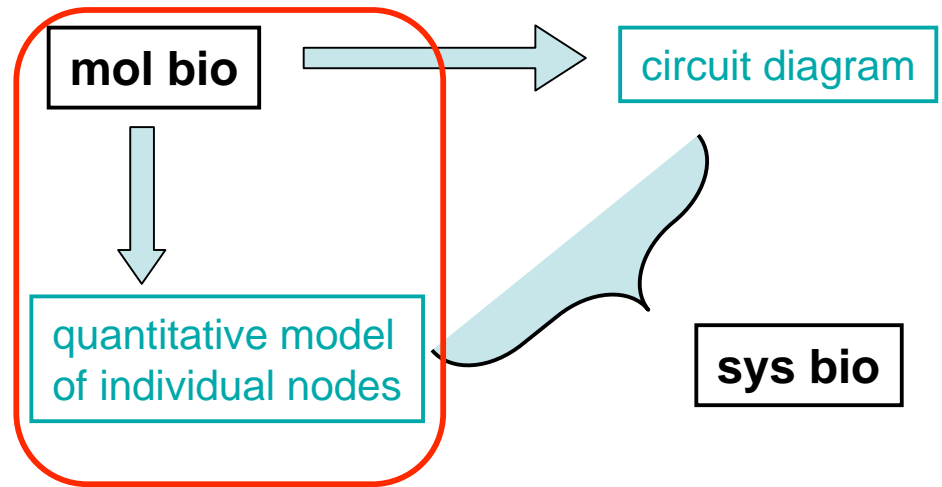


## Focus of our laboratory:

- **individual nodes** of gene network
- **quantitative** study of bacterial gene regulation
  - specificity and cross-talk in two-component signaling
  - combinatorial transcriptional control
  - translational control by small regulatory RNA
  - nonlinear proteolysis
- small regulatory circuits
- metabolic control and growth physiology
- synthetic genetic logic gates and circuits
- **directed evolution** of gene expression and regulation
- ➔ **from molecules to cellular physiology**





# Quantitative characterization of the *lac* promoter

## *lac* promoter of *E. coli*:

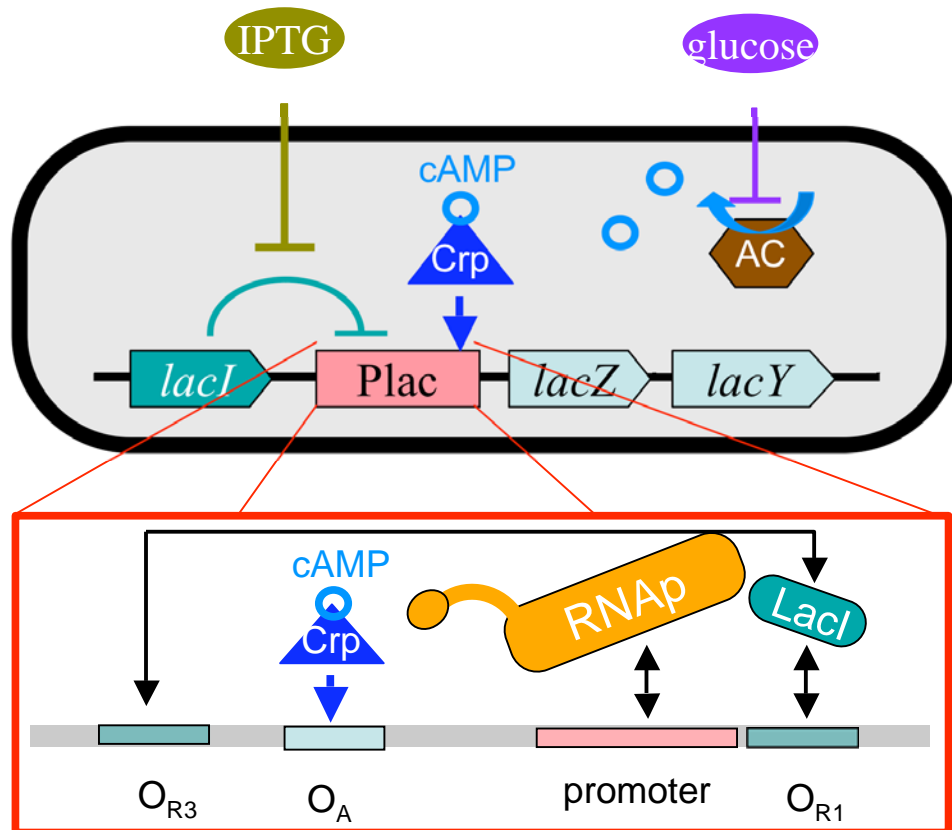
- best-studied system of molecular biology
  - all molecular components characterized
  - many mutants studied *in vivo*
  - most parameters measured *in vitro*
- exemplary model system of combinatorial gene regulation
  - involves activation, repression, and DNA looping

## Quantitative confrontation of model and experiment

- ➔ applicability of the thermodynamic description of tsx control?
- ➔ can the *in vivo* behavior of a system be understood in terms of its parts?

# Review of lactose utilization

- lac operon: pumps in lactose (LacY) and converts it to glucose (LacZ)
- lac promoter (Plac): **express Lac only when lactose is present and glucose is absent**



IPTG	glucose	expression
low	high	<b>OFF</b>
low	low	<b>OFF</b>
high	high	<b>OFF</b>
high	low	<b>ON</b>

## molecular ingredients:

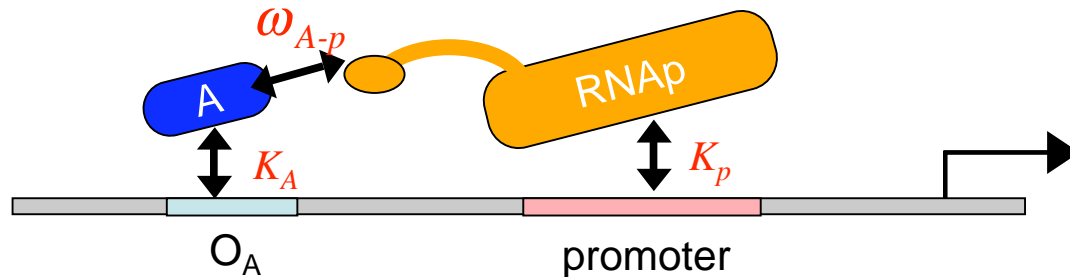
- specific protein-DNA binding
- protein-protein interaction
- protein-mediated DNA looping

→ theory: quantitative prediction of gene regulation by LacI, cAMP-Crp

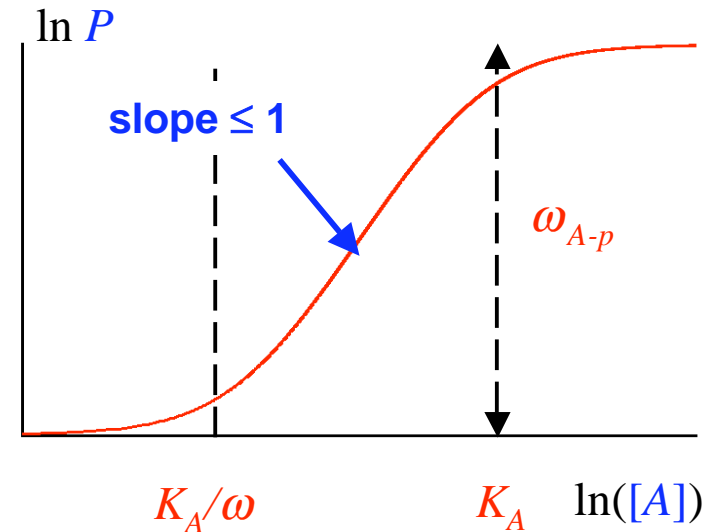
# Thermodynamic framework of gene regulation

[Shea & Ackers, JMB 1985]

gene expression  $\propto$  eq. promoter occupation probability  $P$  in the presence of A



$$P([A],[RNAP]) = \frac{W(0,1) + W(1,1)}{W(0,0) + W(0,1) + W(1,0) + W(1,1)}$$



define  $W(0,0)=1$ , then for activation

$$W(0,1) = [RNAP] / K_p, \quad W(1,0) = [A] / K_A$$

$$W(1,1) = \omega_{A-p} \cdot ([A] / K_A) \cdot ([RNAP] / K_p)$$

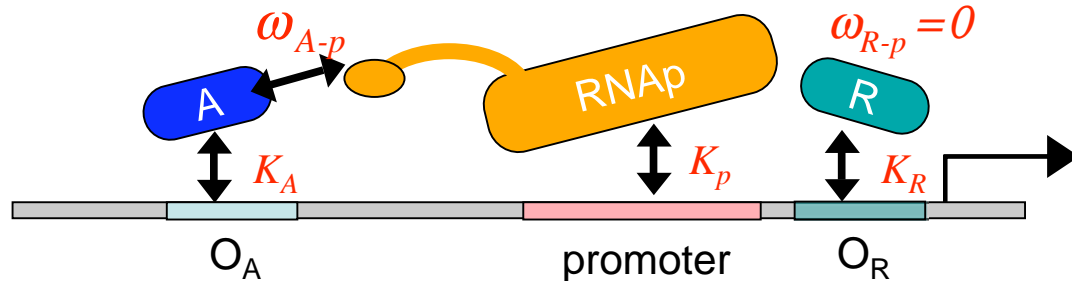
$$P \approx \frac{[RNAP]}{K_p} \cdot \frac{1 + \omega_{A-p} [A] / K_A}{1 + [A] / K_A}$$

(for typical weak promoters)

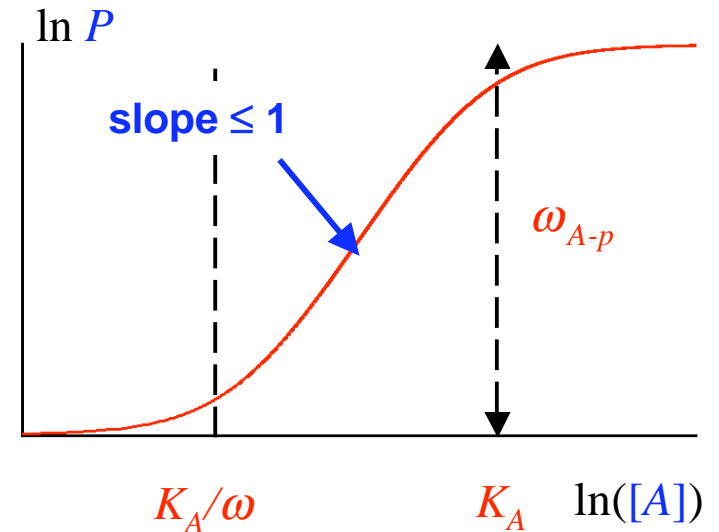
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$$W(0,1) = [RNAP] / K_p, \quad W(1,0) = [A] / K_A$$

$$W(1,1) = \omega_{A-p} \cdot ([A] / K_A) \cdot ([RNAP] / K_p)$$

$$P \approx \frac{[RNAP]}{K_p} \cdot \frac{1 + \omega_{A-p} [A] / K_A}{1 + [A] / K_A}$$

(for typical weak promoters)

for repression,  $W(1,1)=0$

$$P \approx \frac{[RNAP]}{K_p} \cdot \frac{1}{1 + [R] / K_R}$$

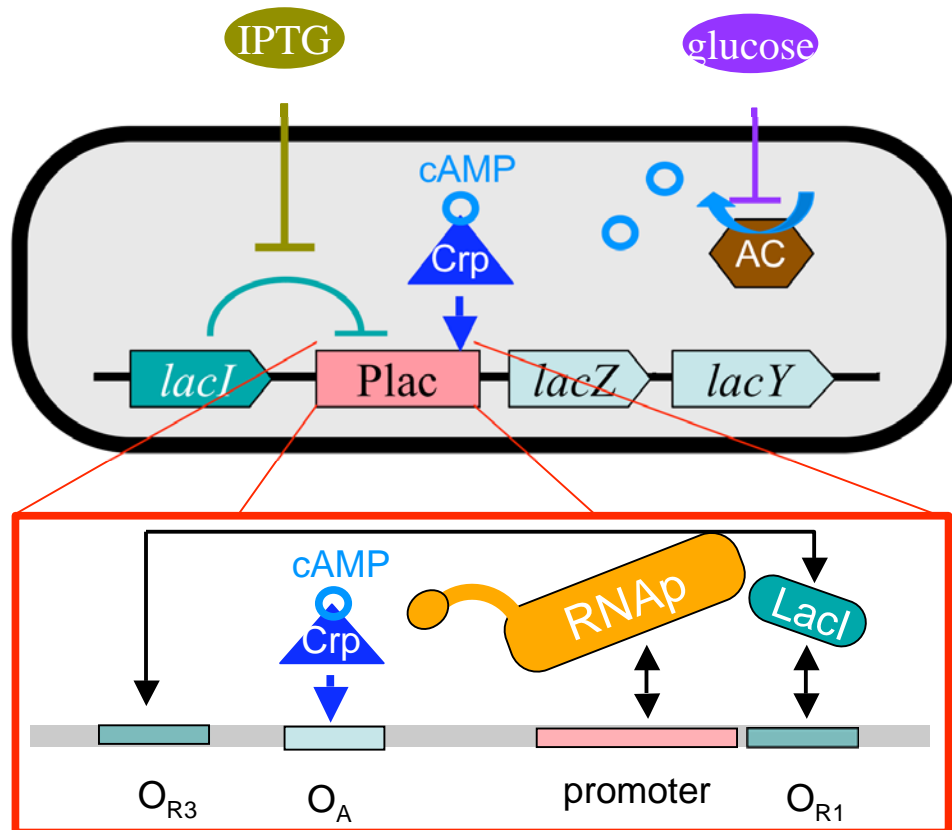
**co-regulation**

multiplicative

$$P \propto \frac{1 + \omega_{A-p} [A] / K_A}{1 + [A] / K_A} \cdot \frac{1}{1 + [R] / K_R}$$

# Review of lactose utilization

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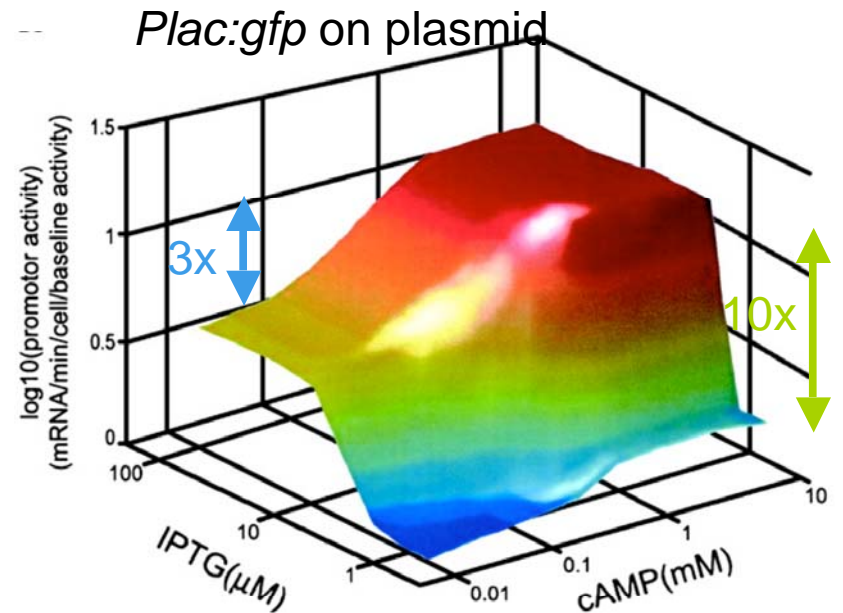
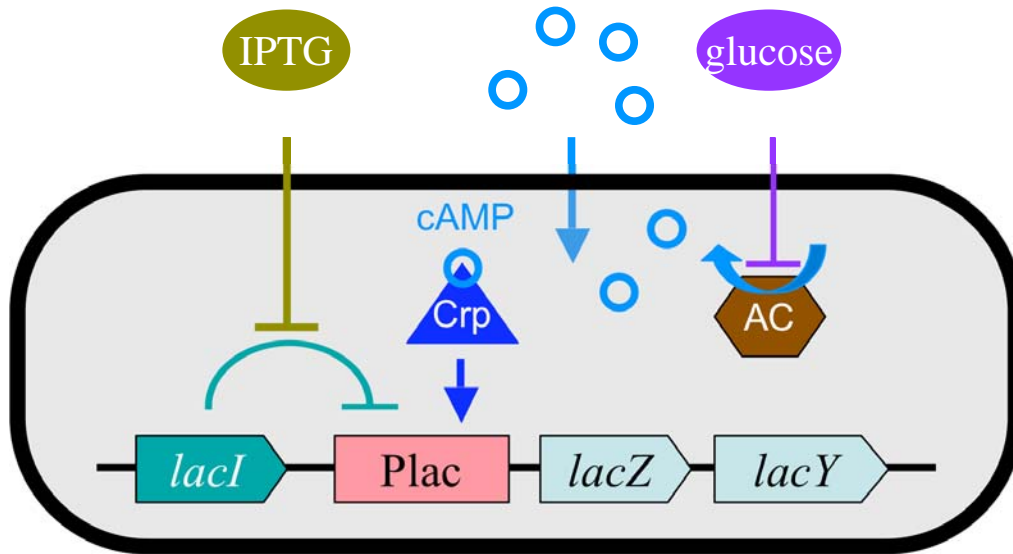
IPTG	glucose	expression
low	high	<b>OFF</b>
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high	low	<b>ON</b>

## molecular ingredients:

- specific protein-DNA binding
- protein-protein interaction
- protein-mediated DNA looping

- ➔ theory: quantitative prediction of gene regulation by LacI, cAMP-Crp
- ➔ expt: characterize **LacZ activity** for different levels of regulatory proteins
  - control protein levels by varying the inducers (IPTG and cAMP)

# Quantitative characterization



Previous expt: [Setty et al, PNAS, 2003]

Grow cells in medium with glucose, cAMP, IPTG

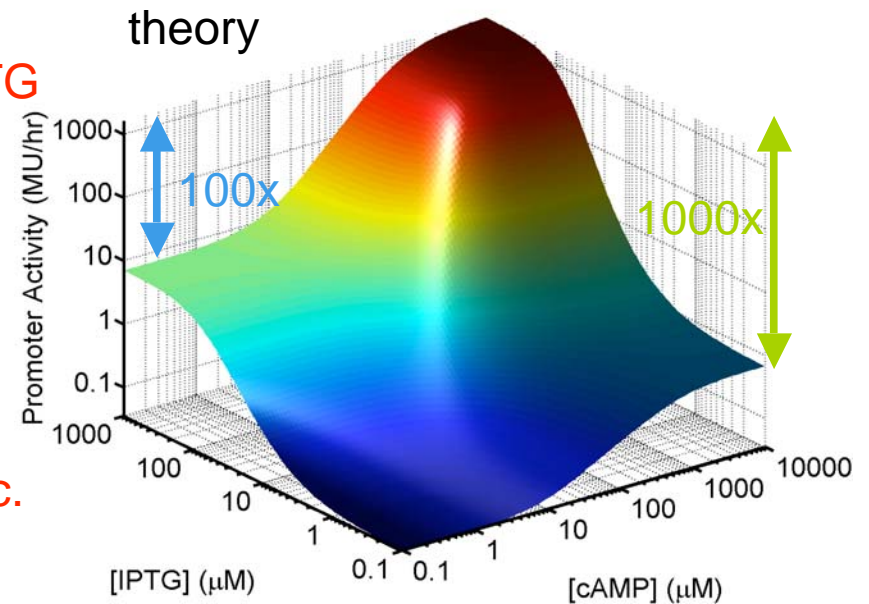
-- use glucose to suppress cAMP synthesis

-- control cAMP-level extracellularly

inconsistent with behavior of mutants:

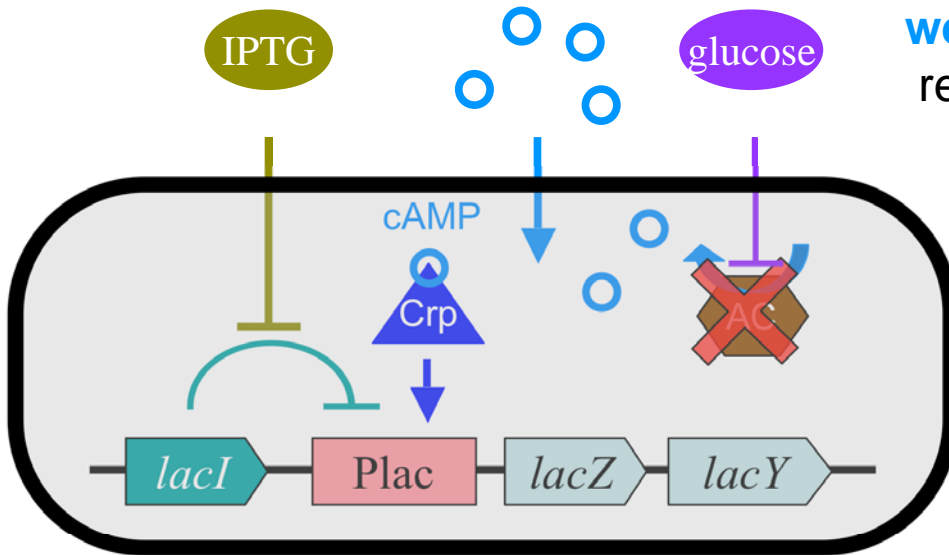
$\Delta lacI$ : > 1000x;  $\Delta crp$  > 50x

→ possible problems: complex links between extracellular and intracellular inducer conc.





# Quantitative characterization of mutants

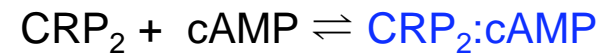


**weak cAMP dependence:** glucose-mediated repression of AC activity may be incomplete

- delete ***cyaA*** gene (encoding **AC**)
- find ~100x change in LacZ activity
- **Hill coeff**  $\approx 2$

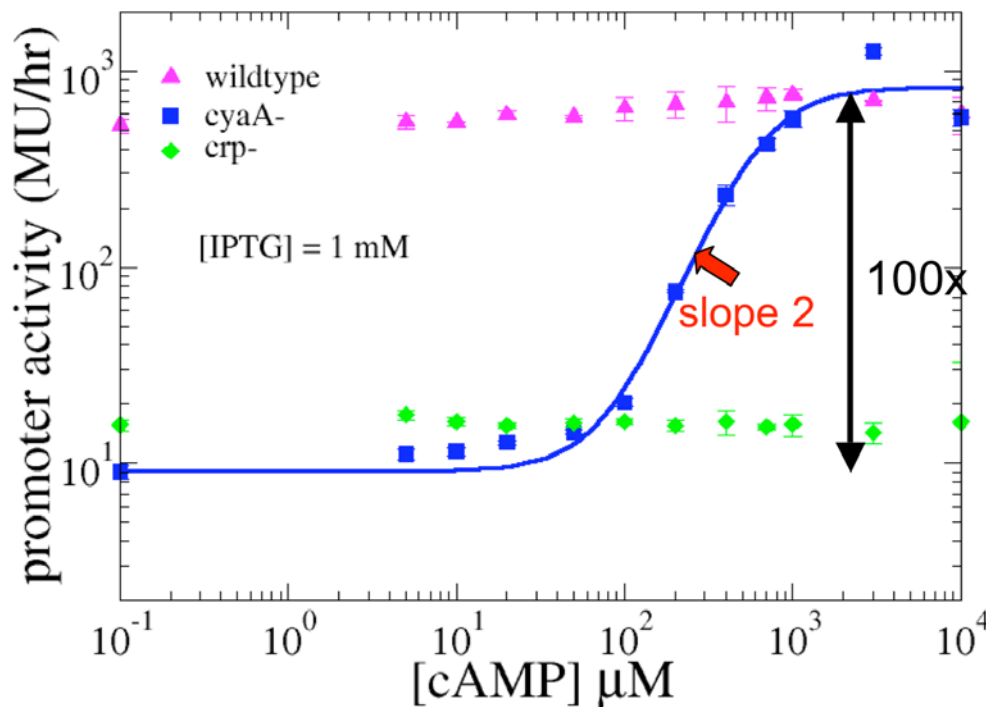
incompatible w/ biochem and thermodynamic model of tsx control

CRP dimer activated by binding of **single** cAMP molecule

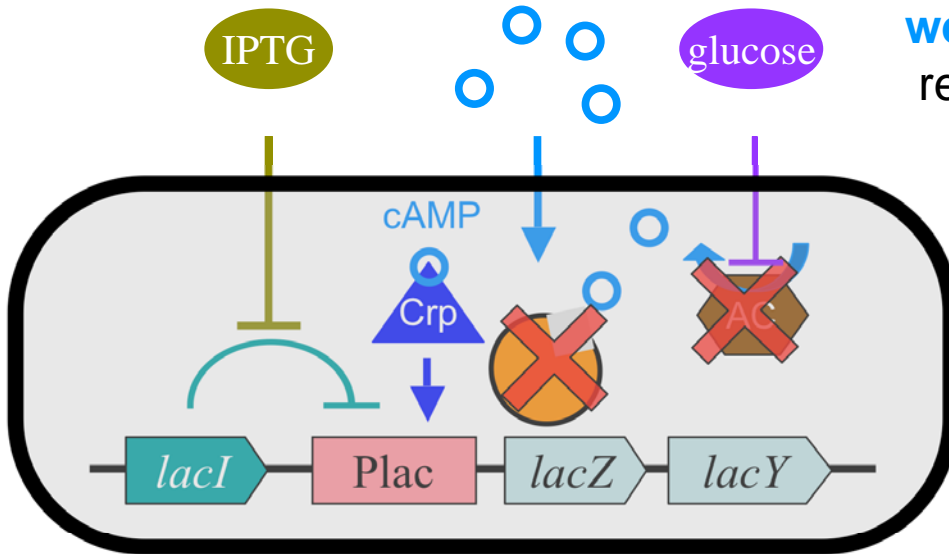


(expect Hill coeff = 1)

*in vitro* biochem irrelevant?  
other effects exerted by CRP-cAMP?



# Quantitative characterization of mutants

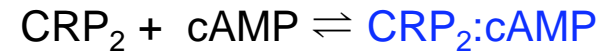


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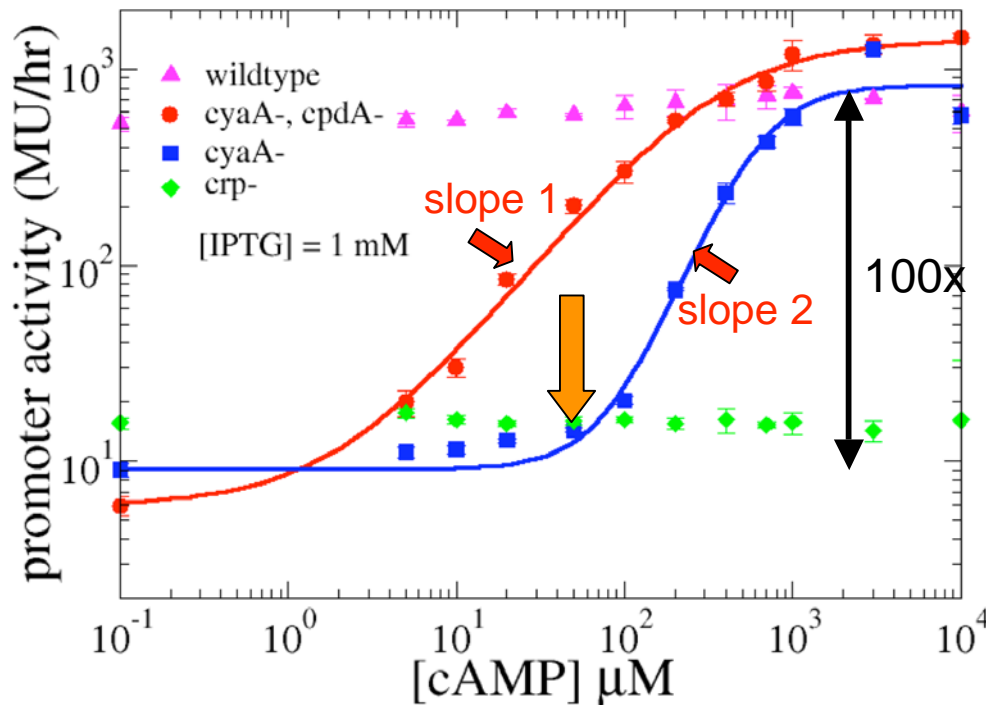


(expect Hill coeff = 1)

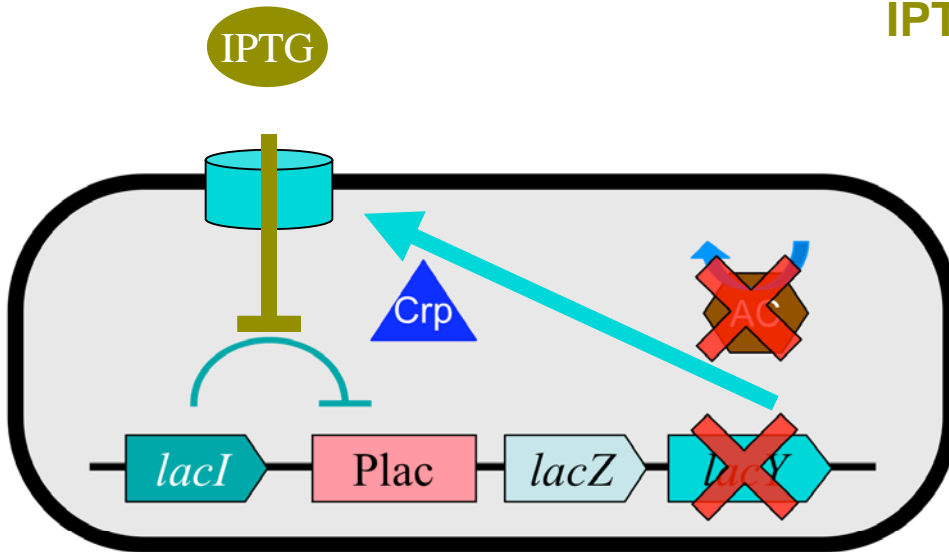
*in vitro* biochem irrelevant?

other effects exerted by CRP-cAMP?

- cAMP degraded by **PDE** (*cpdA*)
- effect of *cpdA* deletion?
- Hill coeff  $\approx 1$ , agrees with model
- role of **PDE**: no known phenotype
- mechanism of cooperativity?



# Quantitative characterization of mutants



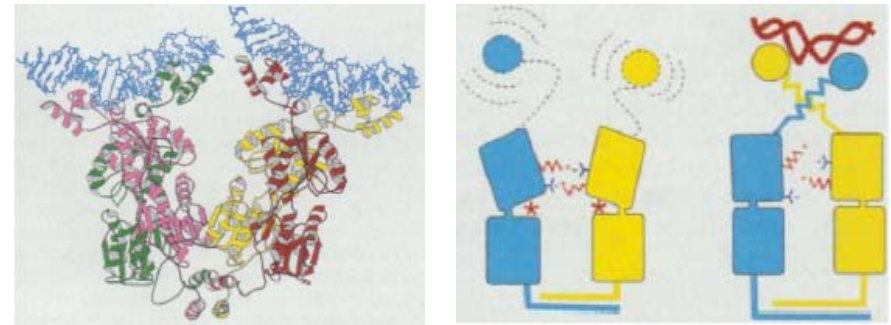
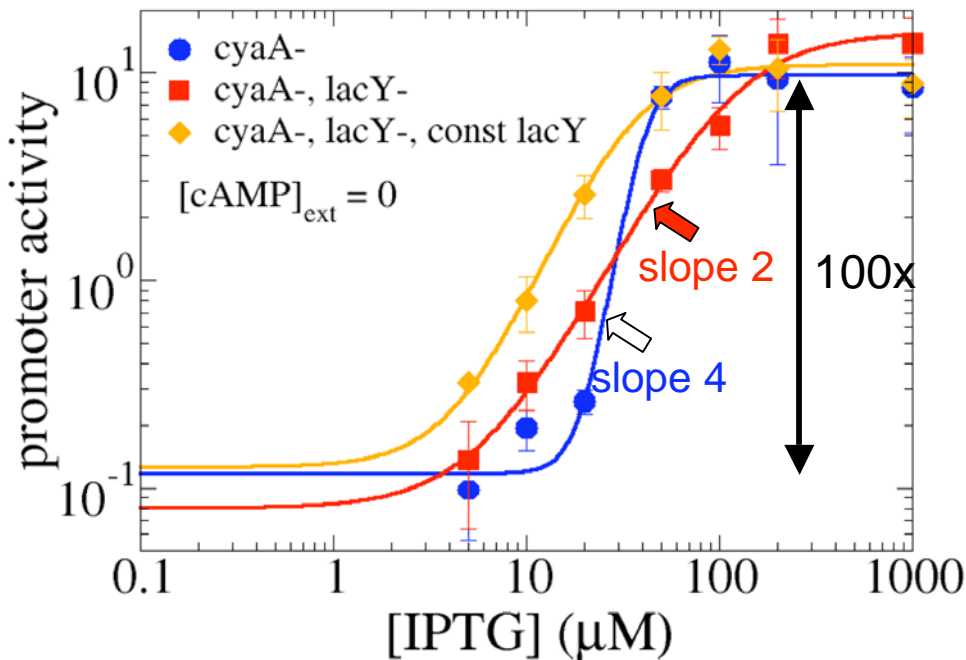
**IPTG dependence:** *cyaA*<sup>-</sup> cells with [cAMP]=0

→ very cooperative! (Hill coeff  $\approx 4$ )

→ delete *lacY* Hill coeff  $\approx 2$

→ constitutive expression of LacY  
only shifted IPTG dependence

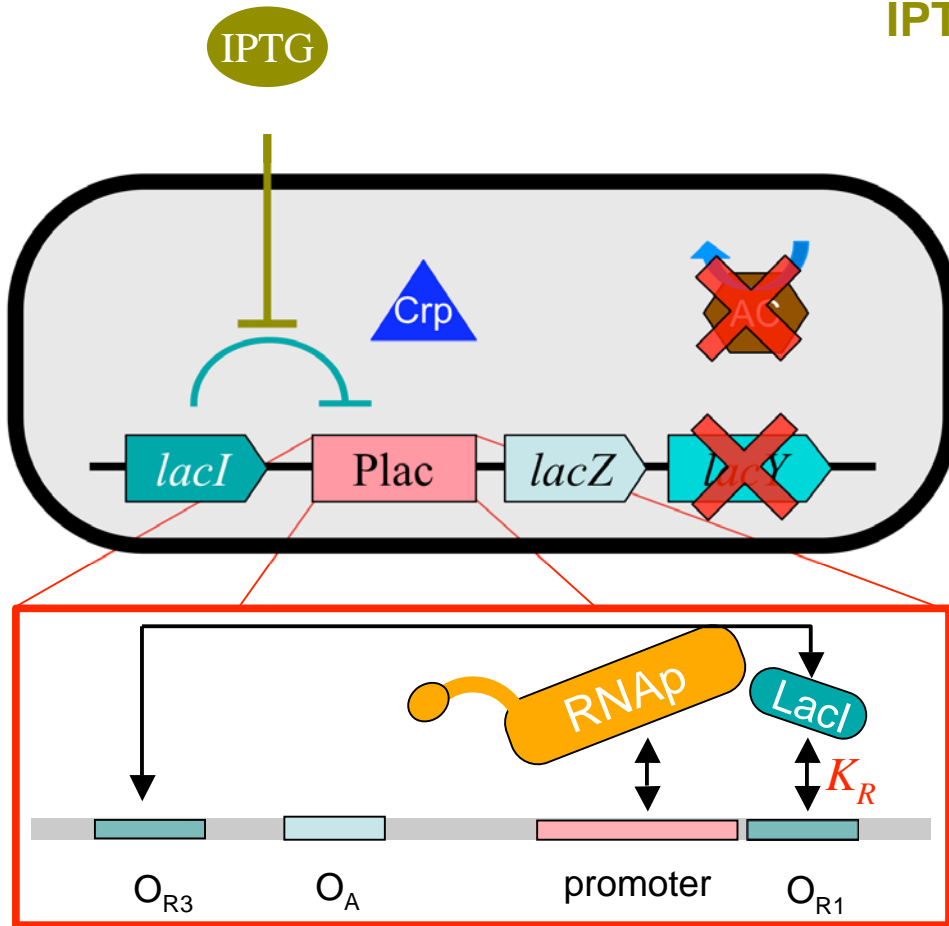
→ Hill coeff = 2 widely cited in literature



- LacI forms tetramer (dimer of dimers)
- strong coupling within each dimer and weak coupling between dimers

**but...** Hill coeff = 2 is one of the many **pseudo-facts** regarding Lac

# Quantitative characterization of mutants



auxiliary Lac operators stabilize  
LacI-O1 binding via **DNA looping** [Muller-Hill]

**IPTG dependence:** *cyaA*- cells with [cAMP]=0

→ very cooperative!

- LacI forms tetramer (dimer of dimers)
- strong coupling within each dimer and weak coupling between dimers

- LacI<sub>4</sub>-IPTG binding **non-cooperative**



- **weakly cooperative** in the presence of operator DNA (**Hill coeff = 1.4 ~ 1.6**)

[Matthews lab, '85]

→ **neither** monomers of LacI dimer can bind IPTG for specific binding to Lac ops

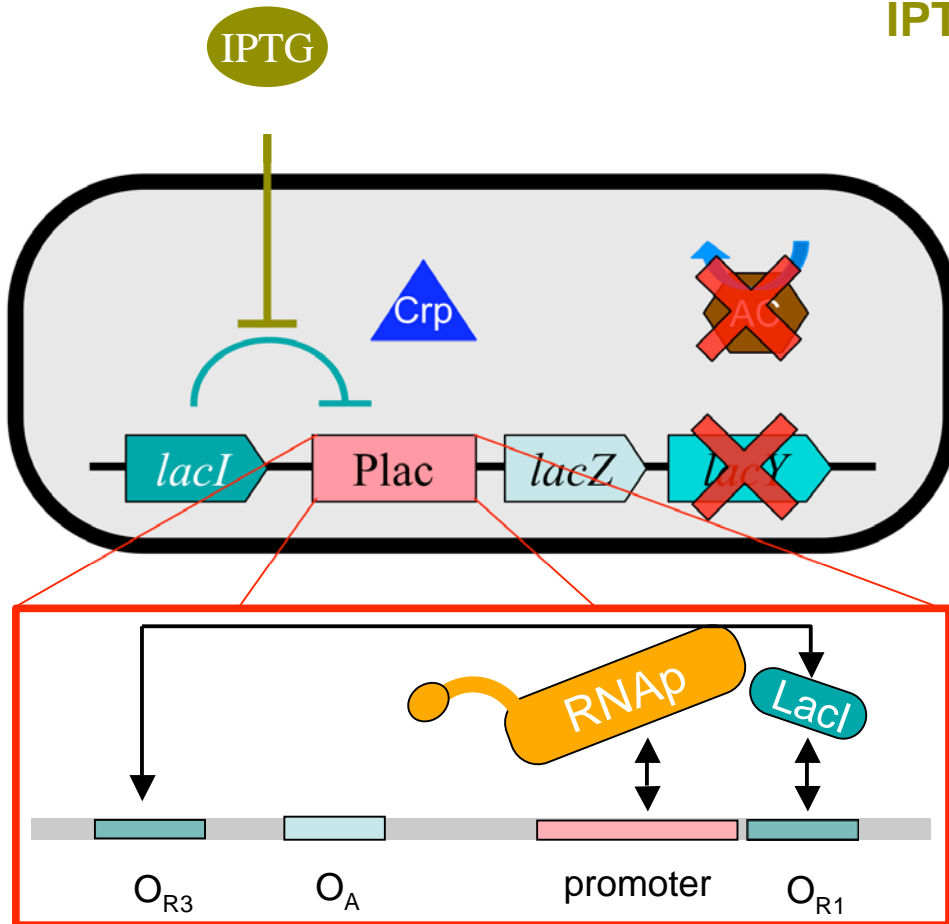
active repressors

$$[R] = \frac{2 \cdot [\text{LacI}_4]_{\text{total}}}{(1 + [\text{IPTG}] / K_{\text{IPTG}})^2}$$

simple repression

$$\text{tsx activity} \propto \frac{1}{1 + [R] / K_R}$$

# Quantitative characterization of mutants



**IPTG dependence:** *cyaA*- cells with [cAMP]=0

→ very cooperative!

- LacI forms tetramer (dimer of dimers)
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→ **neither** monomers of LacI dimer can bind IPTG for specific binding to Lac ops

$$\text{active repressors } [R] = \frac{2 \cdot [\text{LacI}_4]_{\text{total}}}{\left(1 + [\text{IPTG}] / K_{\text{IPTG}}\right)^2}$$

$$\text{simple repression tsx activity} \propto \frac{1}{1 + [R] / K_R}$$

- include DNA looping in model

$$[R] \rightarrow [R] + \frac{\mathcal{L}_o \cdot [\text{LacI}_4]_{\text{total}}}{\left(1 + [\text{IPTG}] / K_{\text{IPTG}}\right)^4}$$

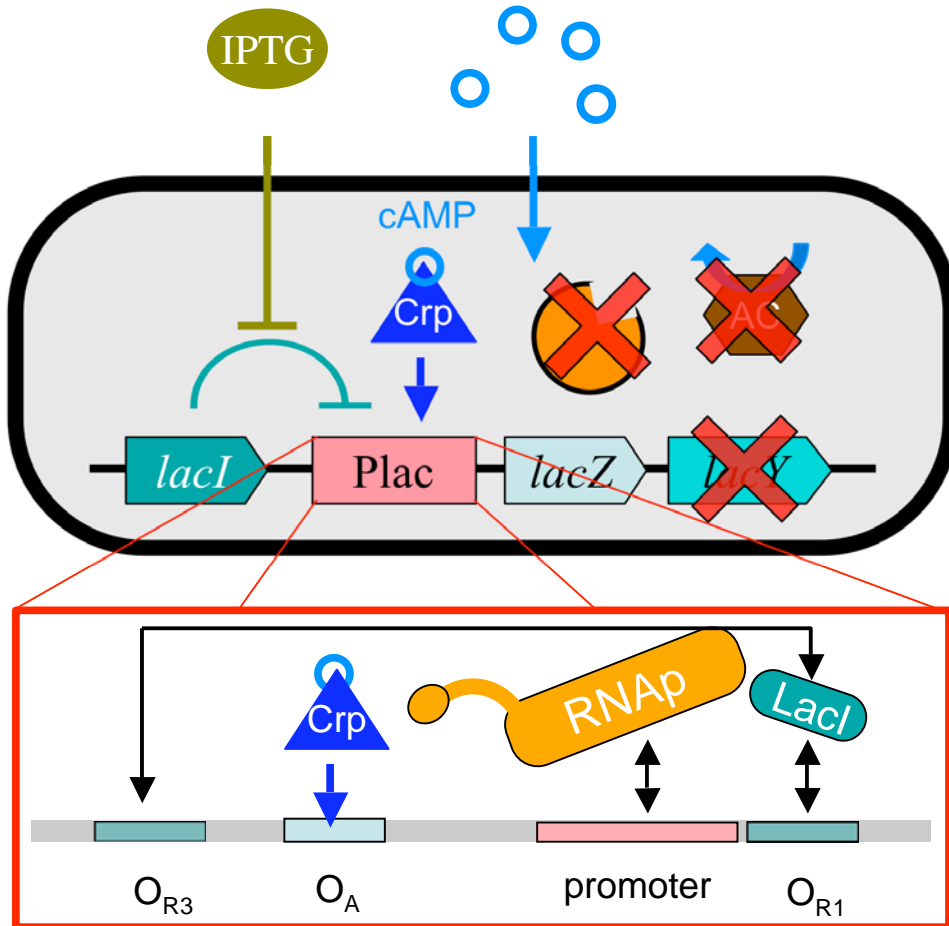
$\mathcal{L}_o$ : local increase of [LacI] due to looping

auxiliary Lac operators stabilize LacI-O1 binding via **DNA looping** [Muller-Hill]

- increase fold-repression by  $\mathcal{L}_o$ -fold
- effective Hill coeff (1.5 ~ 3) depends on  $\mathcal{L}_o$

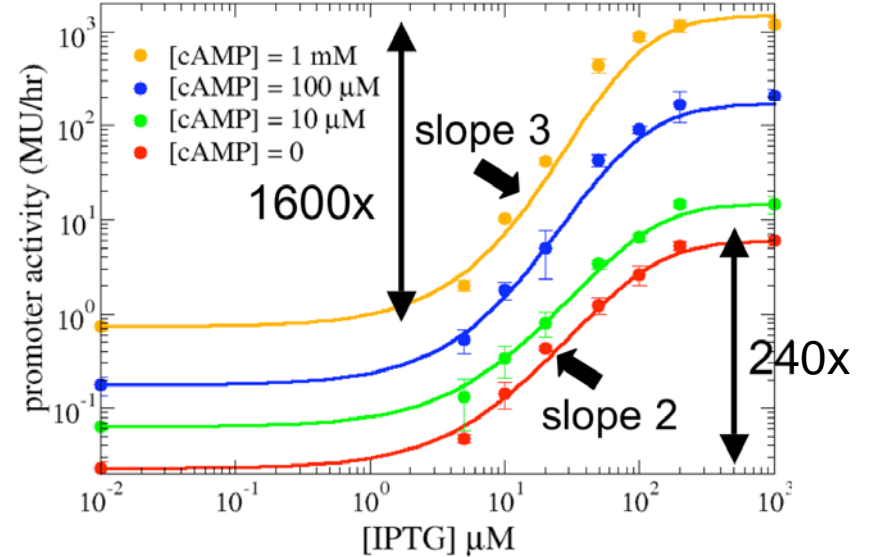
but value of  $\mathcal{L}_o$  not known independently

# Quantitative characterization of mutants

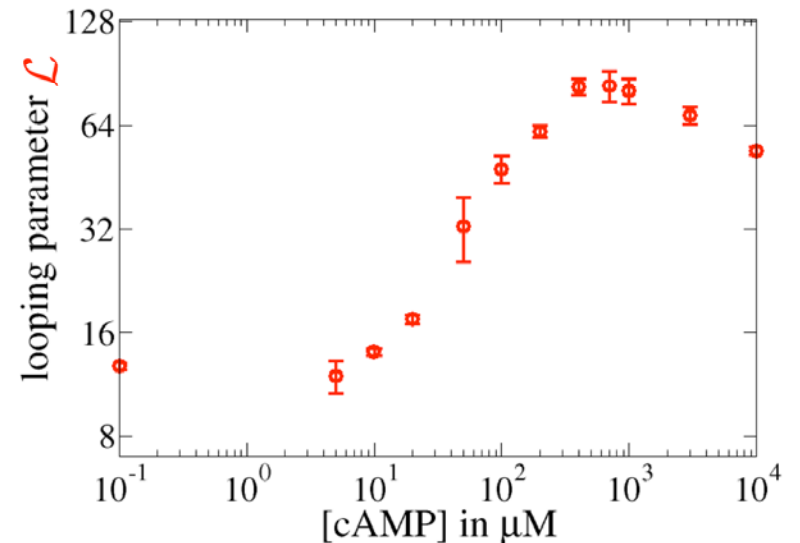


auxiliary Lac operators stabilize  
LacI-*O<sub>1</sub>* binding via **DNA looping** [Muller-Hill]  
 → increase fold-repression by  $\mathcal{L}_0$ -fold  
 → effective Hill coeff (1.5 ~ 3) depends on  $\mathcal{L}_0$   
 but value of  $\mathcal{L}_0$  not known independently

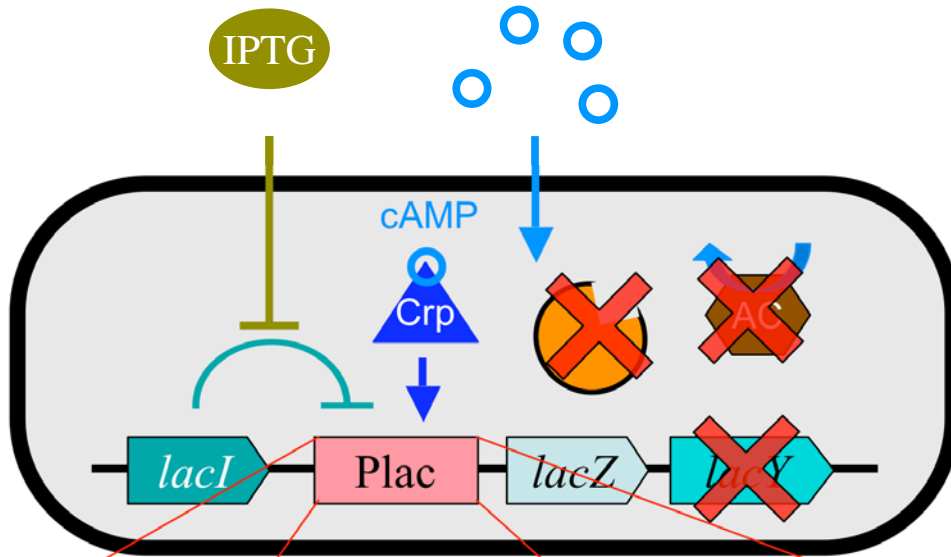
looping model w/  $\mathcal{L}_0 \approx 12$ ,  $2[\text{LacI}_4]/K_R = 20$



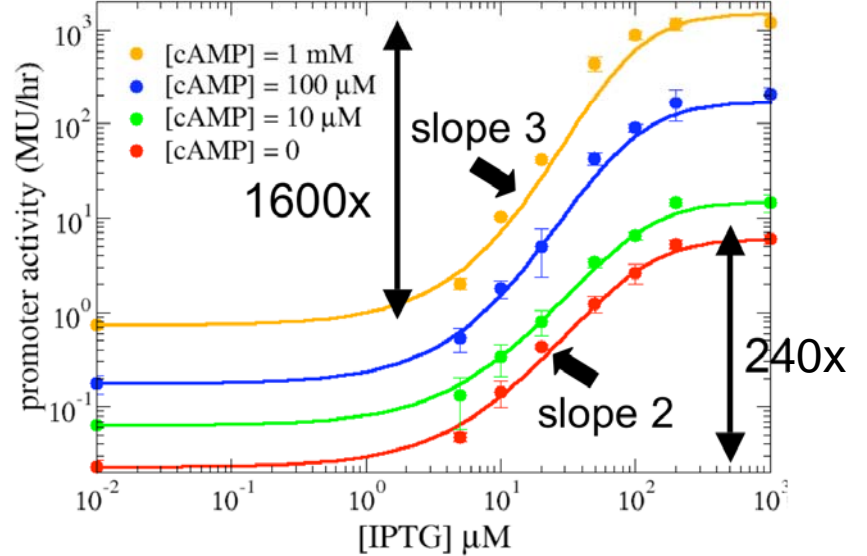
→ single parameter  $\mathcal{L}_0$  fits both  
fold-repression and slope



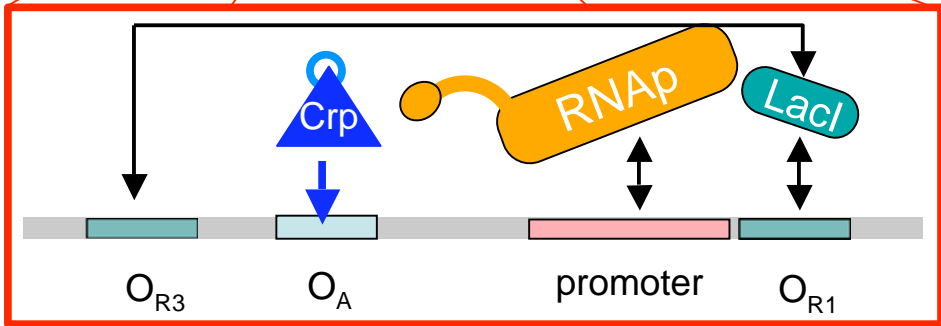
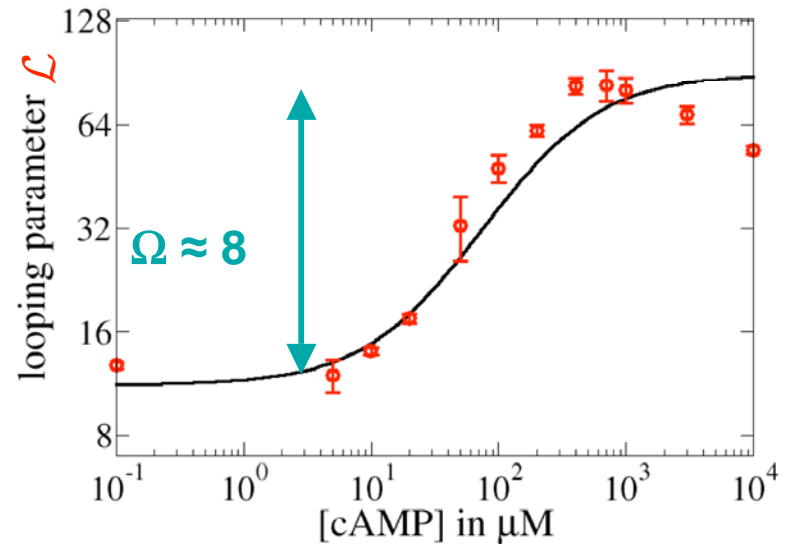
# Quantitative characterization of mutants



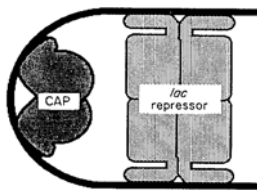
looping model w/  $\mathcal{L}_0 \approx 12$ ,  $2[\text{LacI}_4]/K_R = 20$



→ single parameter  $\mathcal{L}_0$  fits both fold-repression and slope



## Crp-dependence of DNA looping



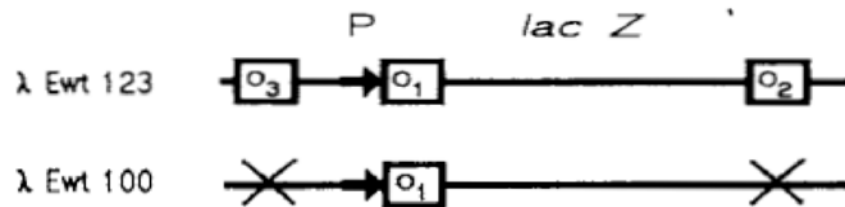
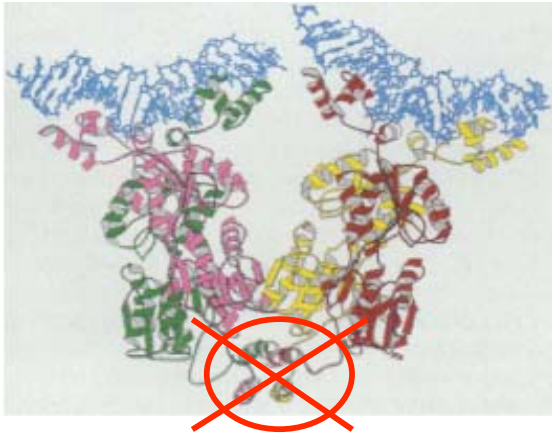
Fried et al, 84;  
Balaeff et al, 04

*in vitro* study found coop. factor  $\Omega = 4 \sim 12$

# Direct probe of DNA looping *in vivo*

Use dimeric LacI mutant

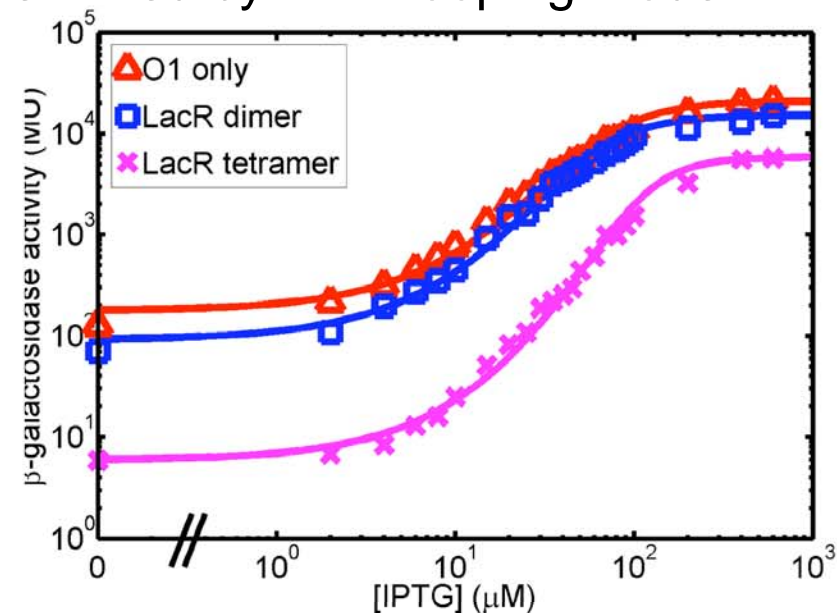
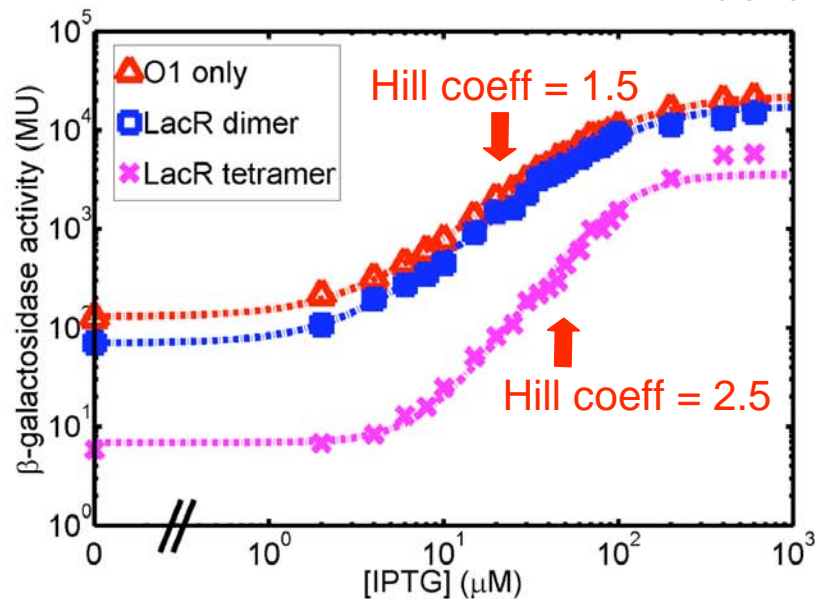
remove auxiliary operators



→ cooperativity in IPTG response requires DNA looping (Lac tetramer + auxiliary ops)

[Oehler & Muller-Hill, 06]

data well-fitted by DNA looping model

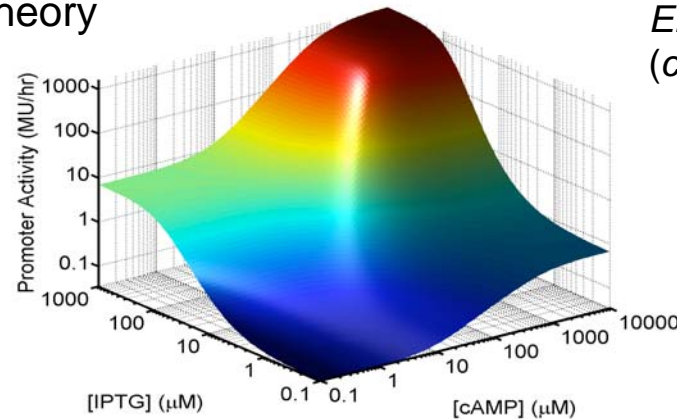


→ IPTG-LacI-operator interaction same as *in vitro*

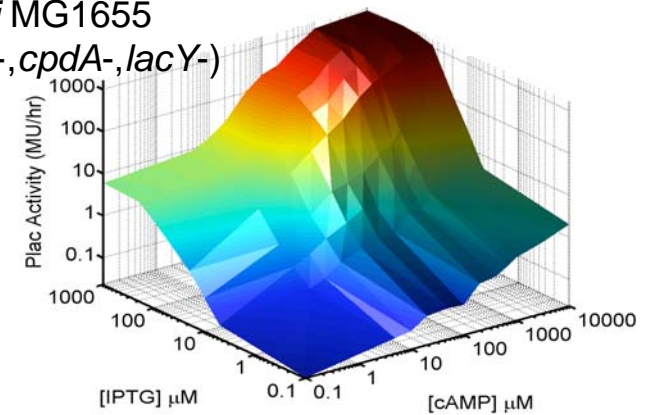


# Summary

theory



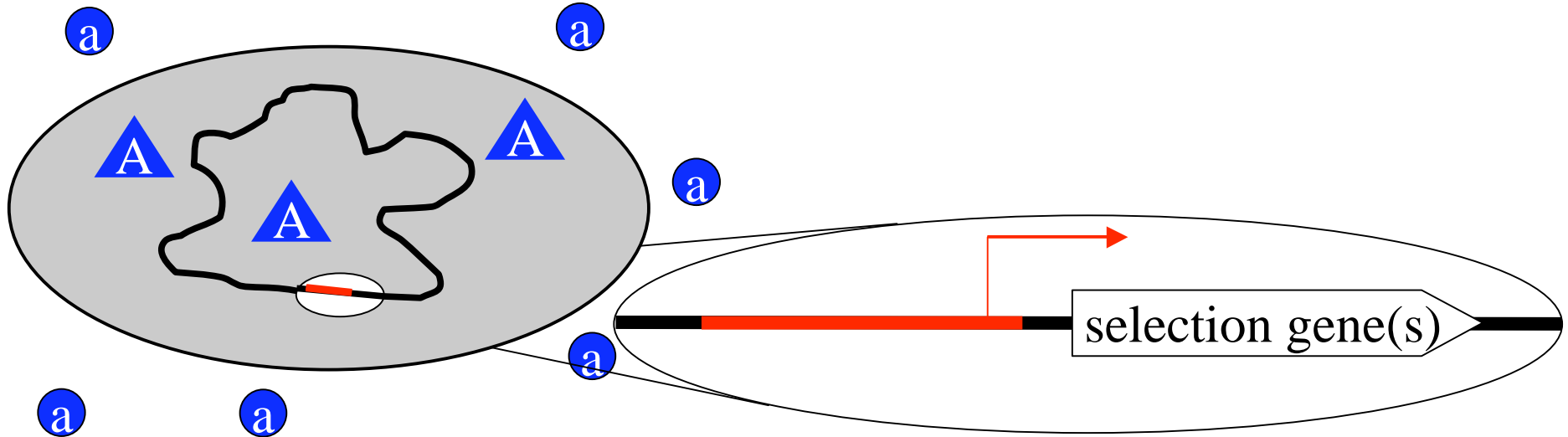
*E. coli* MG1655  
(*cyaA*<sup>-</sup>, *cpdA*<sup>-</sup>, *lacY*<sup>-</sup>)



- **main findings for the *lac* promoter:**
  - Crp enhances DNA looping
  - abrupt IPTG response despite non-cooperative LacI-IPTG interaction;  
→ **suggests physiological role of Crp-cAMP as enhancer of repression**
  - mechanism of Crp-LacI interaction?
  - coop cAMP response due to PDE; physiological function? mechanism?
- **general lessons for quantitative systems biology:**
  - hidden interaction abound even for the “best studied” system
  - pseudo-facts abound even for the best known components
  - quantitative description of *in vivo* biology is possible
  - need **solid, qualitative** knowledge of the components (e.g., Hill coeff)
  - **(semi) quantitative** characterization generates spectrum of phenotypes
  - provides clues for identifying unknown components and mechanisms
  - provides phenomenological description of Plac for high-level studies

# *de novo* evolution of regulatory sequences

want gene expression only in the presence of inducer “a”



Steady level of regulatory protein **A**

e.g, **inverter gate**

TF activation controlled thru inducer **a**

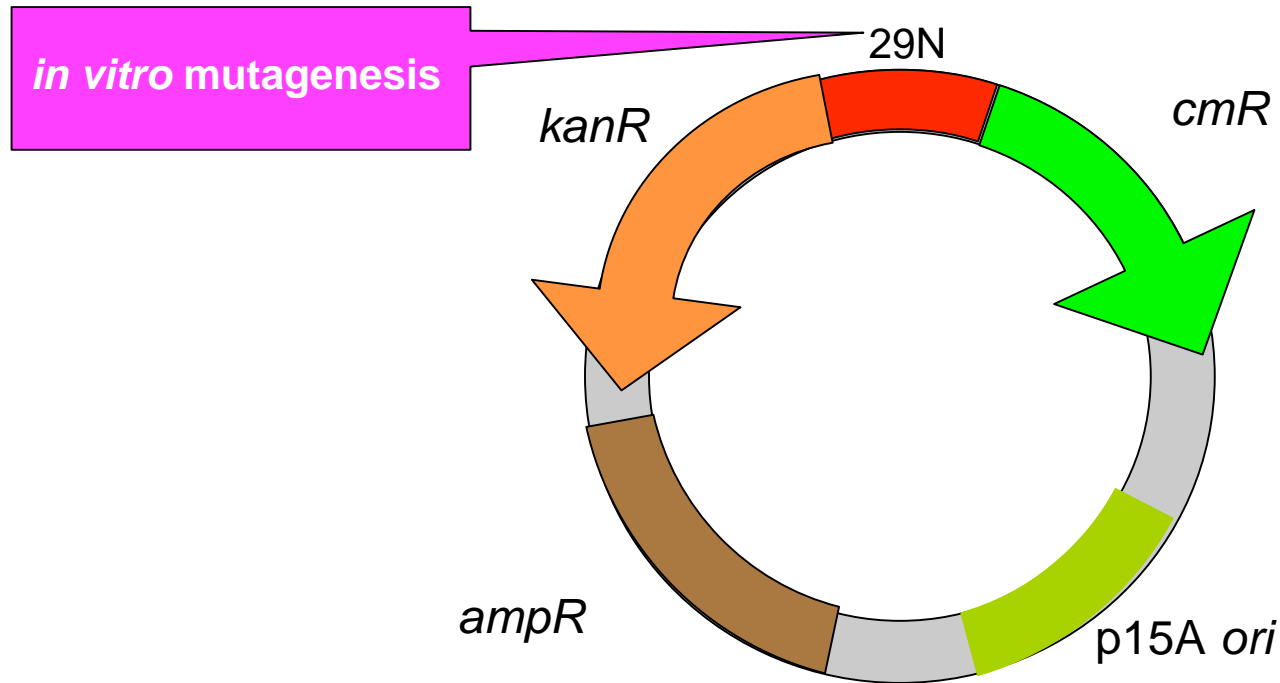
Selectable output:

- gene product **lethal** if **drug 1** present
- gene product **essential** if **drug 2** present

[a]	drug	gene
lo	1	<b>OFF</b>
hi	2	<b>ON</b>

**Defined region** of mutagenesis

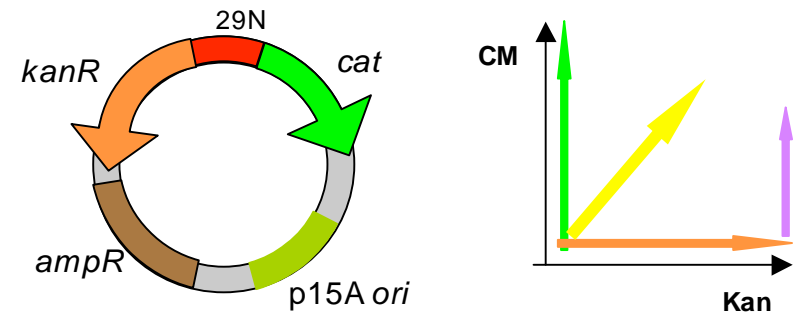
# Directed evolution of **core promoters**



- evolve promoters from random sequences  
in a tight space (29 nt) using **mutagenic PCR**
- **select** for cells with increasing resistant to Cm
- expect two variants of the  $\sigma^{70}$  core promoter:
  - 10/-35 hexamers: **TTGACA**<-- 17nt -->**TATAAT**
  - extended -10: **TGTGNTATAAT**
- two selection genes: **divergent overlapping promoters** possible?
- dependence on evolutionary path?

# Evolution procedure

- initial
  - initial population: **random library** of 29mer ligated into selection plasmid
  - transform plasmid in *E. coli* (TOP10) cells; transformation efficiency **~10<sup>4</sup> indept clones**



- **selection**

- grow on plates with various drug conc ( CM and/or kan )
- collect several hundred clones with the highest drug resistance

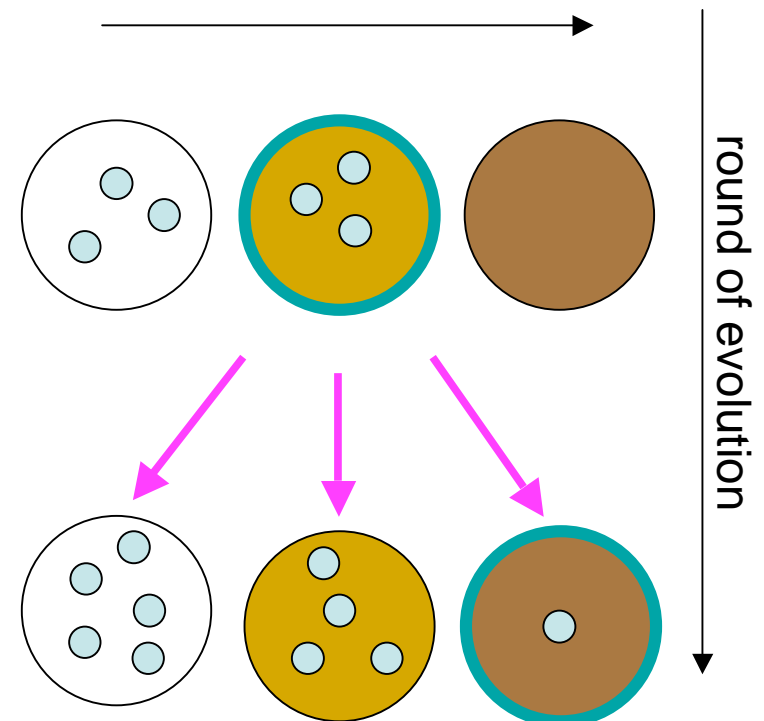
- **mutagenesis**

- plasmid prep
- mutagenic PCR of insert seq (substitution freq **~5%/base**)
- **re-clone** into **initial** vector, and re-transform into **initial** strain

- **selection**

...

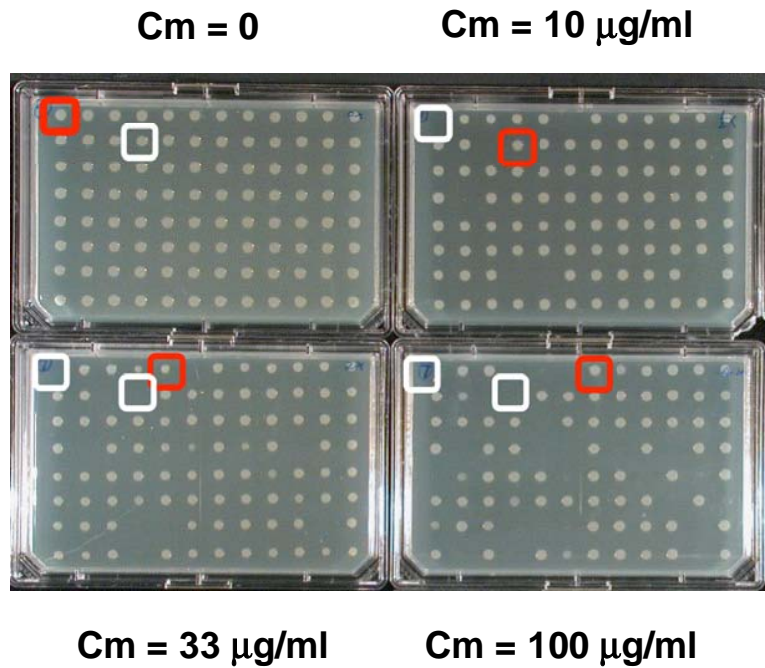
increasing **drug concentration**



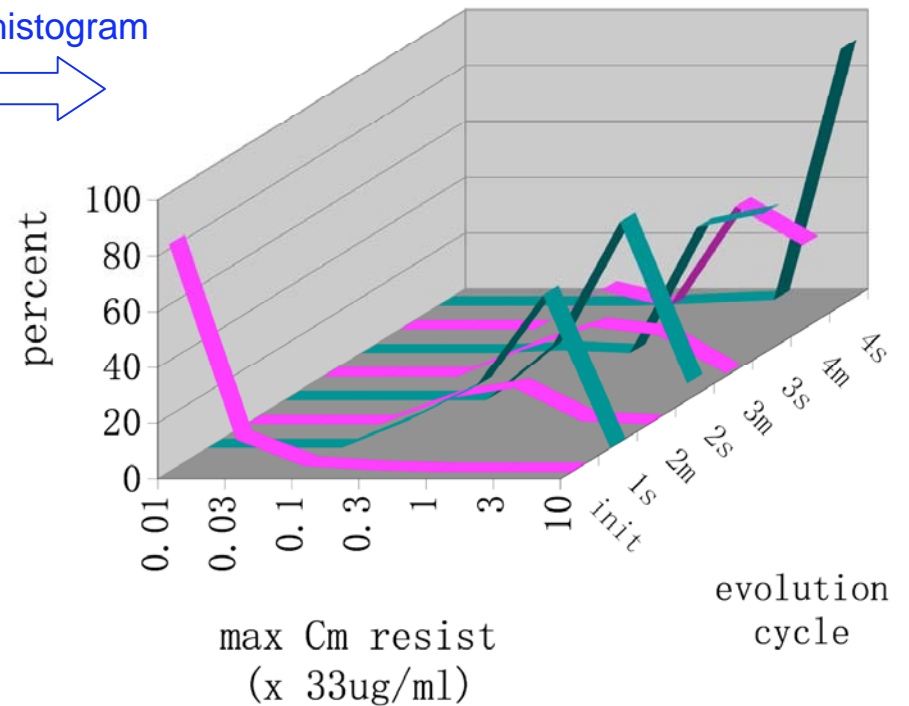
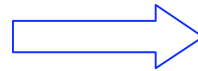
all intermediate clones “saved” for future analysis

# Semi-quantitative phenotype assay

Characterize distribution of phenotypes at each stage of evolution



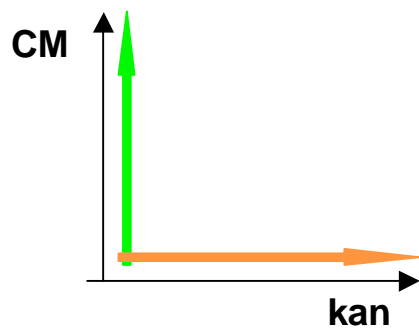
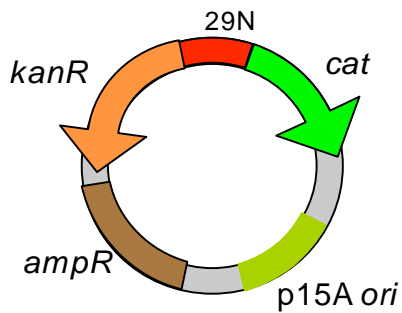
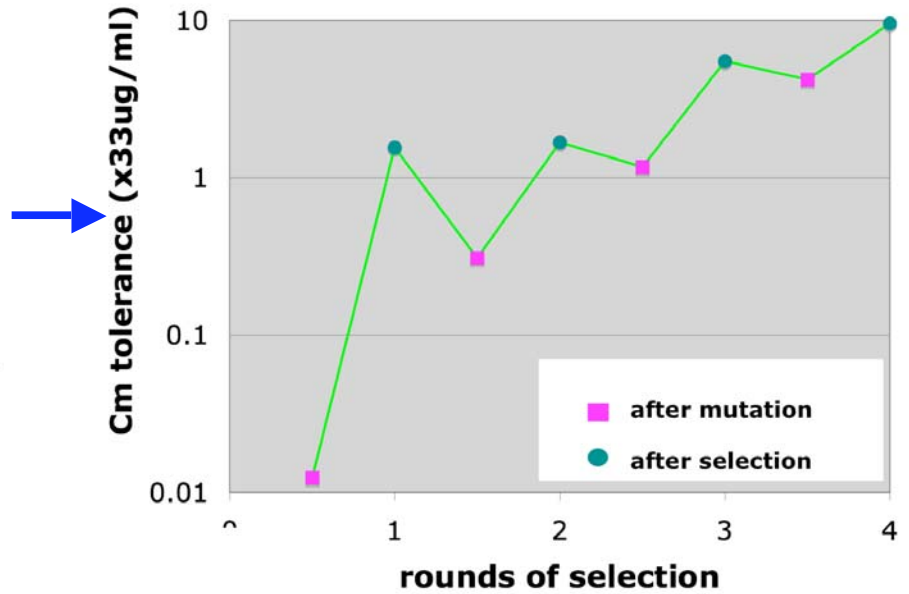
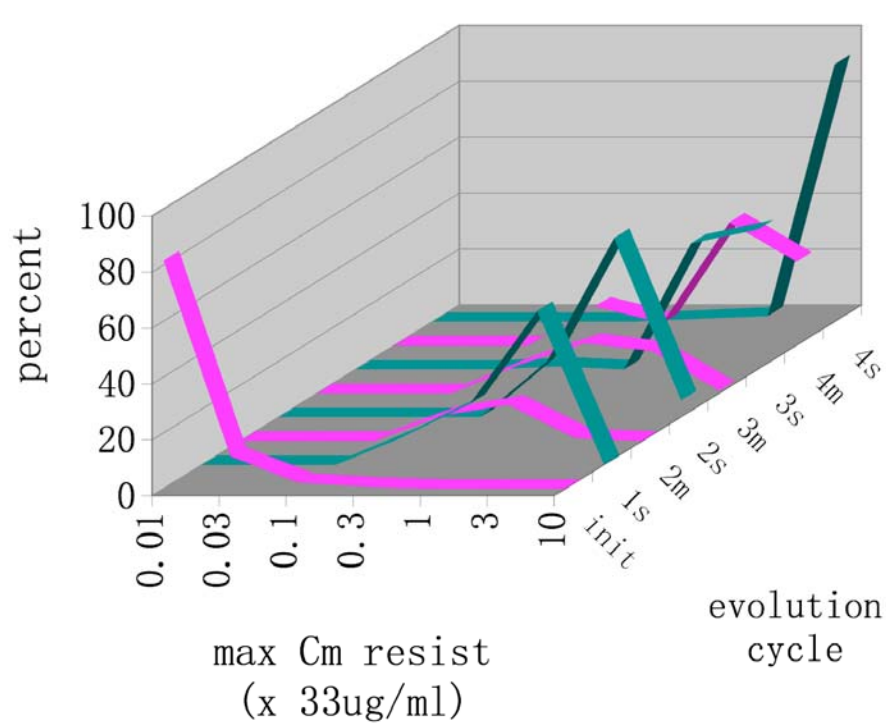
make histogram



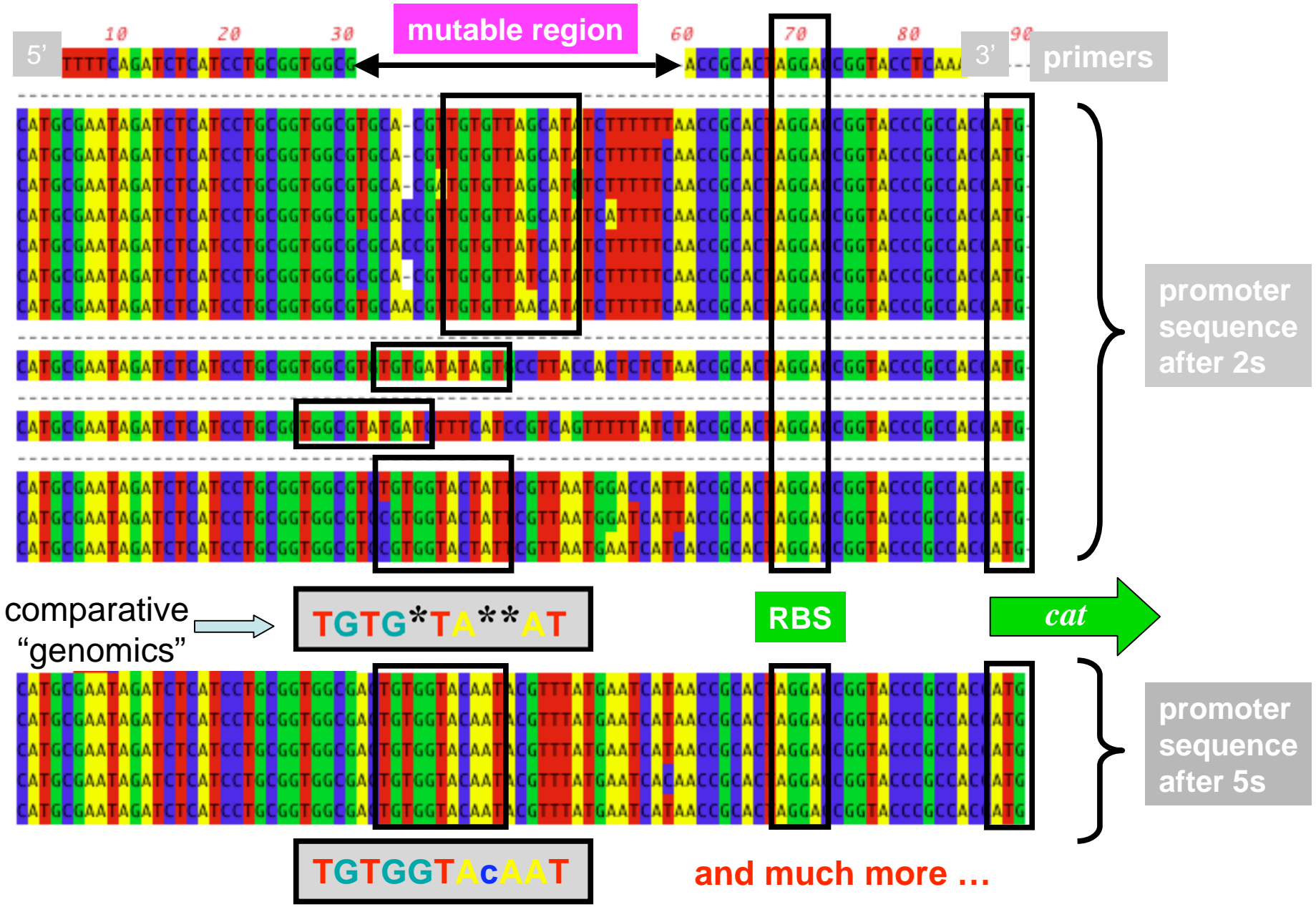
- collect 96 clones
- grow on agar plates with different drug conc
- identify max drug resistance

□ : Max drug resistance for the clone

# Evolution in single direction: phenotype



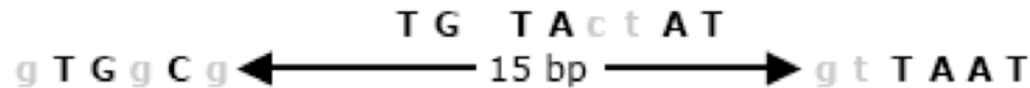
# Evolution in single direction (CM): genotype



# Degeneracy of evolved promoter (Cm direction)

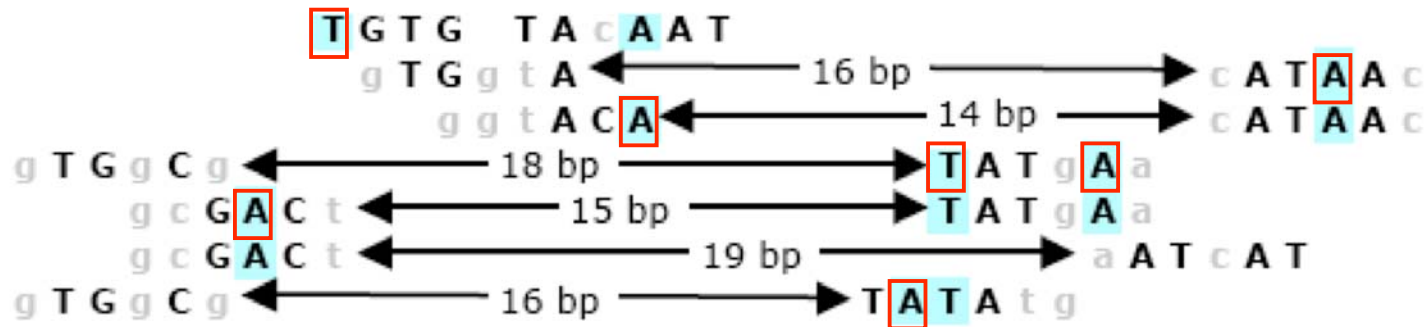
after 1st round (Cm resistance = 1 x 33ug/ml)

GGTGGCGTCCGTGGTACTATTTCGTTAATGGATCATTACC



after 5th round (Cm resistance > 10 x 33ug/ml)

GGTGGCGACTGTGGTACAAATACGTATATGAATCATAAACC



- up to **7 partial promoter motifs** packed in 29-nt region + flanking regions
- (almost) every **fixed mutation** attributable to additional motif(s)

**Why?**

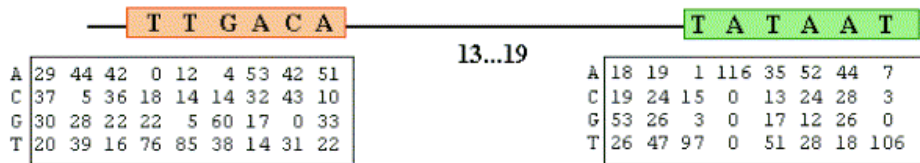
- stronger expression from multiple promoters?
- robustness to mutation provided by multiple copies?

**Benefit:** makes subsequent evolution of activators/repressors easier

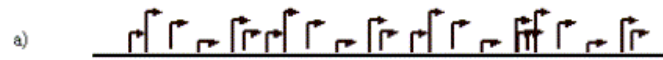


# Multiple promoters seen in bioinfo studies

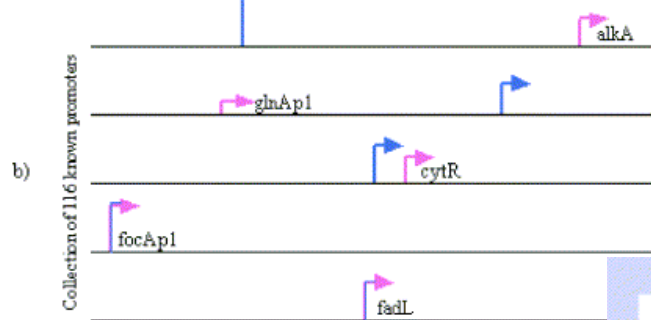
[Huerta & Collado-vides, 03]



Searching

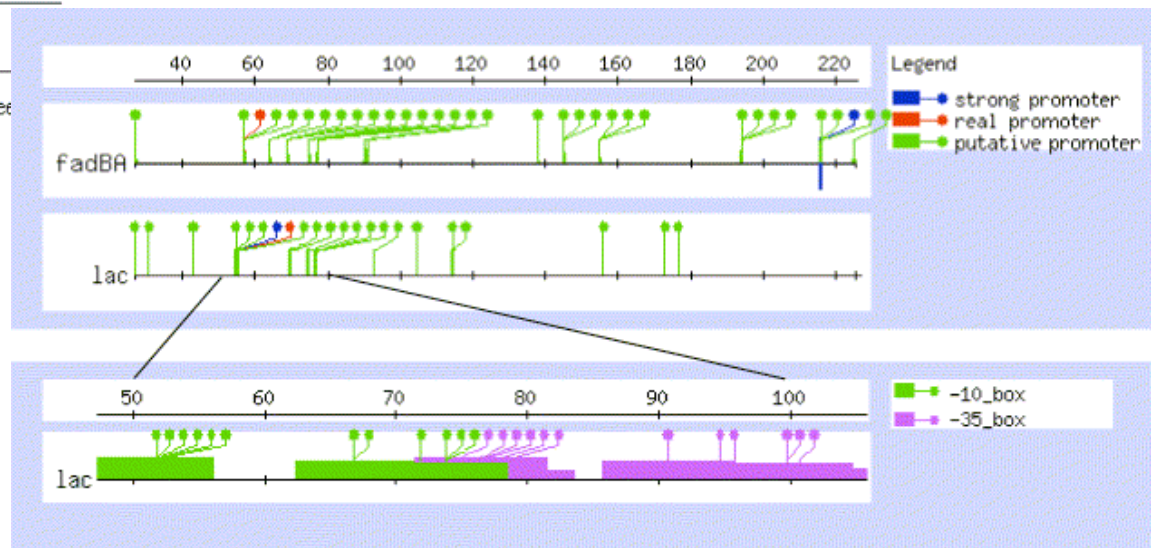


■ functional promoter  
■ strongest promoter

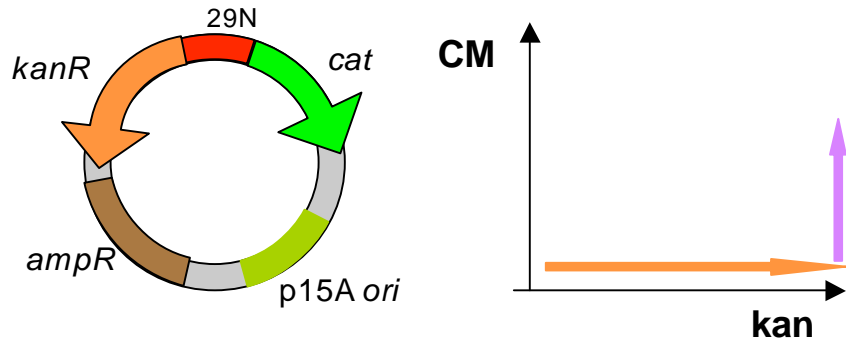


$$\text{Score(Promoter)} = \text{score}(-10 \text{ box}) + \text{score}(-35 \text{ box}) + \text{score}(\text{spacer between})$$

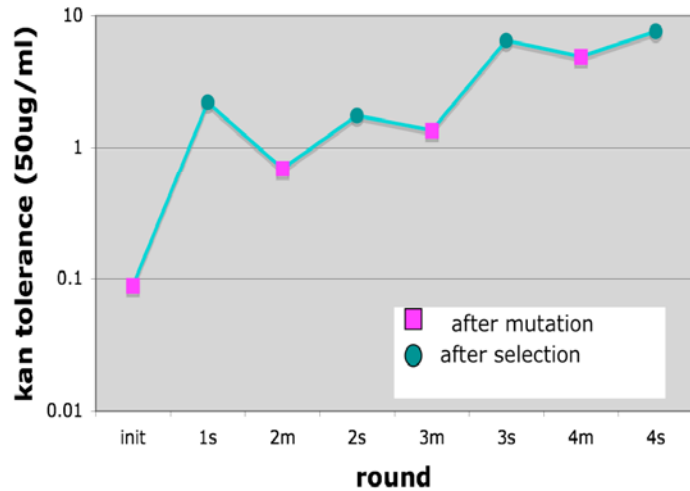
- avg of 38 putative promoter signals observed in a typical 250bp region upstream of gene start;
- in 50% of these regions, the “real” promoter is not the highest scoring promoter



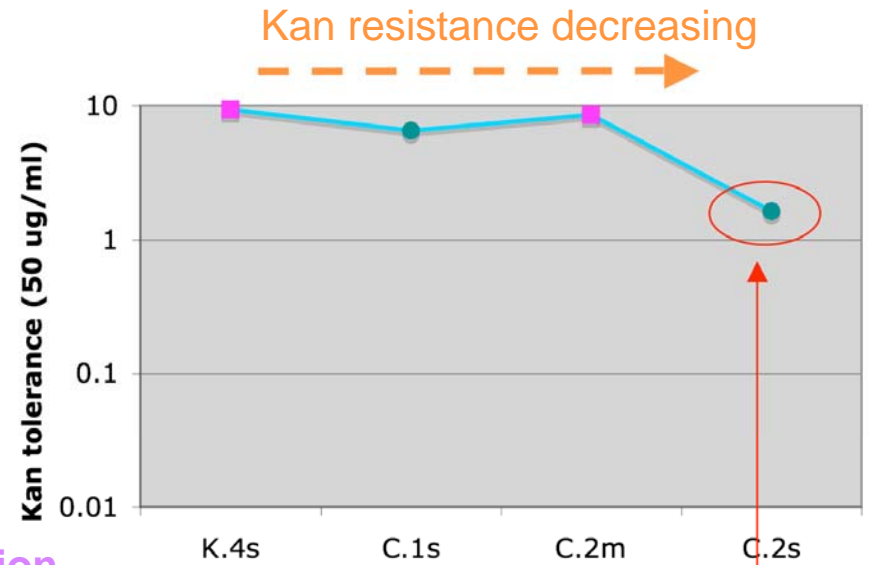
# Reversal of evolution direction: phenotype



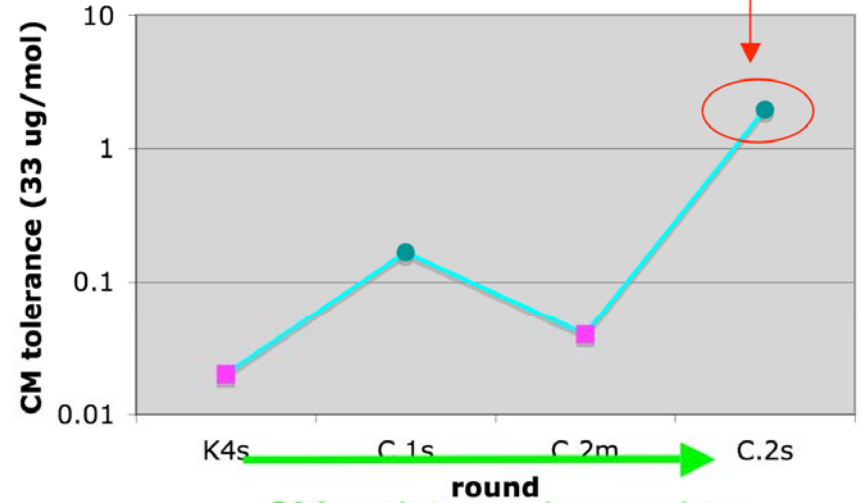
## 4 rounds of selection in Kan direction



revert selection to CM direction



appearance of divergent promoter activity



CM resistance increasing

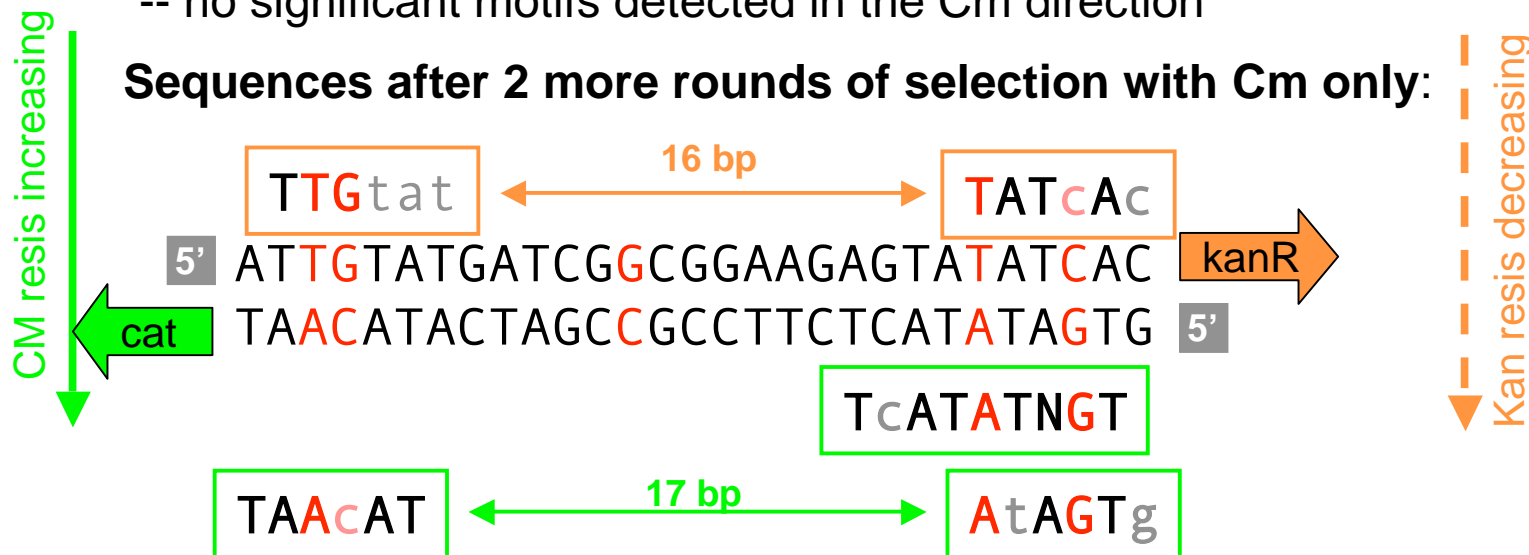
# Reversal of evolution direction: genotype

Sequences obtained after 4th round of selection with Kan only:



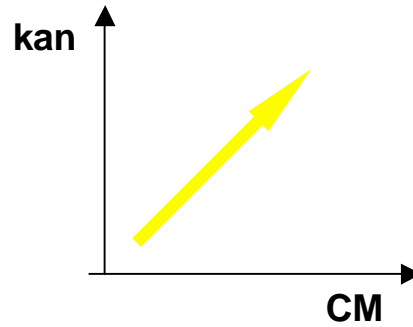
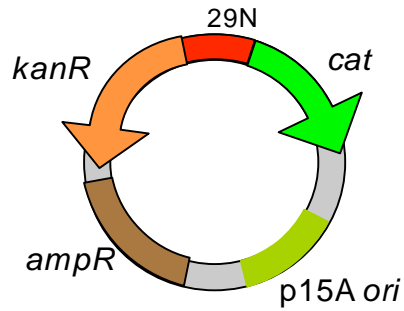
- one **extended -10 motif** and one **-35/-10 motif** in the Kan direction
- no significant motifs detected in the Cm direction

Sequences after 2 more rounds of selection with Cm only:



- one **extended -10** and one standard **-35/-10 motifs** in Cm direction
- weakened **-10/-35 motif** and lost extended -10 and in the Kan direction

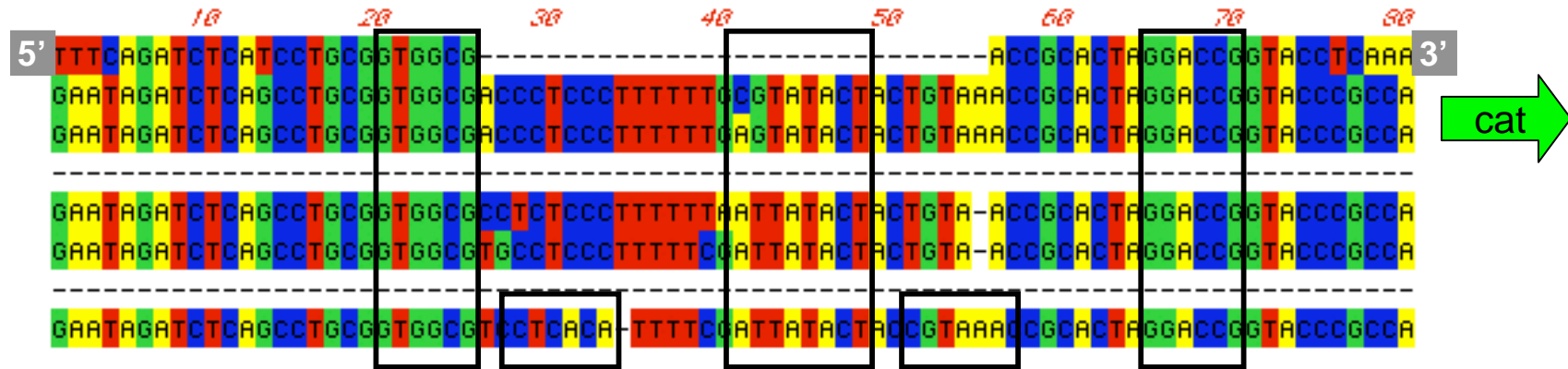
# Evolution in both directions: phenotype



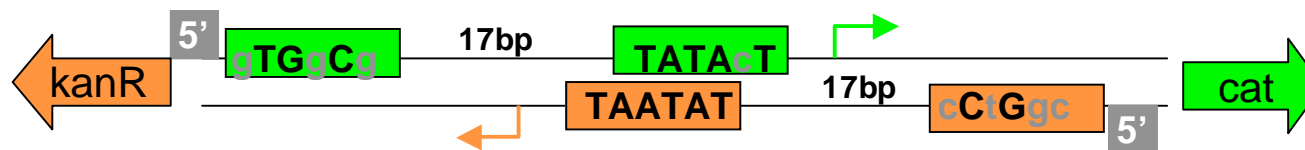
→ evolution slightly slower than that driven in single direction (5 vs 4 rounds)

# Evolution in both directions: genotype (5 rounds)

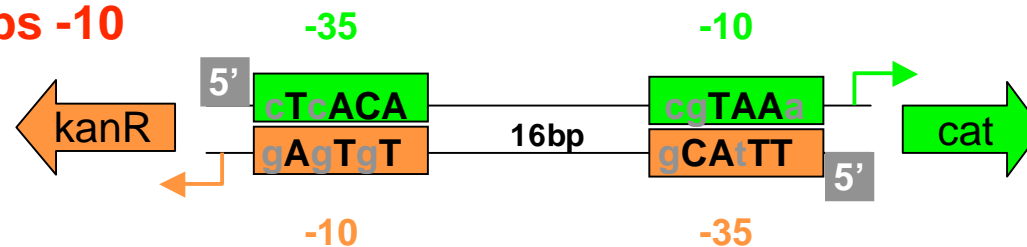
→ found two types of **overlapping** motifs:



**-10 overlaps -10** (with -35 on flanking sequences)

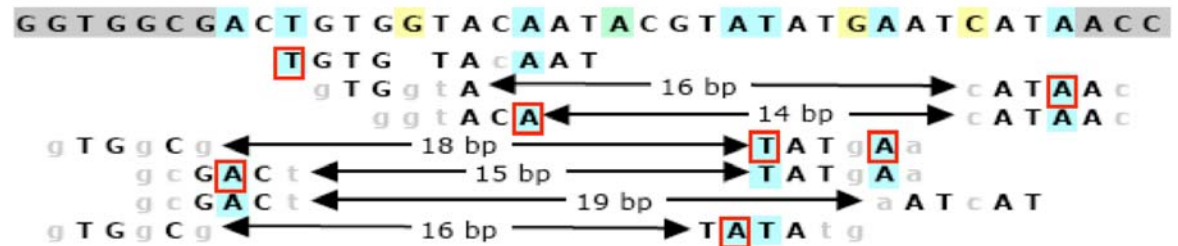
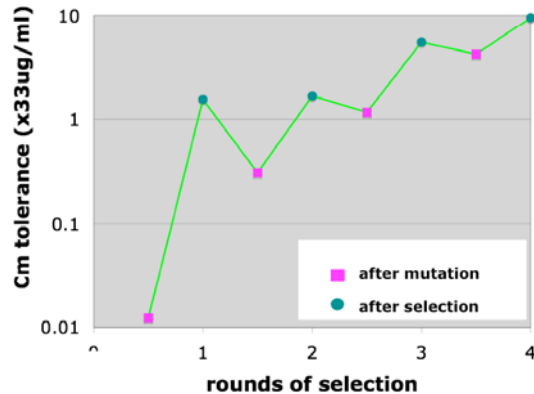


**-35 overlaps -10**



# Summary: promoters are flexible!

- **Single direction:** multiple promoters in confined space

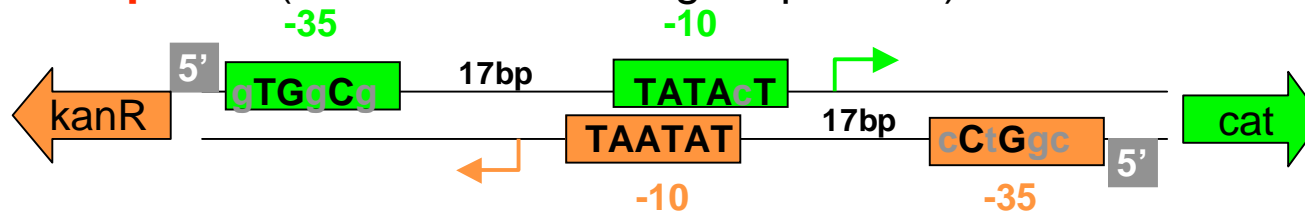


- **Reversal:**

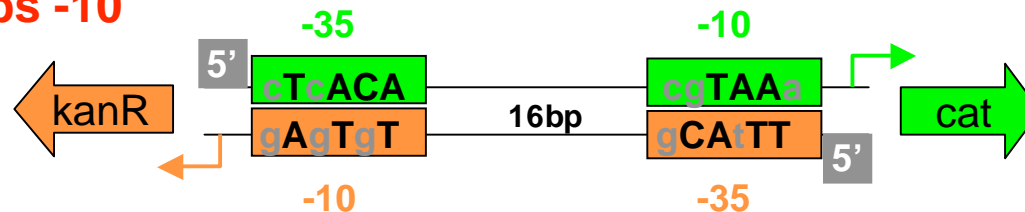
- existing promoter evolve quickly to reverse direction by few mutations
- reduction of promoter activity in the reverse direction important (occlusion)

- **Divergent overlapping promoters:**

**-10 overlaps -10** (with -35 on flanking sequences)



**-35 overlaps -10**

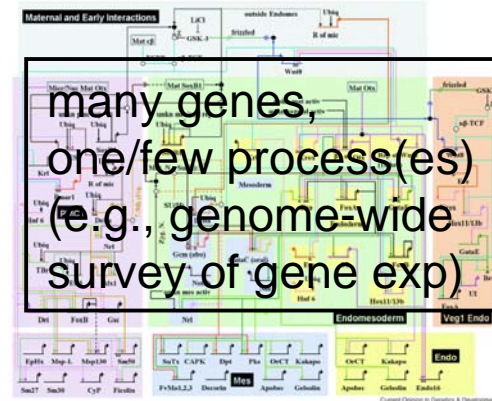


# From molecules to system-level functions

**traditional mol bio:**  
one gene, one process  
(e.g., A activates B)

high throughput methods

bioinformatic analysis

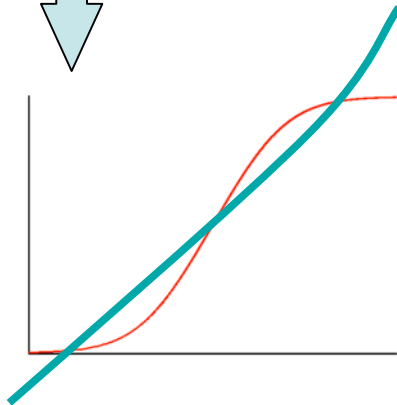


many genes,  
one/few process(es)  
(e.g., genome-wide  
survey of gene exp)

who talks to whom

quantitative analysis  
of individual nodes  
and small circuits

**qualitative** system-level properties  
depend **quantitatively** on  
the degree of regulation

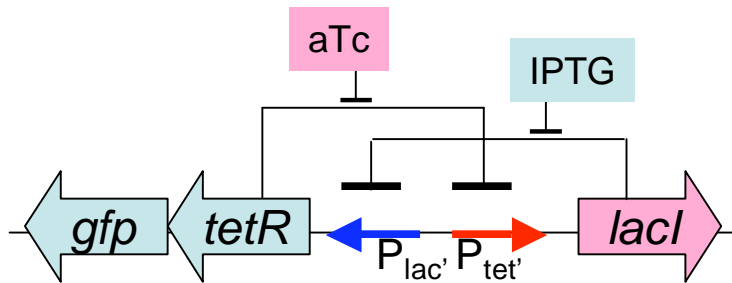


how they talk

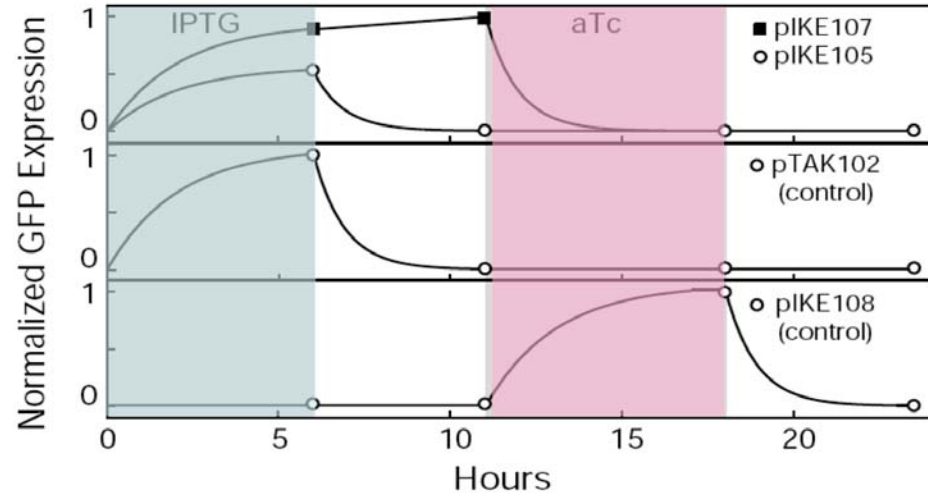
**systems biology:**

many components and processes  
(e.g., predictive modeling of cell  
and multi-cellular organisms)

# Synthetic genetic switch



[Gardner, Cantor and Collins, Nature 2000]



- induction time to switch: ~ 6 hrs (several cell divisions)
- **slow** speed possibly due to passive dilution

➔ “speed limit of gene regulation”

[Rosenfeld et al, Science, 2005]

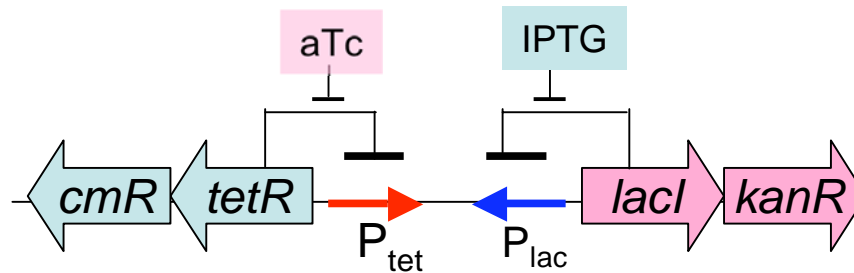
Natural switches (e.g., phage lambda)

- induction time to switch: < 10 min
- ingredients for fast speed
  - proteolysis
  - auto-activation and repression

**Q: faster switch using the same components?**

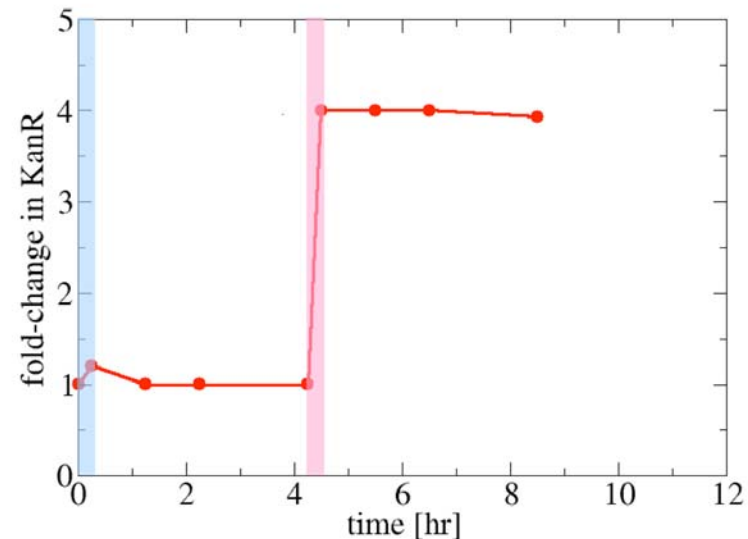
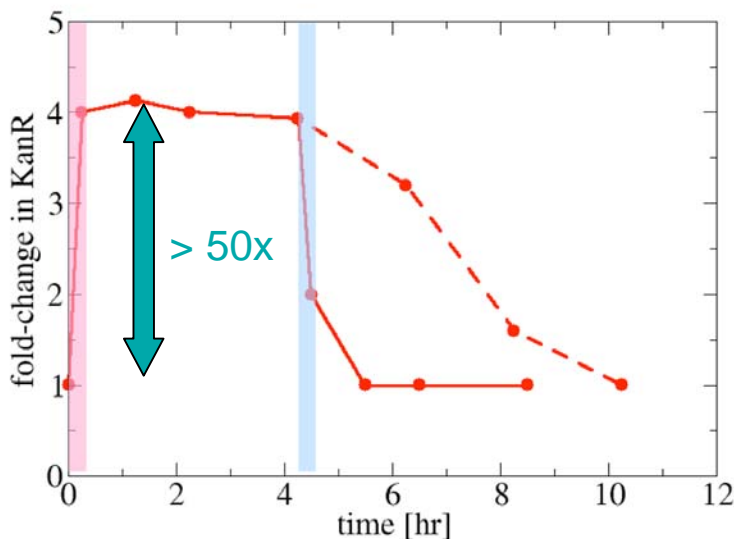


# Alternative switch: face-to-face promoter construct



	aTc	IPTG
KanR	growth	
CmR		growth

generate variants, screen for desired phenotype



- induction time needed for switching ~ 15min (fast)
- stability: 6-8 hours
- large fold-change in induction (LacZ and GFP activity)
- fast switch also in the reverse direction

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  - Eddie Mateescu (growth control)
- experiment
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  - Hendrik Szurmant (two-component signaling)
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related publications: <http://matisse.ucsd.edu/~hwa/pub>