

Low SNR detections of p-modes

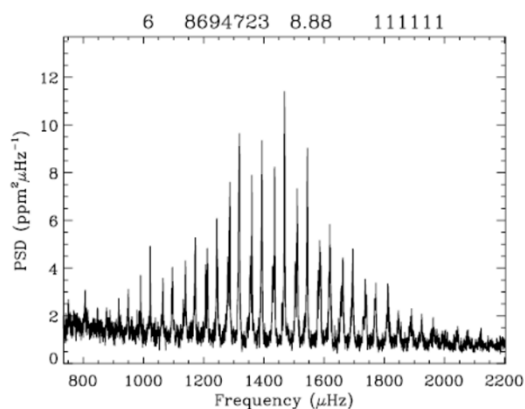
Using asteroseismology to characterize a large number of TESS host stars

Hans Kjeldsen



STELLAR ASTROPHYSICS CENTRE

Properties of exoplanet host stars using Asteroseismology

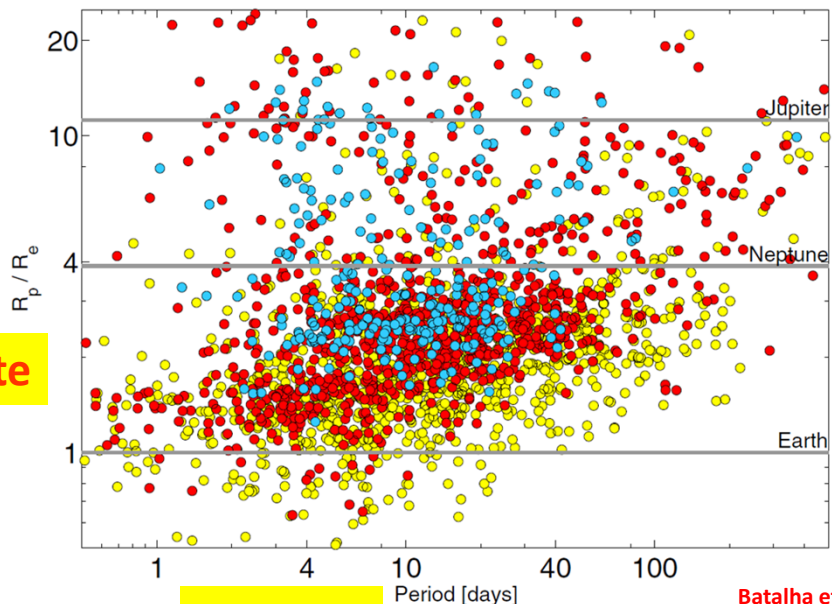


- Time series data
- Low amplitude
- Multi-mode oscillations
- High frequencies

- Detection of a transit (exoplanet):
Radius ratio, Orbital period
- **Asteroseismology (host star):**
Stellar Properties: Mass, Radius, Density, Age, Rotation (spin-orbit)
- Ground-based follow-up (exoplanet):
Velocity signature: Mass ratio

Kepler transits

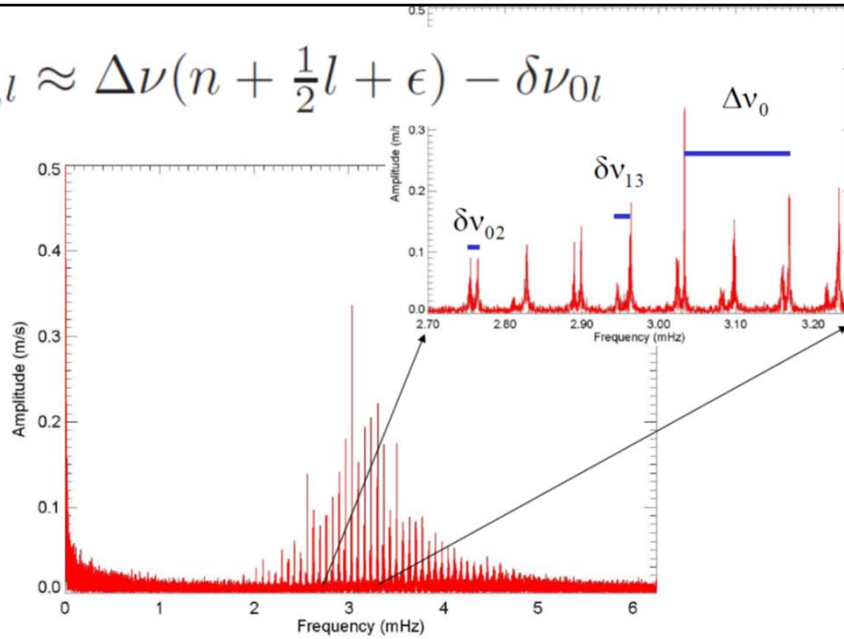
Less accurate



Batalha et al. 2013

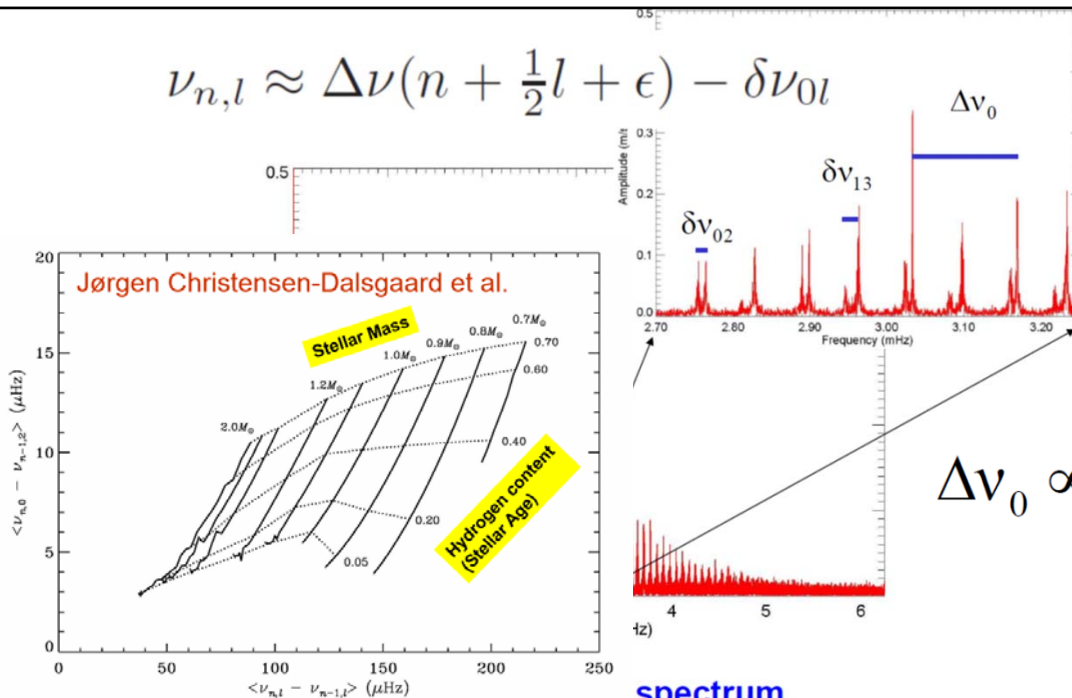
Figure 3. Radius vs. orbital period for exoplanets in the B10 (Borucki et al. 2011a) catalog (blue points), the B11 (Borucki et al. 2011b) catalog (red points), and this contribution (yellow points). Horizontal lines marking the radius of Jupiter, Neptune, and Earth are included for reference.

$$\nu_{n,l} \approx \Delta\nu(n + \frac{1}{2}l + \epsilon) - \delta\nu_{0l}$$



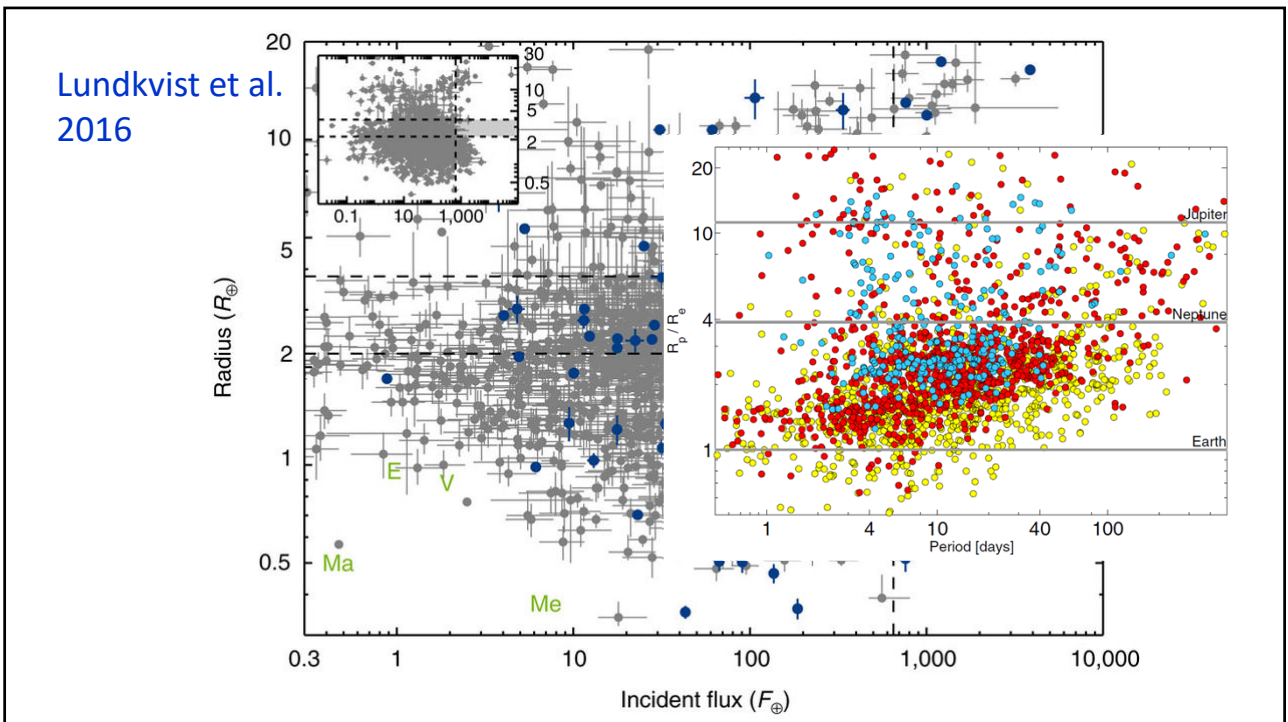
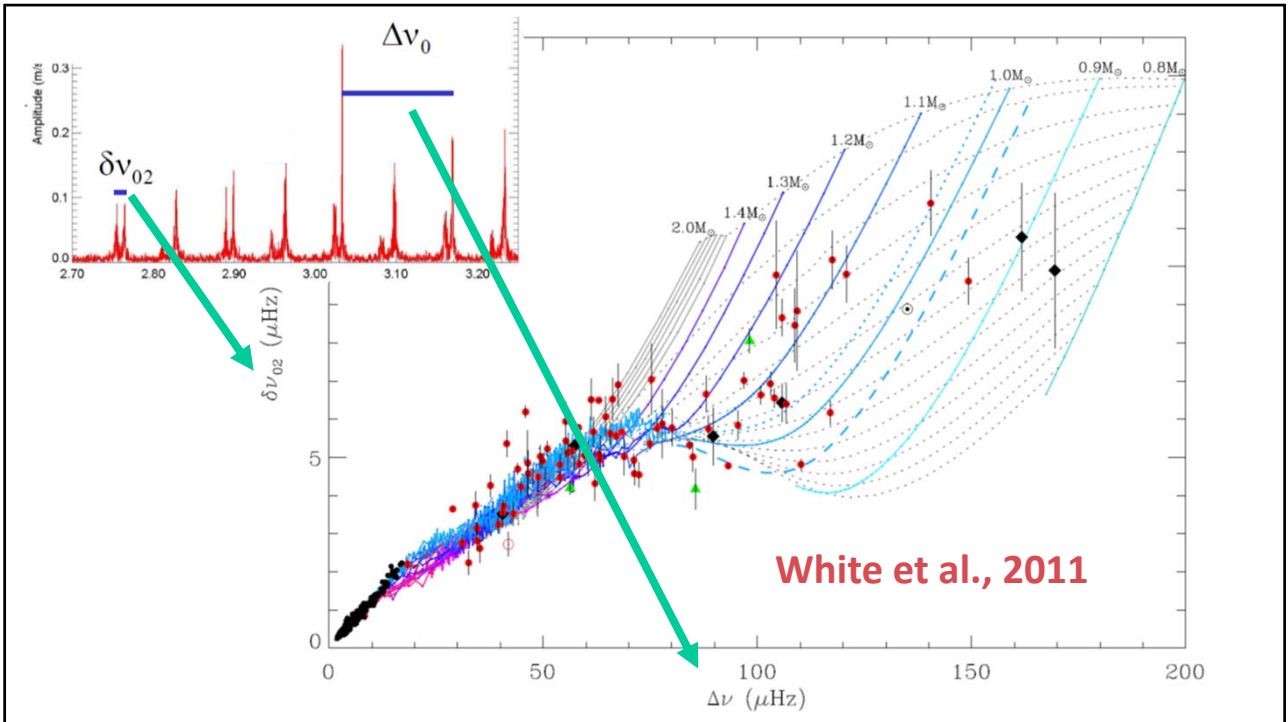
Solar oscillation spectrum

$$\nu_{n,l} \approx \Delta\nu(n + \frac{1}{2}l + \epsilon) - \delta\nu_{0l}$$

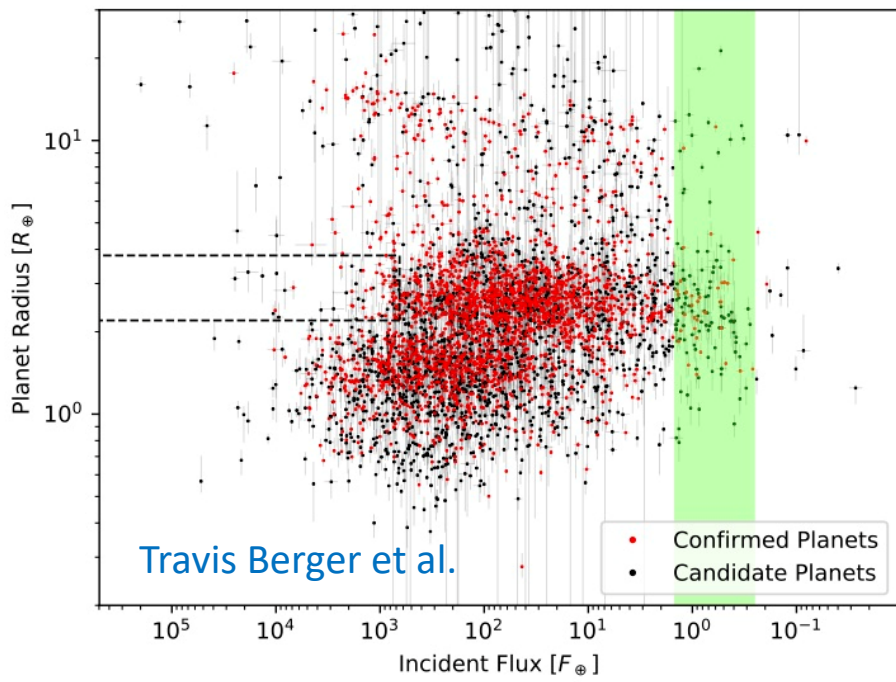
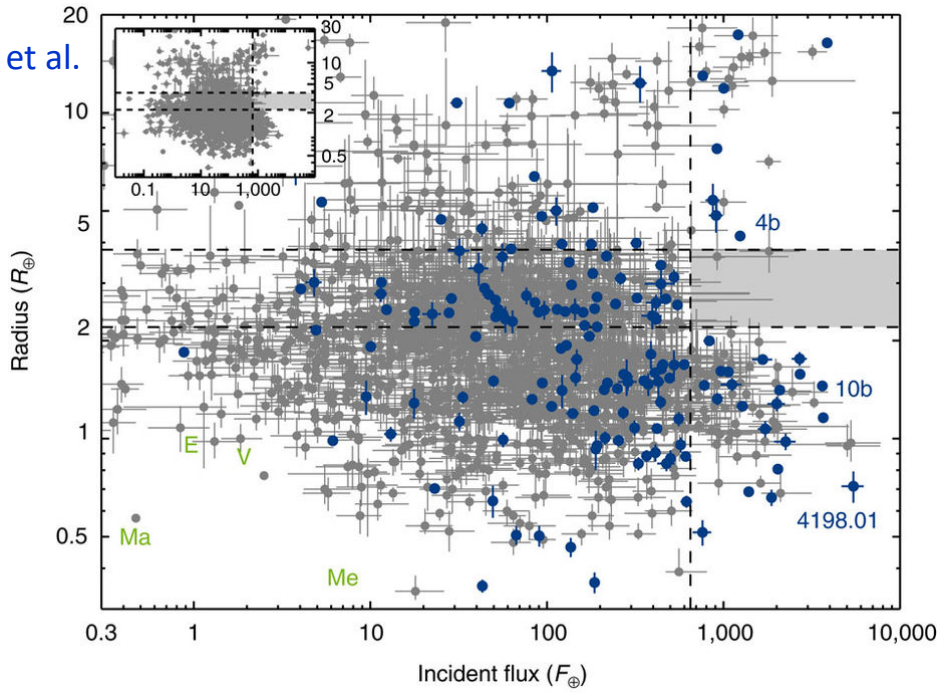


spectrum

$$\Delta\nu_0 \propto \sqrt{\rho}$$



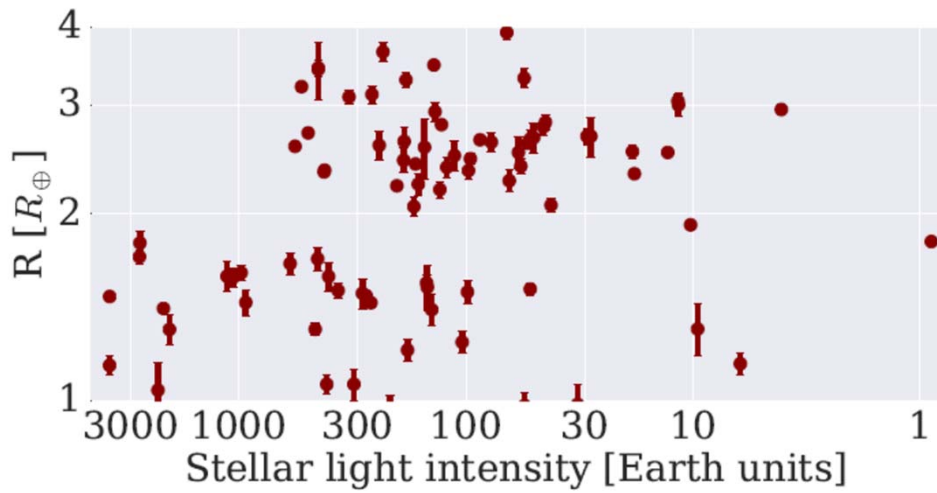
Lundkvist et al.
2016



Travis Berger et al.

• Confirmed Planets
• Candidate Planets

Van Eylen, Agentoft, Lundkvist, et al. 2018



Luminosity

$$L = R^2 \cdot T_{eff}^4 \quad \text{Solar units}$$



Flux at distance a

$$F = \frac{L}{a^2} \quad \text{Solar and Earth units}$$

$$a^3 = M \cdot P^2$$

Solar and Earth units

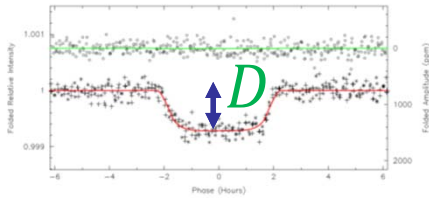
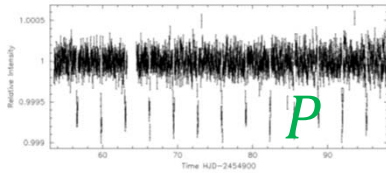
Planet Radius

$$r_p = 109 \cdot R \cdot \sqrt{D}$$

Solar and Earth units

Luminosity

$$L = R^2 \cdot T_{eff}^4 \quad \text{Solar units}$$



Flux at distance a

$$F = \frac{L}{a^2} \quad \text{Solar and Earth units}$$

$$a^3 = M \cdot P^2 \quad \text{Solar and Earth units}$$

Planet Radius

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Flux at distance a

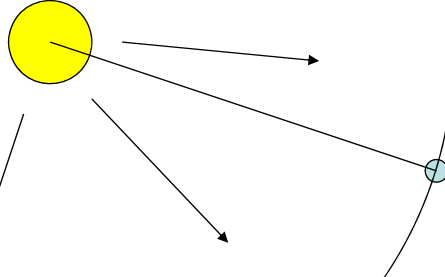
$$F = \frac{R^2 \cdot T_{eff}^4}{M^{2/3} \cdot P^{4/3}} \quad \text{Solar and Earth units}$$

Planet Radius

$$r_p = 109 \cdot R \cdot \sqrt{D} \quad \text{Solar and Earth units}$$

Luminosity

$$L = R^2 \cdot T_{eff}^4 \quad \text{Solar units}$$



Talk by Travis Berger

Flux at distance a

Gaia

Solar and Earth units

$$F = \frac{R^2 \cdot T_{eff}^4}{M^{2/3} \cdot P^{4/3}}$$

25%

Planet Radius

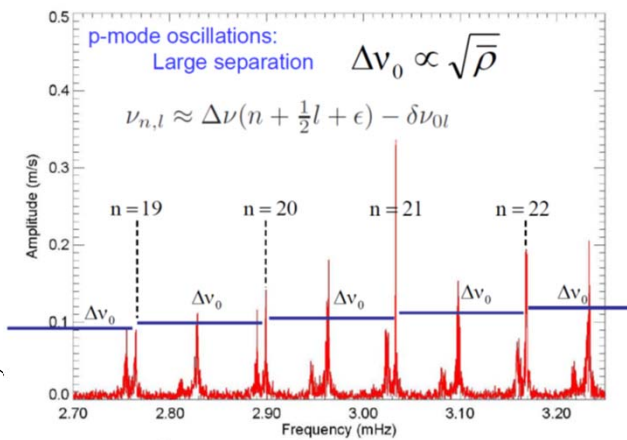
$$r_p = 109 \cdot R \cdot \sqrt{D}$$

8%

Solar and Earth units

Asteroseismology

$$R, \Delta\nu_0$$



Flux at distance a

$$F = \frac{T_{eff}^4}{\Delta\nu_0^{4/3} \cdot P^{4/3}}$$

Solar and Earth units

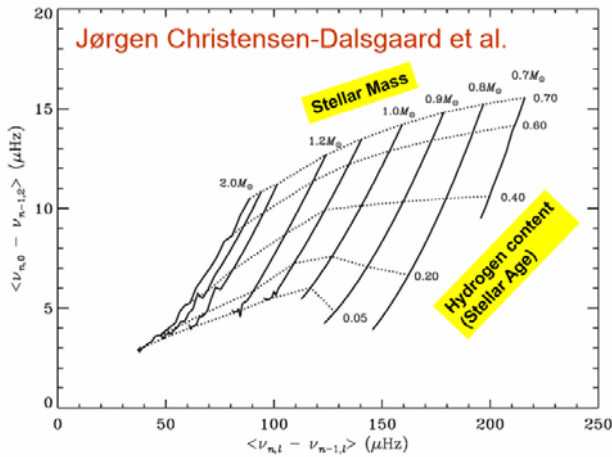
Planet Radius

$$r_p = 109 \cdot R \cdot \sqrt{D}$$

Solar and Earth units

Asteroseismology

$$R, \Delta\nu_0$$



Flux at distance a

$$F = \frac{T_{eff}^4}{\Delta\nu_0^{4/3} \cdot P^{4/3}}$$

Solar and Earth units

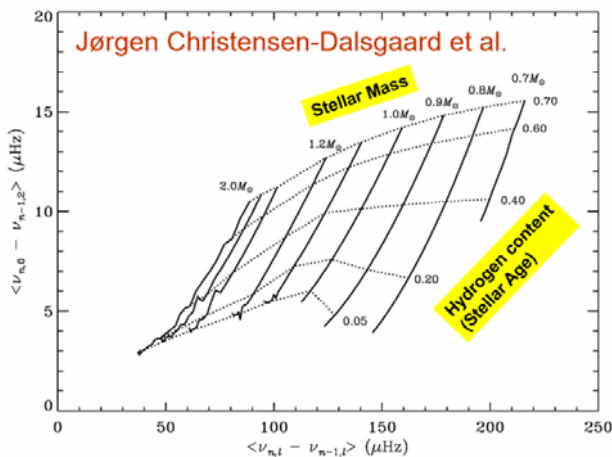
Planet Radius

$$r_p = 109 \cdot R \cdot \sqrt{D}$$

Solar and Earth units

Asteroseismology

$$R, \Delta\nu_0, \rho \text{ 1\%}$$



Flux at distance a

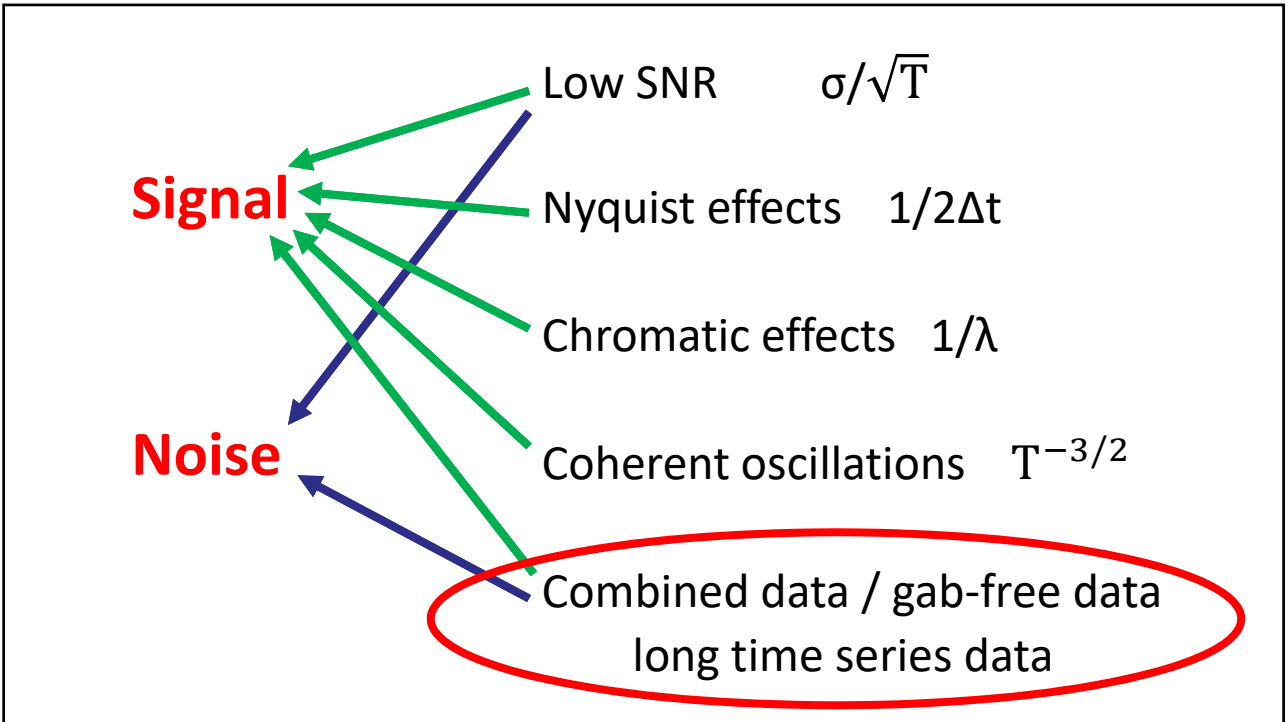
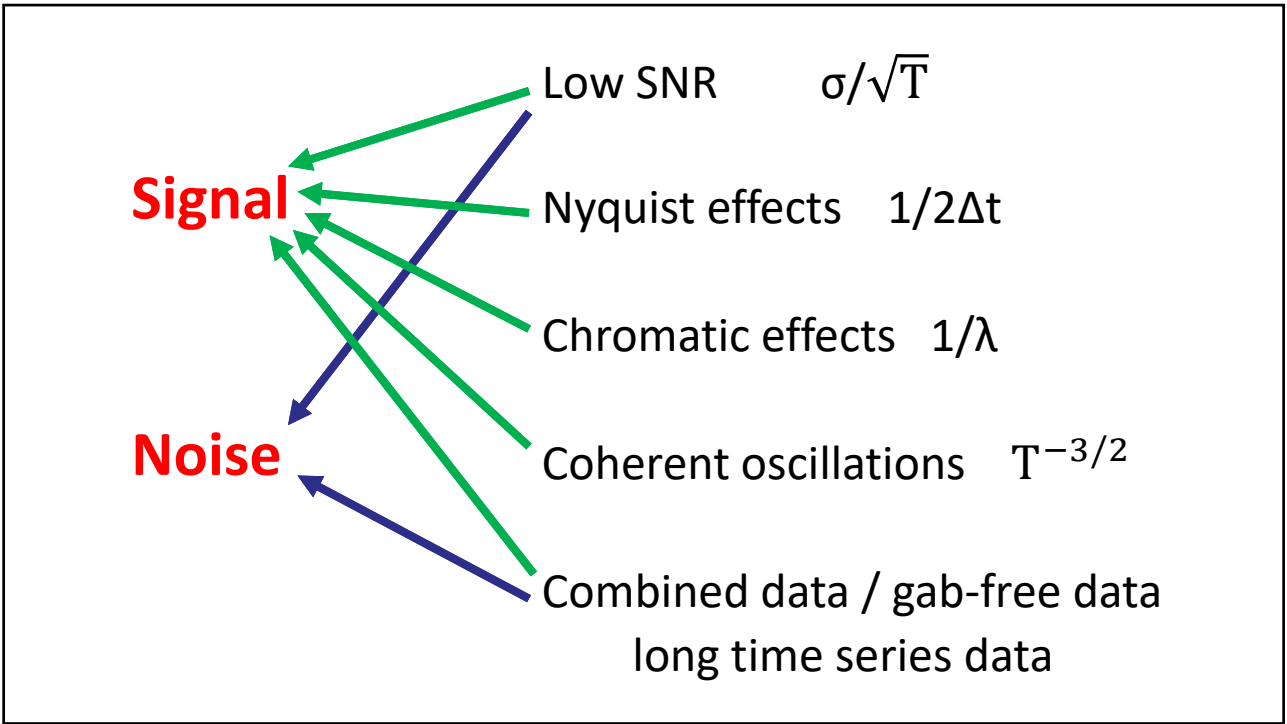
$$F = \frac{T_{eff}^4}{\Delta\nu_0^{4/3} \cdot P^{4/3}}$$

7% Solar and Earth units

Planet Radius

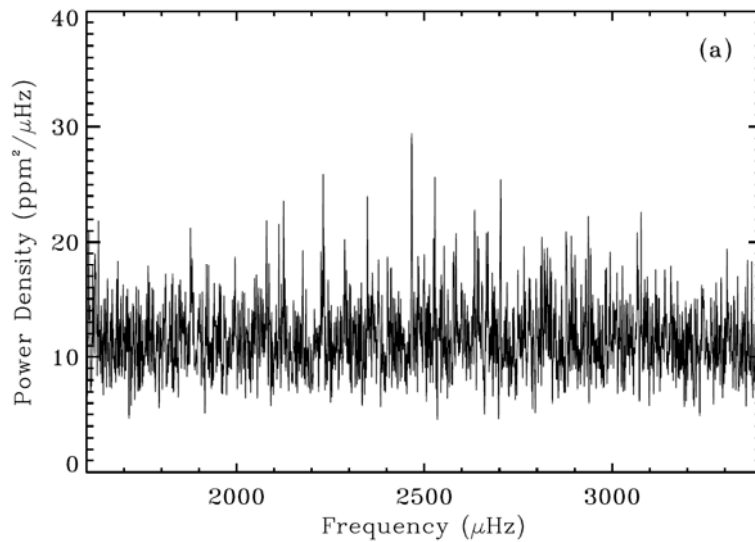
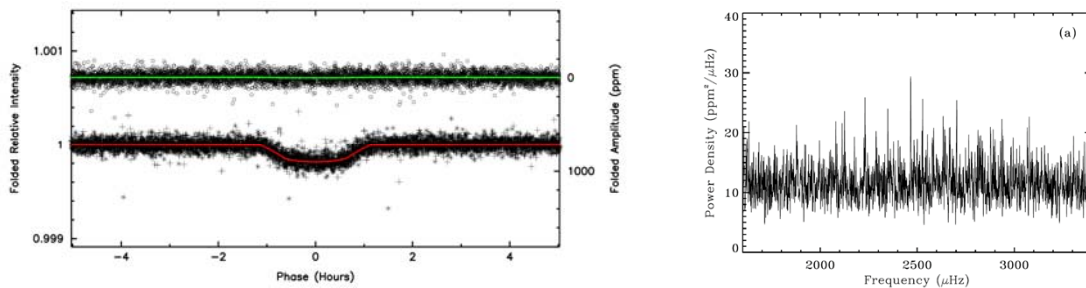
$$r_p = 109 \cdot R \cdot \sqrt{D}$$

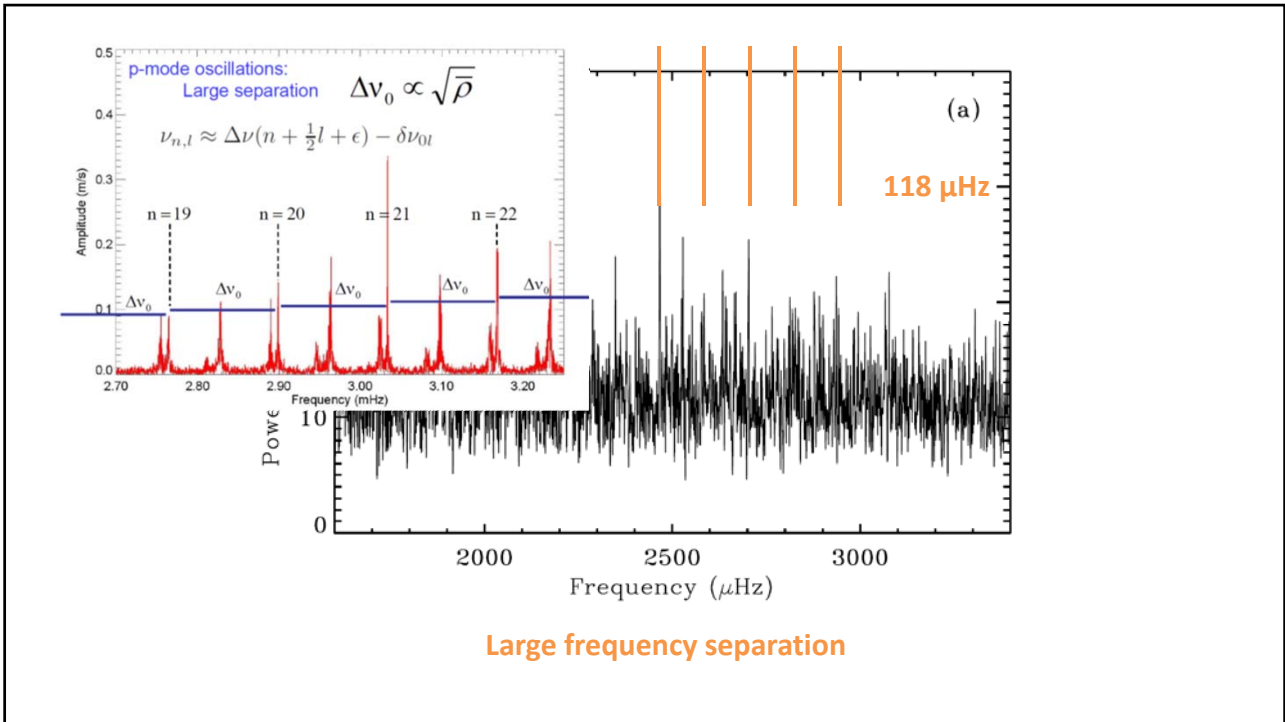
2% Solar and Earth units



KEPLER'S FIRST ROCKY PLANET: KEPLER-10b*

NATALIE M. BATALHA¹, WILLIAM J. BORUCKI², STEPHEN T. BRYSON², LARS A. BUCHHAVE³, DOUGLAS A. CALDWELL⁴,
JØRGEN CHRISTENSEN-DALSGAARD^{5,6}, DAVID CIARDI⁷, EDWARD W. DUNHAM⁸, FRANCOIS FRESSIN³, THOMAS N. GAUTIER III⁹,
RONALD L. GILLILAND¹⁰, MICHAEL R. HAAS², STEVE B. HOWELL¹¹, JON M. JENKINS⁴, HANS KJELSDSEN⁵, DAVID G. KOCH²,
DAVID W. LATHAM³, JACK J. LISSAUER², GEOFFREY W. MARCY¹², JASON F. ROWE², DIMITAR D. SASSELOV³, SARA SEAGER¹³,
JASON H. STEFFEN¹⁴, GUILLERMO TORRES³, GIBOR S. BASRI¹², TIMOTHY M. BROWN¹⁵, DAVID CHARBONNEAU³,
JESSIE CHRISTIANSEN², BRUCE CLARKE⁴, WILLIAM D. COCHRAN¹⁶, ANDREA DUPREE³, DANIEL C. FABRYCKY³, DEBRA FISCHER¹⁷,
ERIC B. FORD¹⁸, JONATHAN FORTNEY¹⁹, FORREST R. GIROUARD²⁰, MATTHEW J. HOLMAN³, JOHN JOHNSON²¹, HOWARD ISAACSON¹²,
TODD C. KLAUS²⁰, PAVEL MACHALEK⁴, ALTHEA V. MOOREHEAD¹⁸, ROBERT C. MOREHEAD¹⁸, DARIN RAGOZZINE³,
PETER TENENBAUM⁴, JOSEPH TWICKEN⁴, SAMUEL QUINN³, JEFFREY VANCLEVE⁴, LUCIANNE M. WALKOWICZ¹²,
WILLIAM F. WELSH²², EDNA DEVORE⁴, AND ALAN GOULD²³

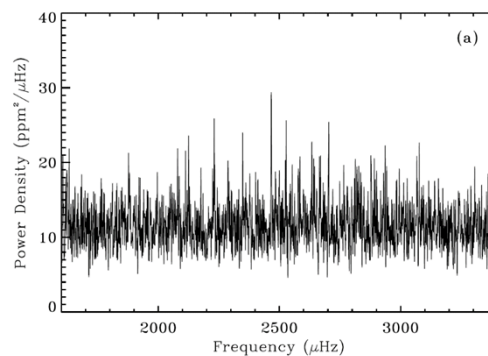




Kepler-10

Mass (M_{sun})	0.995 ± 0.060	(6%)
Radius (R_{sun})	1.056 ± 0.021	(2%)
Age (Gyr)	11.9 ± 4.5	(38%)

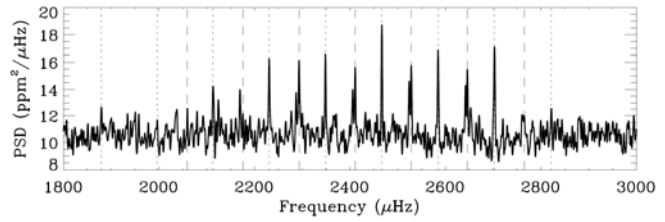
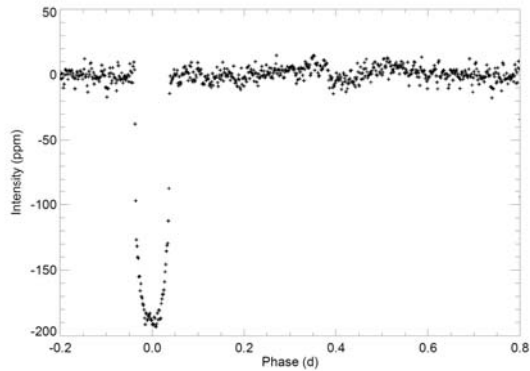
- Batalha et al. 2011



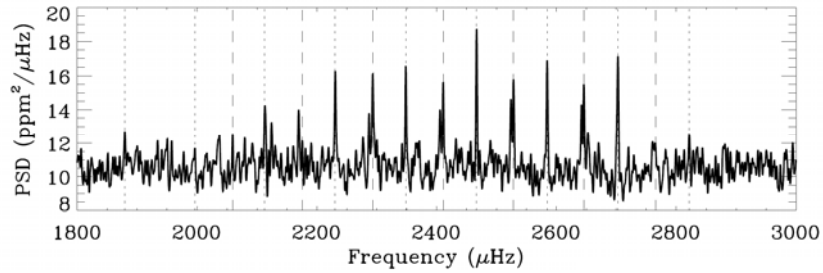
ACCURATE PARAMETERS OF THE OLDEST KNOWN ROCKY-EXOPLANET HOSTING SYSTEM: KEPLER-10 REVISITED

ALEXANDRA FOGTMANN-SCHULZ, BRIAN HINRUP, VINCENT VAN EYLEN, JØRGEN CHRISTENSEN-DALSGAARD,
 HANS KJELDSSEN, VÍCTOR SILVA AGUIRRE, AND BRANDON TINGLEY
 Stellar Astrophysics Centre, Department of Physics and Astronomy, Aarhus University, Ny Munkegade 120,
 DK-8000 Aarhus C, Denmark; alfosc@phys.au.dk

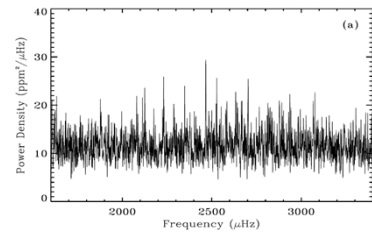
Received 2013 August 28; accepted 2013 December 3; published 2014 January 9



~ 850 days

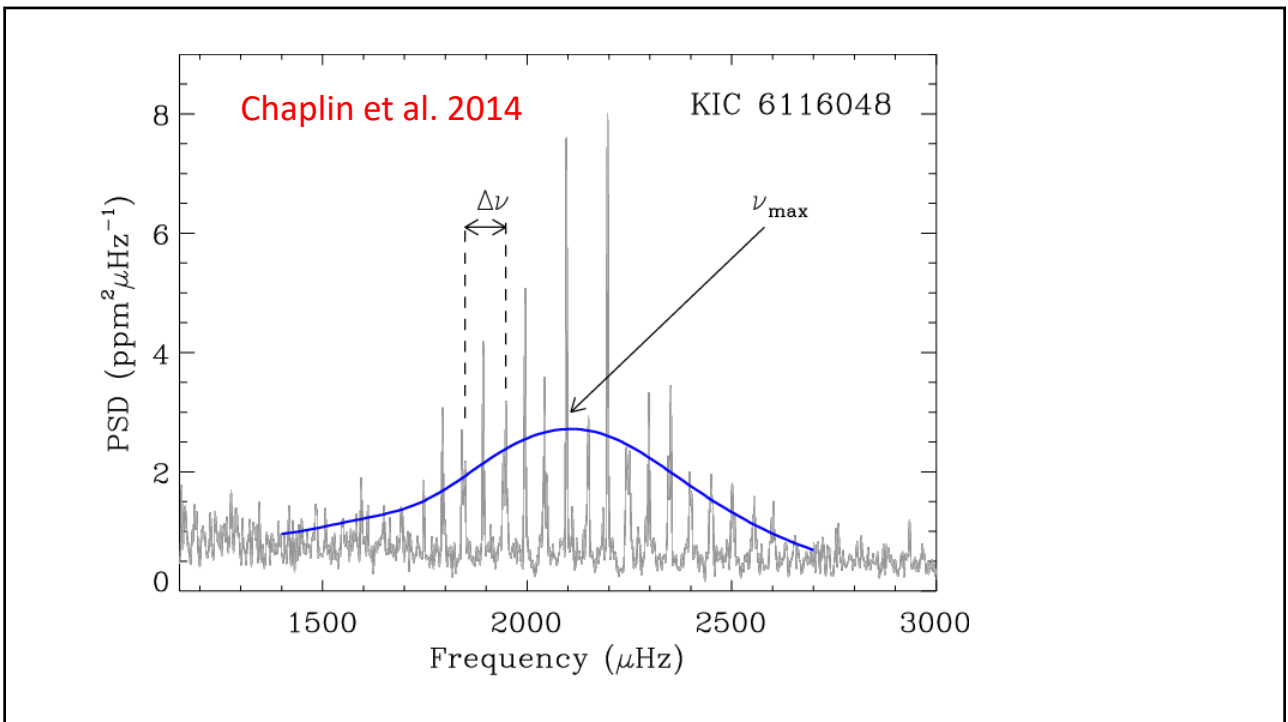
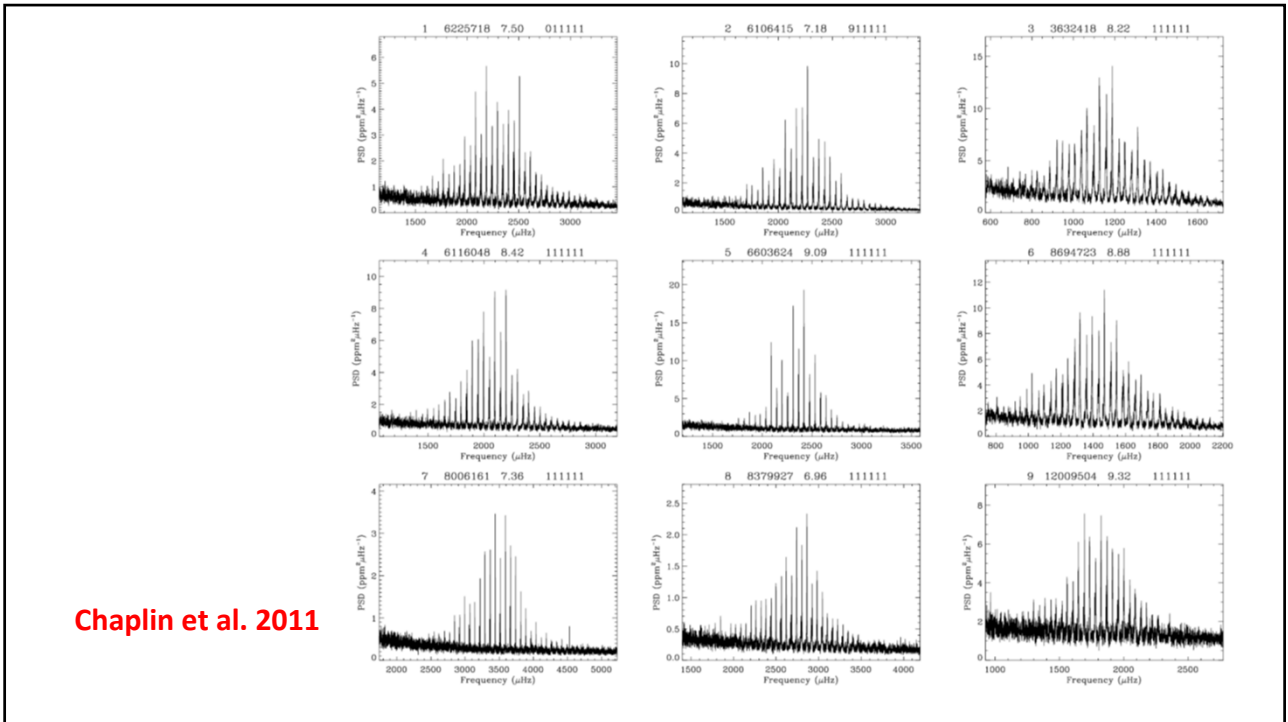


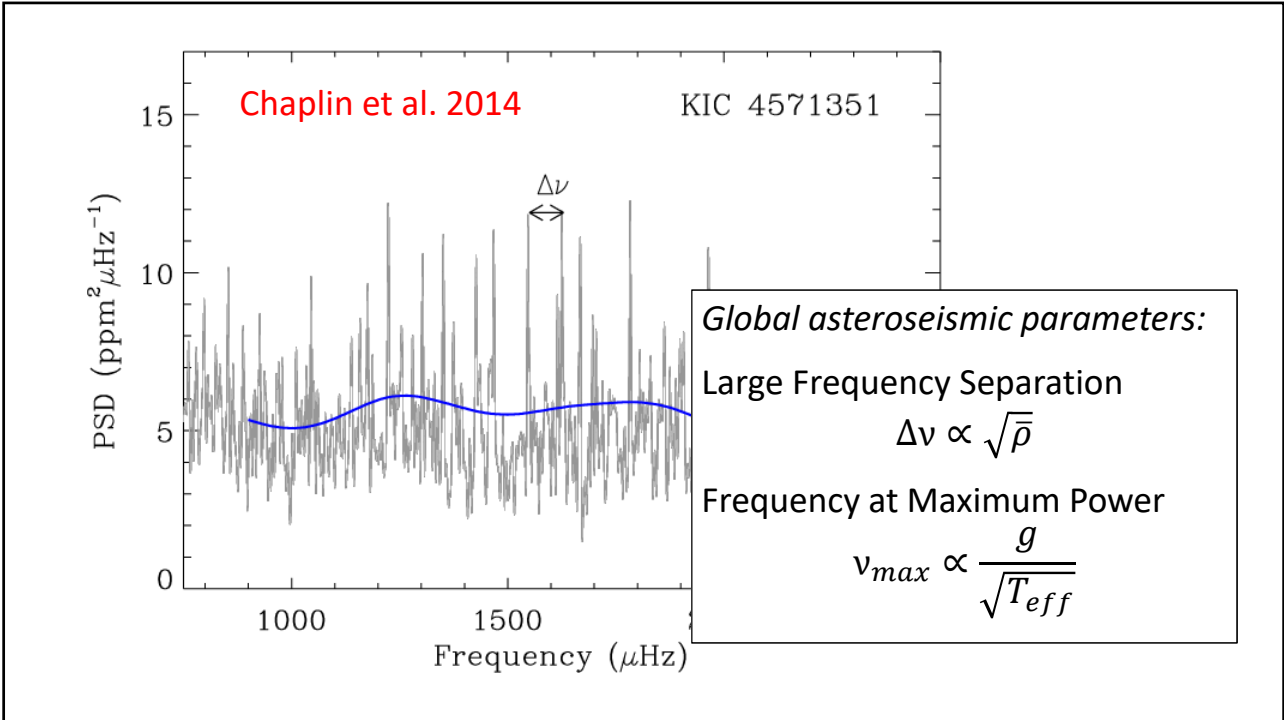
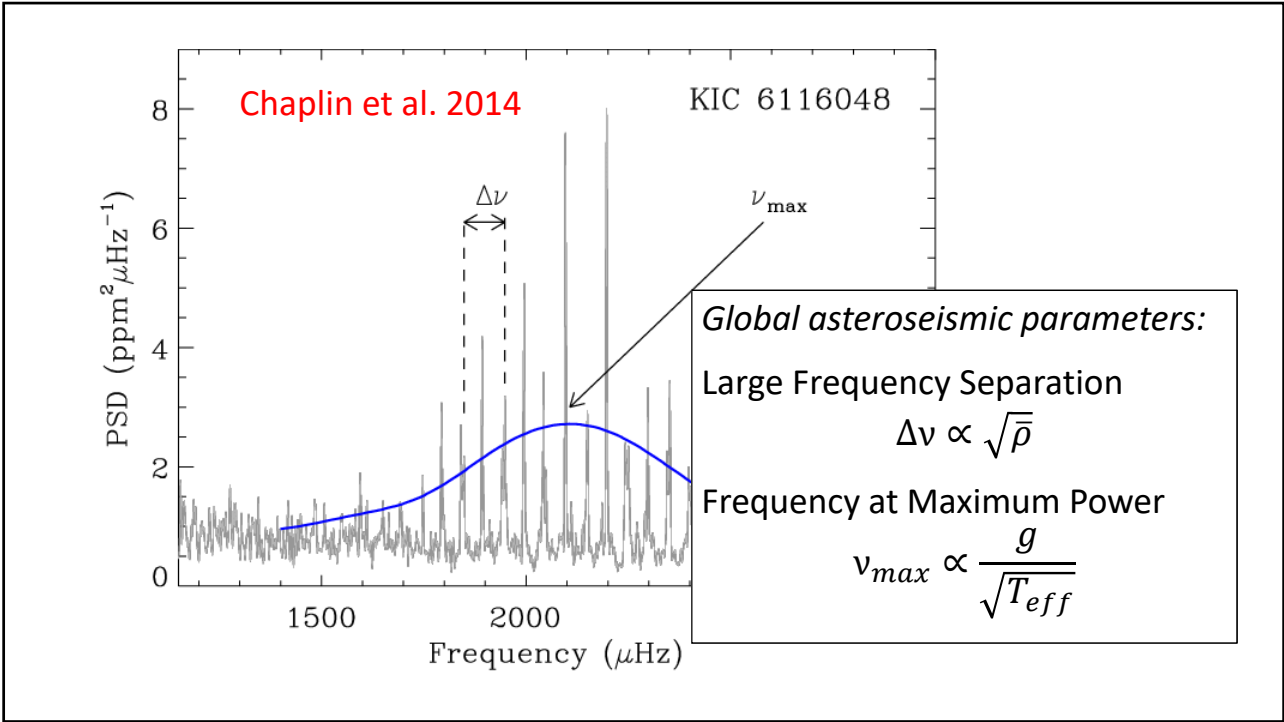
Mass (Msun)	0.913 ± 0.022	(2.4 %)
Radius (Rsun)	1.065 ± 0.009	(0.8 %)
Age (Gyr)	10.4 ± 1.4	(13.5 %)

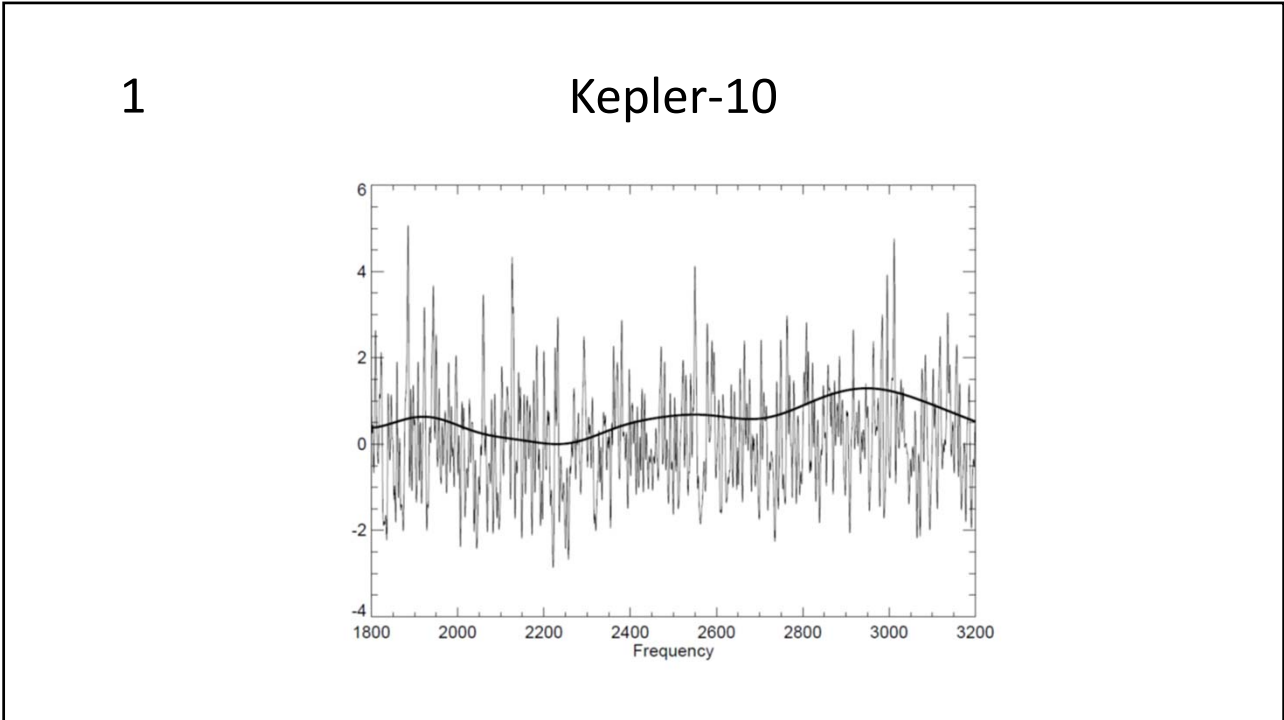
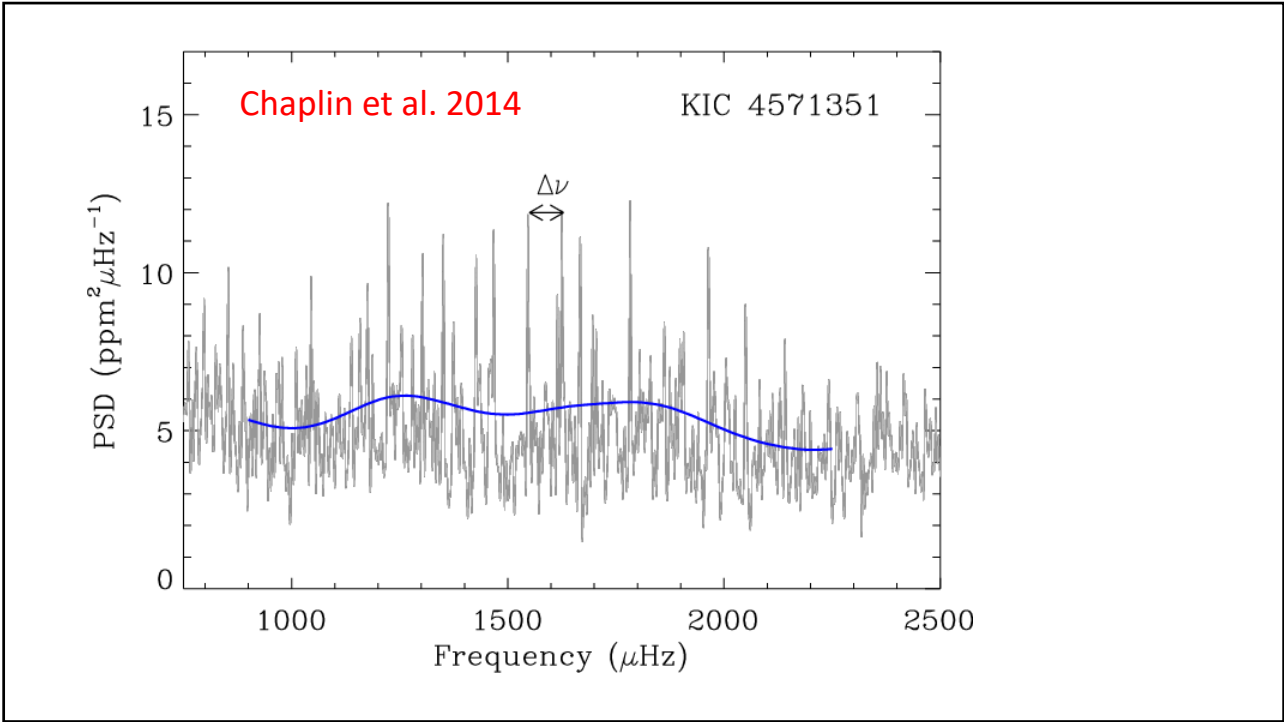


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- Batalha et al. 2011

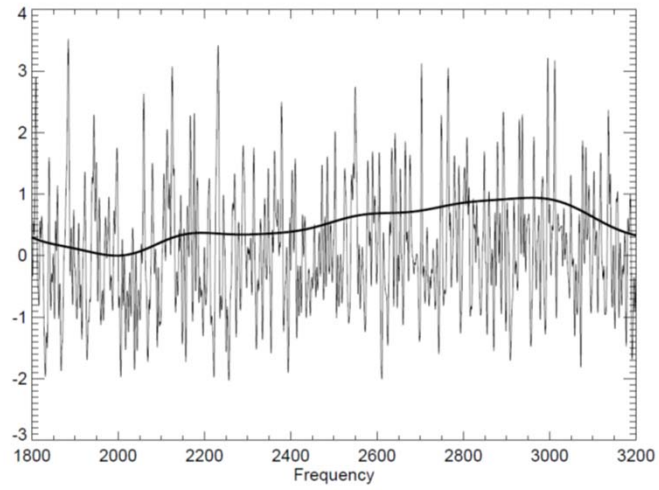






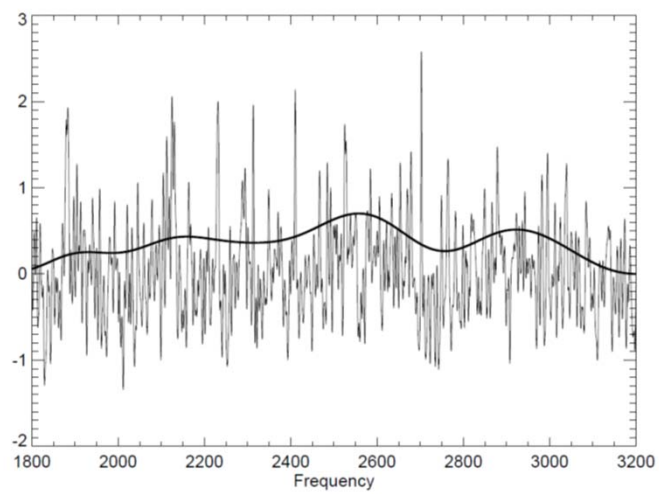
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Kepler-10



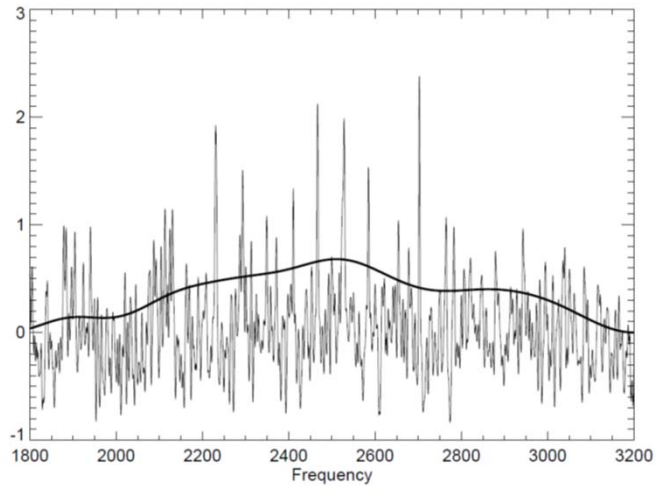
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Kepler-10



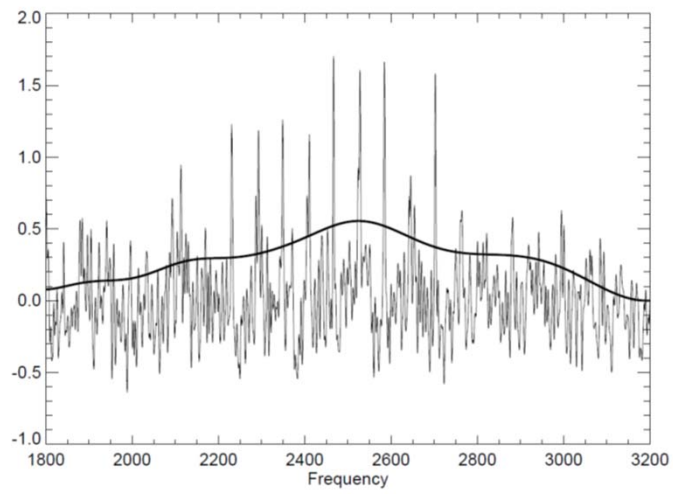
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Kepler-10



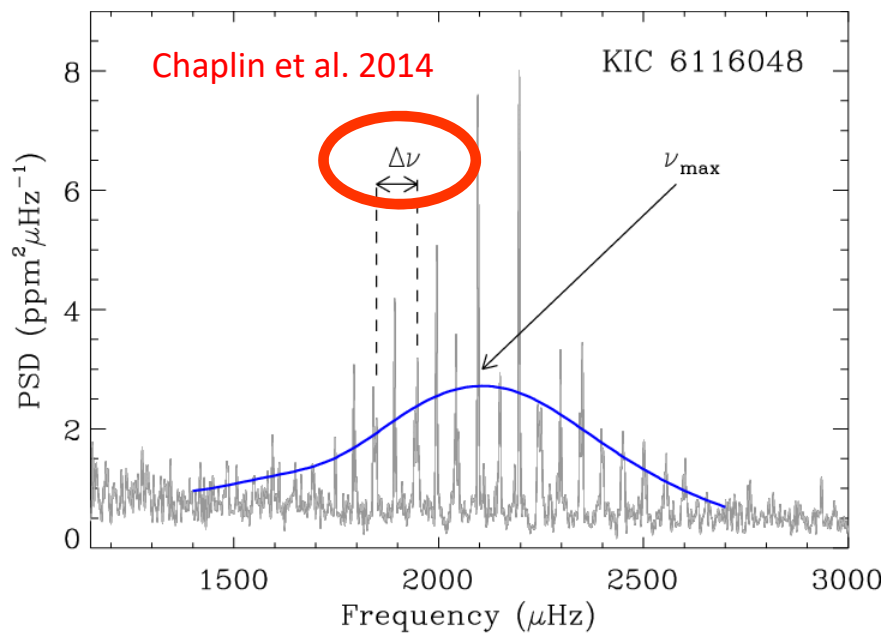
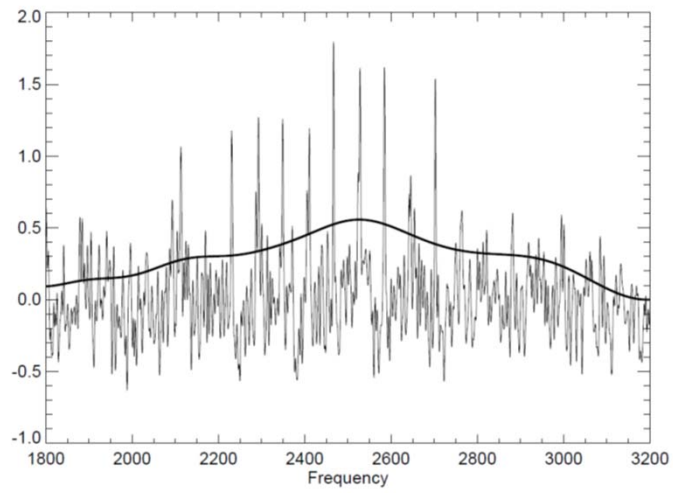
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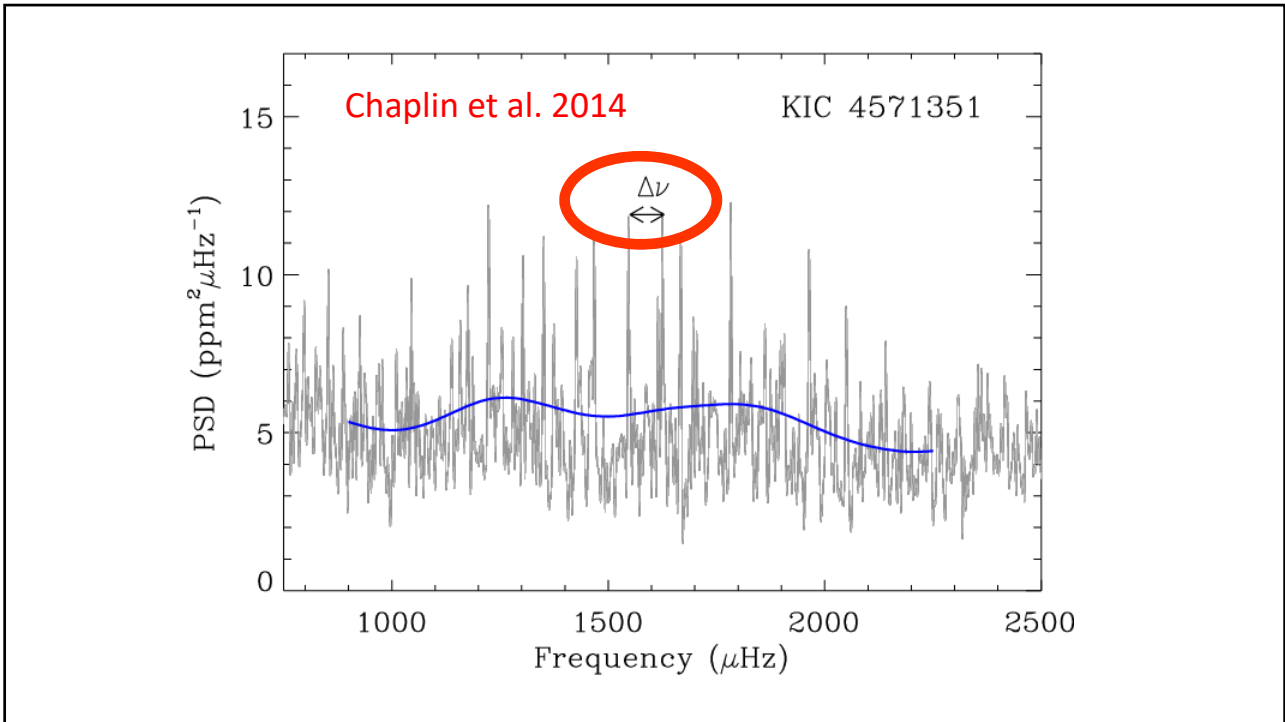
Kepler-10



34

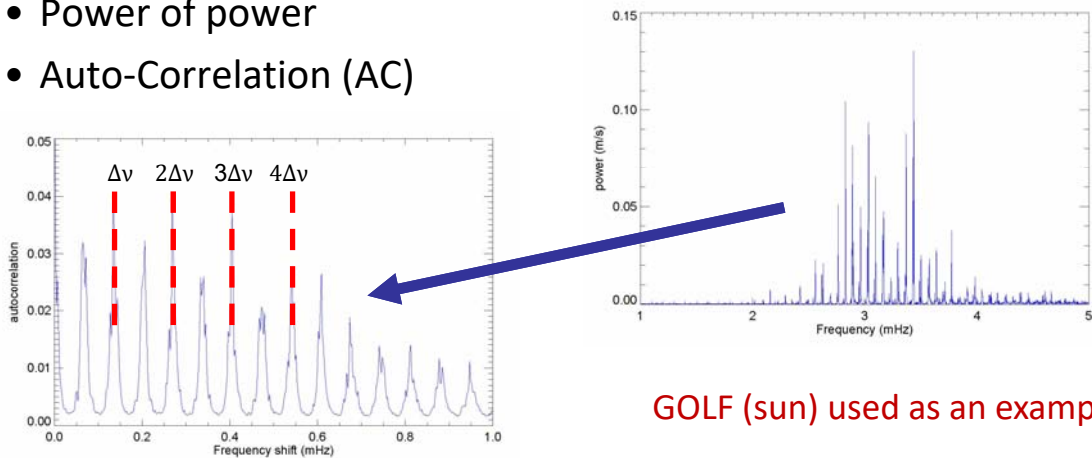
Kepler-10





Measuring the large frequency separation and detecting the p-mode signal

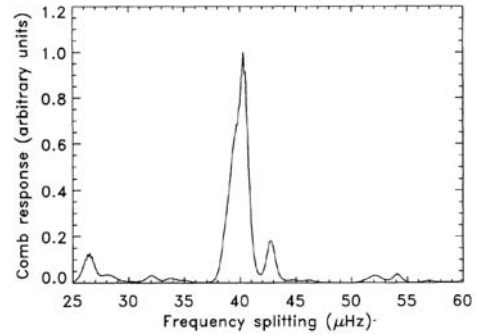
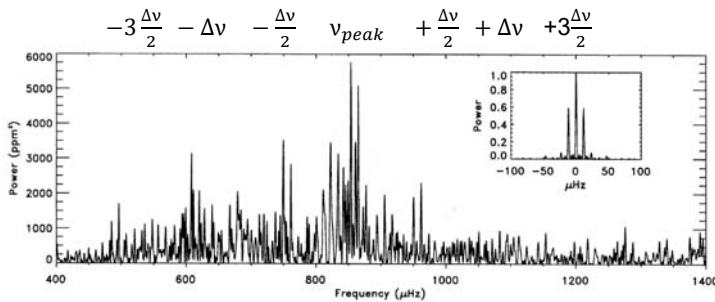
- Power of power
- Auto-Correlation (AC)



GOLF (sun) used as an example

Measuring the large frequency separation and detecting the p-mode signal

- Power of power
- Auto-Correlation (AC)
- Comb Response



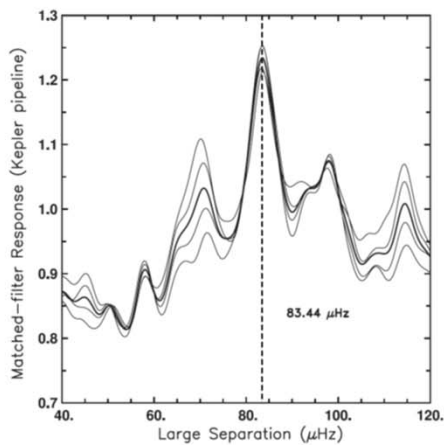
Kjeldsen, Bedding, Viskum, Frandsen, 1995

THE ASTROPHYSICAL JOURNAL, 726:2 (17pp), 2011 January 1
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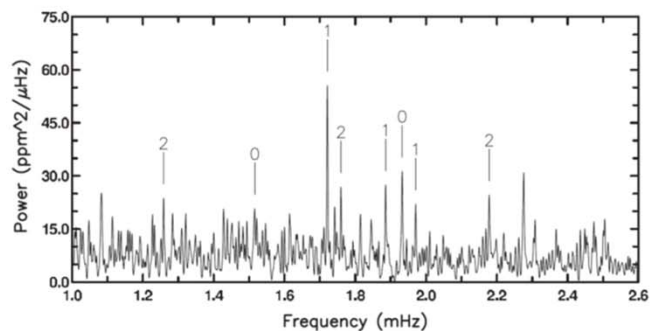
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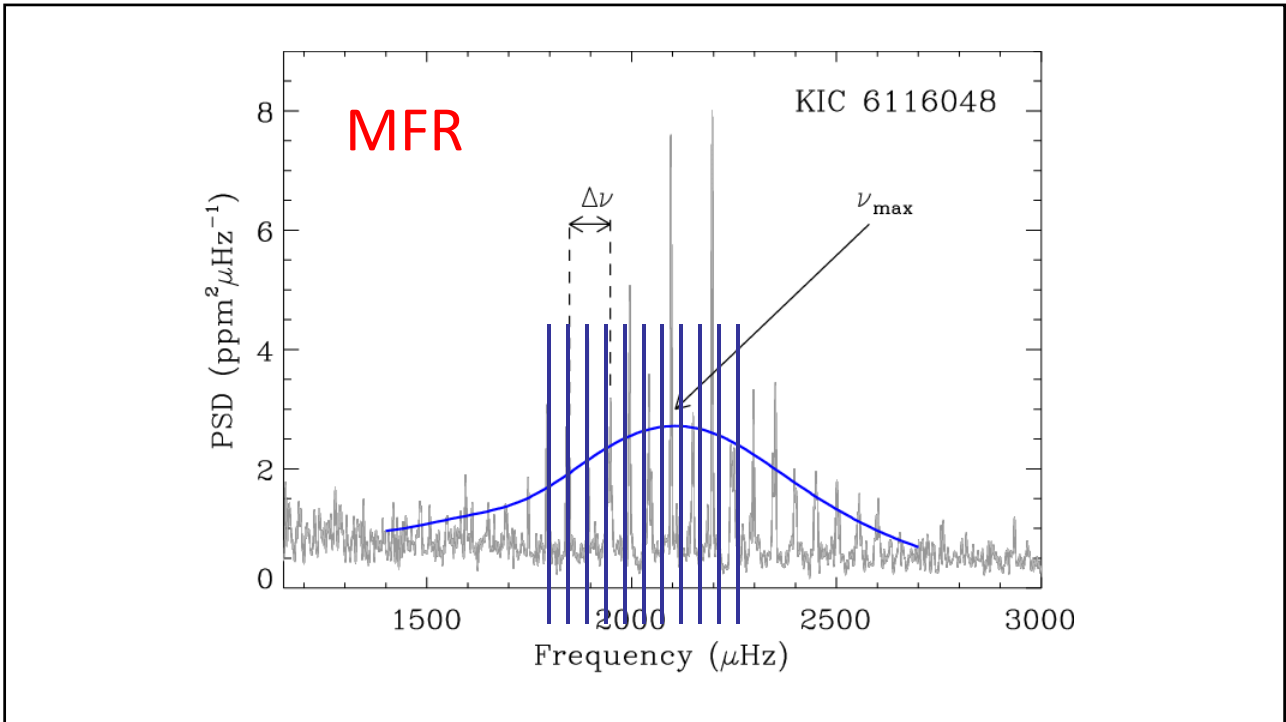
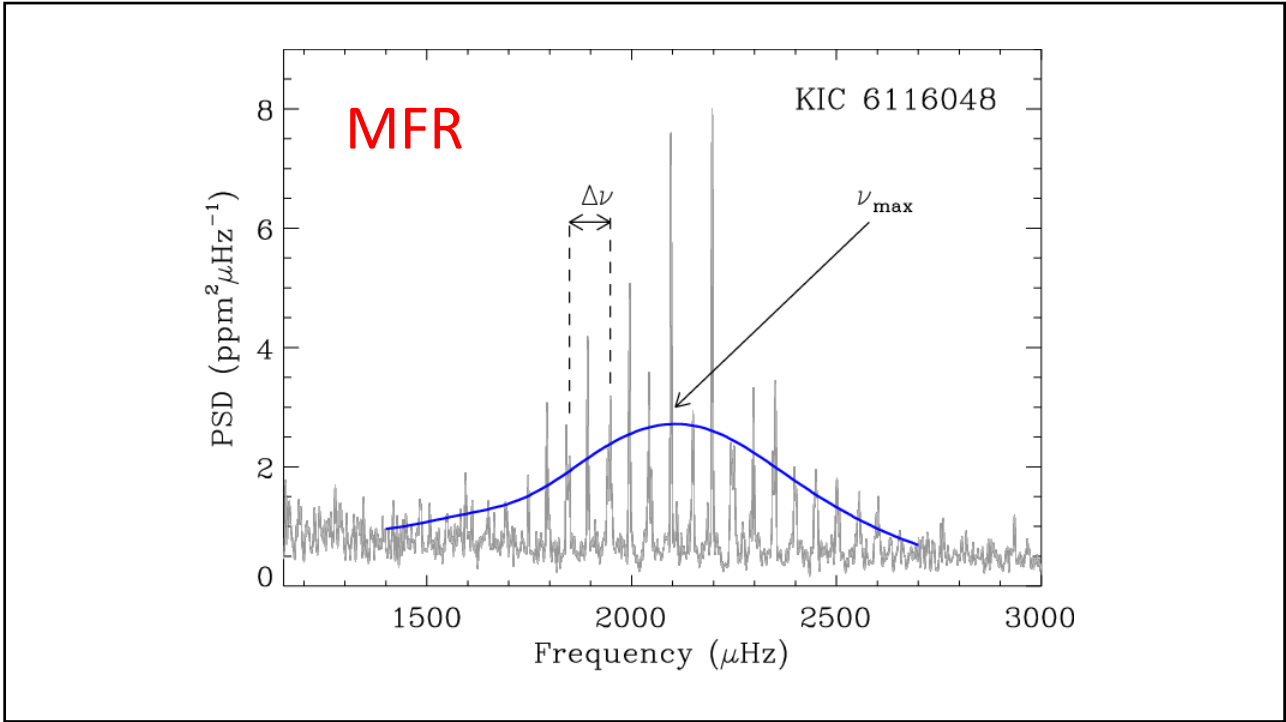
ASTEROSEISMOLOGY OF THE TRANSITING EXOPLANET HOST HD 17156 WITH HUBBLE SPACE TELESCOPE FINE GUIDANCE SENSOR*

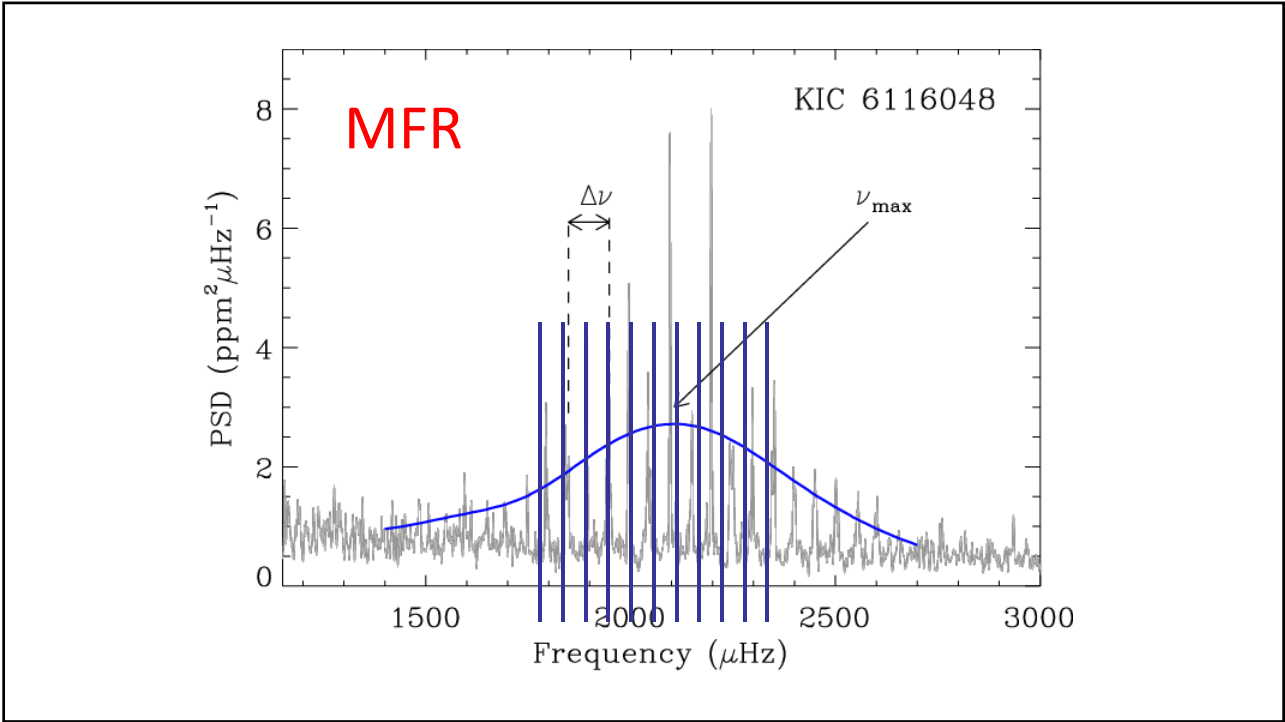
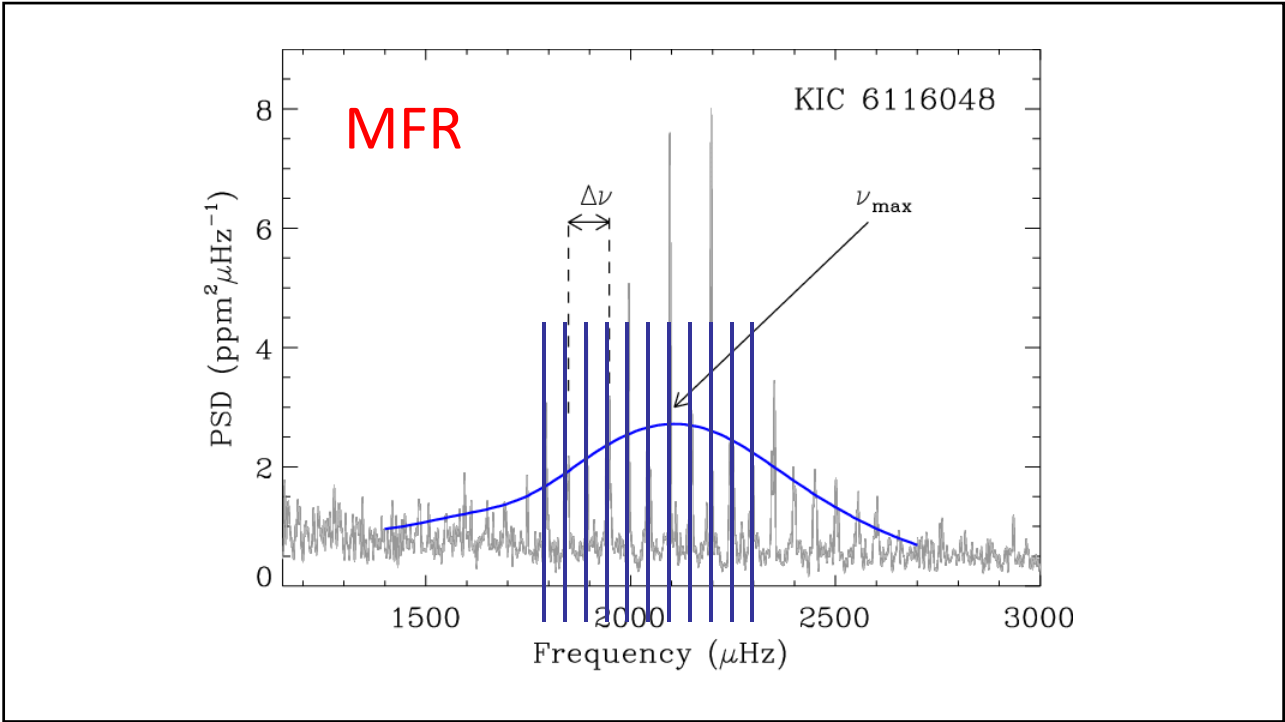
RONALD L. GILLILAND¹, PETER R. MCCULLOUGH¹, EDMUND P. NELAN¹, TIMOTHY M. BROWN², DAVID CHARBONNEAU³, PHILIP NUTZMAN³, JØRGEN CHRISTENSEN-DALSGAARD⁴, AND HANS KJELDEN⁴

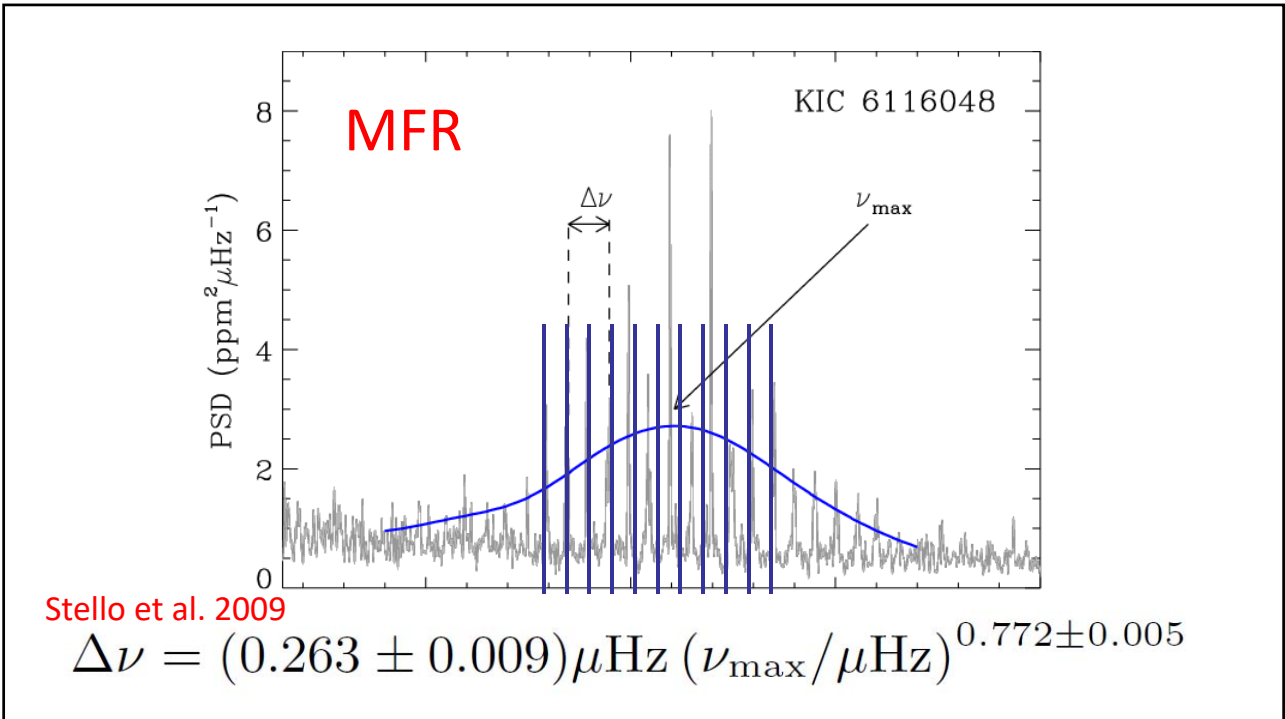
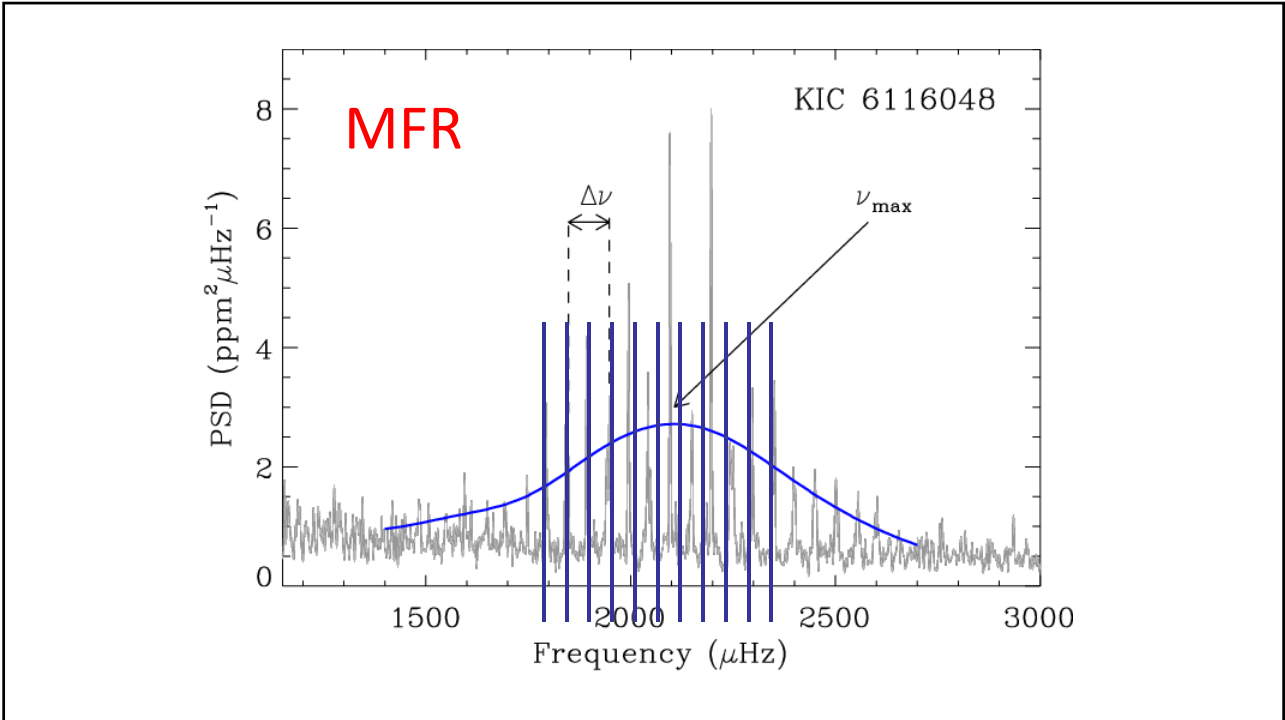


MFR: Matched-filter Response



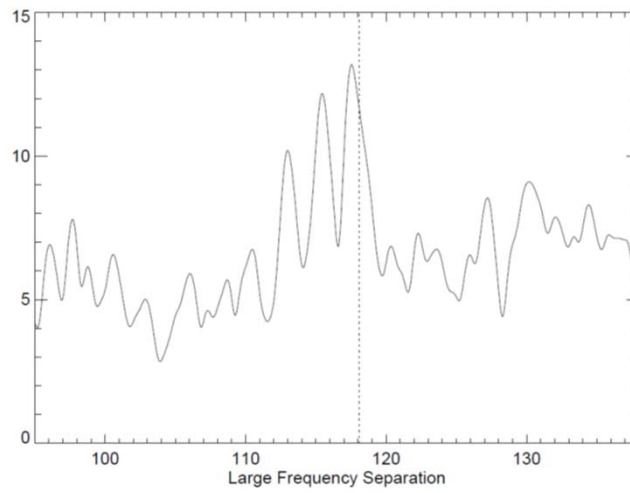






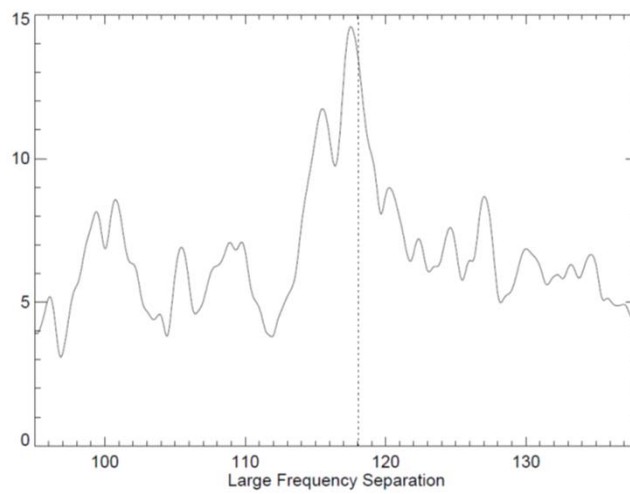
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Kepler-10



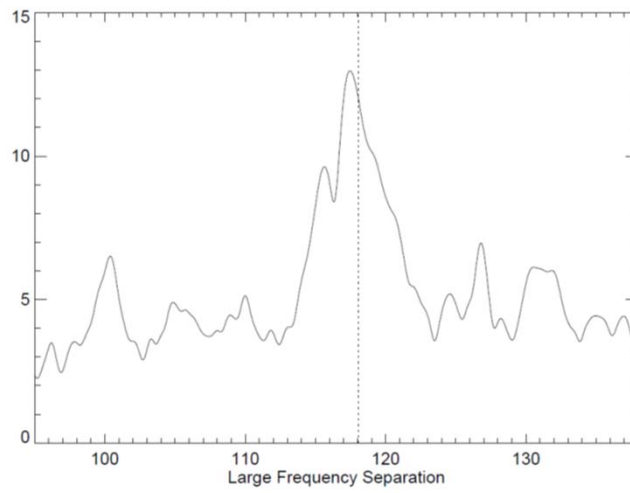
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Kepler-10



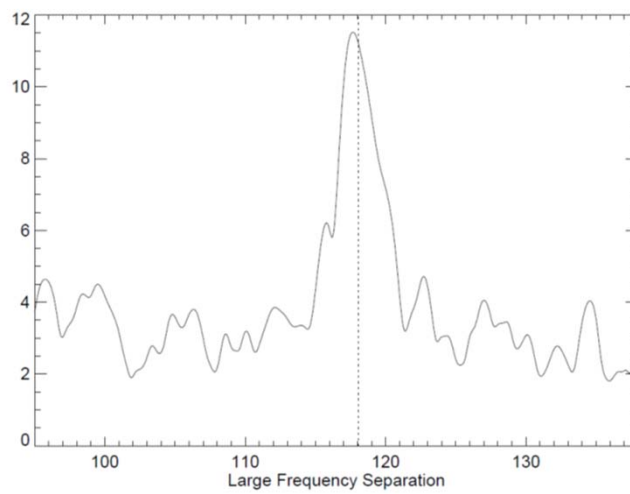
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Kepler-10



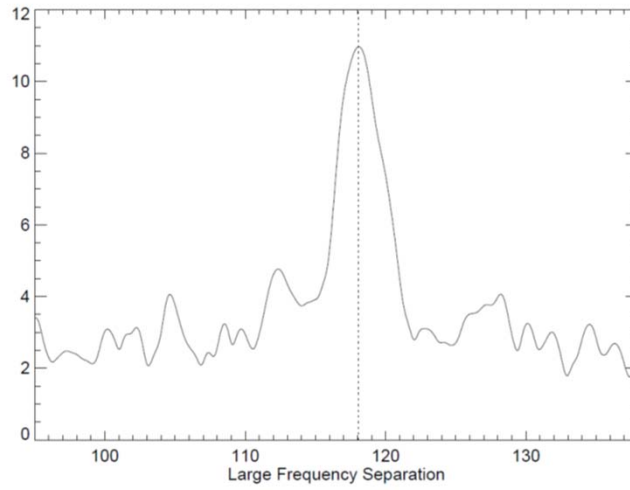
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Kepler-10



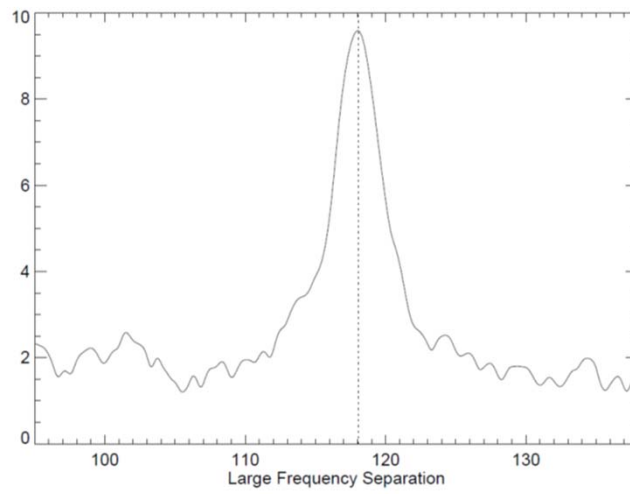
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Kepler-10



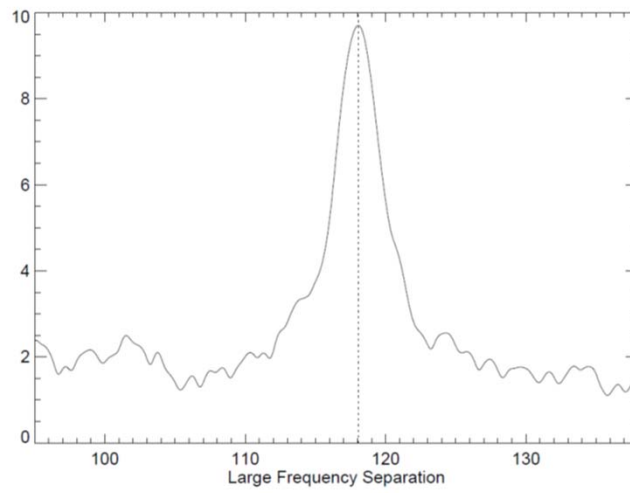
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Kepler-10



34

Kepler-10

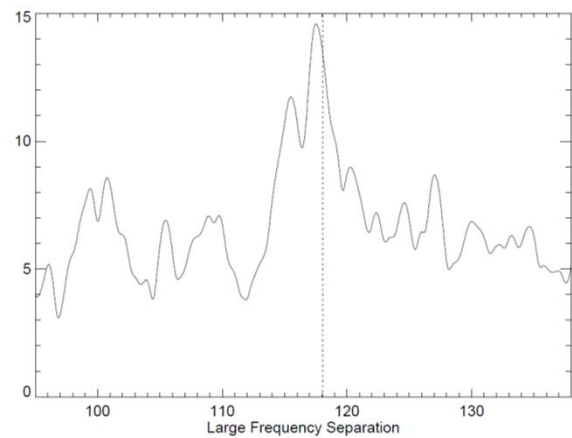
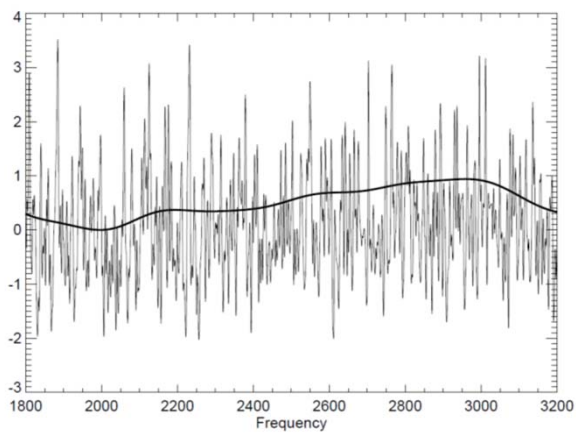


60 d

Kepler-10

V=11.16

TESS=6.0

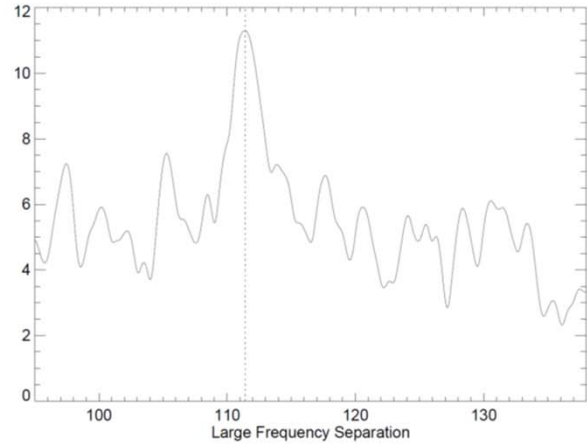
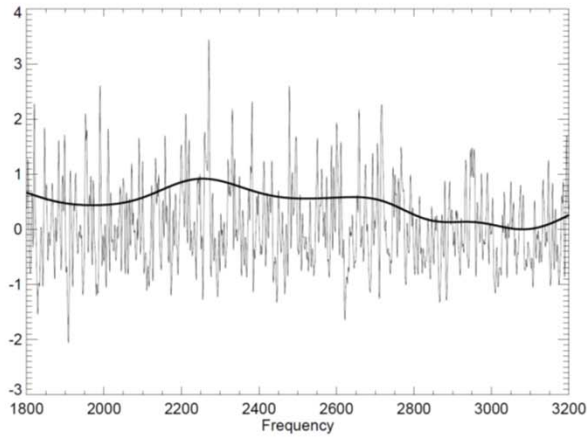


30 d

KIC 7106245

V=10.81

TESS=5.8

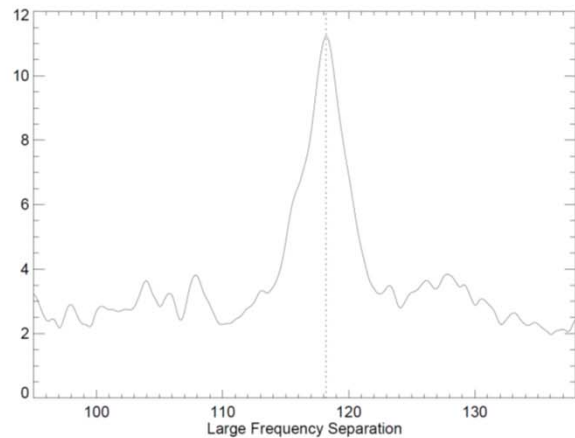
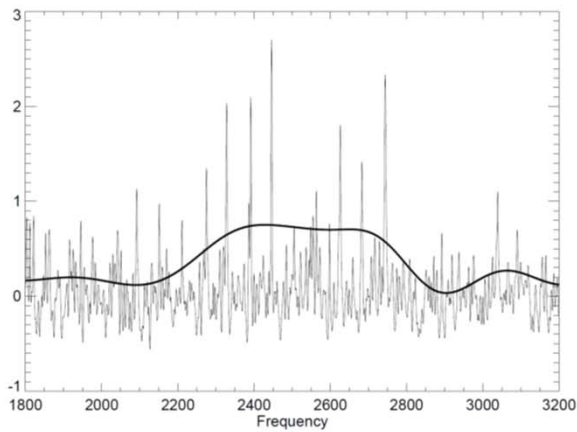


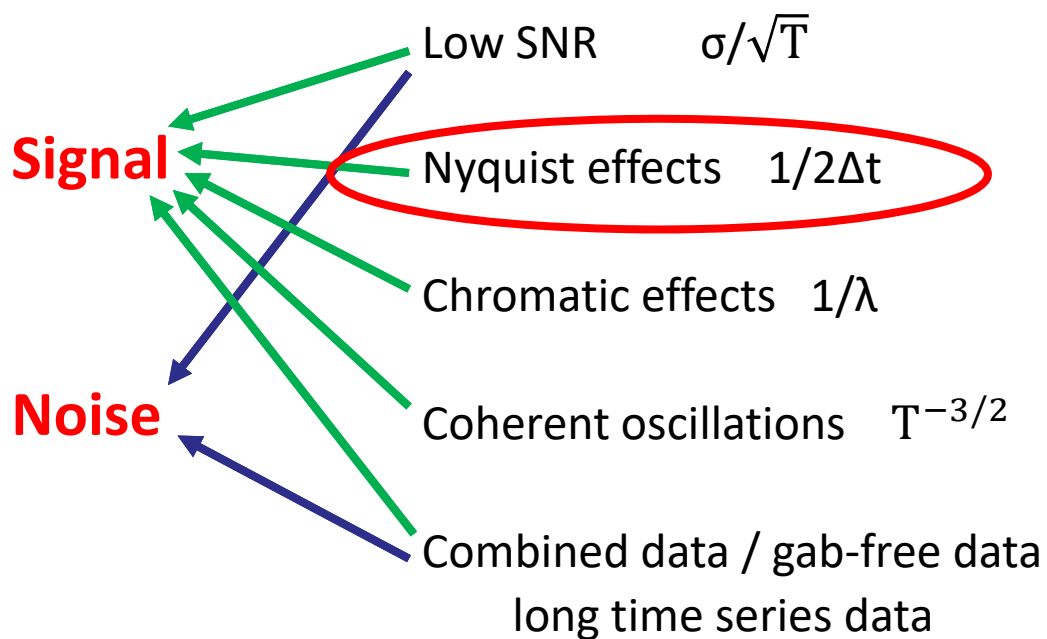
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KIC 8760414

V=9.79

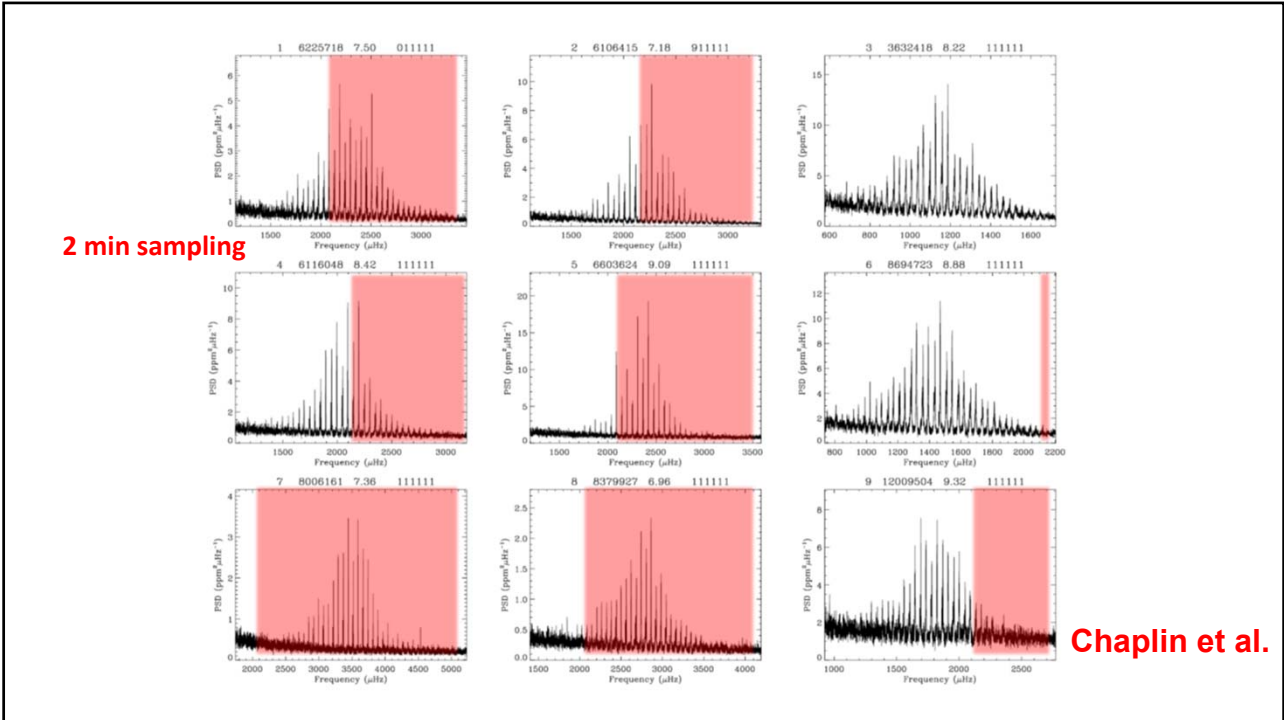
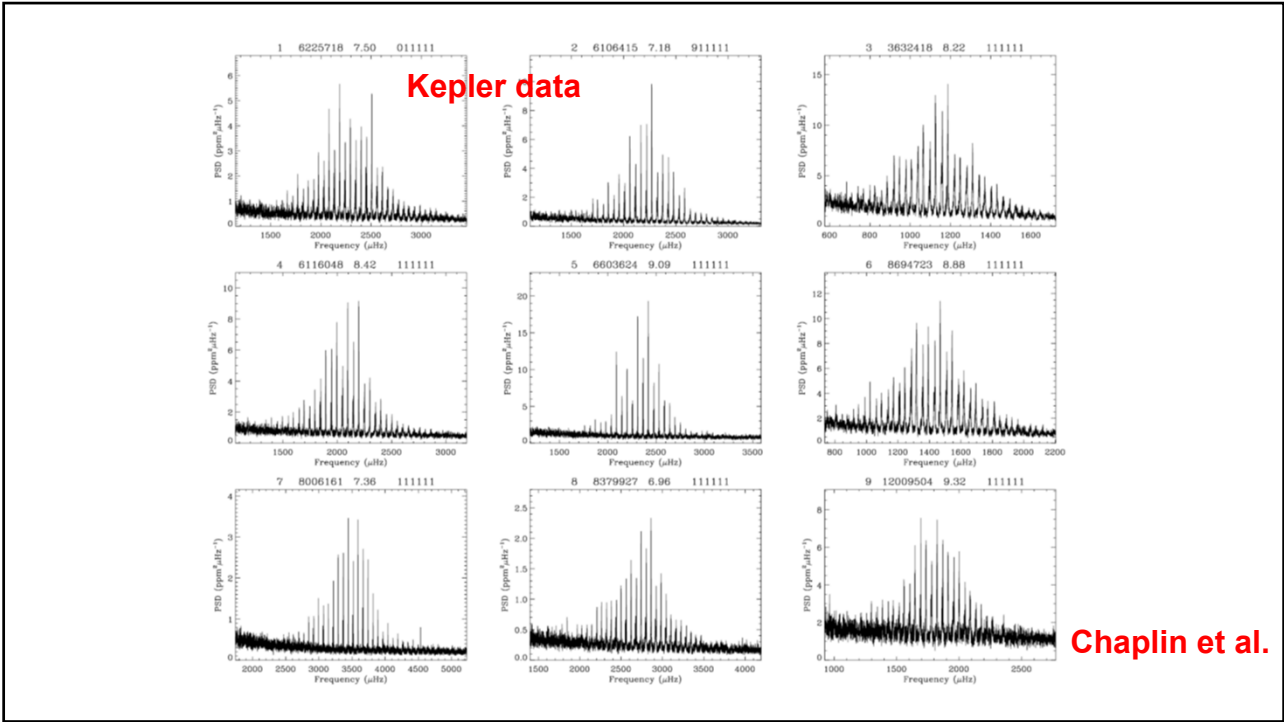
TESS=4.8

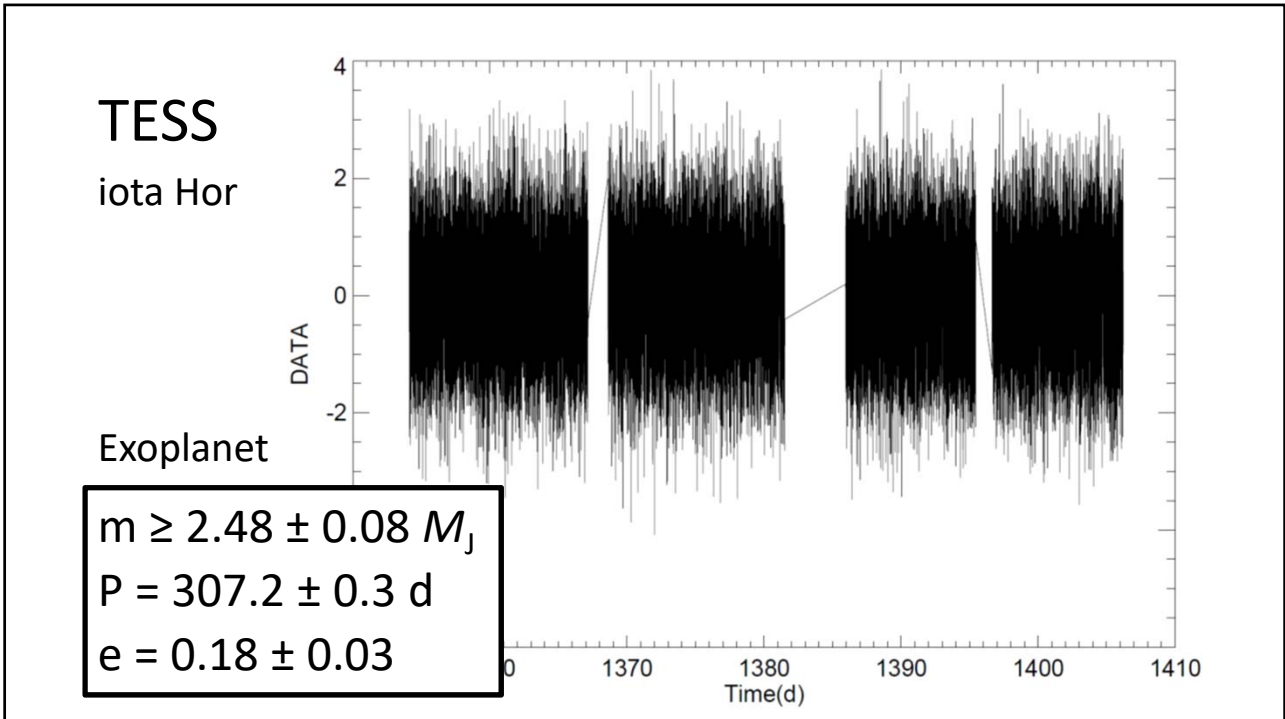
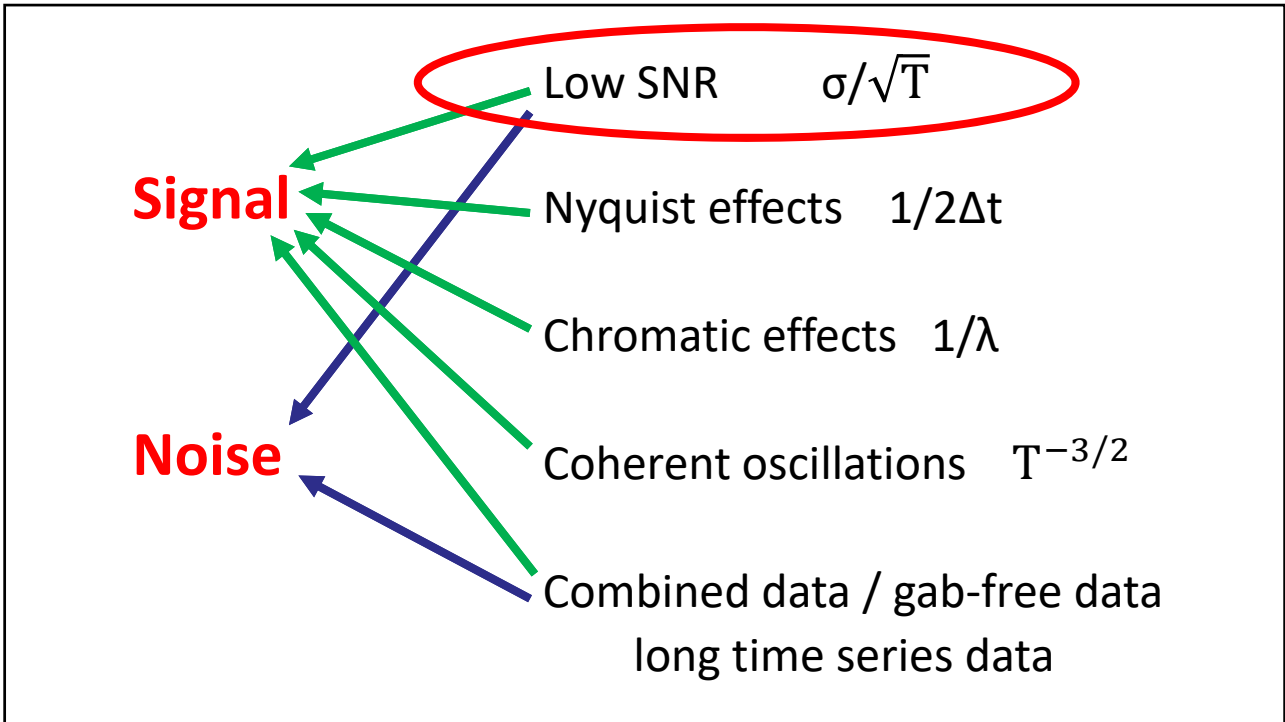




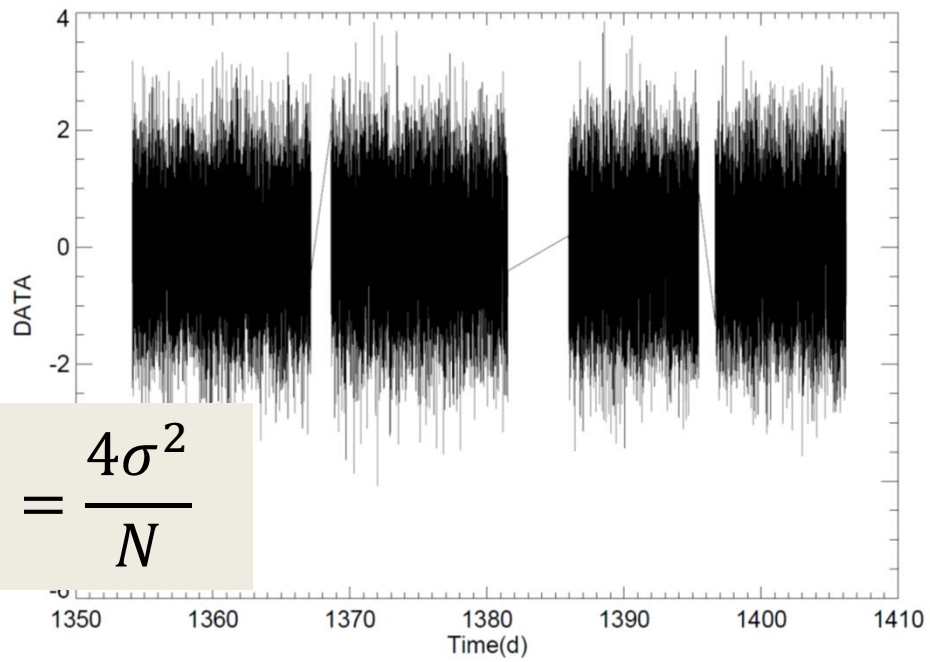
Sampling effects

- Useful frequency domain: $0 \rightarrow \nu_{Nyq} \equiv \frac{1}{2\Delta t}$ where Δt is the sampling time
- Frequency resolution: $\frac{1}{T_{obs}}$
- If data are taken as the integration over Δt one will see a decrease in amplitude of coherent oscillations (which will depend on the phase of the specific oscillation)

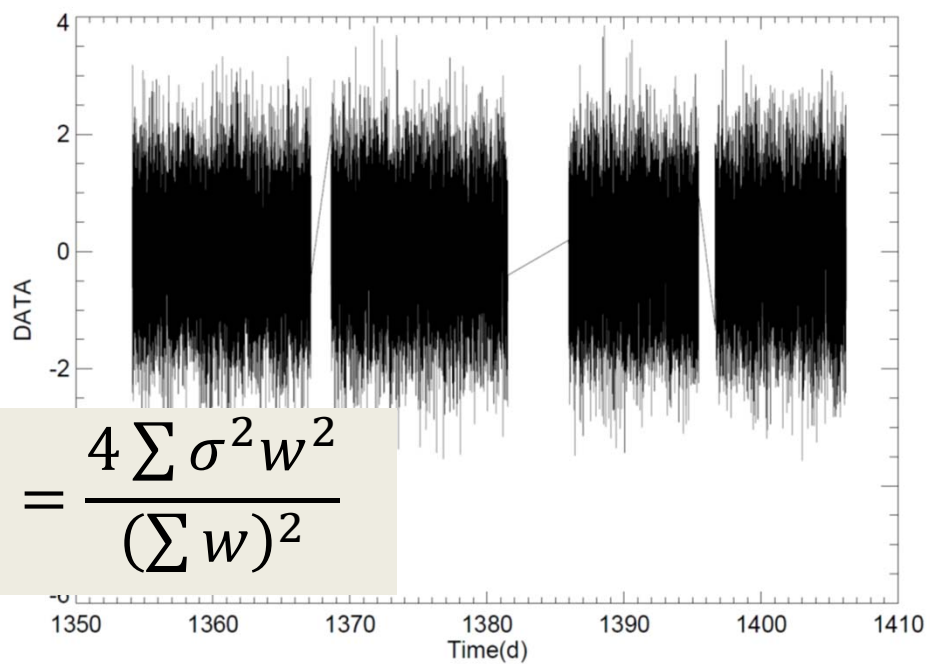




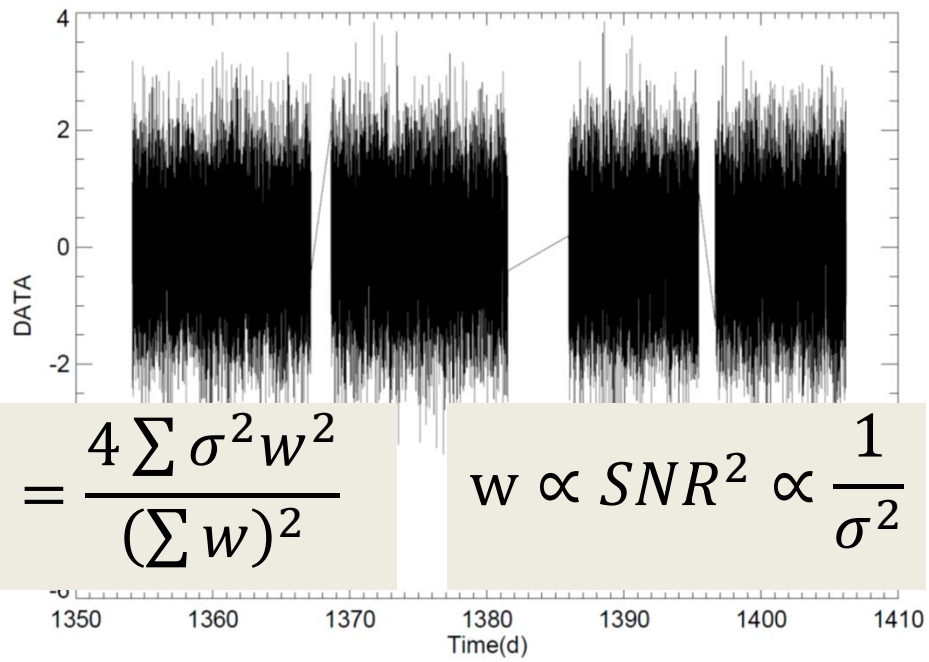
TESS
iota Hor



TESS
iota Hor



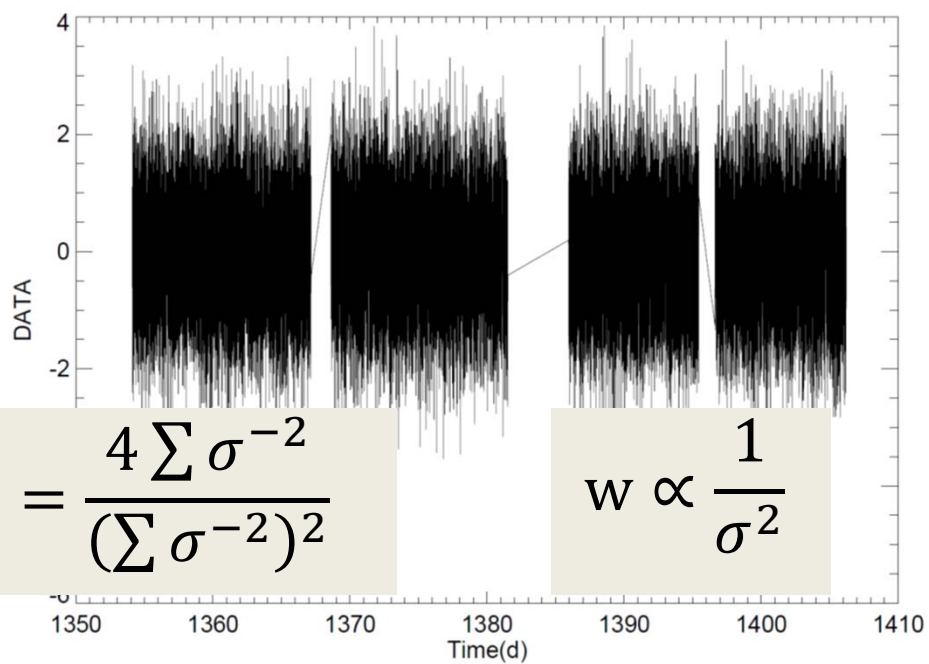
TESS
iota Hor



$$P_{noise} = \frac{4 \sum \sigma^2 w^2}{(\sum w)^2}$$

$$w \propto SNR^2 \propto \frac{1}{\sigma^2}$$

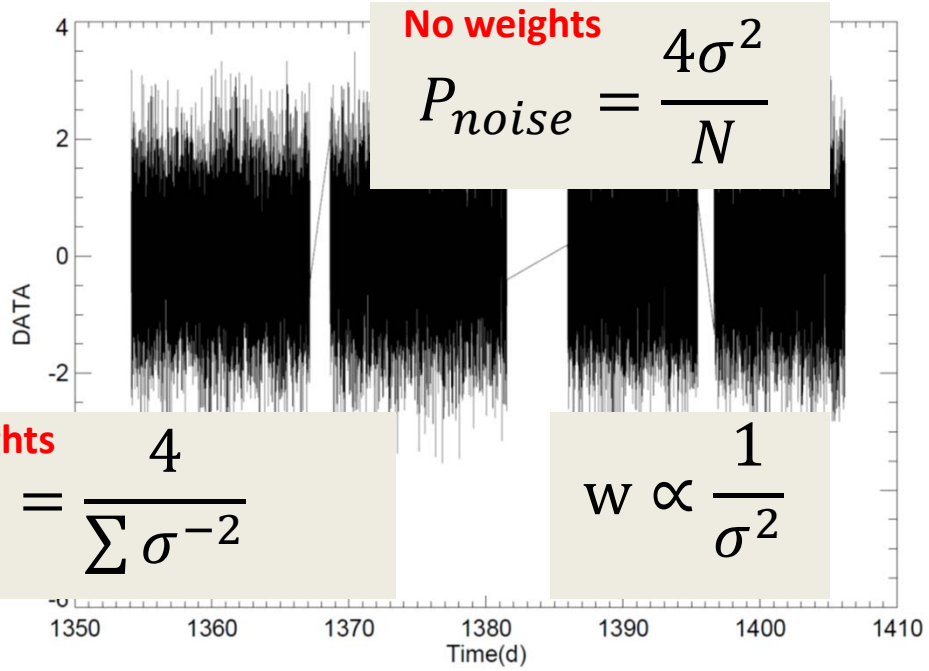
TESS
iota Hor



$$P_{noise} = \frac{4 \sum \sigma^{-2}}{(\sum \sigma^{-2})^2}$$

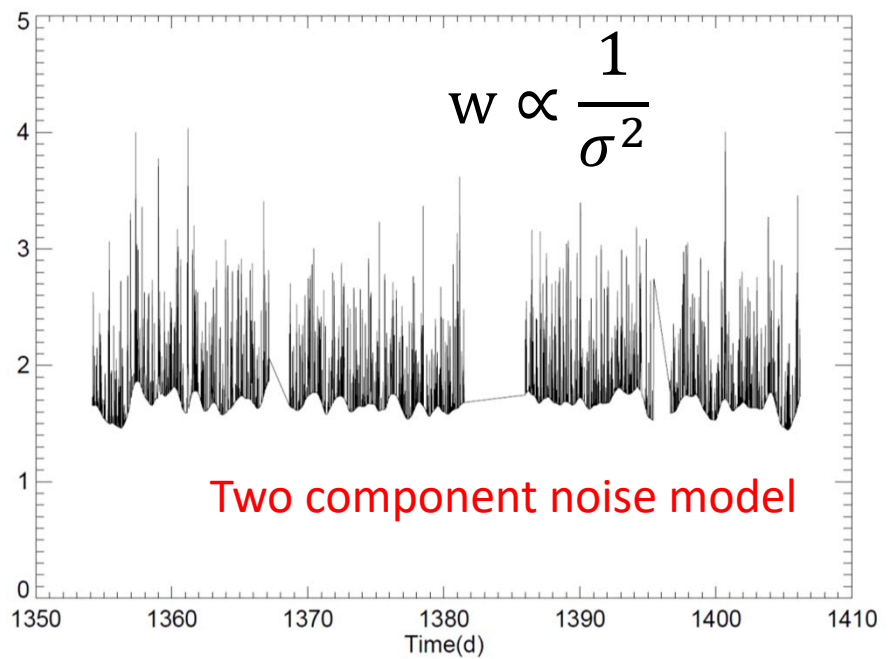
$$w \propto \frac{1}{\sigma^2}$$

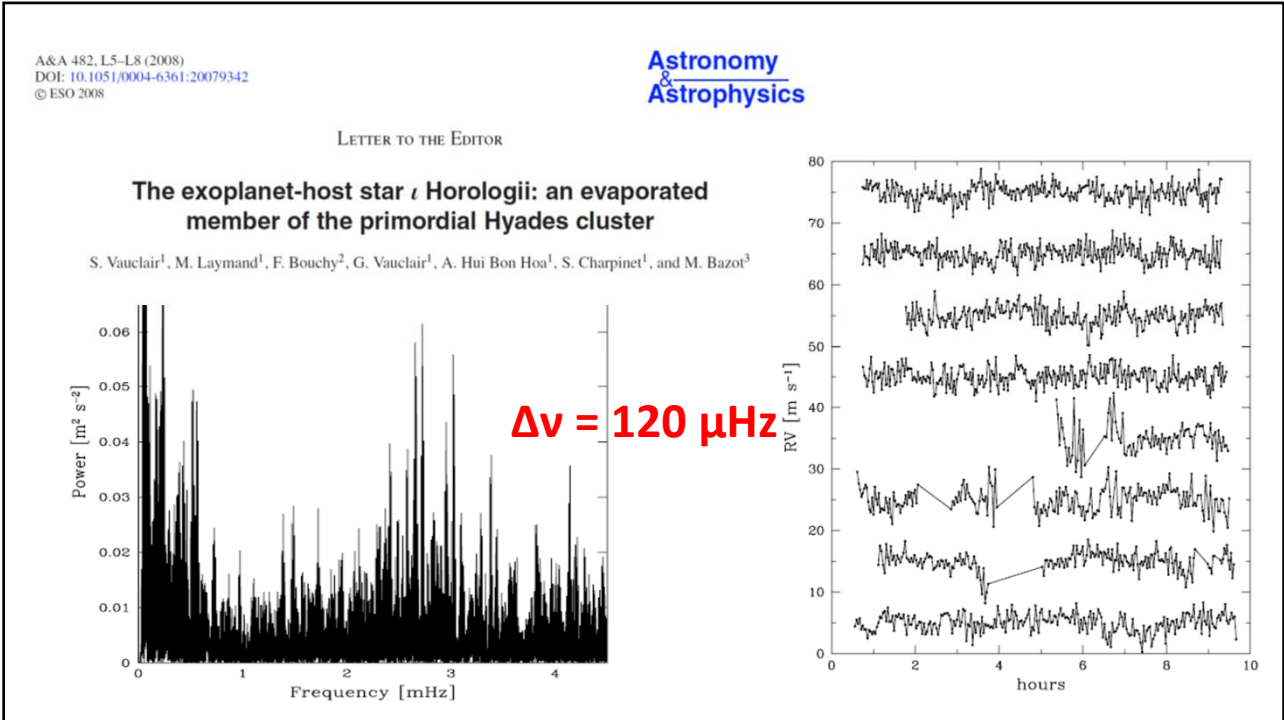
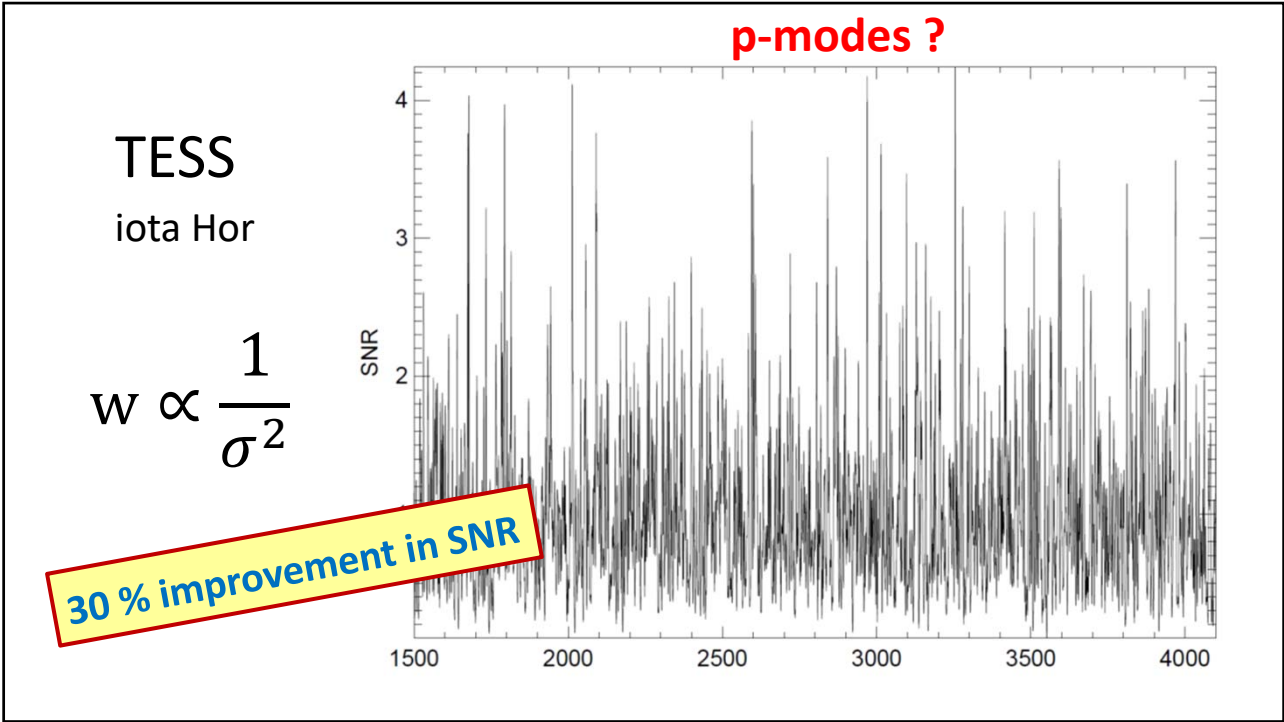
TESS
iota Hor



TESS
iota Hor

Scatter and
Statistical
weights





iota Hor – TESS and HARPS

