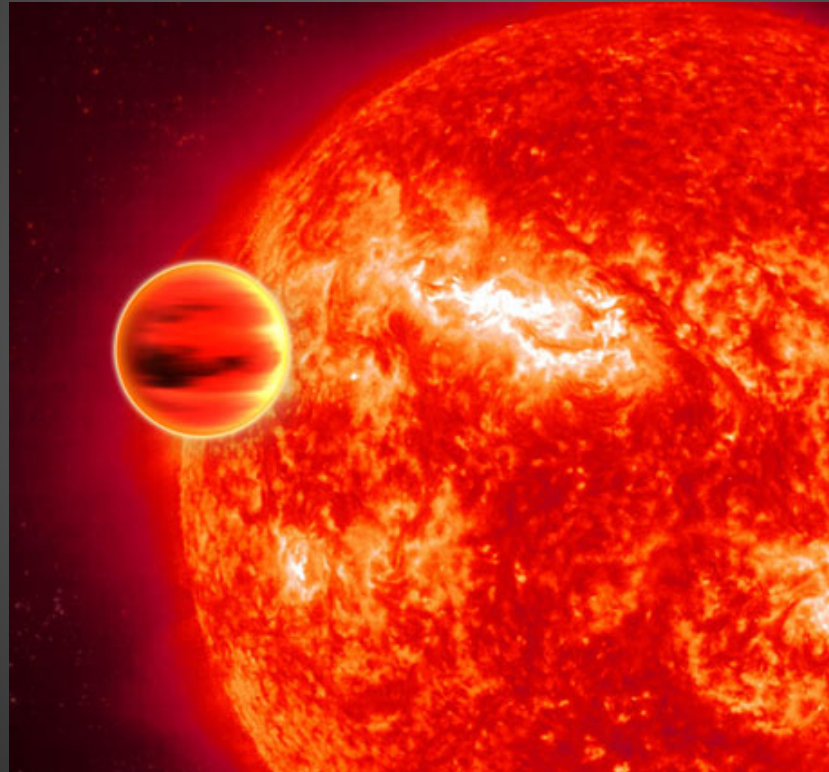


Non-Hydrostatic Dynamical Models of Giant Planet Atmospheres

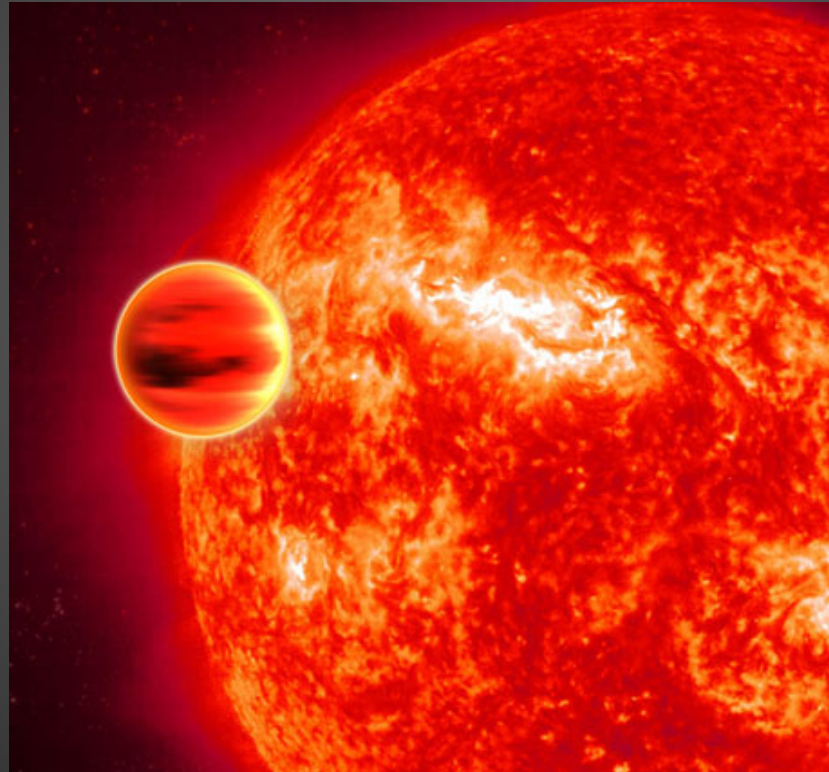


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Outline

- Dynamical/Radiative Modeling Methodologies
- General Properties/Thermal Inversions (x2)
- Variations of Viscosity
- Changing Jets
- Shocks/ Potential Vorticity Generation
- Weather
- Observable Consequences
- Eccentric Planets

Dynamical Modeling Methodologies



Dynamical Methods

Completeness

- Equivalent Barotropic and Shallow Water (2D)
 - Cho et al (2003,2008) Langton and Laughlin (2007,2008) Rauscher et al (2007, 2008)
- Navier-Stokes equation (2D)
 - Burkert et al. 2007
- Primitive equations (~3D)
 - Showman et al. (2002, 2005, 2006, 2008, 2009), Menou and Rauscher (2009)
- Eulers equations (3D)
 - Dobbs-Dixon and Lin (2008)
- Navier-Stokes equations (3D)
 - Dobbs-Dixon et al (2010)

Resolution

Radiation Transfer Methods

- Relaxation methods (Newtonian heating)
 - Cho et al (2003,2008) Langton and Laughlin (2007,2008) Rauscher et al (2007, 2008), Showman et al. (2002, 2005, 2006, 2008), Menou and Rauscher (2009)
- 2/3D one temperature flux-limited radiative diffusion
 - Burkert et al. (2007), Dobbs-Dixon and Lin (2008)
- 3D FLD + decoupled thermal and radiative components
 - Dobbs-Dixon et al (2009)
- 1D (radial) wavelength-dependent radiative transfer
 - Showman et al. (2009)

$$\rho \frac{\partial u}{\partial t} + u \frac{\partial \rho}{\partial t} = - \frac{1}{r \cos \phi} \frac{\partial p}{\partial \lambda} + \rho \left(2\Omega + \frac{u}{r \cos \phi} \right) (\sin \phi) v - \rho \left(2\Omega \cos \phi + \frac{u}{r} \right) w$$

East-West

$$- \left[\frac{1}{r \cos \phi} \frac{\partial}{\partial \lambda} (\rho u^2) + \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (\rho u w \cos \phi) + \frac{1}{r^2} \frac{\partial}{\partial r} (\rho u w r^2) \right] + \rho F_\lambda,$$

$$\rho \frac{\partial v}{\partial t} + v \frac{\partial \rho}{\partial t} = - \frac{1}{r} \frac{\partial p}{\partial \phi} - \rho \left(2\Omega + \frac{u}{r \cos \phi} \right) (\sin \phi) u - \rho \frac{v w}{r}$$

North-South

$$- \left[\frac{1}{r \cos \phi} \frac{\partial}{\partial \lambda} (\rho u v) + \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (\rho v^2 \cos \phi) + \frac{1}{r^2} \frac{\partial}{\partial r} (\rho r^2 v w) \right] + \rho F_\phi,$$

$$\rho \frac{\partial w}{\partial t} + w \frac{\partial \rho}{\partial t} = - \frac{\partial p}{\partial r} - \rho g + \rho \left(2\Omega \cos \phi + \frac{u}{r} \right) u + \rho \frac{v^2}{r}$$

Radial

$$- \left[\frac{1}{r \cos \phi} \frac{\partial}{\partial \lambda} (\rho u w) + \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (\rho v w \cos \phi) + \frac{1}{r^2} \frac{\partial}{\partial r} (\rho r^2 w^2) \right] + \rho F_r.$$

Gilman and Glatzmaier 1981

3D Navier-Stokes, flux limited diffusion and decoupled thermal and radiative components

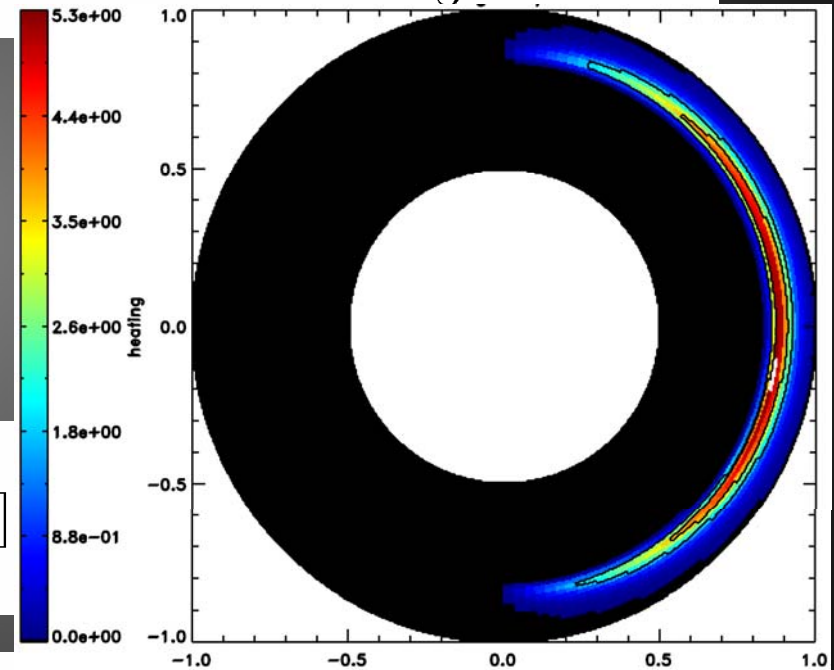
$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\frac{\nabla P}{\rho} + \mathbf{g} - 2\boldsymbol{\Omega} \times \mathbf{u} - \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{r}) + \nu \nabla^2 \mathbf{u} + \frac{\nu}{3} \nabla (\nabla \cdot \mathbf{u})$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\mathbf{F} = -\lambda \frac{c}{\rho \kappa_R(T, P)} \nabla E_R$$

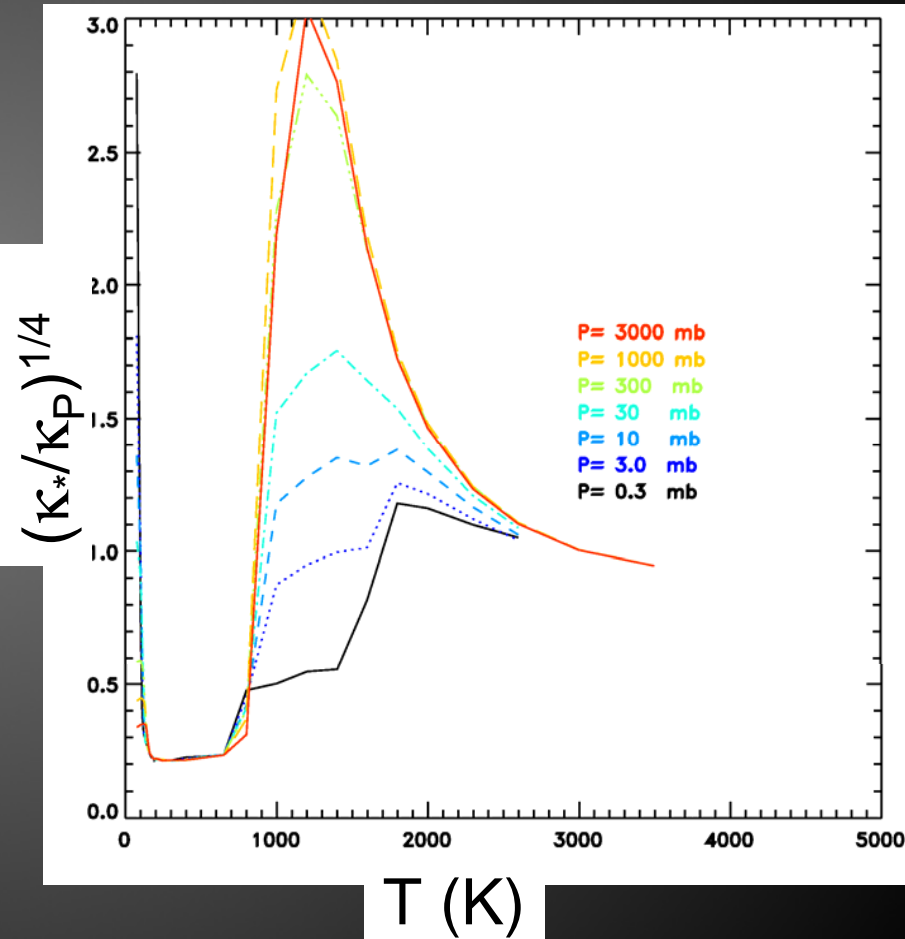
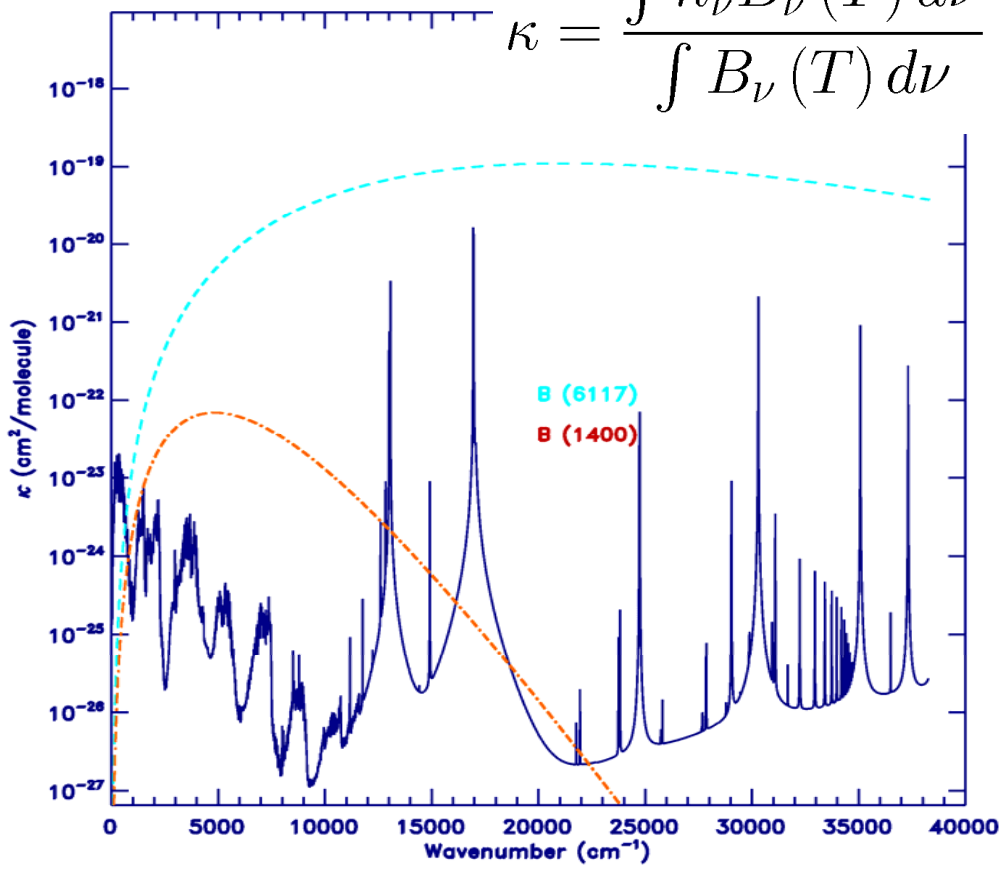
$$\frac{\partial E_R}{\partial t} + \nabla \cdot \mathbf{F} = \rho \kappa_P(T, P) [B(T) - cE_R]$$

$$\left[\frac{\partial \epsilon}{\partial t} + (\mathbf{u} \cdot \nabla) \epsilon \right] = -P \nabla \cdot \mathbf{u} - \rho \kappa_P(T, P) [B(T) - cE_R] + \rho \kappa_\star(T, P) F_\star e^{-\tau_\star} + \Phi_\nu$$

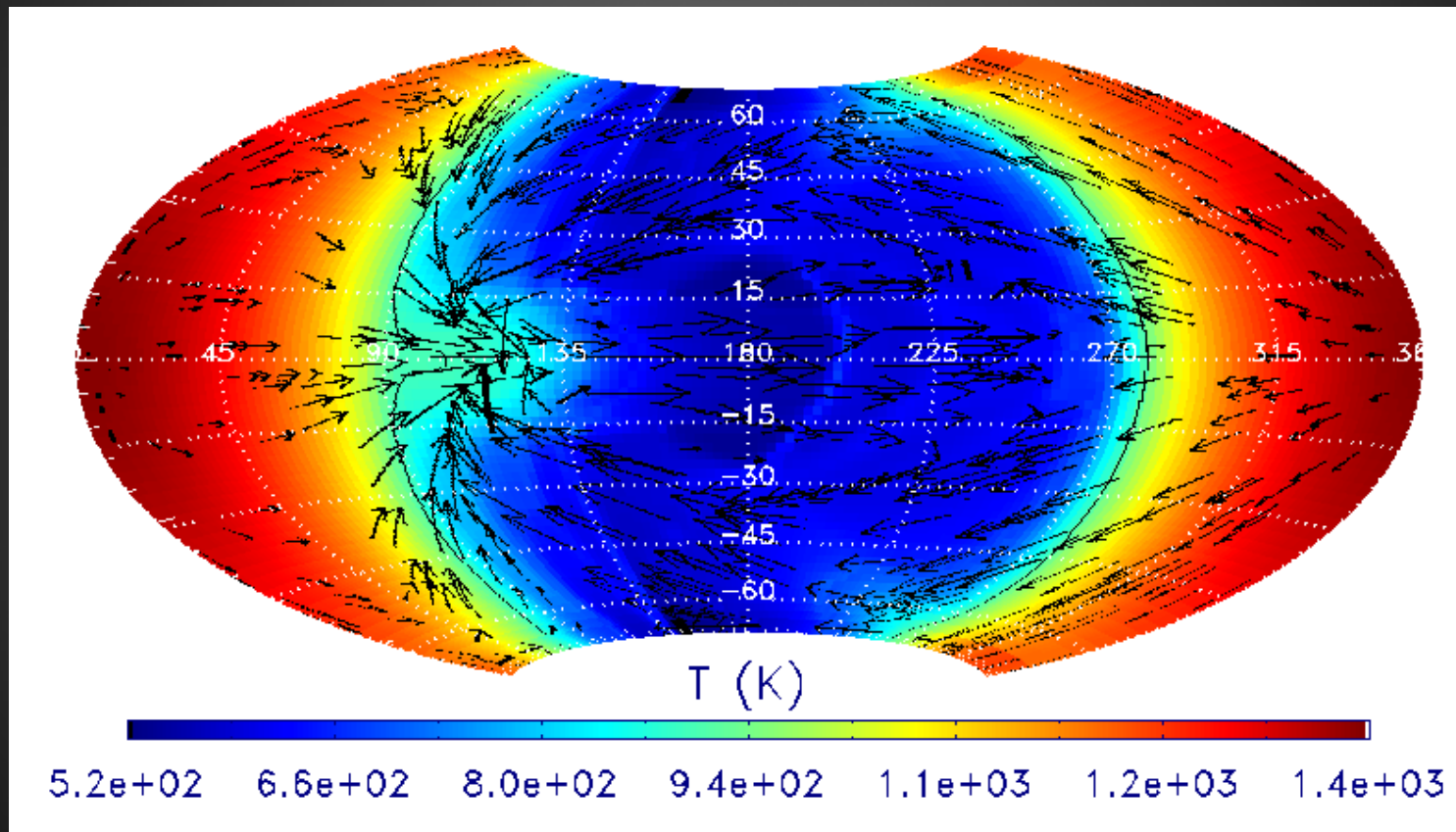


Absorption vs. Emission Opacities

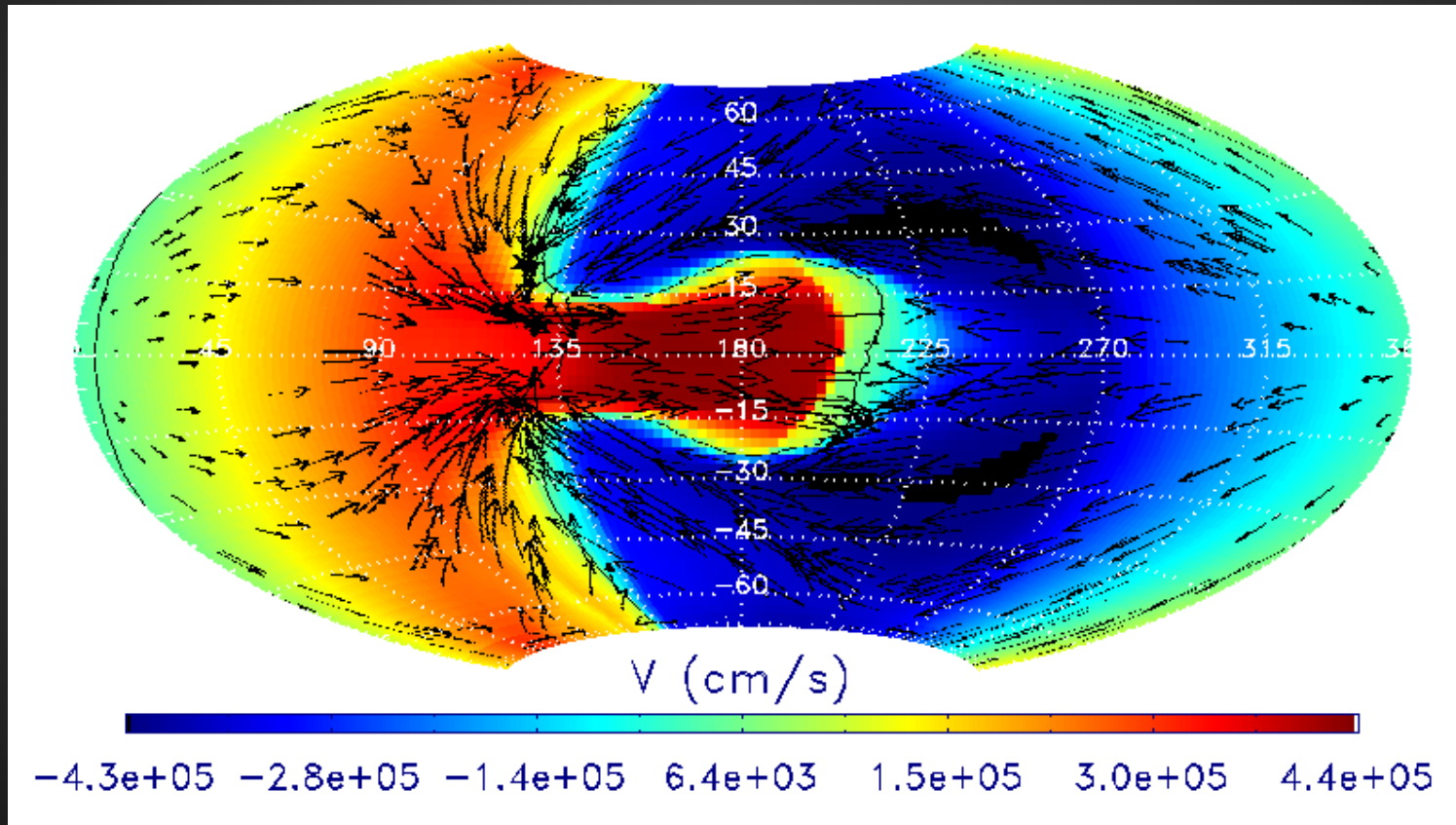
$$\kappa = \frac{\int \kappa_\nu B_\nu(T) d\nu}{\int B_\nu(T) d\nu}$$



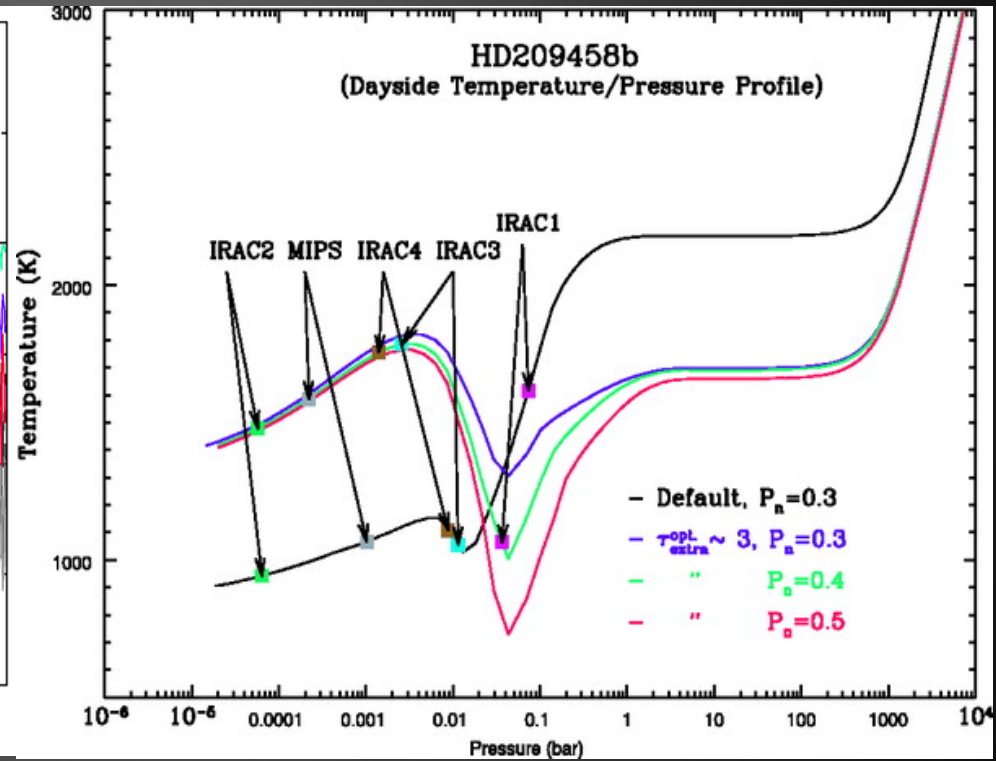
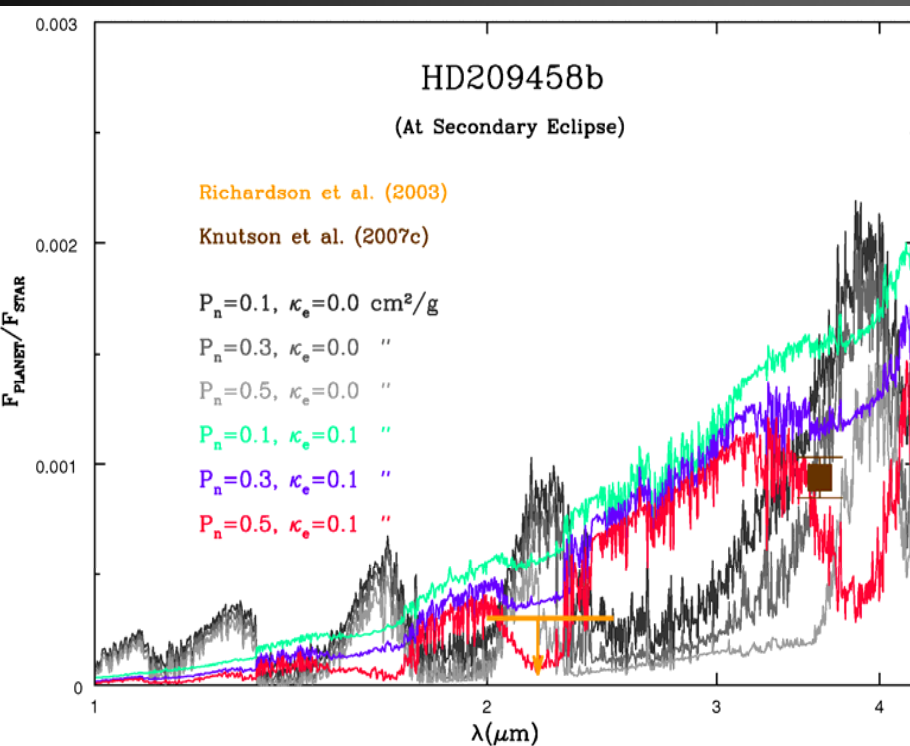
$$P_{\text{rot}} = P_{\text{orb}} = 3.52\text{d}, T_{\star} = 6117\text{K}$$
$$M_{\text{p}} = 0.69M_{\text{J}}, R_{\text{p}} = 1.3R_{\text{J}}$$



Photospheric Velocities

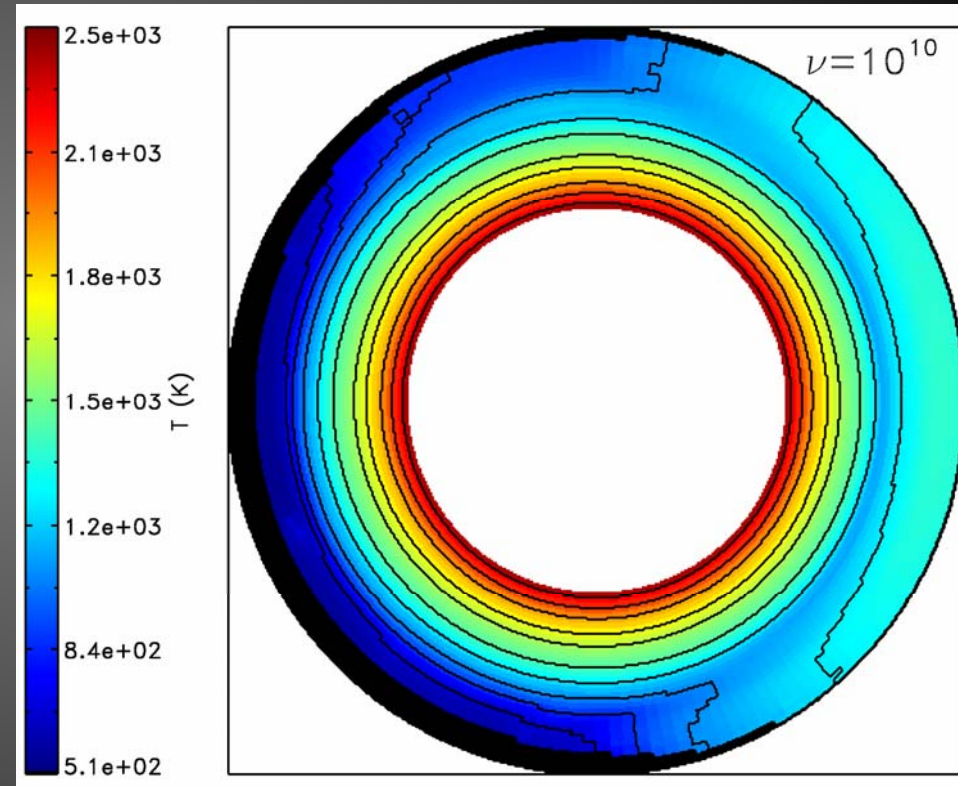
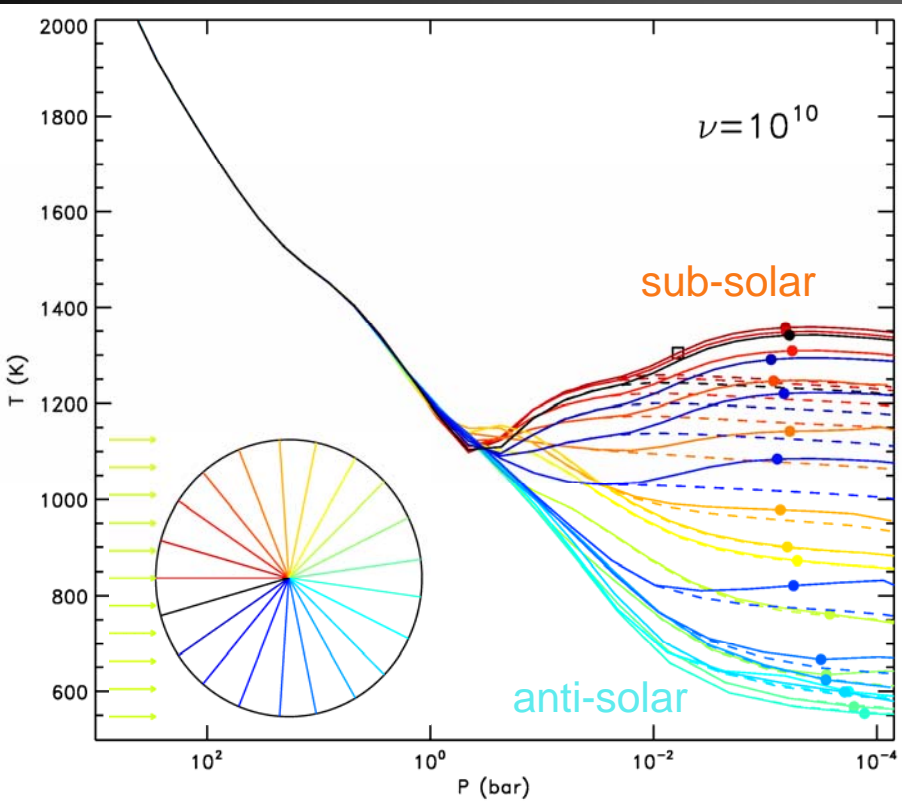


Observed Inversion (HD 209458b)



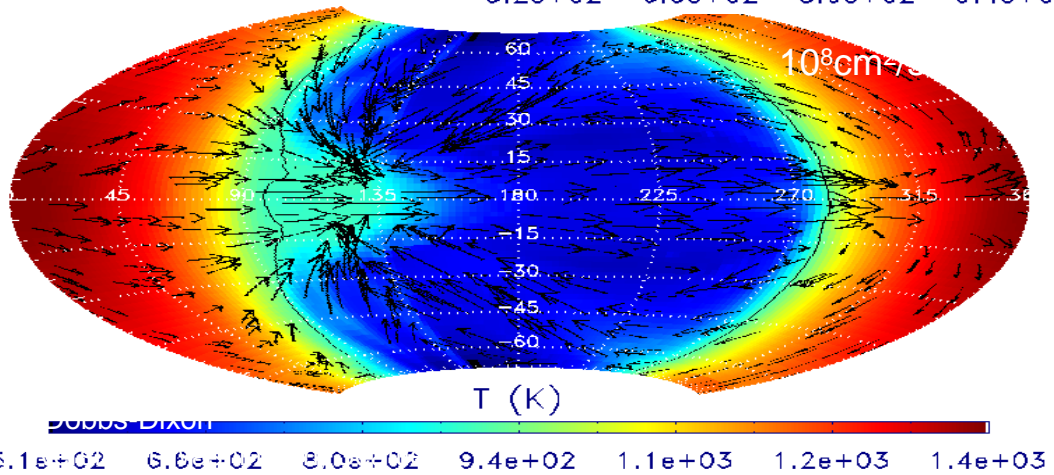
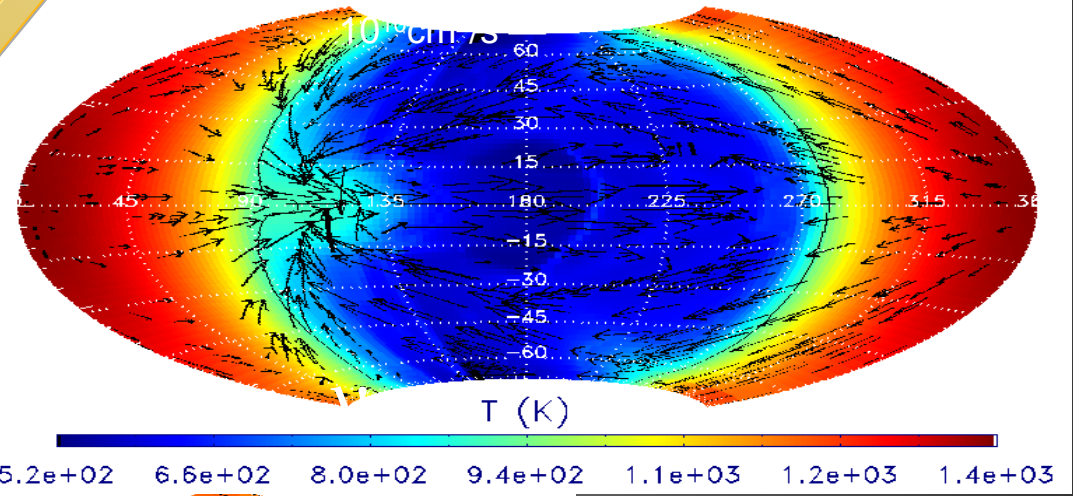
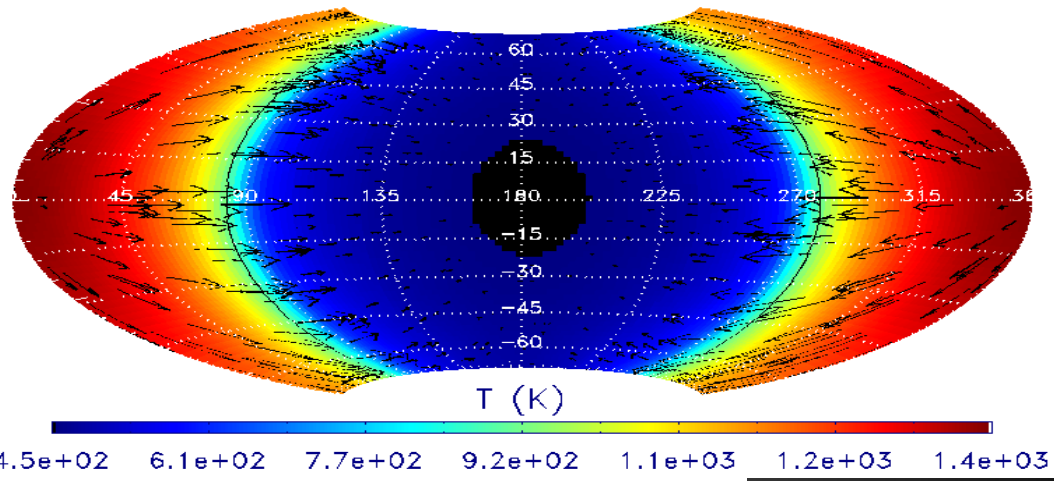
Burrows et al (2007)

HD209458b



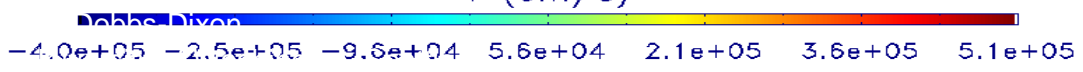
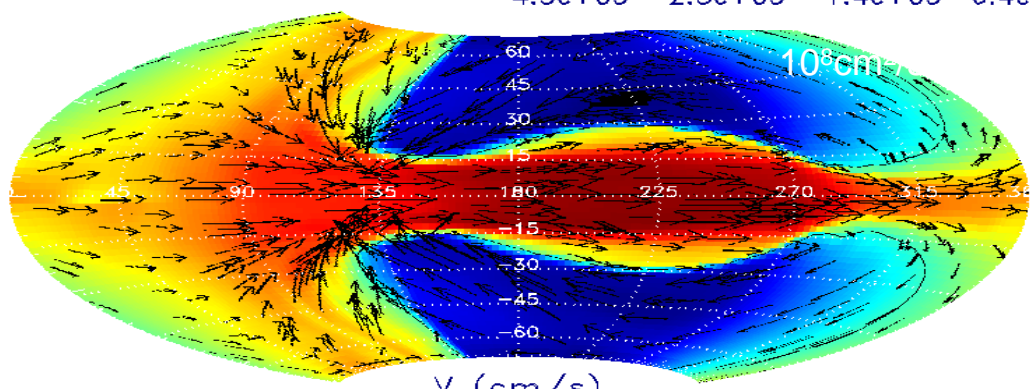
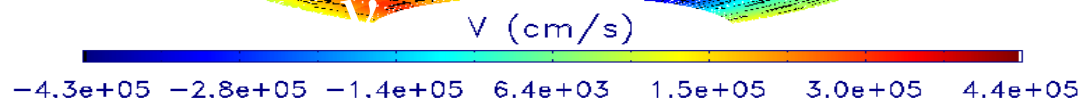
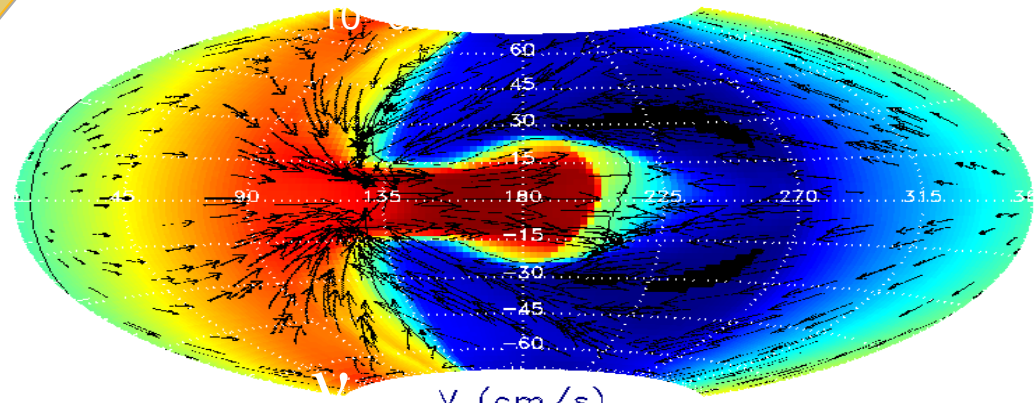
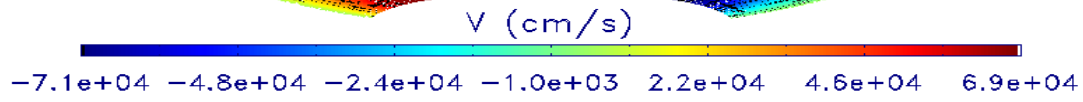
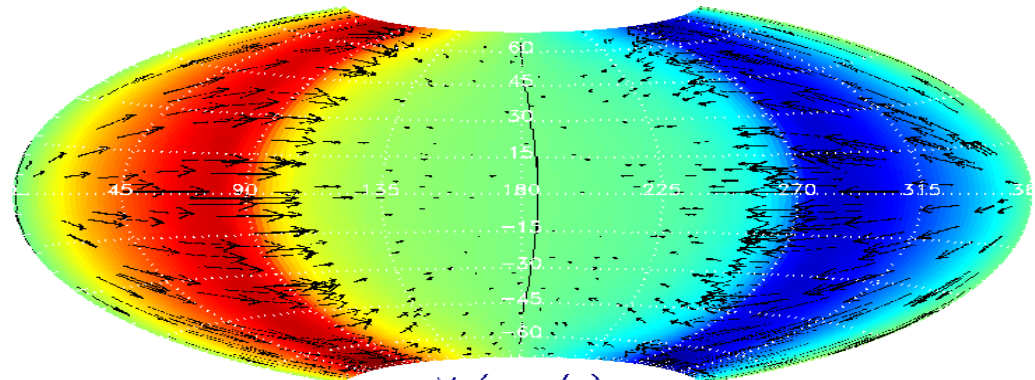
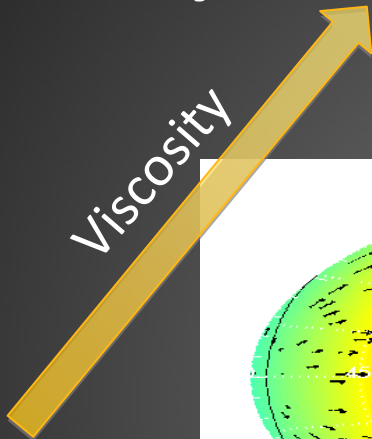
Varying Viscosity

Viscosity



Varying Viscosity

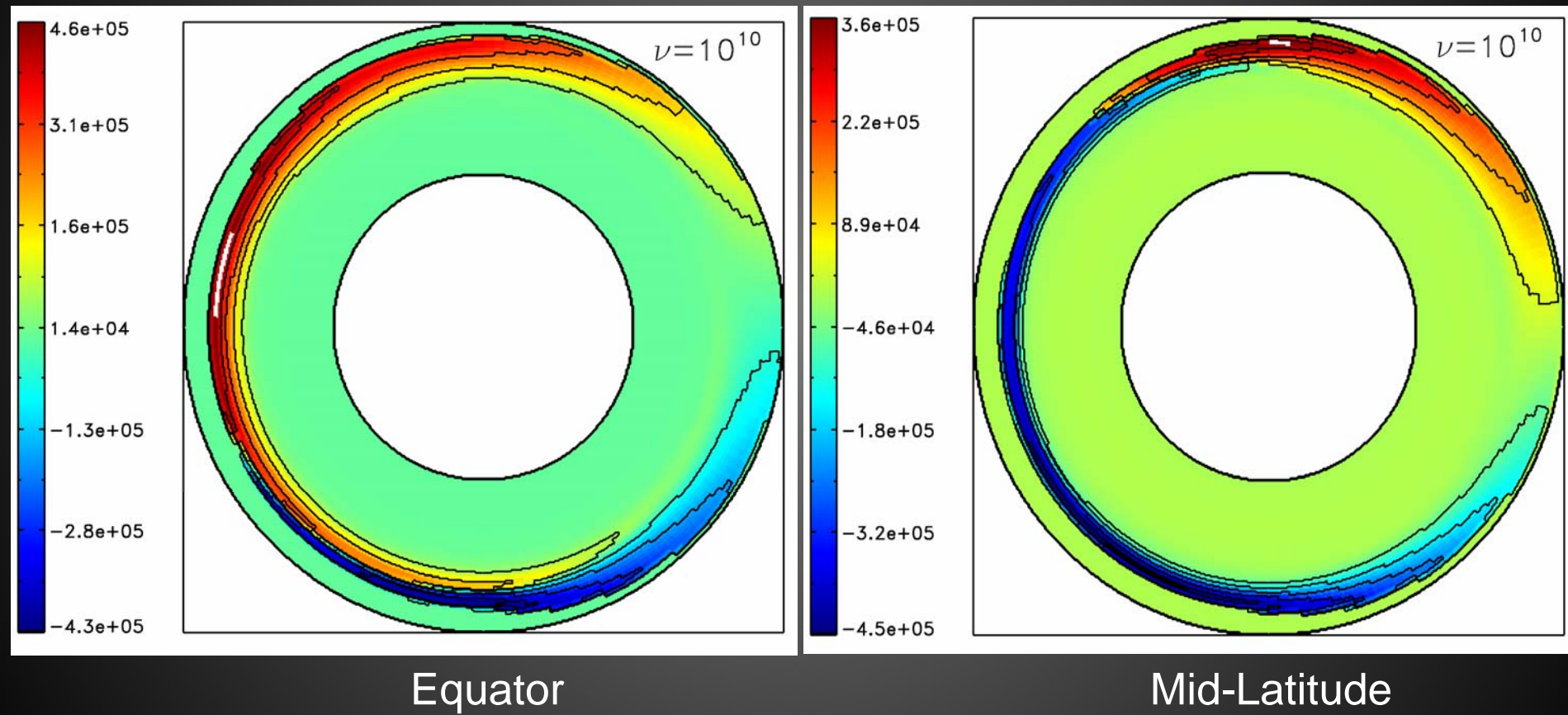
Viscosity

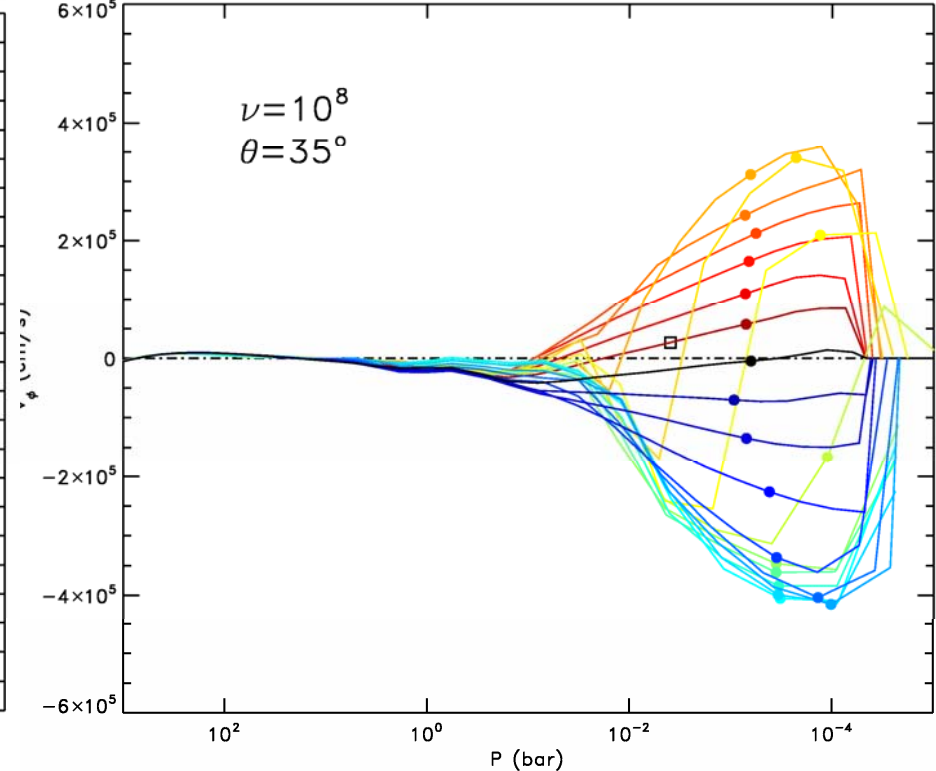
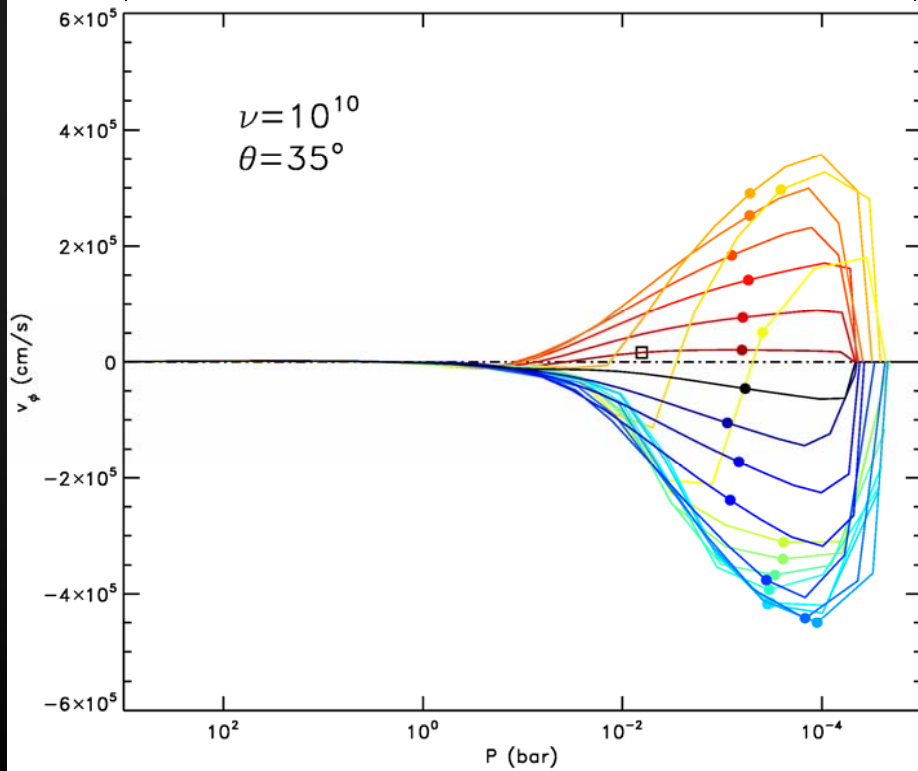
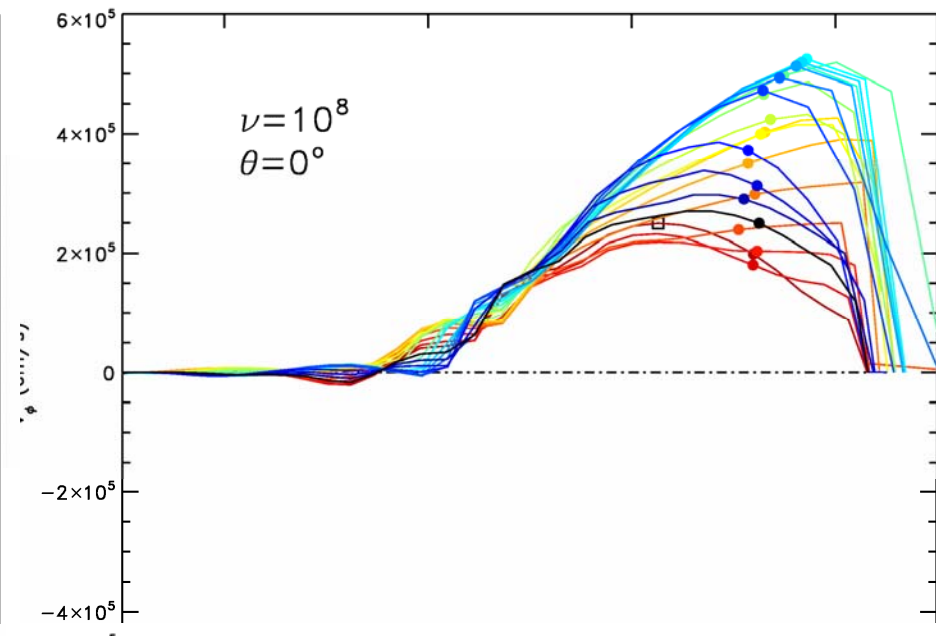
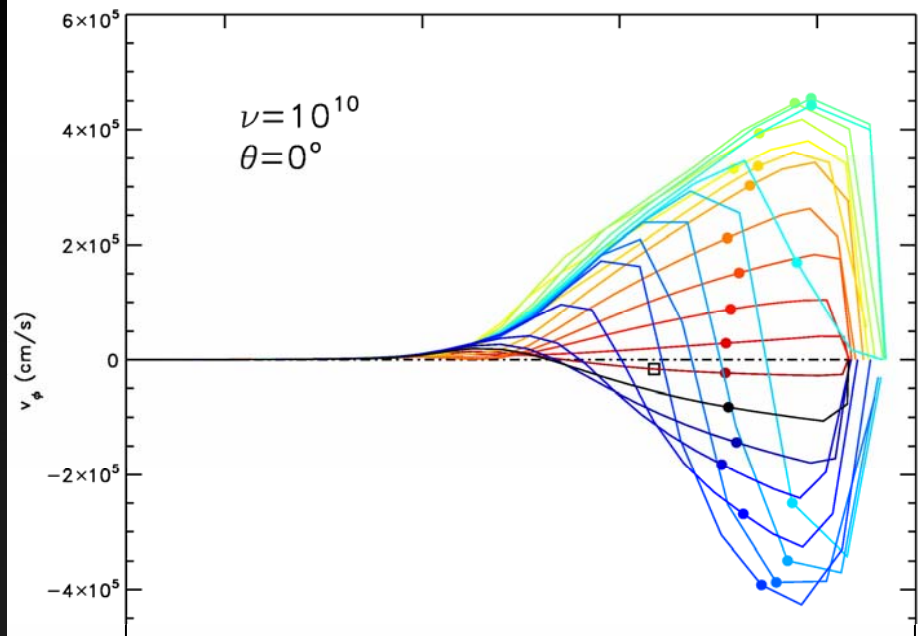


10^8 cm^{-2}

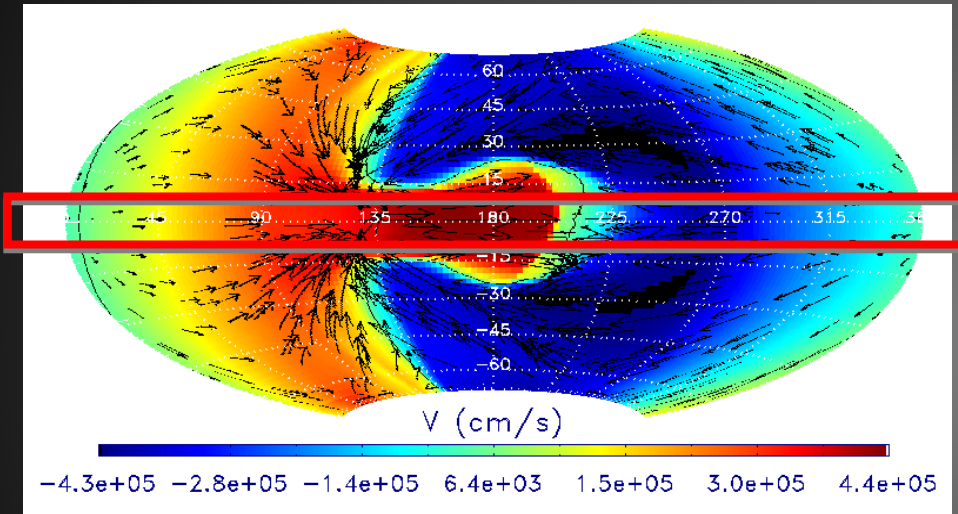
Johns-Dixon

Velocity Structure with Radius

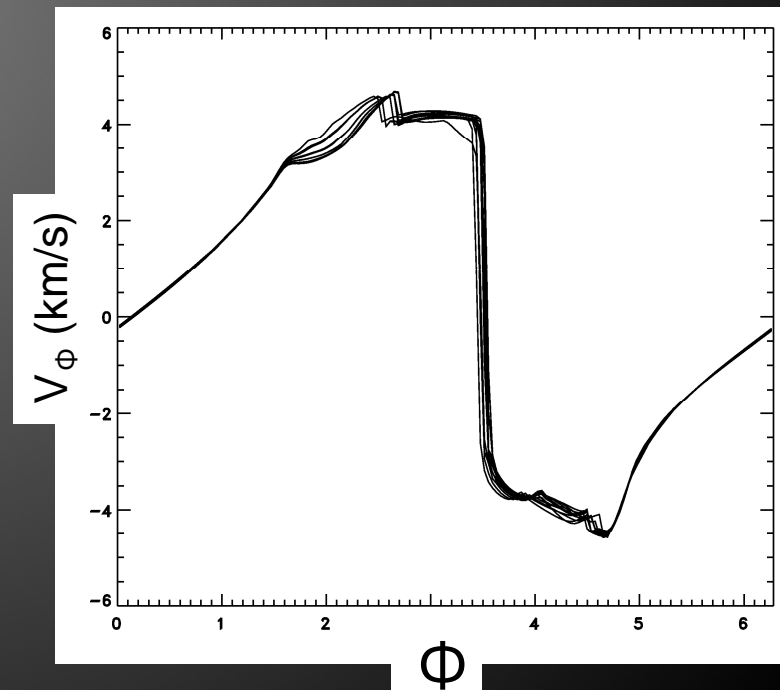
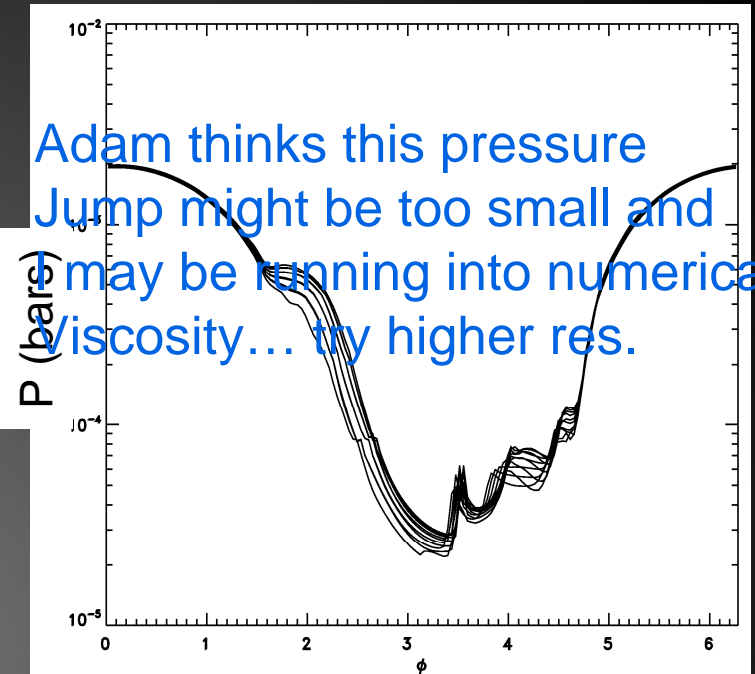
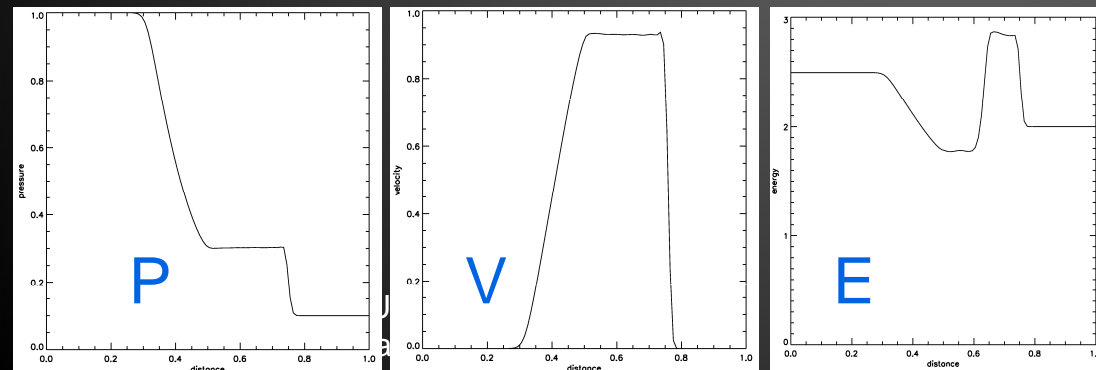




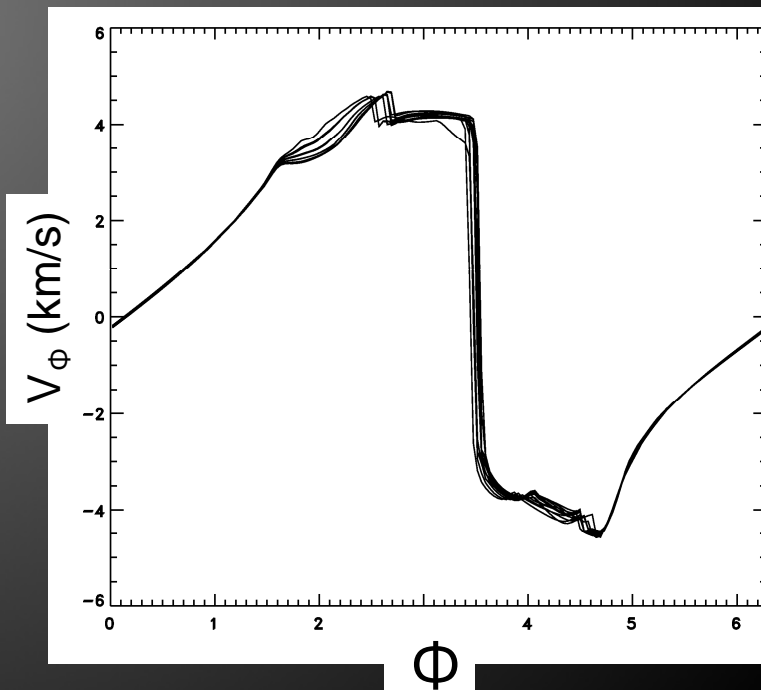
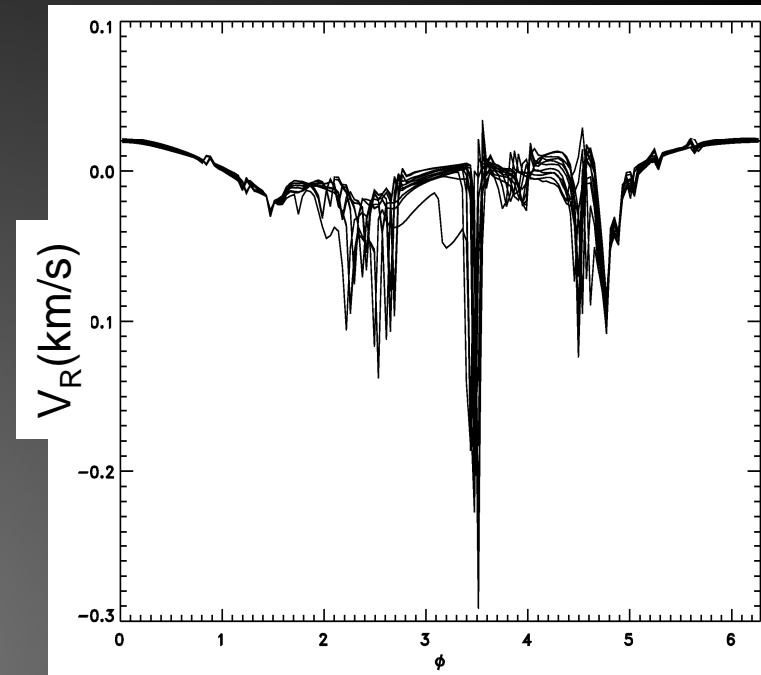
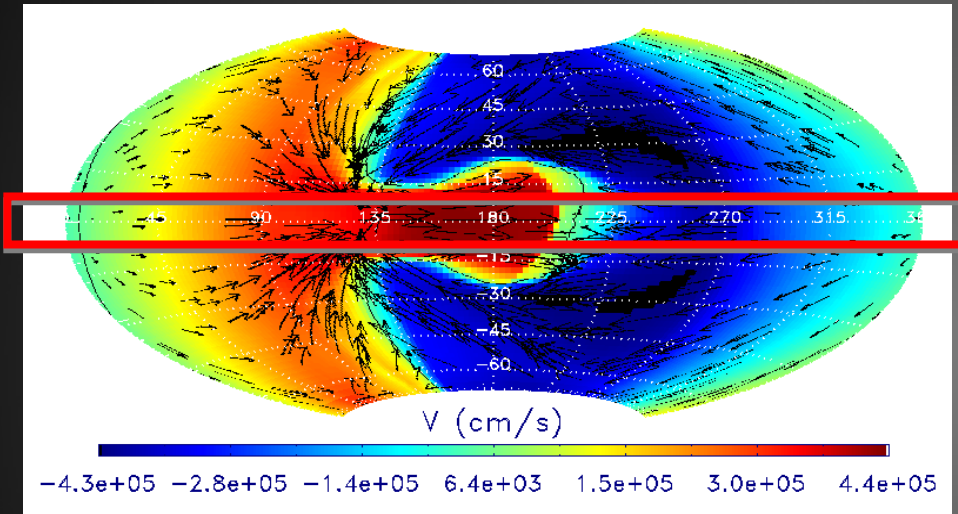
Horizontal Equatorial Shock Structure



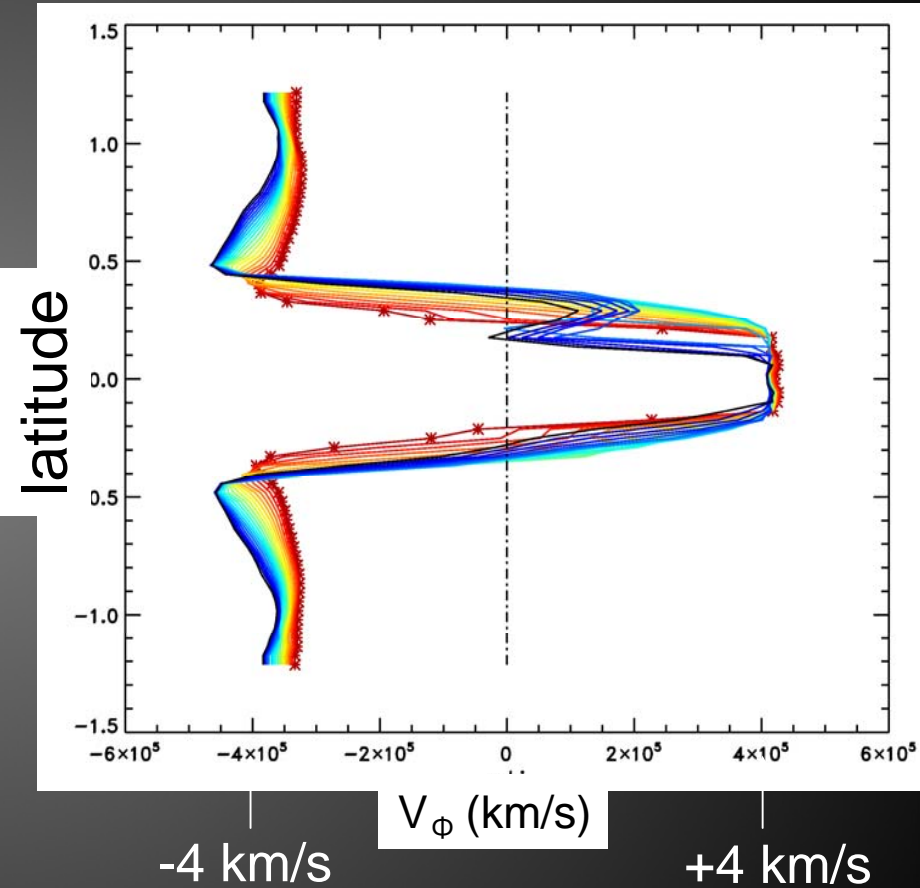
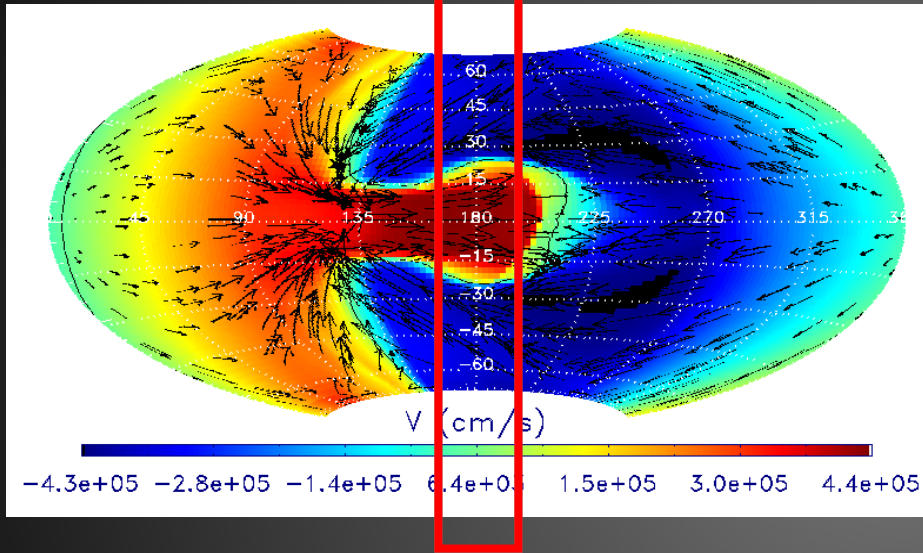
1D Riemann shock tube



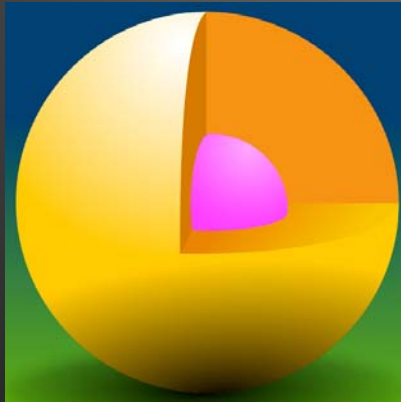
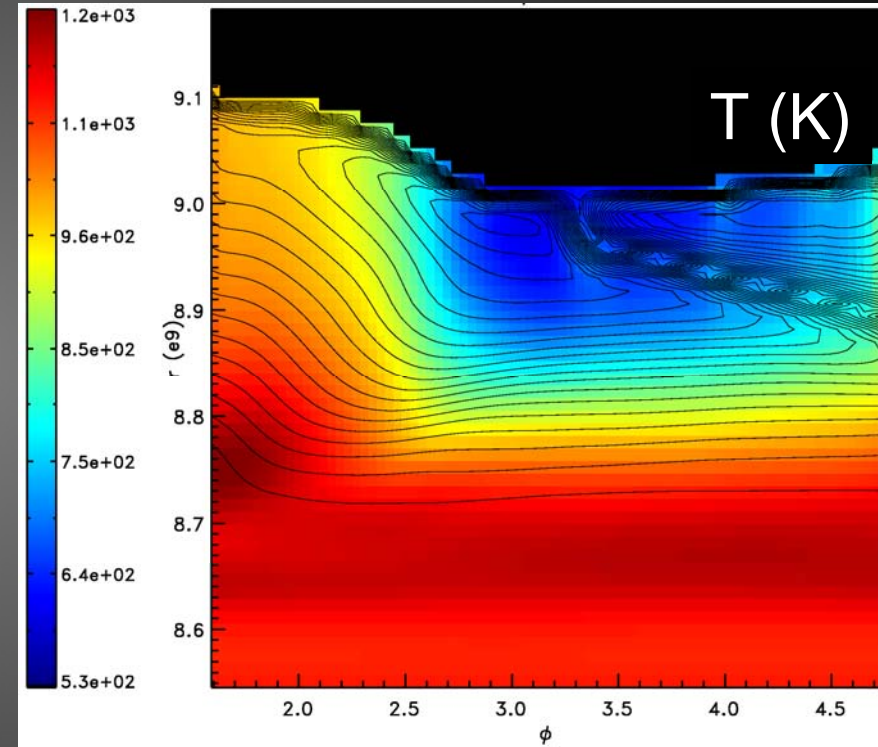
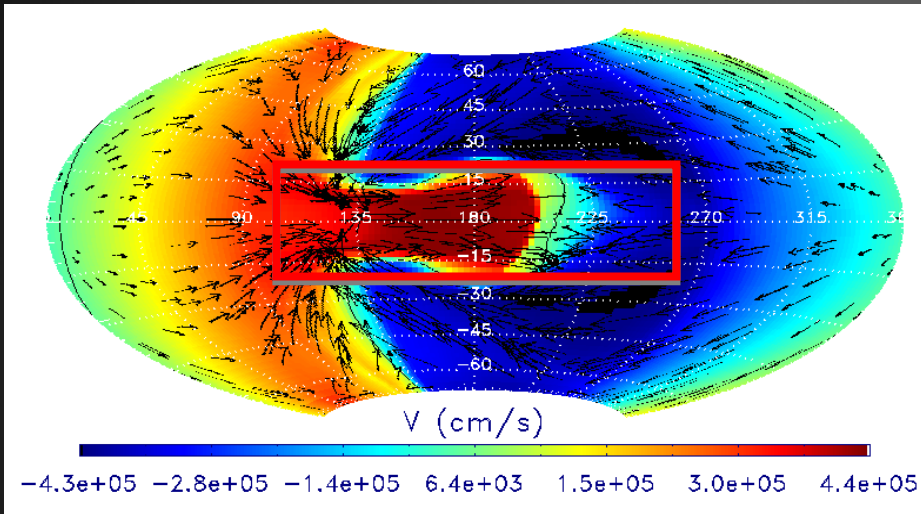
Horizontal Equatorial Shock Structure

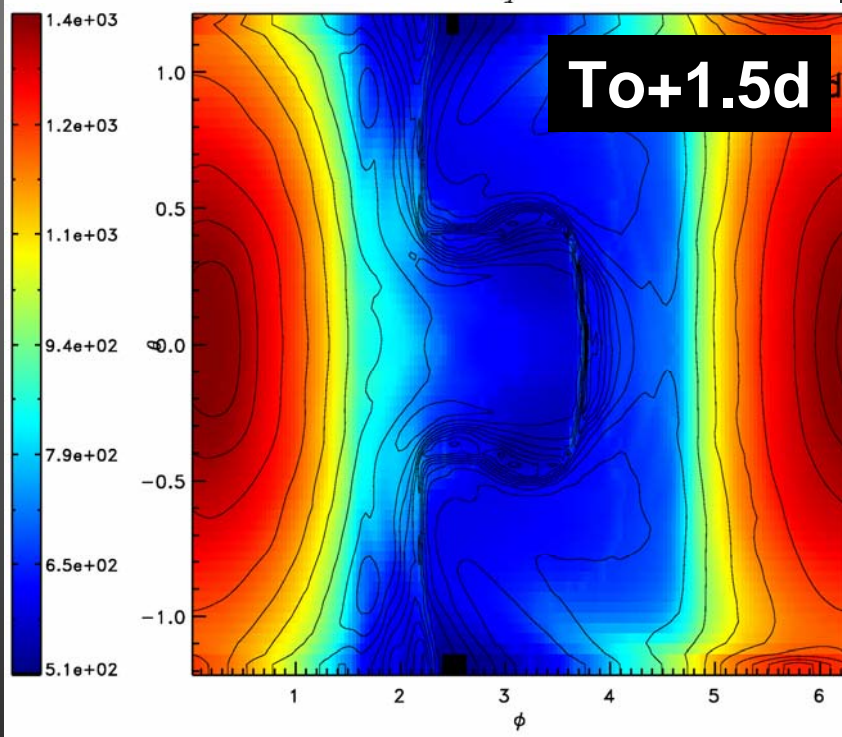
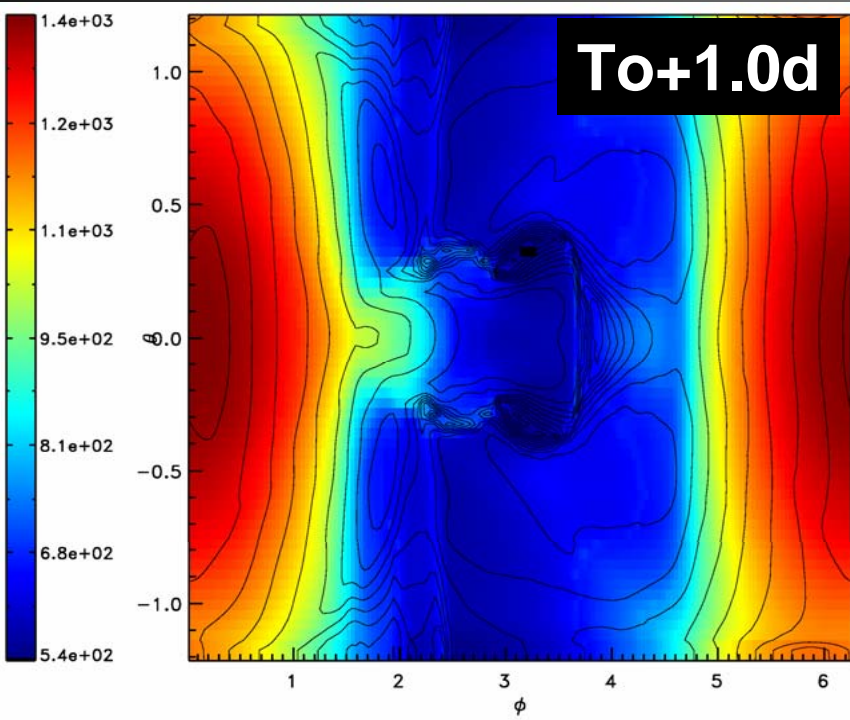
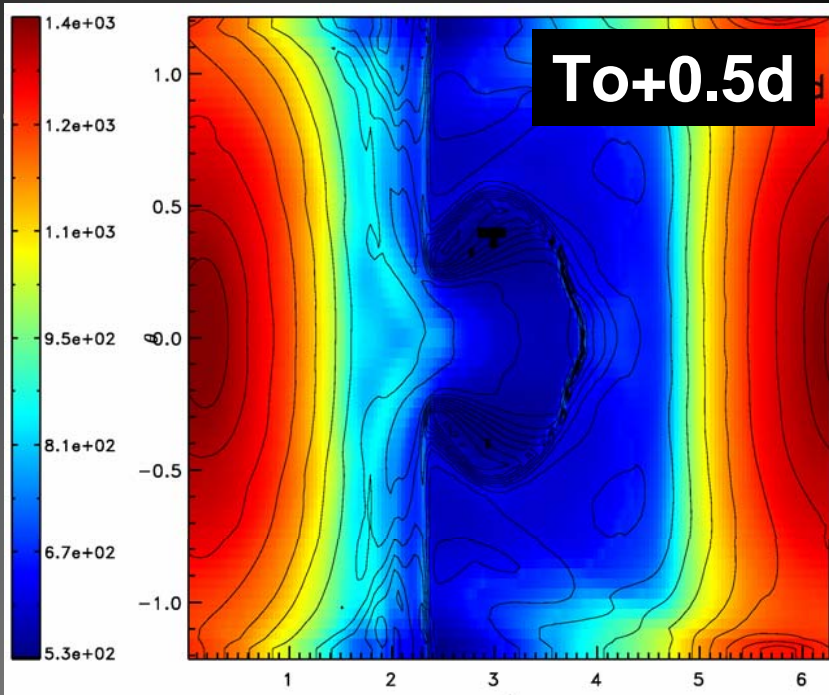
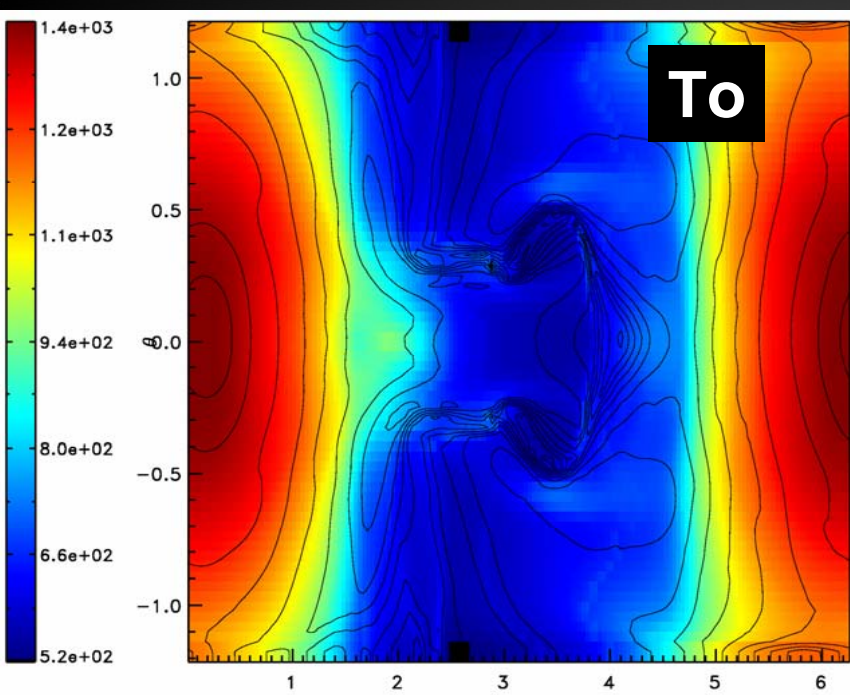


Horizontal Latitudinal Shearing

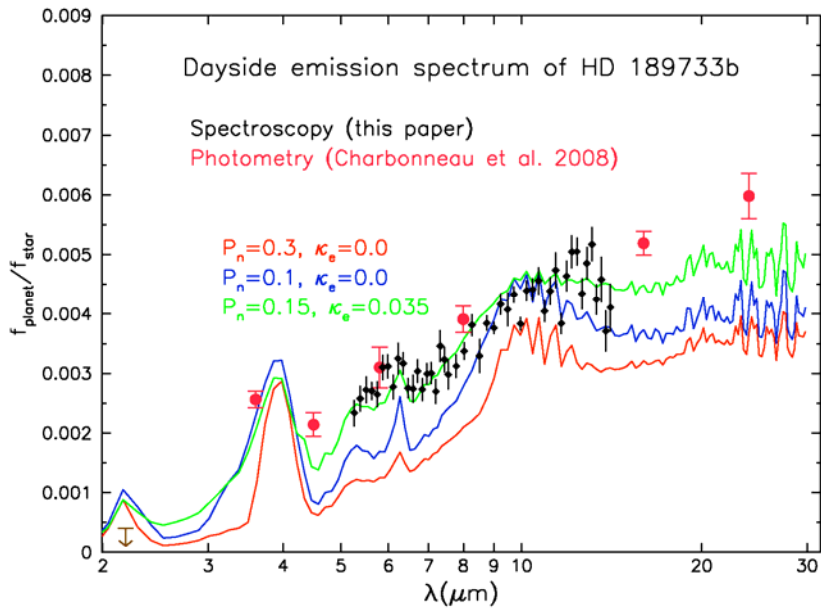


Radial Shearing

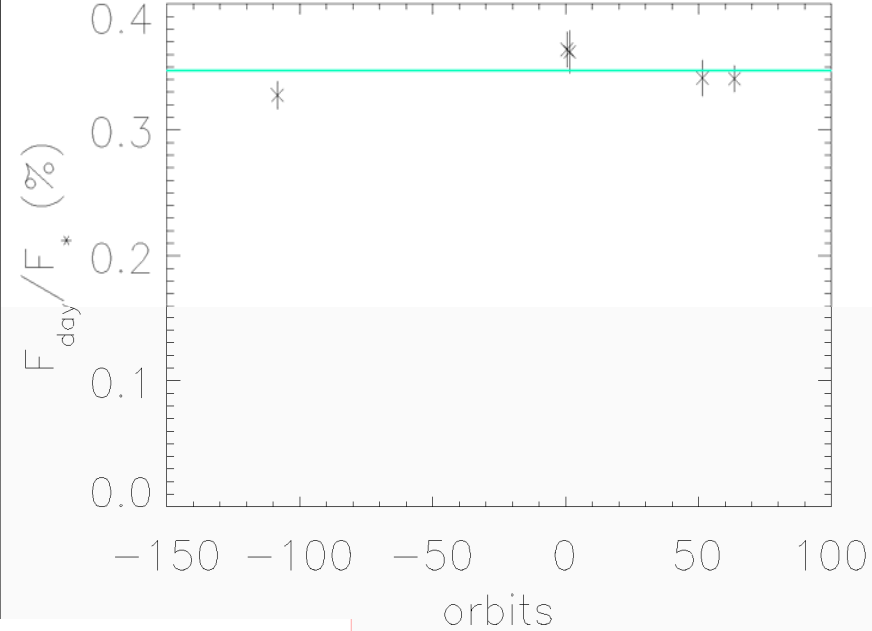




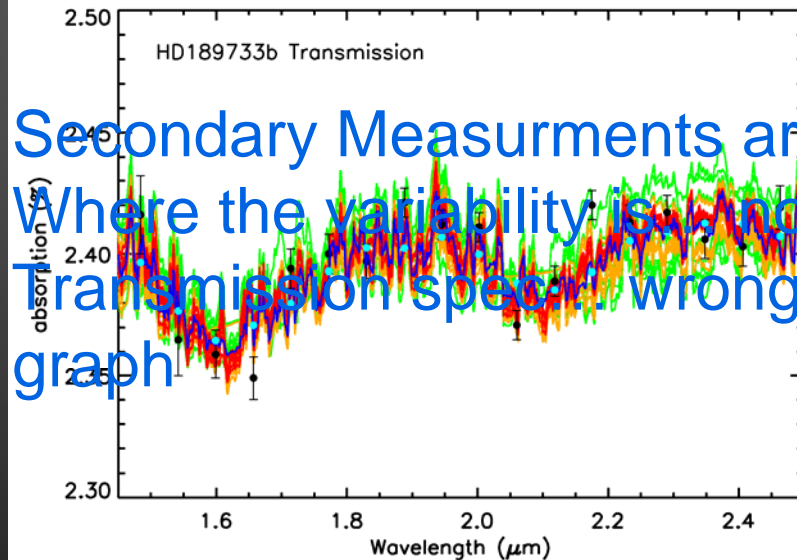
Observed Variability?



Grillmair et al 2008



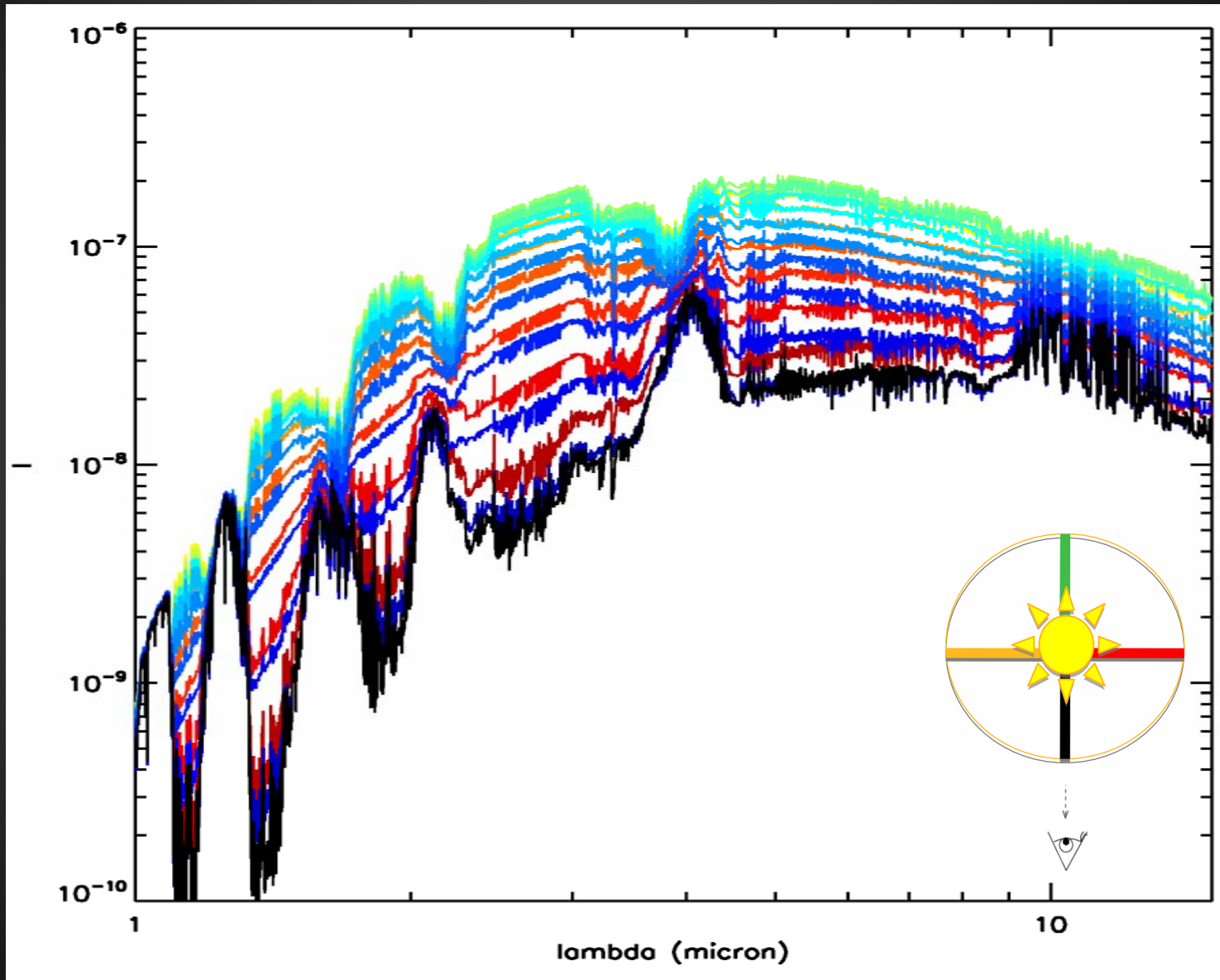
Agol et al 2009



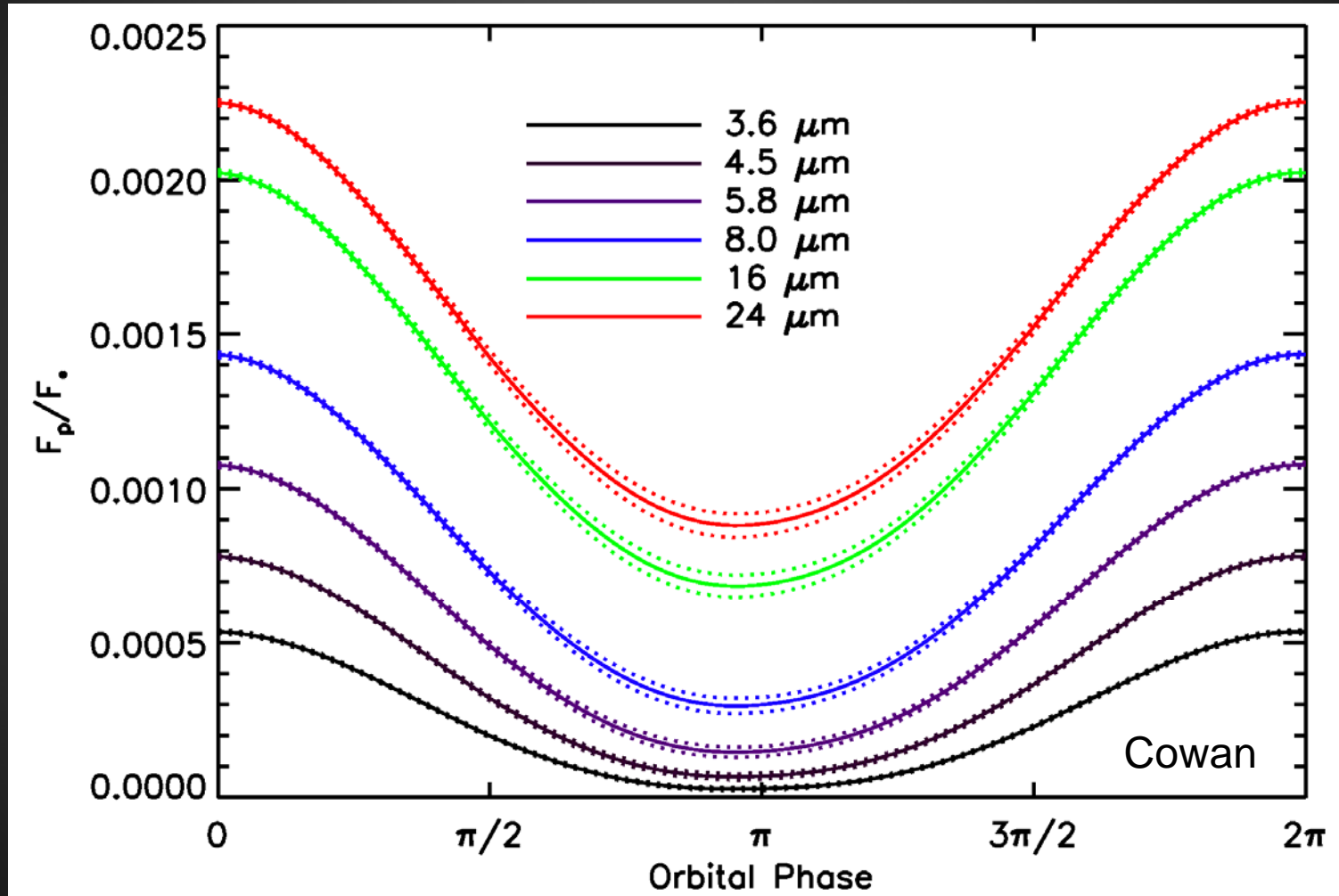
Secondary Measurements are
Where the variability is not
Transmission spec: wrong
graph

Madhusudhan and Seager 2009

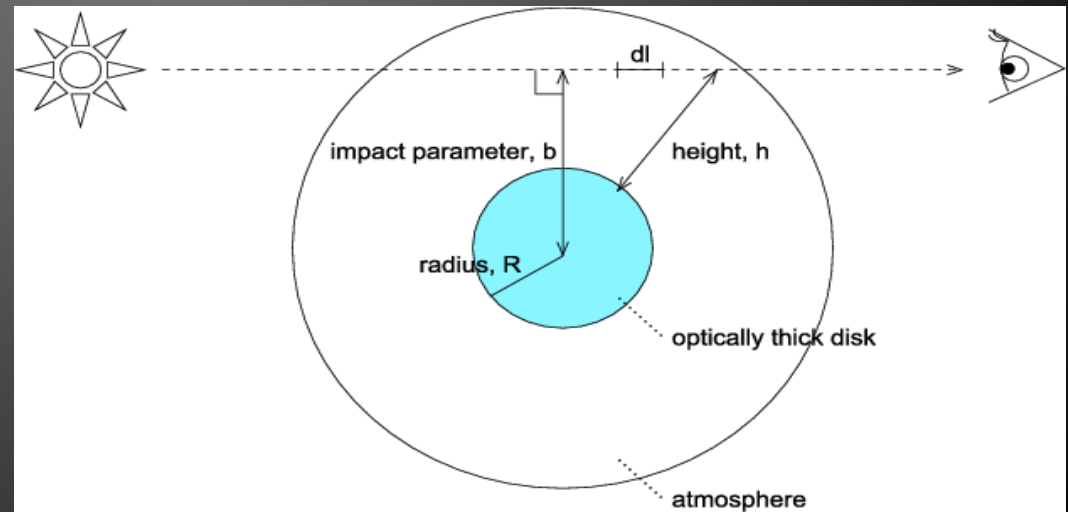
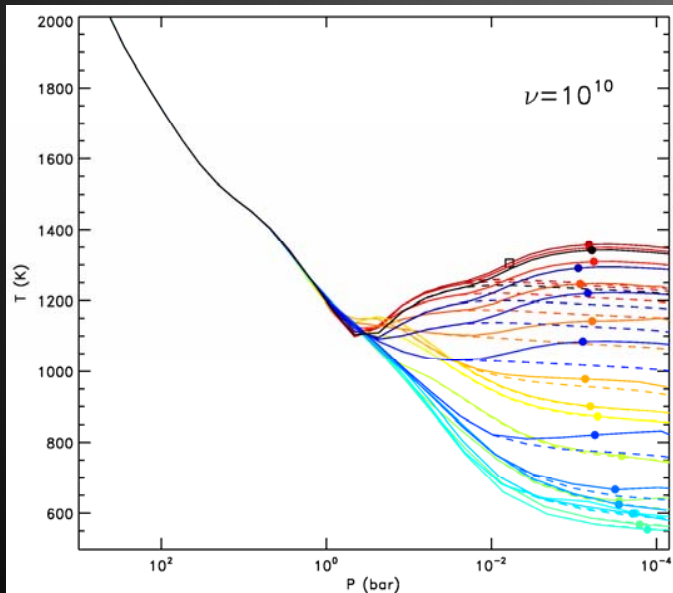
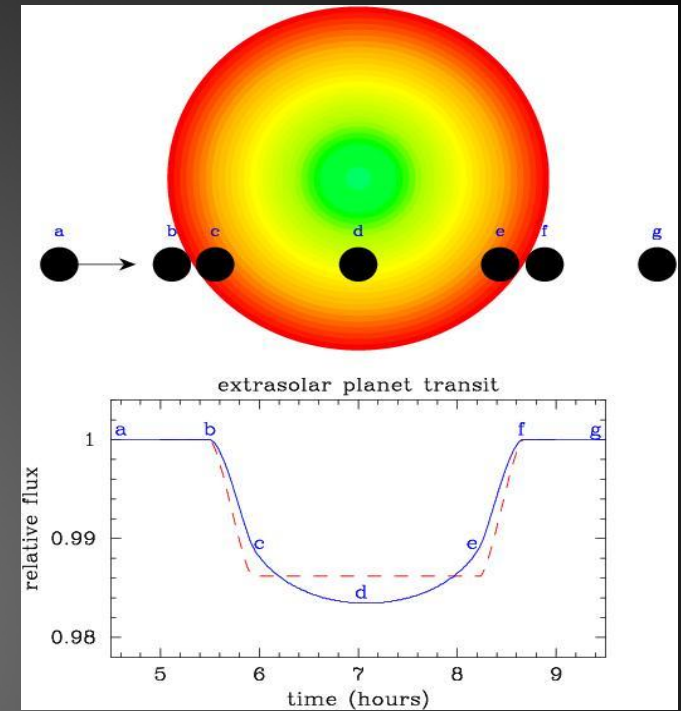
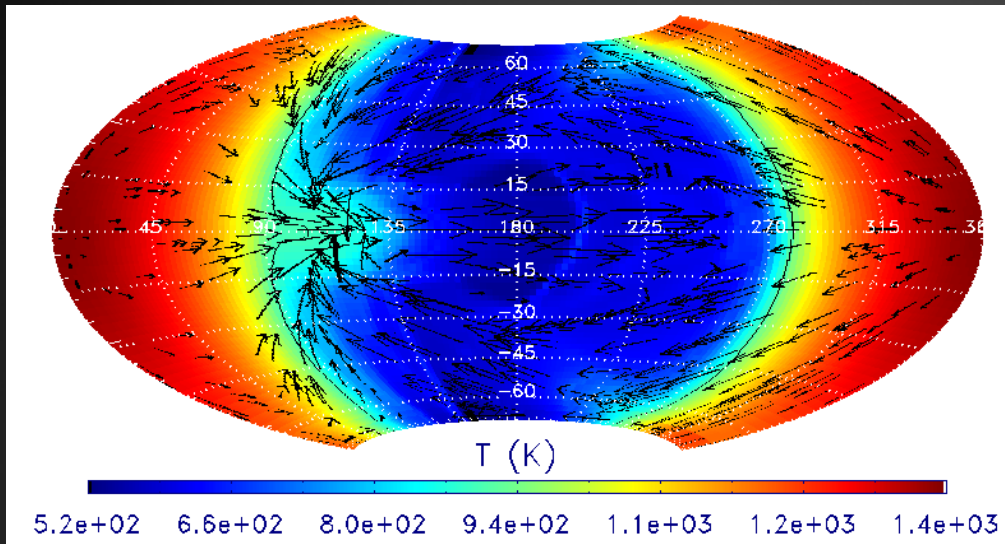
Emission Spectra



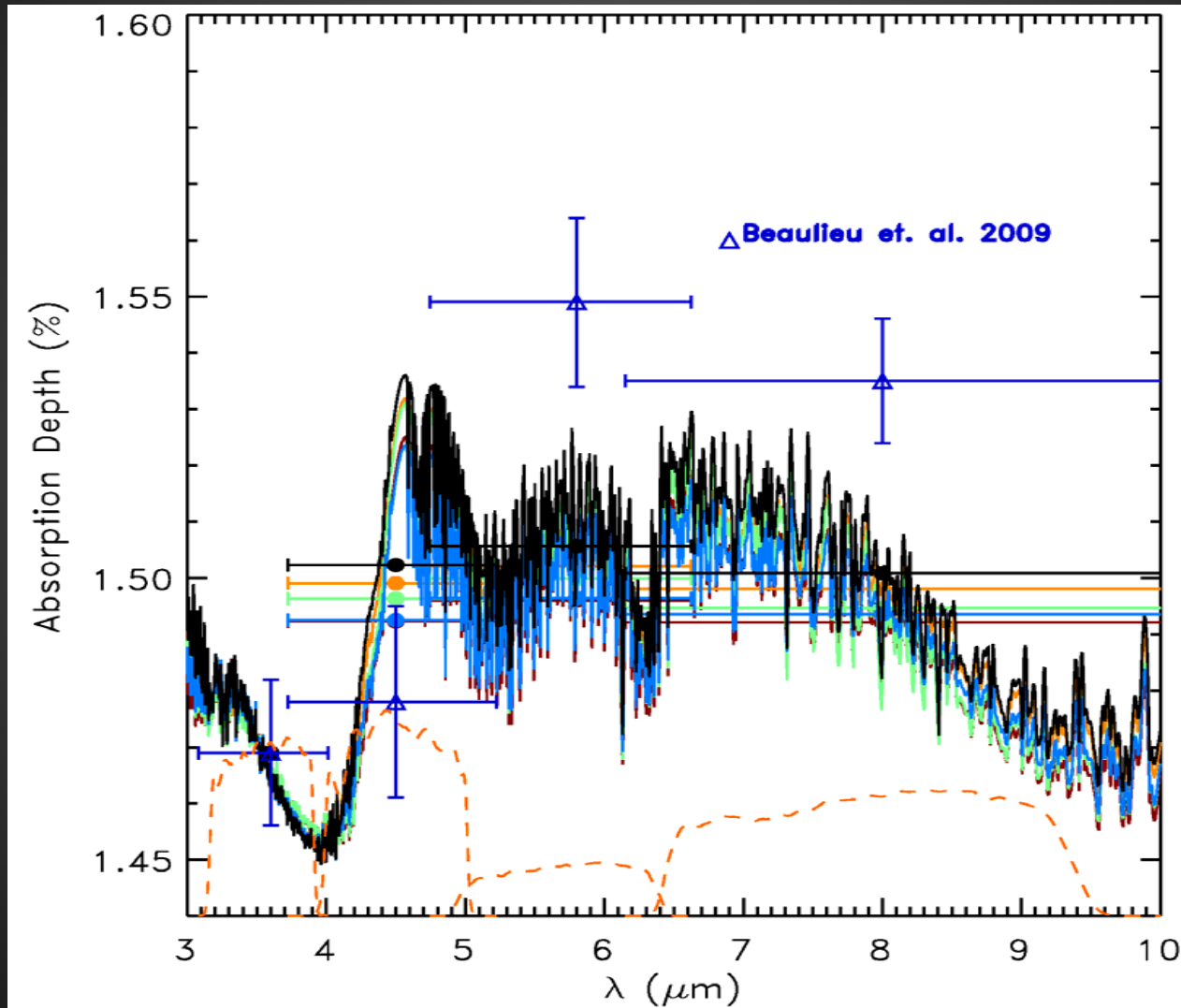
Emission Spectra



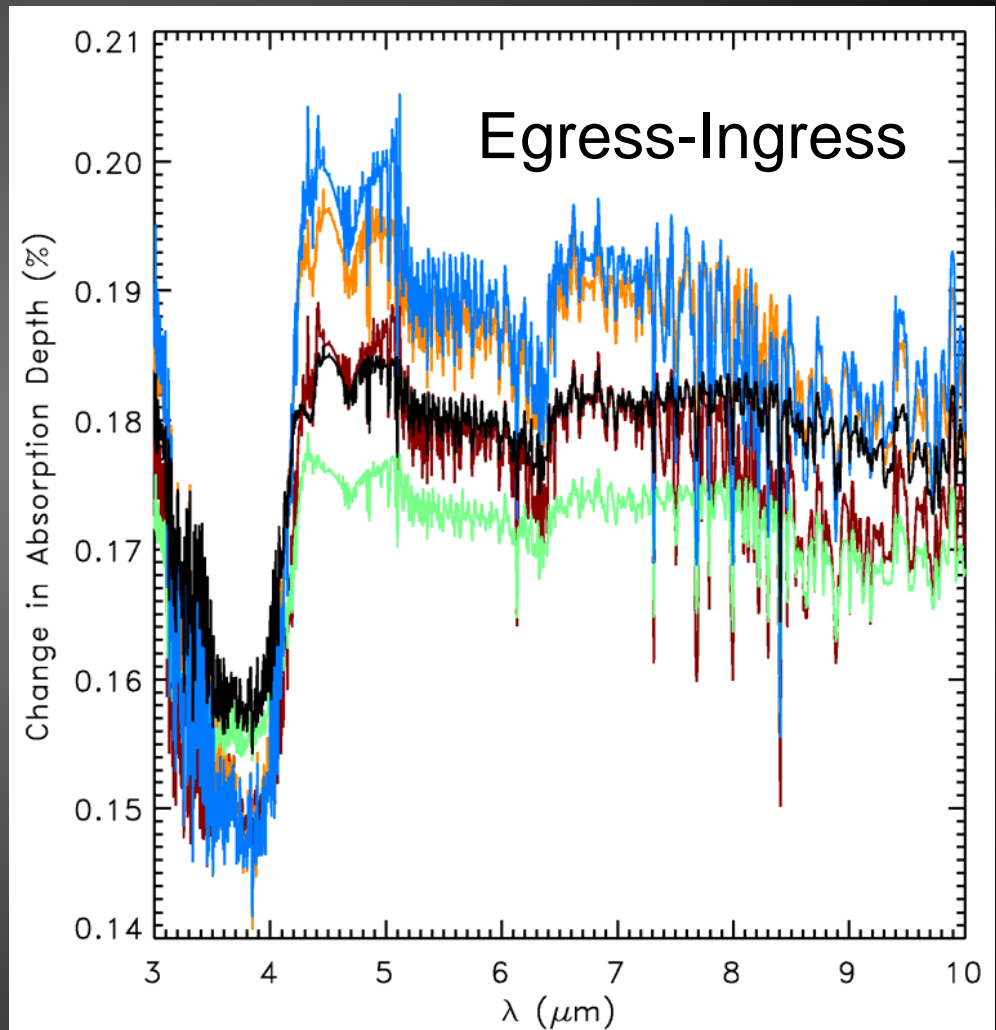
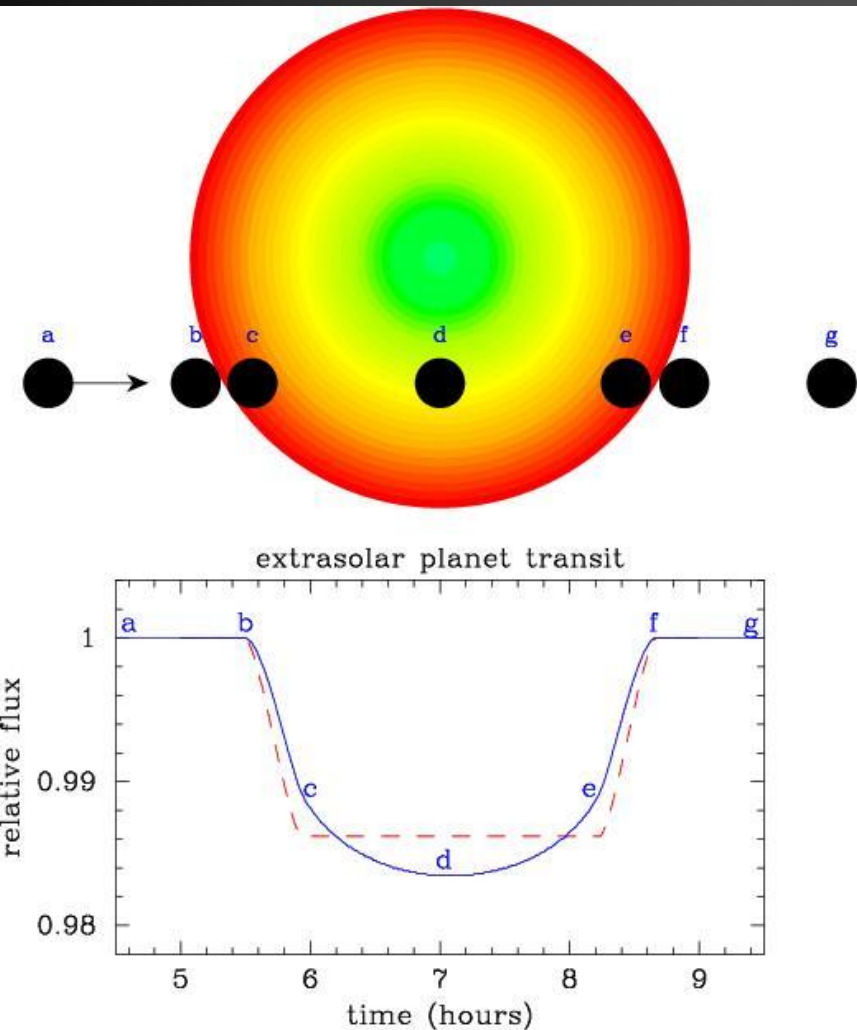
Transmission Spectra



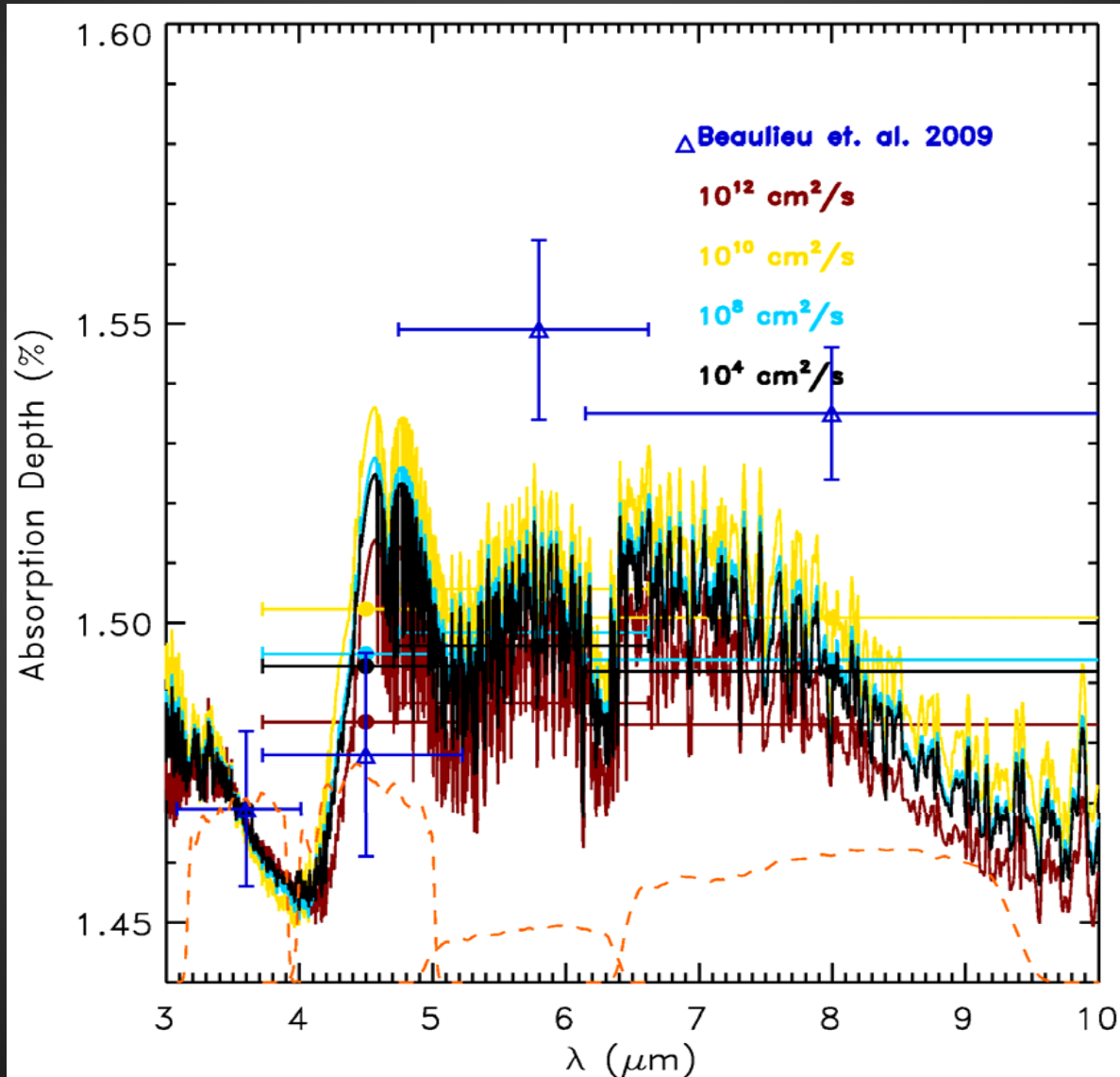
Transmission Spectra: temporal variations



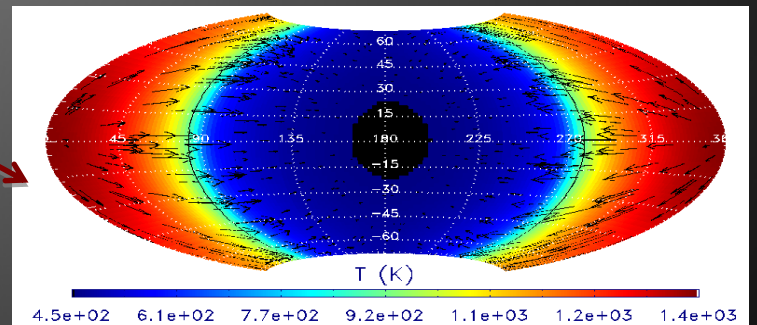
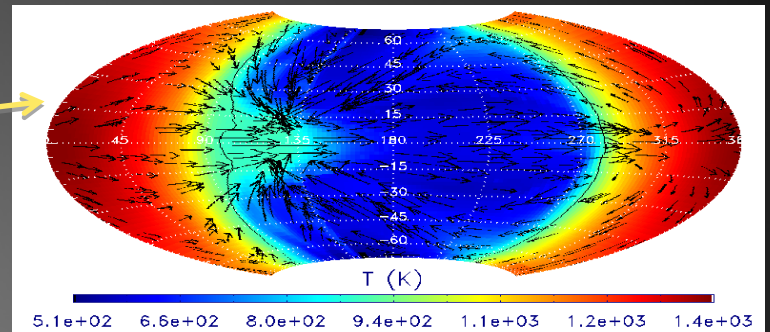
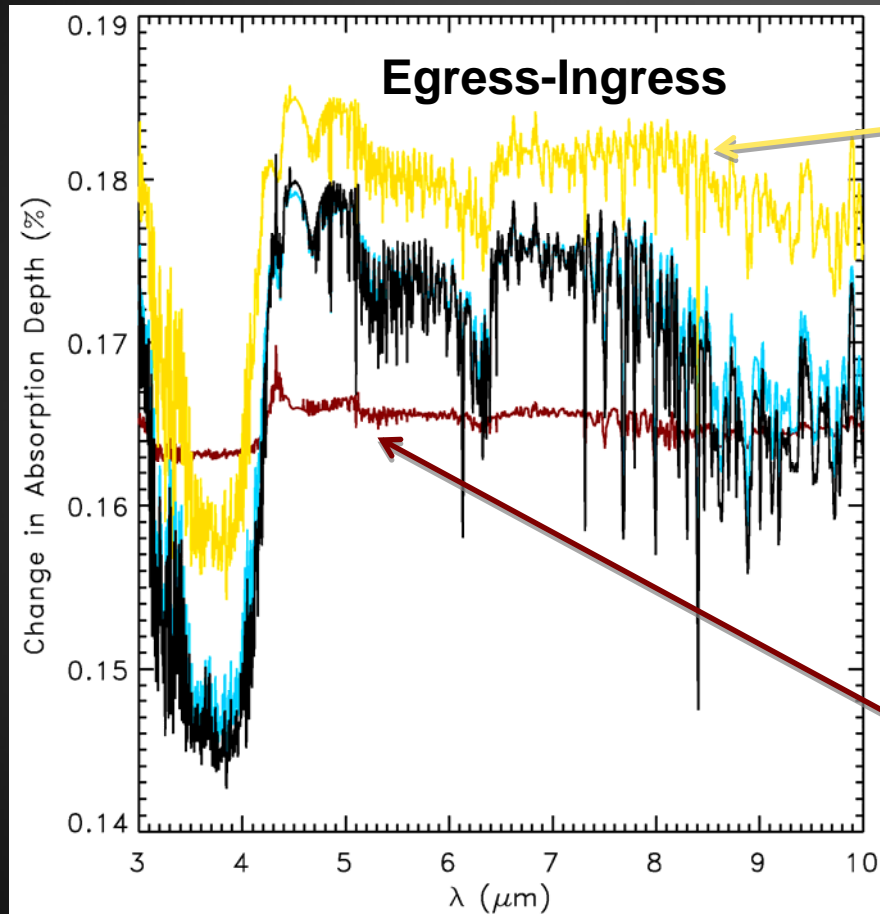
Transmission Spectra: temporal variations



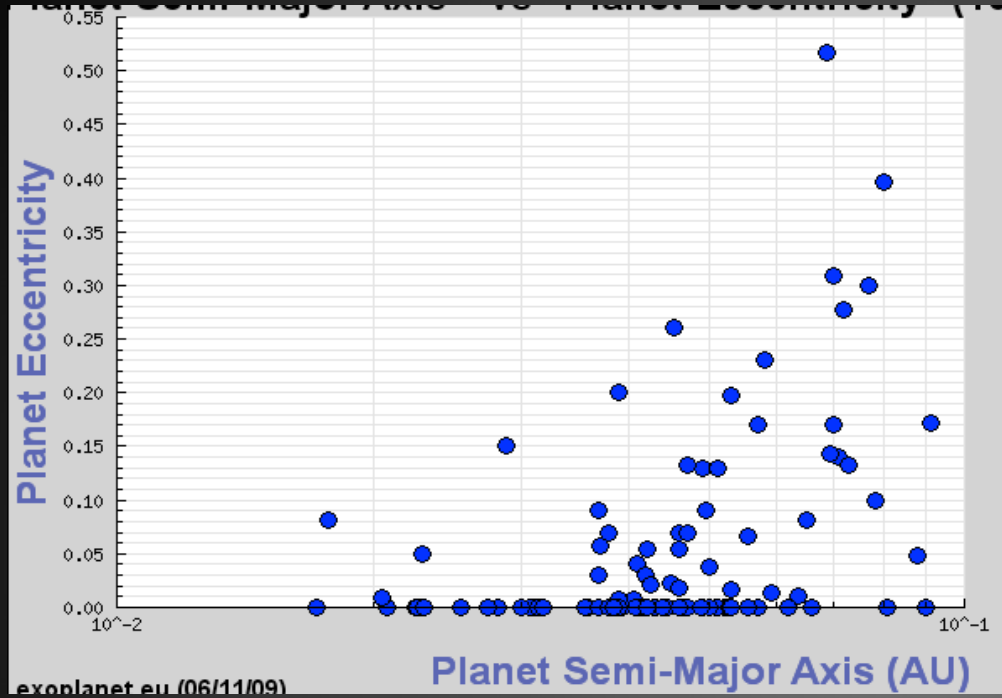
Transmission Spectra: viscous effects



Transmission Spectra: Viscous Variations

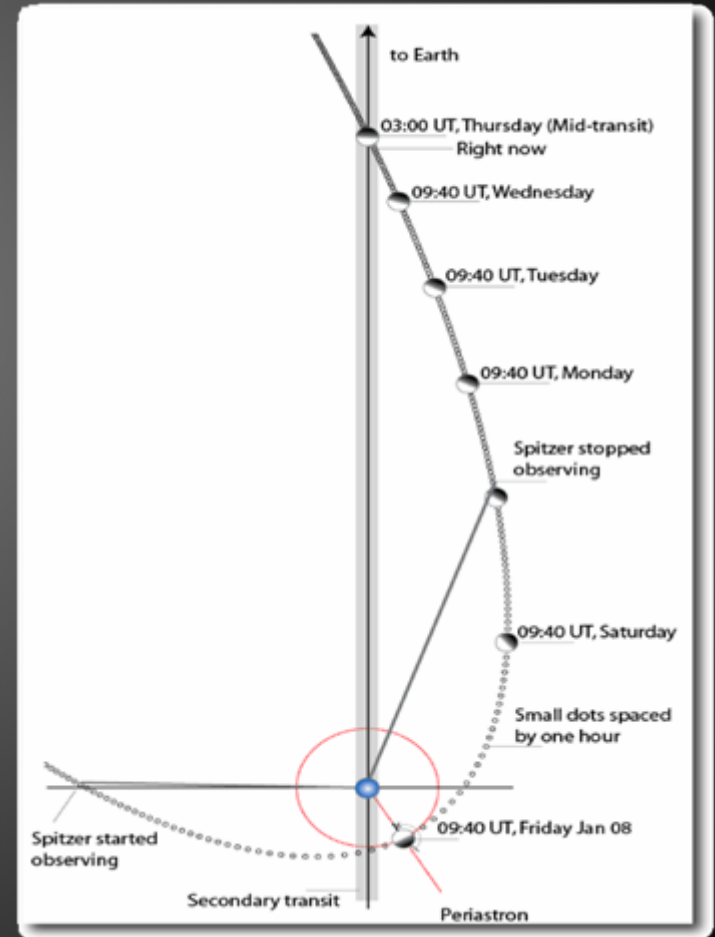


Eccentric Planets

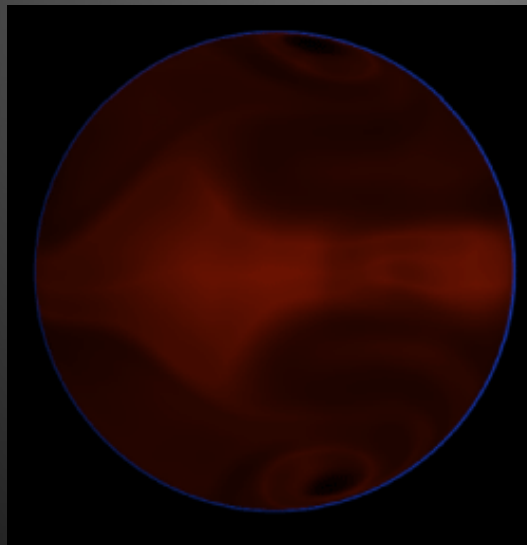


HD80606b

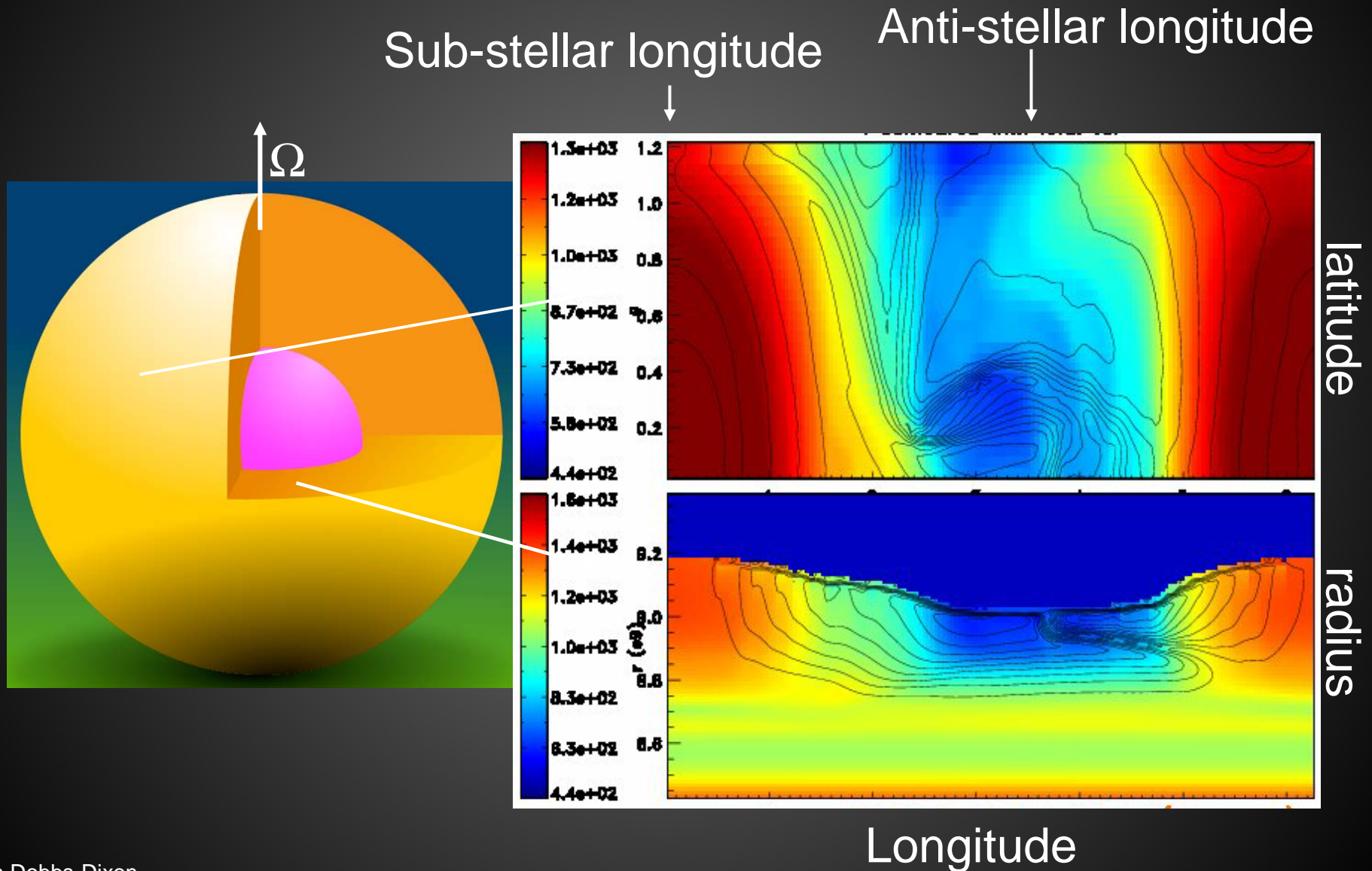
$P=111$ days, $e=0.9$



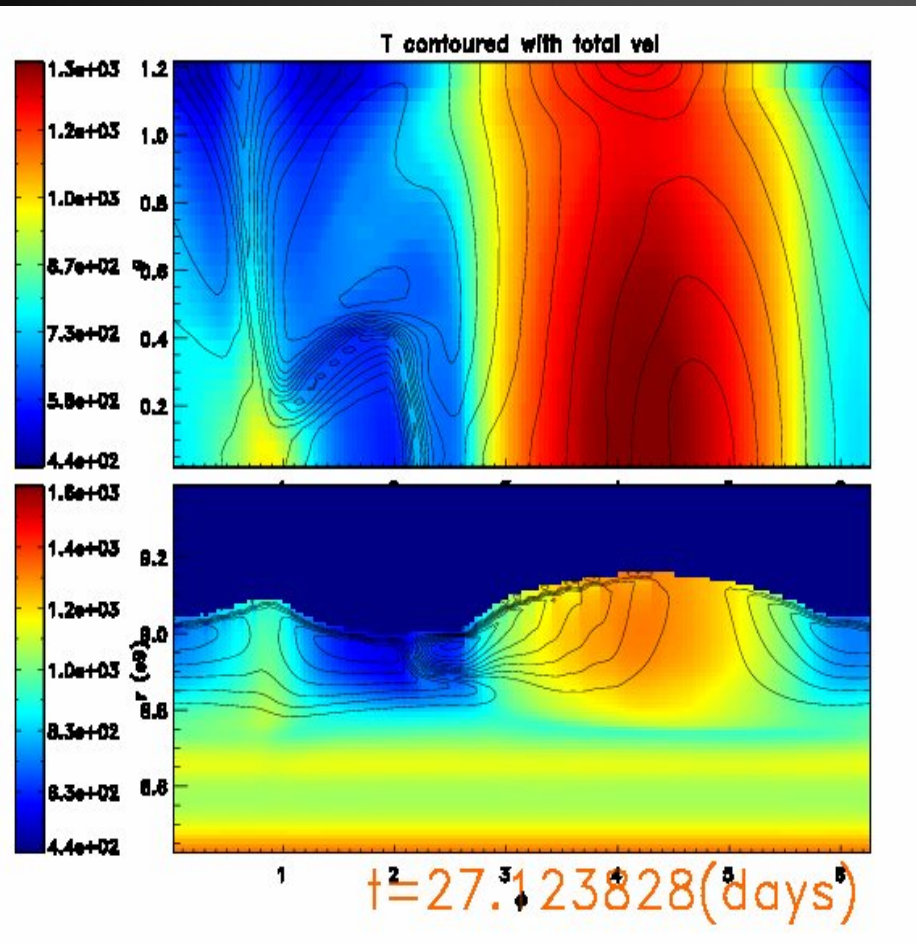
Langton and Laughlin



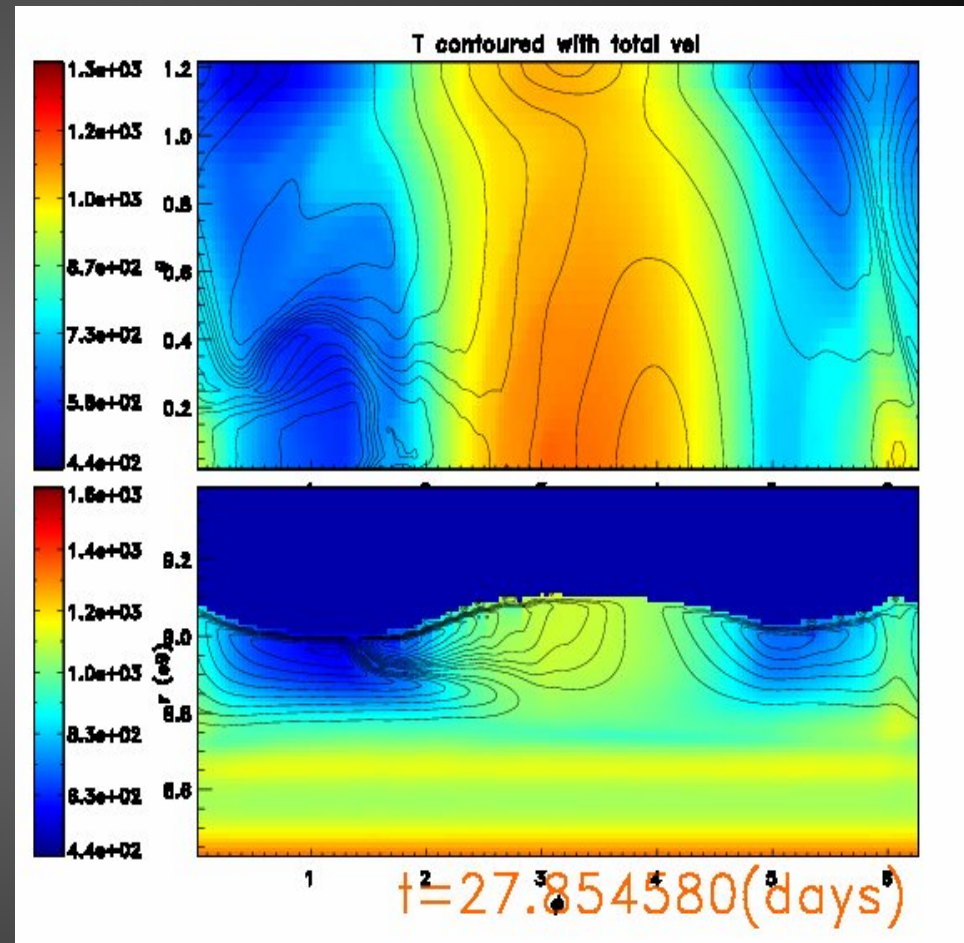
Eccentric Planets



Eccentric Planets ($e=0.5$)

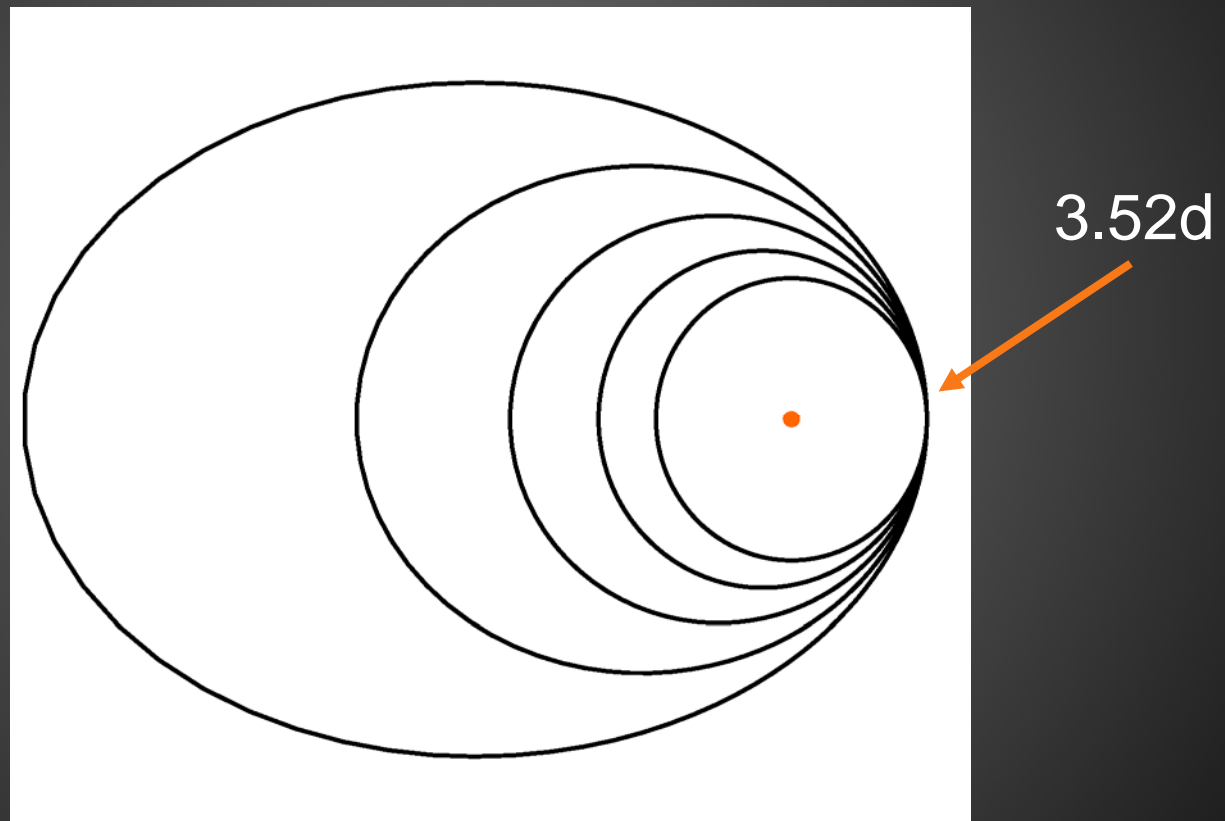


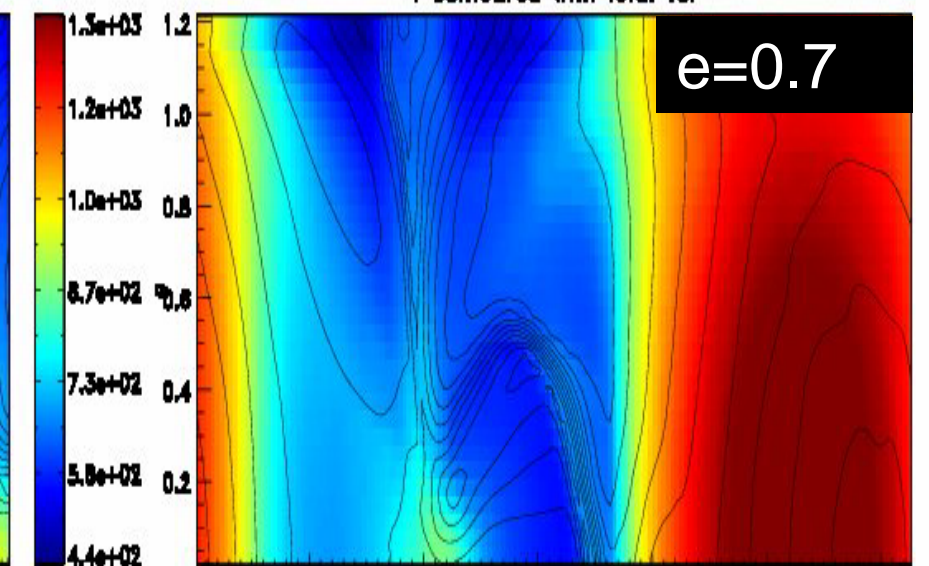
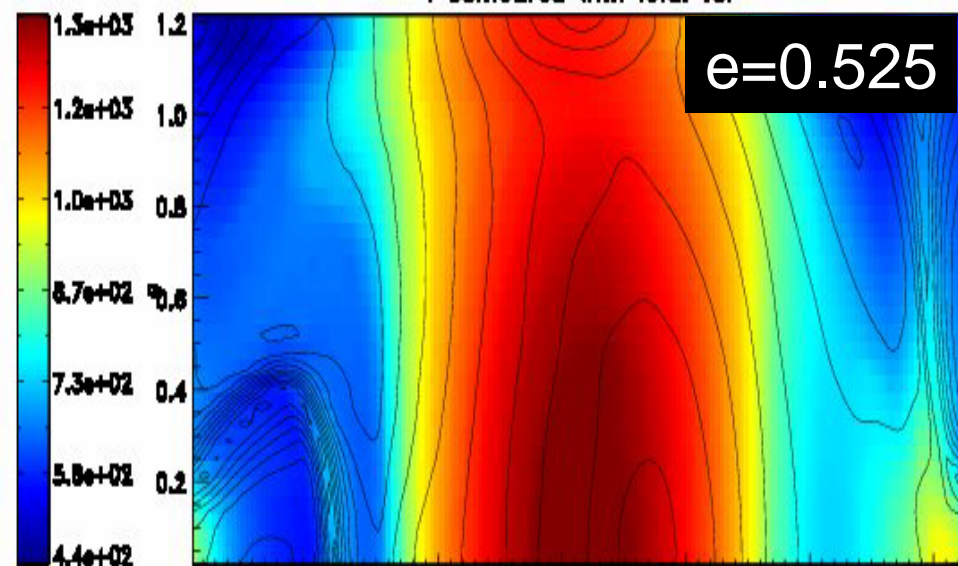
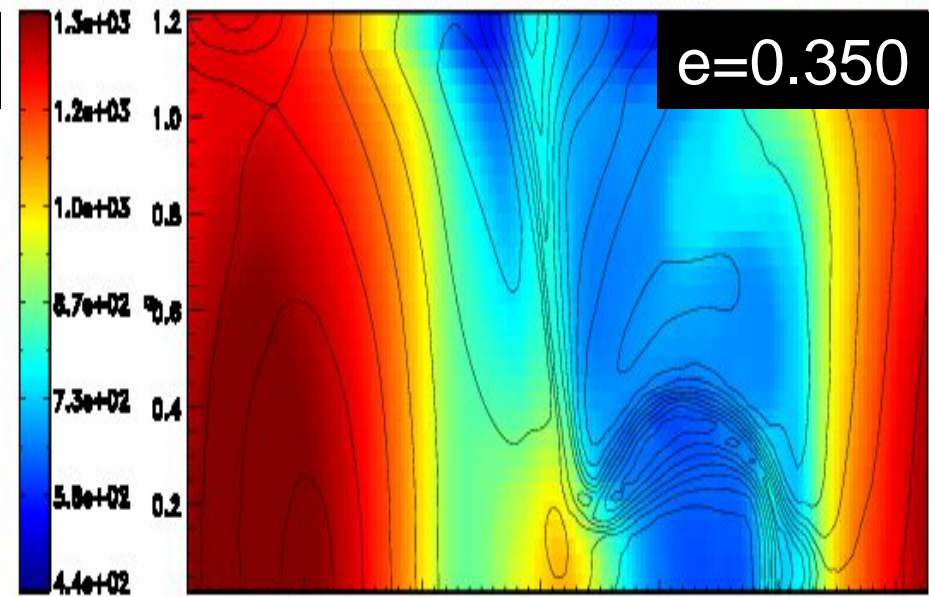
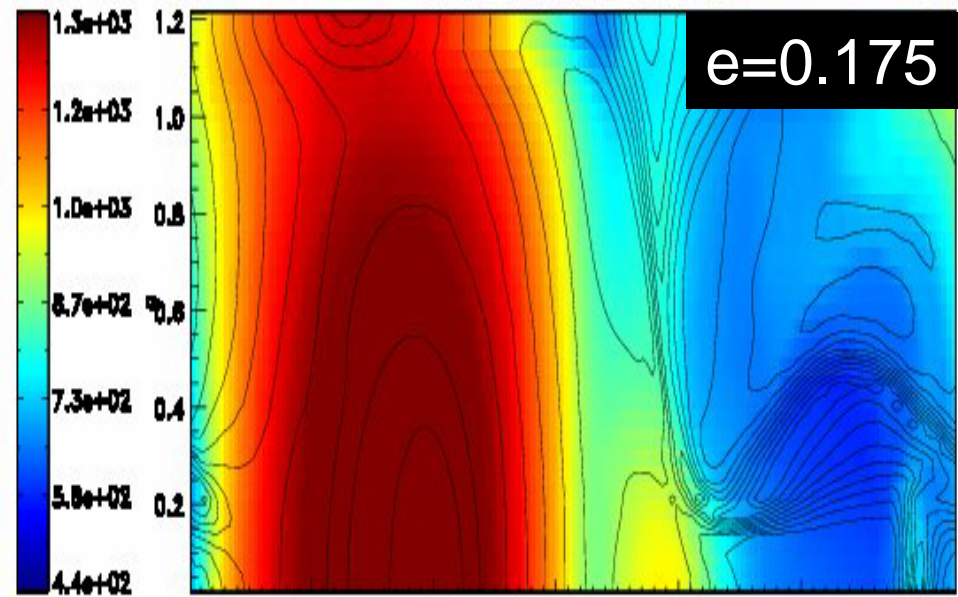
T_{peri}



$T_{\text{peri}} + 15\text{hr}$

Eccentric Planets





Conclusions

- Numerical treatment of radiation and dynamics must be included as coupled model.
- Three (pseudo) jets (one equatorial and two mid-lat.) are common features, with width decreasing with increased planetary rotation.
- Optical and IR opacities both are important in determining location of stellar energy deposition and efficiency of redistribution to the night-side.
- Changing viscosity drastically alters streamlines, changing overall thermal structure
- Caution must be exercised in regions where material passes through strong shocks. Radial velocity becomes very important
- Dynamically driven variability causes variations transit spectra, but variation in hemispherically averaged phase curves will be difficult.
- Differences between ingress and egress transmission spectra may prove to be powerful tools for model diagnostics.
- Continuing observational programs, and coupling of dynamical and spectral models should allow tighter constraints on dynamical processes: eccentric planets, multiple wavelength (and continuous) observations, lower masses, younger planets.