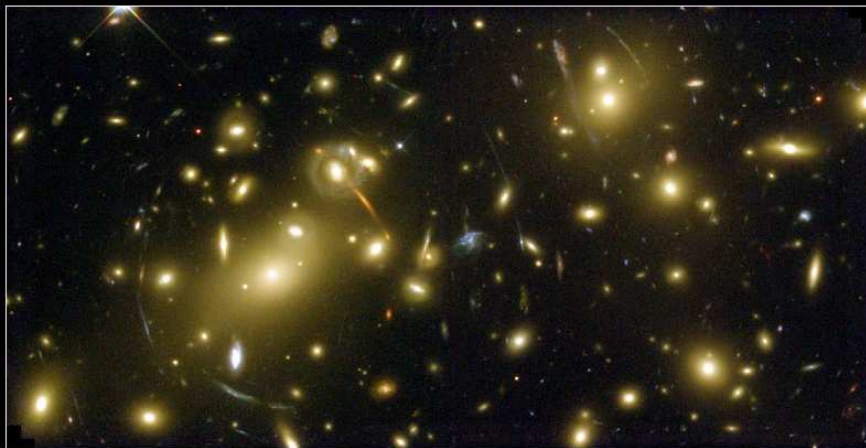


Outline

- **Galaxy clusters from weak lensing**
- **Dark clusters?**
- **Cluster Tomography**
- **N-body simulations**
- **Optimal filtering**
- **Constraining dark energy**

Gravitational Lensing

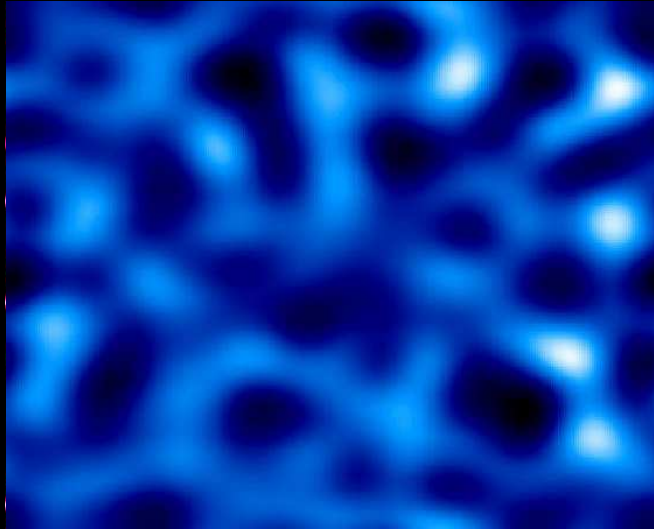


Galaxy Cluster Abell 2218

NASA, A. Fruchter and the ERO Team (STScI, ST-ECF) • STScI-PRC00-08

HST • WFPC2

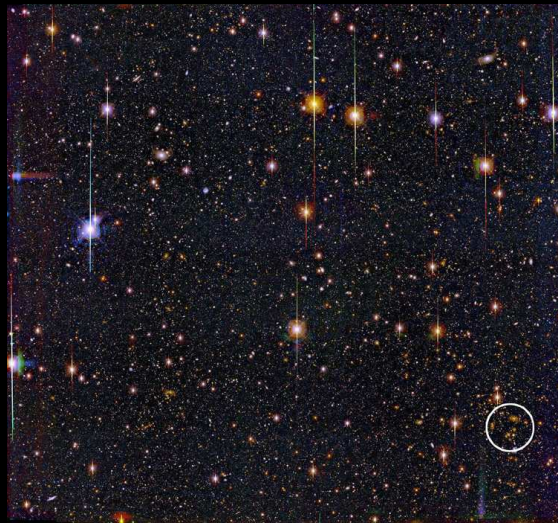
Weak Lensing by Large Scale Structure



Courtesy of Alexander Refregier

First Mass-Selected Cluster

(Wittman et al. 2001)



- First cluster discovered through its lensing effect rather than radiation!
- $\sigma_{\text{vel}} = 615 \text{ km s}^{-1}$
- $z_{\text{spectra}} = 0.28$
- Deep Lens Survey (DLS)
 - 28 deg²
 - could find ~ 200 clusters
- LSST
 - 30,000 deg²
 - up to 300,000 clusters

← 40' →

Mass-Selected Cluster Samples

How can we find clusters of galaxies?

- Optical
- X-ray
- Sunyaev-Zeldovich effect
- Weak lensing survey

} **Biased?**

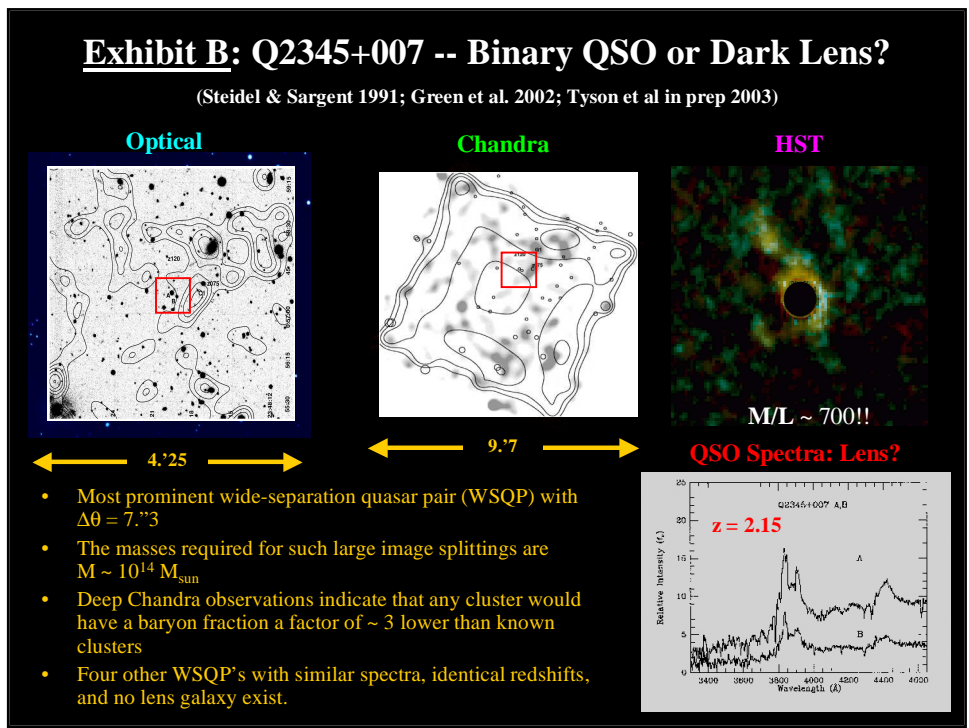
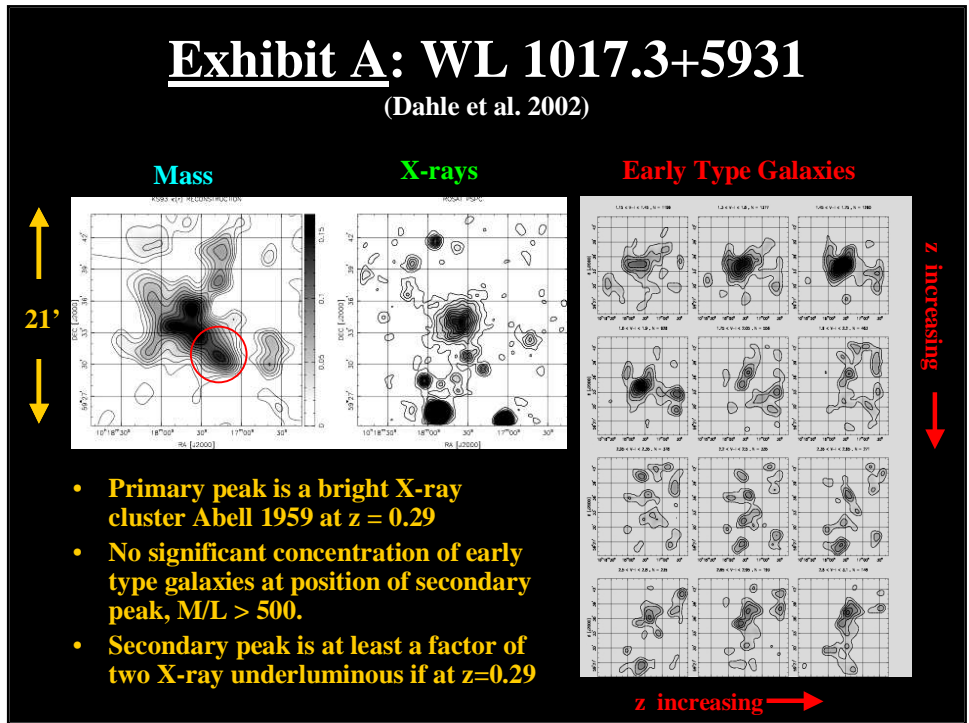
The first **Mass-Selected** cluster sample WILL:

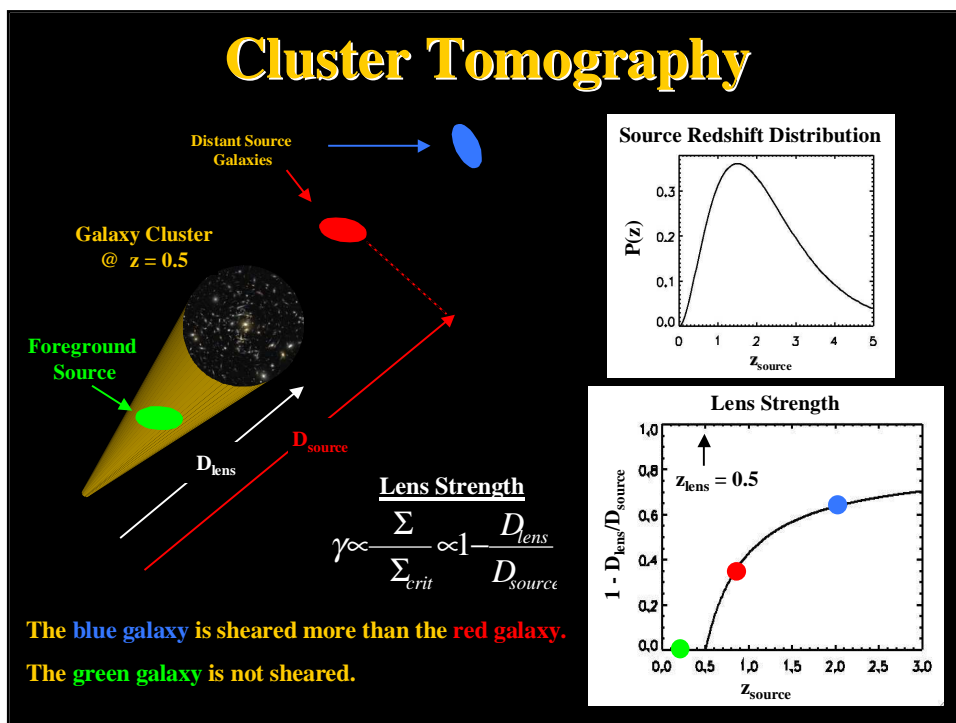
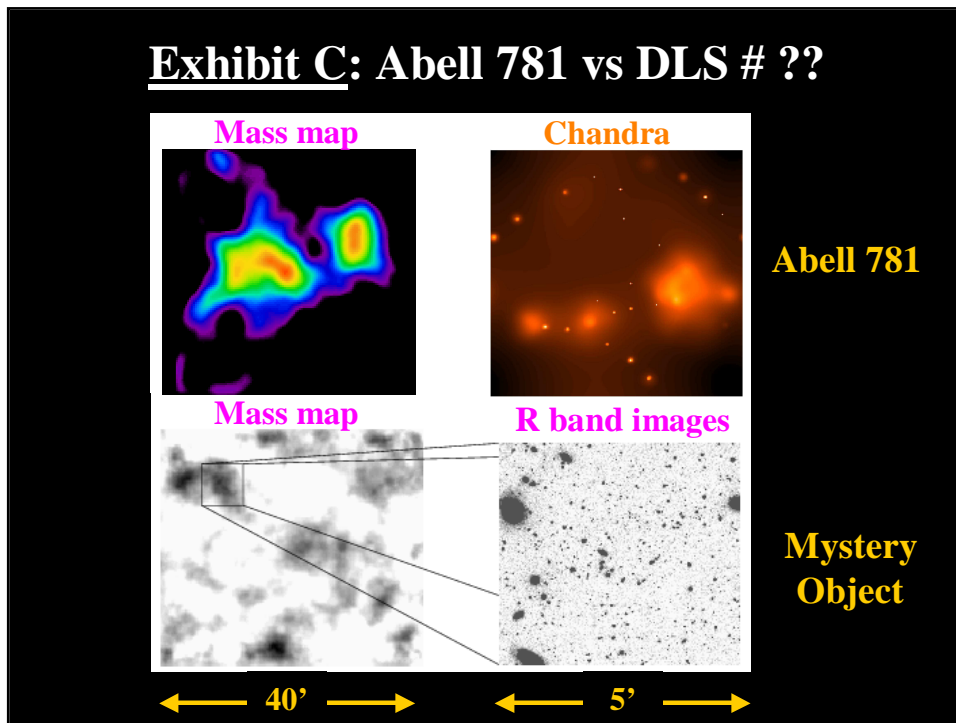
- Determine biases in other cluster samples
 - richness and morphology?
 - relaxed or merging?
- Test the “fair sample” hypothesis used to determine Ω_m . Is there a class of high M/L clusters?
- Number counts. Cosmological parameters with little assumption about baryons in clusters **➡ CONstrain DARK ENERGY**

Is there a population of **DARK CLUSTERS?**

The Case For Dark Clusters

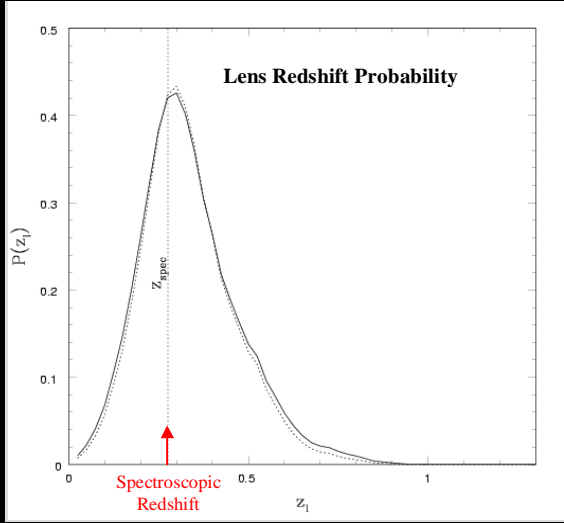
(circa 2002)





Cluster Tomography

(Wittman et al. 2001, 2002)

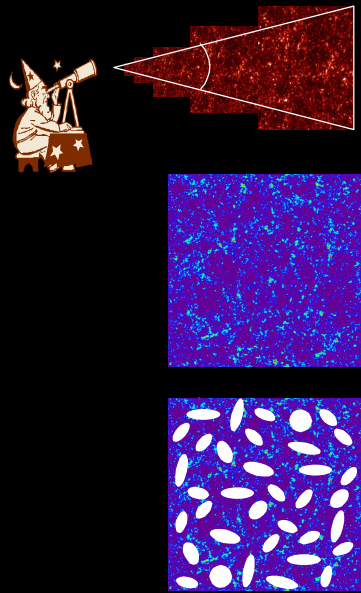


- Assume a mass profile and fit for shear as a function of source photometric redshift
- $z_{\text{spectra}} = 0.28$
- photo z's + tomography
 ➔ $z_{\text{lensing}} = 0.30$

How reliable is this technique?

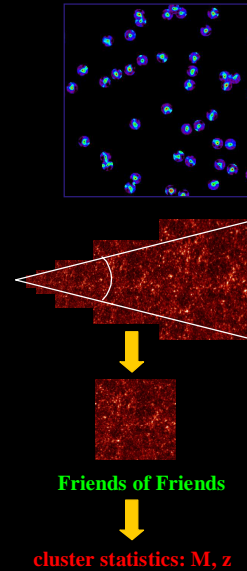
Weak Lensing Simulations

- Tile the light cone with N-body simulation cubes (White & Hu 1999)
- Project the matter distribution to determine the shear field at the observer
- Place mock source galaxies at random positions, consistent with observed number densities and intrinsic ellipticities
- Shear the mock galaxies with the shear field



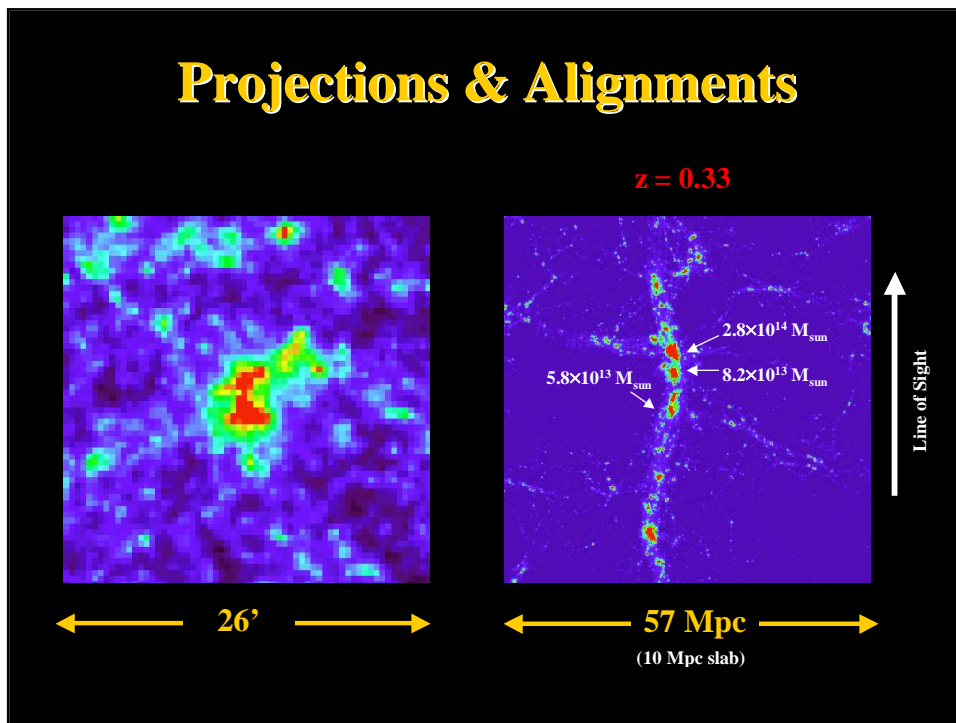
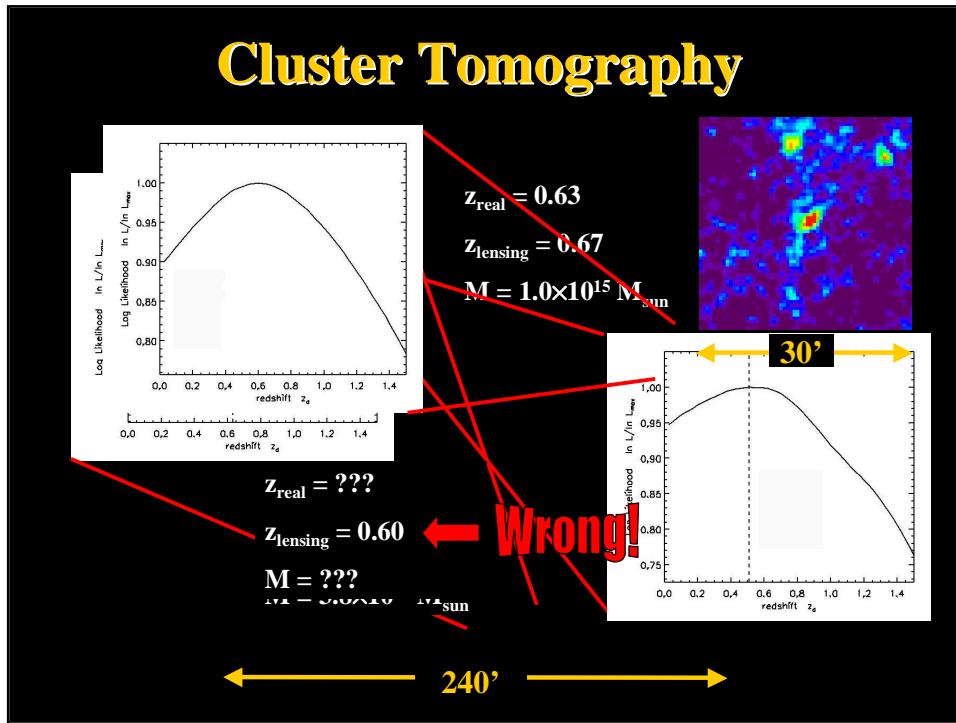
Weak Lensing Simulations

- Smooth the shear field with an “optimal filter” and search for peaks
- Apply a group finder to find collapsed halos. Detected clusters are traced back to simulation cubes for cluster statistics.



Advantages of Simulations

- **Properly simulate alignments and projections, which can be severe.**
- **The selection function can be simulated for any cosmology, foregoing the need to acquire a “complete” sample.**
- **Mock observations allow us to Monte-Carlo simulate parameter estimates, for realistic error forecasts.**
- **Fast Particle Mesh (PM) algorithm:**
 - simulate large areas of sky to accurately represent the statistics of rare events (every cluster is unique)
 - allows rapid exploration of parameter space



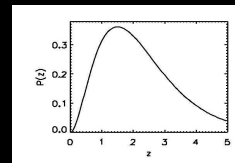
Optimal Filtering

- “Noise” in weak lensing searches for clusters requires that shear maps be smoothed
 - white noise from finite sampling and intrinsic ellipticities
 - confusion from large scale structure
 - projection effects
- For white noise a “matched filter” will optimally extract a signal of known shape
- Galaxy clusters are identified as the peaks in smoothed maps that lie above a threshold ν
- For any given threshold ν define the efficiency as the ratio
$$\text{efficiency} = n_{\text{clusters}} (> \nu) / n_{\text{peaks}} (> \nu)$$

Adaptive Matched Filter

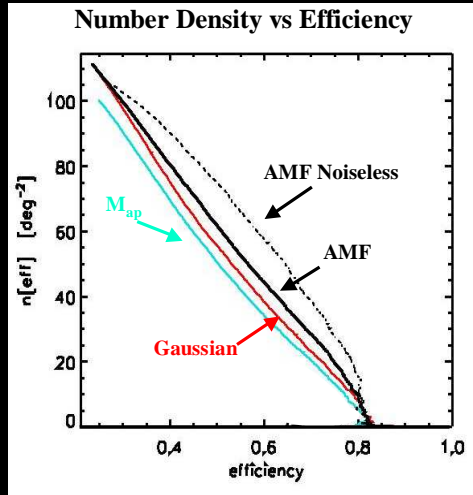
- In the absence of source redshifts, the observable is the mean shear averaged over the source redshift distribution

$$\bar{\gamma} = \int P(z) \gamma(z) dz$$



- Two filters have been widely used on this quantity
 - Gaussian
 - Aperture Mass $M_{\text{ap}}(\theta)$
- If photometric redshifts are available for some sources, tomography and matched filtering can be combined.
- *Adaptive Matched Filtering* uses redshift information to optimally weight source galaxies, producing a likelihood and tomographic redshift for each line of sight

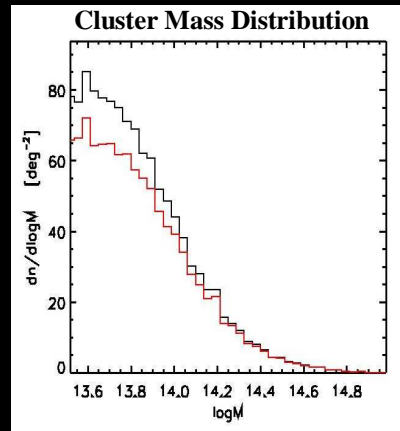
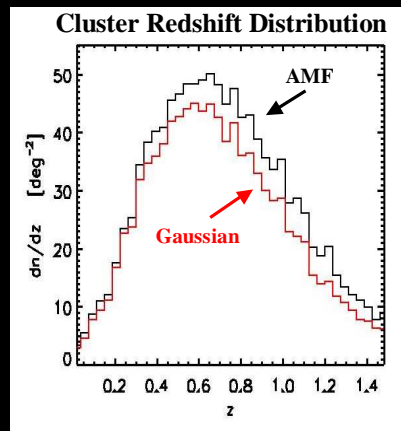
Adaptive Matched Filter



LSST noise model: $n = 80 \text{ arcmin}^{-2}$; $\sigma_g = 0.33$; photo z 's for 80% of sources

- The maximum intrinsic efficiency of weak lensing cluster surveys is $\sim 80\%$
- Dark clusters cannot be distinguished from the projections, but statistical conclusions can be made
- For the most significant detections, the dispersion in tomographic redshifts is still $\sigma_z \approx 0.2$
- Photo z 's increase the number of clusters detected by 10-20%

Adaptive Matched Filter



The Adaptive Matched Filter detects more clusters at high redshift and low mass.

Cluster Counting Basics

- Goal: Determine cosmological parameters by comparing the observed distribution of clusters to predictions from theory/N-body simulations
- However cluster mass is not an observable. Instead we measure:
 - SZ decrement
 - X-rays (L_X or T_X)
 - Richness
 - Galaxy σ_v
 - Shear γ
- To interpret the observations we must know
 - $M(\text{observables}, z)$
 - $\text{Completeness}(\text{observables}, z)$

Cluster Counting Caveats

- Usually one writes

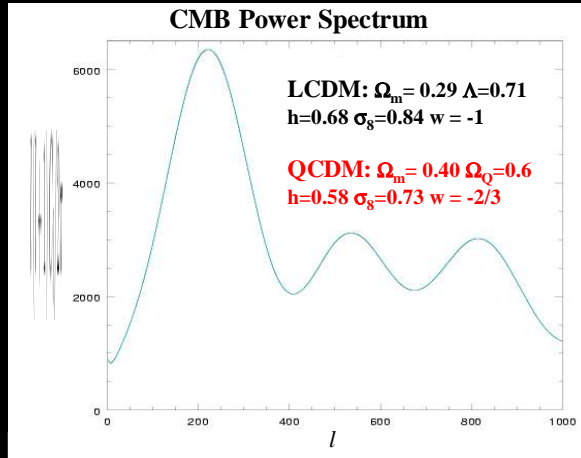
$$\frac{dN}{d\Omega dz}(w) = \frac{dV}{d\Omega dz} \int_{M_{\text{limit}}(z)}^{\infty} C(M, z) \frac{dn}{dM}(M, z | w) dM$$

Are we learning about this number?

Or about these quantities?

- The mass function is steep and exponentially sensitive to errors in $M_{\text{limit}}(z)$ and uncertainty in $M(\text{observables}, z)$. These errors mimic cosmological parameter changes!
- Until these relationships (and their scatter) can be empirically calibrated, this test relies on **uncertain assumptions about baryons in clusters**
- Solutions: Either determine $M_{\text{limit}}(z)$ from your cluster survey, or devise a test that is insensitive to the limiting mass.

CMB Degeneracy



Quintessence parameter 'w'

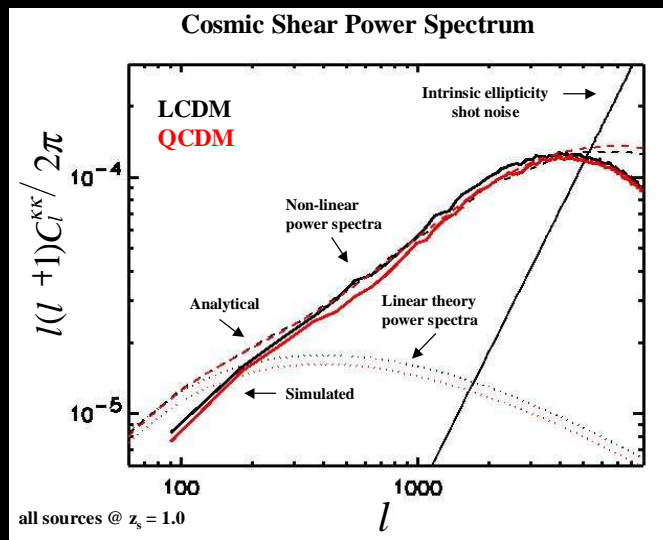
$$\rho_{DE} = w\rho_{DE}$$

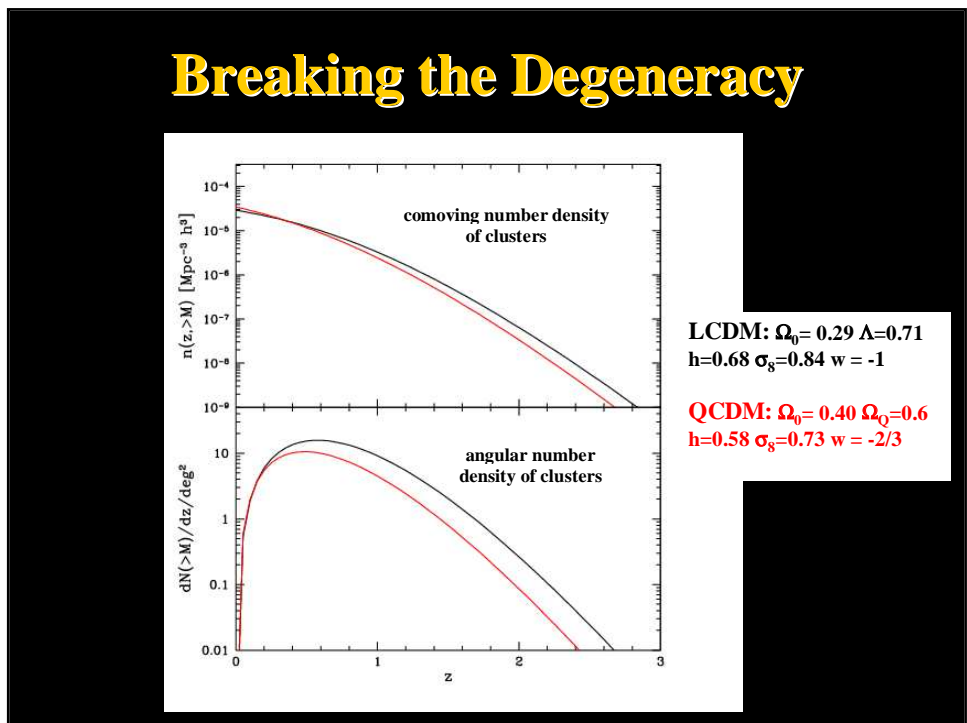
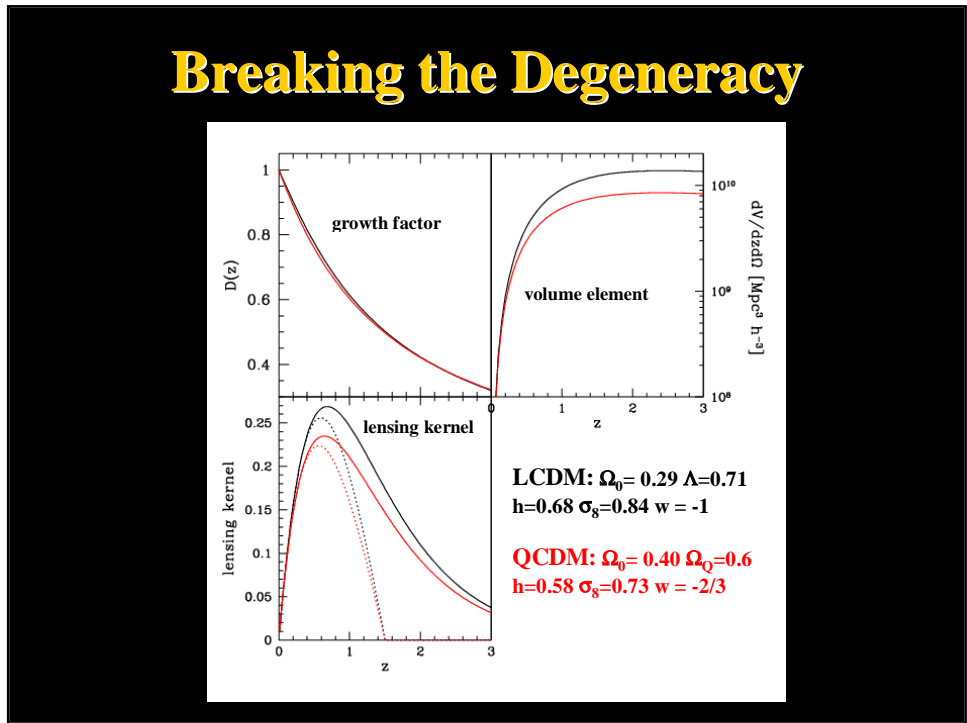
$w = 0$ -- matter
 $w = -1$ -- Λ , cosm const
 $w = 1/3$ -- radiation

$$\rho_{DE} \propto (1+z)^{3(1+w)}$$

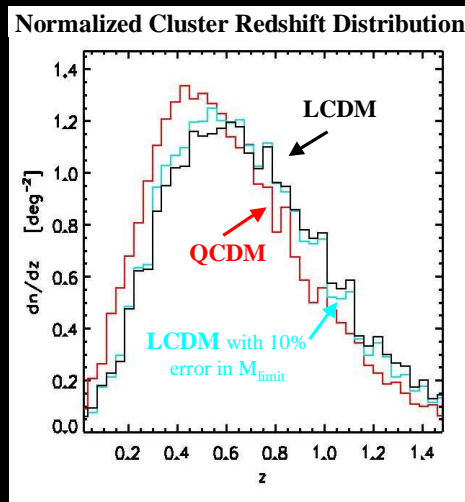
Parameter combinations that leave the angular diameter distance to the last scattering surface *and* the physics of acoustic oscillations unchanged produce identical CMB power spectra

Cosmic Shear Degeneracy





QCDM or LCDM?



- Redshift distributions differ at a high statistical significance
- The lensing efficiency is broader for LCDM than for QCDM, and thus probes a broader range of z and M
- Unlike other cluster counting surveys, this test is **ROBUST** against uncertainties in mass limit.

Conclusions

- Fast numerical simulations of weak lensing are a valuable tool to accurately predict cluster statistics over a large region of parameter space
- Using photo z 's with an Adaptive Matched Filter detects up to 10-20% more clusters and recovers more clusters at high redshift and low mass.
- Even for the most significant detections, the dispersion in tomographic redshifts is still $\sigma_z \approx 0.2$.
- Weak lensing cluster surveys are plagued by projections --- the maximum intrinsic efficiency is $\sim 80\%$.
- Only statistical statements about a population of dark clusters can be made from weak lensing
- The normalized redshift distribution of mass selected clusters is a powerful probe of dark energy and is insensitive to uncertainties in the mass limit.