

Fig. 4.16. The vertical, radial, and transverse components of ground motion (velocity) from the January 17, 1994 Northridge earthquake recorded at the IRIS/IDA station OBN at 88.5° range. The original broadband records have been filtered to between 15 and 100 s period. Time is in minutes relative to the earthquake origin time; amplitudes are self-scaled.

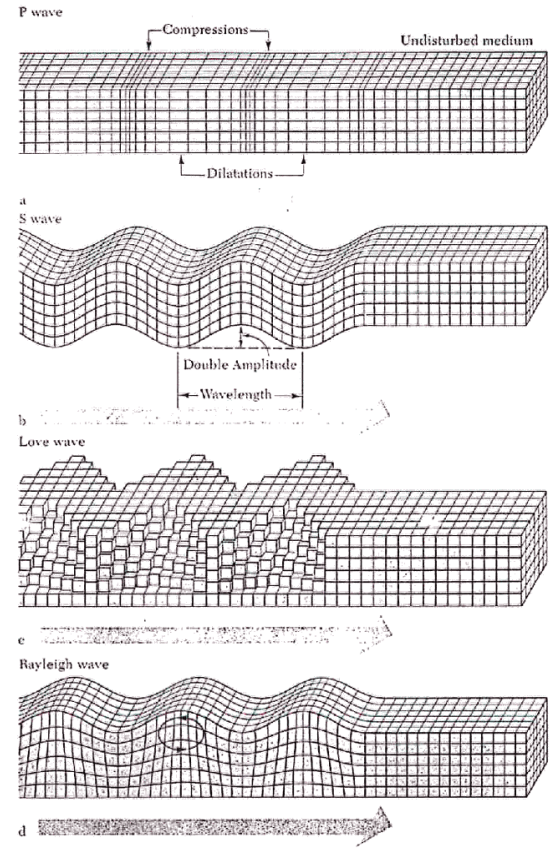
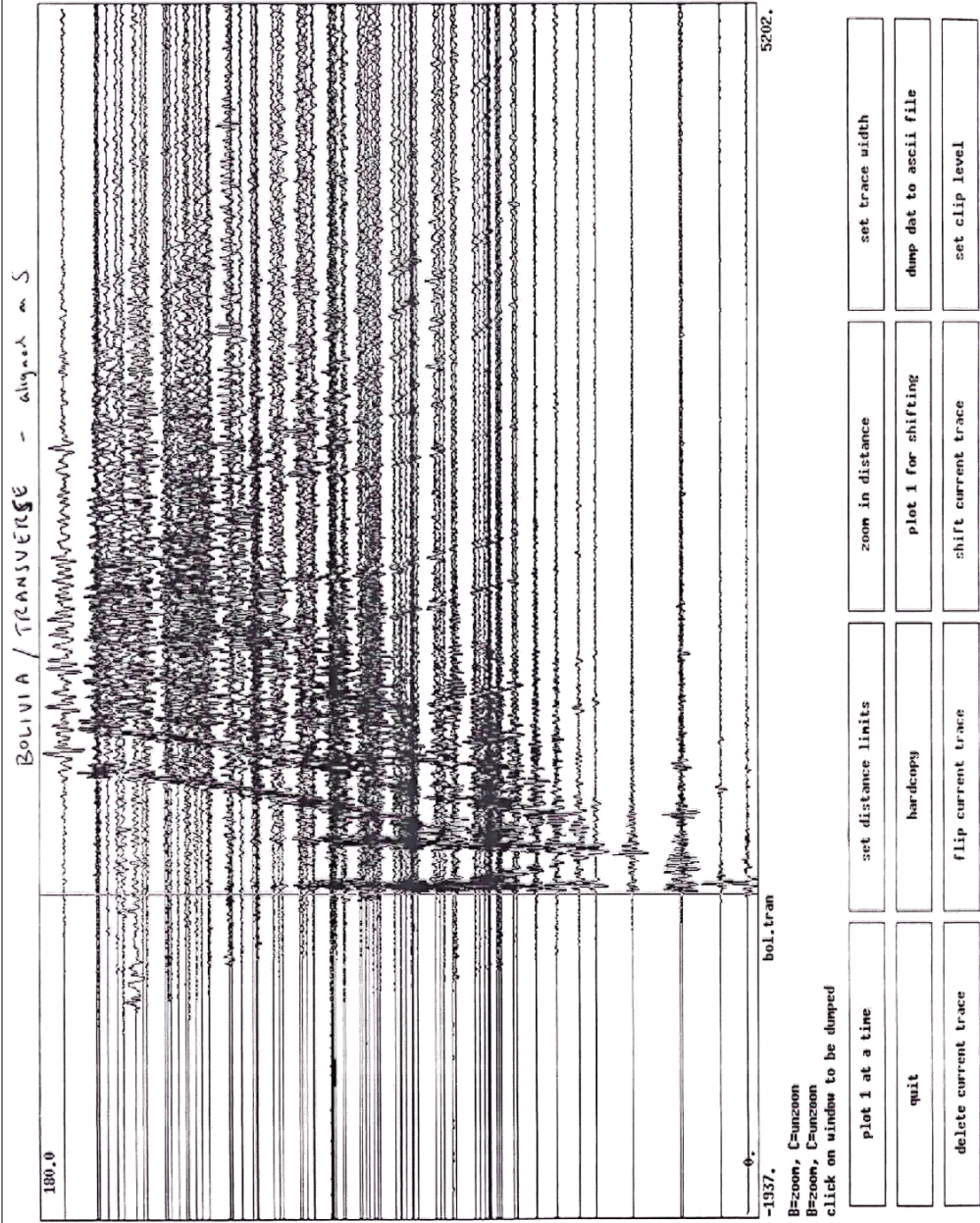
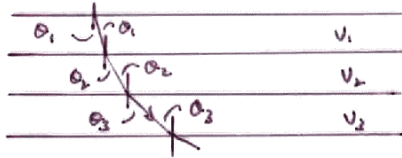


FIGURE 5  
Diagram illustrating the forms of ground motion near the ground surface in four types of earthquake waves. [From Bruce A. Bolt, *Nuclear Explosions and Earthquakes*. W. H. Freeman and Company. Copyright © 1976.]

Ray Theory

Flat

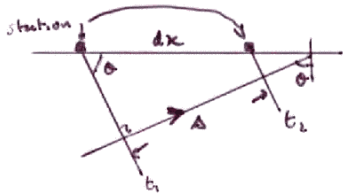


Snell's Law

$$\frac{1}{v_1} \sin \theta_1 = \frac{1}{v_2} \sin \theta_2 = \frac{1}{v_3} \sin \theta_3 = \dots$$

Ray parameter

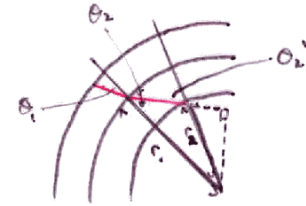
$$p = \frac{1}{v} \sin \theta = \frac{1}{v \cos \phi}$$



$$\Delta = \int \delta \cdot v = \int dx \sin \theta$$

$$\therefore \frac{d\Delta}{dx} = \frac{1}{v} \sin \theta = p$$

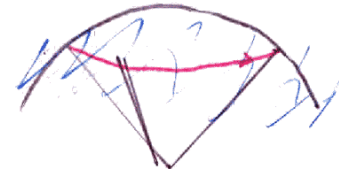
Spherical Earth



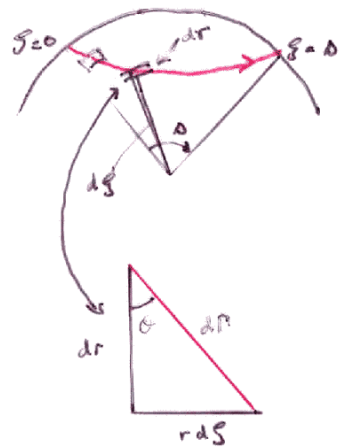
$$\theta_2 \neq \theta_2'$$

$$r_1 \sin \theta_2 = r_2 \sin \theta_2'$$

$$\therefore p = \frac{r}{v} \sin \theta = \frac{dT}{d\Delta} \quad (\text{seconds/radian})$$



(3)



$$\sin \theta = r \frac{dS}{dR}$$

$$\therefore dR = \frac{r^2}{pV} dS$$

$$T = \int_p^R \frac{1}{v} dR$$

$$\delta T = - \int_p^R \frac{\delta v}{v^2} dR \quad (\text{Fermat})$$

rewrite over distance

$$\delta T = \int_0^\Delta G(s) \delta v(s) ds$$

$$G(s) = - \frac{1}{v^2} \frac{dR}{ds} = - \frac{r^2}{pV^2}$$

Need to know  $r(s)$  to get  $v(s)$

$$\text{Now } \tan \theta = r \frac{dS}{dr} = \frac{\frac{r}{p}}{(1 - (\frac{r}{p})^2)^{1/2}} \therefore \frac{dS}{dr} = \frac{r}{p} \left( \frac{r^2}{v^2} - p^2 \right)^{-1/2}$$

(4)

1D Earth

$$\frac{dS}{dr} = \frac{r}{p} \left( \frac{r^2}{v^2} - p^2 \right)^{-1/2}$$

$$\therefore \Delta = 2 \int_{r_T}^R \frac{dS}{dr} dr$$

$$\Delta = 2 \int_{r_T}^R \frac{r}{p} \left( \frac{r^2}{v^2} - p^2 \right)^{-1/2} dr \quad *$$

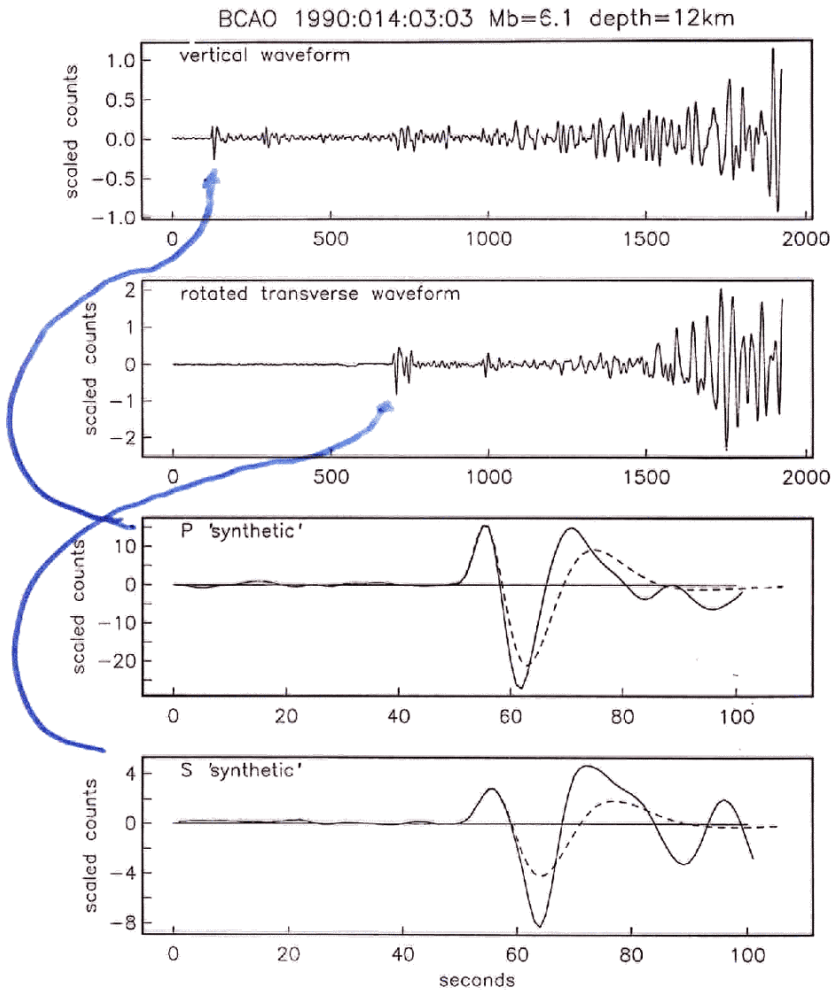
$$dT = \frac{dR}{v} = \frac{r^2}{pV^2} dS$$

$$\therefore \frac{dS}{dr} = \frac{pV^2}{r^2} \frac{dT}{dr} \quad \text{or} \quad \frac{dT}{dr} = \frac{r}{pV^2} \frac{dS}{dr}$$

$$T = 2 \int_{r_T}^R \frac{dT}{dr} dr$$

$$= 2 \int_{r_T}^R \frac{r}{pV^2} \left( \frac{r^2}{v^2} - p^2 \right)^{-1/2} dr \quad \leftarrow$$

Square root singularity  $\Rightarrow$  sensitivity to turning point structure  
 $(p = \frac{r}{v} \text{ at } r_T)$



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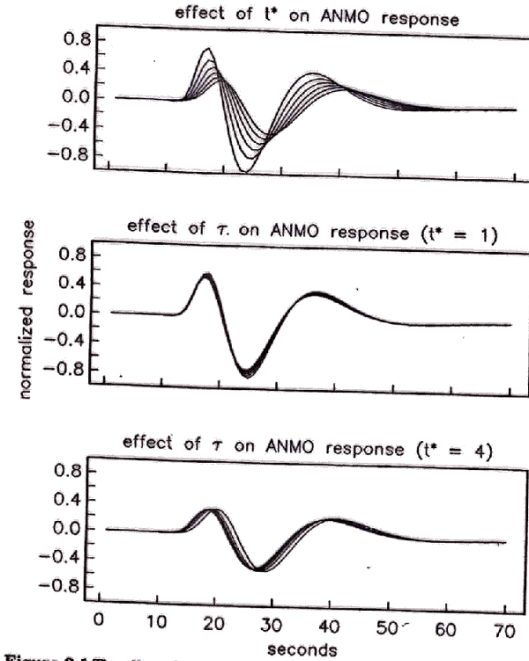
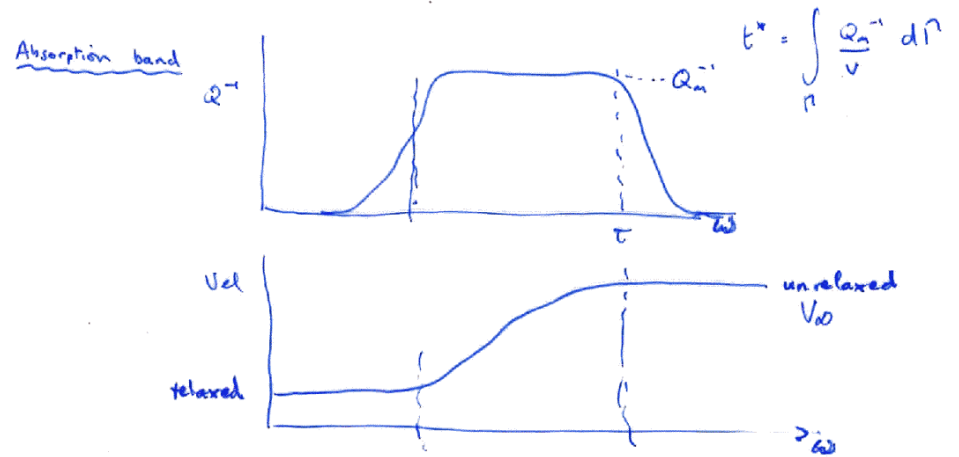
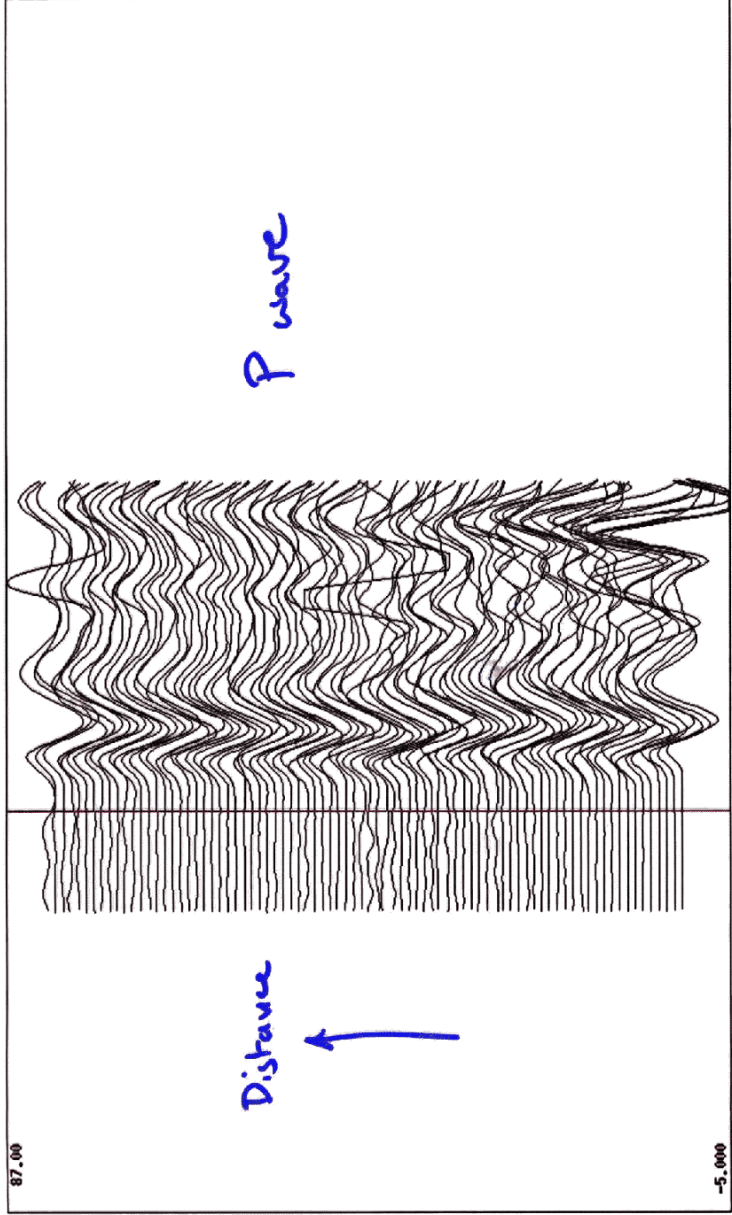


Figure 2.1 The effect of changing  $t^*$  and  $\tau_1$  on the absorption-band attenuation operator is illustrated. A change in  $\tau_1$  mainly causes a delay of the whole waveform. An increase in  $t^*$  leads to both a delay and a broadening.

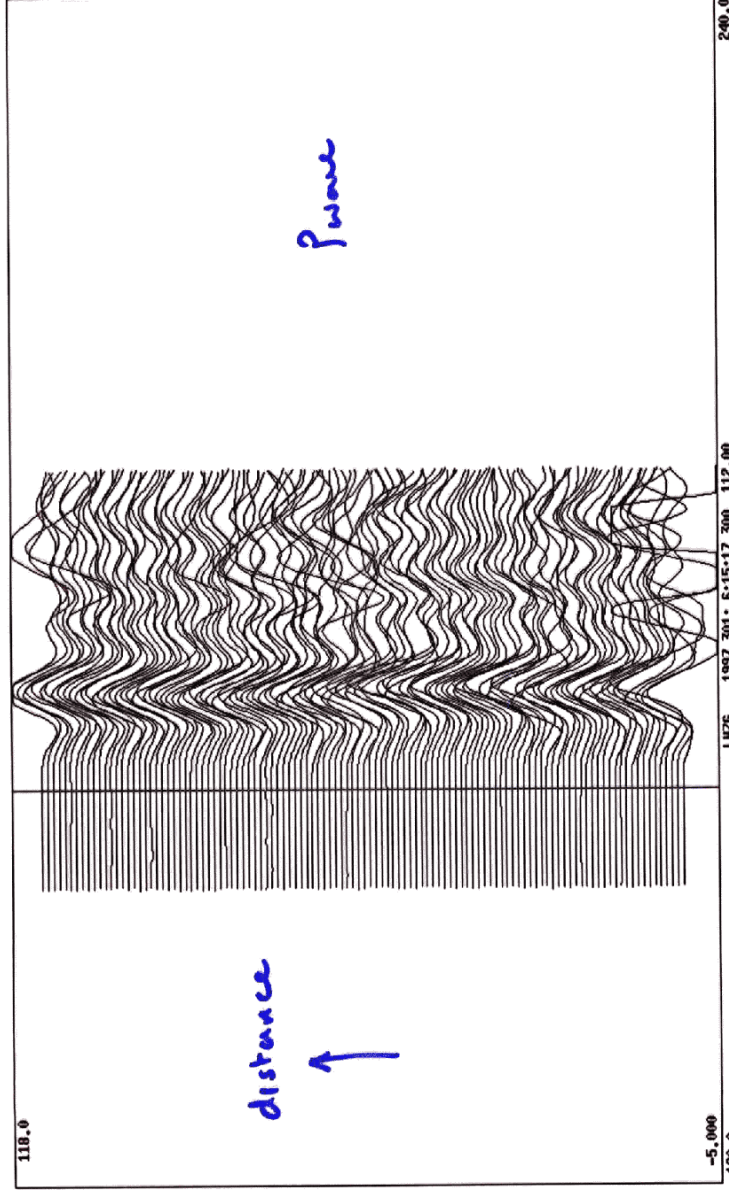




LN26 1997 313:22:56-42.700 176.00

click on new time  
 A,B: zoom C: unzoom  
 click on window to be dumped

dist/az	Alt+Shift B:rrain C:mr	zoom in distance	set trace width
quit	hardcopy	A,B: next event, C: last event	dump dat to ascii file
set clip level	select one trace	A,B: align, Cpilot raw data	dump data for cluster plot



LN26 1997 301: 6:15:17.300 112.00

click on new time  
 A,B: zoom C: unzoom  
 click on window to be dumped

dist/az	Alt+Shift B:rrain C:mr	zoom in distance	set trace width
quit	hardcopy	A,B: next event, C: last event	dump dat to ascii file
set clip level	select one trace	A,B: align, Cpilot raw data	dump data for cluster plot

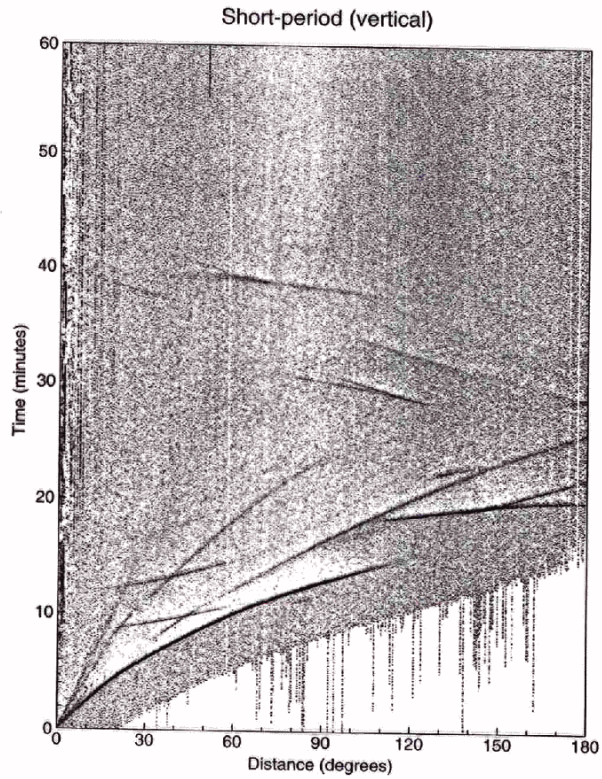


Fig. 4.18. A stack of short-period (<math>< 2\text{ s}</math>), vertical component data from the global networks between 1988 to 1994. See Figure 4.19 for a key to the phase names. (From Astiz et al., 1996.)

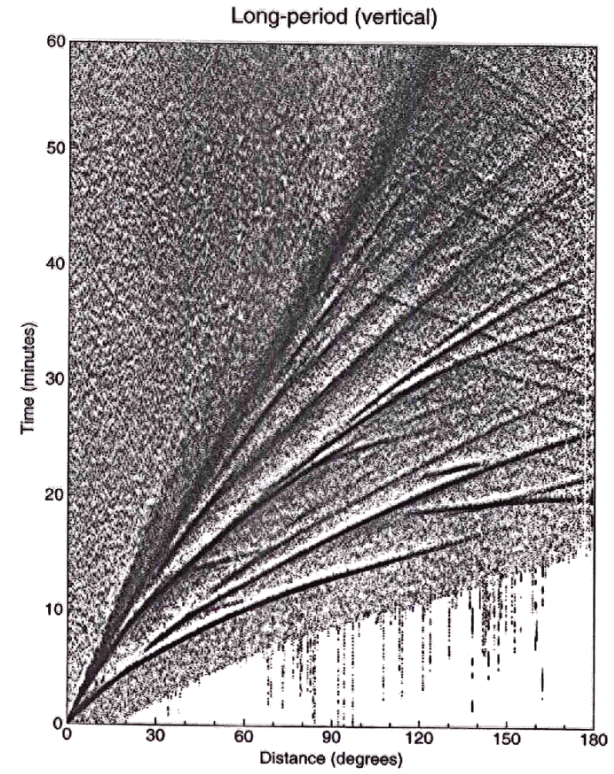


Fig. 4.20. A stack of long-period (>math>> 10\text{ s}</math>), vertical component data from the global networks between 1988 to 1994. See Figure 4.23 for a key to the phase names. (From Astiz et al., 1996.)

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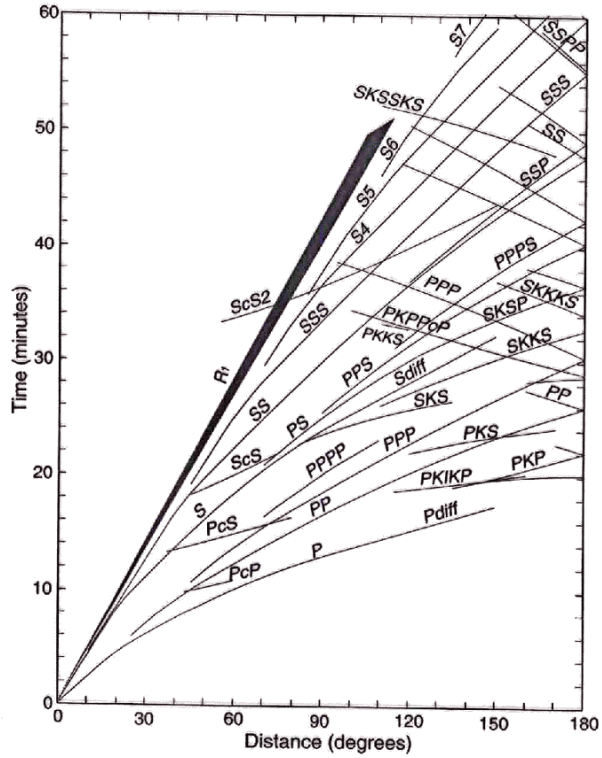


Fig. 4.23. The phases visible in the long-period stacks shown in Figures 4.20–4.22. Travel time curves are calculated using the IASP91 velocity model (Kennett and Engdahl, 1991). (From Astiz et al., 1996.)

E 2  
4.1

4.2

4.3

4.4

4.5

4.6

4.9 GLOBAL BODY WAVE OBSERVATIONS

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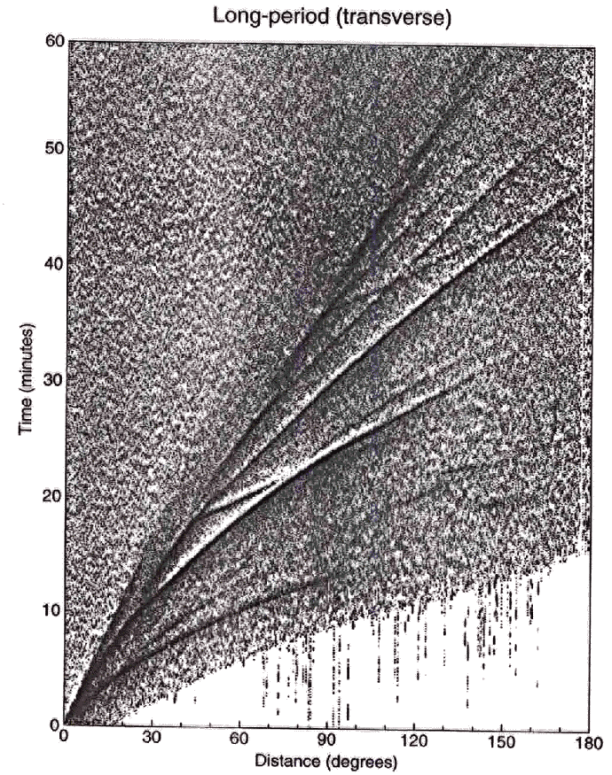


Fig. 4.22. A stack of long-period (> 10 s), transverse component data from the global networks between 1988 to 1994. See Figure 4.23 for a key to the phase names. (From Astiz et al., 1996.)



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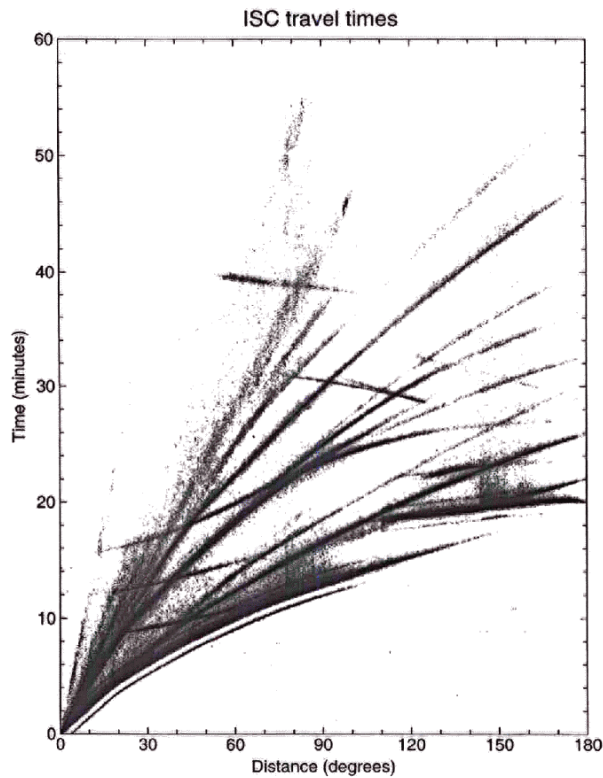
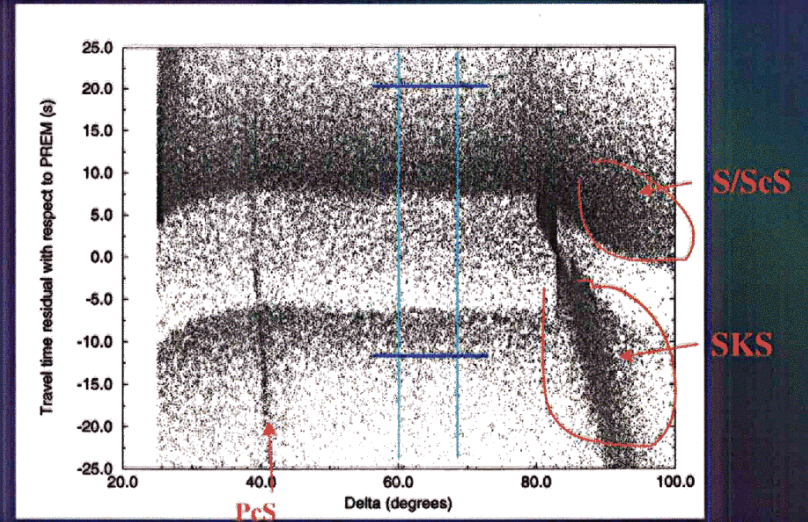


Fig. 4.17. Travel time picks collected by the ISC between 1964 and 1987 for events shallower than 50 km. Over five million individual picks are plotted, the bulk of which are *P*, *PKP*, and *S* arrivals. However, several later arriving branches can also be seen, including *PP*, *PKS*, *PcP*, *PcS*, *ScS*, *PKKP*, and *PKPPKP*. See Figures 4.19 and 4.23 for a key to the phase names. The phases visible at  $\pm 1$  minute from the *P*-wave are due to errors in assigning times.

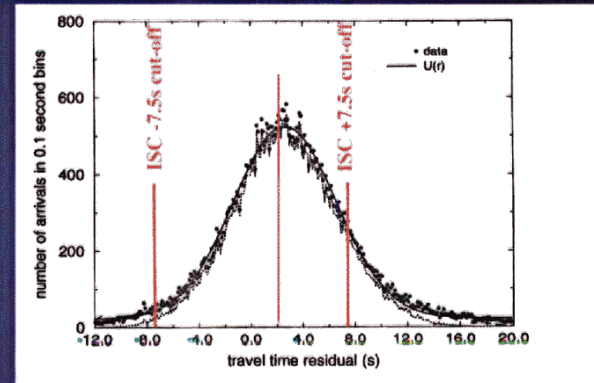
6  
5  
4  
3  
2  
1

## ISC S Travel Times Relative to PREM

Arrivals after identified ISC S (Jeffreys-Bullen  $\pm 7.5s$ ) have been removed



Data Binned in the 60-70° Epicentral Distance Range



Modified from Robertson and Woodhouse, 1995