checkbox"/>
QUADRATIC	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
QUADROID	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
REVERSEQU...	- -	- -	Interpolation Layer	0		<input checked="" type="checkbox"/>
si3n4-t	T	si3n4-t #608SiN/glassGermany95%SiN		1.00		<input checked="" type="checkbox"/>

Add Material

Plot Spectra

Extract Material

Create Dispersion Spectrum

Delete Material

Add To Project

Material: ice-d

Arbitrary

Arbitrary

current project: ice-water-air

Number	Material	nVis	Thickness	Dynamics
1	ice-d	1.55	-1	HalfSpace
2	water-	1.33	1	Center
3	vacuum-p	1	-1	HalfSpace

Move Up

Move Down

Delete Layer

Clone Layer

Edit Parameters

Plot nVis

Calculate

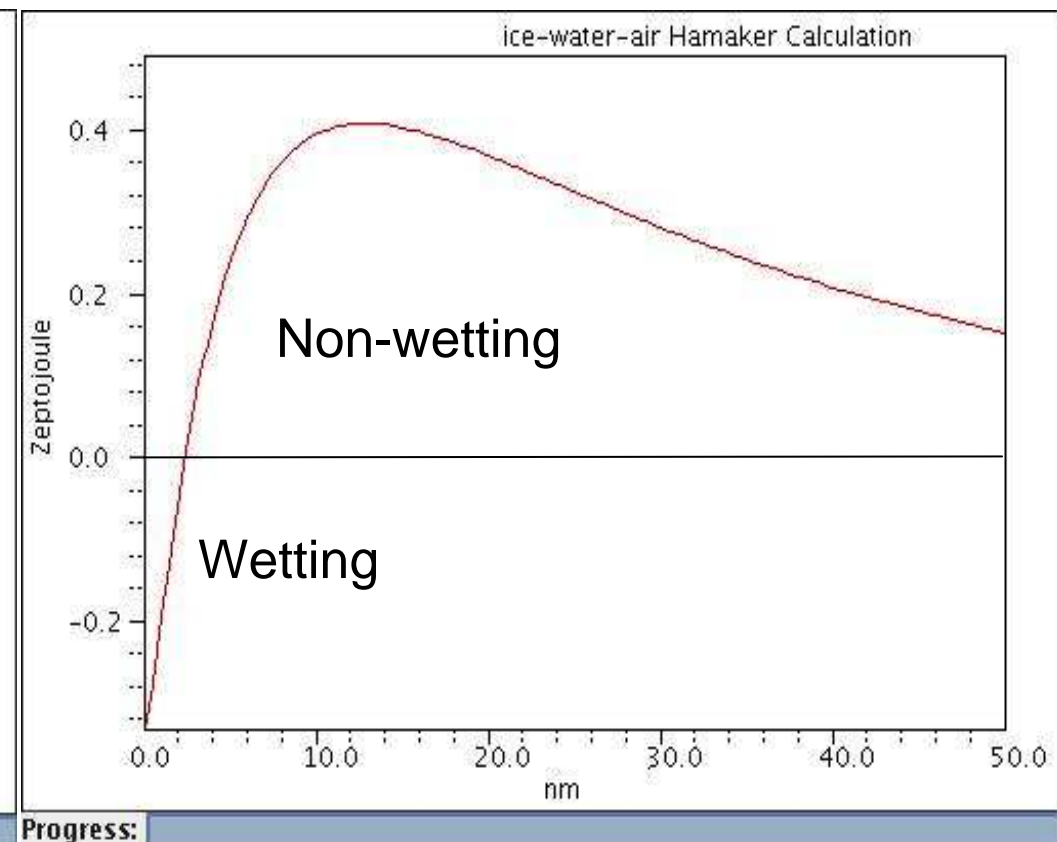
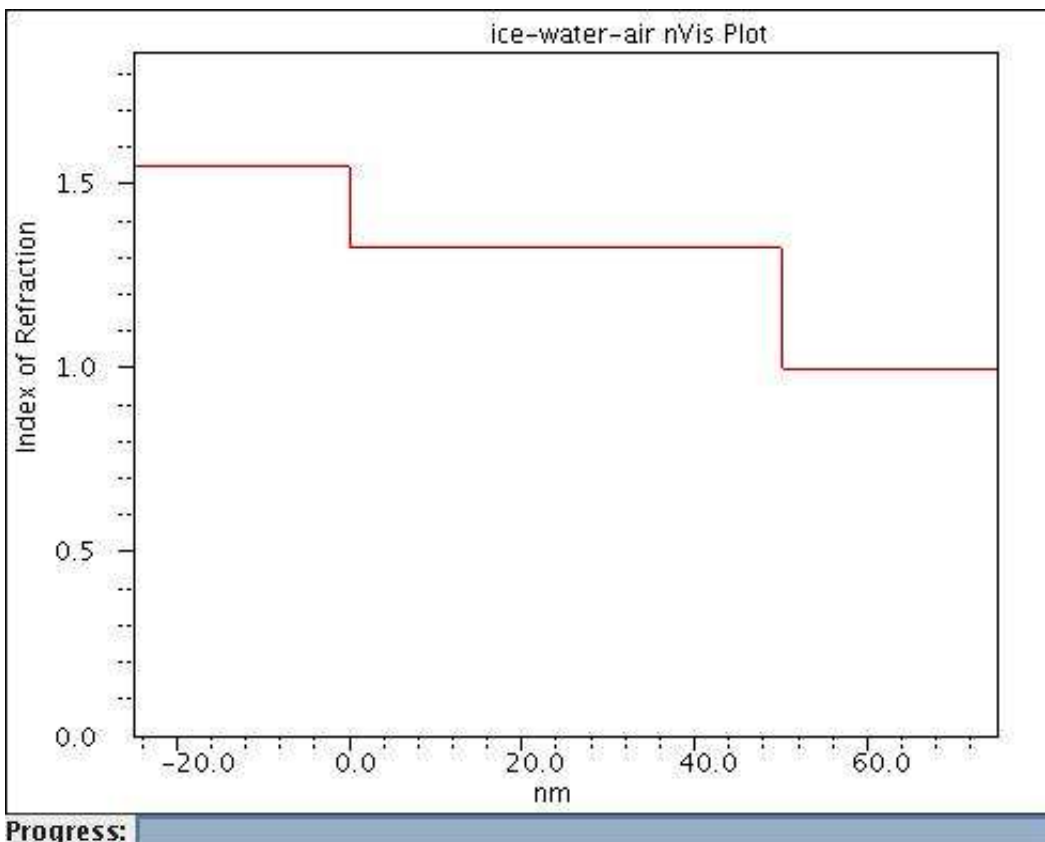
Projects...

New

Save

Save As

Equilibrium Surficial Film: A [Ice | Water | Air]



Index Of Refraction Profile

- Showing Steps In Index
- For Surficial Film On Ice

Retarded Hamaker Coefficient

- Novel Dispersion Interaction
- Wetting To Non-wetting Transition
 - With Surficial Film Thickness

Make State Of The Art Hamaker Calculations Available To All

- Open Source Program, Under GNU Public License

Controlled Wetting by Elec. Structure Doping

Electronic Structure and Dopants

- Glass Additives
 - Increase Index of Refr.
- Crossing Condition
 - London Dispersion Spectra
 - Equib. Surf. Films

Al_2O_3 | SiO_2 | Air

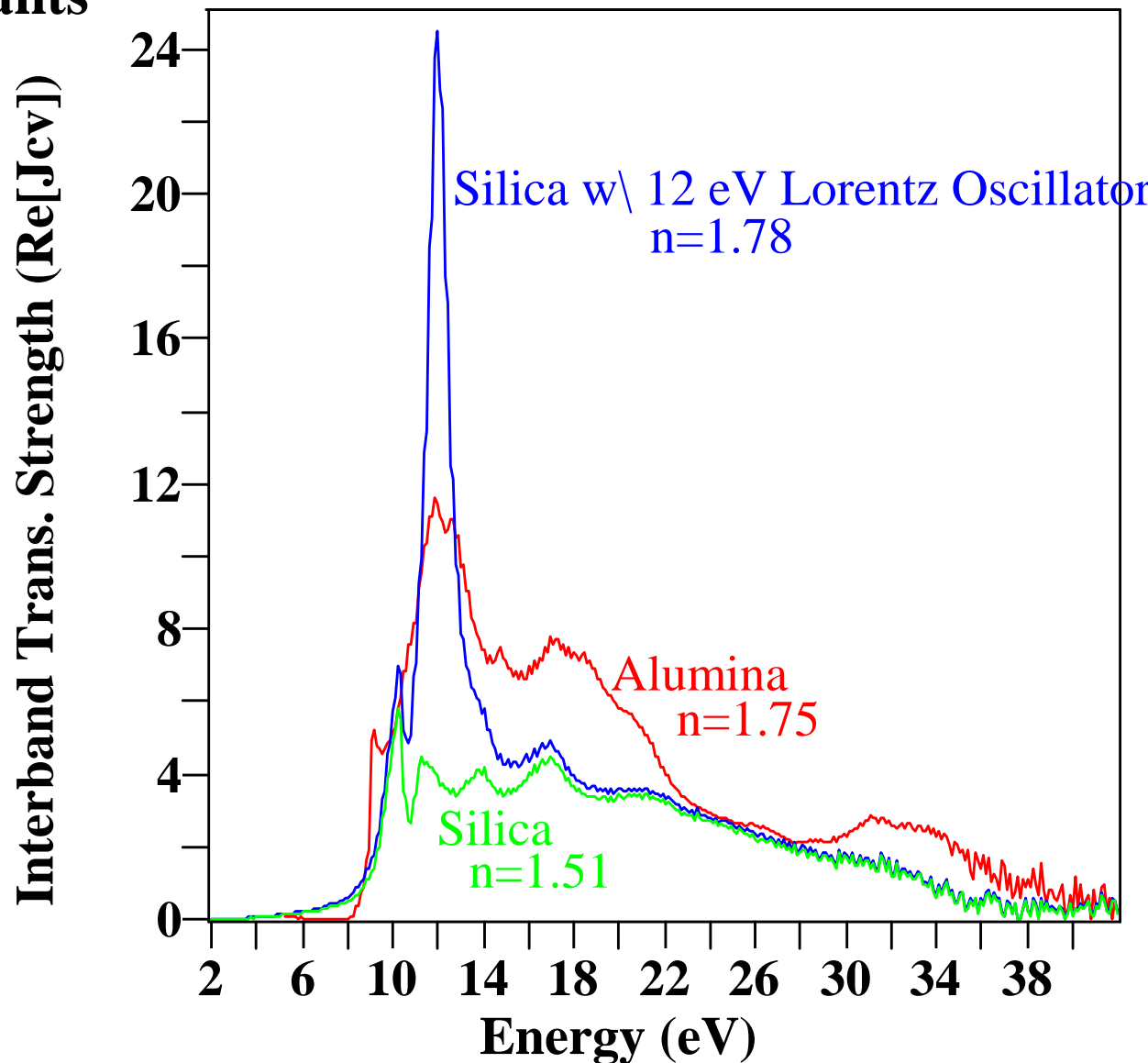
- Decreasing Indices
- Normal Wetting

Add Dopant at 12 eV Energy

- Increase Index of Refraction

Similar to Doping a Glass

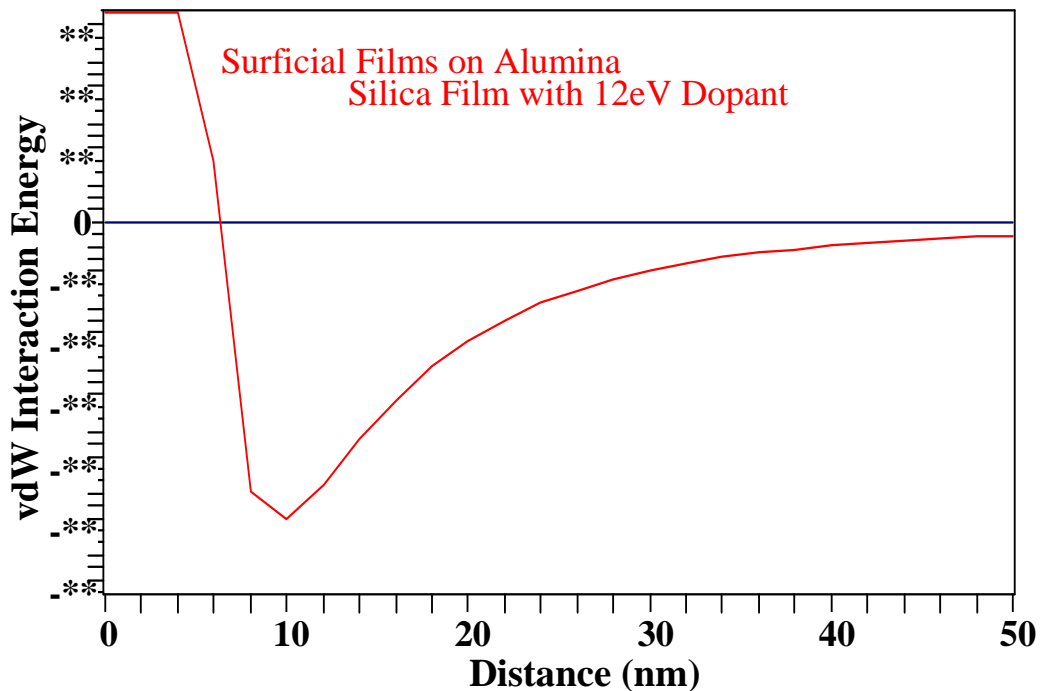
- Na, Ca, Ba, Y, La, Yb
- Exhibit Narrow Int. Band Tr.



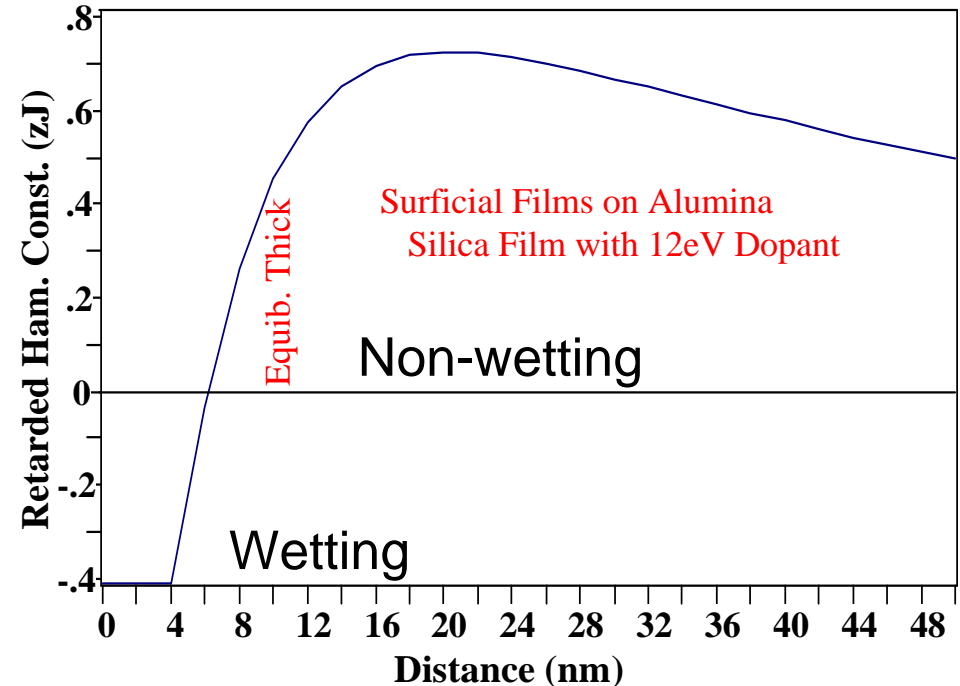
Control Of Dispersion Interactions By Electronic Structure & Chemistry

Equilibrium Surficial Films by ES Doping

Interaction Energy



Retarded Hamaker Constant



Equilibrium Surficial Film ↑

Al_2O_3 | SiO_2 with 12 eV Dopant | Air

Energy Minima, Zero Crossing of Hamaker Constant

- Now Equilibrium Thickness Surficial Film
- Wetting of 1.75 with 1.78 Matl: Index “Rules “ Violated

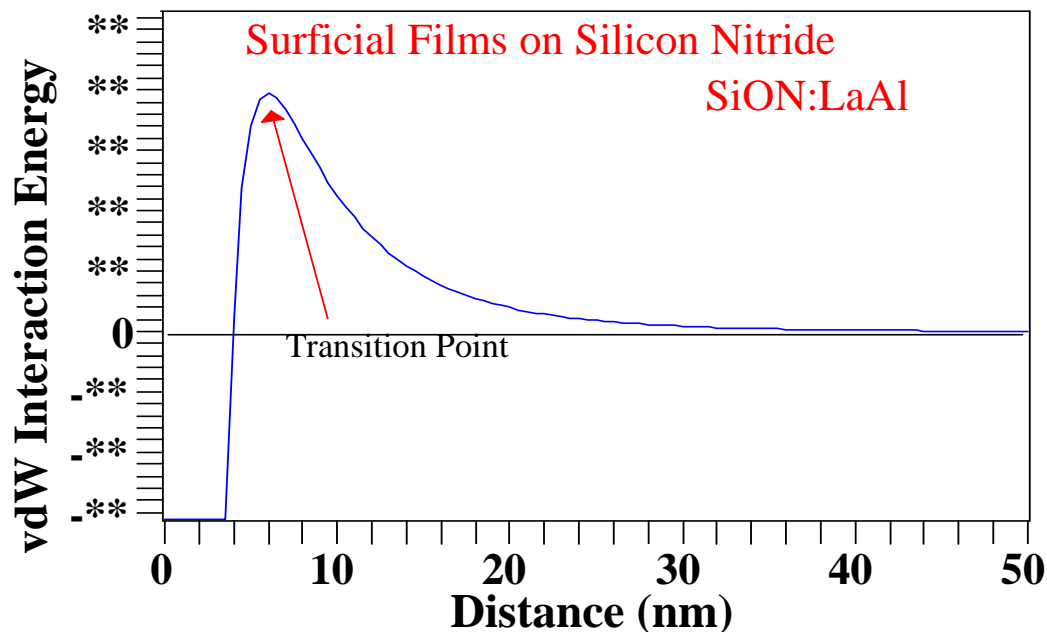
Design of Equib. Surficial Films By Doping

By Compositional Doping

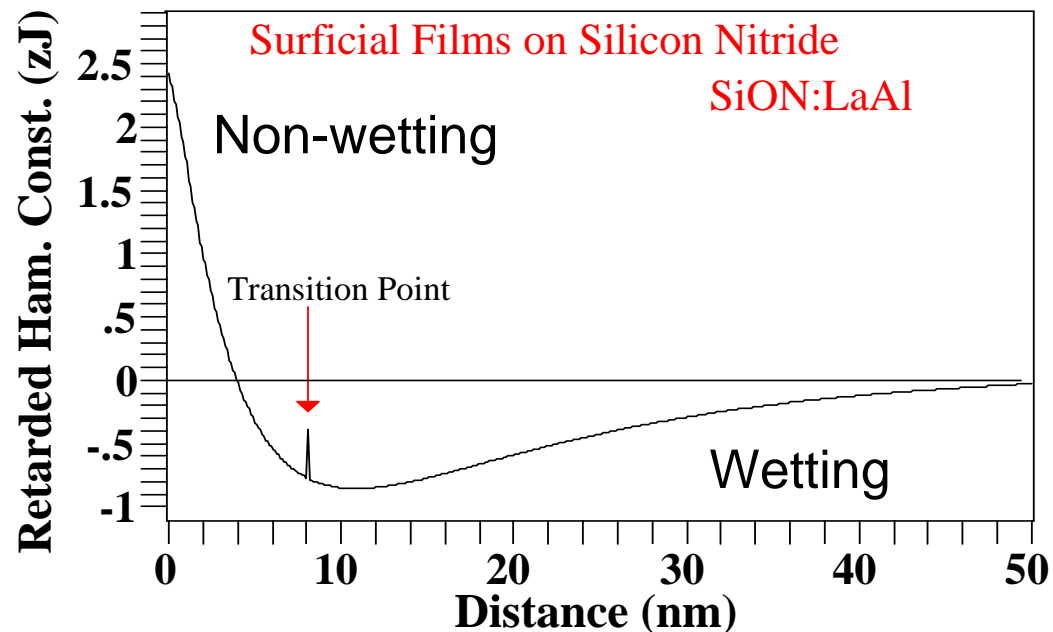
Can Achieve Same
Wetting/Non-wetting Transition
As In Water And Ice

Bimodal: Nonwetting/Wetting

Interaction Energy



Retarded Hamaker Constant



Bimodal: Nonwetting, With Wetting

Different Condition From Equilibrium Surficial Film

- Note Zero Crossing & Curvature

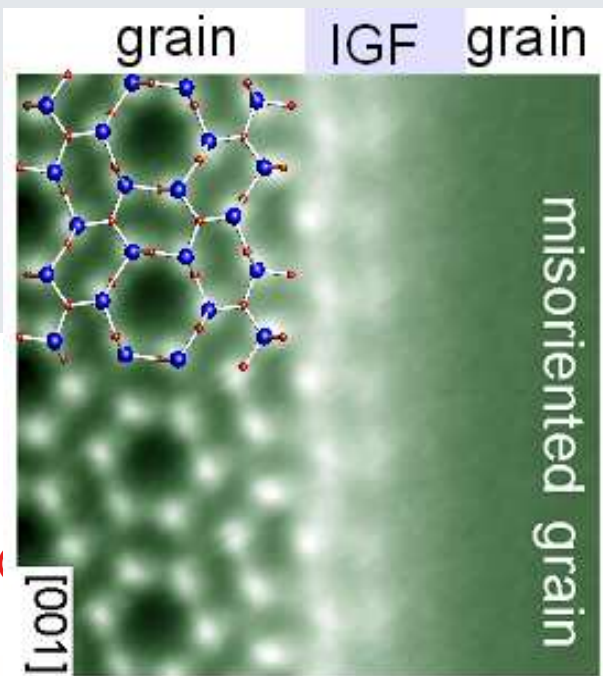
Note Transition Point Thickness

- DeWetting Films Below Transition Point
- Metastable Wetting Films Above Transition Point Thickness

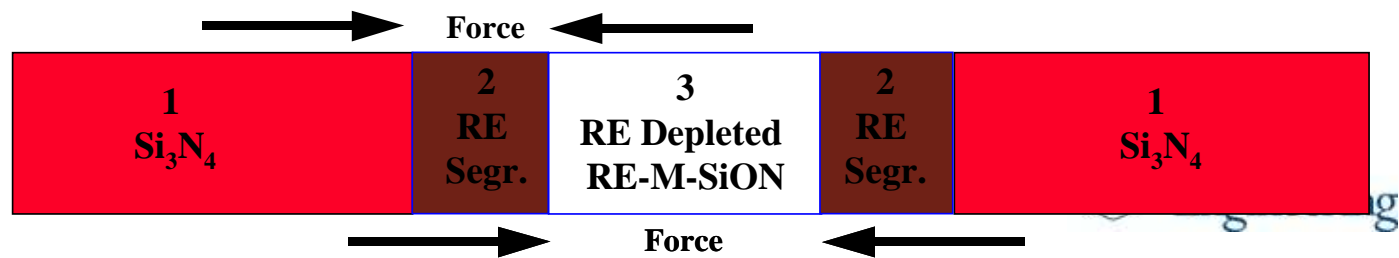
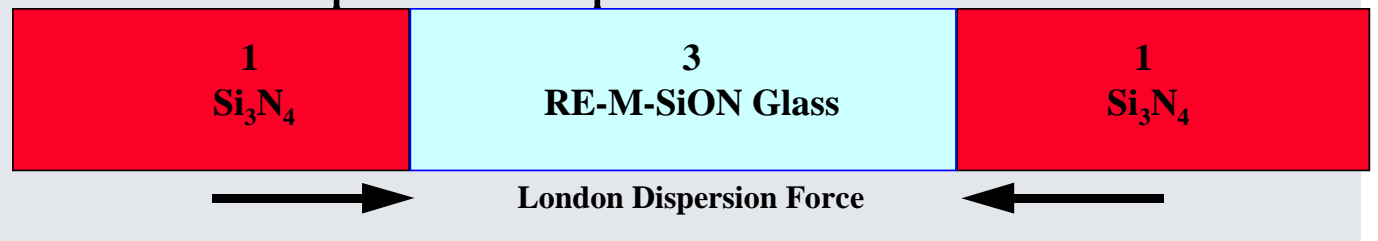
Useful for Microstructural Design

An Option For
“Lubricated Assembly”
With Snap-In
At Assembly Completion?

vdW-Ld Driven Rare Earth Segregation In RE-M-SiON: Si_3N_4

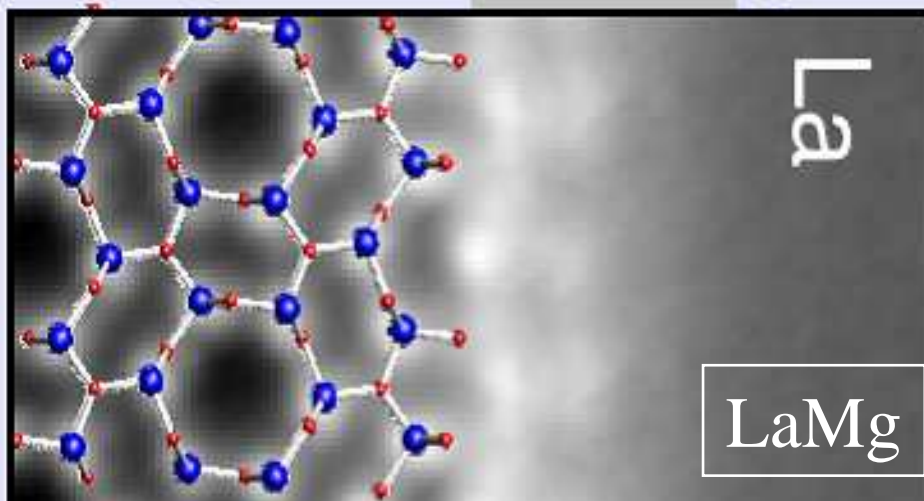


Coupled Compositional Variations

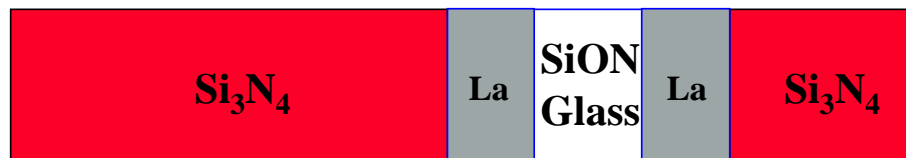


Dimensions In Rare Earth-M-SiON:Si₃N₄ IGFs

grain IGF grain



→ 1.8 nm ←
→ 0.6 ←

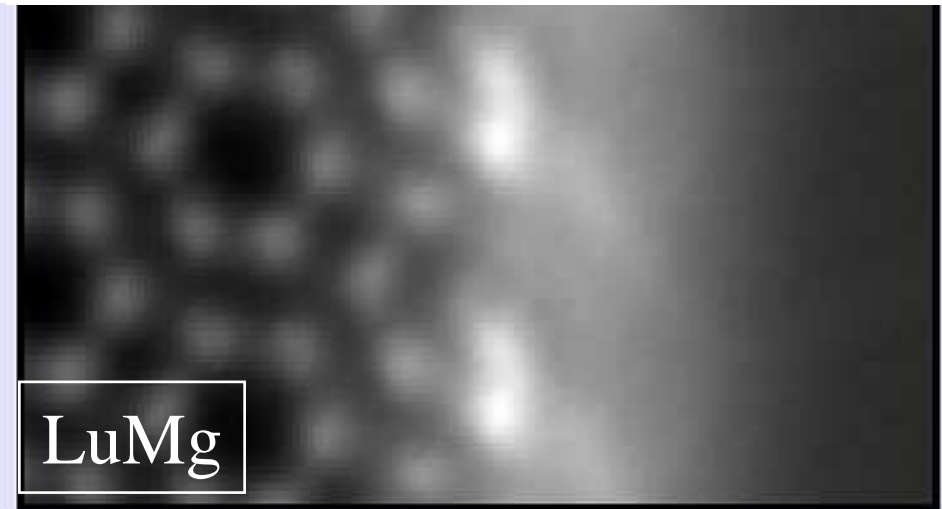


→ 0.6 ↔ 0.6 ←

LaMgSiON:Si₃N₄

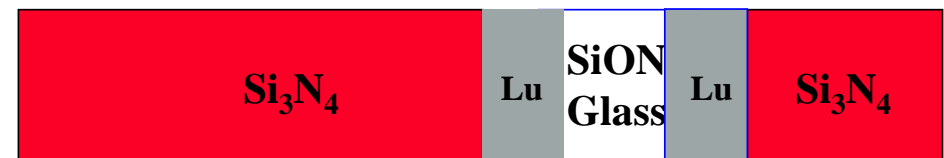
1.8 nm Film Width

- 0.6 nm La Segregation Layers
- 0.6 nm Central Layer



grain IGF grain

→ 1.5 nm ←
→ 0.5 ←



→ 0.5 ↔ 0.5 ←

LuMgSiON:Si₃N₄

1.5 nm Full Film Width

- 0.5 nm La Segregation Layers
- 0.5 nm Central Layer

Index Profiles Across Uniform & Segr. Interfaces

Homogenous IG Film

Interfacial RE Segr.

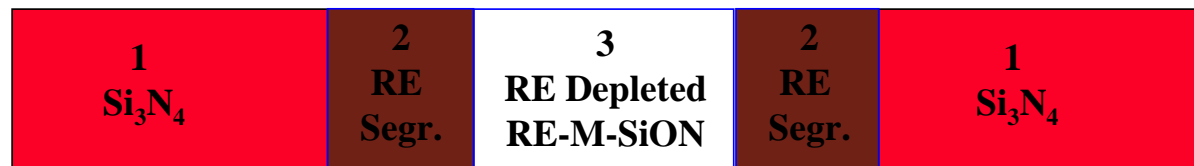
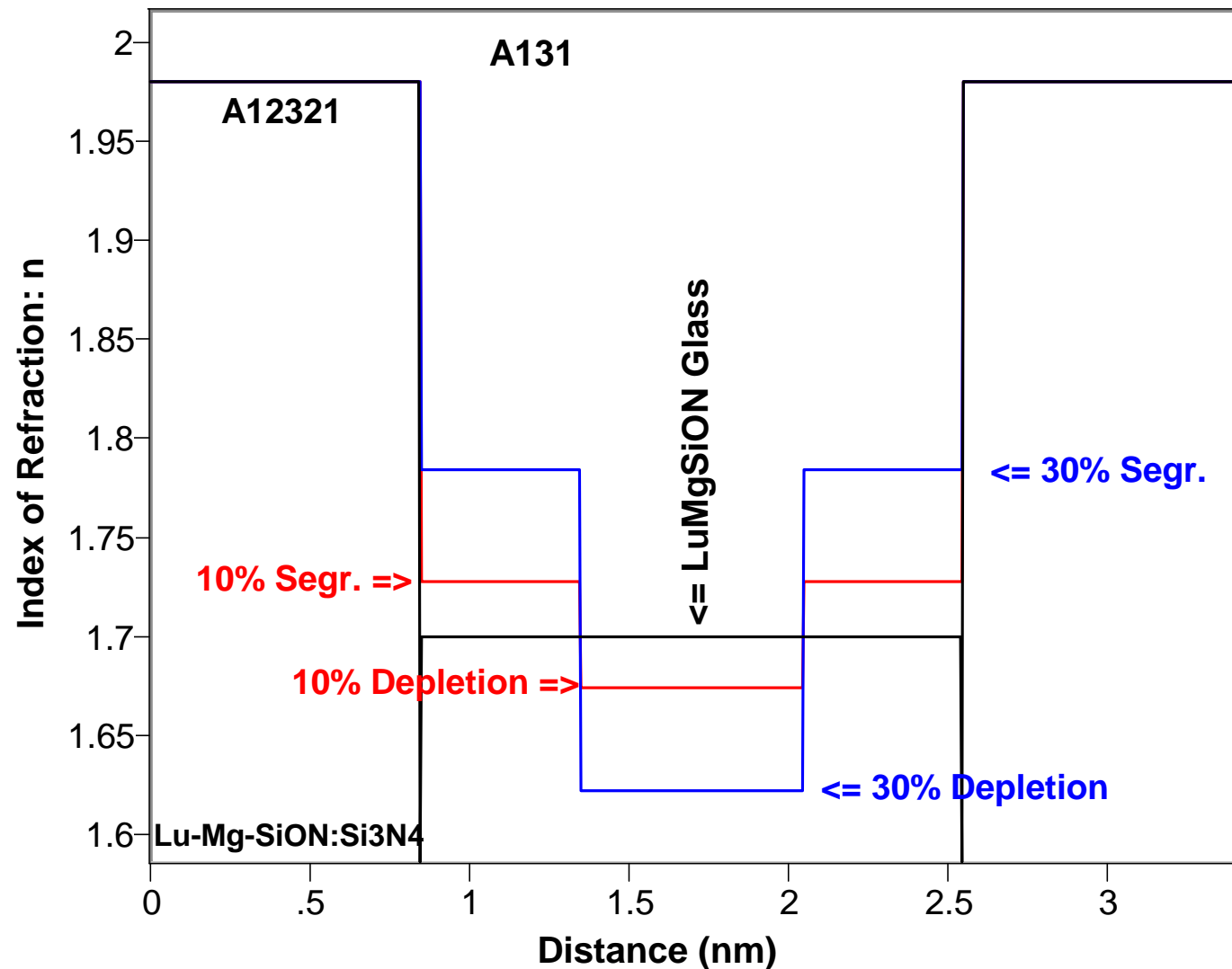
- Increases Index or Ref.
- At Interface

RE Interfacial Layer

- Shields Grains
- From Each Other

Study Two Levels

- 10 % Segregation
- 30% Segregation



Depletion Layer (3) Ham. Coeff.

Non-Wetting Disp. Interaction

RE Segregation Reduces

- Hamaker Coefficient
- London Interaction Energy

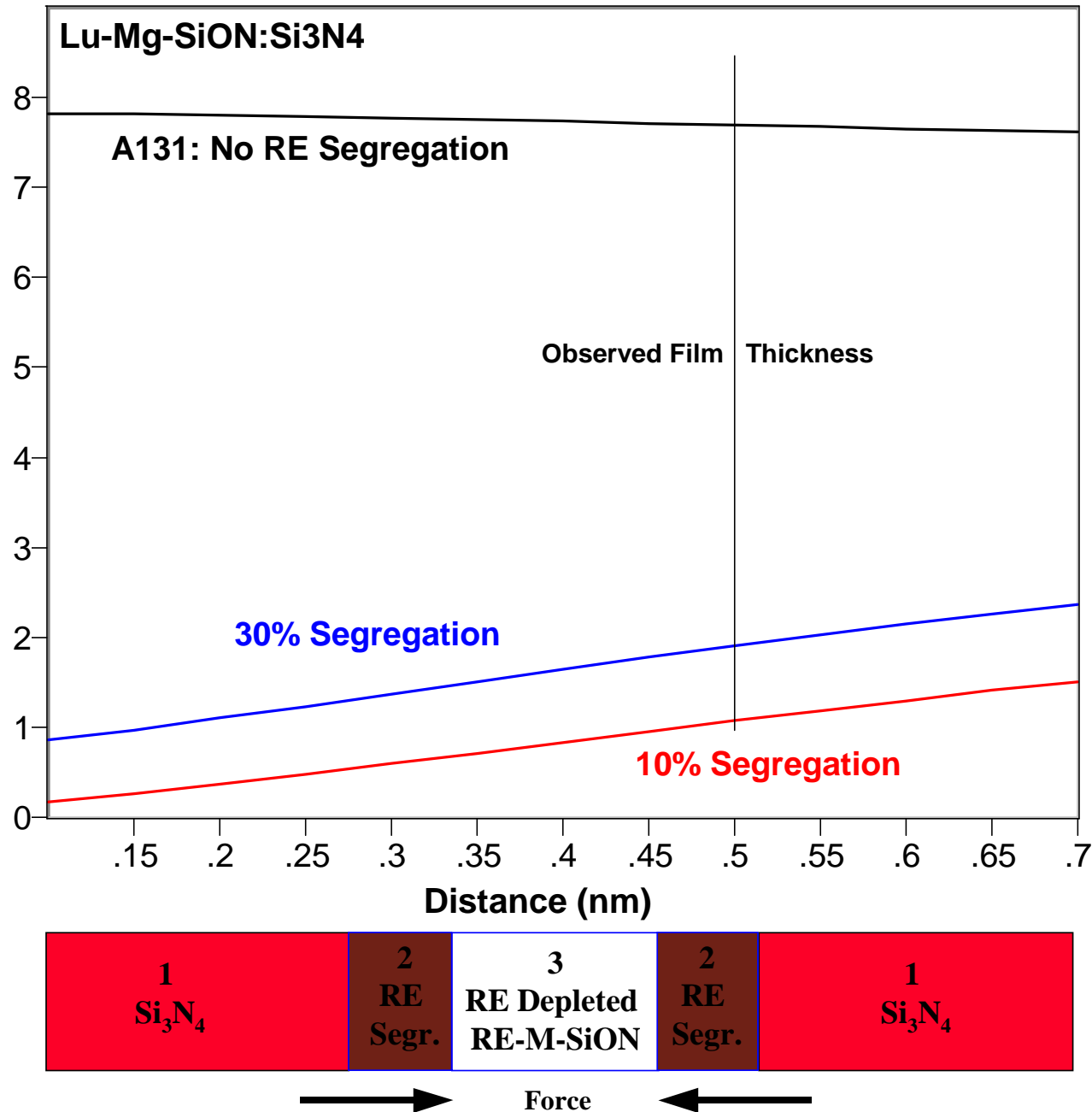
Depletion In SiON

- Dispersion Driven

Must Consider Whole System

$E_{L,Disp.} = -\frac{A(l)}{12\pi l^2}$ $D_0=0.22 \text{ nm}$	Hamaker Coeff. A (zJ)	London Energy (mJ/m ²)
No RE Segr.	7.2	4.0
10% Segr.	1.1	0.6
30% Segr.	1.9	1

Hamaker Coefficient (zJ)



Segregation Layer (2) Ham. Coeff.

Wetting To Non-Wetting Transition

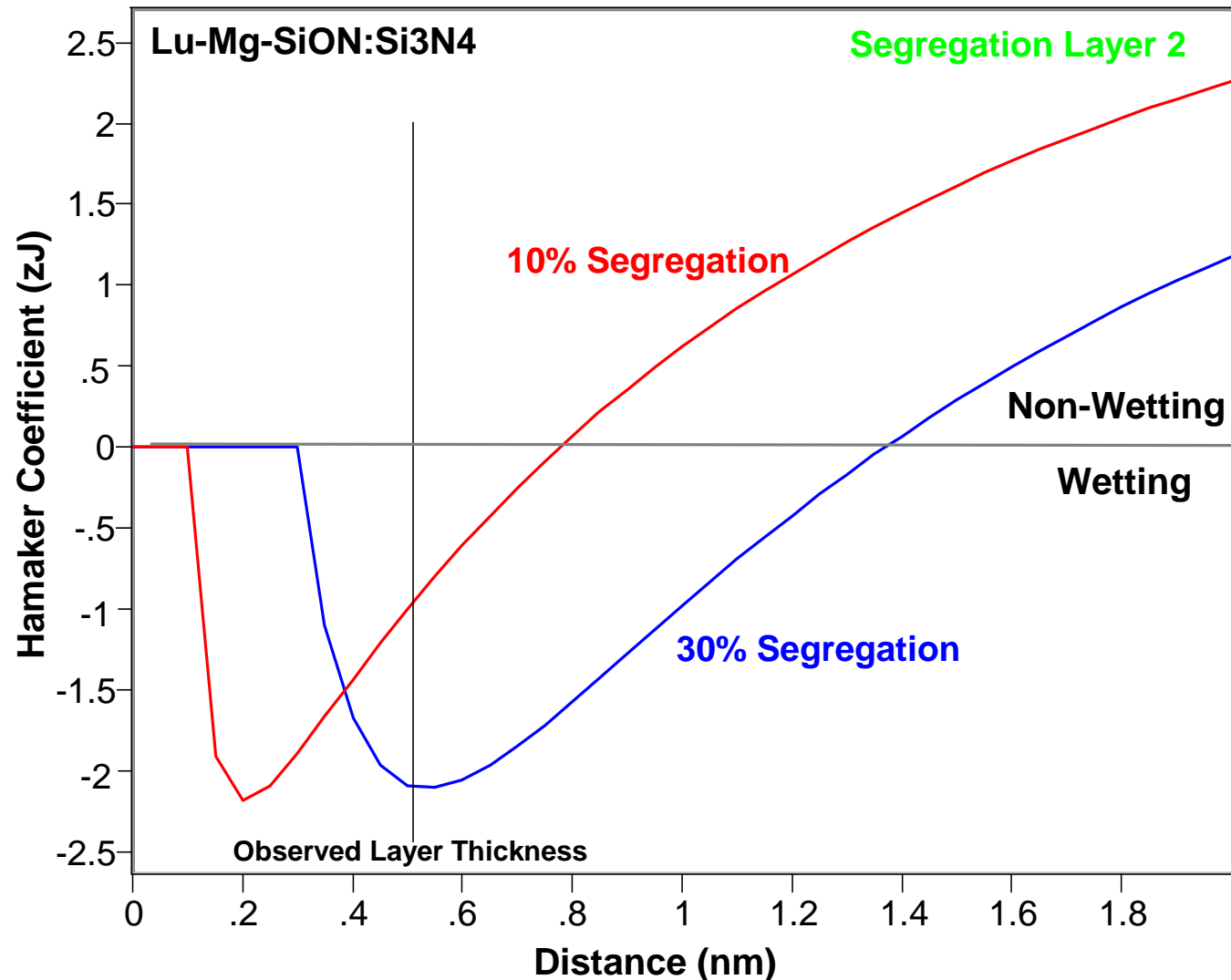
Thickness Dependent Wetting Transition

Compare To Water On Ice

- Equilibrium Water Film
- Lond. Dispersion Stabilized
- See Elbaum, Schick PRL

RE Segregation Driven

- By Increased Index
- In Segr. Layer



Dispersion Driven Interfacial RE Segregation

RE Segr. Coupled System

- With RE Depletion In Center
- RE Segregation To Interface

Equilibrium Layer Configuration

- London Dispersion Stabilized

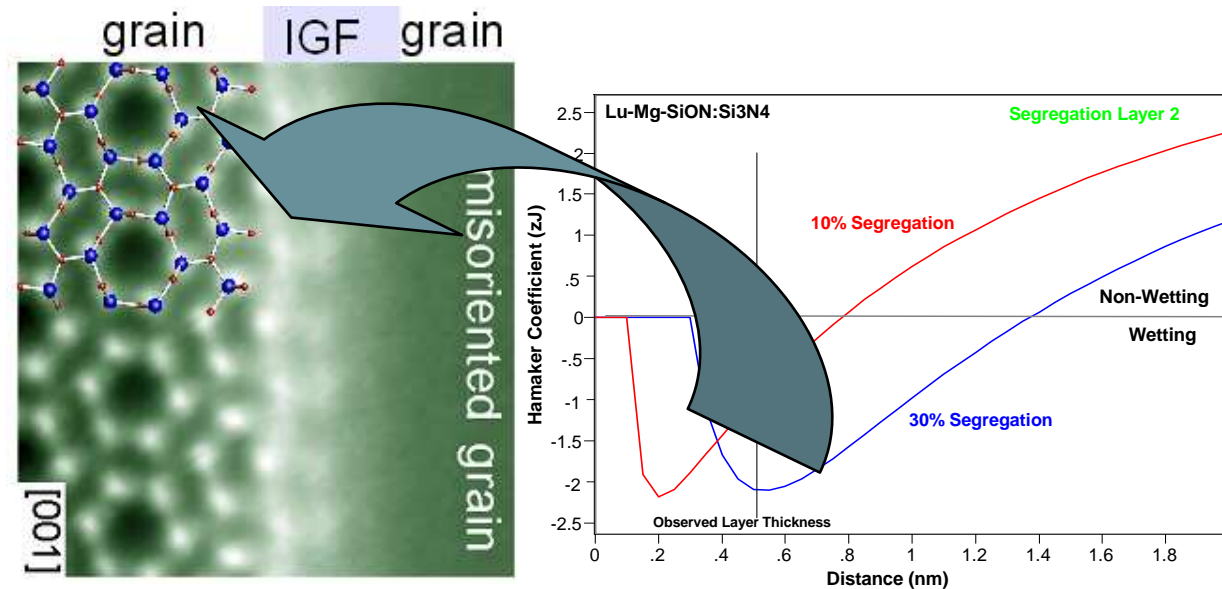
Comparable To Lu Segr. In Si_3N_4

Combined Disp. Energy

- Of Segr Layer
- And Depletion Layer

Lowers Dispersion E

- Of Intergranular Film



	Depletion Layer 3 (SiON Center)		Segr. Layer 2 (Si_3N_4 Interface)		Total Disp. Energy mJ/m^2 $E_{L,Disp.} = -\frac{A(l)}{12\pi l^2}$
	A (zJ)	Lond. E (mJ/m^2)	A (zJ)	Lond. E (mJ/m^2)	
No RE Segr.	7.2	4.0			4.0
10% Segr.	1.1	0.6	-1	-0.6	0
30% Segr.	1.9	1	-2.1	-1.2	-0.2

Conclusions

Long Range Interactions In Nanoscale Science

- **Electrodynamics:** vdW-L Dispersion
- **Electrostatics**
- **Polar Interactions**

SrTiO₃ Grain Boundary Dispersion Energies

- Reduced Physical & Electron Density
- ~ 5 to 10% of Chemical GB Energy

Novel Wetting Conditions

- Wetting/Non-wetting Transitions: Premelting
- Non-wetting/Wetting Transitions:
 - Lubricated Assembly?

Dispersion Driven Interfacial Segregation

- But What About The Electrostatic Energy

New Non-Plane Parallel Hamaker Development

- Carbon Nanotubes

