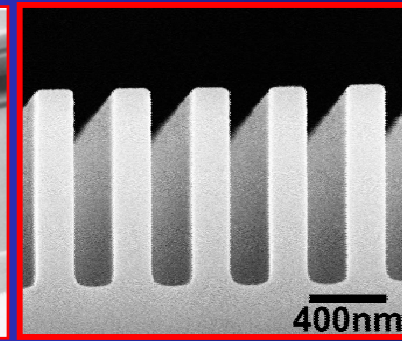
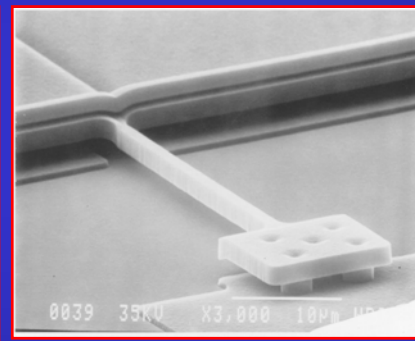
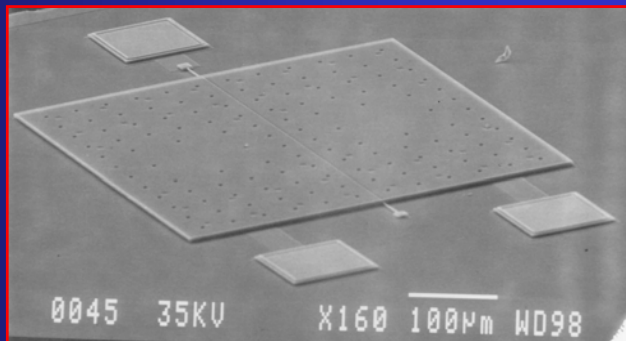


Measurement of the Casimir force on nanoscale corrugated surfaces

Ho Bun Chan



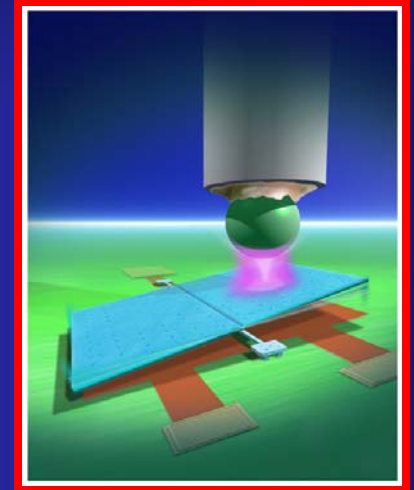
October 1st, 2008. KITP

Outline

- Micromechanical torsional oscillator for measuring the Casimir force.
- nonlinear Casimir micromechanical oscillator.
- Geometry dependence of the Casimir force:
- Experiment on strongly deformed surface: array of nanoscale trenches

Up to 30% deviation from pairwise additive approximation

A factor of 2 smaller than theory on perfect metals



Collaborators

University of Florida

Yiliang Bao

Jie Zou

University Paris-Sud

Thorsten Emig

UT Brownsville

Andreas Hanke

Bell Labs

Federico Capasso

Vladimir Aksyuk

Raffi Kleiman

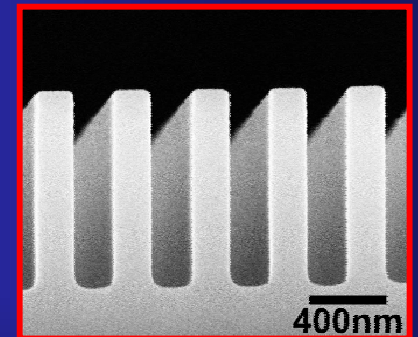
David Bishop

Ray Cirelli

Fred Klemens

Bill Mansfield

C.S. Pai



Casimir force

Hendrik B. G. Casimir 1948

- attractive force between two electrically neutral conducting surfaces
- arise from zero point fluctuations of the electromagnetic field

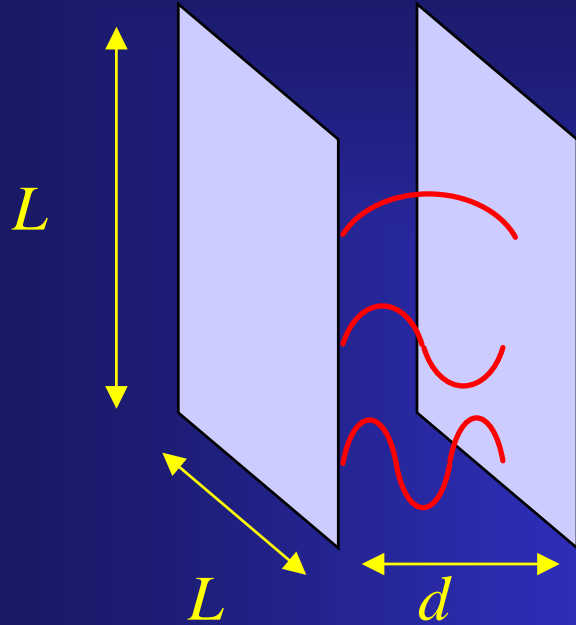
Energy for each electromagnetic mode
with frequency ω :

$$E_{n,\omega} = (n + 1/2)\hbar\omega$$

Uncertainty Principle: electric and magnetic
fields fluctuate, even at ground state ($n = 0$)

Total zero point energy: $E_{total} = \sum_{\omega} \frac{1}{2} \hbar \omega$

Derivation of Casimir force



$$\omega_{k_x k_y n} = c \left(k_x^2 + k_y^2 + \frac{\pi^2}{d^2} n^2 \right)^{1/2}$$

Total zero point energy: $E = \sum_{k_x k_y n} \frac{1}{2} \hbar \omega_{k_x k_y n}$

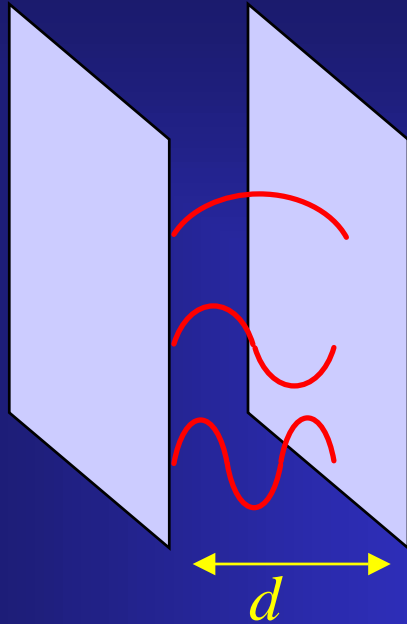
$$E(d) = \frac{\hbar c L^2}{\pi^2} \sum_n \int_0^\infty dk_x \int_0^\infty dk_y \left(k_x^2 + k_y^2 + \frac{\pi^2}{d^2} n^2 \right)^{1/2}$$

Potential energy
of the plates:

$$U(d) = E(d) - E(\infty) = -\frac{\pi^2 \hbar c}{720 d^3} L^2$$

Casimir force

$$F = \frac{-U'(d)}{L^2} = -\frac{\pi^2 \hbar c}{240 d^4}$$



Casimir force between conducting surfaces:

$$F_{Casimir} = -\frac{\pi^2 \hbar c}{240d^4} \text{ per unit area}$$

Quantum effect due zero-point fluctuations on a macroscopic system

Between 2 μm thick silicon plates.

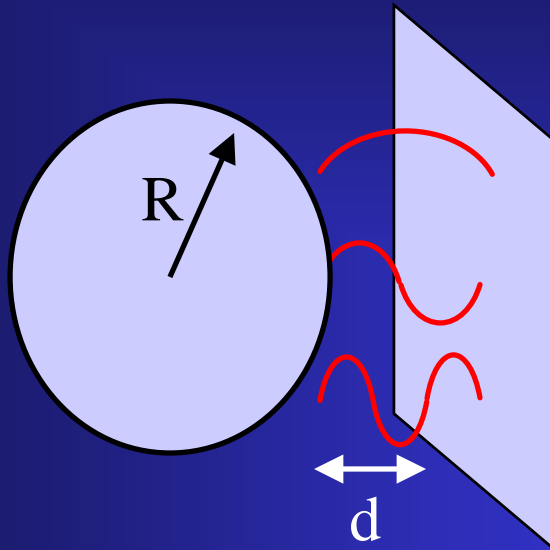
At $d = 1 \mu\text{m}$, $F_{Casimir} \sim$ gravitational attraction

At $d = 10 \text{ nm}$, 10^8 times larger,

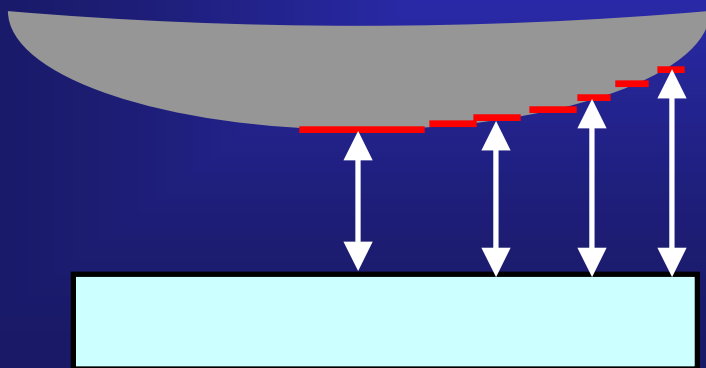
$F_{Casimir} \sim 1$ atmosphere of pressure.

Non-ideal surfaces: finite conductivity, roughness, finite temperature, geometry effects

Experiments measuring Casimir force:



$$F_{Casimir} = -\frac{\pi^3 R \hbar c}{360 d^3}$$



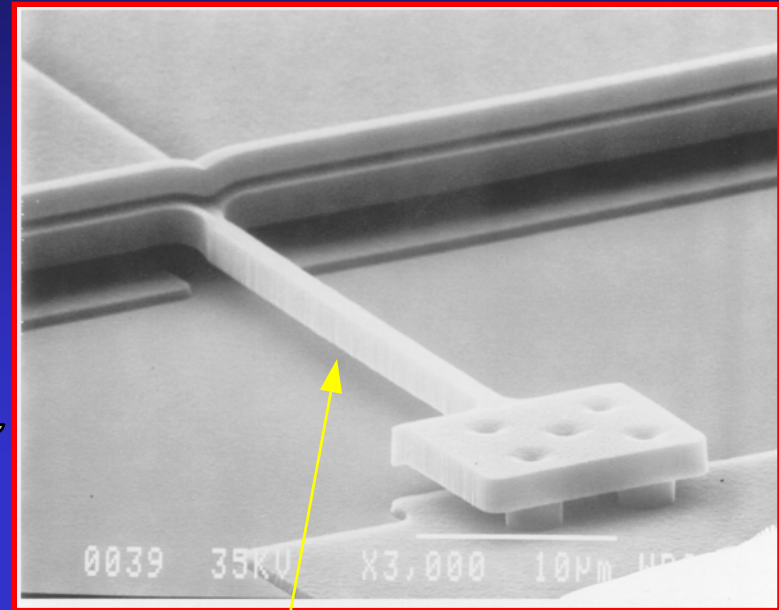
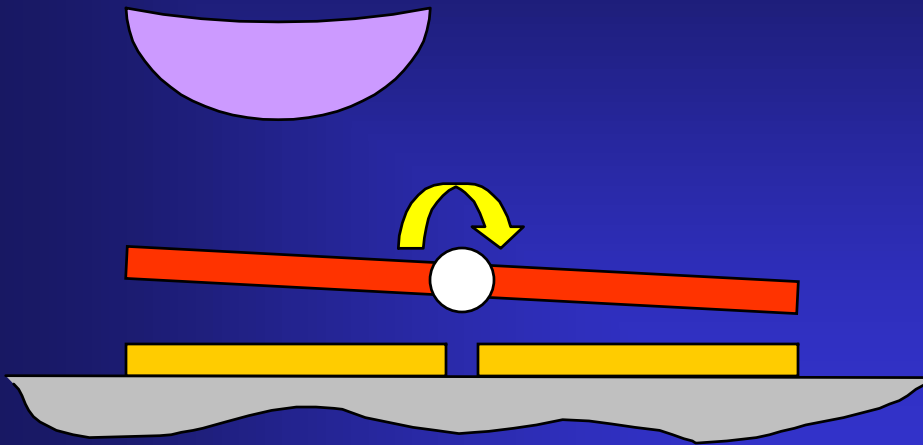
- Lamoreaux '1997
Torsional Pendulum
5% agreement with theory
- Mohideen & Roy '1998
AFM, 1 % agreement with theory
- Ederth '2000
cylindrical geometry
- Chan, Aksyuk, Kleiman, Bishop & Capasso '2001
Actuation of micromechanical devices using the Casimir force
- Bressi, Carugno, Onofrio & Ruoso '2002
parallel plates
- Decca, Lopez, Fischbach & Krause '2003
dissimilar metals, 'Casimir-less' experiments

Proximity force approximation (Derjaguin approx)

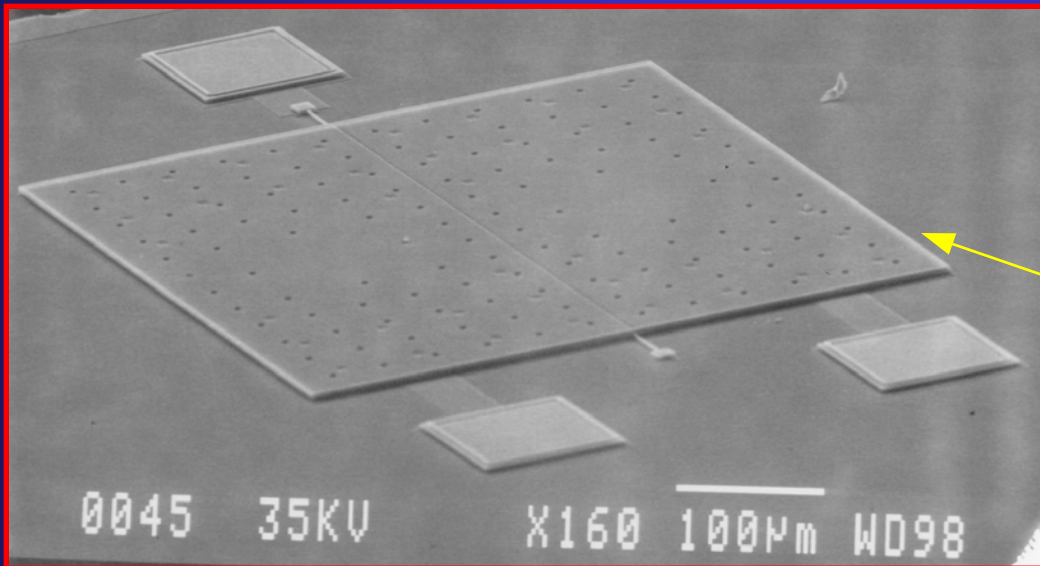
Valid for $d \ll R$

(typical $d \sim 100$ to 400 nm, $R \sim 50$ to 100 μm)

Micromechanical torsional device

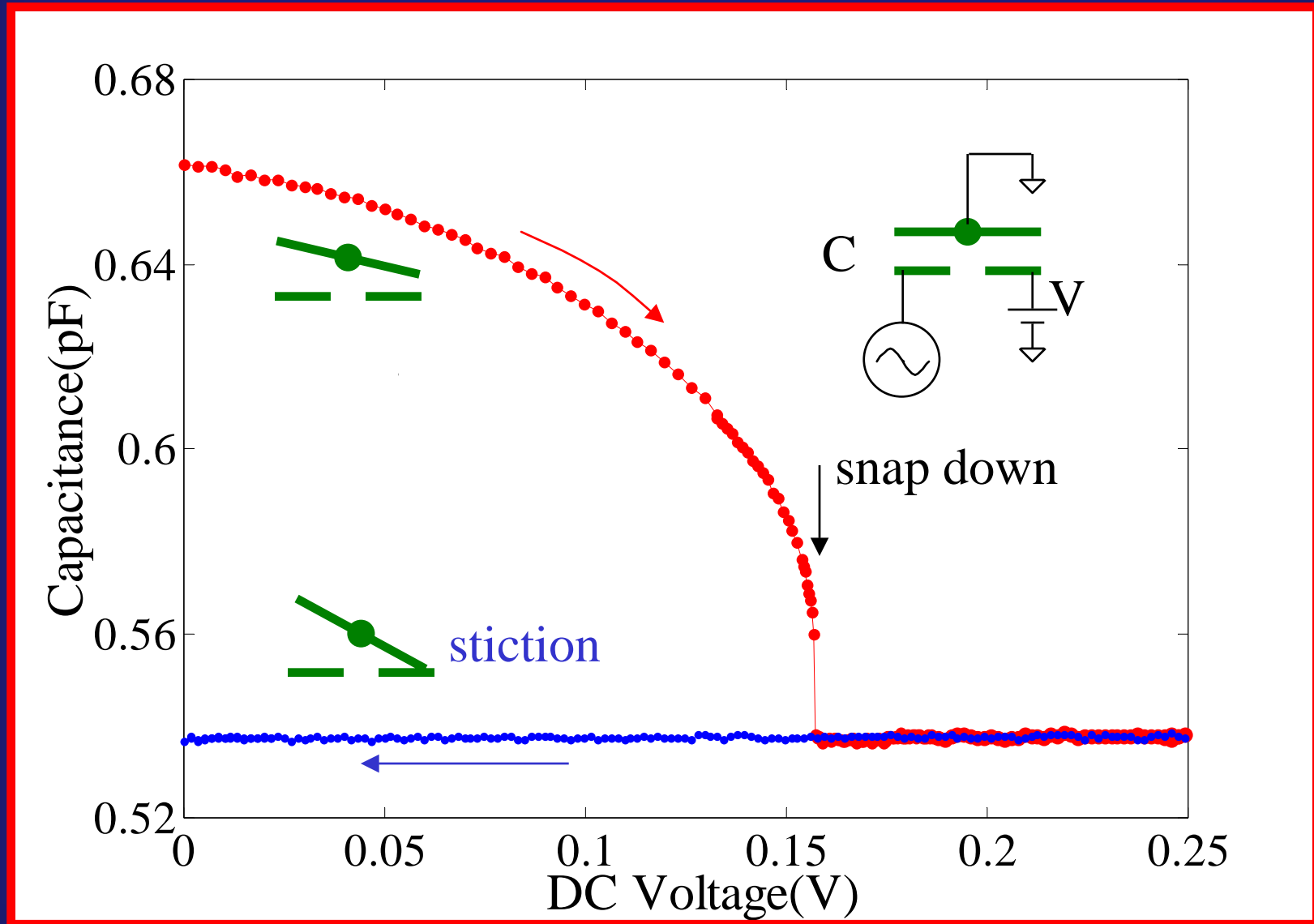


Torsional rod
cross section: $1.5 \times 2 \mu\text{m}^2$

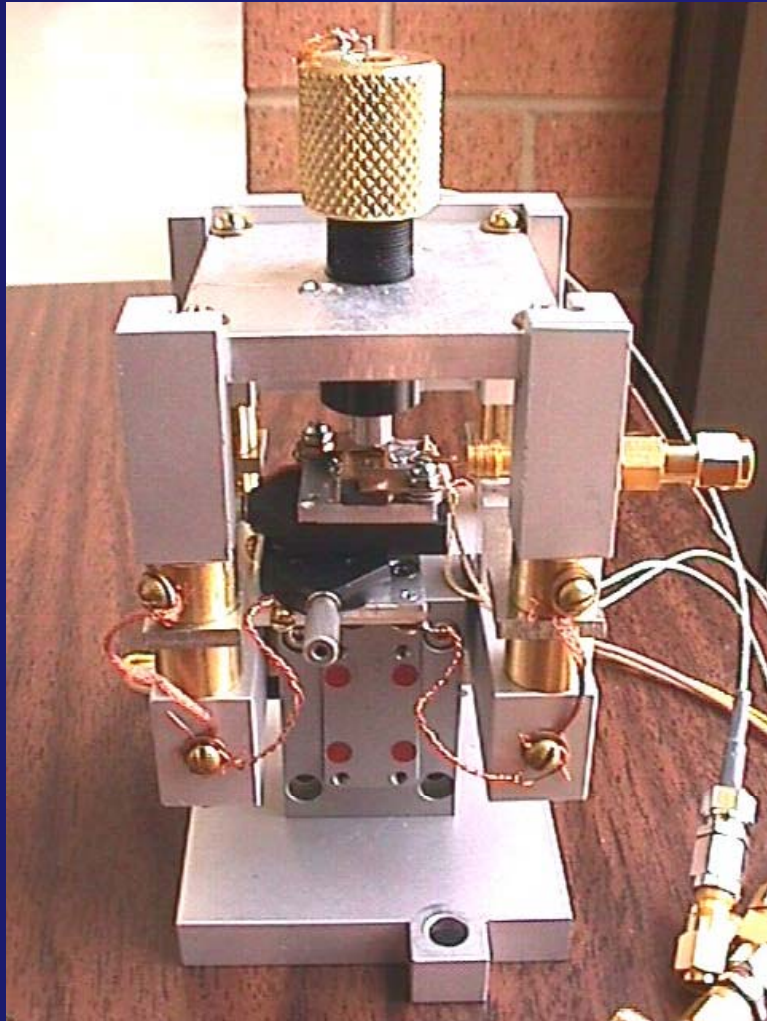


poly-Si plate:
 $500 \mu\text{m} \times 500 \mu\text{m} \times 3.5 \mu\text{m}$

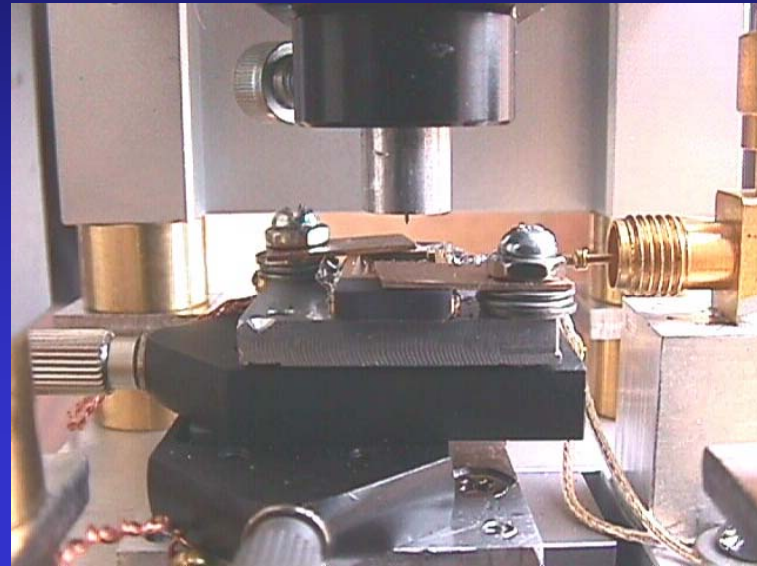
Tilting the top plate by applying DC bias to electrode



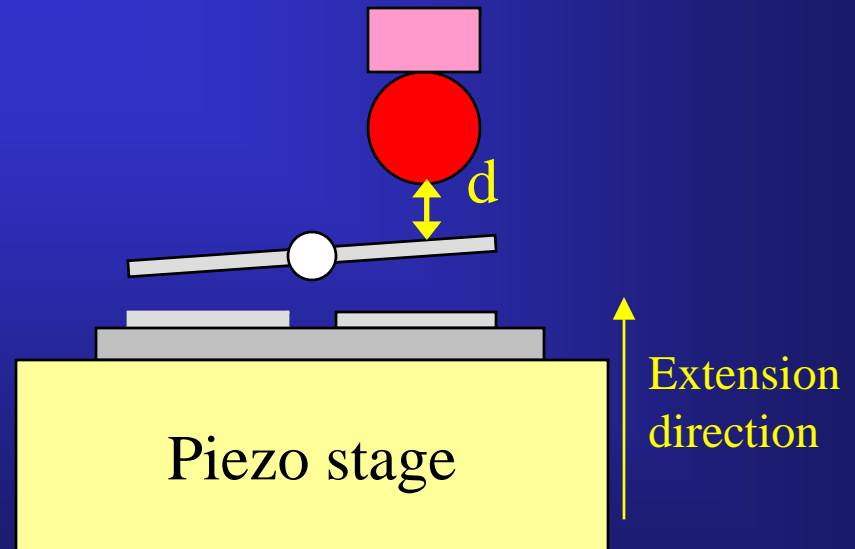
Experimental setup



2.5''

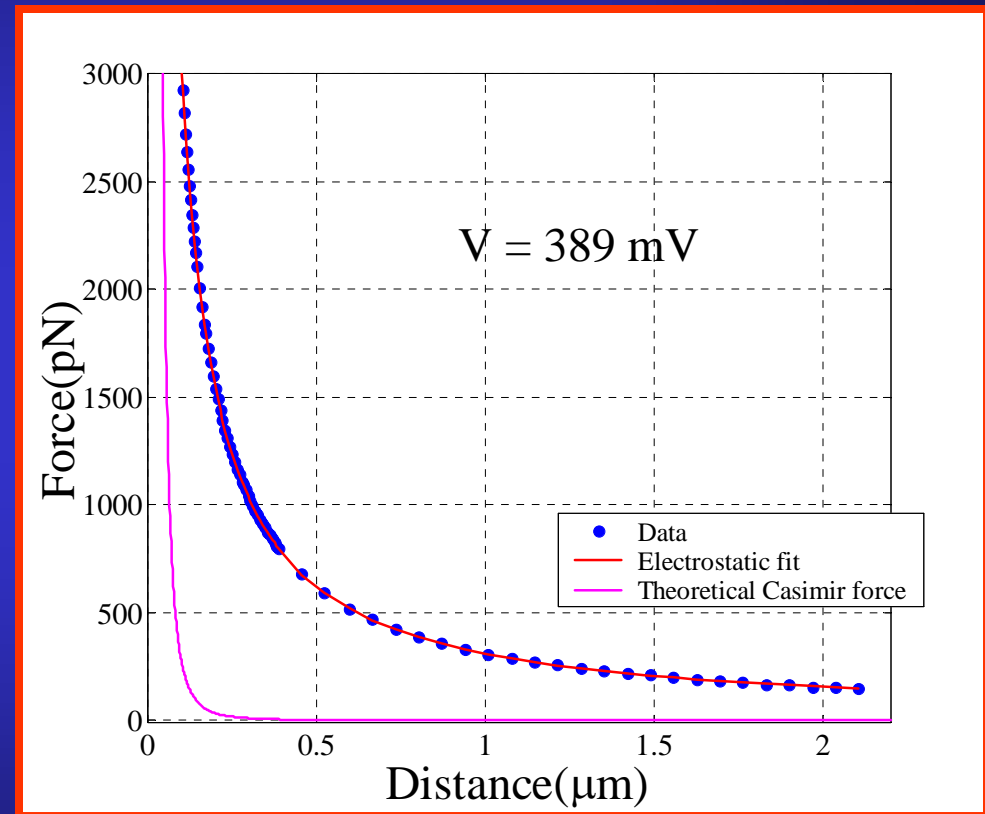
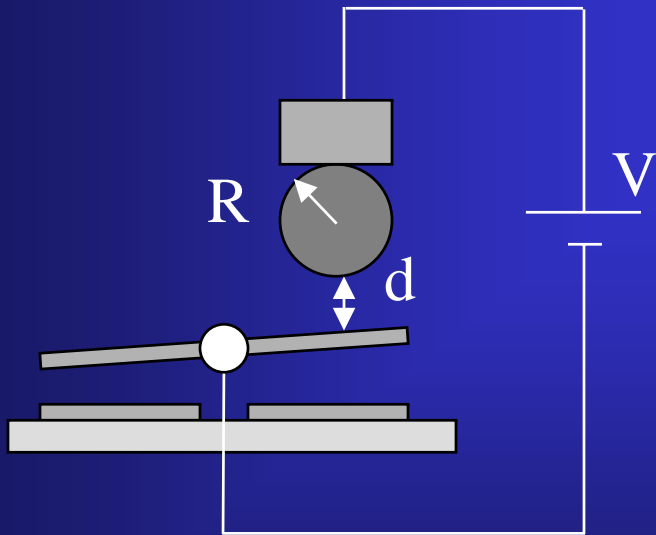


0.5''



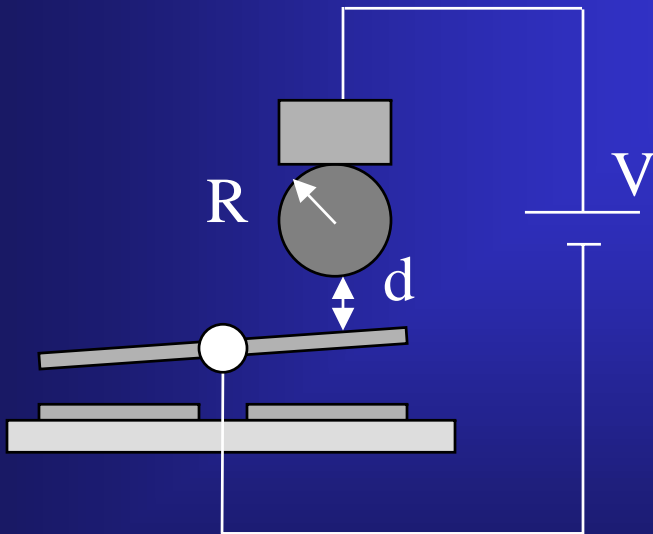
Calibration by electrostatic force

$$F = \epsilon_0 \pi R \frac{(V - V_o)^2}{d}$$

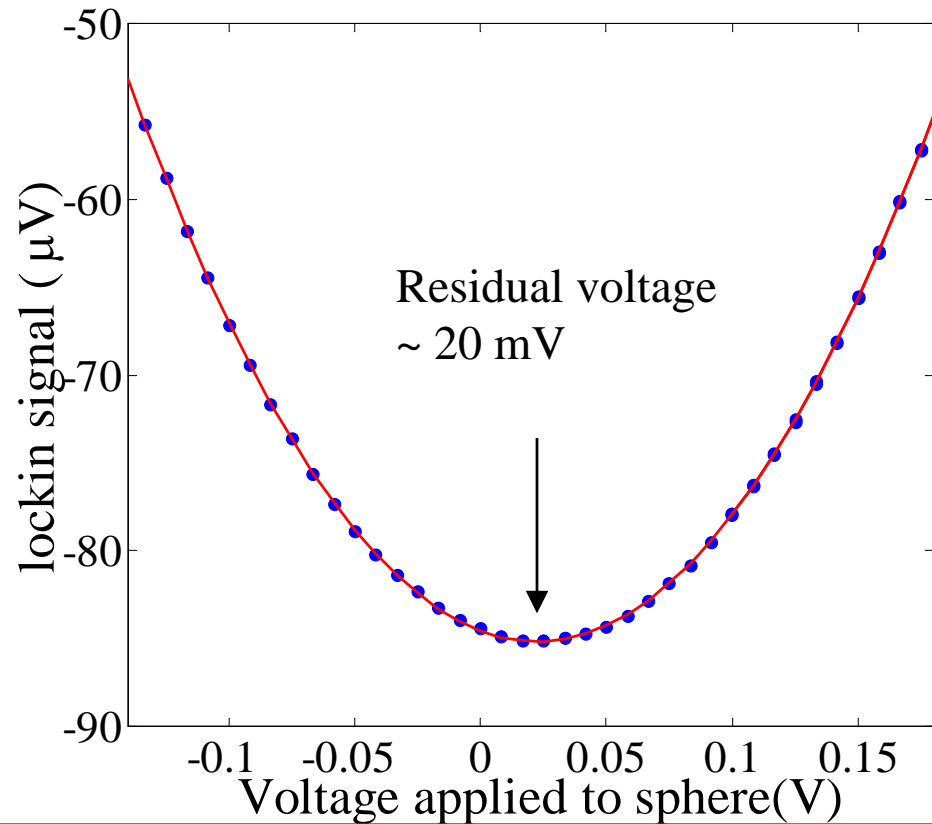


Residual voltage

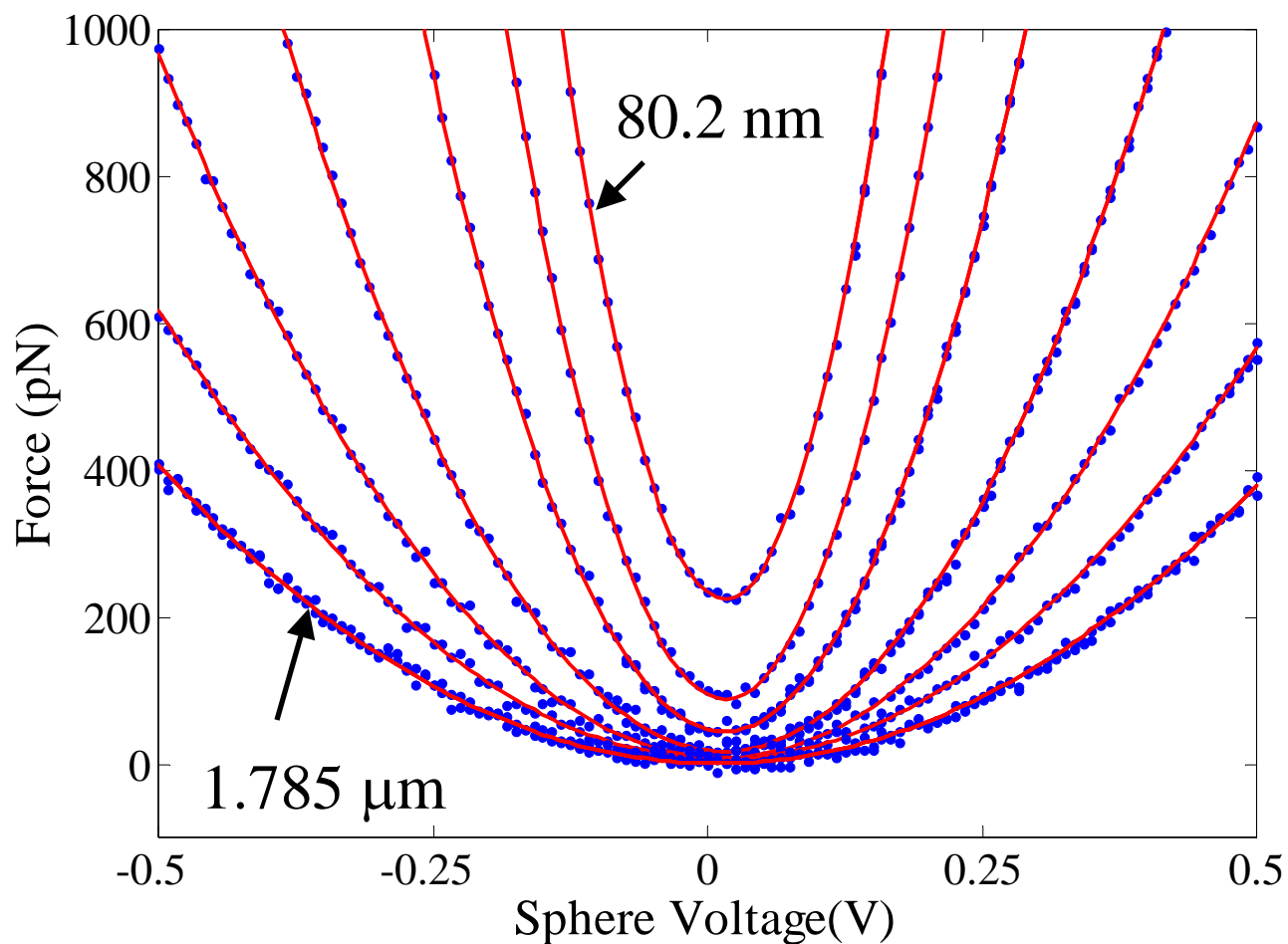
$$F = \epsilon_0 \pi R \frac{(V - V_o)^2}{d}$$



Differences in work functions
of metal films



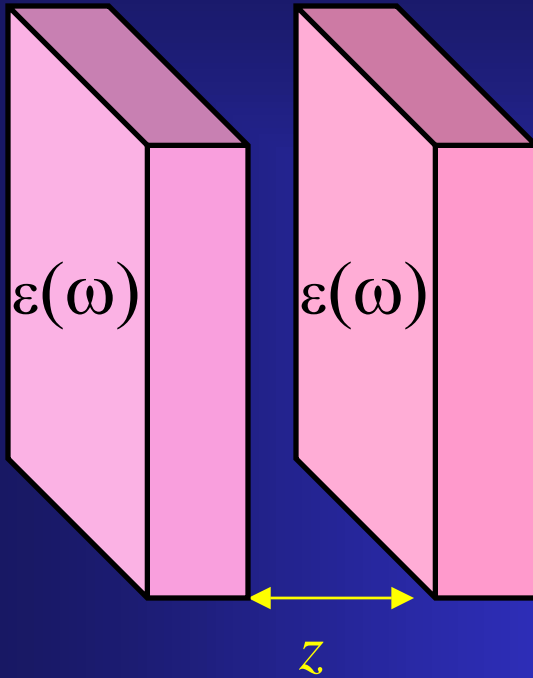
Residual voltage dependence on distance



$$F_{total} = V^2 F_{electrostatic}(d) + F_{Casimir}(d)$$

Finite conductivity corrections

Lifshitz `1956



in material body:
fluctuating electromagnetic field
 \Leftrightarrow Charge and current fluctuations

+ boundary conditions

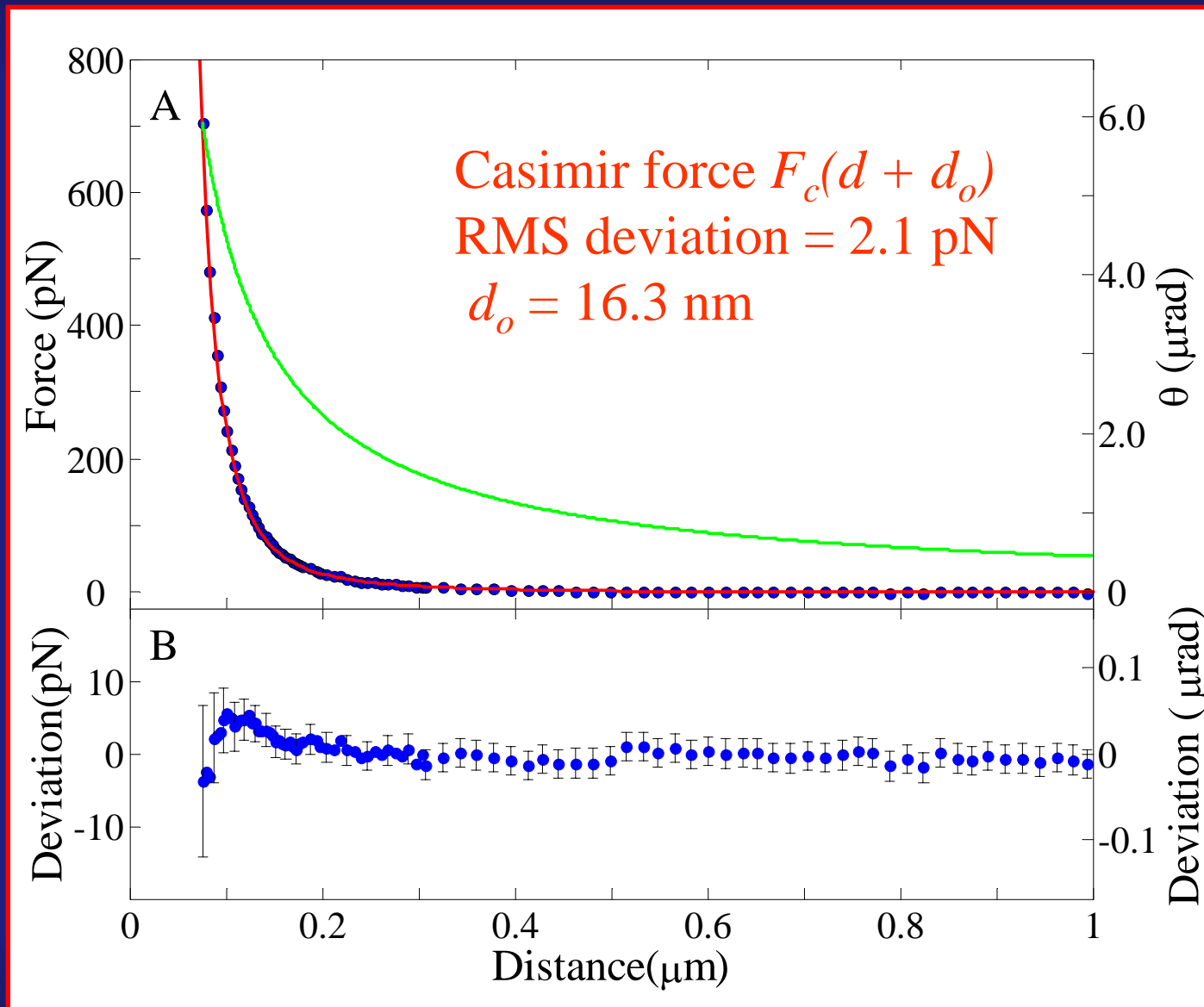
$$F_{Lifshitz}(z) = \frac{\hbar}{2\pi c^2} R \int_0^\infty \int_1^\infty p \xi^2 \left\{ \ln \left[1 - \frac{(s-p)^2}{(s+p)^2} e^{-2pz\xi/c} \right] + \ln \left[1 - \frac{(s-p\epsilon)^2}{(s+p\epsilon)^2} e^{-2pz\xi/c} \right] \right\} dp d\xi$$

$$s = \sqrt{\epsilon(i\xi) - 1 + p^2} \quad \epsilon(i\xi) = \frac{2}{\pi} \int_0^\infty \frac{x \epsilon''(x)}{x^2 + \xi^2} dx + 1 \quad \text{Kramers-Kronig}$$

Need: $z, \epsilon''(\omega)$

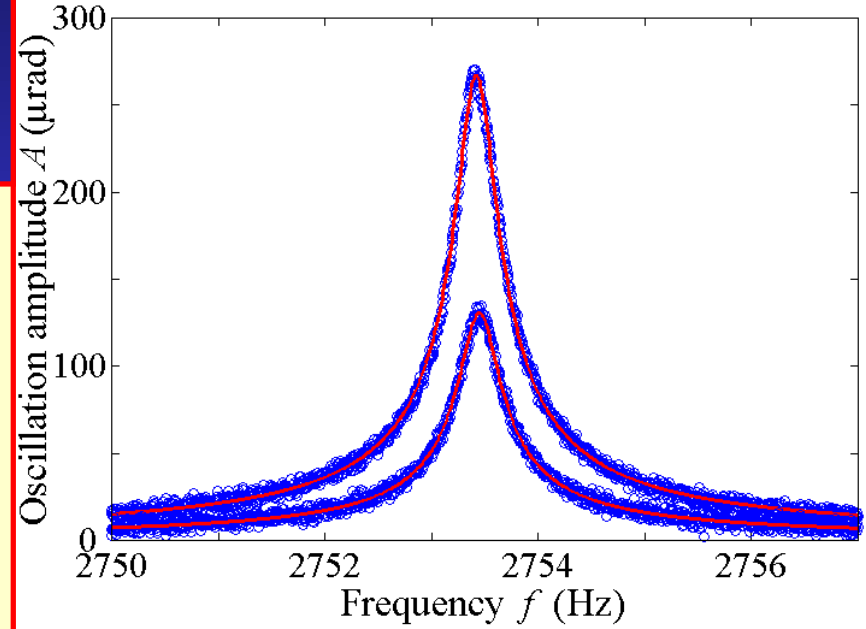
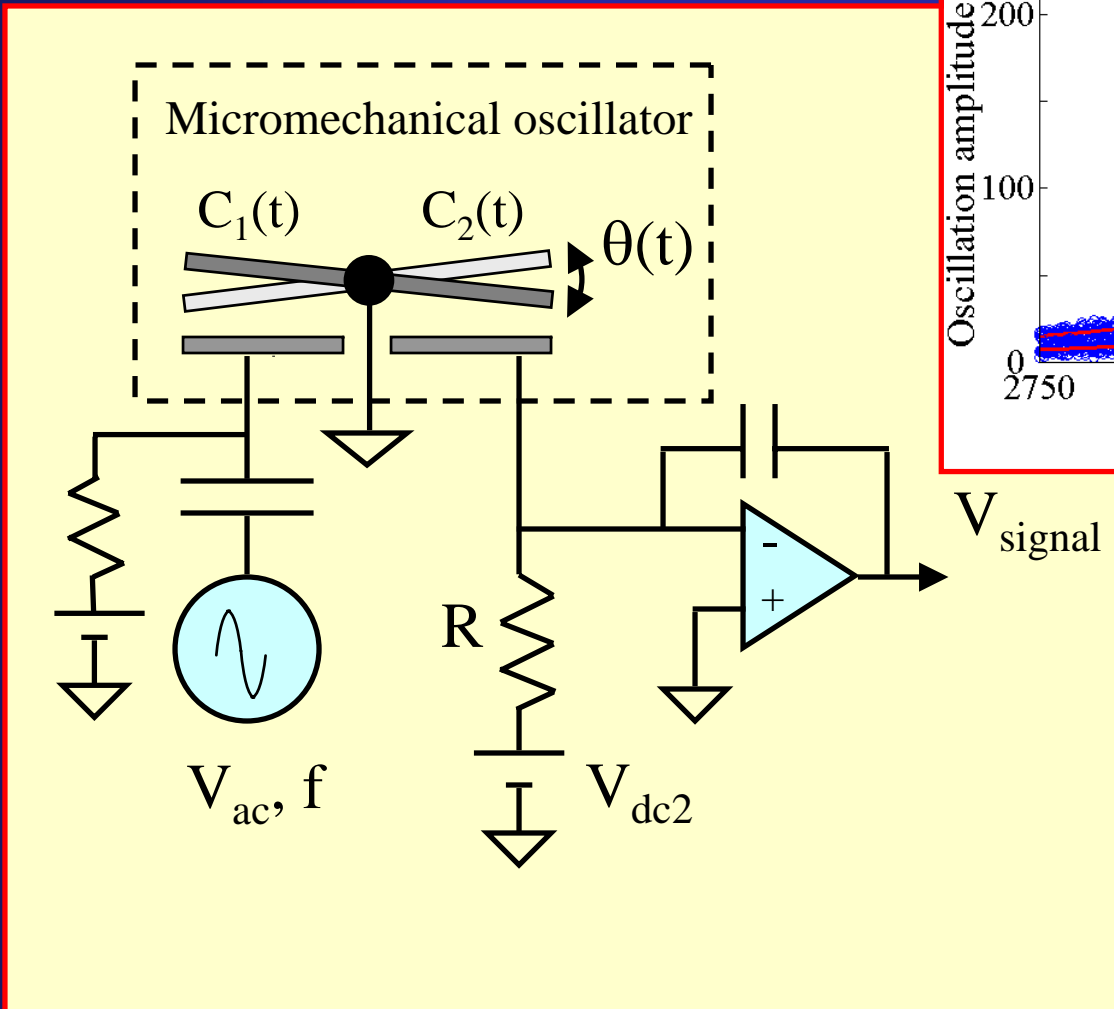
← tabulated in data books

Casimir force with roughness and finite conductivity corrections



Chan *et al.*, Science **291**, 1941 (2001).

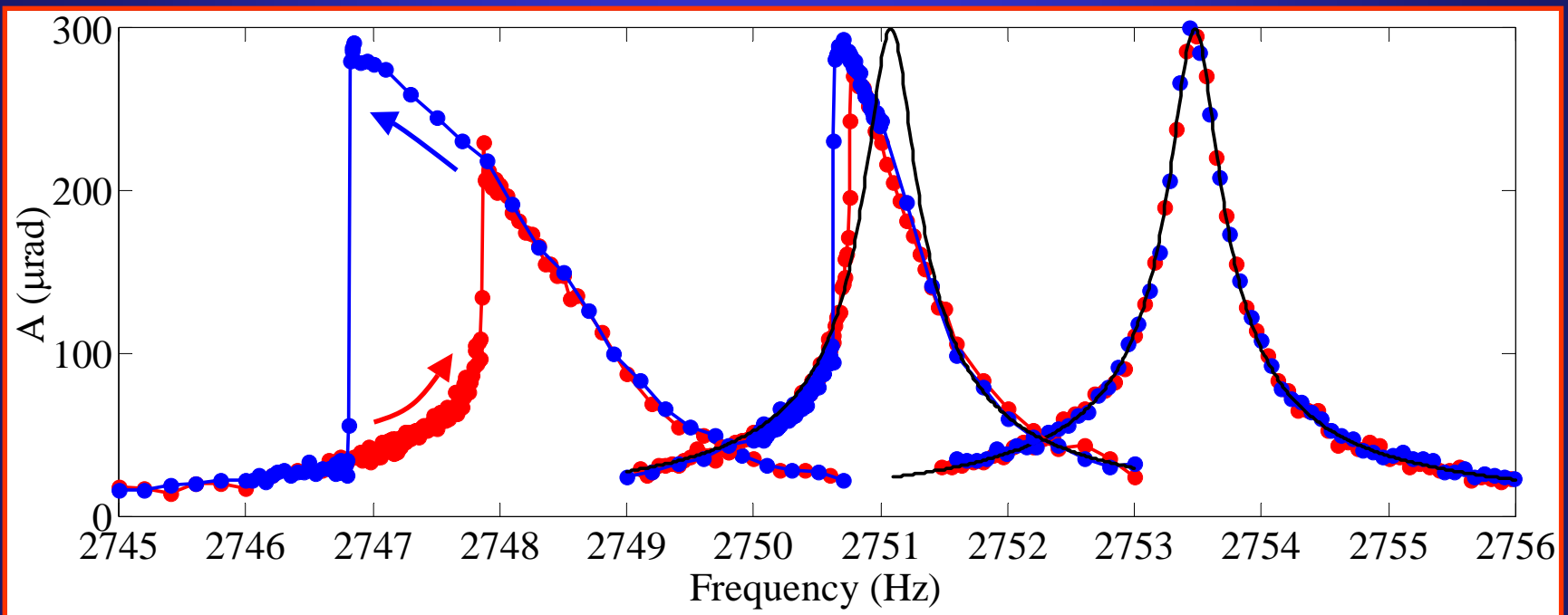
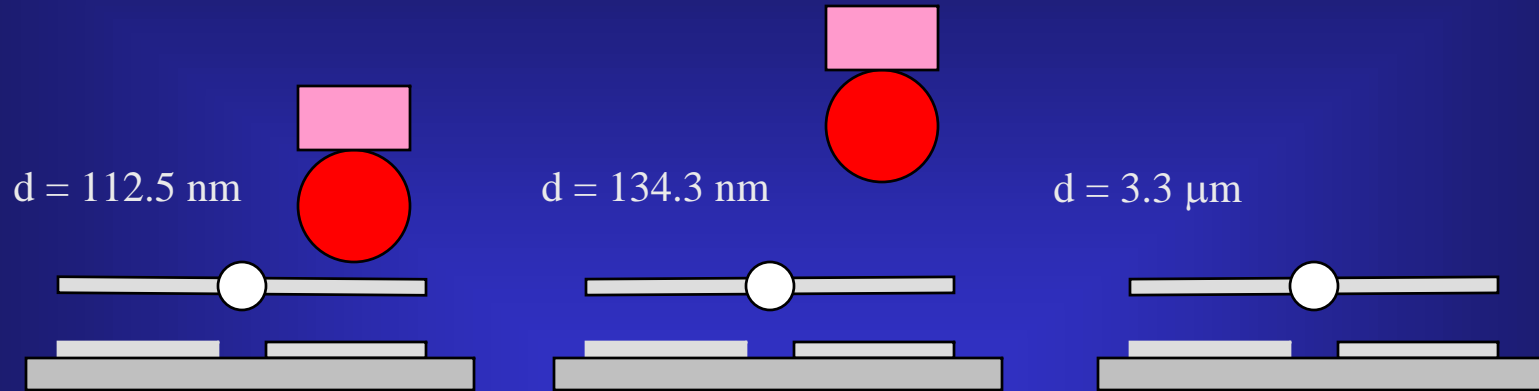
Simple Harmonic Oscillations



At small excitation,
response depends linearly
on excitation voltage

$$Q = 7150$$

Nonlinear behavior induced by the Casimir force

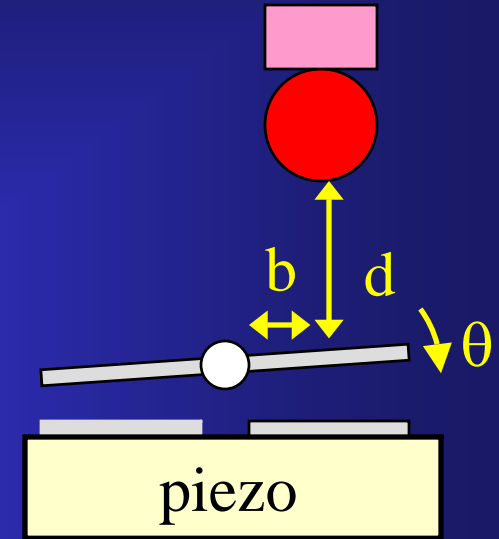


Anharmonic Oscillator: Equation of motion

$$I\ddot{\theta} + \lambda\dot{\theta} + k\theta = \tau \cos \omega t + bF(d + b\theta)$$

Taylor series:

$$F(d + b\theta) = F(d) + F'(d)(b\theta) + \frac{1}{2}F''(d)(b\theta)^2 + \frac{1}{6}F'''(d)(b\theta)^3$$



$$\ddot{\theta} + 2\gamma\dot{\theta} + \left[\omega_o^2 - \left(\frac{b^2}{I} \right) F'(d) \right] \theta = \left(\frac{\tau}{I} \right) \cos \omega t + \frac{bF(d)}{I} - \alpha\theta^2 - \beta\theta^3$$

Frequency shift:

$$\Delta\omega = -\frac{b^2}{2I\omega_o} F'(d)$$

Nonlinear terms:

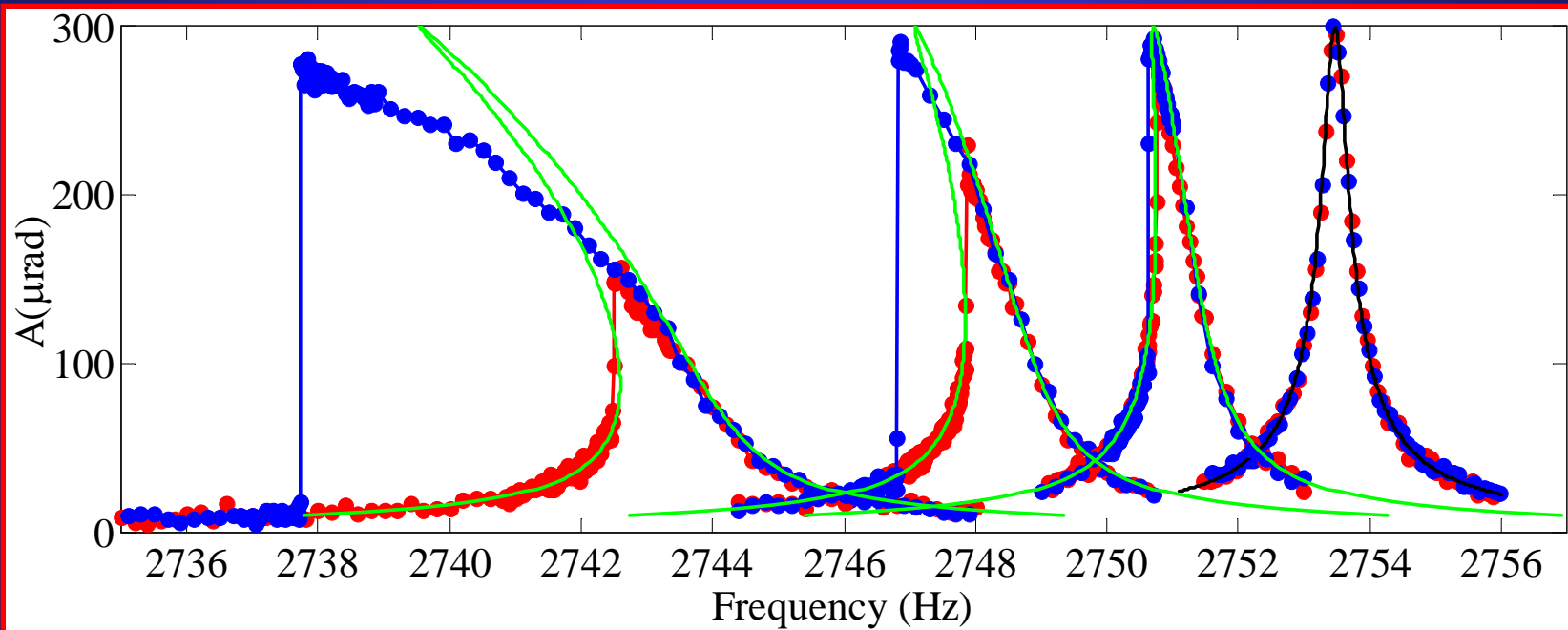
$$\alpha = -b^3 F''(d)/2I \quad \beta = -b^4 F'''(d)/6I$$

Nonlinear Casimir oscillator

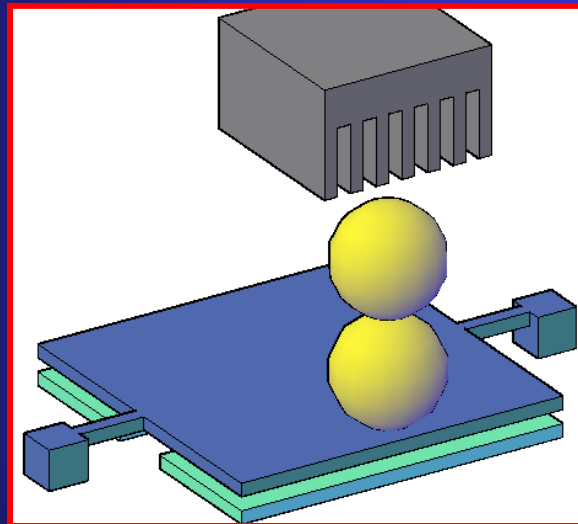
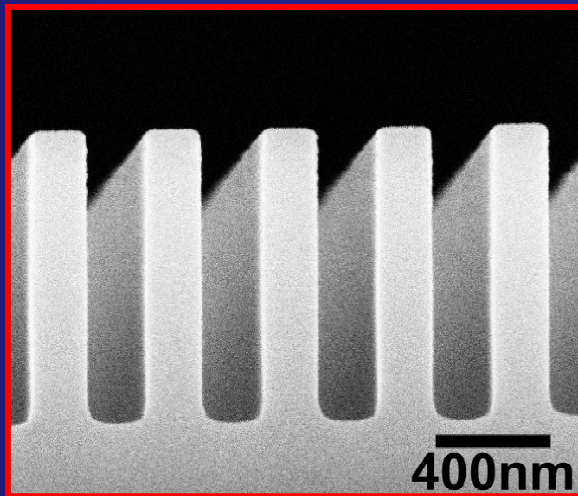
$$I\ddot{\theta} + \lambda\dot{\theta} + k\theta = \tau \cos \omega t - \alpha\theta^2 - \beta\theta^3$$

Strongly nonlinear oscillator

bistability and hysteresis



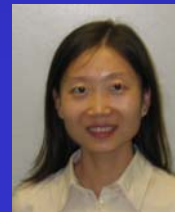
Geometry dependence of the Casimir force: Nanoscale trench arrays



Ho Bun Chan (U Florida)

Yiliang Bao (U Florida)

Jie Zou (U Florida)



Yiliang
Bao



Jie Zou

Ray Cirelli (Bell Labs)

Fred Klemens (Bell Labs)

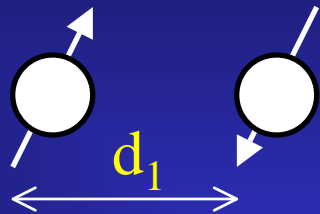
Bill Mansfield (Bell Labs)

C.S. Pai (Bell Labs)



Chan et al., PRL 101, 030401 (2008).

Quantum fluctuations: Casimir force vs van der Waals' force



$$d_1 < c \tau$$

$$V_{vdw} = -\frac{B}{r^6}$$



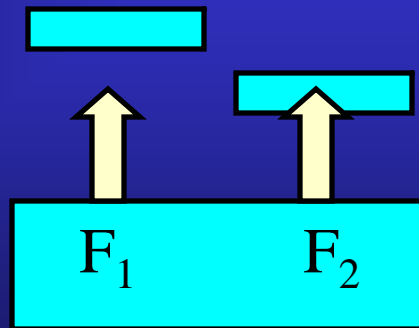
$$d_2$$

$$d_2 > c \tau$$

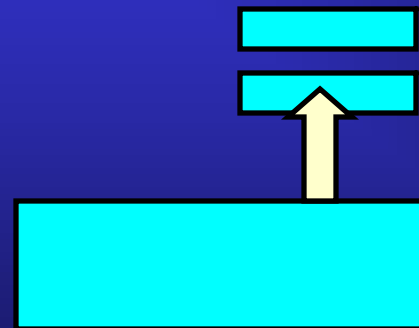
$$V_{retarded\ vdw} = -\frac{B'}{r^7}$$

retardation effects: finite propagation speed of light

Non-pairwise additivity



$$F_{total} \sim F_1 + F_2$$



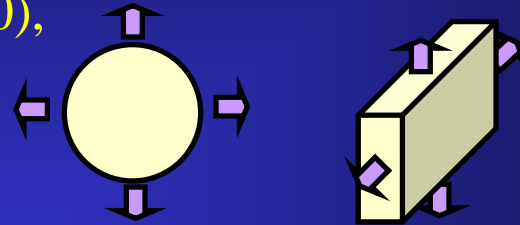
$$F_{total} \neq F_1 + F_2$$

Repulsive Casimir force and micromechanics

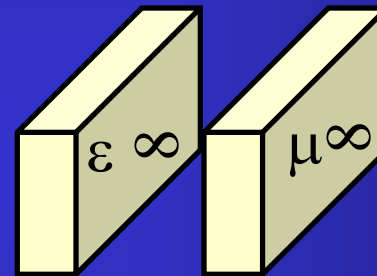
If experimentally feasible, repulsive Casimir force can potentially reduce stiction.

1. Closed geometries: Boyer (1968), Maclay (2000),

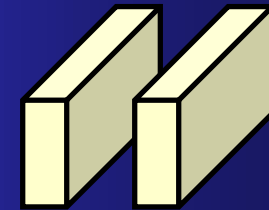
cannot cut sphere or box in half



2. Make one surface infinitely permeable (Hushwater 96)



3. Introduce liquid into the gap (current experiments by Capasso)



4. Possible use of meta material (Leonhardt and Philbin 2007)

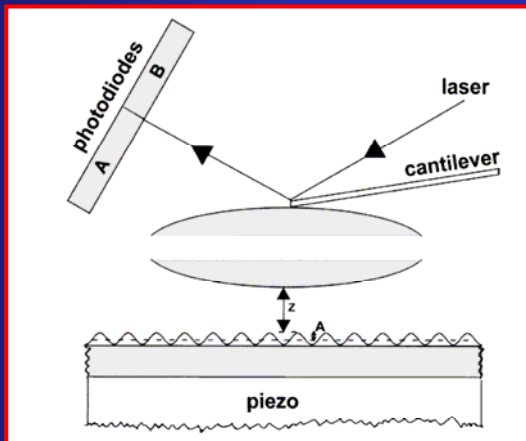
need negative index over a wide spectral range

introduce gain (Lifshitz formula no longer applies)

It remains a major challenge to generate repulsive Casimir force with a vacuum gap.

Experimental attempts to demonstrate the non-trivial boundary dependence of the Casimir force

- Experiment: Roy & Mohideen, PRL **82**, 4380 (1999).



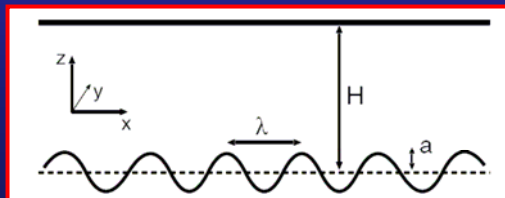
A large sphere and a plate with periodic sinusoidal corrugation

$$a = 59.4\text{nm}, \lambda = 1.1 \mu\text{m}, H/\lambda \approx 0.1-0.8$$

Measured force exceeds pairwise additive interaction

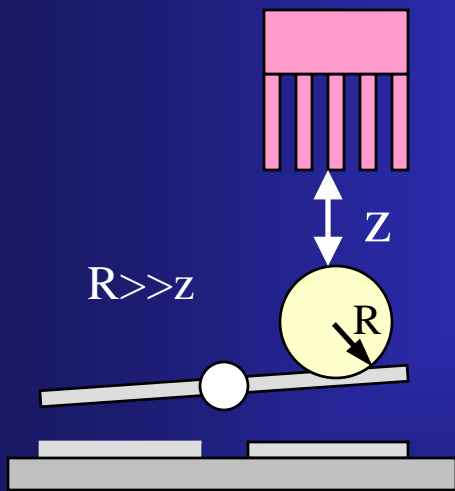
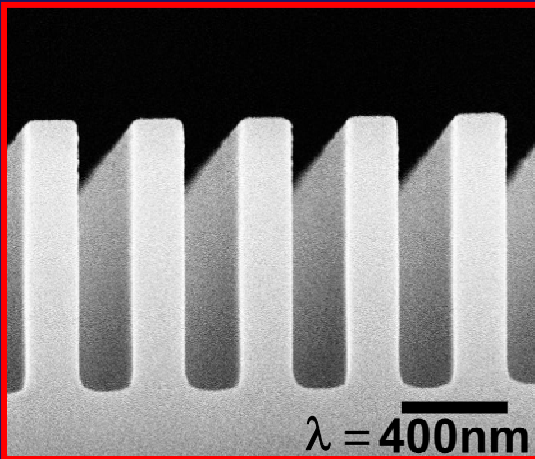
Klimchitskaya *et al.* PRA 63, 014101 (2001):
possibility of lateral force

- Theory: Emig, Hanke, Golestanian & Kardar, PRL **87**, 260402 (2001):
a path integral quantization of the electromagnetic field



Correction is strong with large H/λ

Non-trivial boundary dependence of the Casimir force

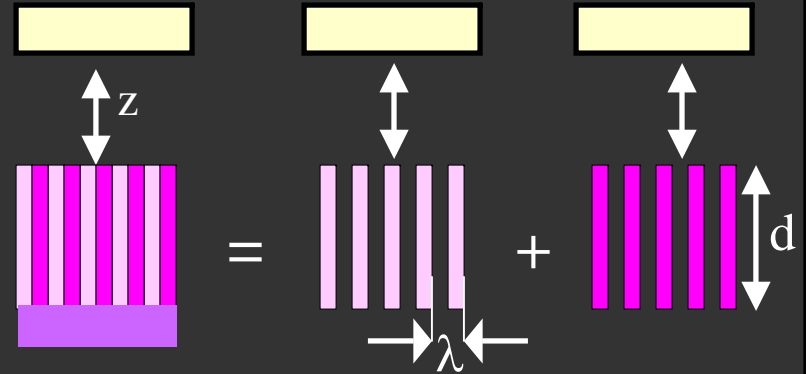


Chan et al., PRL 101, 030401 (2008).

Pairwise additive approximation (PAA)

If $d \gg z$, for all λ ,

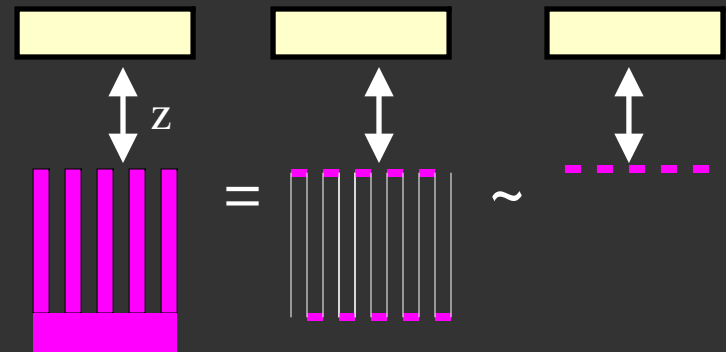
$$F_{\text{corrugated}}(z) = \frac{1}{2} F_{\text{flat}}(z)$$



Proximity force approximation (PFA)

If $d \gg z$, for all λ ,

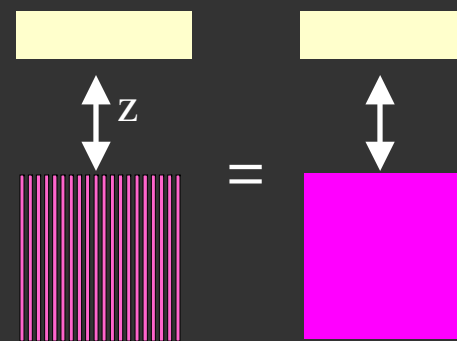
$$F_{\text{corrugated}}(z) = \frac{1}{2} F_{\text{flat}}(z)$$



Casimir force for perfect metal

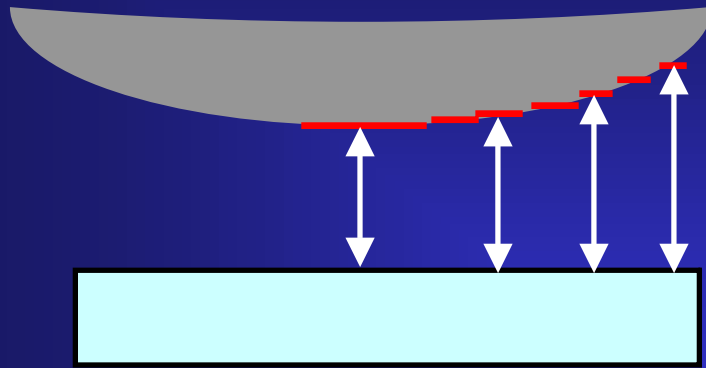
for $\lambda \ll z$,

$$F_{\text{corrugated}}(z) = F_{\text{flat}}(z)$$



Buscher & Emig, PRA 69, 062101 (2004).

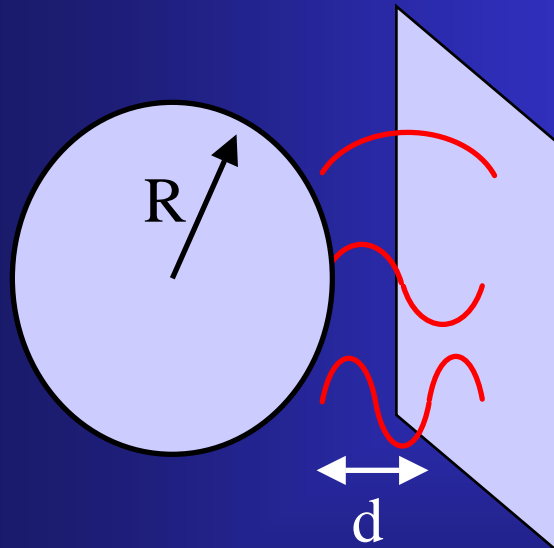
Experiments measuring Casimir force:



Proximity force approximation

Valid for $d \ll R$

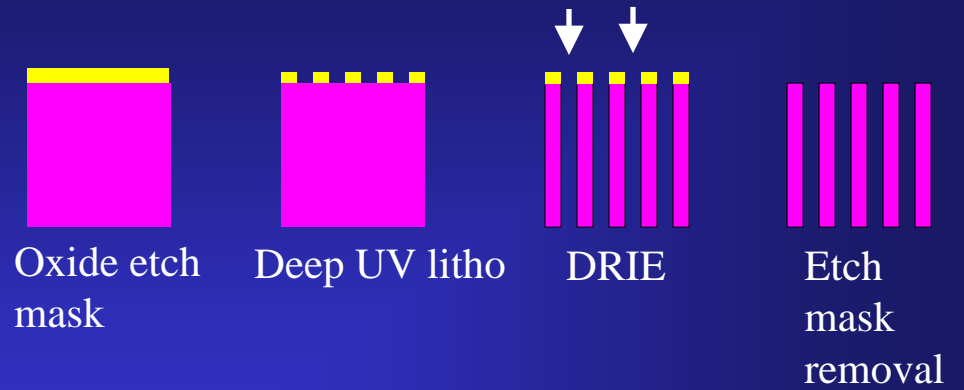
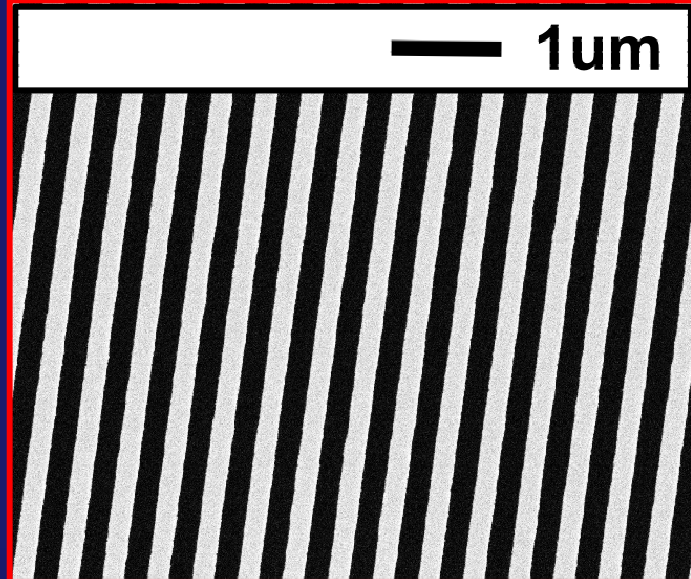
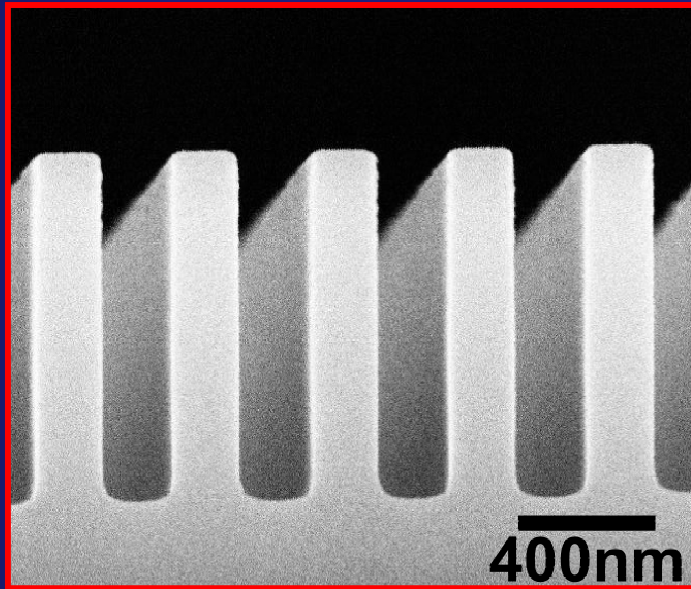
(typical $d \sim 100$ to 400 nm, $R \sim 50$ to 100 μm)



$$F_{\text{Casimir}} = -\frac{\pi^3 R \hbar c}{360 d^3}$$

- Lamoreaux '1997
Torsional Pendulum
5% agreement with theory
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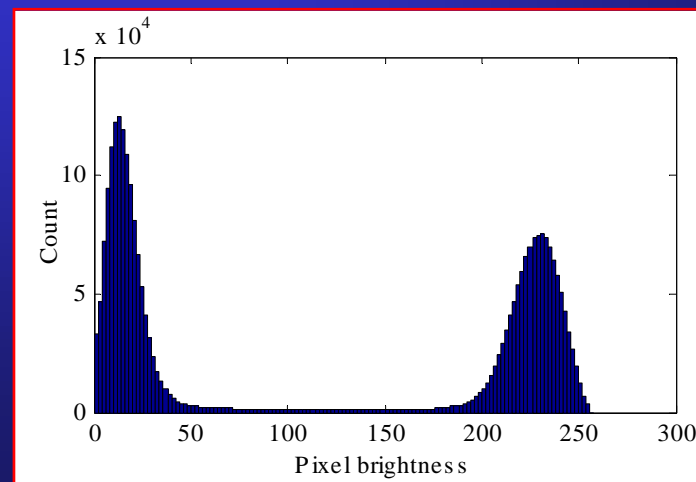
Sample fabrication and characterization



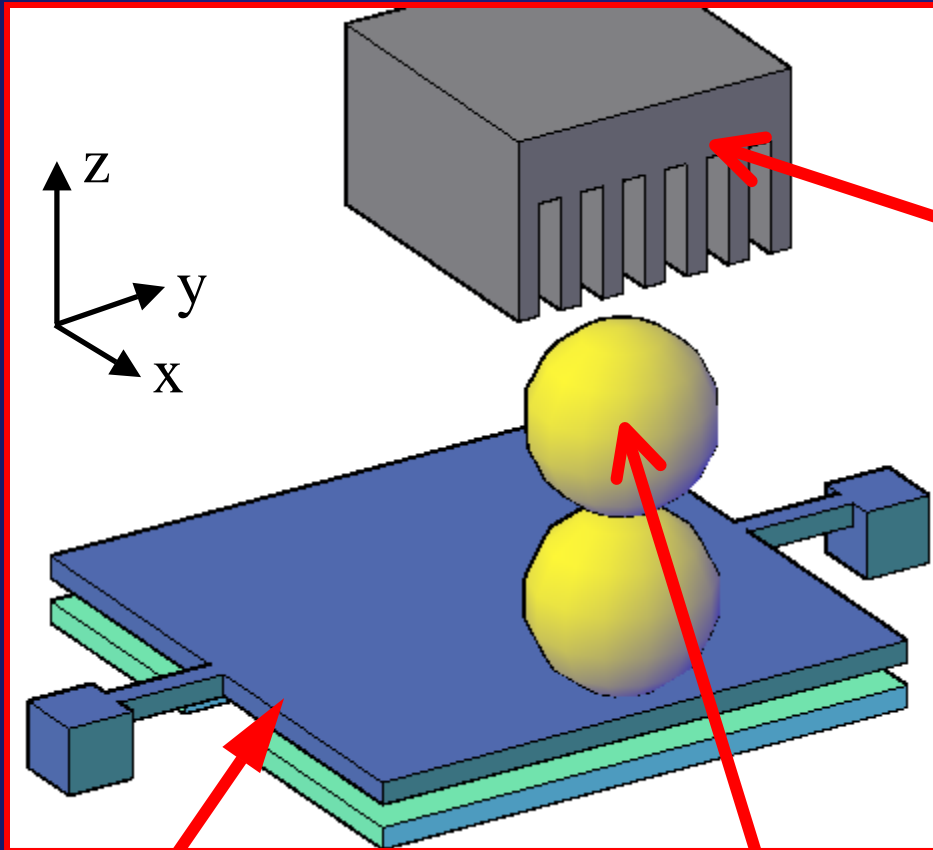
Solid fraction $p = 0.51 + 0.001$

histogram of pixel brightness in top view
average from 10 pictures

Depth = 1.07 um



Experiment setup



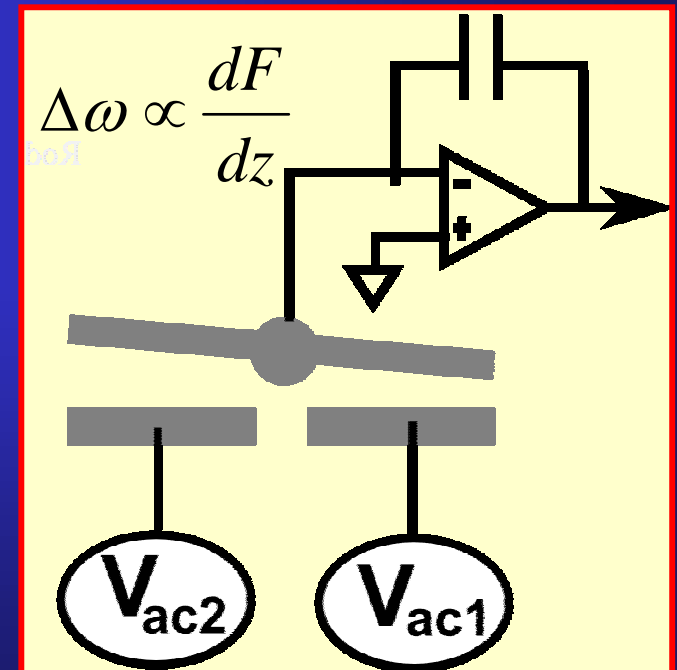
Sample orientation eliminate lateral motion.

Immediately before pump down
HF remove native oxide layer, hydrogen
termination of the surface

poly-Si plate:
500 μm x 500 μm x 3.5 μm

Glass sphere: d~100 μm

Sputtering: 400nm gold



Calibration by electrostatic force

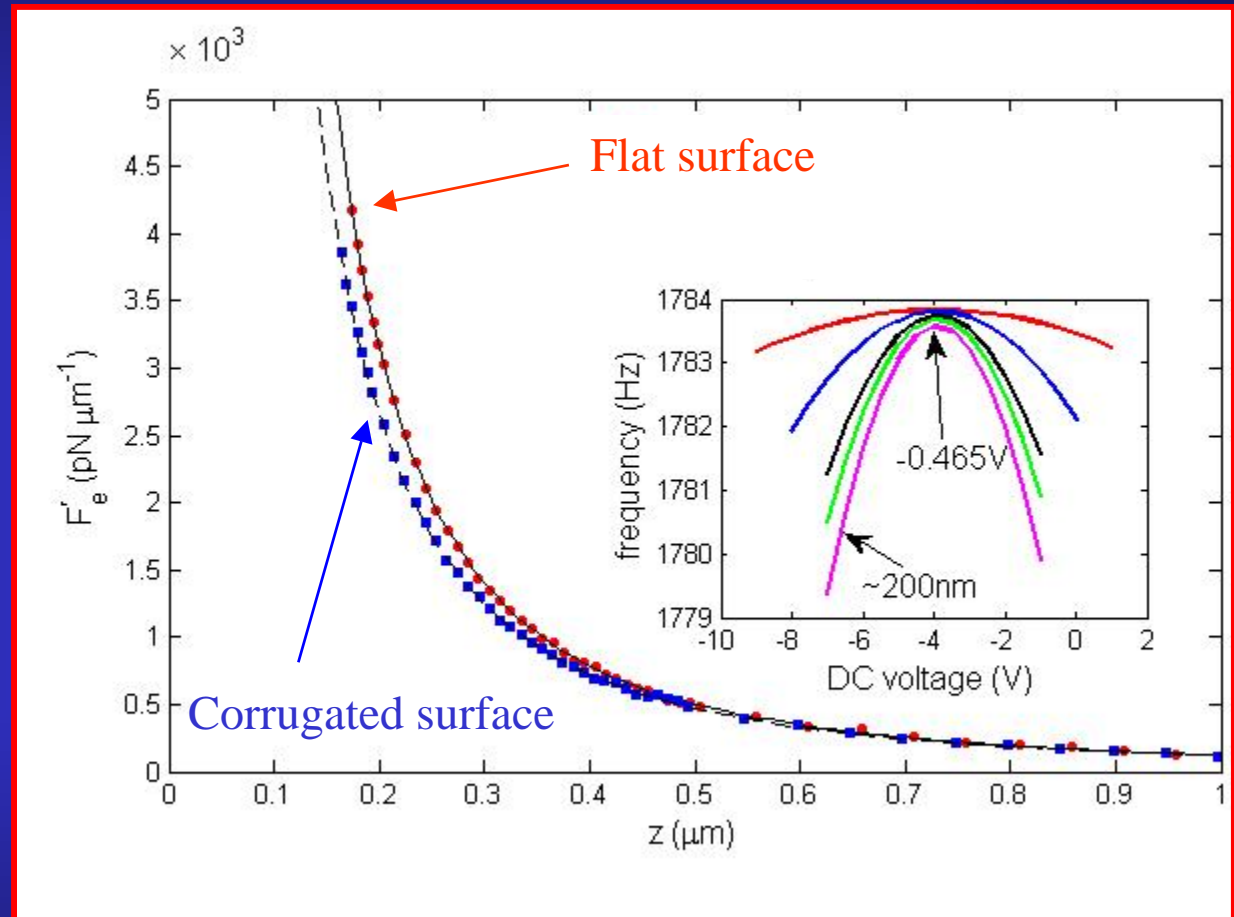
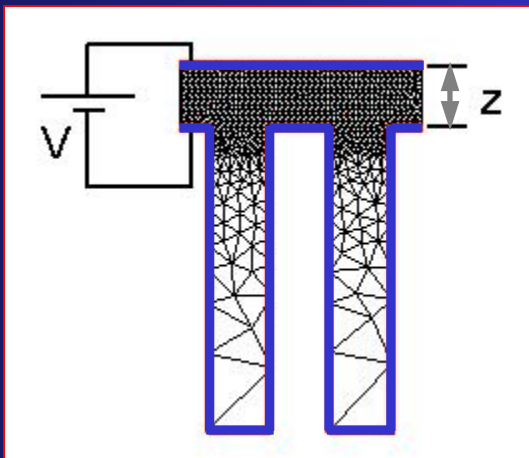
Flat surface

$$F'_e = \varepsilon_0 \pi R \frac{(V - V_0)^2}{(z + z_0)^2}$$

V_0 : residual voltage

z_0 : closest approach distance

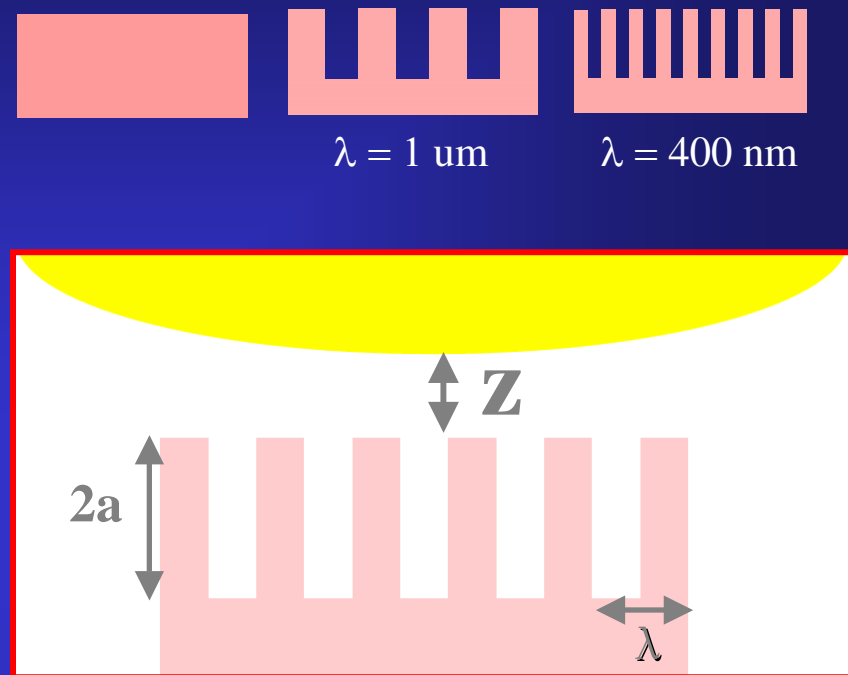
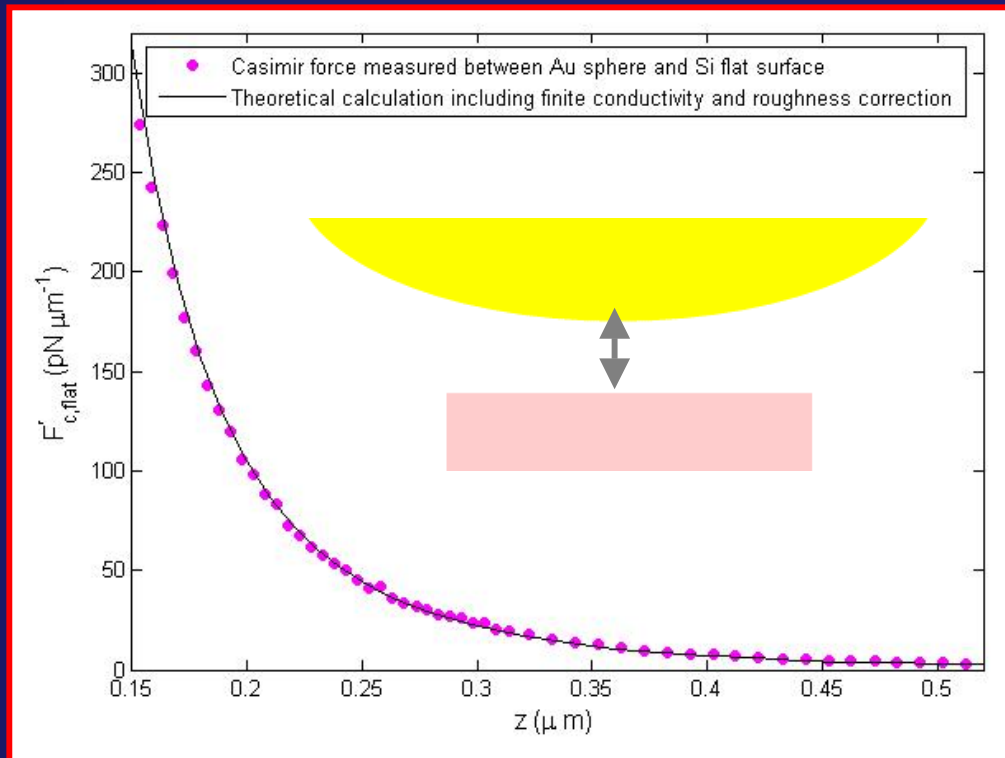
Corrugated surface



- Finite element analysis to solve 2D Poisson equation: $N > 10\,000$ triangles
- Proximity force approximation: $F_{\text{sphere-corrugate}} = 2 \pi R E_{\text{flat-corrugate}}$
- Check convergence: double N changes force by 0.1%

Casimir force measurements

3 samples made from the same silicon wafer



Pairwise additivity:

$$F_{c,trench} = \frac{1}{2} F_{c,flat}$$

For all λ

For solid fraction p :

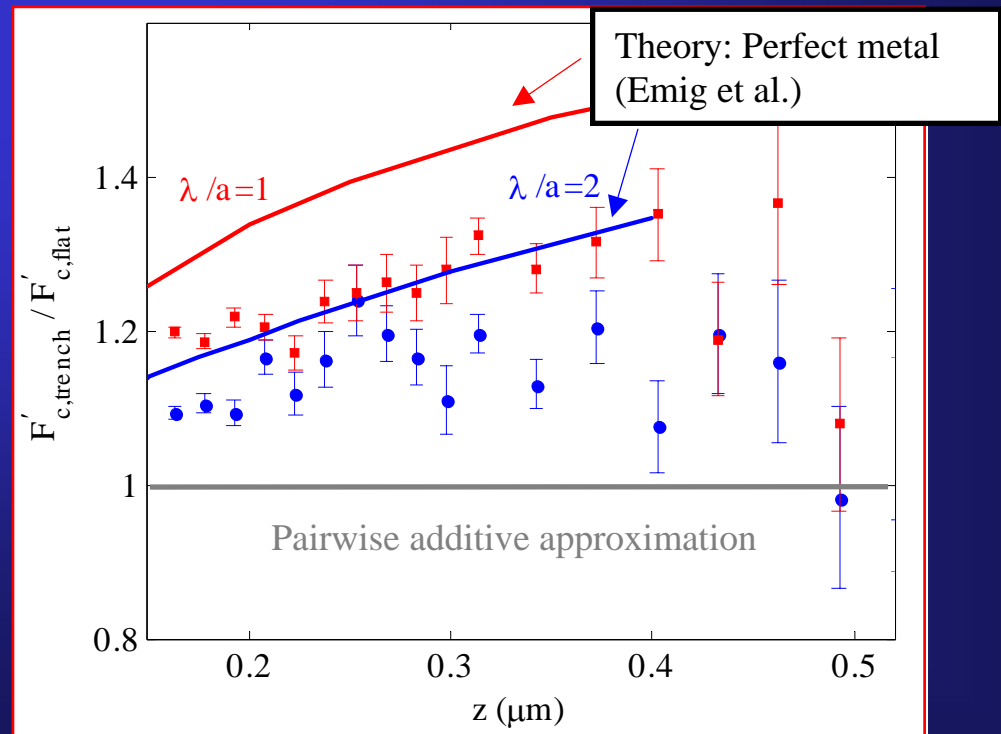
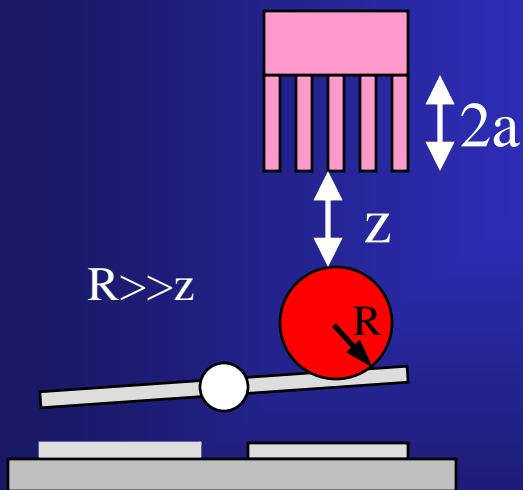
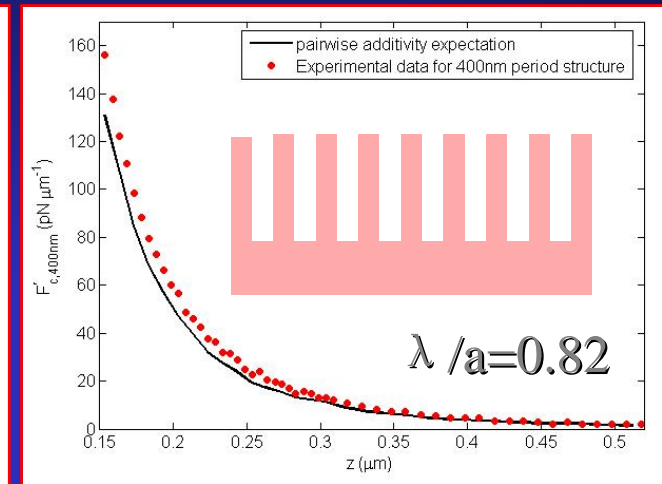
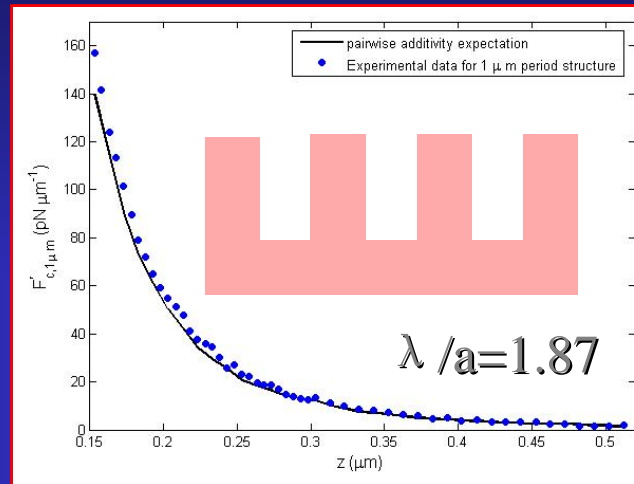
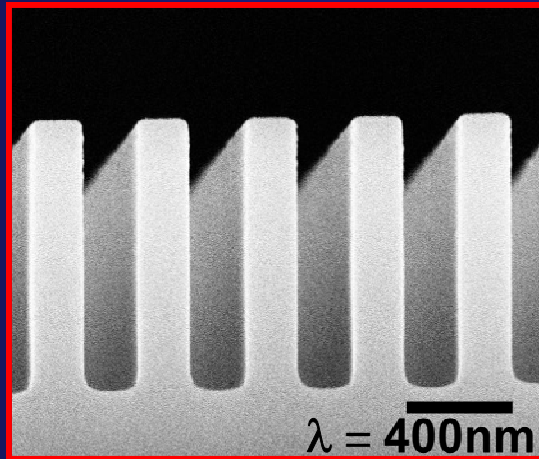
$$F_{c,trench} = p F_{c,flat}$$

For all material

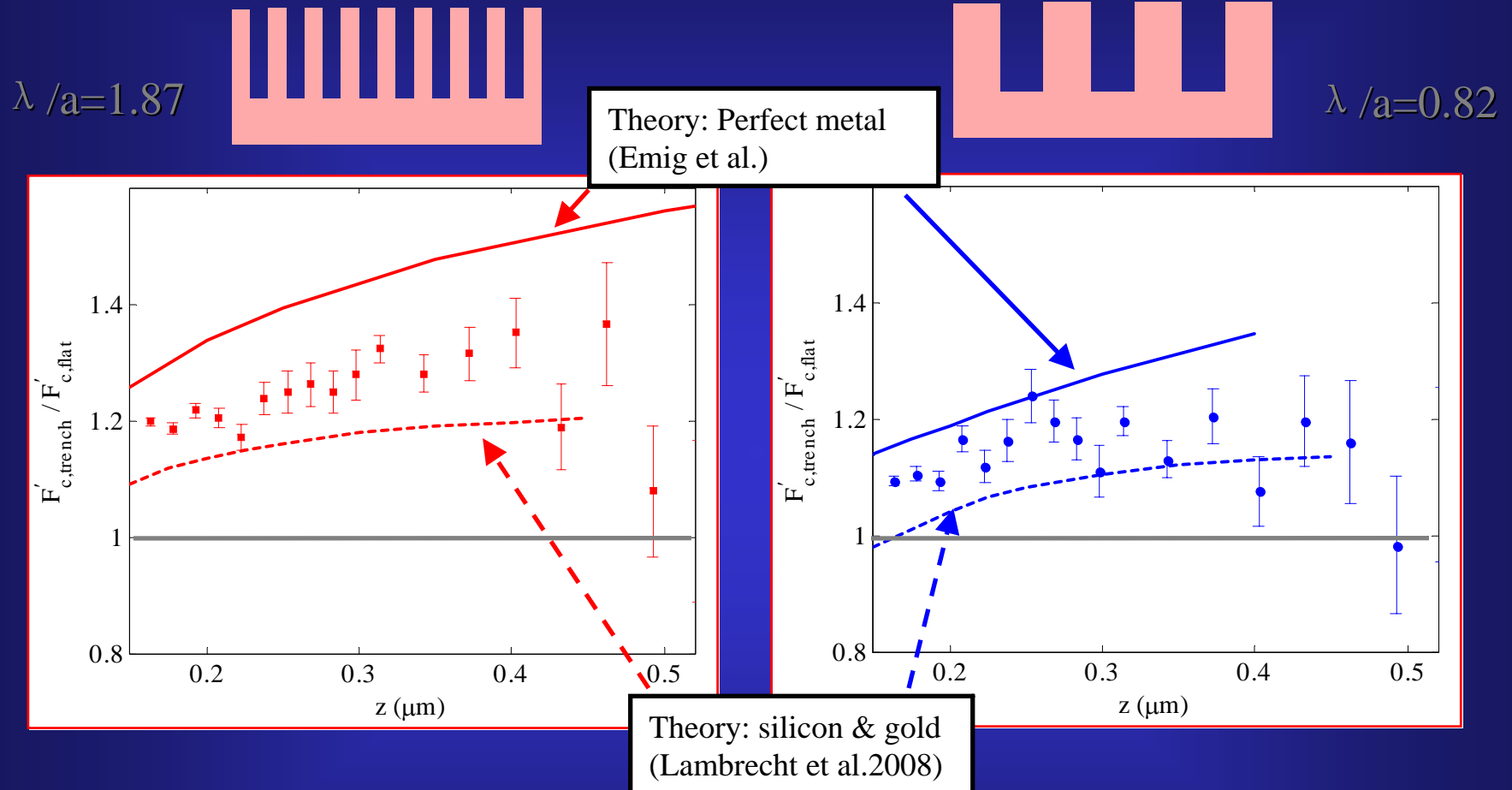
Any deviation of measured force on corrugation from $pF_{c,flat}$

→ deviation from pairwise additivity (dependence of Casimir force on geometry)

Non-trivial boundary dependence of the Casimir force



Interplay of finite conductivity and geometry effects



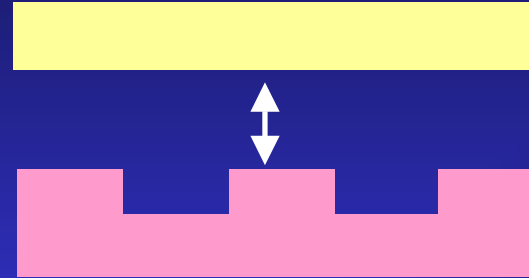
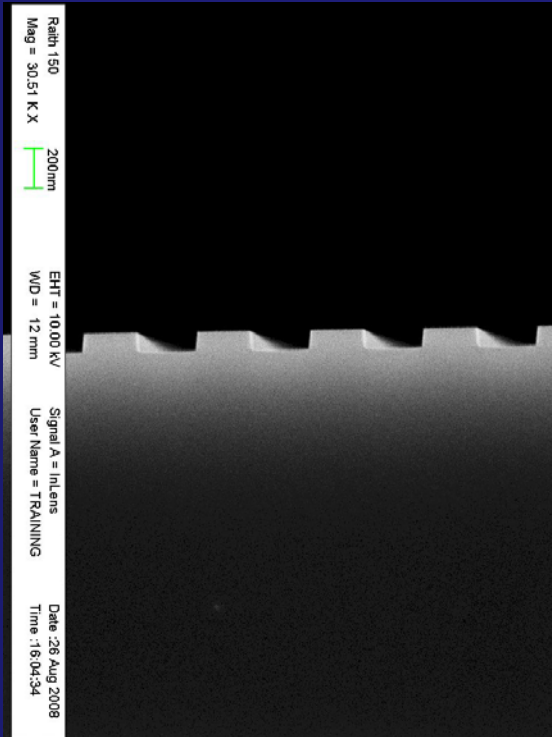
Lambrecht & Marachevsky 2008: includes both finite conductivity and geometry effects.

Using reflection coefficients and argument principle

Possible reason for discrepancy:

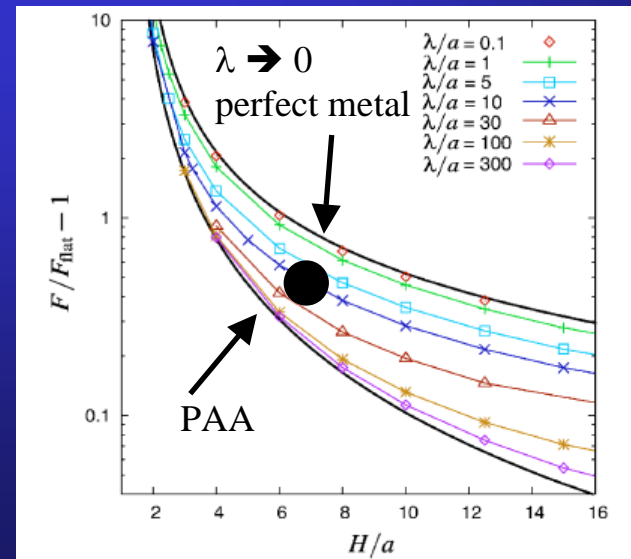
uncertainties in the optical properties of gold and silicon

In progress: shallow trench arrays



Contribution of bottom surface not negligible
Easier for comparison to theory (perturbative approaches)

↑ Deep trench experiment ($\lambda/a = 0.8$, $H/a \sim 1$)



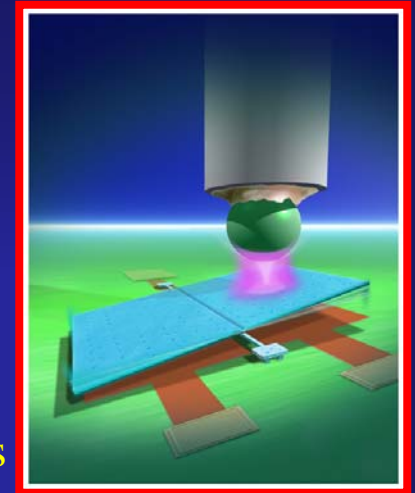
Buscher & Emig, PRA **69**, 062101 (2004).

Summary

- Micromechanical torsional oscillator for measuring the Casimir force.
- nonlinear Casimir micromechanical oscillator.
- Geometry dependence of the Casimir force:
- Experiment on strongly deformed surface: array of nanoscale trenches

Up to 30% deviation from pairwise additive approximation

A factor of 2 smaller than theory on perfect metals



Collaborators

University of Florida

Yiliang Bao

Jie Zou

University Paris-Sud

Thorsten Emig

UT Brownsville

Andreas Hanke

Bell Labs

Federico Capasso

Vladimir Aksyuk

Raffi Kleiman,

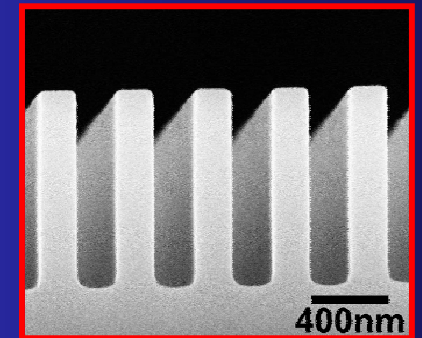
David Bishop

Ray Cirelli

Fred Klemens

Bill Mansfield

C.S. Pai



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