

# “Ultracold Atoms – Dilute Gases with Strong Interactions”

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4/23/07

KITP Workshop  
Santa Barbara

# BCS Theory 1957 -2007



**John Bardeen**



**Leon Neil Cooper**



**John Robert  
Schrieffer**

# BCS state in lithium

## BCS-1 Lithium Ion Battery Charger

▶ [Comp](#)



This dedicated charger for the BLS-1 Lithium Ion Battery (BLS-1) charges the BLS-1 in about 210 minutes (at room temperature). Rated for 100 to 240 V allows use internationally\*.

\* Power outlet shapes vary by country/region, so be sure you have the needed plug(s) before traveling.



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**Product:**

# Superconductivity in Dense Lithium

Viktor V. Struzhkin,<sup>1\*</sup> Mikhail I. Erements,<sup>2</sup> Wei Gan,<sup>1,3</sup>  
Ho-kwang Mao,<sup>1</sup> Russell J. Hemley<sup>1</sup>

Superconductivity in compressed lithium is observed by magnetic susceptibility and electrical resistivity measurements. A superconducting critical temperature ( $T_c$ ) is found ranging from 9 to 16 kelvin at 23 to 80 gigapascals. The pressure dependence

SCIENCE VOL 298 8 NOVEMBER 2002

## Superconductivity in compressed lithium at 20 K

Katsuya Shimizu<sup>\*†</sup>, Hiroto Ishikawa<sup>\*</sup>, Daigoroh Takao<sup>\*</sup>, Takehiko Yagi<sup>‡</sup>  
& Kiichi Amaya<sup>\*†</sup>

NATURE | VOL 419 | 10 OCTOBER 2002 | [www.nature.com/nature](http://www.nature.com/nature)

## BCS-superconductivity of lithium at 50 GigaPascal

This talk:

BCS-superfluidity of lithium at 1 nanoPascal

Ultracold: nanokelvin

100 million times colder than outer space

Ultralow density:  $10^{14} \text{ cm}^{-3}$

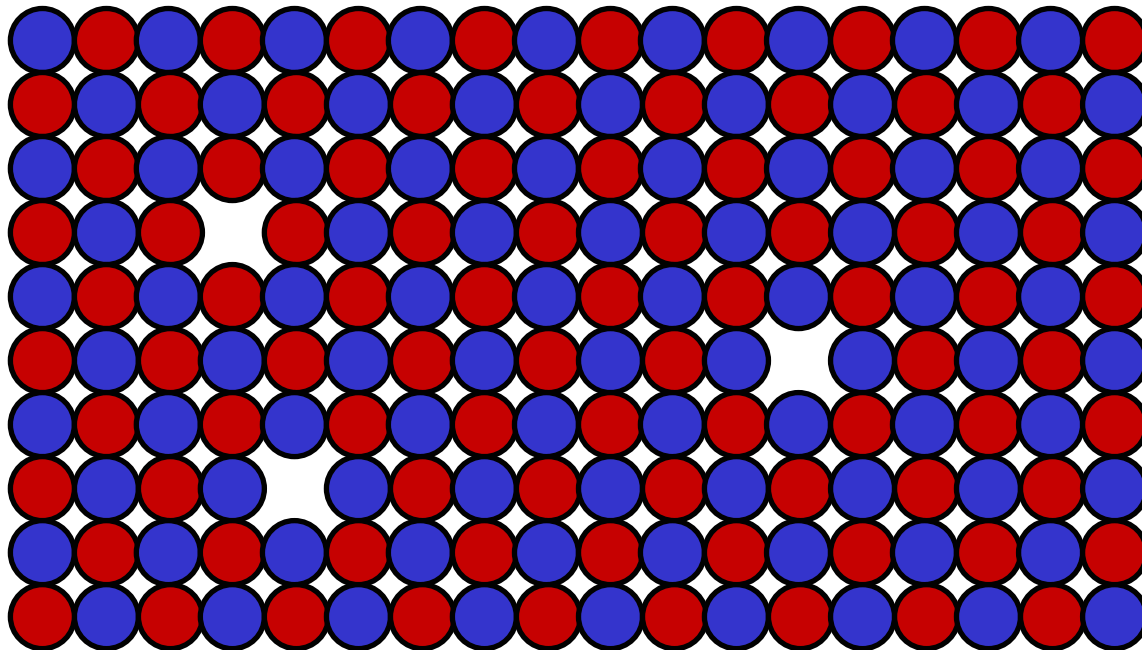
100,000 thinner than air

# Ultracold atoms

## A “toolbox” for designer matter

Normal matter

- Tightly packed atoms
- Complicated Interactions
- Impurities and defects



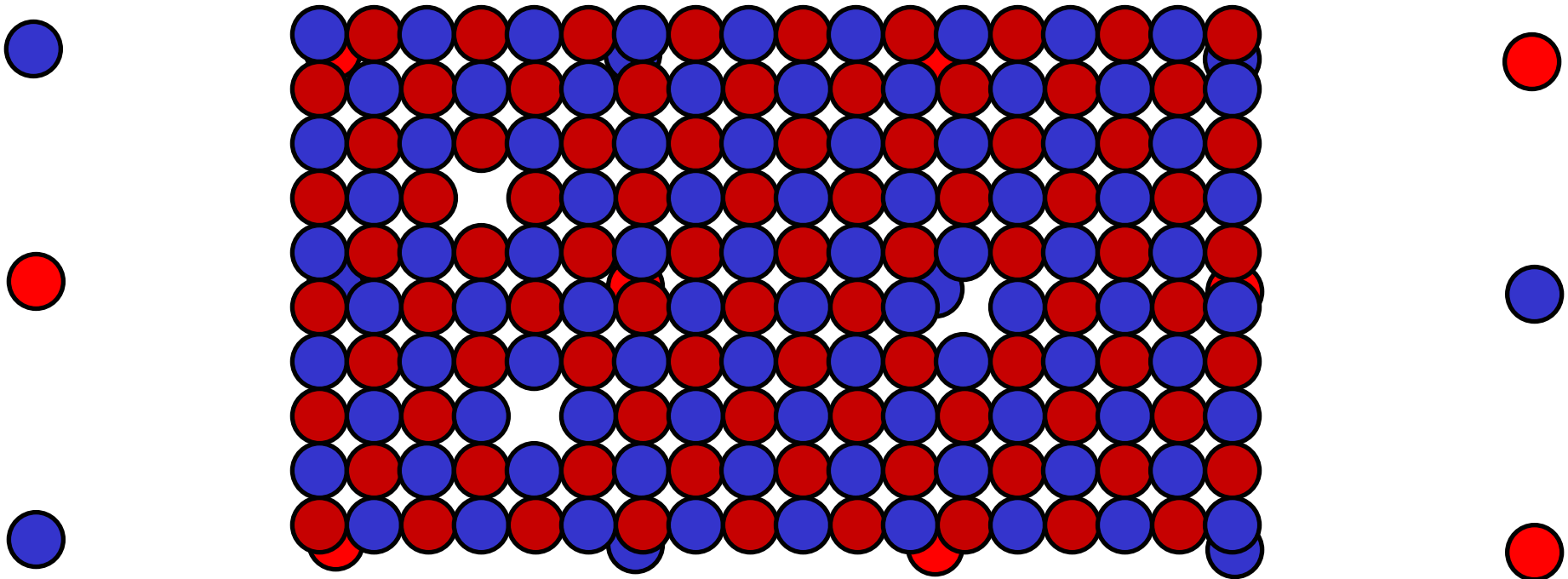
# Ultracold atoms

## A “toolbox” for designer matter

Matter of ultracold atoms

- 100 million times lower density

Need 100 million times colder temperatures

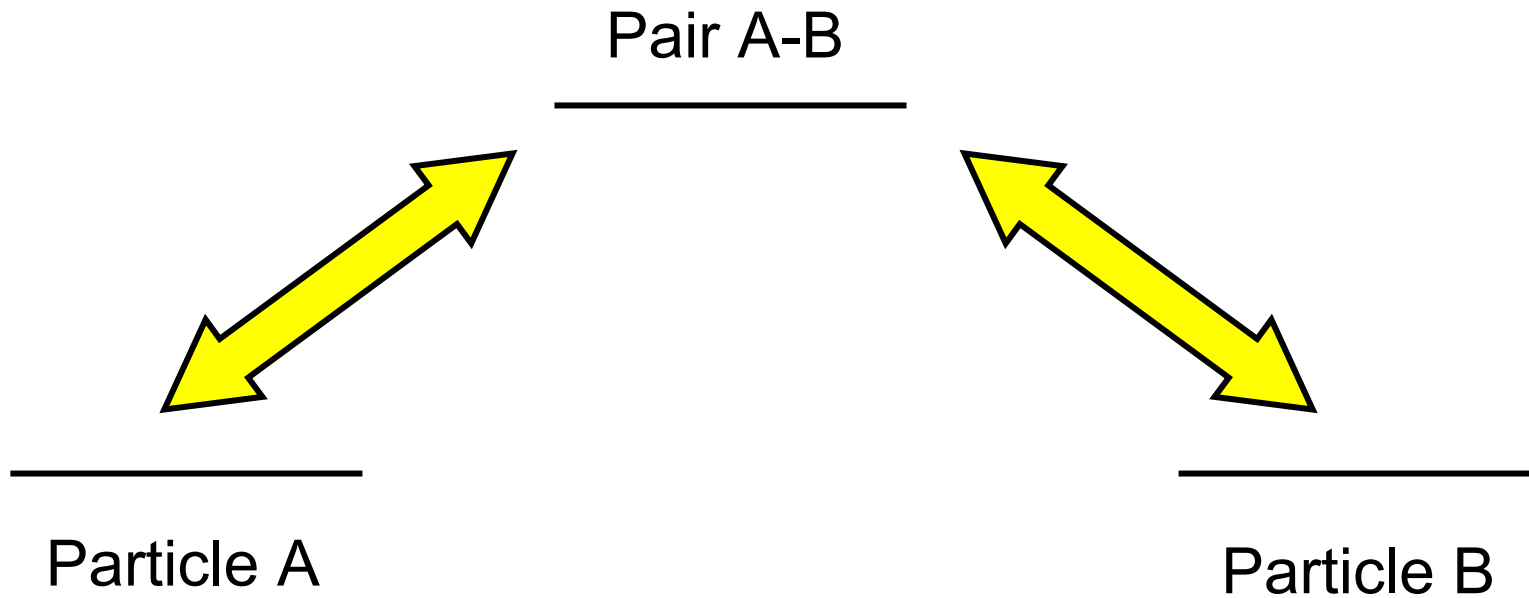




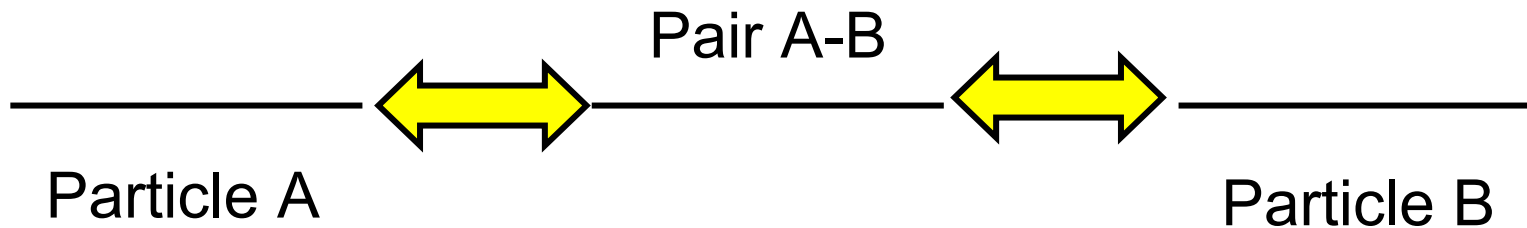
The combination of low density and low temperature provides a new approach to study strongly interacting systems in a controlled way

- Interactions understood and controlled
- no impurities
- exact calculations possible

# How to get strong interactions?

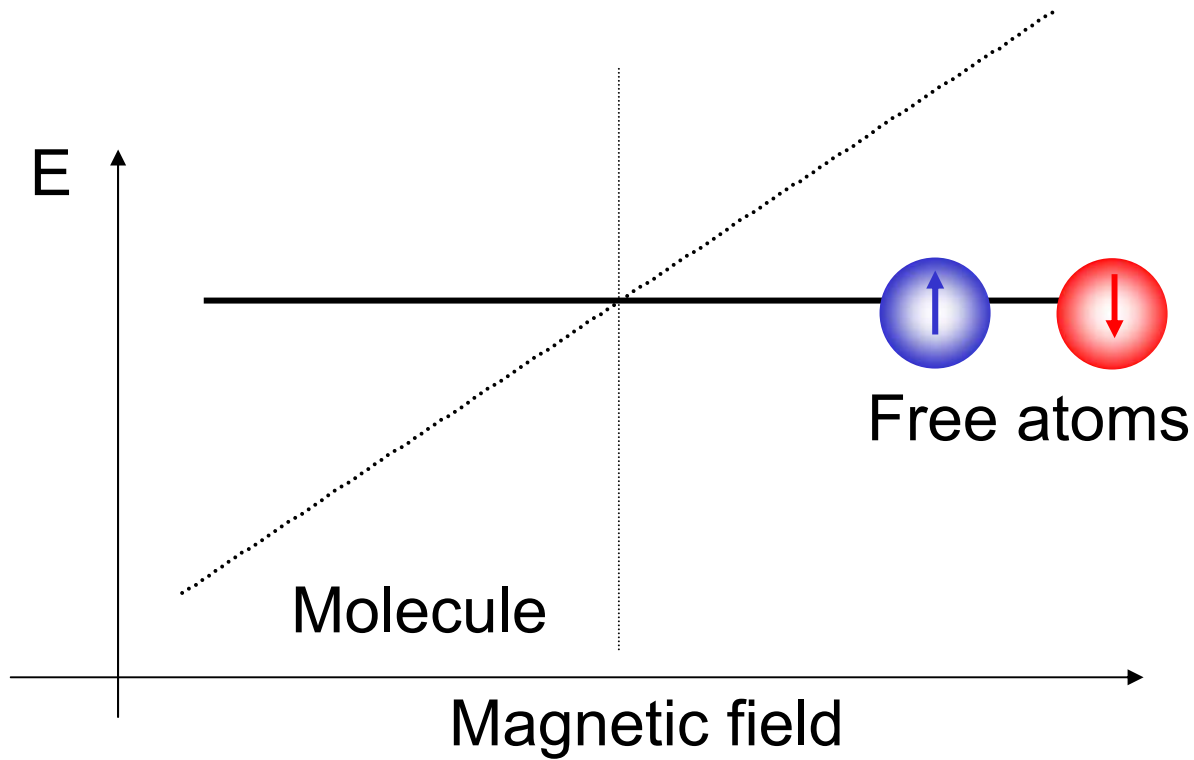


# Resonant interactions have infinite strength



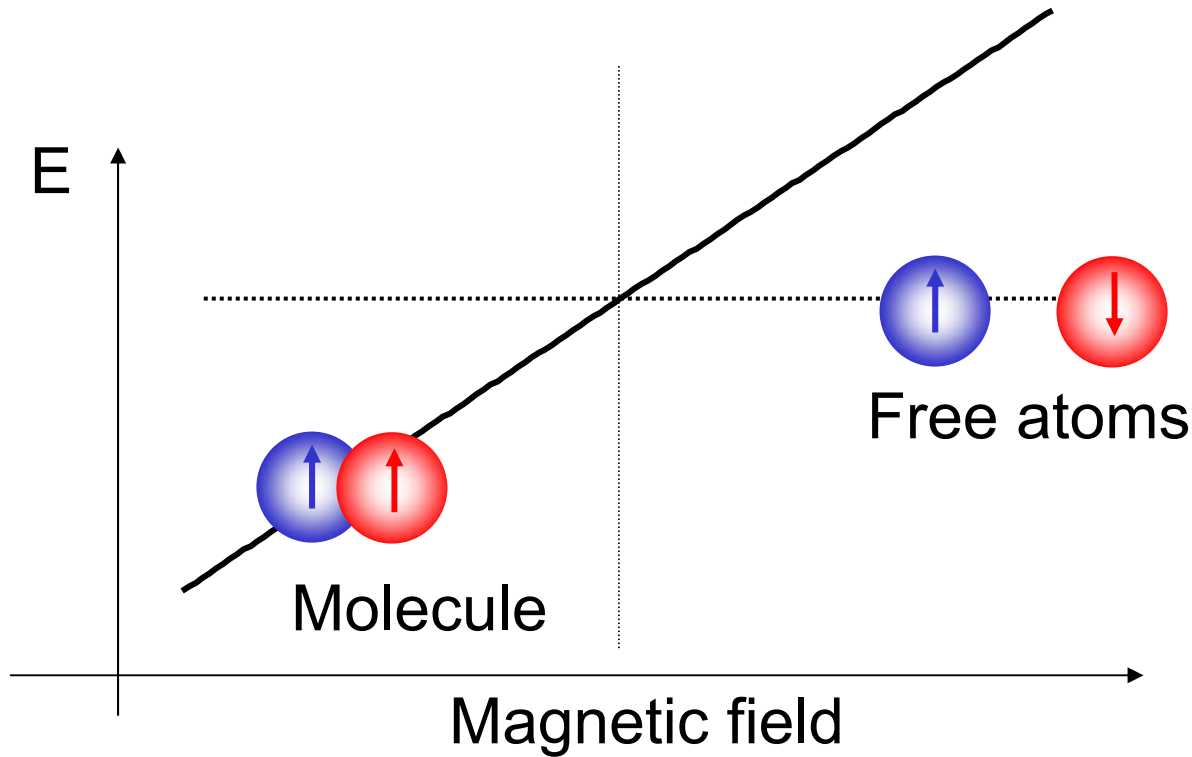
## Unitarity limited interactions:

- Pairing in ultracold fermions
- Relevant to quark-gluon plasmas



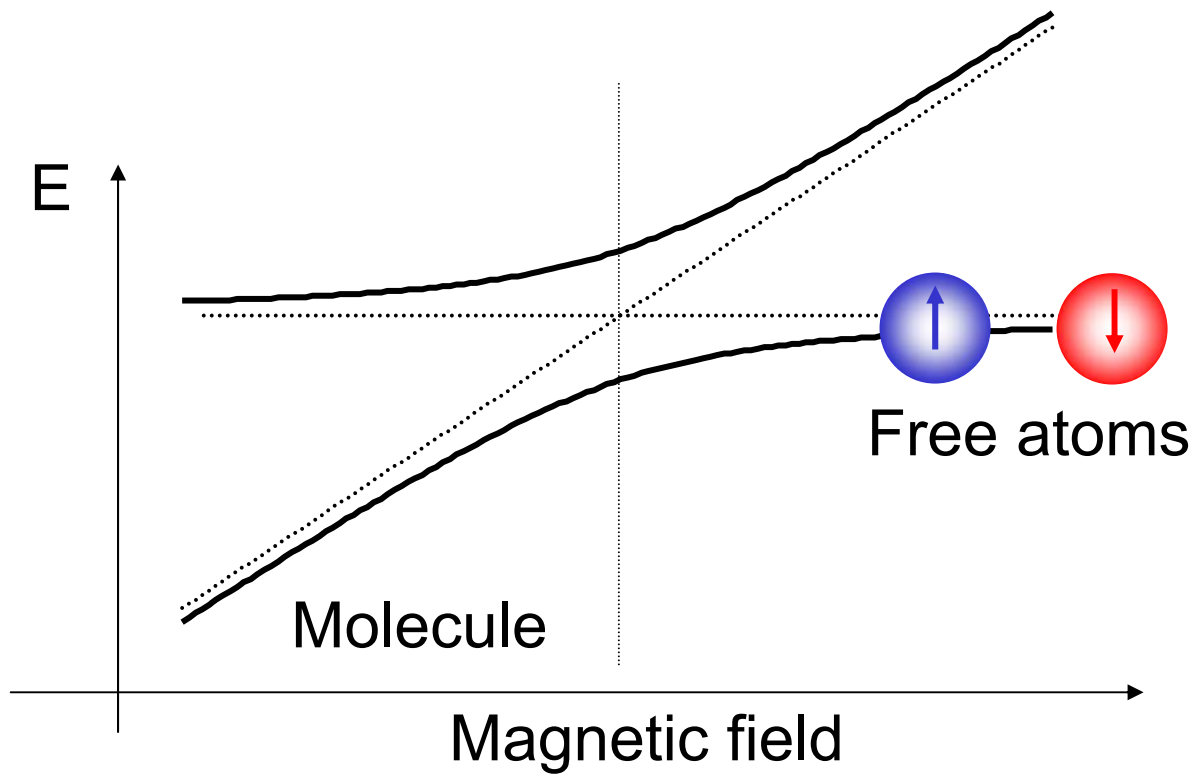
Feshbach resonance

Disclaimer: Drawing is schematic and does not distinguish nuclear and electron spin.



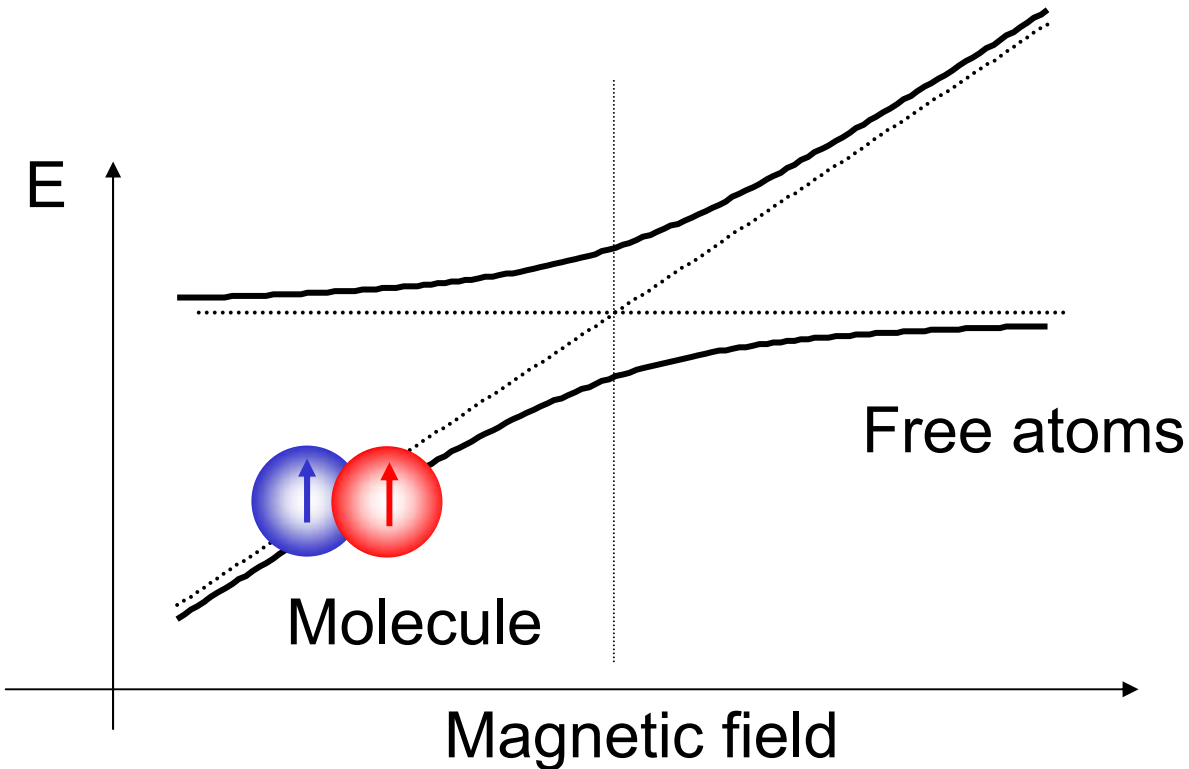
Feshbach resonance

Two atoms ....



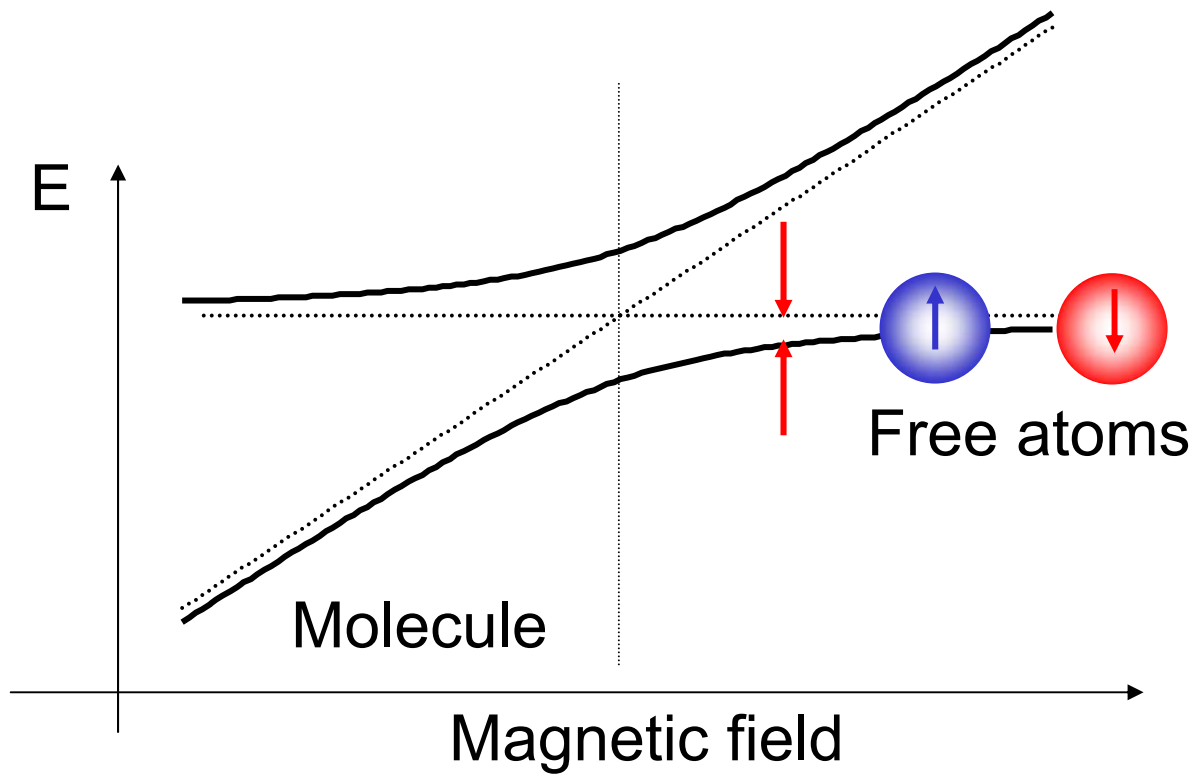
Feshbach resonance

... form a stable molecule



Feshbach resonance

Atoms attract each other

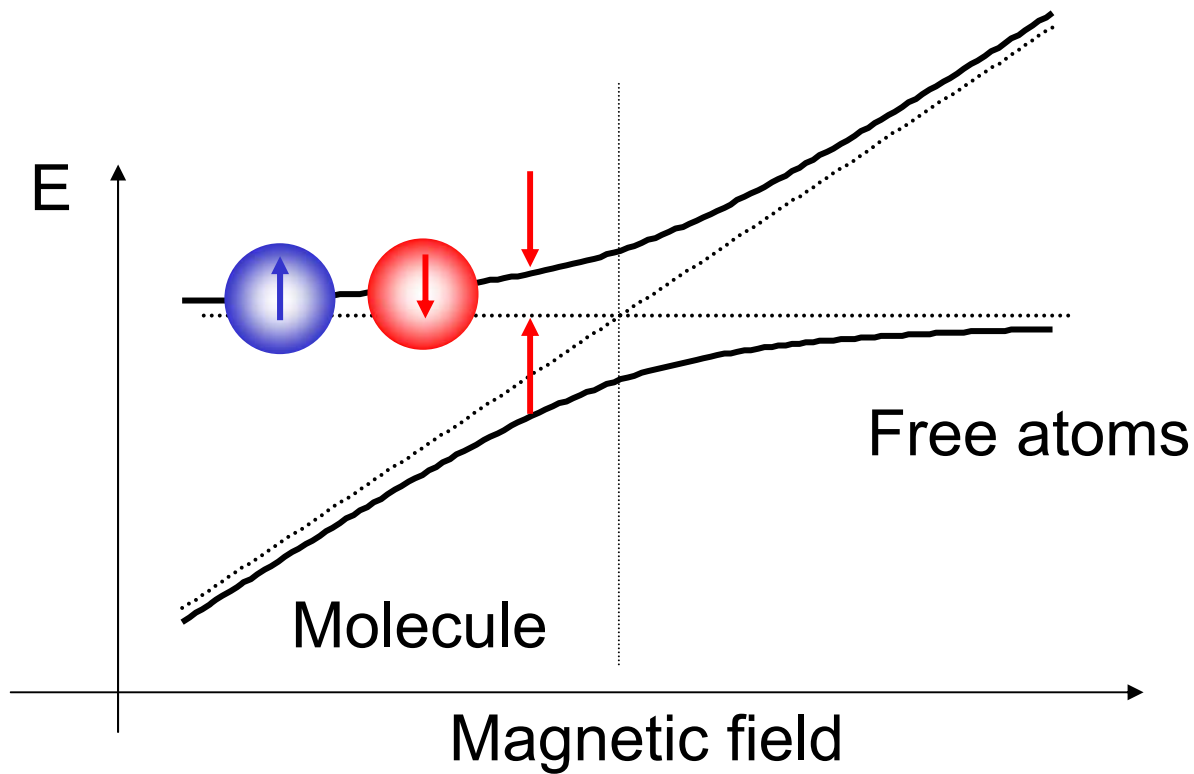


Feshbach resonance



Atoms repel each other

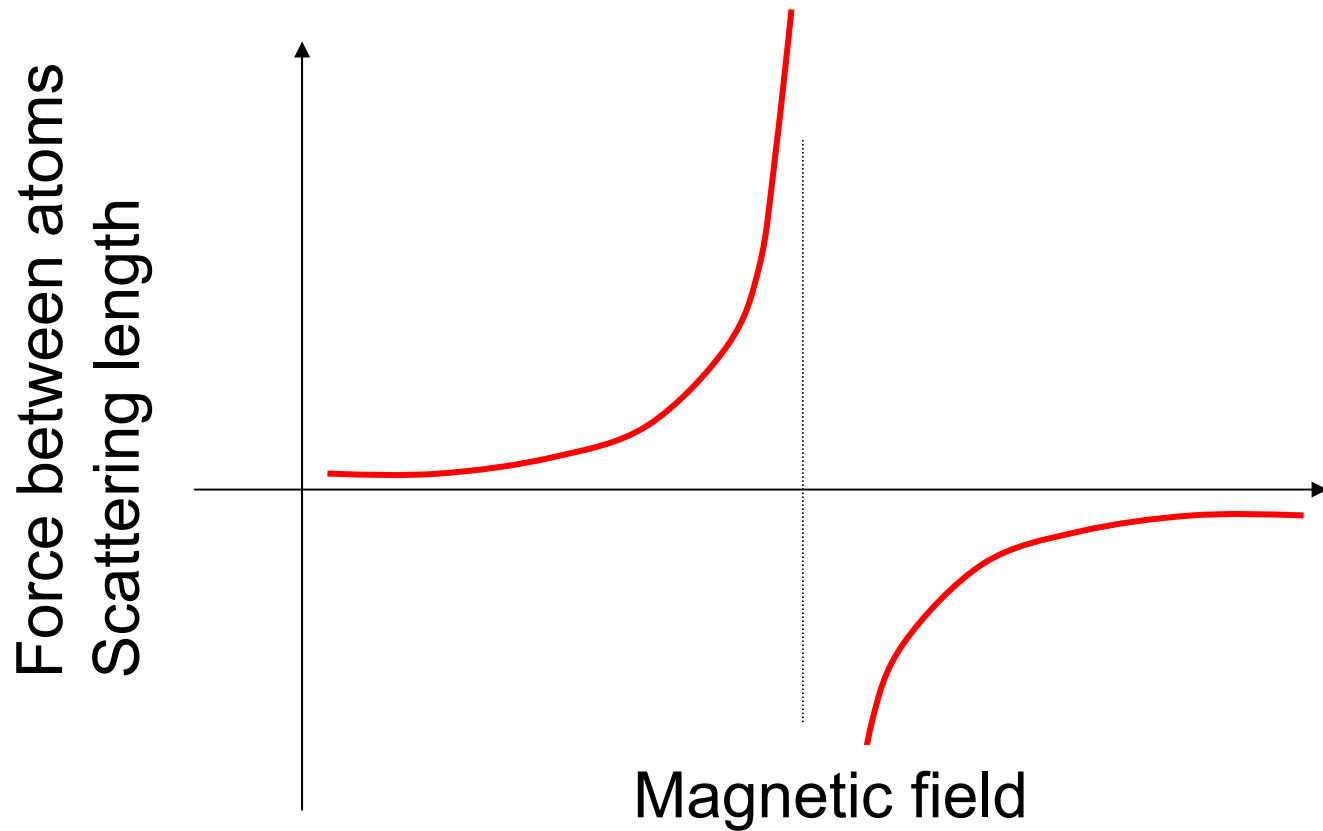
Atoms attract each other



Feshbach resonance

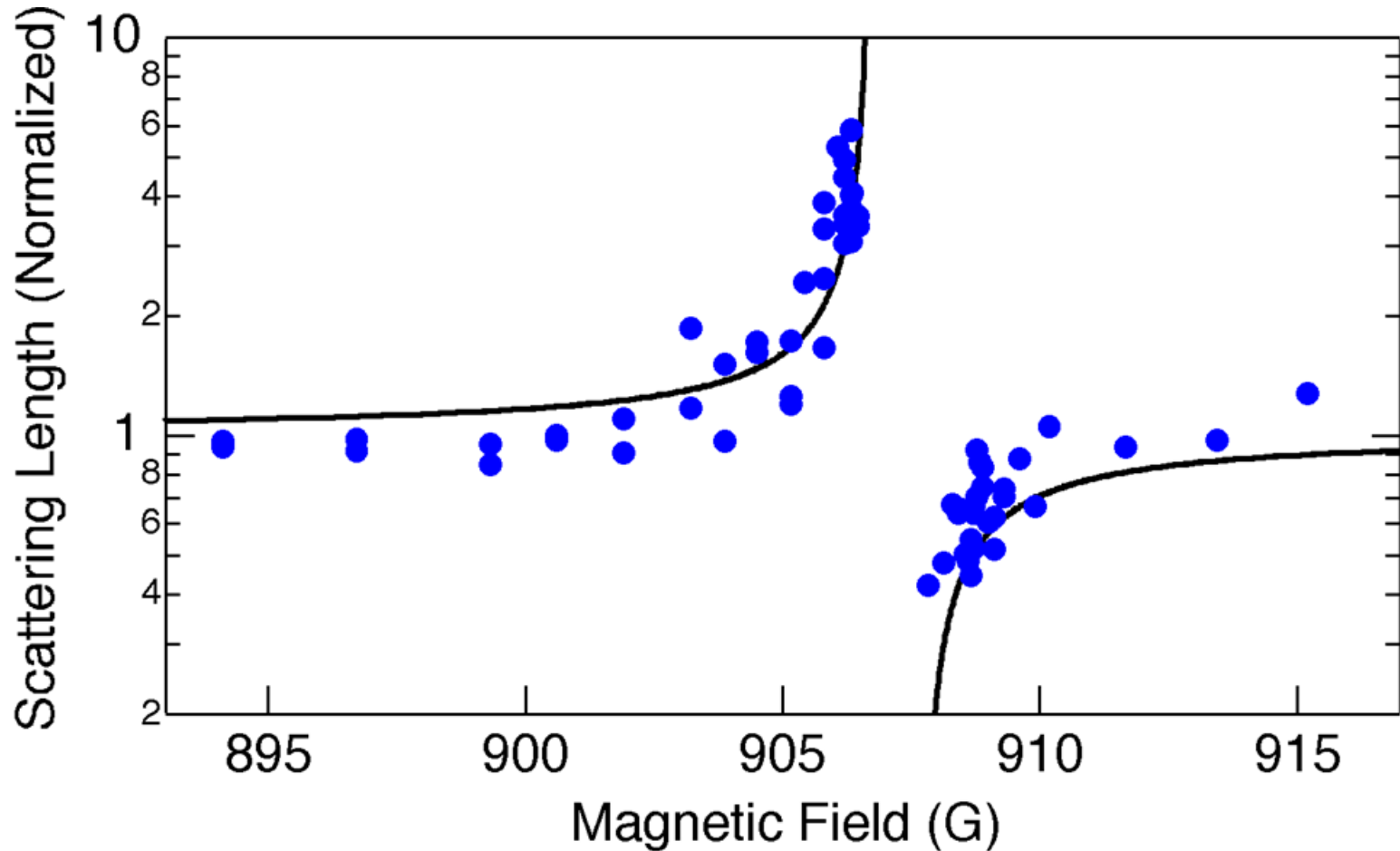
Atoms repel each other

Atoms attract each other



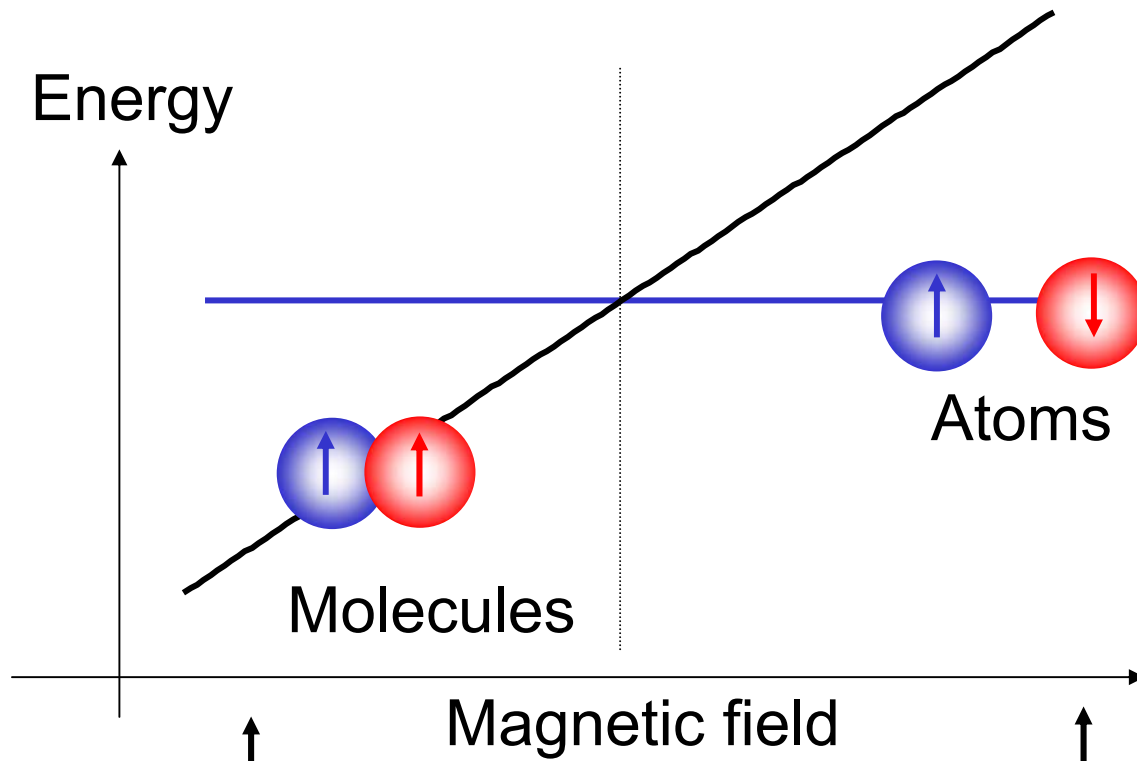
Feshbach resonance

# Observation of a Feshbach resonance



S. Inouye, M.R. Andrews, J. Stenger, H.-J. Miesner, D.M. Stamper-Kurn, WK,  
Nature **392** (1998).

# **Feshbach resonances in ultracold Fermi gases**



Atoms form stable molecules

**Atoms repel each other**  
 **$a > 0$**

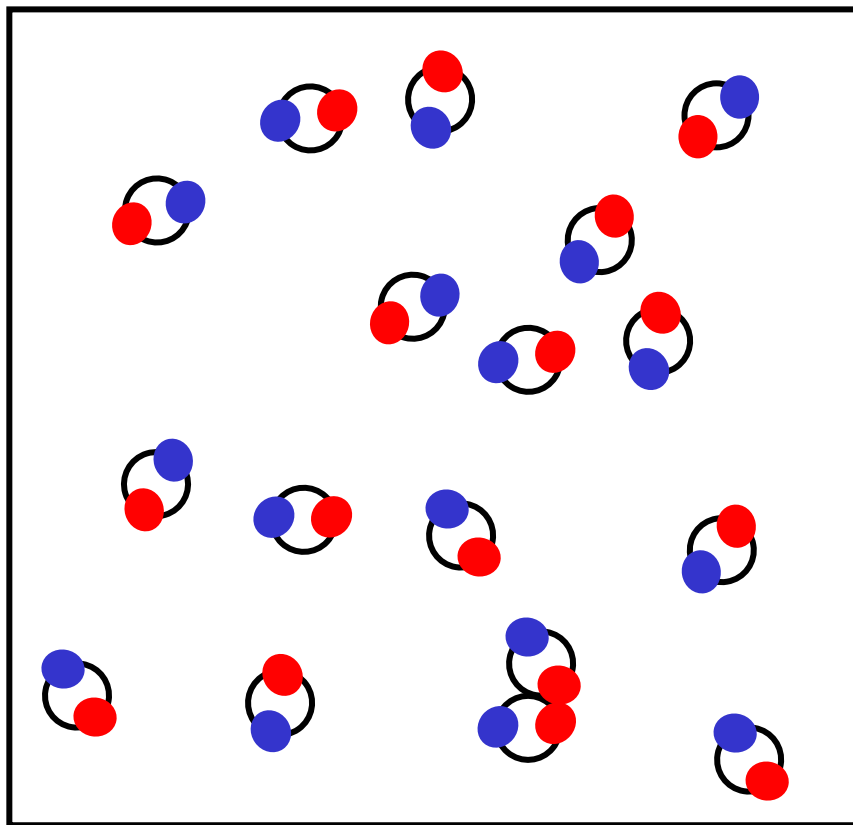
BEC of Molecules:  
Condensation of  
tightly bound fermion pairs

Molecules are unstable

**Atoms attract each other**  
 **$a < 0$**

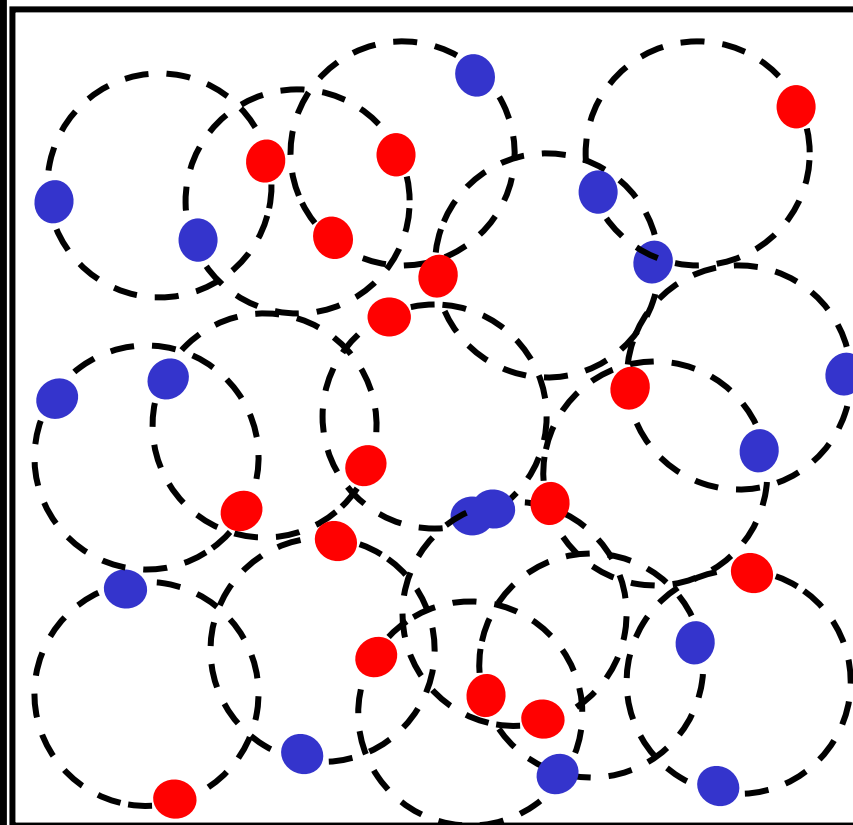
BCS-limit:  
Condensation of  
long-range Cooper pairs

Atom pairs

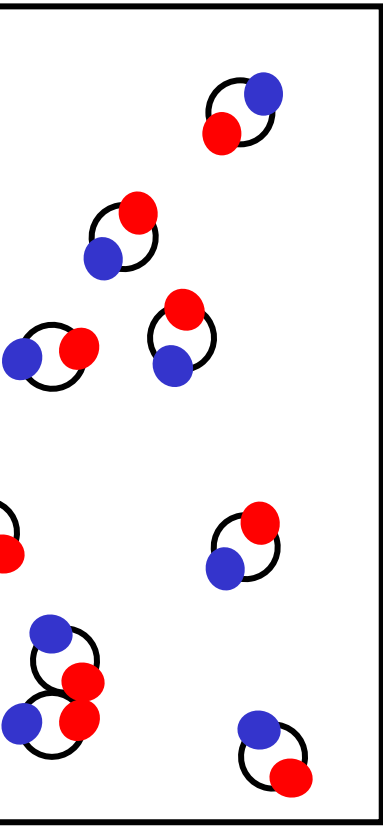


Bose Einstein condensate  
of molecules

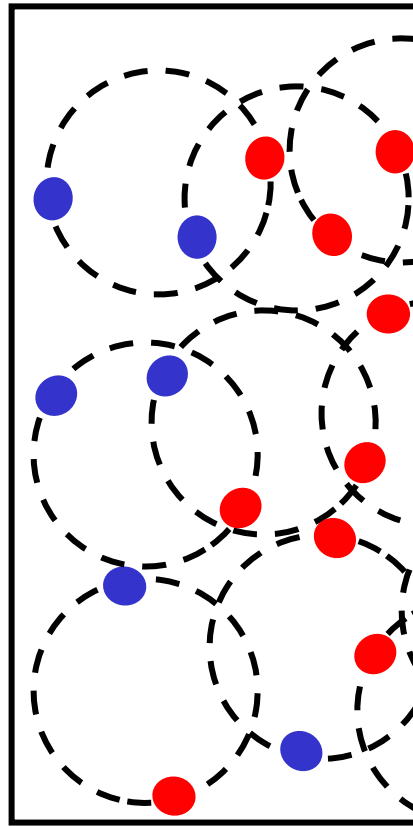
Electron pairs



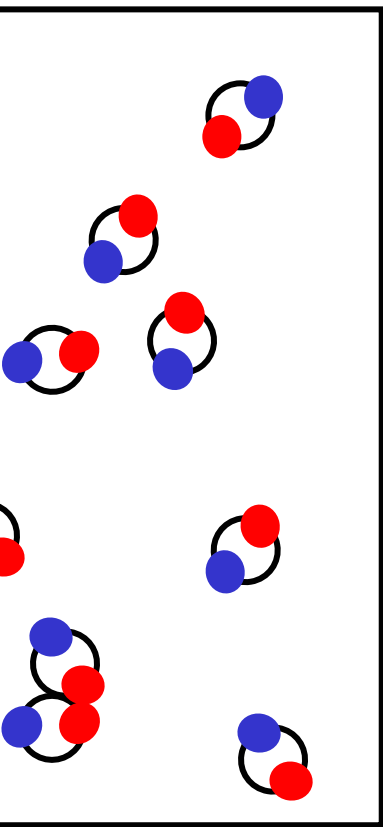
BCS Superconductor



BEC



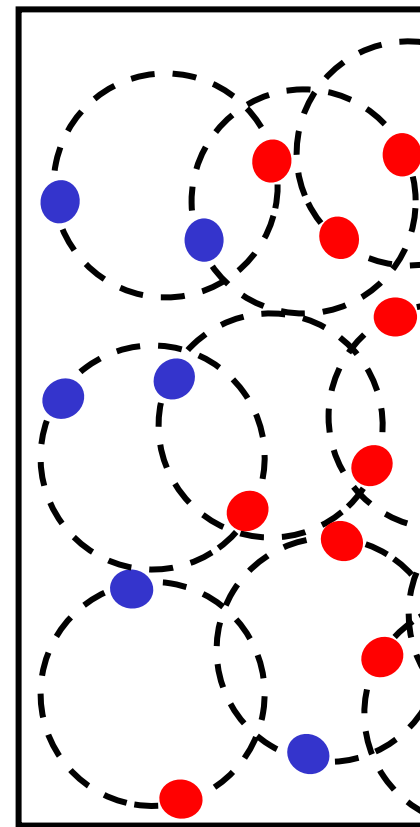
BCS sup



BEC

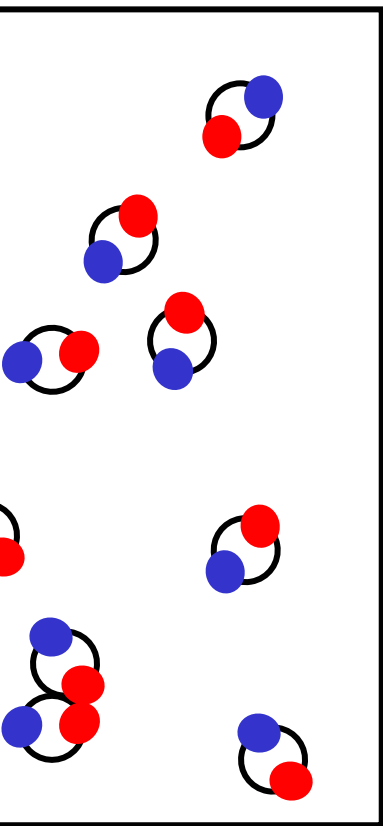


Magnetic field

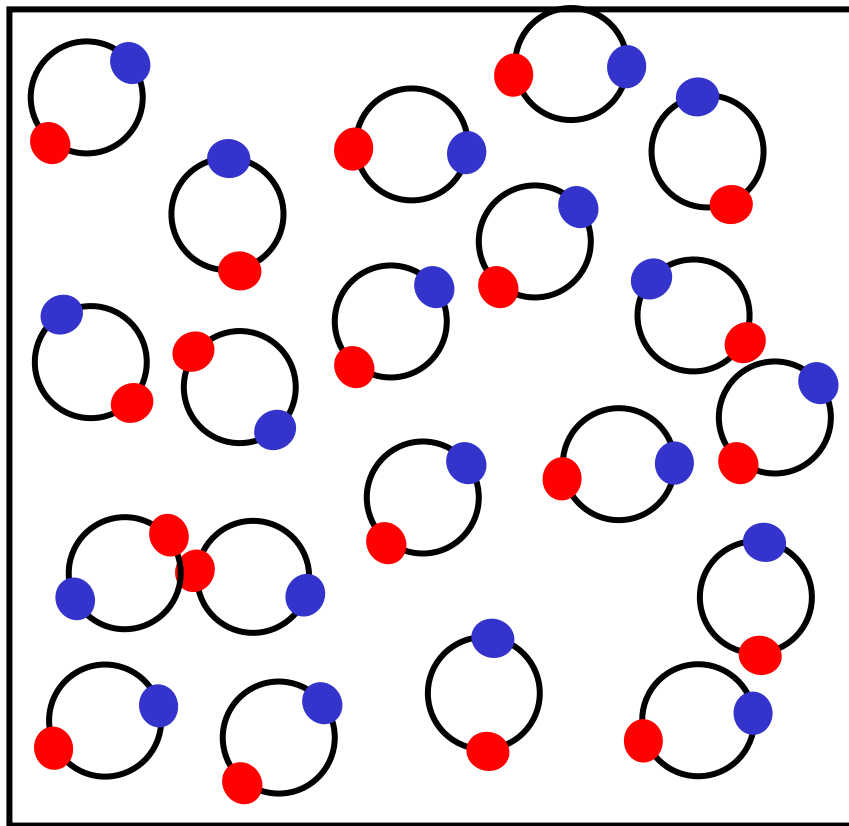


BCS sup

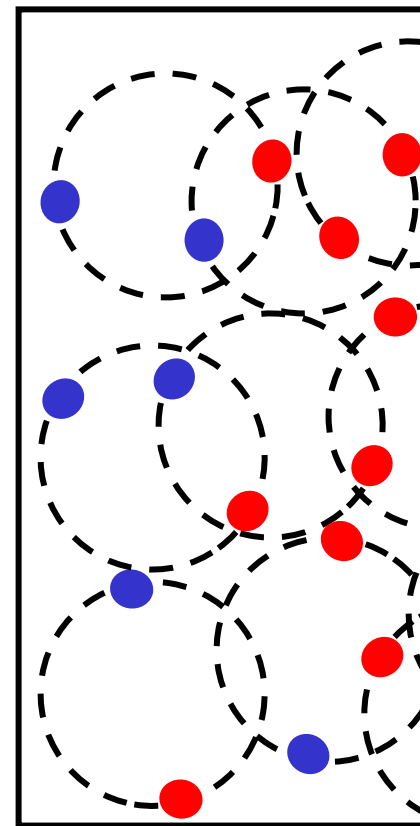




BEC



Crossover superfluid



BCS sup

# High-temperature superfluidity at 100 nK?

Transition temperature  $\approx$  Binding energy of pairs

Fermi temperature ← Fermi energy

$\propto (\text{density})^{2/3}$

$10^{-5}$  ...  $10^{-4}$

normal superconductors

$10^{-3}$

superfluid  $^3\text{He}$

$10^{-2}$

high  $T_c$  superconductors

**0.2**

**high  $T_c$  superfluid**

Scaled to the density of electrons in a solid:

**Superconductivity far above room temperature!**

BCS state

$$|Z_{\text{BCS}}\rangle = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}) |0\rangle$$

BCS state

$$|Z_{BCS}\rangle = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}) |0\rangle$$

Bound molecular pair

$$C_0^{\dagger} = \sum_{\mathbf{k}} \phi_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}$$

BCS state

$$|Z_{\text{BCS}}\rangle = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}) |0\rangle$$

Bound molecular pair

$$c_0^{\dagger} = \sum_{\mathbf{k}} \phi_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}$$

BEC state of  $N$  pairs

$$|Z_{\text{BEC}}\rangle = (c_0^{\dagger})^N |0\rangle$$

BCS state

$$|Z_{BCS}\rangle = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}) |0\rangle$$

Bound molecular pair

$$c_0^{\dagger} = \sum_{\mathbf{k}} \phi_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}$$

BEC state of  $N$  pairs

$$|Z_{BEC}\rangle = (c_0^{\dagger})^N |0\rangle$$

alternatively  $\exp(N^{1/2} c_0^{\dagger}) |0\rangle$

# BEC - BCS crossover

$$|Z_{\text{BEC}}\rangle = \exp\left(\sum_{\mathbf{k}} N^{1/2} \Phi_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}\right) |0\rangle$$

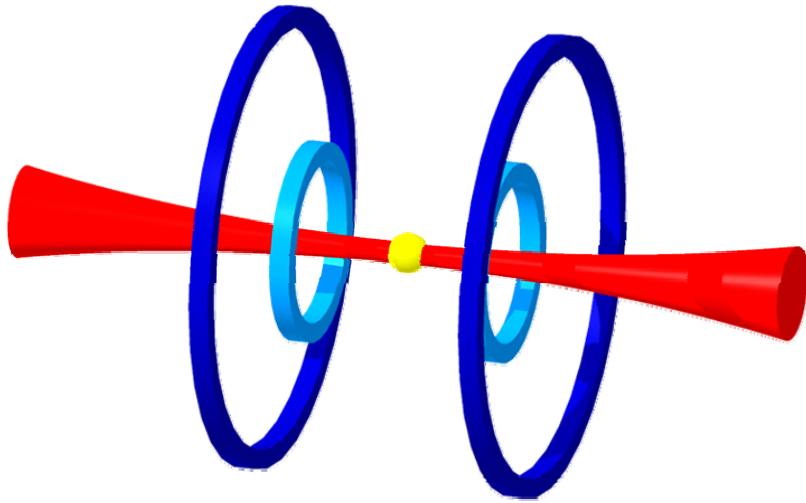
$$\approx \prod_{\mathbf{k}} \left(1 + N^{1/2} \Phi_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}\right) |0\rangle$$

$$\approx \prod_{\mathbf{k}} \left(u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^{\dagger} a_{-\mathbf{k},\downarrow}^{\dagger}\right) |0\rangle =$$

$$\text{with } v_{\mathbf{k}} = \frac{N^{1/2} \Phi_{\mathbf{k}}}{\underbrace{(1 + N |\Phi_{\mathbf{k}}|^2)^{1/2}}_{\approx 1}}$$

$$= |Z_{\text{BCS}}\rangle$$

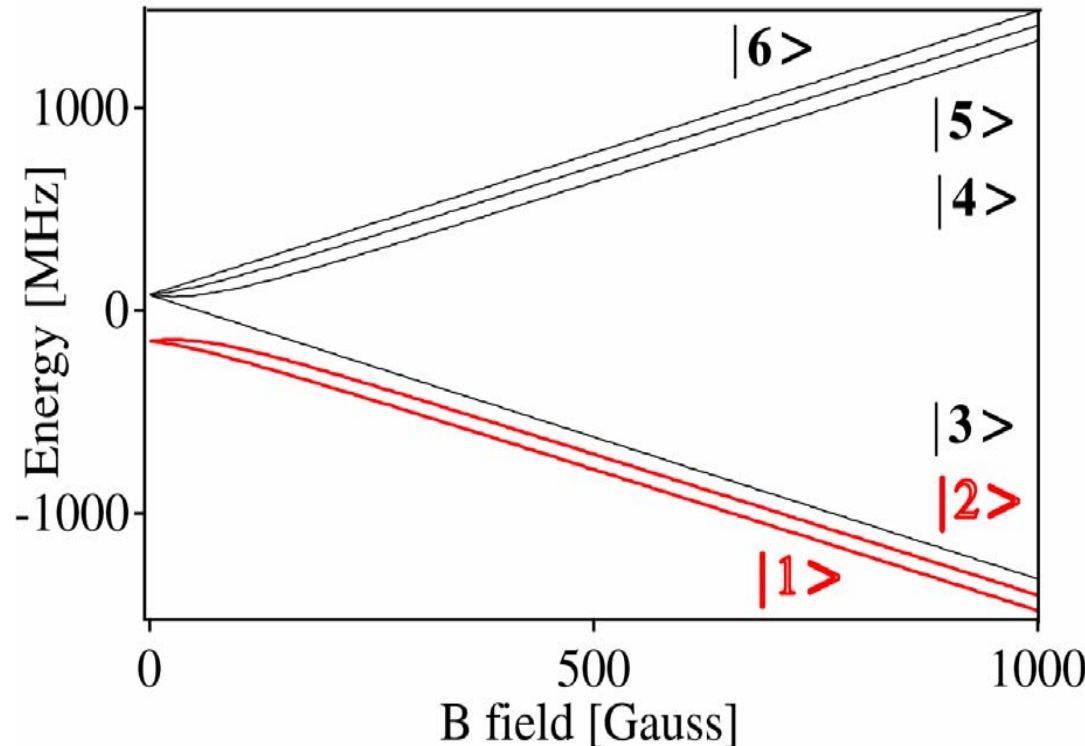
# Preparation of an interacting Fermi system in ${}^6\text{Li}$



Setup:

Optical trapping:  
9 W @ 1064 nm

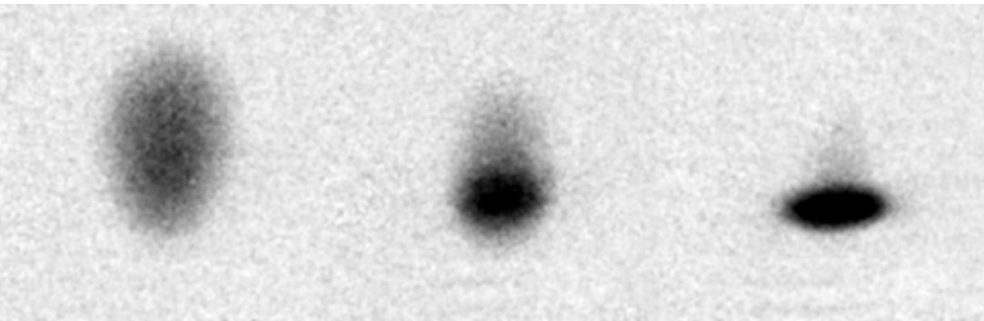
$\omega = 2\pi \times (16, 16, 0.19)$  kHz  
 $E_{\text{trap}} = 800 \mu\text{K}$



States  $|1\rangle$  and  $|2\rangle$  correspond to  $|\uparrow\rangle$  and  $|\downarrow\rangle$



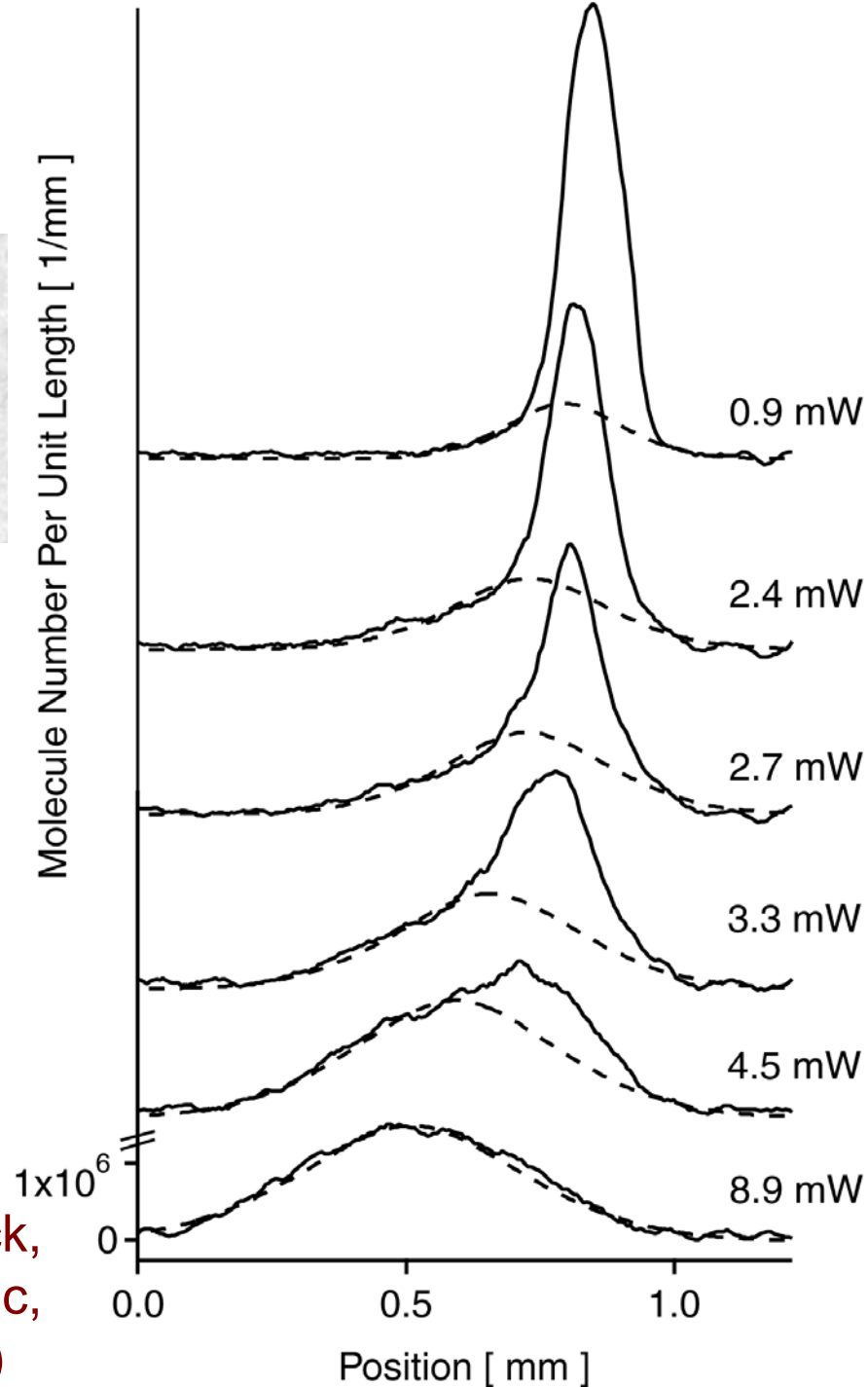
# BEC of Fermion Pairs (“Molecules”)



These days: Up to 10 million condensed molecules

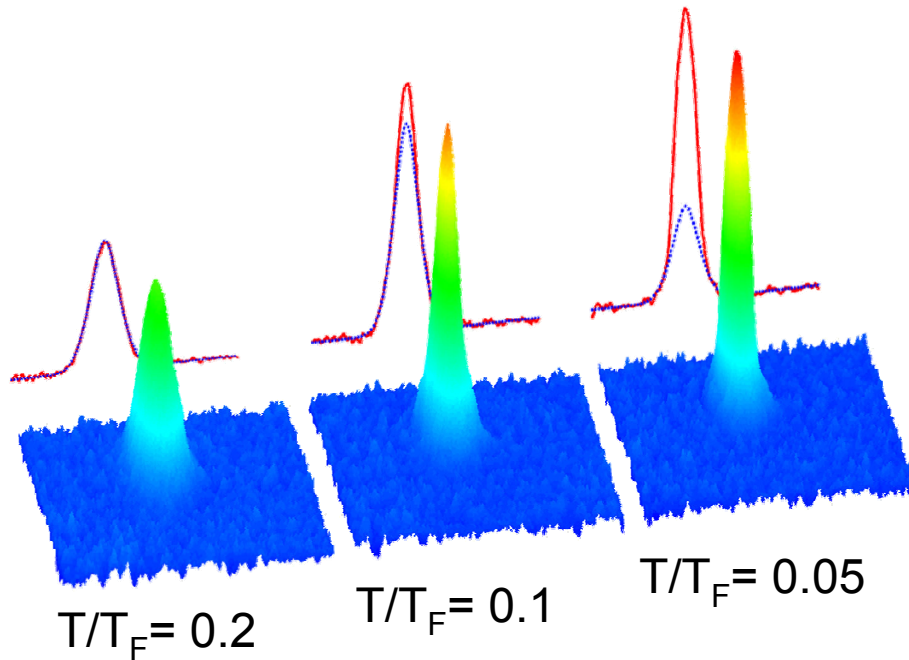
Boulder Nov '03  
Innsbruck Nov '03, Jan '04  
MIT Nov '03  
Paris March '04  
Rice, Duke

M.W. Zwierlein, C. A. Stan, C. H. Schunck, S.M. F. Raupach, S. Gupta, Z. Hadzibabic, W.K., Phys. Rev. Lett. 91, 250401 (2003)

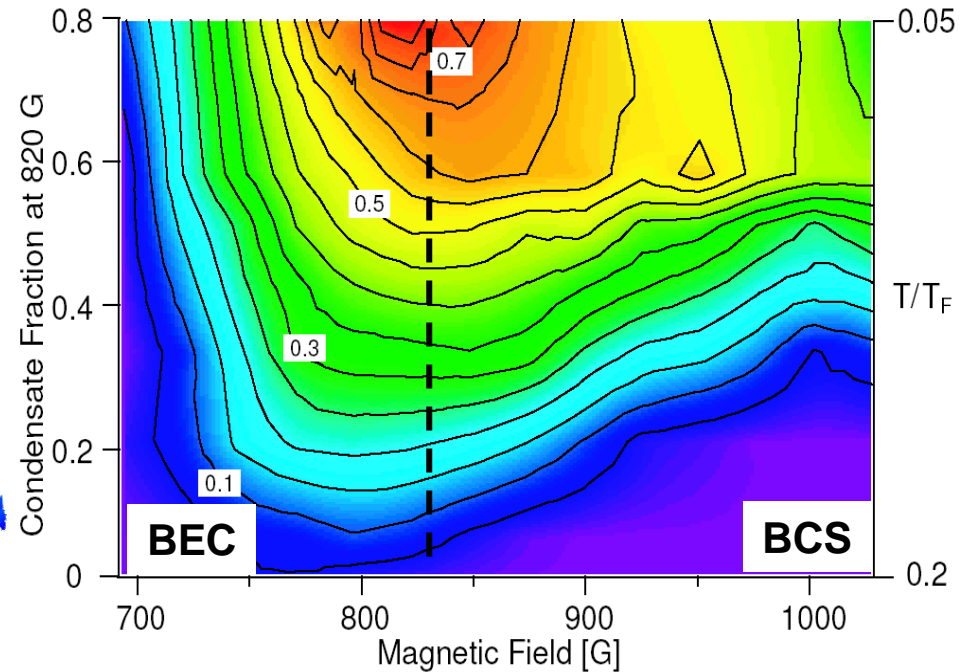


# Observation of Pair Condensates

At 900 G



Condensate Fraction



C.A. Regal *et al.*, PRL **92**, 040403 (2004)  
M.W. Zwierlein *et al.*, PRL **92**, 120403 (2004)

# Quantum degenerate fermions

Potassium  $^{40}\text{K}$

Boulder

Toronto

Florence

Mainz

Zürich

Hamburg

Lithium  $^6\text{Li}$

Rice

Tübingen

Paris

Duke

MIT

Innsbruck

Ytterbium  $^{173}\text{Yb}$

Kyoto

Helium  $^3\text{He}$

Amsterdam

Lots of work in progress:

more lithium, potassium (Munich, Melbourne, Amsterdam, Orsay,...), **chromium** (Stuttgart), **strontium** (Innsbruck)

# Characterization of the strongly interacting regime

## “Energy measurements”

Interaction energy  
Duke, Innsbruck, Paris, Rice, JILA

Specific heat  
Duke

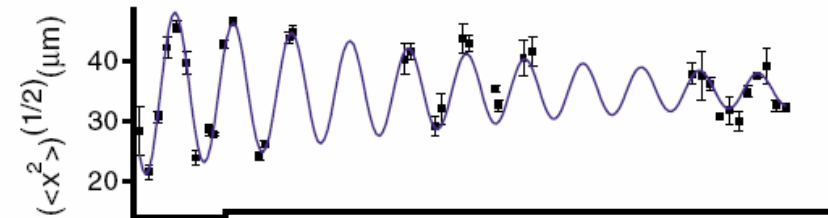
Momentum distribution  
JILA, Paris

## “Other”

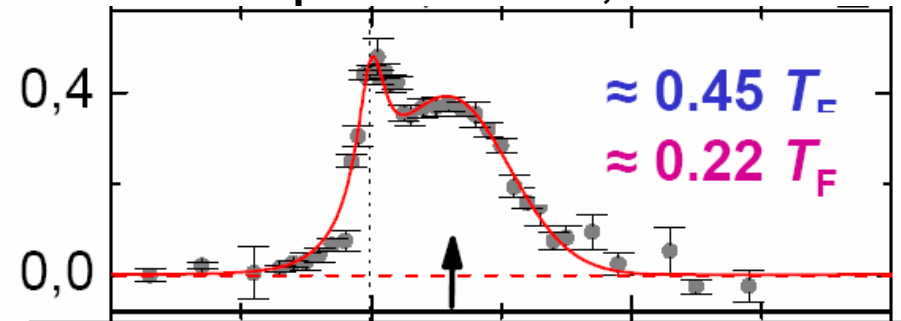
Condensate formation time  
MIT

Characterization of pairs  
Rice

## “Excitation measurements”



Collective excitation  
Innsbruck, Duke



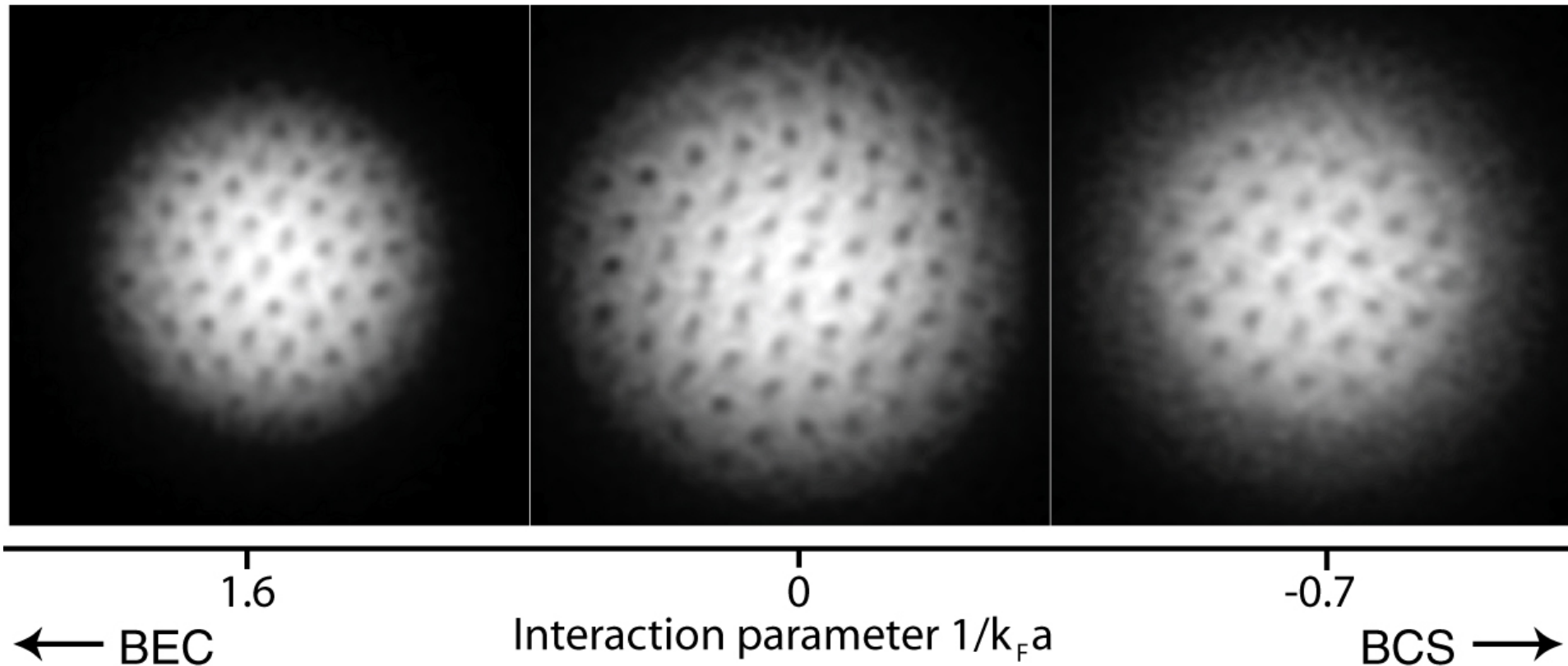
RF spectroscopy, pairing gap  
Innsbruck

Magnetic modulation spectrum  
JILA

Sound propagation, Duke 2006

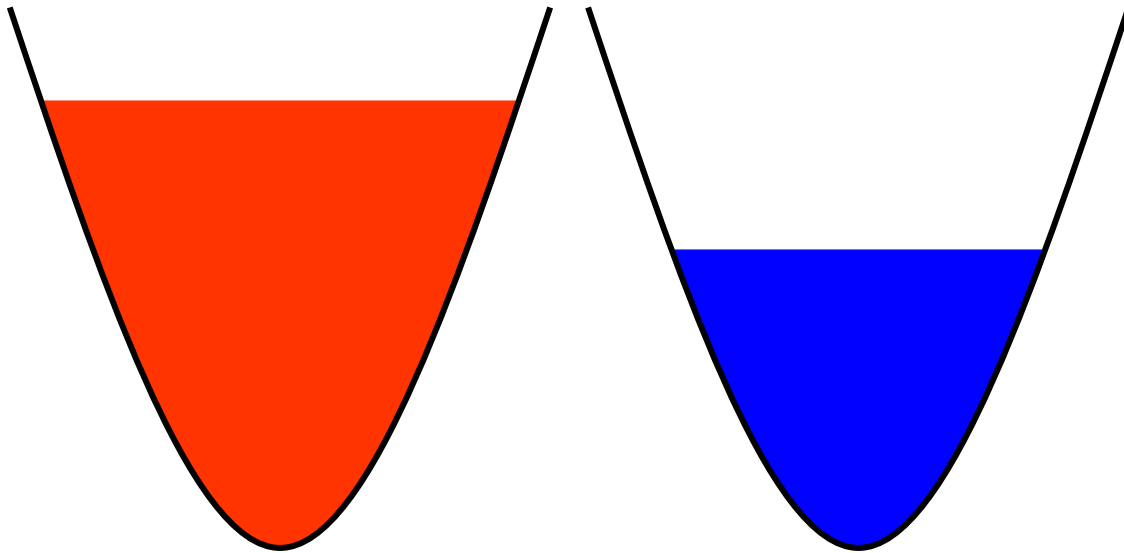
# Vortex lattices in the BEC-BCS crossover

This establishes **phase coherence** and **superfluidity** in gases of molecules and of fermionic atoms



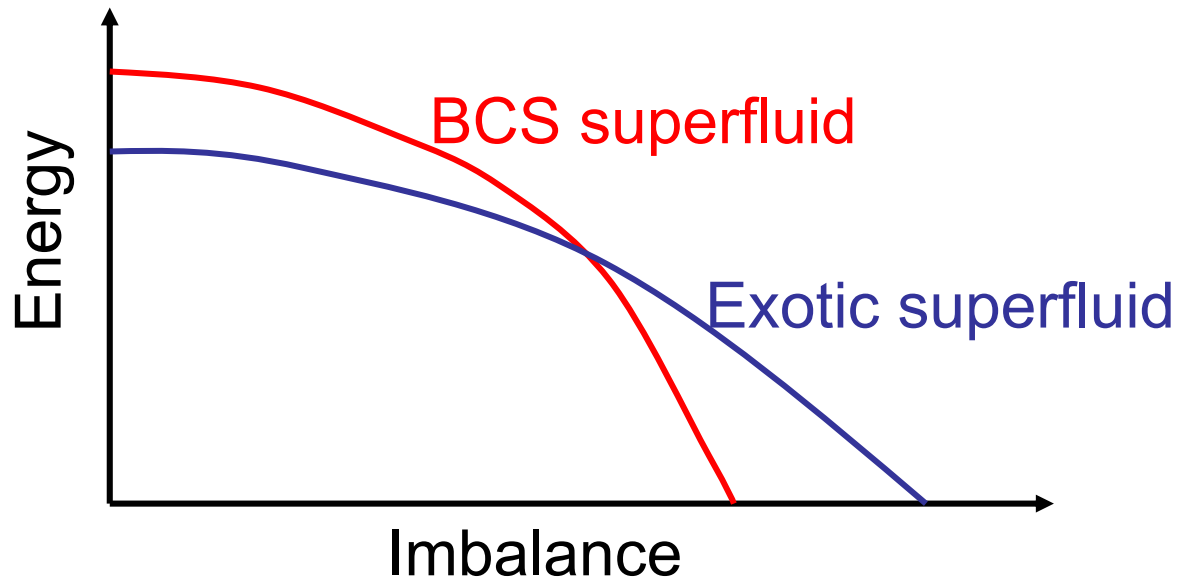
M.W. Zwierlein, J.R. Abo-Shaeer, A. Schirotzek, C.H. Schunck, W. Ketterle,  
Nature 435, 1047-1051 (2005)

# Fermionic Superfluidity with Imbalanced Spin Populations

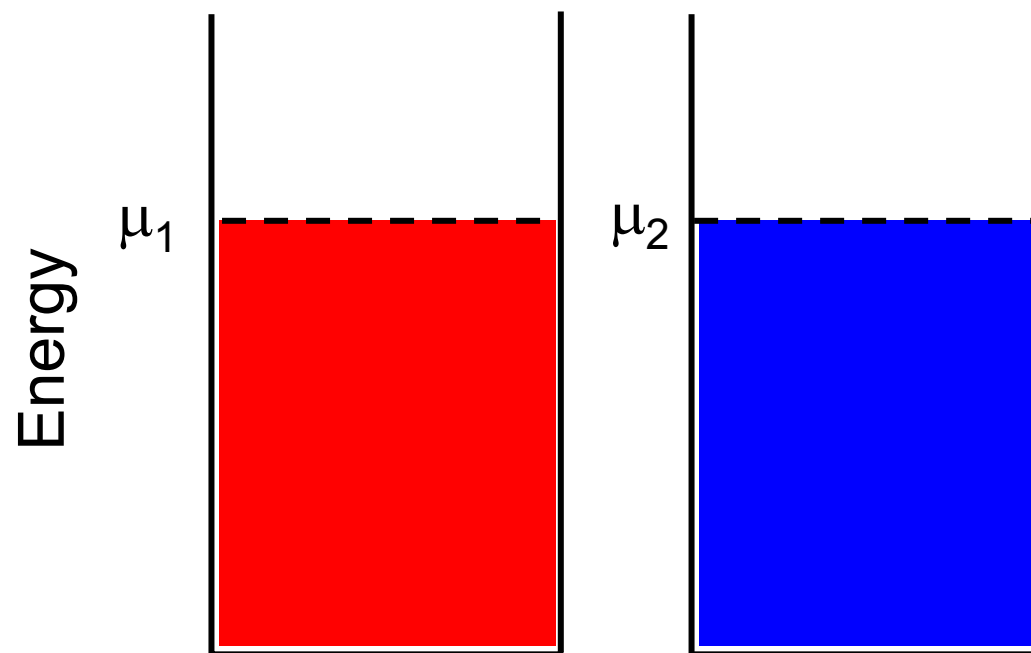


## Why is superfluidity with unequal Fermi energies interesting?

- Superfluidity in quarks involves unequal Fermi surfaces (due to different quark masses)
- New superfluid states predicted:



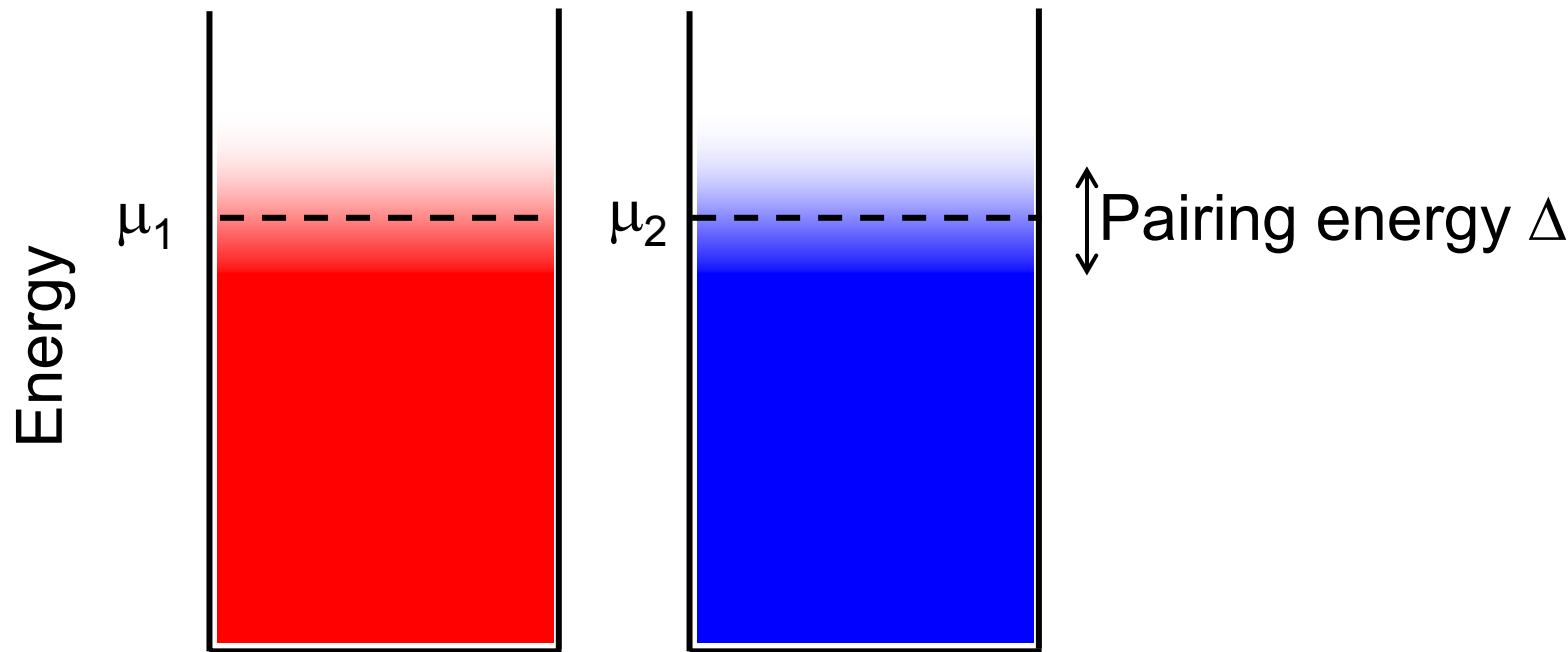
# BCS Pairing of Fermions



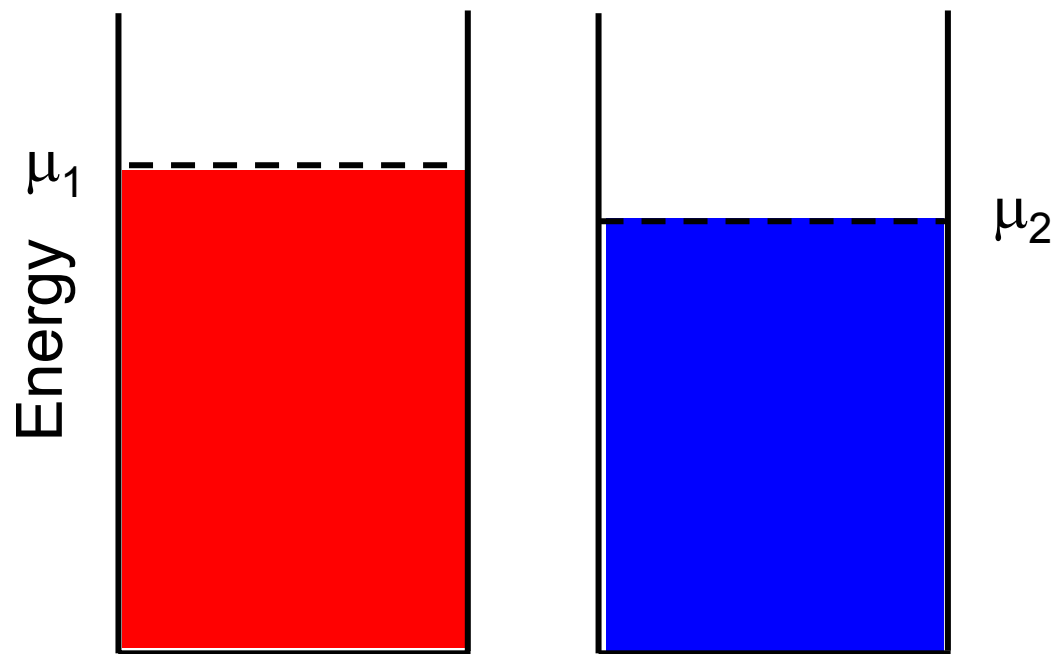


# BCS Pairing of Fermions

Pairing costs kinetic energy, but there is gain in potential energy (attractive interaction between fermions)

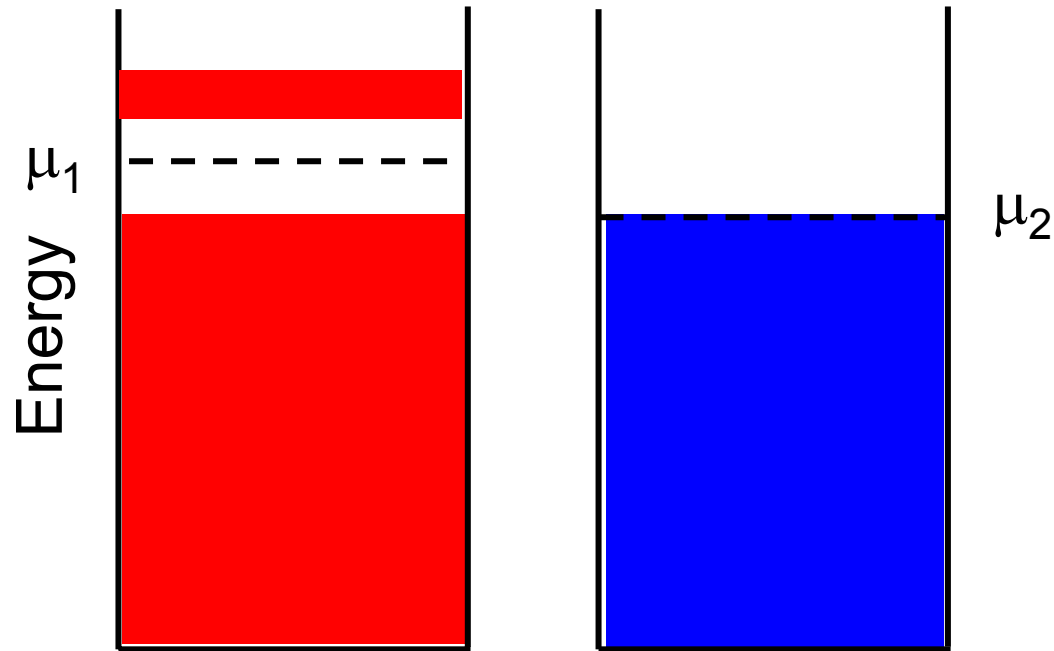


# Sarma state



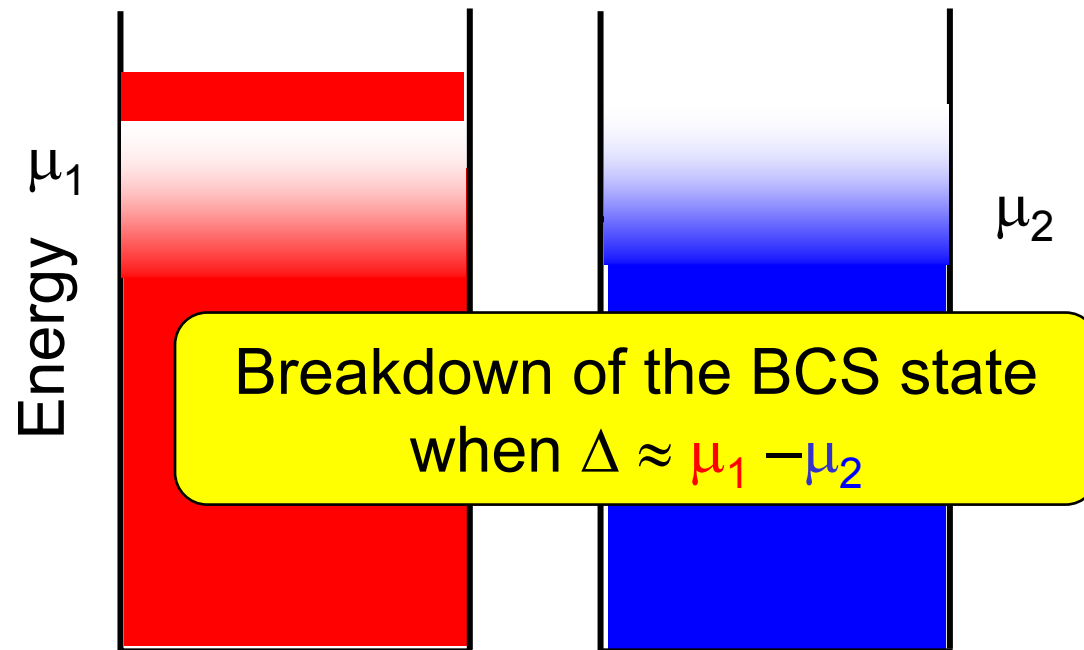
# Sarma state

Fraction of atoms  $(\mu_1 - \mu_2)/E_F$  moved up by  $\Delta$



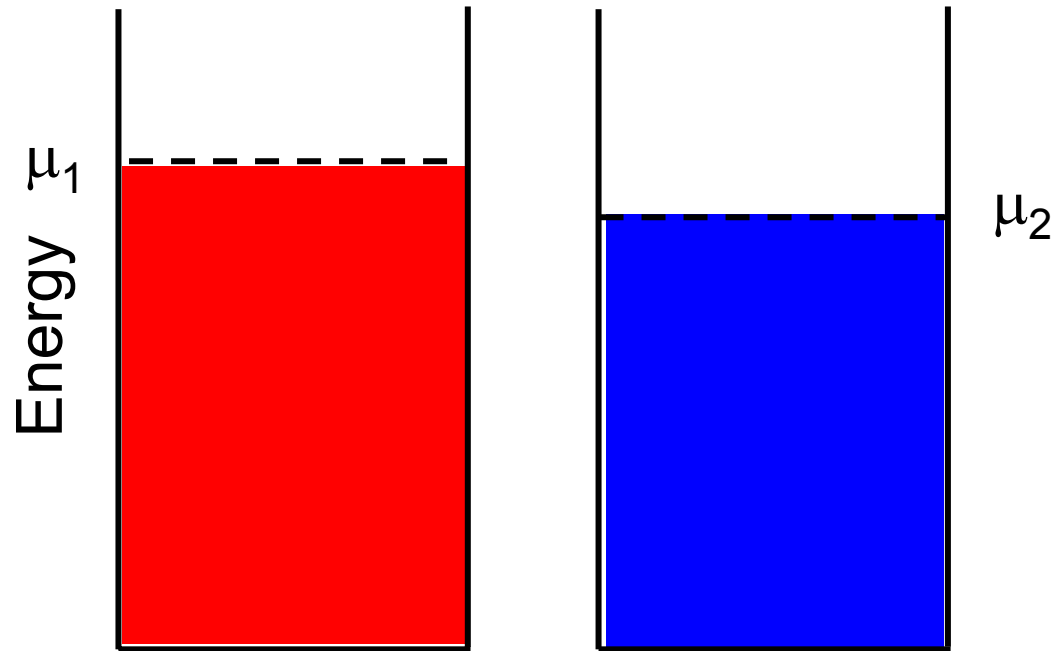
# Sarma state

Fraction of atoms  $(\mu_1 - \mu_2)/E_F$  moved up by  $\Delta$   
Fraction of atoms  $\Delta/E_F$  gain energy  $\Delta$



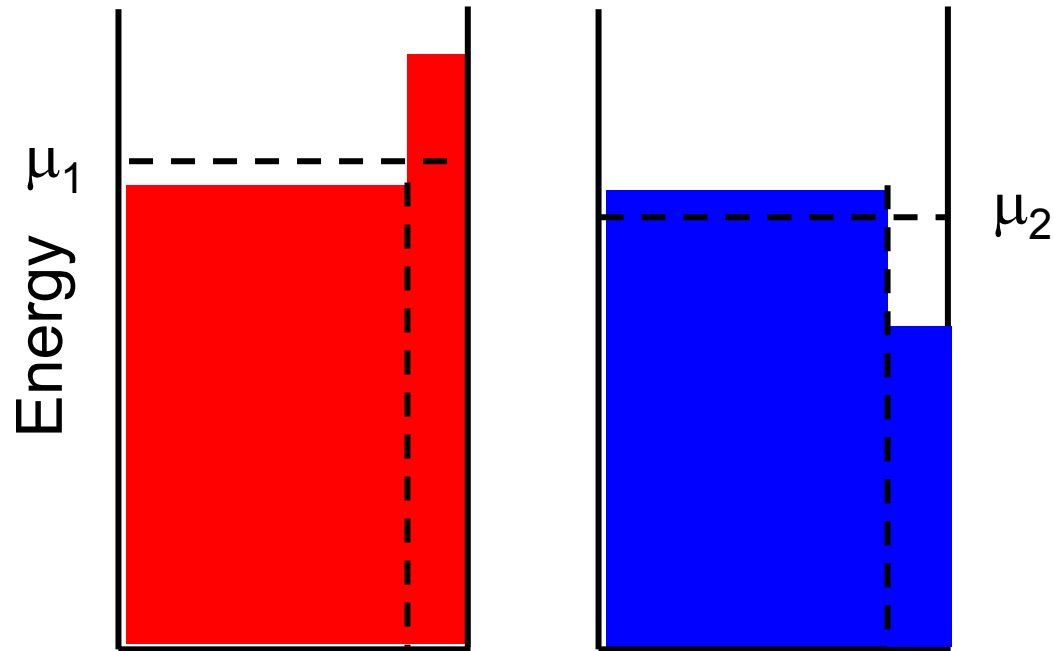
# BCS Pairing of Fermions

Phase separation (Bedaque, Caldas, Rupak 2003)



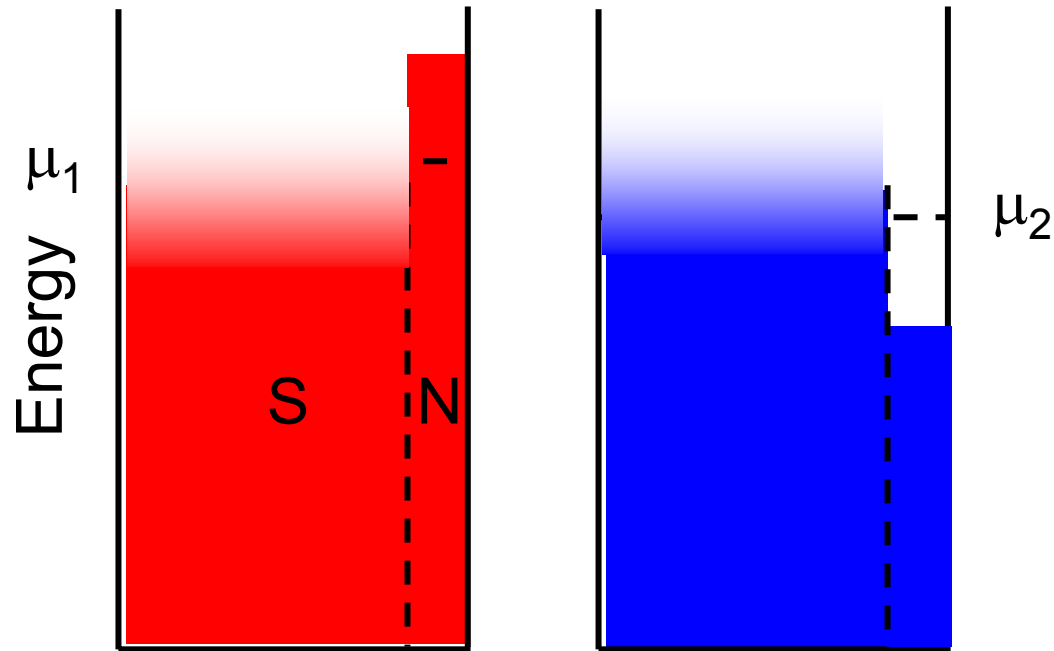
# BCS Pairing of Fermions

Phase separation (Bedaque, Caldas, Rupak 2003)



# BCS Pairing of Fermions

Phase separation (Bedaque, Caldas, Rupak 2003)



# Superfluid dance with unequal populations

Does an excess population of men stop the dance?

Do the excess men stay off the dance floor?

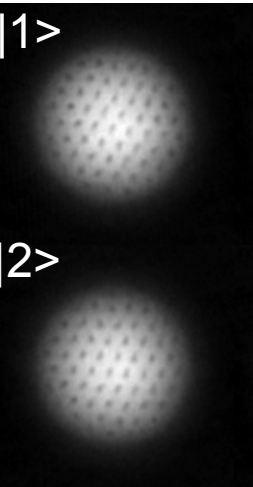
Do the excess men lead to a new dance where the partners are no longer matched?



# Fermionic Superfluidity with Imbalanced Spin Populations

BEC-Side 

$$1/k_F a = 0.2$$

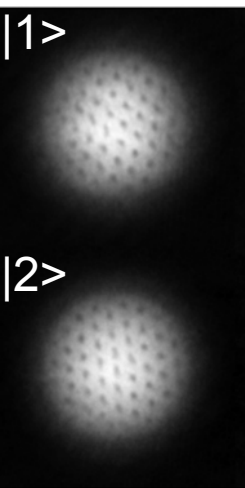


0%

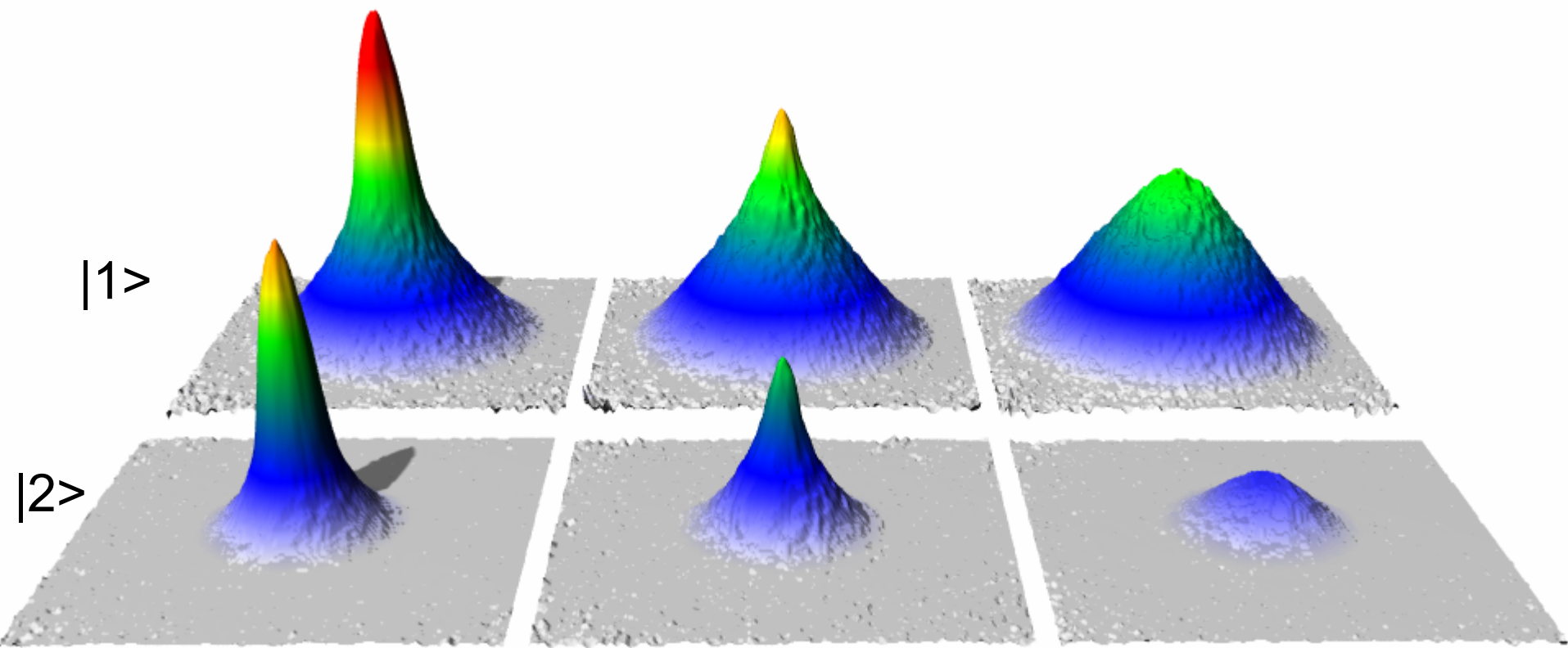
BCS-Side 

Population Imbalance:  $\delta = (N_2 - N_1) / (N_2 + N_1)$

$$1/k_F a = -0.15$$

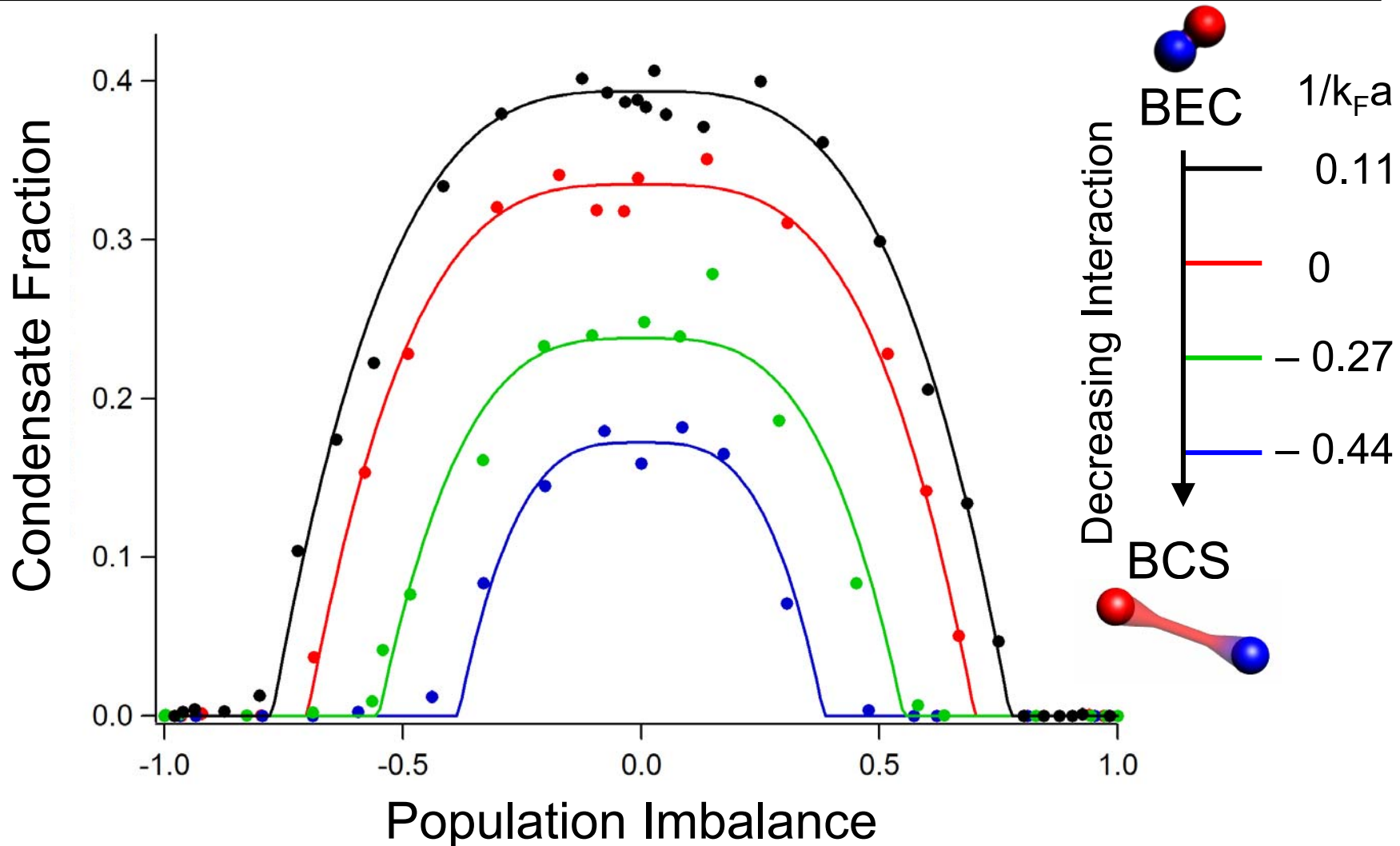


0%



Increase population imbalance

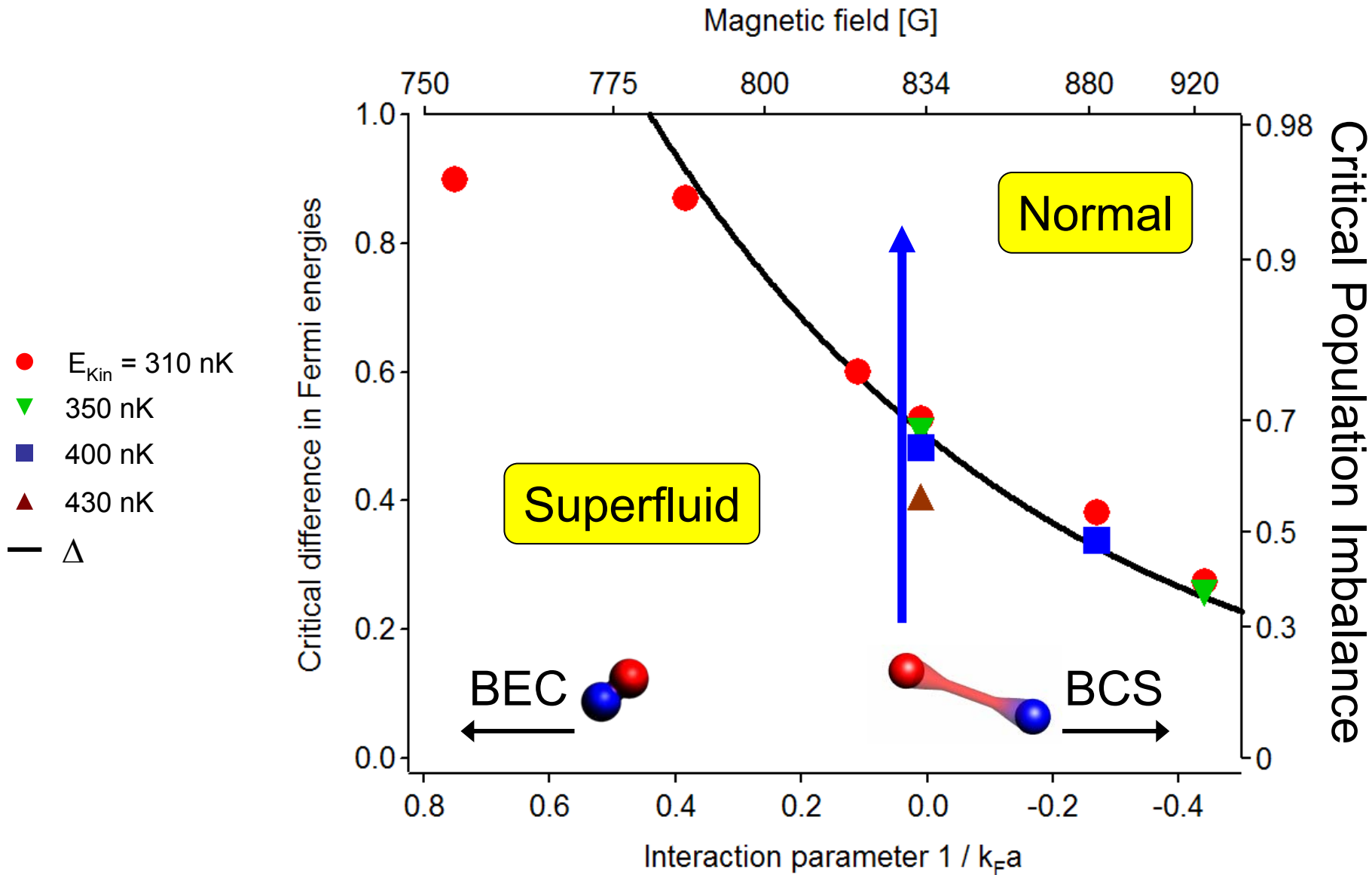
# The Window of Superfluidity



Superfluidity is robust in the strongly interacting regime!

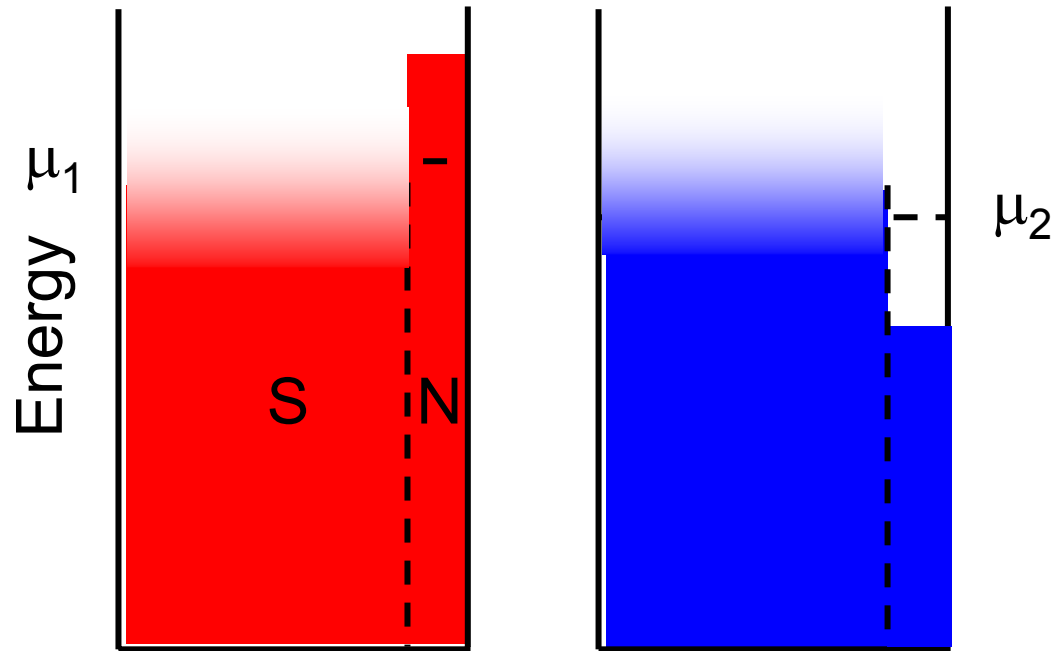
M.W. Zwierlein, A. Schirotzek, C.H. Schunck, W. Ketterle,  
Science 311, 492 (2006), published online on Science Express 21 December 2005

# Phase Diagram for Unequal Mixtures



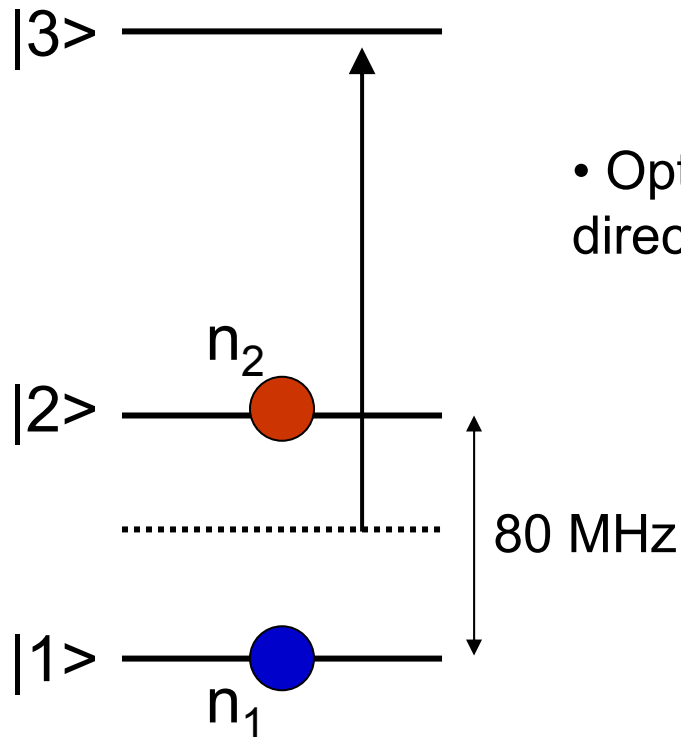
**Breakdown:** Critical mismatch in Fermi energies  $\Delta E_F \approx \text{Gap } \Delta$

# What is the nature of the superfluid state?

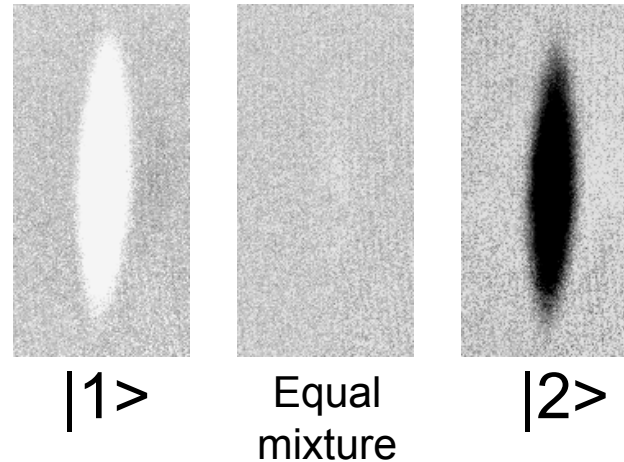


# Phase Contrast Imaging

- Imaging beam **red**-detuned for  $|1\rangle$ ,  
**blue**-detuned for  $|2\rangle$
- Optical signal of phase-contrast imaging directly measures density difference  $\Delta n = n_2 - n_1$

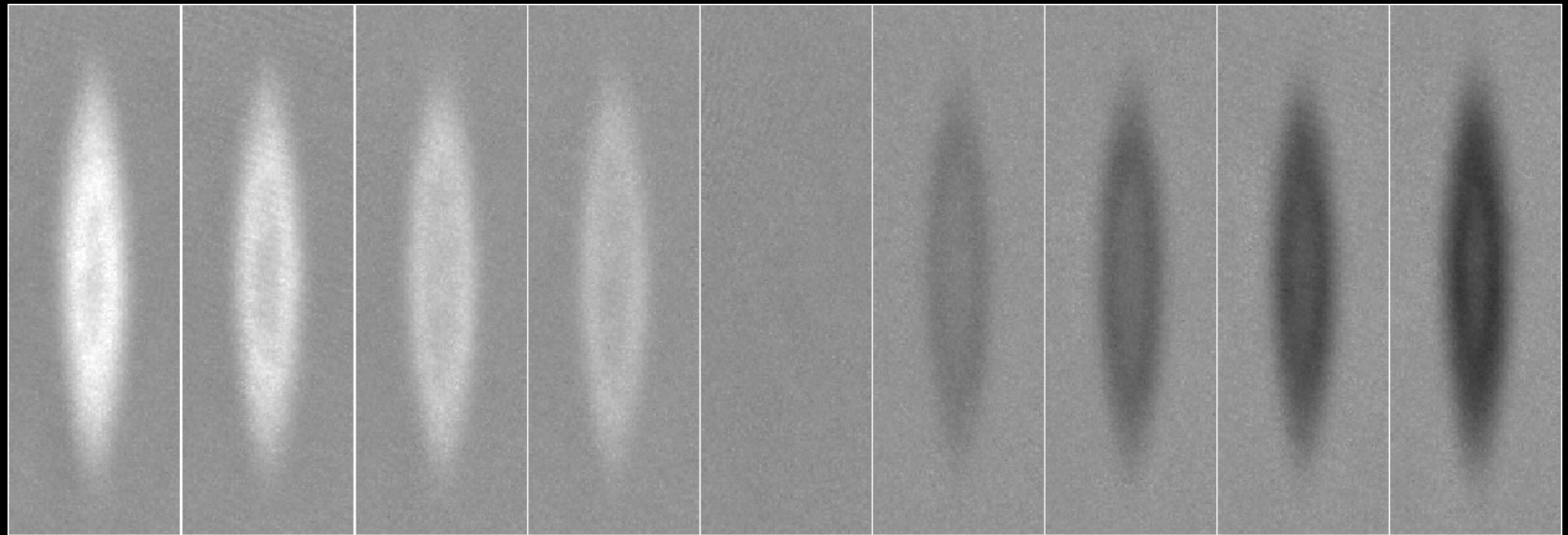


Li linewidth:  $\Gamma = 6$  MHz



In-trap images

# Direct imaging of the density difference



-50%

-37%

-30%

-24%

0%

20%

30%

40%

50%

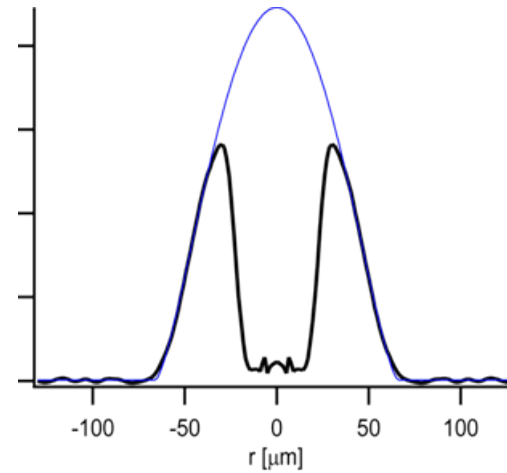
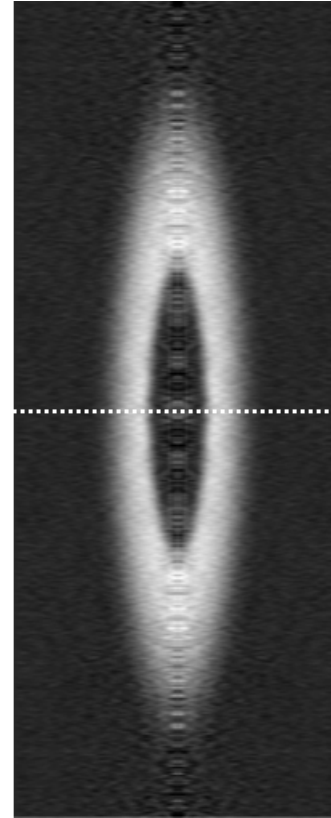
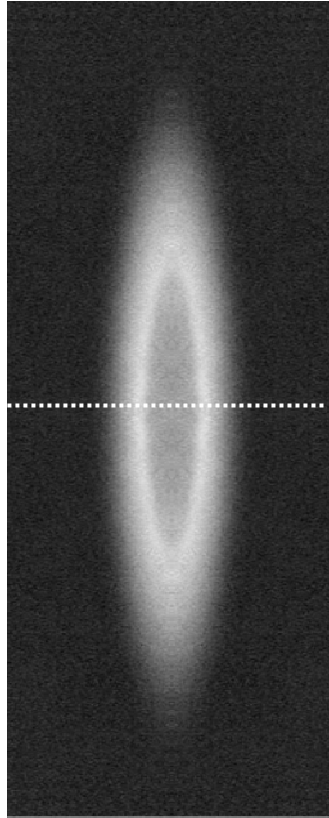
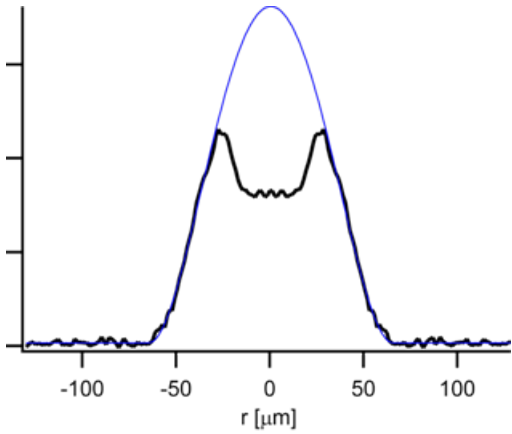
Population imbalance

The shell structure is a hint of the phase separation.

# Reconstruction of 3D density profile

$\delta=0.6$

Only assumption: cylindrical symmetry

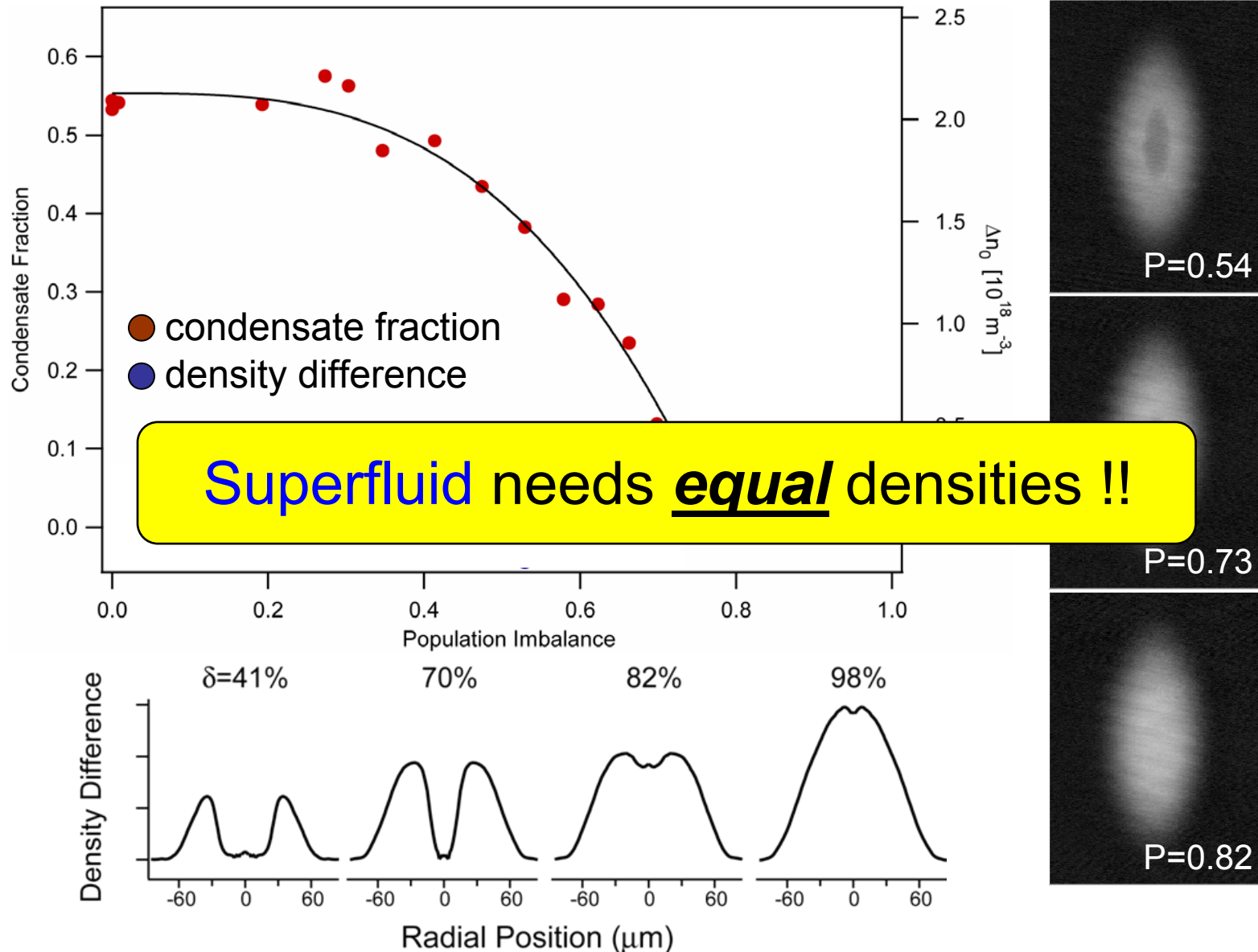


*Phase Separation !!*



# Superfluidity vs Polarization

Strategy: Correlation of Superfluidity and Central Polarization

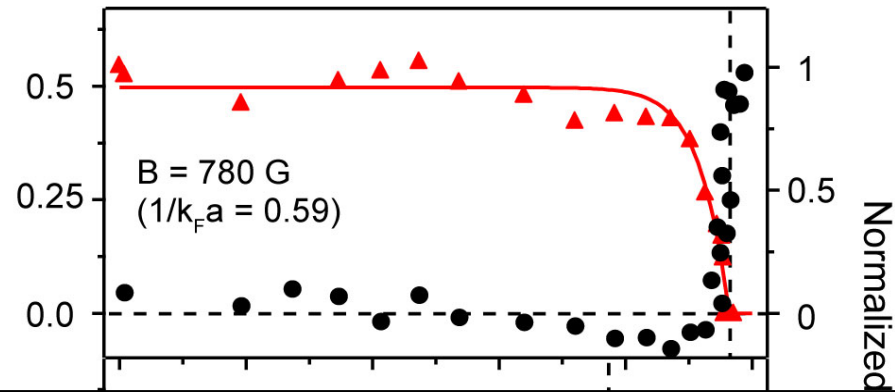


# Phase Separation of a Polarized Fermi Gas

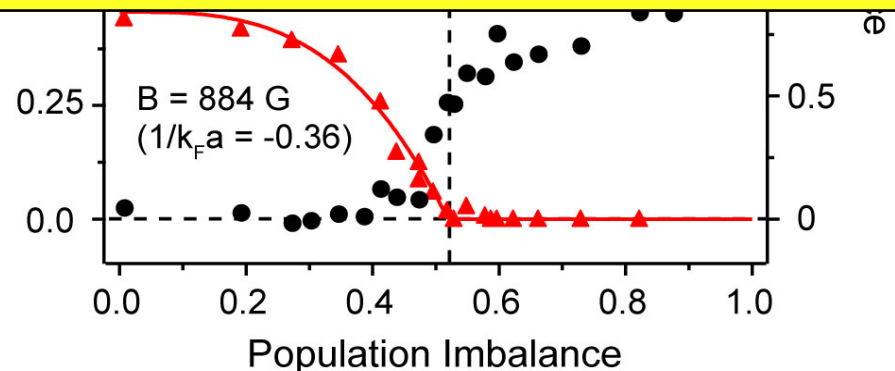
BEC-side

resonance

ion



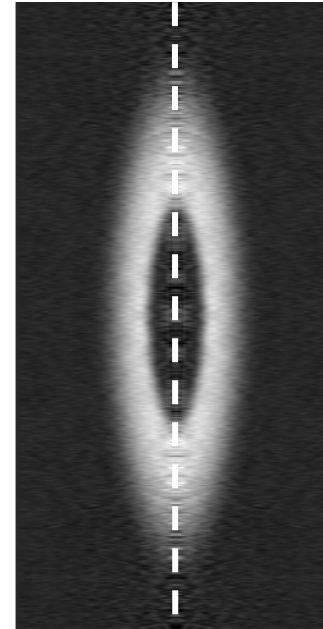
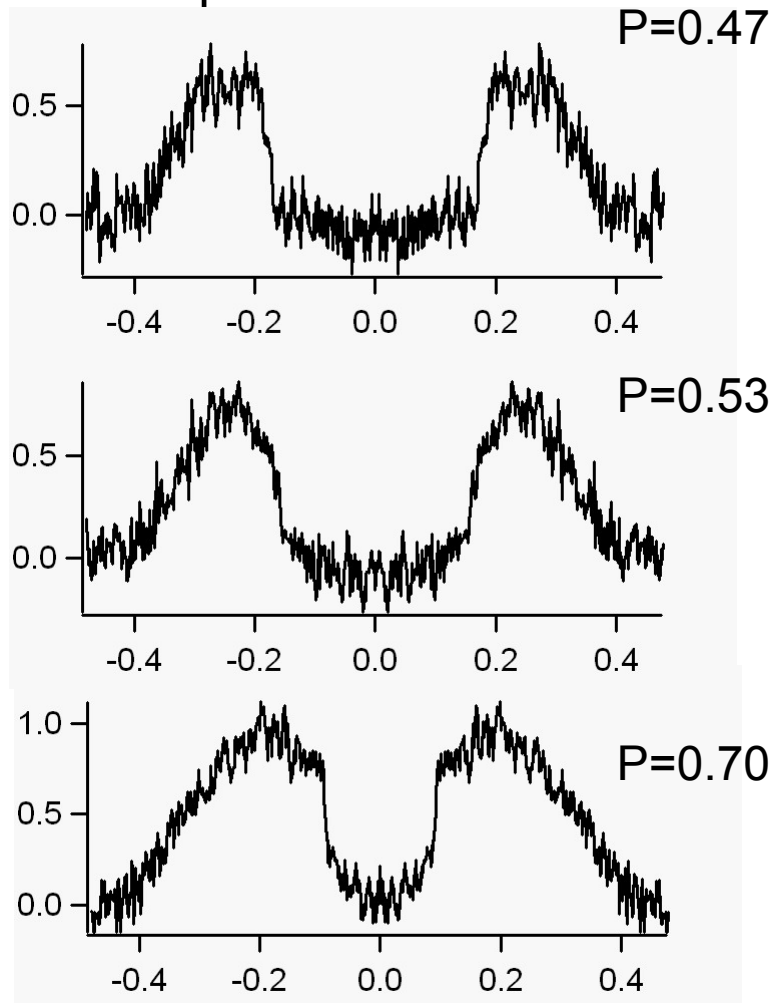
a **Superfluid** region of **equal** densities  
is spatially separated from  
a **Normal** region of non-equal densities



# Phase Separation: First-order Phase Transition ?

Sharpness of the boundary (the intermediate region)

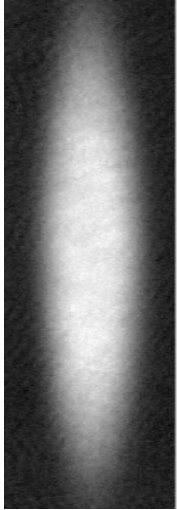
Axial profiles



# Direct Observation of Phase Transition

---

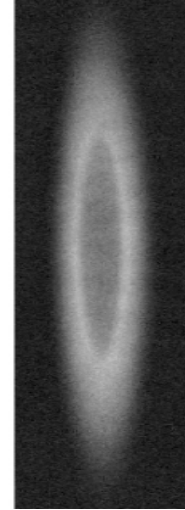
Normal



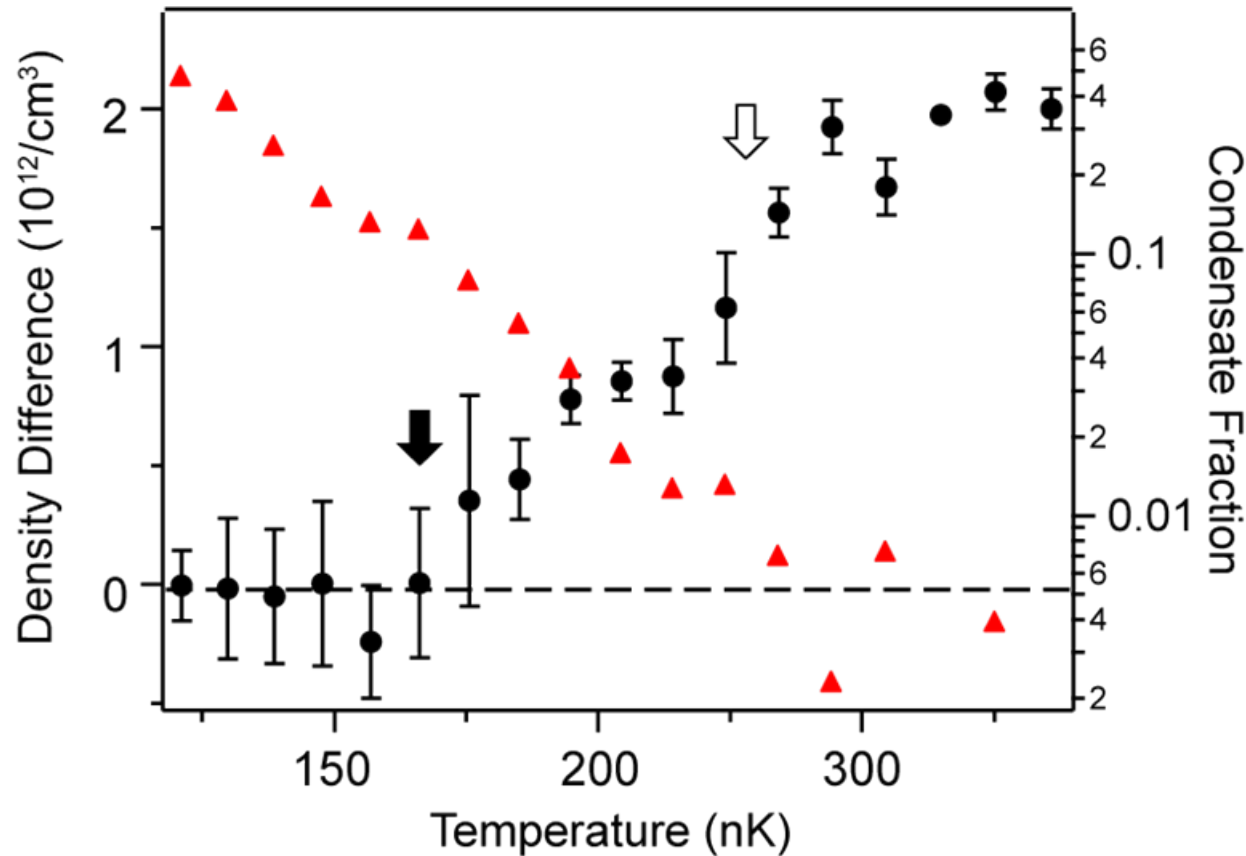
Cooling down



Superfluid



# Finite Temperature Effects

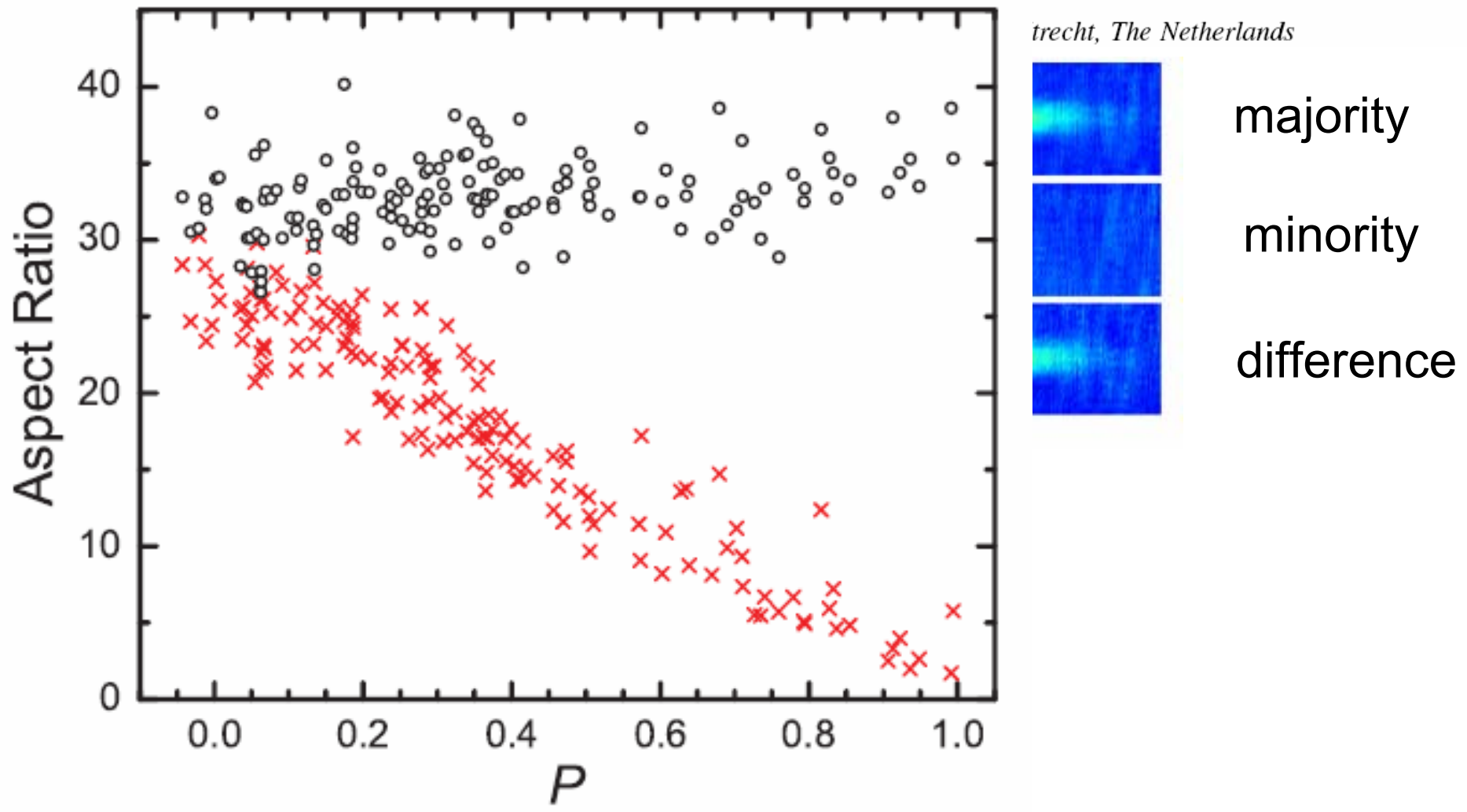


- Temperature-induced polarized superfluid.
- Thermal population of quasiparticles ( $k_B T > \Delta$ )

# Deformation of a Trapped Fermi Gas with Unequal Spin Populations

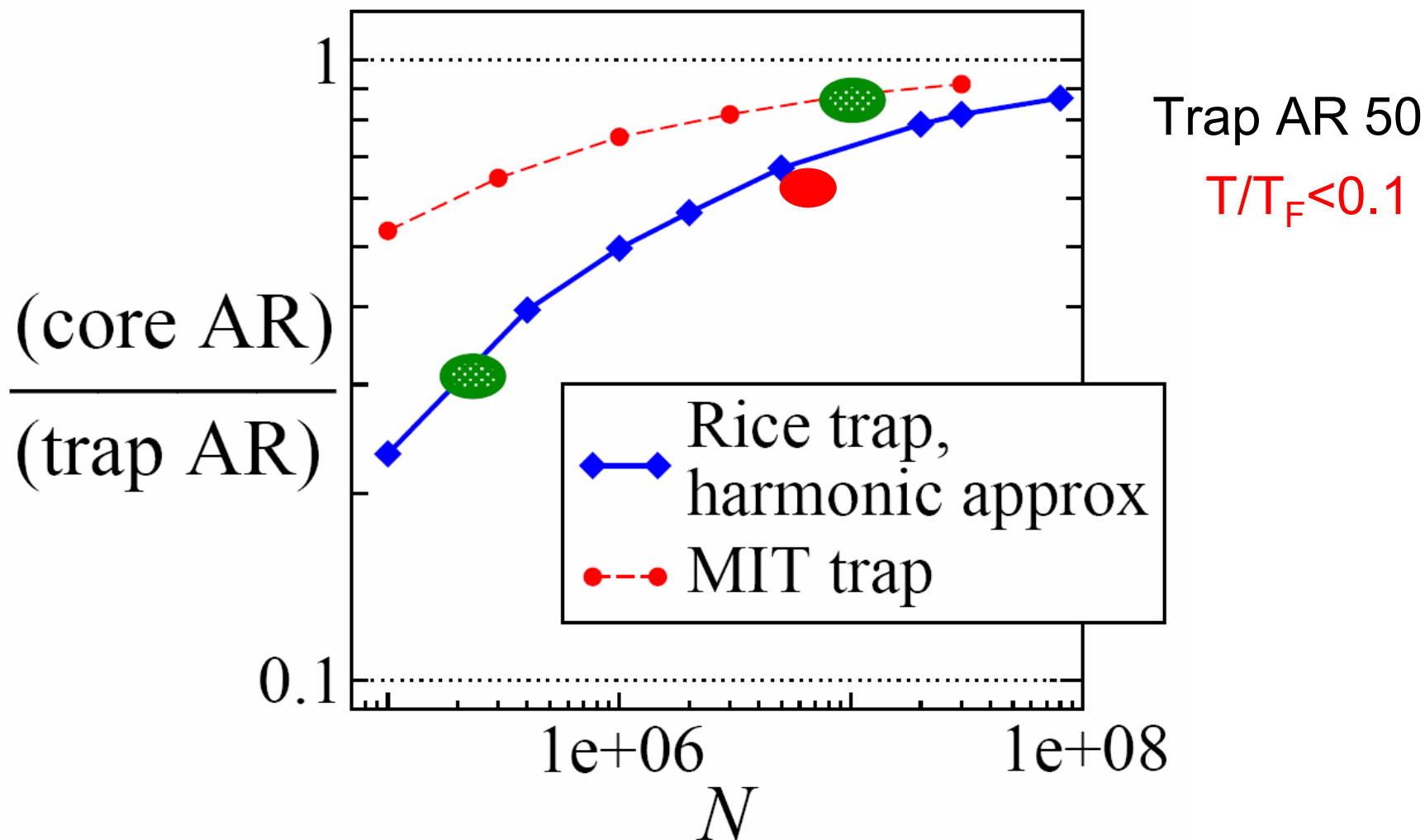
G. B. Partridge, Wenhui Li, Y. A. Liao, and R. G. Hulet

*Department of Physics and Astronomy and Rice Quantum Institute, Rice University, Houston, Texas 77251, USA*



# Spatial distortion of trapped Fermi gases

Masudul Haque<sup>1,2</sup> and H. T. C. Stoof<sup>2</sup>



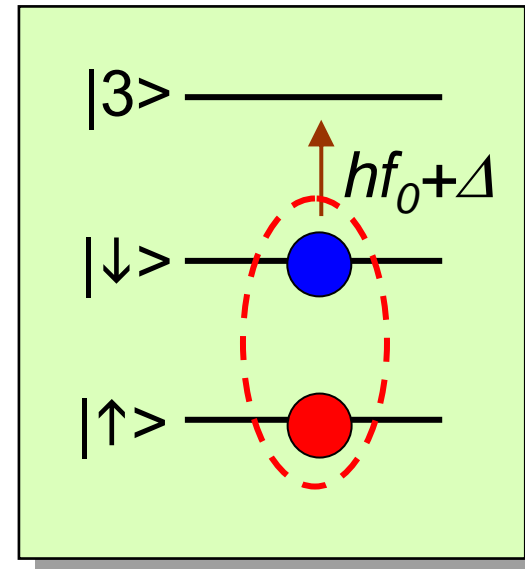
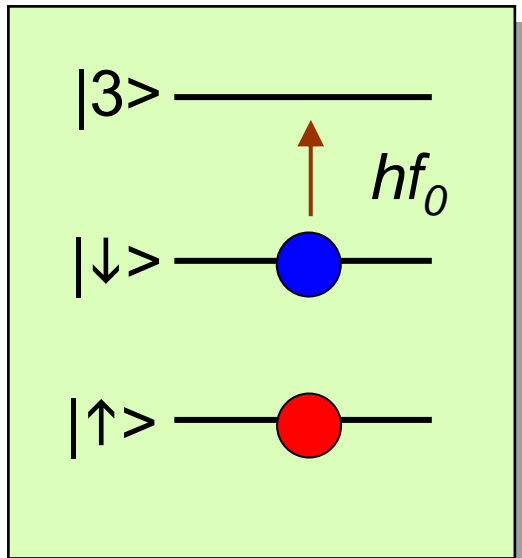
**What happens at the Chandrasekhar-Clogston limit?**

**Also called the Pauli pair breaking limit ...**

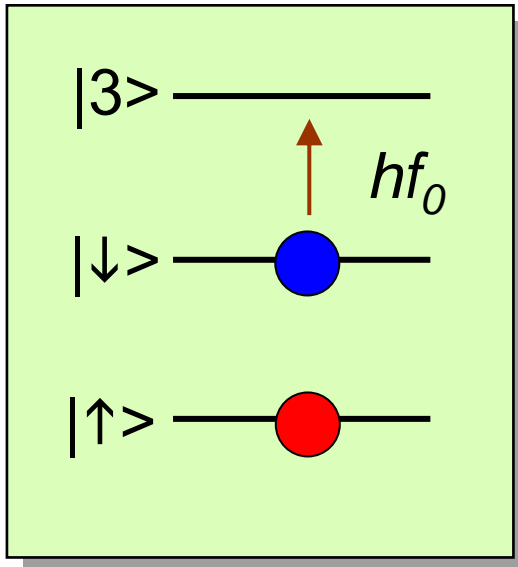


# RF spectroscopy

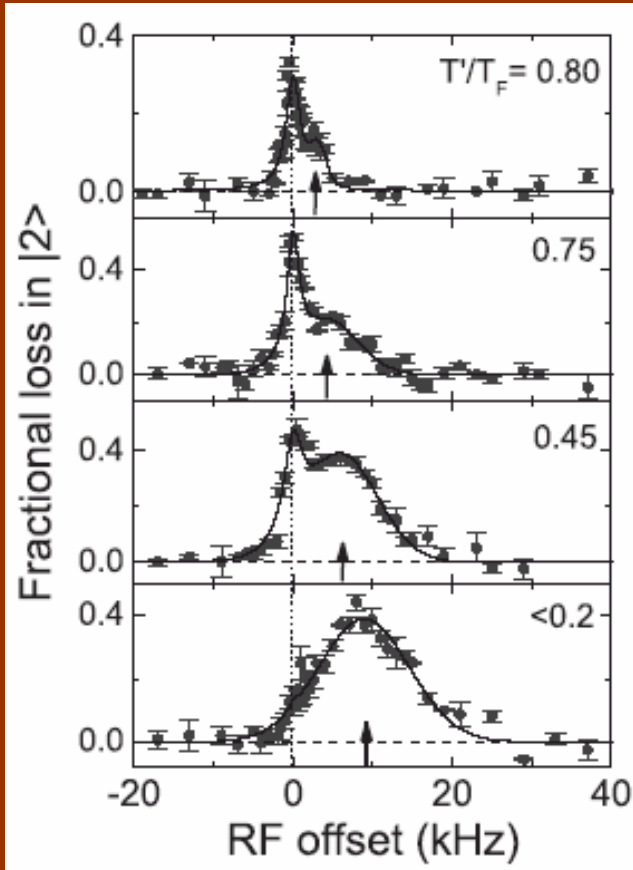
---



# RF spectroscopy



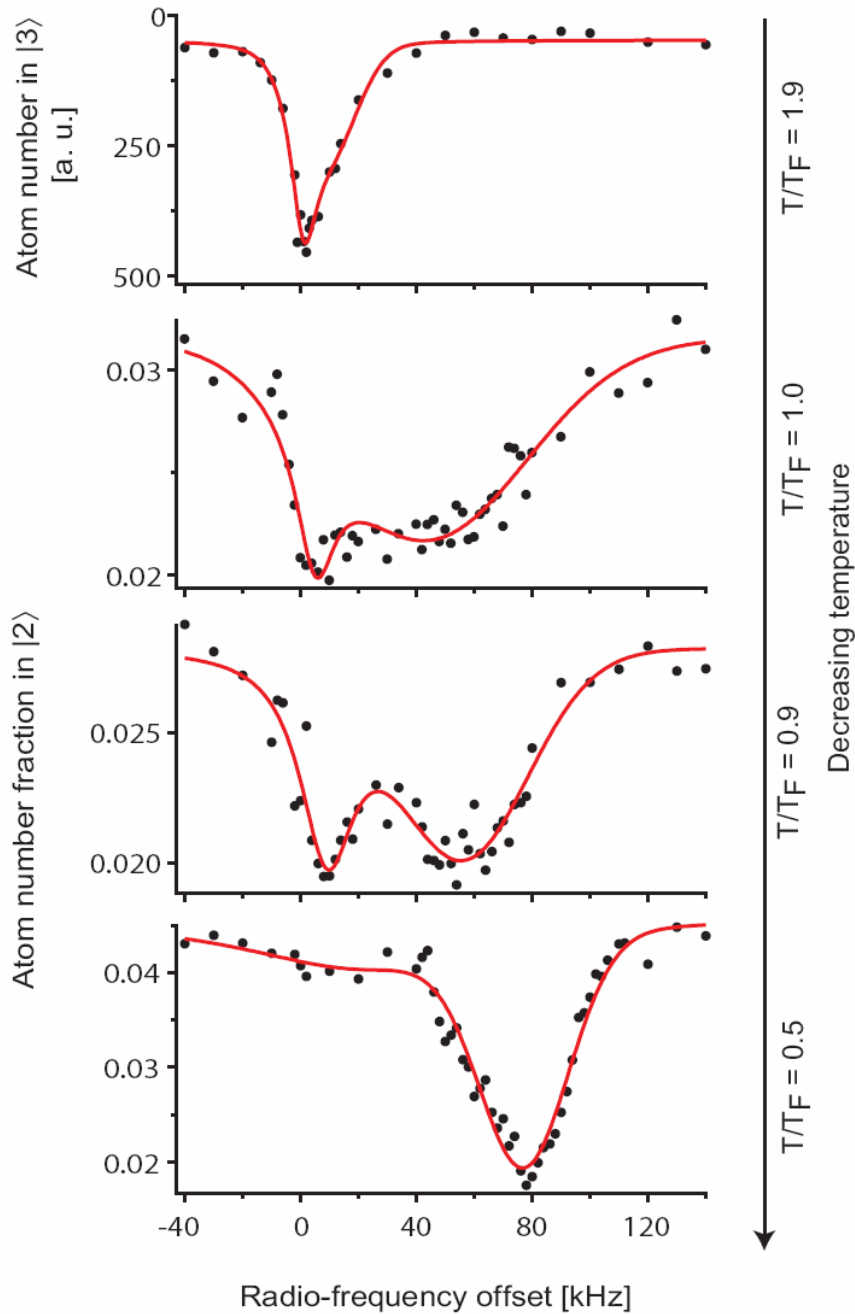
With Equal Mixtures



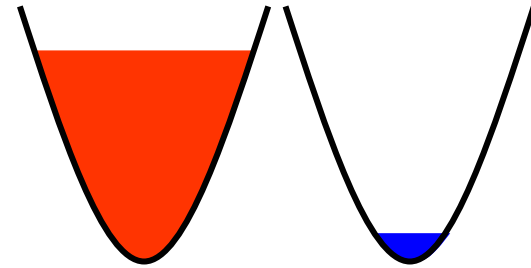
C. Chin et al., Science 305, 1128 (2004)

The double peak structure indicates the presence of pairing.

# RF Spectroscopy with Imbalanced Mixtures



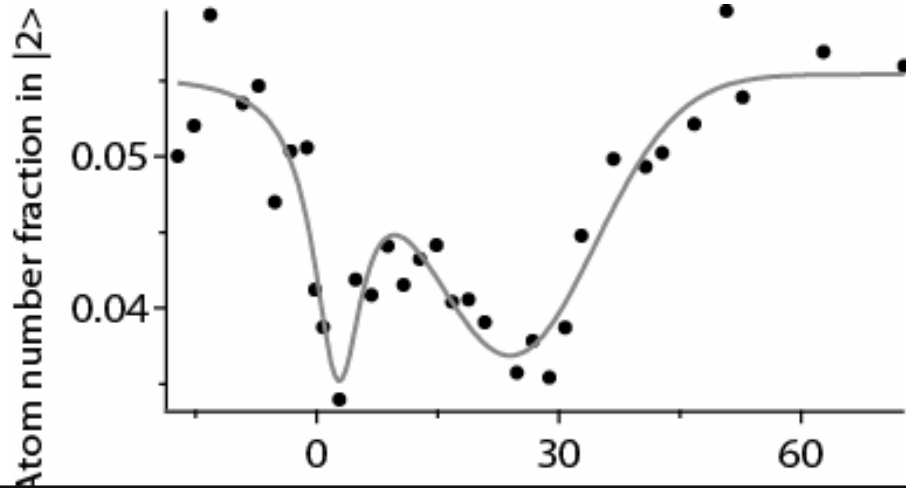
Imbalance  $\delta > 90\%$



Atoms can be fully paired  
in the normal phase  
*even above* the critical  
imbalance.

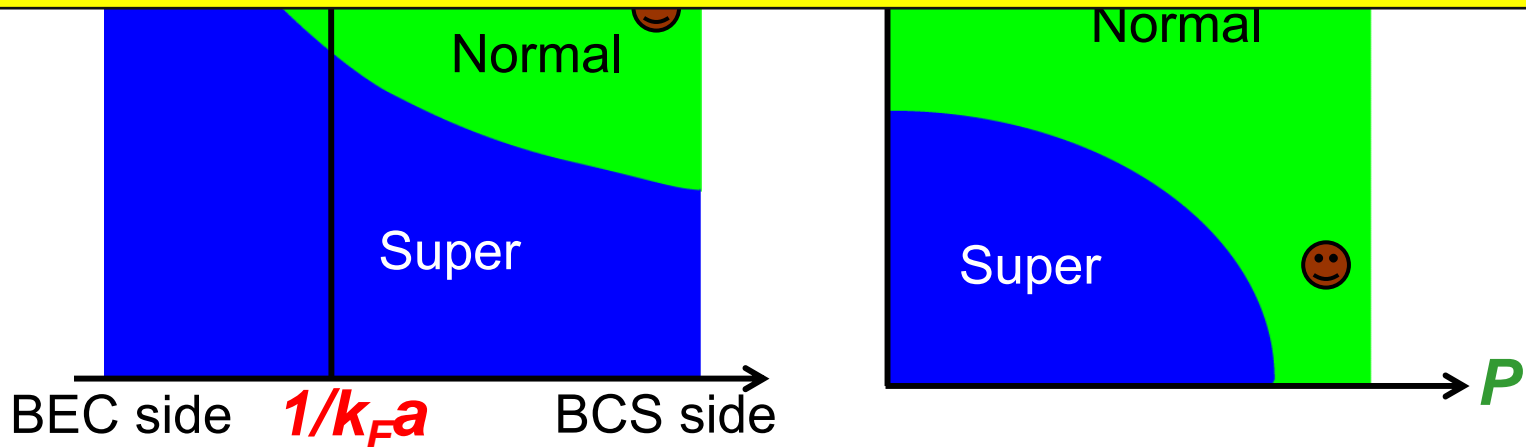
C.H. Schunck, Y. Shin, A. Schirotzek,  
M.W. Zwierlein, WK:  
Science, in print; cond-mat 0702066

# Pairing without Superfluidity

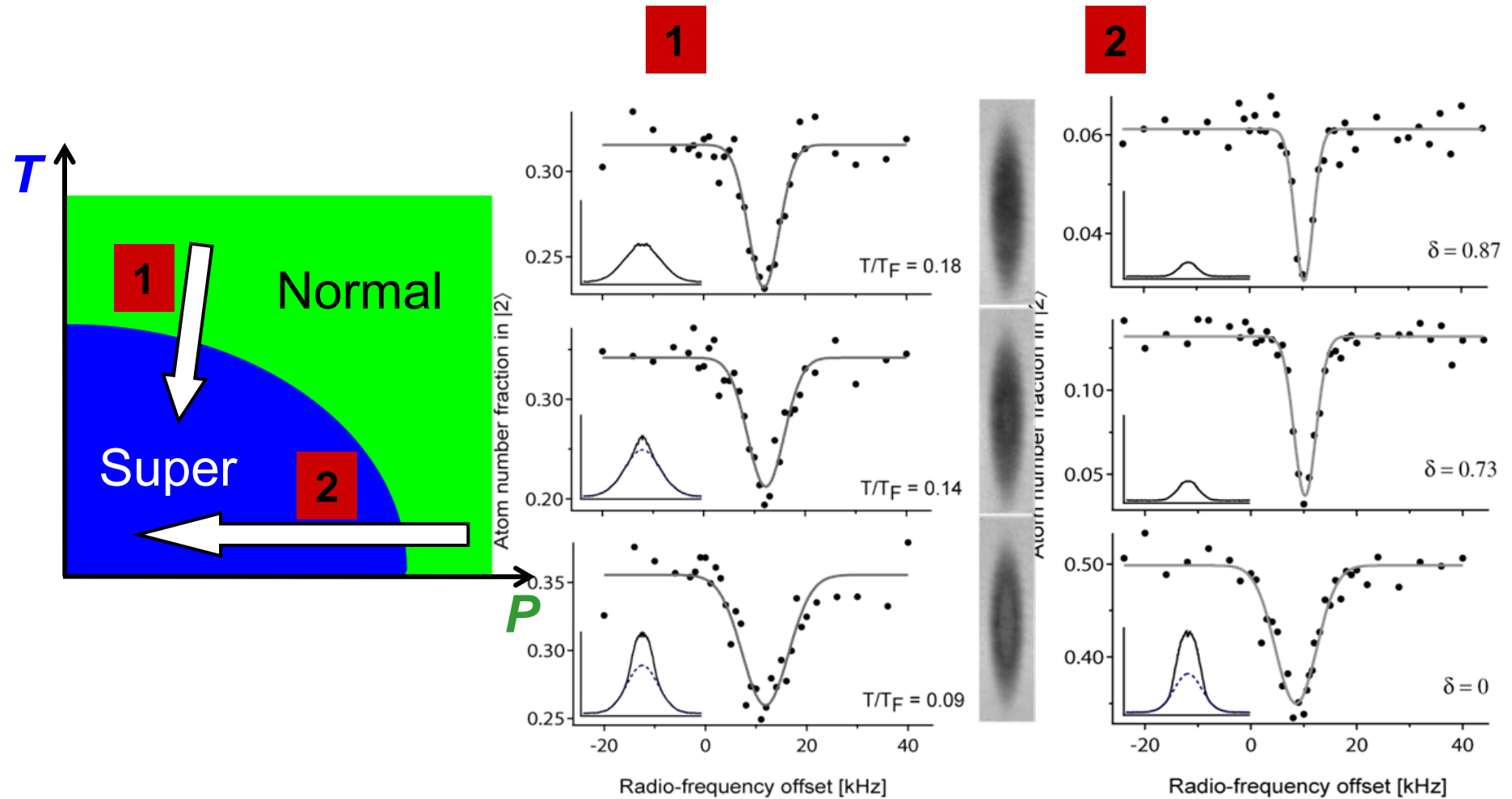


On the BCS side (936G)  
 Imbalance  $\delta \sim 90\%$   
 $T/T_F \sim 0.3$  ( $E_F \sim h \times 280\text{kHz}$ )  
 $1/k_F a = -0.18$   
 $\delta_{c,\text{exp}} \sim 60\%$

Fermion pairs(?) *cannot* Bose-condense even at  $T=0$  !!  
**Pairing** is *not* necessarily a precursor of **Superfluidity**.



# Rf spectroscopy across the phase transition



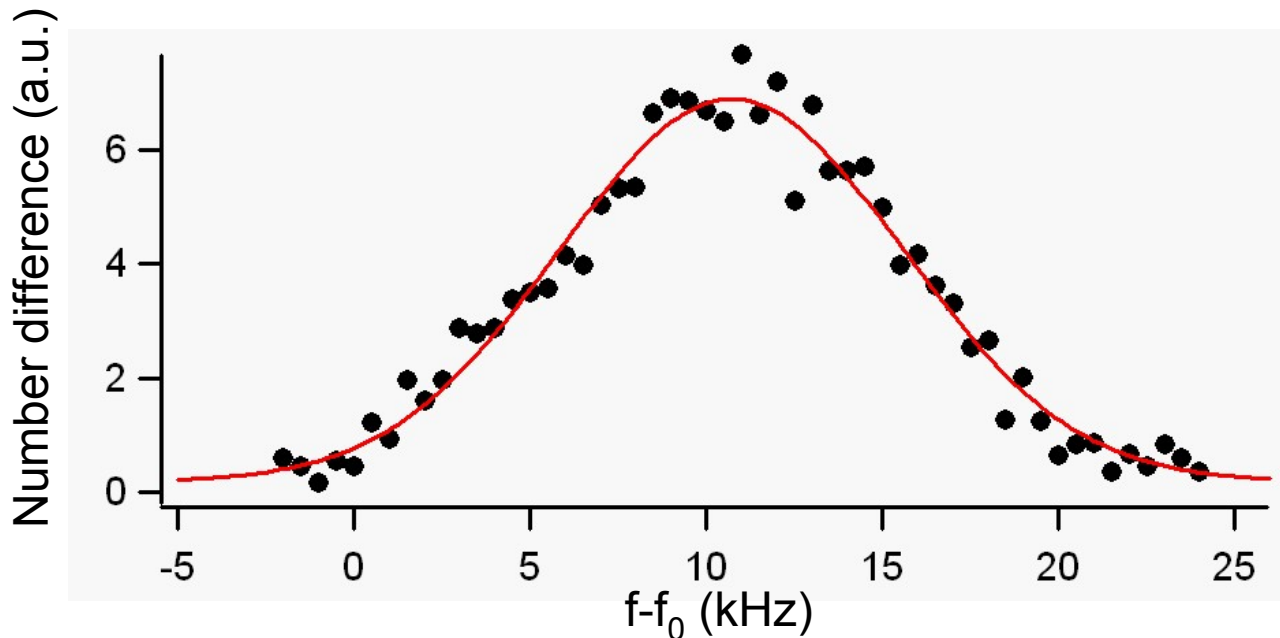
Rf-spectroscopy cannot reveal the onset of superfluidity.

# Gap Tomography

# Inhomogeneous Sample

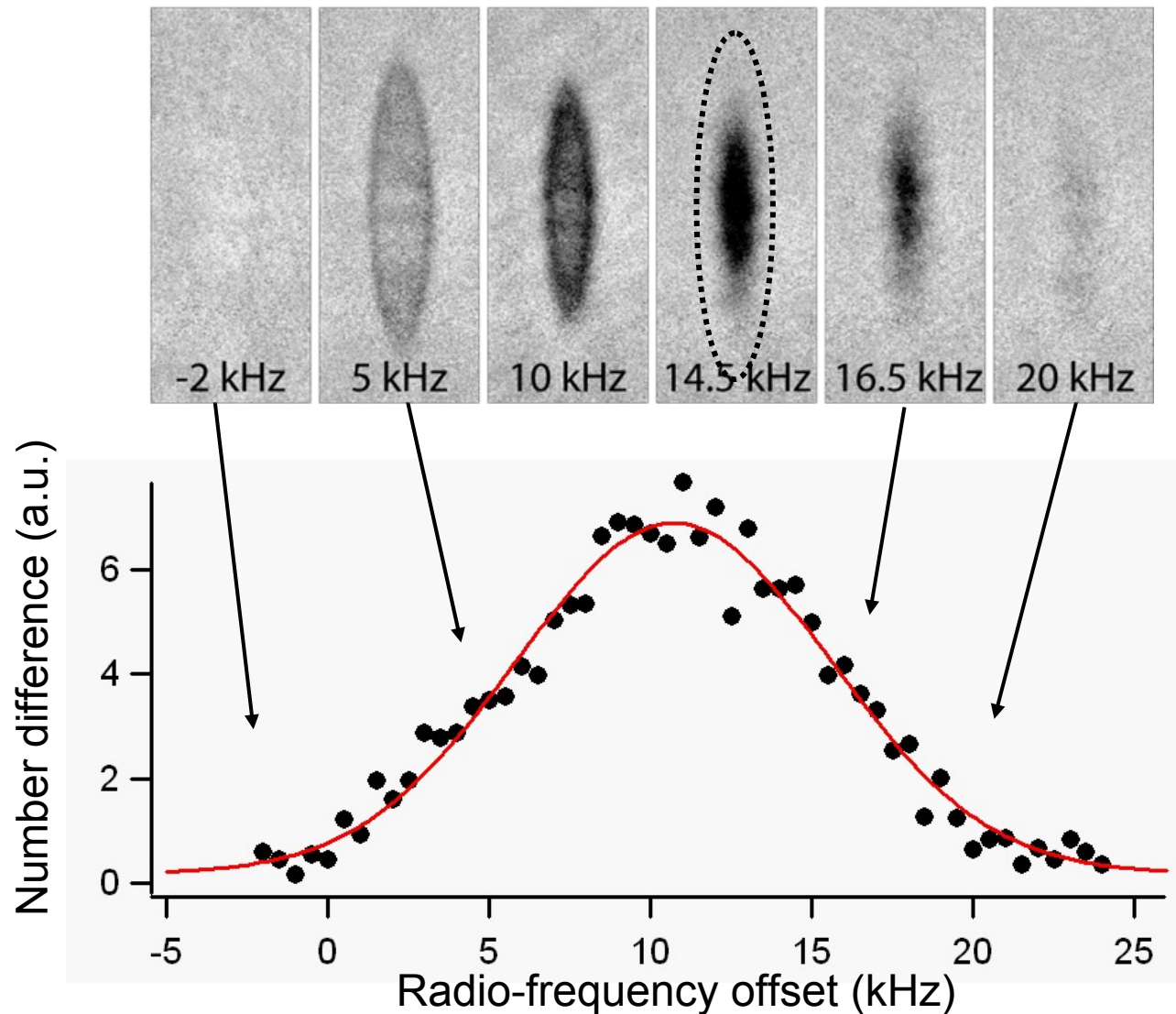
- Ultracold atom sample confined in a harmonic trap
- Inhomogeneous density profiles
  - Density broadening in the spectroscopic signal
  - Difficult to compare with theoretical prediction

## RF spectroscopy with equal mixtures



# RF Spectroscopy with *in situ* Images

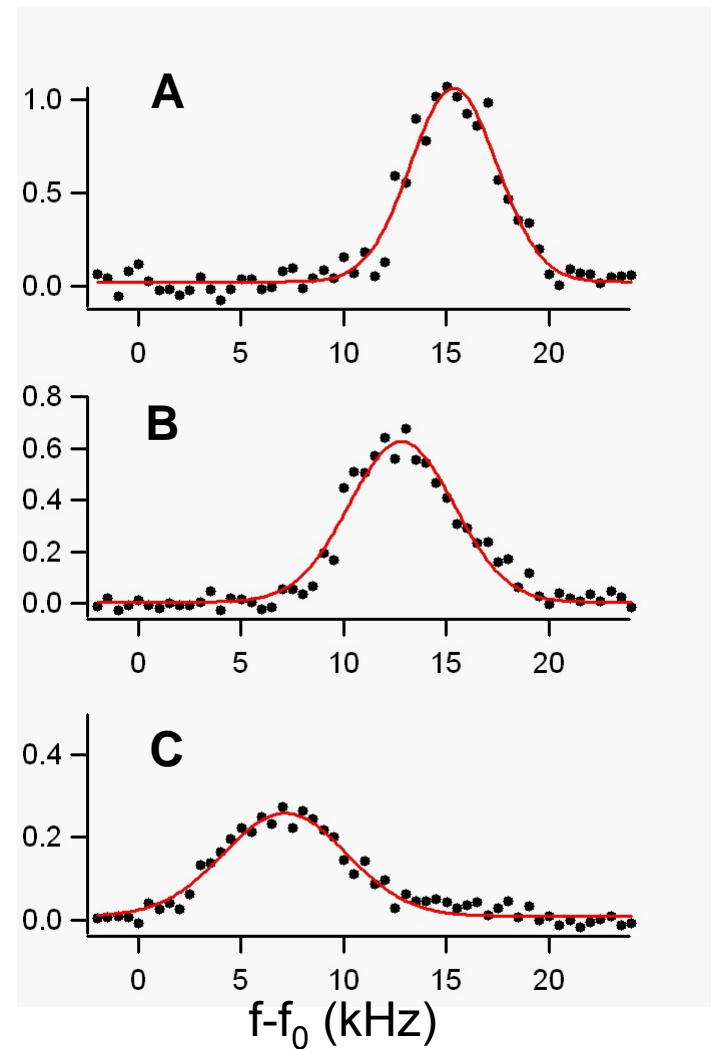
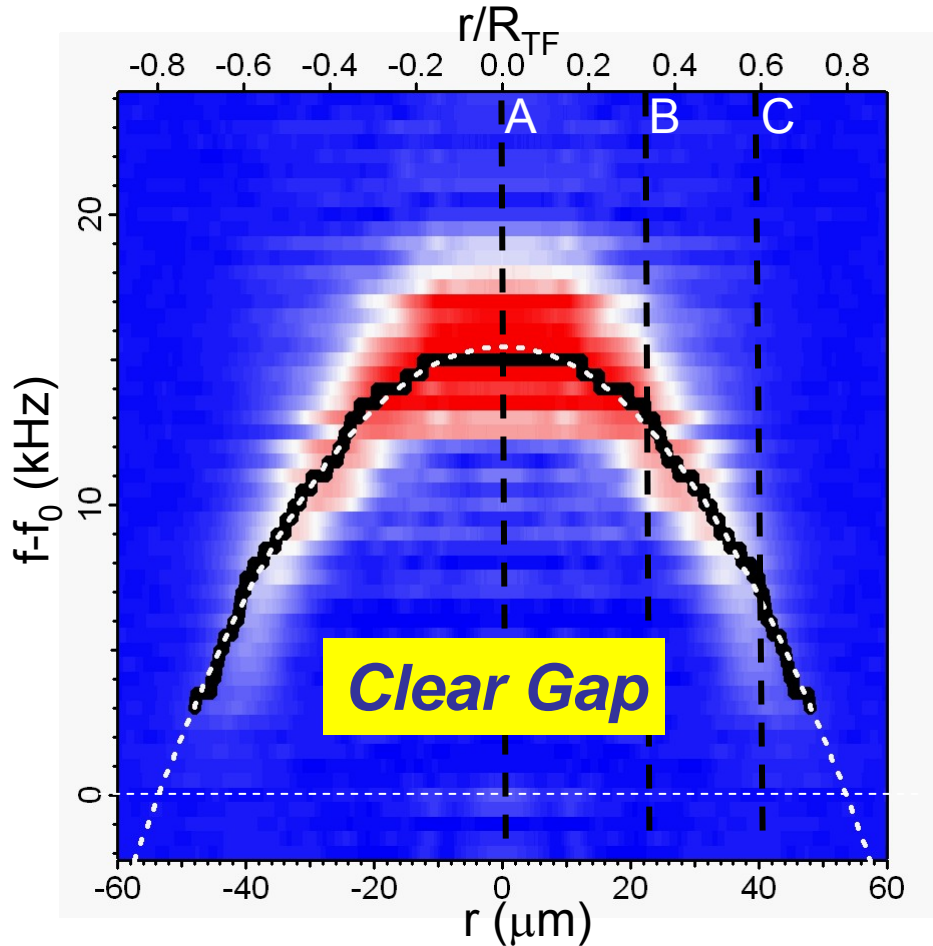
*In situ* phase contrast images measure the depletion region





# Spatially resolved RF spectroscopy

On resonance,  $T'/T_F < 0.05$

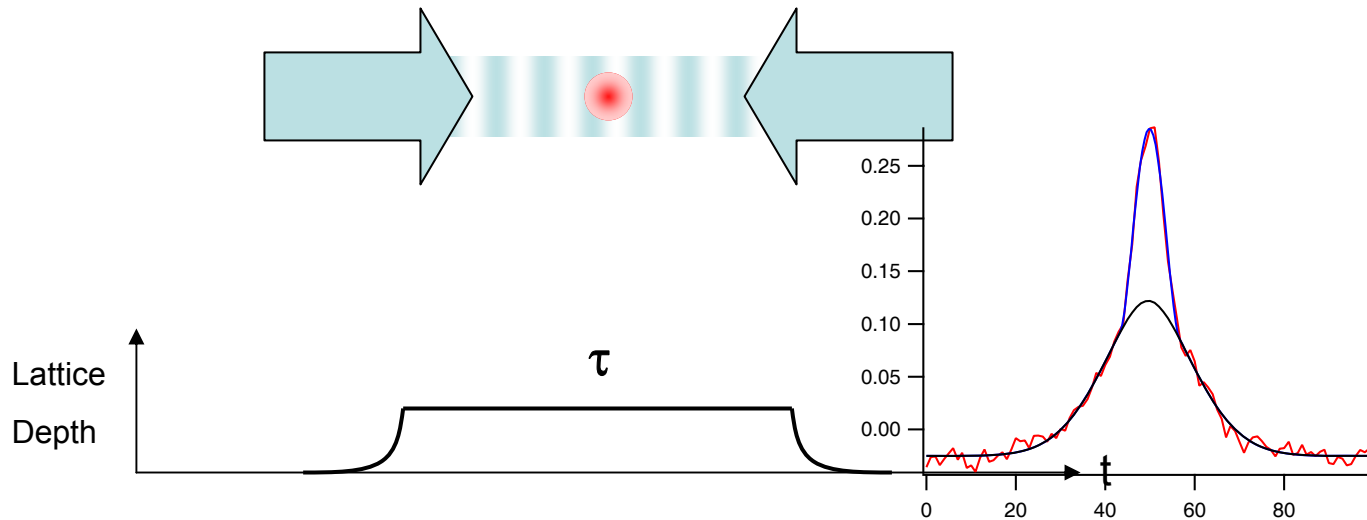


The parabolic profile is consistent with the harmonic confinement.

# Critical Velocity

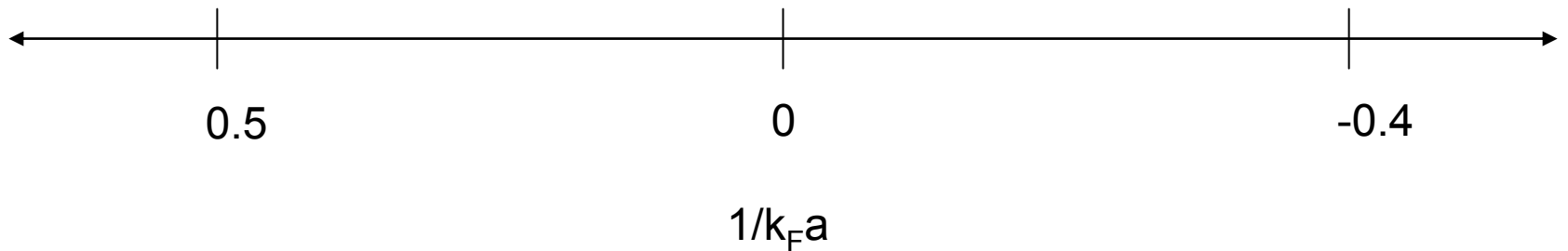
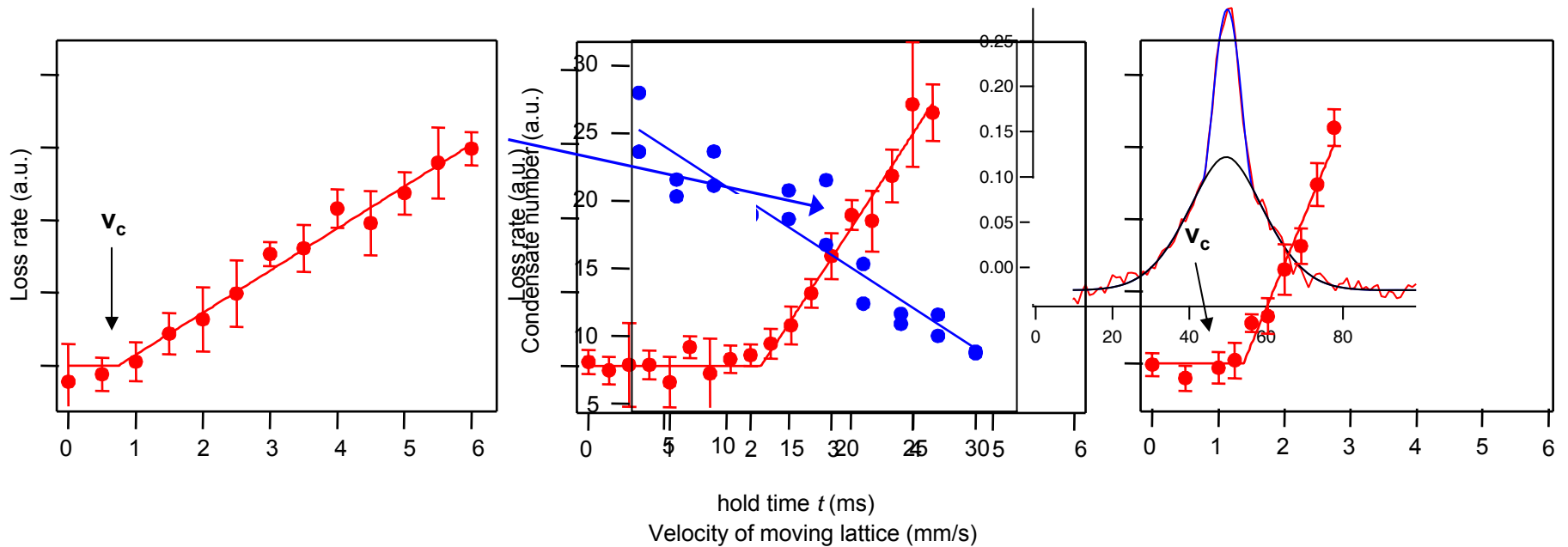
Dan Miller, Jitkee Chin et al., unpublished

# Experiment Overview

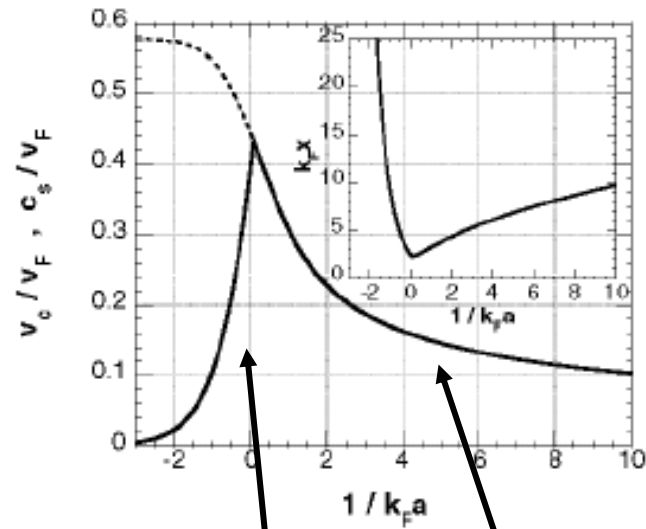
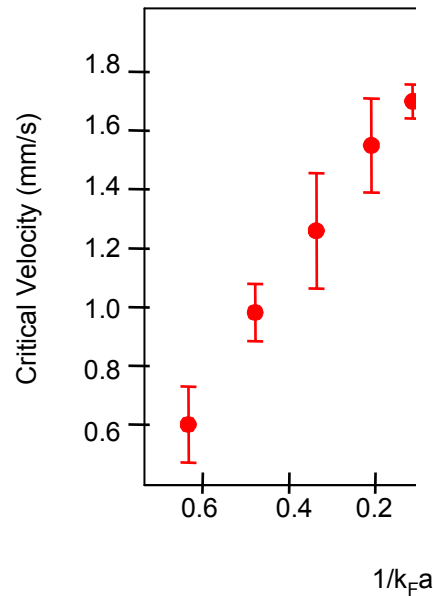


- A lattice with some fixed velocity is ramped up and held for a time  $\tau$ .
- The cloud is released. Time of flight imaging reveals a bimodal distribution.

# Experiment Overview



# Conclusions



The superfluid is most robust on resonance

Observed *critical velocity* is an order of magnitude smaller than predicted.

Pair  
breaking

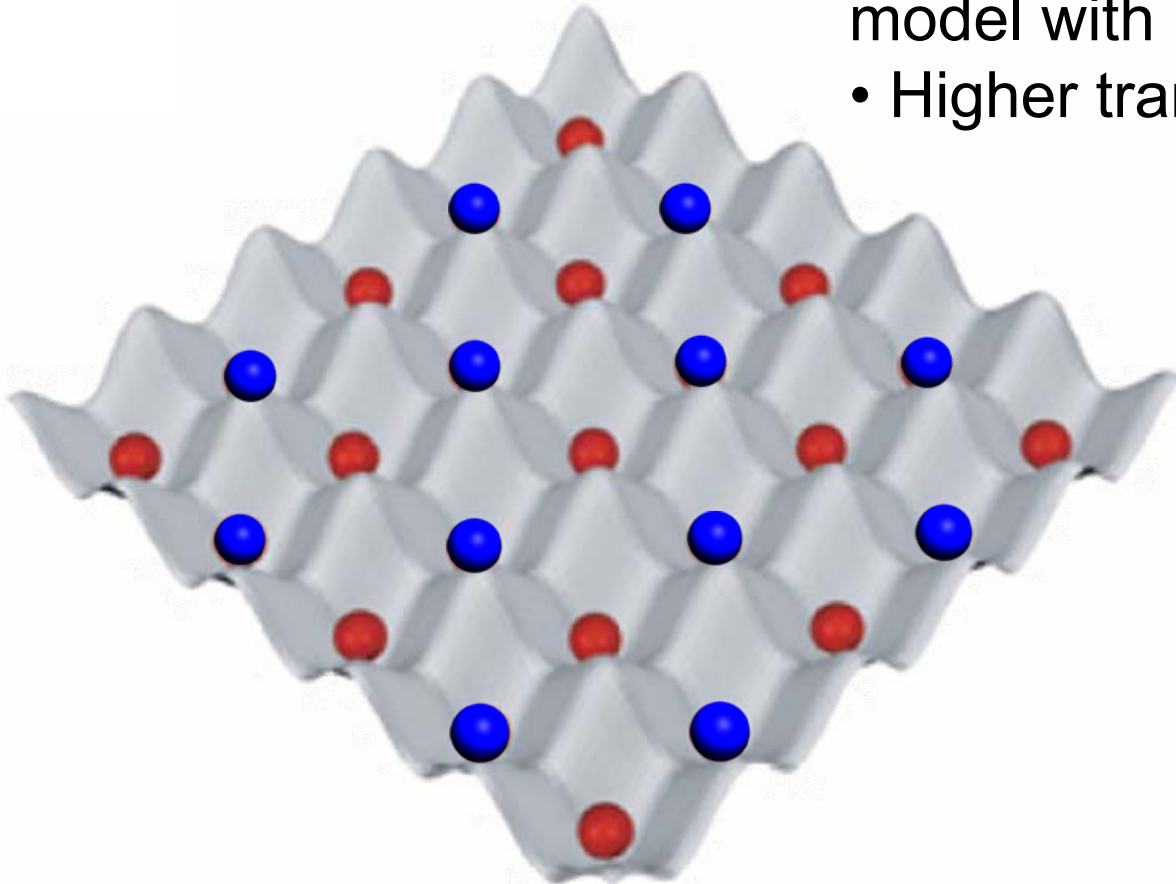
Phonons

# Superfluidity of Ultracold Fermions in an Optical Lattice

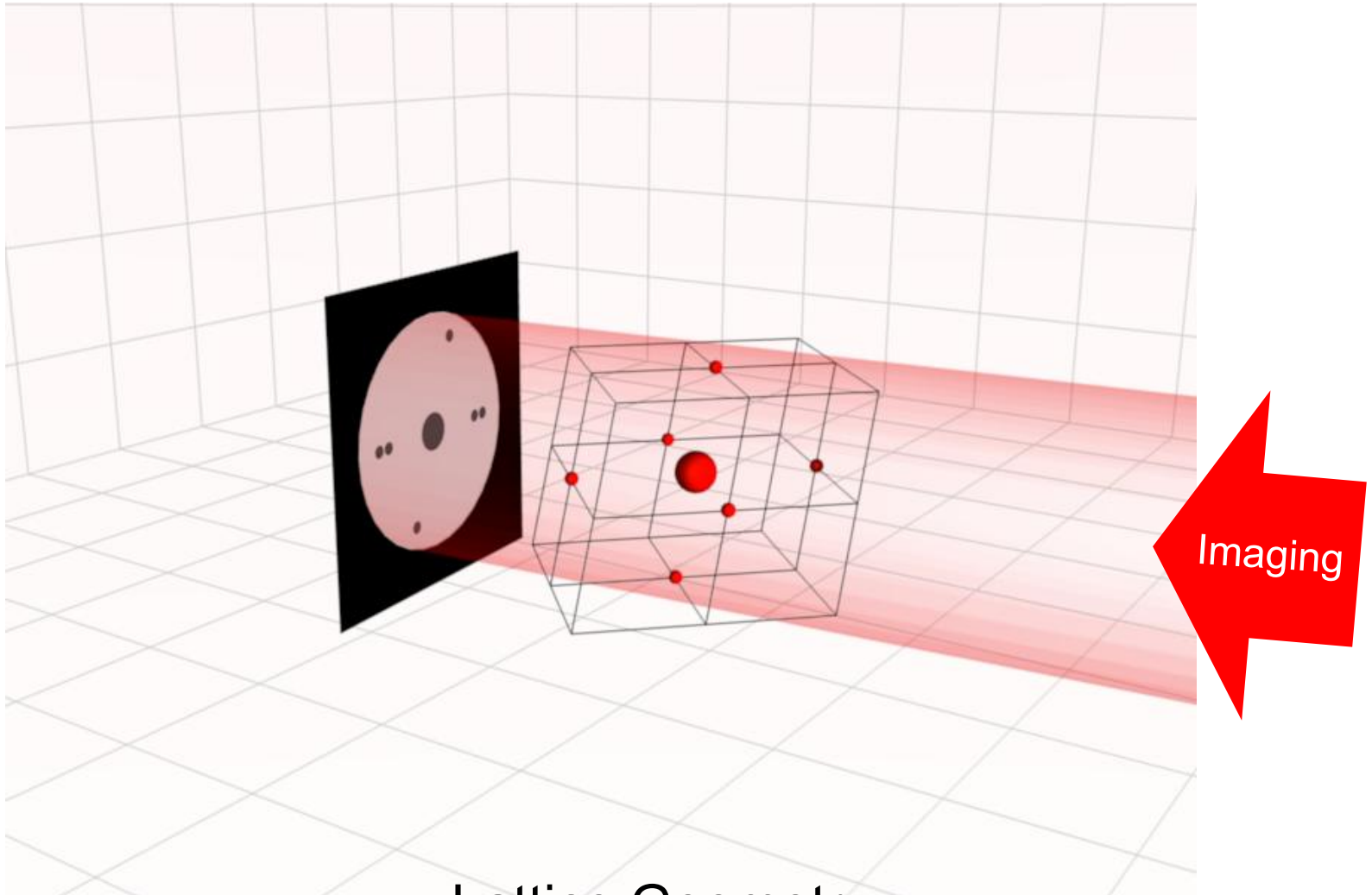
J.K. Chin, D.E. Miller, Y. Liu, C. Stan, W. Setiawan, C. Sanner, K. Xu, W.K., *Nature* **443**, 961-964 (2006).

# Why lattice?

- Crystalline materials in nature
- Hubbard models; rich new phenomena
- Minimal model for high- $T_c$  d-wave superfluidity is lattice Hubbard model with repulsive interactions
- Higher transition temperature



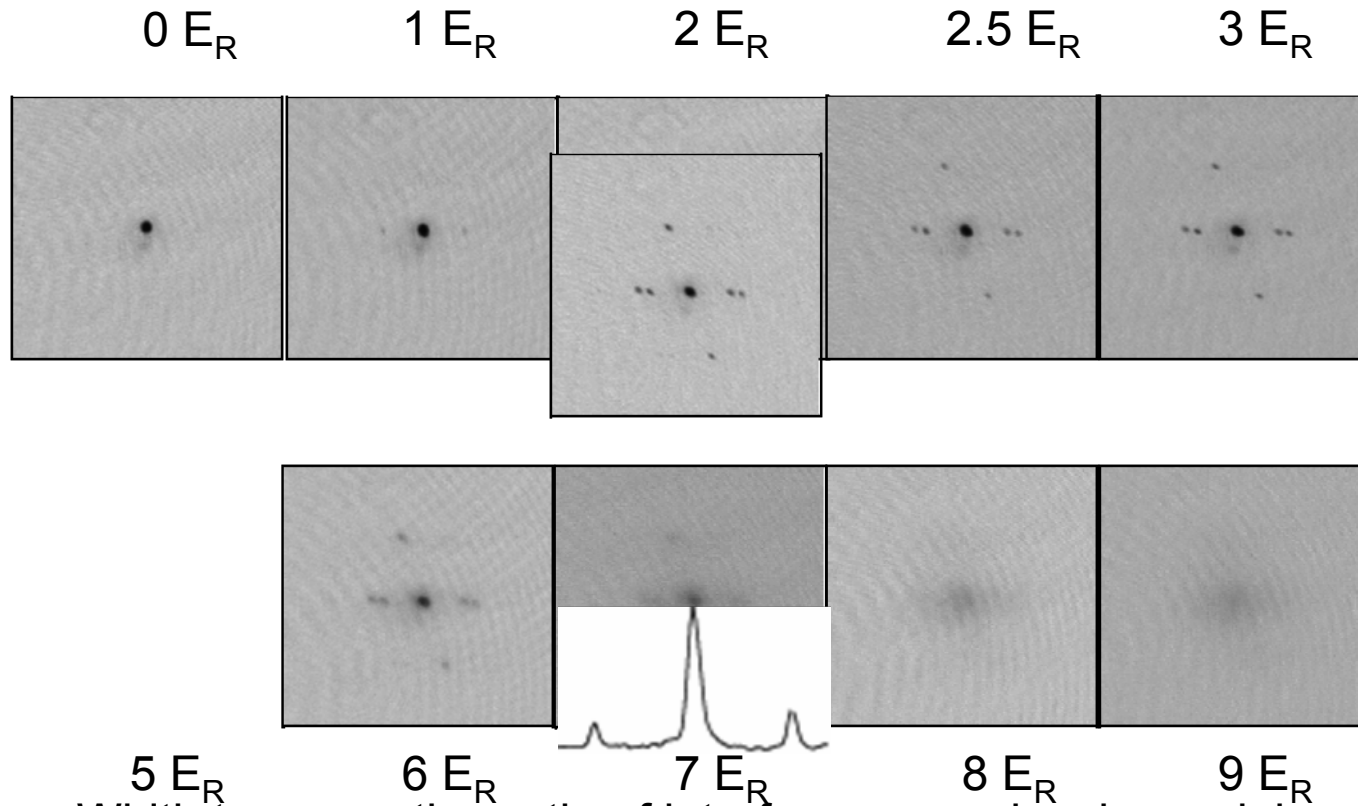
Retro-reflect far-detuned 1064nm light to form standing wave potentials in 3 dimensions.



Lattice Geometry  
as seen in time-of-flight



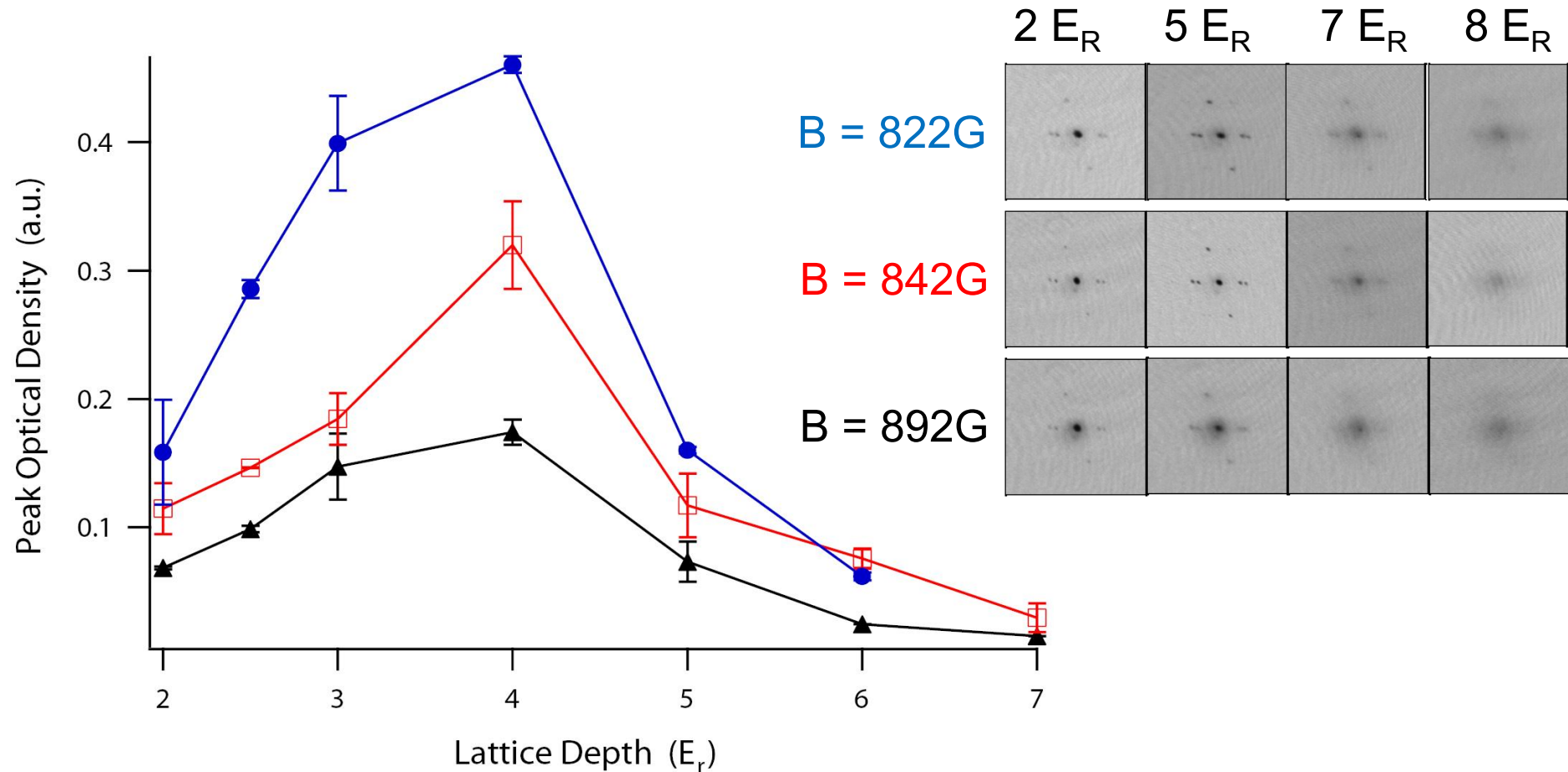
Starting with a condensate of Li-6 pairs, then applying an optical lattice:



Width to separation ratio of interference peaks gives minimum coherence length of 10 lattice sites.

**Long range phase coherence => Superfluidity!**  
B = 842 G (on BCS side of the resonance)

# BEC-BCS Crossover in an Optical Lattice



Overall contrast decreases, but no change in the “transition point”

Nanokelvin atoms are a new toolbox to  
address fundamental questions of many-body  
physics

**Quantum simulations of strongly correlated,  
strongly interacting systems**

# BEC I

Ultracold  
fermions

Christian Schunck  
Andre Schirotzek  
Yong-II Shin

# BEC II

Na, Li  
Optical Lattices

Jit Kee Chin  
Daniel Miller  
Yingmei Liu  
Widagdo Setiawan  
Christian Sanner  
Aviv Keshet

Opening for  
Postdoc

# BEC III

Atom chips,  
surface atom  
optics

Tom Pasquini  
Gyu-Boong Jo  
Caleb Christensen  
Ye-ryoung Lee  
Jae Choi  
Tony Kim  
**D.E. Pritchard**

# BEC IV

Atom optics  
and optical  
lattices  
Jongchul Mun  
Patrick Medley  
David Hucul  
David Weld  
**D.E. Pritchard**

\$\$

NSF  
ONR  
DARPA