

## Small-Scale Structure in Gravitational Lens Galaxies

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### What can you do with strong lensing?

#### Traditional ideas

- $H_0$  – *hard; systematic uncertainties in lens models*
- $\Omega_\Lambda$  – *I say no; degeneracy between cosmology and evolution*  
(“Rethinking Lensing and  $\Lambda$ ” ApJL 575:L1)
- **dark matter and physical properties of (elliptical) galaxies – *yes!***

#### New ideas

- **quasar host galaxies at  $z \sim 1-5$**
- **quasar microlensing**
- **galaxy evolution in groups at  $z \sim 0.2-1$**
- **substructure and properties of dark matter**

## Small-Scale Structure: Two Problems

### *“Missing” core images*

- Prediction: a faint image near the center of every lens galaxy
- Not seen!
- Probe of density inside  $R < 20\text{--}200\text{ pc}$

### *Anomalous flux ratios*

- Flux ratios are notoriously hard to fit
- Due to **small mass clumps** ( $10^4\text{--}10^8 M_{\text{sun}}$ ) in lens galaxies?
- Resolution to CDM “satellite crisis”?

## Strong Gravitational Lensing

S

quasar,  
 $z \sim 1\text{--}5$

L

O

elliptical,  $z \sim 0.2\text{--}1$

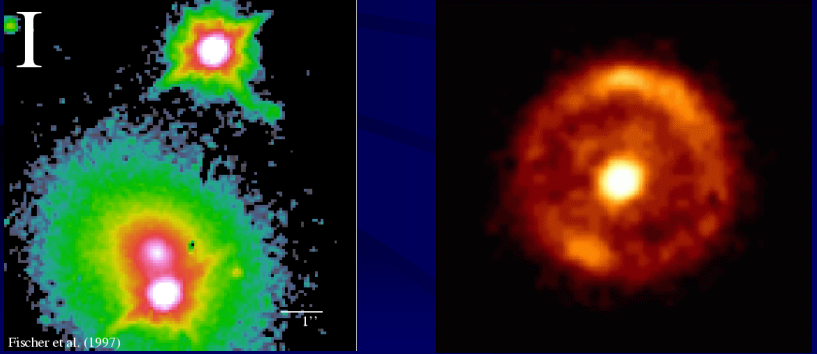
$$\text{Lens equation: } u = x - (D_l/D_{os}) \alpha$$

Lensing is sensitive to *all* mass, be it  
luminous or dark, smooth or lumpy.

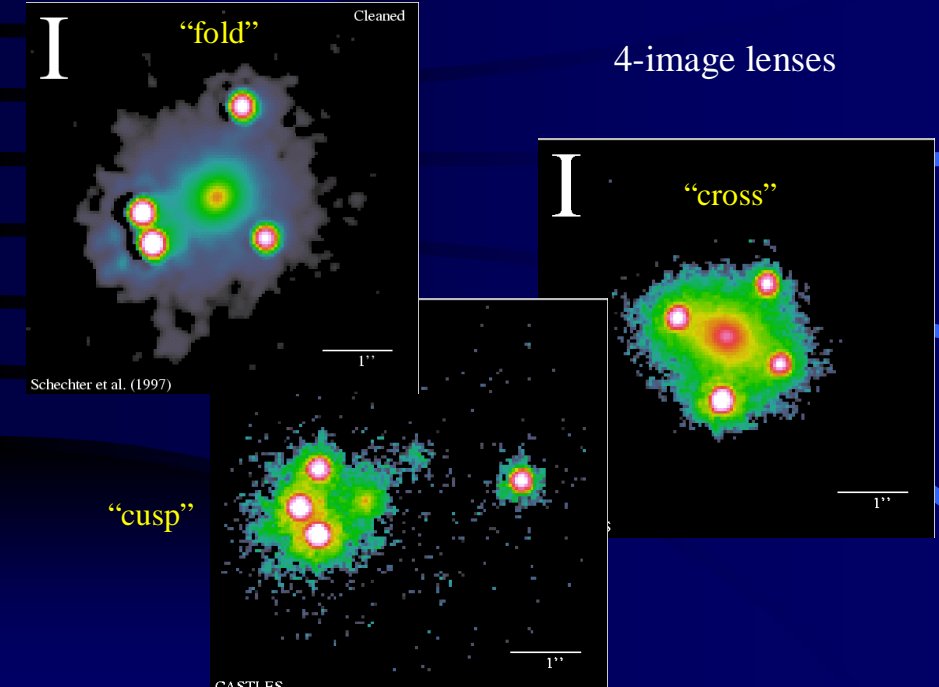
**CfA/Arizona Space Telescope Lens Survey  
(CASTLES)**

*C. Kochanek, E. Falco, C. Impey, CRK, J. Lehar,  
B. McLeod, J. Muñoz, C. Peng, H.-W. Rix*

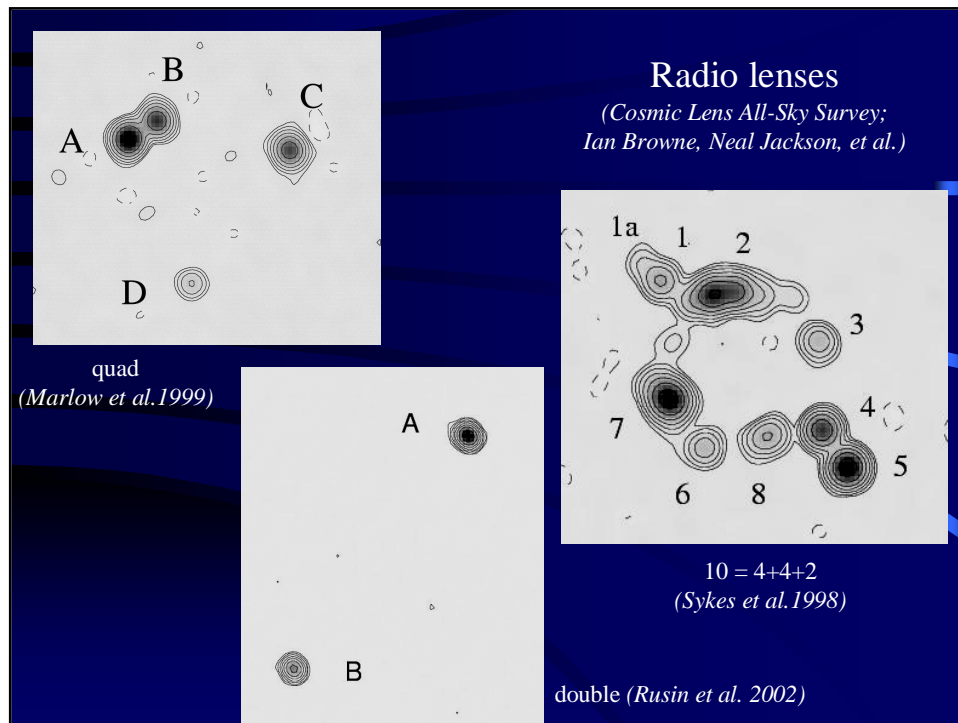
<http://cfa-www.harvard.edu/castles>



**4-image lenses**



## Small Scale Structure and Gravitational Lensing



### Problem #1: Core Images and the Centers of Distant Ellipticals

*(CRK ApJ in press, astro-ph/0206243)*

- Odd image theorem (Burke 1981):  
*cusp shallower than  $\rho \propto r^{-2}$*   
 $\Rightarrow$  *odd number of images*  
 $\Rightarrow$  *2/4 observed images + 1 "core" image*
- Current (radio) dynamic range = 100–2000.
- Q: Where are the (radio) core images?  
 A: Demagnified by high central density.
- Do the numbers work out?
- Long-standing puzzle with implications for core radii, density cusps.  
*(e.g., Narasimha et al. 1986; Wallington & Narayan 1993; Rusin & Ma 2001)*

### Connections

Galaxy centers are interesting.

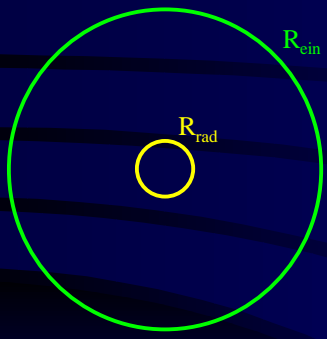
- dynamics
- remnants of galaxy formation
- clues to baryon/DM interactions?

CDM concentration problem.

- Predicted densities *too high* on kpc scales.
  - rotation curves *(e.g., McGaugh & de Blok 1998)*
  - bars *(Debatista & Sellwood 2000)*
  - strong lensing statistics *(CRK 2001)*
  - microlensing *(Binney & Evans 2001)*
- Core images: densities *too low* on ~100 pc scales? *(CRK 2001)*

Can core images constrain supermassive black holes out to  $z \sim 1$ ? *(Mao et al. 2001)*

### Lensing Critical Curves



Two “critical radii”:

- *Einstein radius*  $R_{\text{ein}}$  – tangential arcs
- *radial critical curve*  $R_{\text{rad}}$  – radial arcs

Image Locations	double	quad
outside $R_{\text{ein}}$	1	2
between $R_{\text{rad}}$ and $R_{\text{ein}}$	1	2
inside $R_{\text{rad}}$	1	1

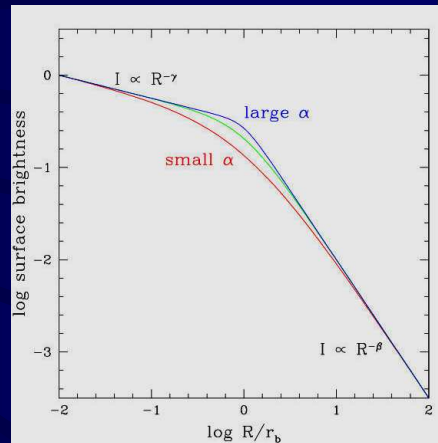
*Higher central density  $\Rightarrow$  smaller  $R_{\text{rad}}$   $\Rightarrow$  fainter core images*

## Models

“Nuker law,” from surface brightness profiles of early-type galaxies.

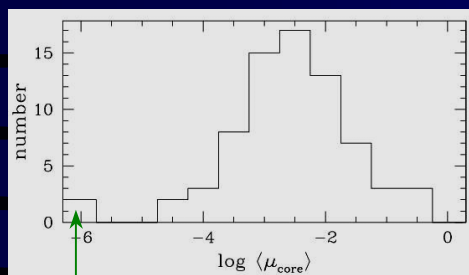
Realistic parameters:

- Take 73 nearby ellipticals from the literature.
- Shift to  $z = 0.5$  as mock lens galaxies.



(Faber et al. 1997; Carollo et al. 1997; Carollo & Stiavelli 1998; Ravindranath et al. 2001)

## A plethora of core images

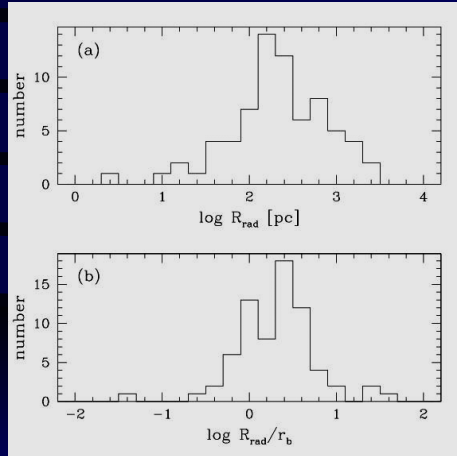


galaxies steeper  
than  $\rho \propto r^{-2}$

Among the 73 galaxies...

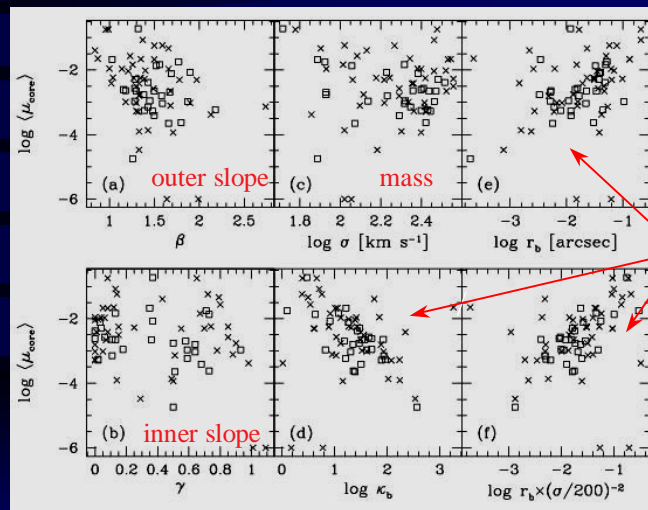
- 2 don't produce core images.
- $\langle \mu \rangle$  spans 4 dex!  
⇒ Some bright, many faint.

Physical scale



- Median  $R_{\text{rad}} \sim 200 \text{ pc}$ , range 10–2000 pc
- $R_{\text{rad}}$  typically slightly larger than Nuker break radius

Parameter dependences

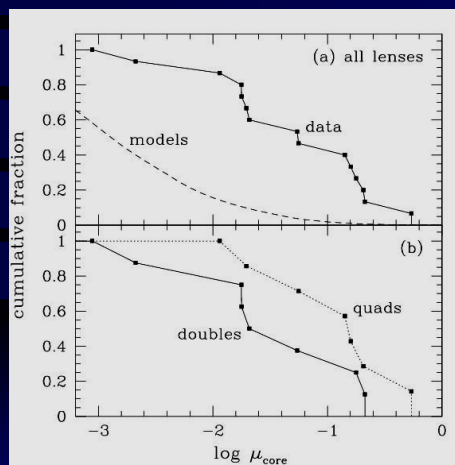


- $\langle \mu \rangle$  “tends” to decrease as concentration increases
- But no simple trend – and remarkably large scatter

### Should we see core images?

- Which galaxies have  $\langle\mu\rangle > 0.1$ ?
  - NGC 4239 and 5273: dwarf galaxies – *poor lenses*
  - NGC 6166: brightest cluster galaxy; most distant and least concentrated galaxy in Faber et al. (1997) sample – *atypical*
- Such galaxies are likely to be rare in lens samples.
- Thus, bright core images are likely to be rare.

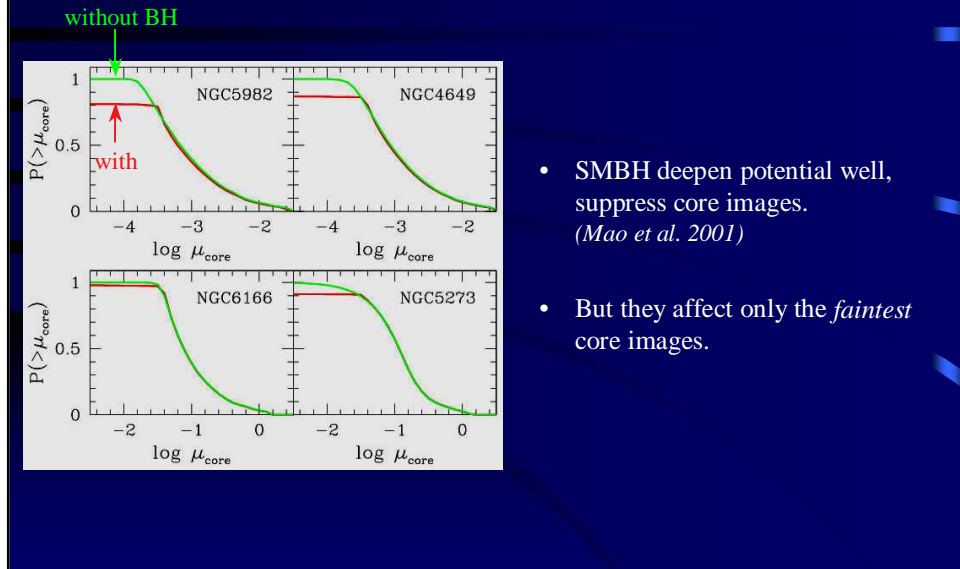
### Comparison to data



- Data from CLASS – only *upper limits* on  $\mu$ .  
(Norbury et al., in prep.)
- Models do not predict core images brighter than observed.
- Doubles yield stronger limits, better targets for follow-up.




## Supermassive black holes?



## Implications

- Unique probe of densities inside  $\sim 200$  pc in ellipticals at  $z \sim 0.2-1$ .
- Expect a remarkably wide range of core image properties.
- Stellar densities can explain the absence of core images so far.
- New searches:
  - *better radio sensitivity*
  - *narrow-band optical imaging?*
  - ??

Problem #2: Anomalous flux ratios  
and CDM substructure



In CDM, halos are lumpy

- CDM leads to *hierarchical structure formation*.
- Small objects are dense, not fully disrupted by tidal forces.
- Large halos contain remnants of their many progenitors.
- Clusters look like this – good!
- Galaxies don't – bad?

(Moore et al. 1999)

## A substructure crisis?

CDM seems to overpredict substructure. What does it mean?

### Particle physics possibilities:

- Maybe dark matter isn't cold and collisionless.
- Maybe it is *warm*, *self-interacting*, *fuzzy*, *sticky*, ...

### Astrophysics possibilities:

- We only see clumps via stars, gas.
- Maybe galaxies contain lots of clumps but most are invisible.

*Is this mainly a problem for particle physicists or astrophysicists?*

## Substructure and Lensing

- Need to find (or rule out) a population of objects detectable *only by their mass*.
- Effects on strong lenses?
  - *image positions* –  $\partial\phi$  – *fairly insensitive to clumps*
  - *image brightnesses* –  $\partial^2\phi$  – *very sensitive to clumps*
- So, seek lenses where smooth models can reproduce positions but not brightnesses.
- (Recall quasar microlensing...)

*(Mao & Schneider 1998; Metcalf & Madau 2001; Chiba 2001; Dalal & Kochanek 2002)*

### Typical Numbers

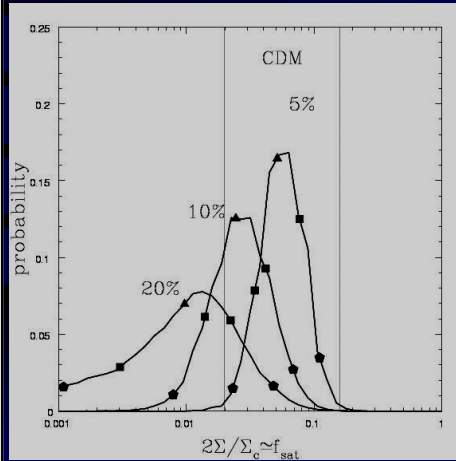
	<i>Stars</i>	<i>Satellites</i>
<i>mass</i>	$1 M_{\text{sun}}$	$10^6 M_{\text{sun}}$
$R_{\text{ein}}$	$2 \mu\text{as}$	$1 \text{mas}$
<i>time delays</i>	$\delta\tau \approx 0$	$\delta\tau \approx 0$
<i>positions</i>	$\delta x \approx 2 \mu\text{as}$	$\delta x \approx 1 \text{mas}$
<i>fluxes</i>	$\delta f \sim \text{arbitrary}$	$\delta f \sim \text{arbitrary}$

### From lensing to dark matter physics

- Observe lenses.
- Find systems inconsistent with smooth lens models.
- Infer amount of substructure. (Add substructure until the models are *statistically* consistent with the data.)
- Connect to CDM predictions.
- Constrain physics of dark matter.

## Dalal & Kochanek: "Detection of CDM Substructure"

(2002 ApJ 572:25)



satellite mass fraction,  $f_{\text{sat}}$

- Bayesian analysis of substructure parameters.
- Main result is lower limit on  $f_{\text{sat}}$ .
- $f_{\text{sat}} \sim 2\%$  (0.6–7% at 90% confidence)
- A detection of substructure!

## Implications?

Appears to be a *major success* for the CDM paradigm:

- Confirms predictions on very small spatial scales.
- Rules out alternatives like warm or self-interacting dark matter.

But recall the assumptions:

- The need for substructure is inferred from the failure of models to fit observed fluxes..
- The substructure is assumed to be the granular stuff predicted by CDM.

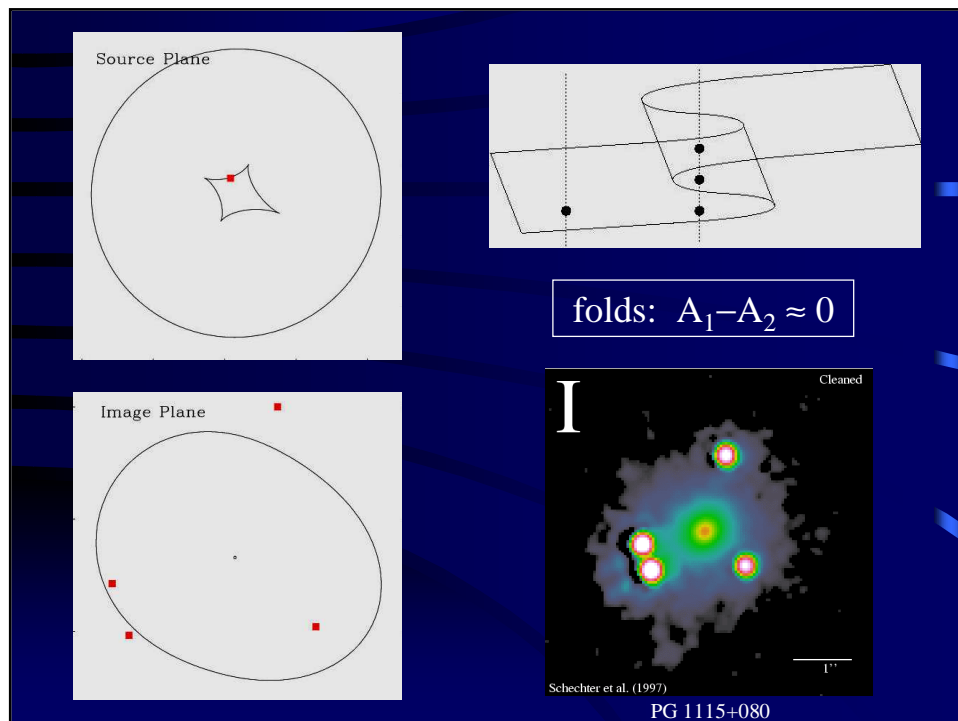
*We need to rebuild the chain  
of logic, link by link...*

## Link #1: Finding the Anomalies

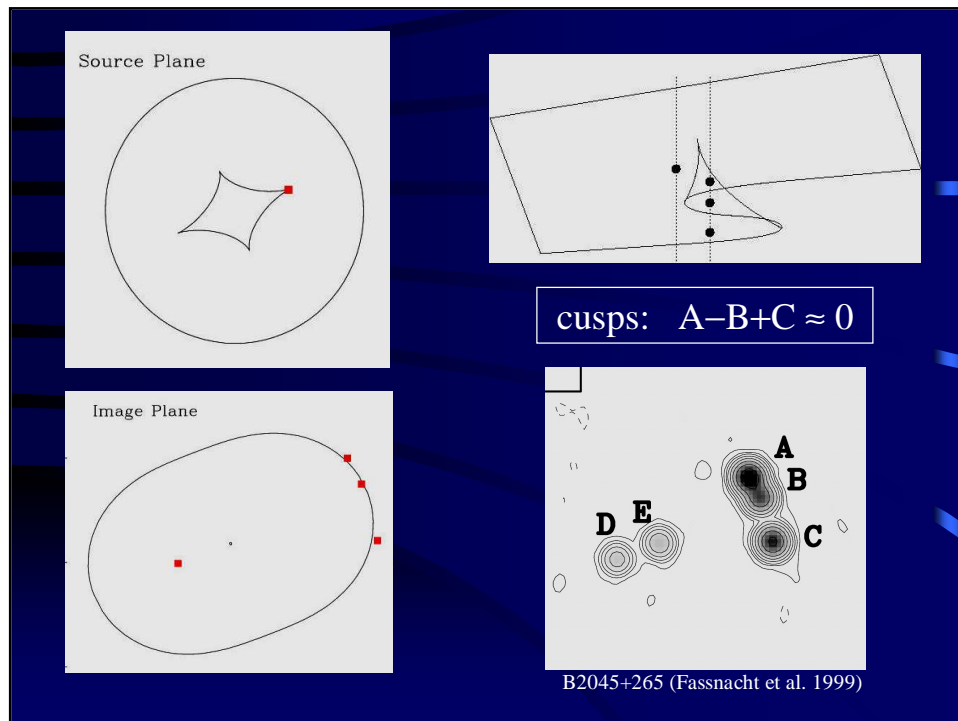
(CRK, Gaudi & Petters, astro-ph/0210318)

- Do the “anomalies” really indicate substructure? Or just a failure of imagination in the models?
- Proving a negative is hard!
- Fortunately, strong generic statements can be made about certain combinations of fluxes...

*(Forget about the causes or implications of the anomalies; for now let's just focus on finding them.)*



## Small Scale Structure and Gravitational Lensing

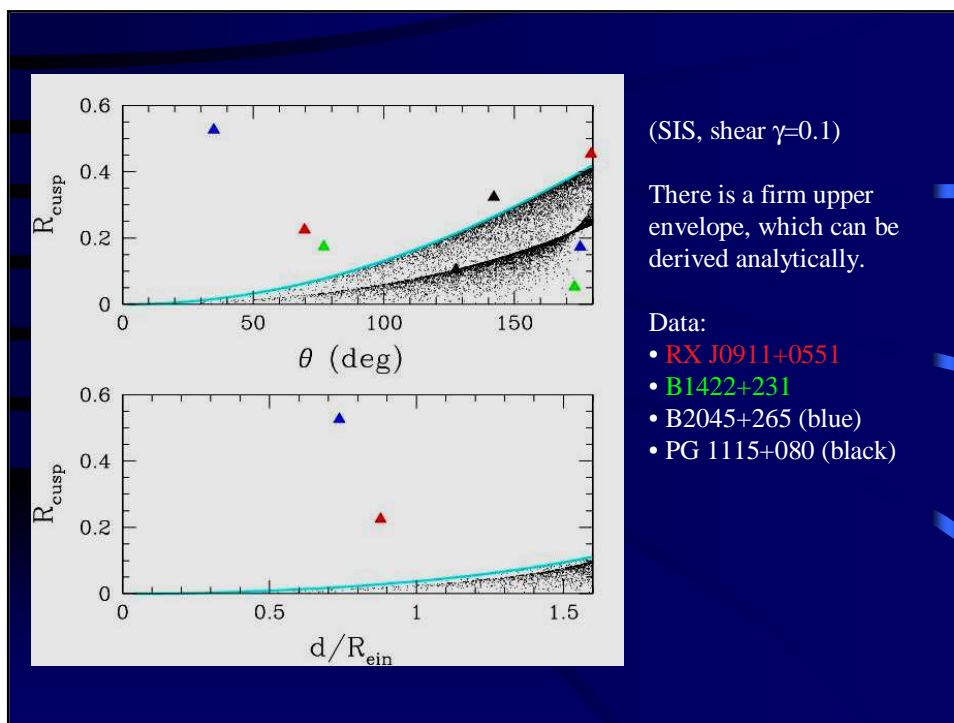


### Robustly Identifying Flux Ratio Anomalies

- The fold and cusp relations are strong model-independent statements.
- Violating them requires structure on scales smaller than the separation.
- But they require a source asymptotically close to the fold/cusp.
- How well do they hold in practice?  
Can we identify flux ratio anomalies directly from the data?

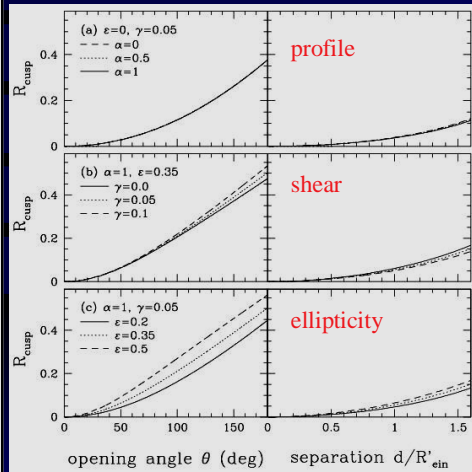
### Identifying cusp anomalies

- Pick a triplet of images
- Let:  
 $d$  = maximum separation  
 $\theta$  = angle subtended
- Define  
 $R_{\text{cusp}} = (A-B+C)/(A+B+C)$
- Now do Monte Carlos: generate mock lenses, examine distribution for  $R_{\text{cusp}}$

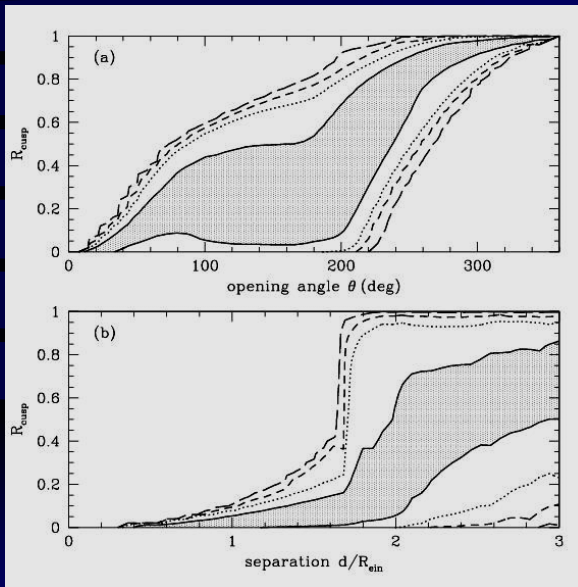




Parameter dependences

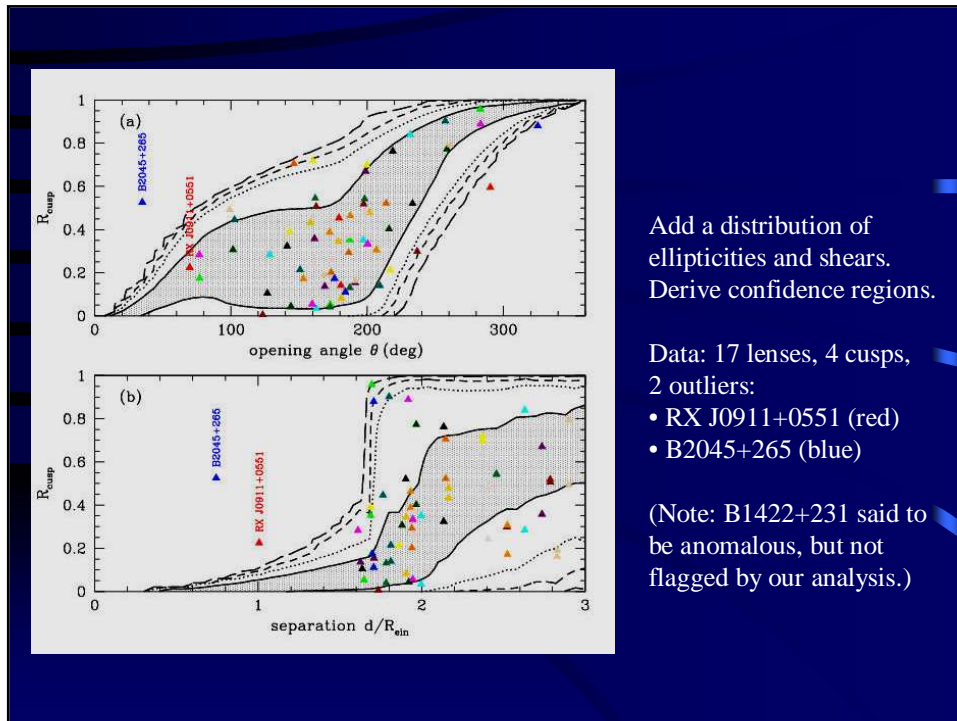


- Look at the (analytic) upper bound.
- Most sensitive to ellipticity, then shear.
- Not very sensitive to profile.
- General scaling  $R_{\text{cusp}} \propto \theta^2 \propto d^2$  for small  $\theta, d$



Add a distribution of ellipticities and shears. Derive confidence regions.

## Small Scale Structure and Gravitational Lensing



## Identifying flux ratio anomalies

- There are observed flux ratios that cannot be fit by any (reasonable) smooth model.
- We can find them using the fold and cusp relations.
- More sophisticated – less robust – methods are needed in some cases.
- Still, first link in chain from lenses to dark matter can be made strong.

## From lensing to dark matter physics

### Find flux ratio anomalies.

- Okay!

### Infer amount of substructure.

- What do flux ratio anomalies imply about galaxy mass distributions?
- What is ‘substructure’?
- Must the departure from smoothness be granular CDM clumps?
- Could it be stars, dwarf satellites, tidal streams, dark matter caustics, etc.?
- *Could the anomalies be caused by electromagnetic effects?*

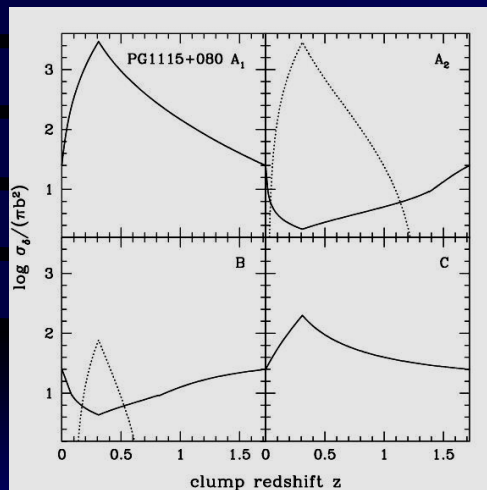
### Connect the substructure to CDM predictions.

- If it is CDM substructure, how much is there?
- What does CDM predict for the substructure mass fraction, the mass function and spatial distribution of subhalos, the amount of power on small scales?

### Constrain properties of the dark matter particle.

- How do predictions depend on assumption of cold, collisionless dark matter?

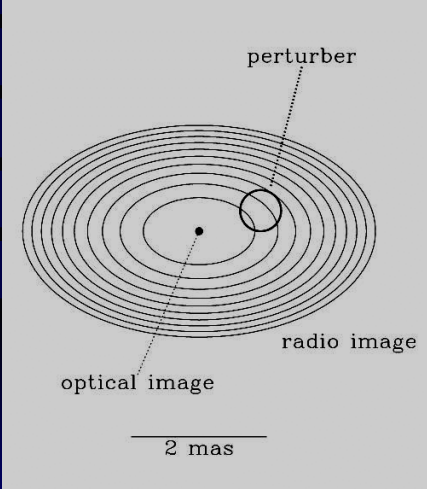
## Where do the clumps live?



(CRK astro-ph/0209040)

- Assumption: clumps lie in lens galaxy halos
- What about free-floating clumps?
- Effects strongest near lens galaxy, but still significant at  $\Delta z \sim 0.2$ .
- Jacqueline Chen: *isolated* clumps contribute few % of optical depth; *correlated* clumps may be more important.

### Beyond basic fluxes



- Source size often varies with wavelength
- Use to distinguish between stars, satellites
- Need  $R_{\text{ein}} \geq R_{\text{src}}$  to see an effect
- B1422+231:
  - Optical image *not* perturbed
  - Radio:  $R_{\text{src}} \sim 1 \text{ mas}$  implies  $M_{\text{sat}} \geq 10^6 M_{\text{sun}}$

(CRK astro-ph/0111595)

### Summary

**Current status:**

- Flux ratio anomalies can robustly be identified  
*... using the fold and cusp relations*
- Substructure has been detected  
*... in quantities that cannot be attributed to normal satellite populations*

**New theory:**

- To understand what we measure, what CDM predicts

**New data:**

- Source size, wavelength dependence, image shapes ...to distinguish between different types of substructure
- More lenses!

## Conclusions

### Core images:

- Probe densities in inner  $\sim 200$  pc of distant ellipticals.
- Stellar densities can explain the lack of observed core images.

### Flux ratio anomalies:

- There are flux ratios that cannot be fit by any smooth lens model, as shown by the fold and cusp relations.
- Compelling evidence for substructure, and hints of a link to the physics of dark matter.