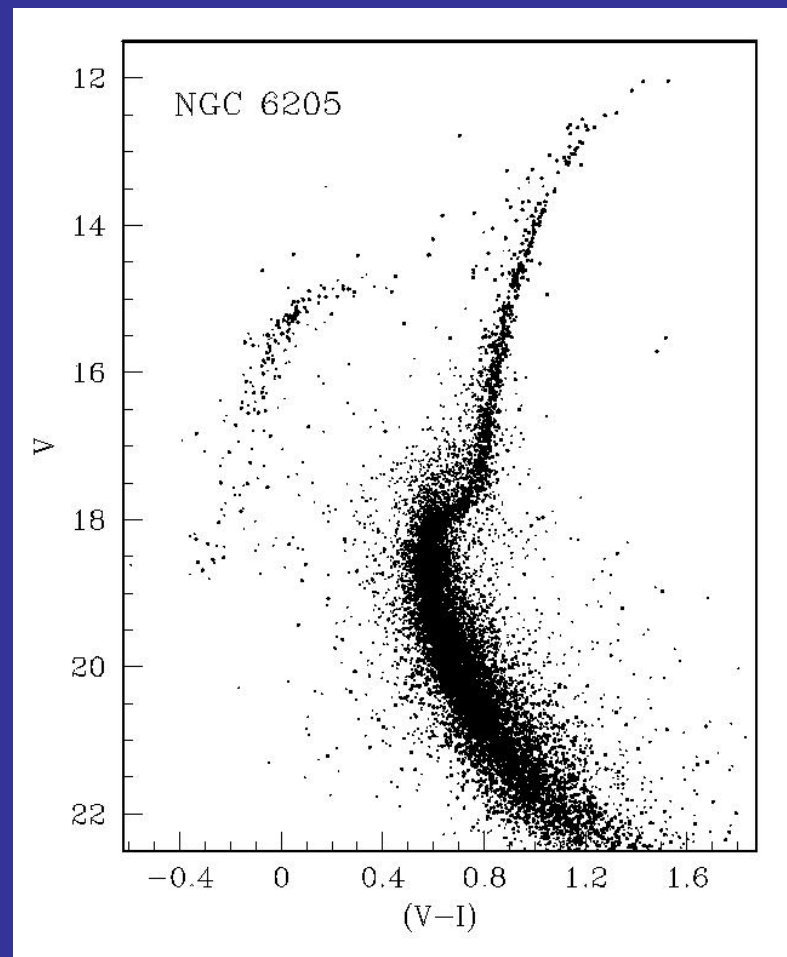
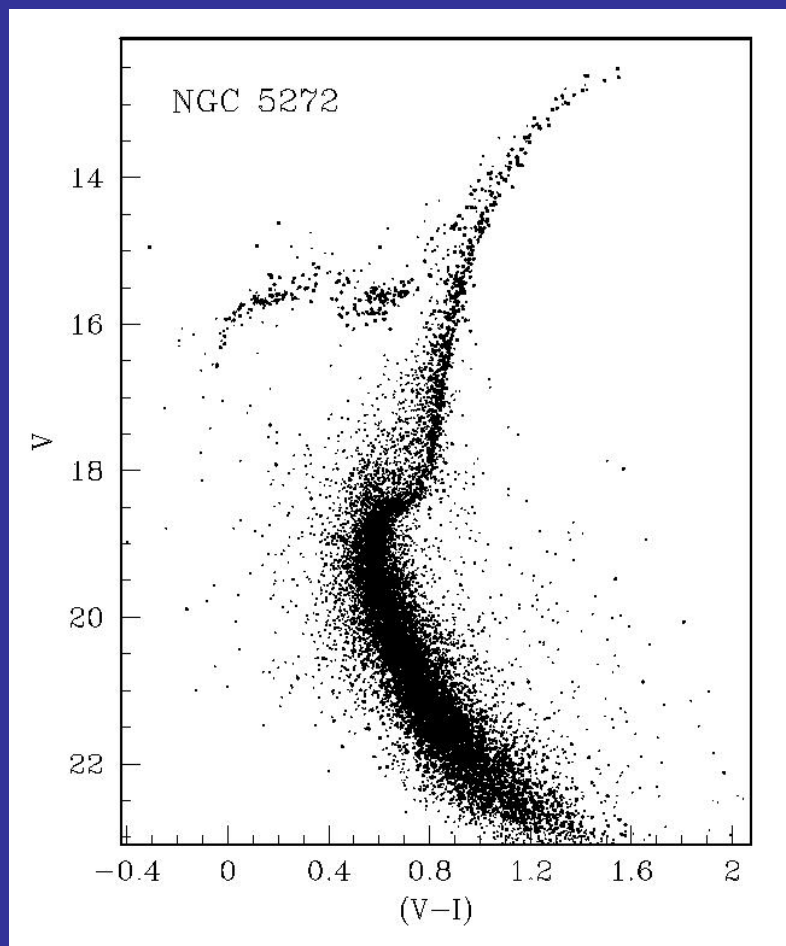


Na-O Anticorrelation and the distribution of stars along the HB

*Raffaele Gratton, Eugenio Carretta,
Angela Bragaglia, Sara Lucatello
and all the Naaah collaboration*

Faulkner (1966): metallicity drive colours of HBs for GCs
Second parameter effect (discovered by Sandage & Wildey 1967; and Van den Bergh 1967)

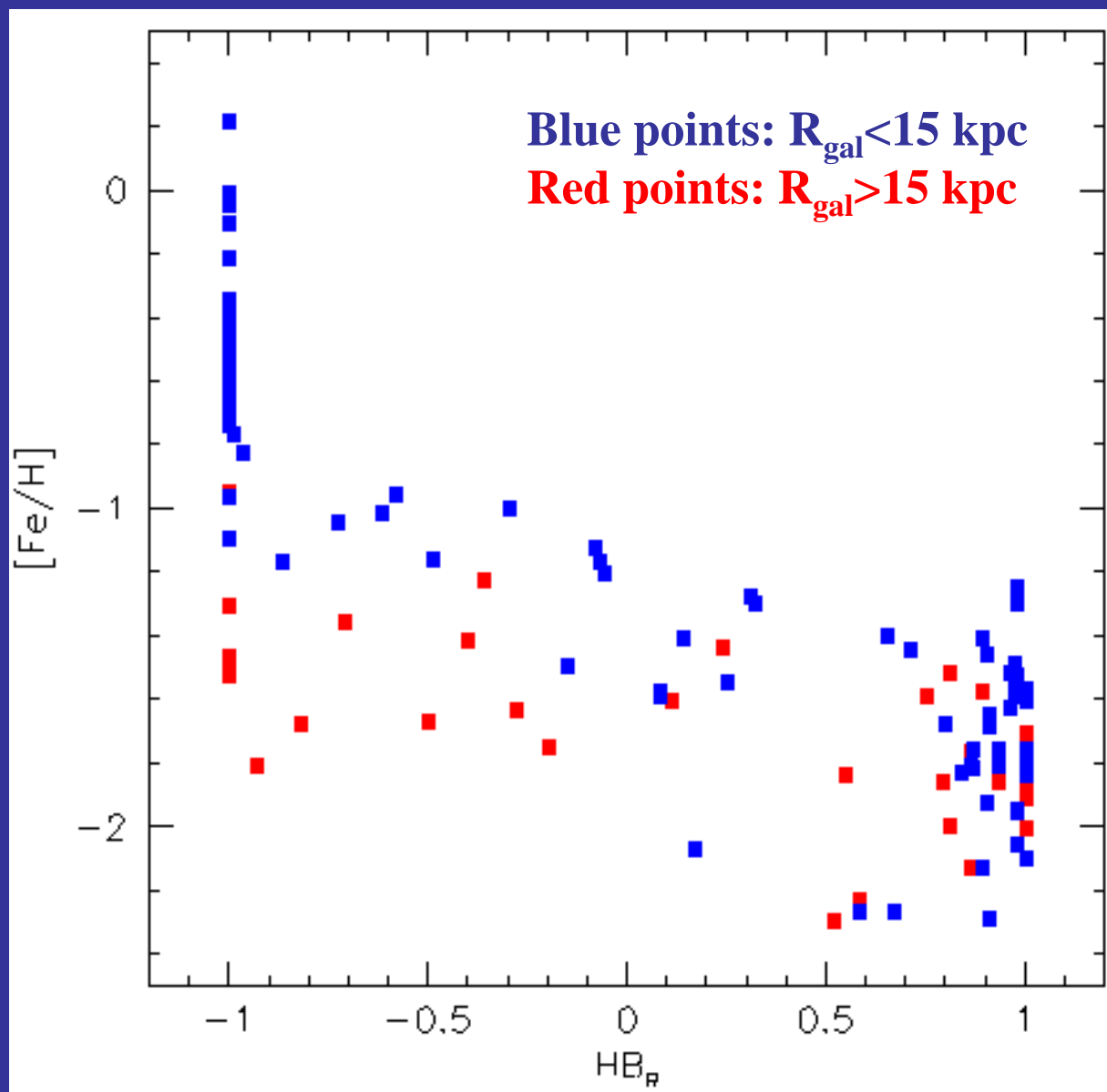
(M3-M13: data from Rosenberg): The two clusters have nearly the same metallicity ($[Fe/H] \sim -1.4$) and very different HB



Second parameter effect

Zinn (1978) noticed that the galactocentric distance r_{gal} is a second parameter.

This might be related to age differences of about 2 Gyrs between inner and outer halo GCs

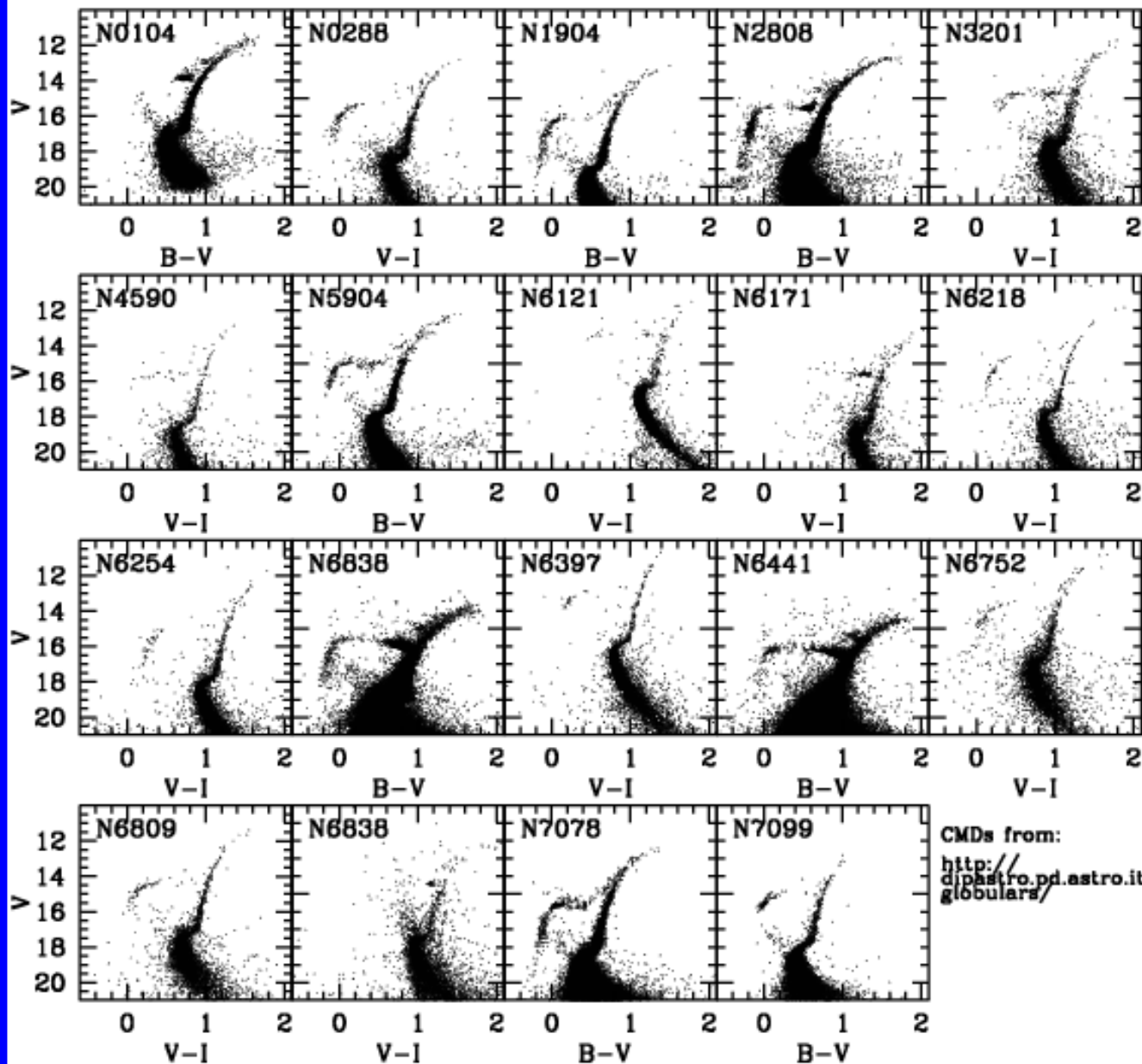


The second parameter

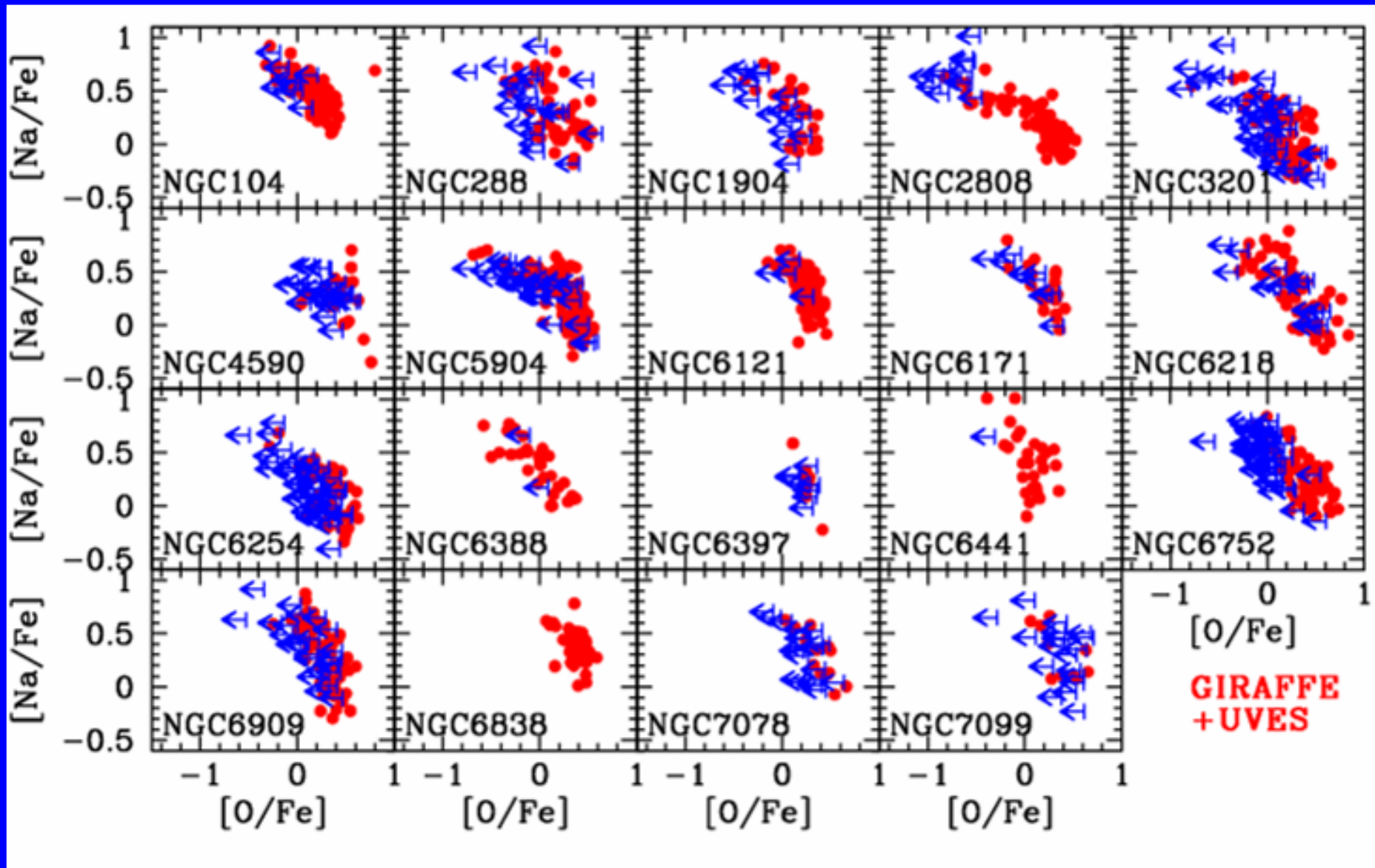
- However there is more than one second parameter
- Many indications that the second parameter is related to the O-Na anticorrelation (D'Antona & Caloi, etc.)
- A way to discuss the second parameter is quantifying mass loss between the TO and the HB

New data available

- Homogeneous set of c-m diagrams
- Accurate relative age determinations (Rosenberg et al., De Angeli et al.): error ~5-7% (even best from ACS data, but not yet published)
- Our new determinations of the chemical composition



From
 Piotto's
 database
 (Padova)



Homogeneous analysis, Giraffe spectra for large statistics in Na and O, UVES spectra for a lot of elements + Some literature data (NGC 362, M3, M13, M92)

Mass Loss determination

- Masses of stars at Turn-off:
from the following relation fitting isochrones:

$$M_{\text{TO}} = 0.834 \cdot 10^{-0.259 \log \text{Age}} \cdot (1.0 + 0.297 \times 10^{[\text{Fe}/\text{H}] + 0.7 [\alpha/\text{Fe}]}) M_{\odot}$$

Age
term

$[\alpha/\text{Fe}]$
term

Metal
abundance
term

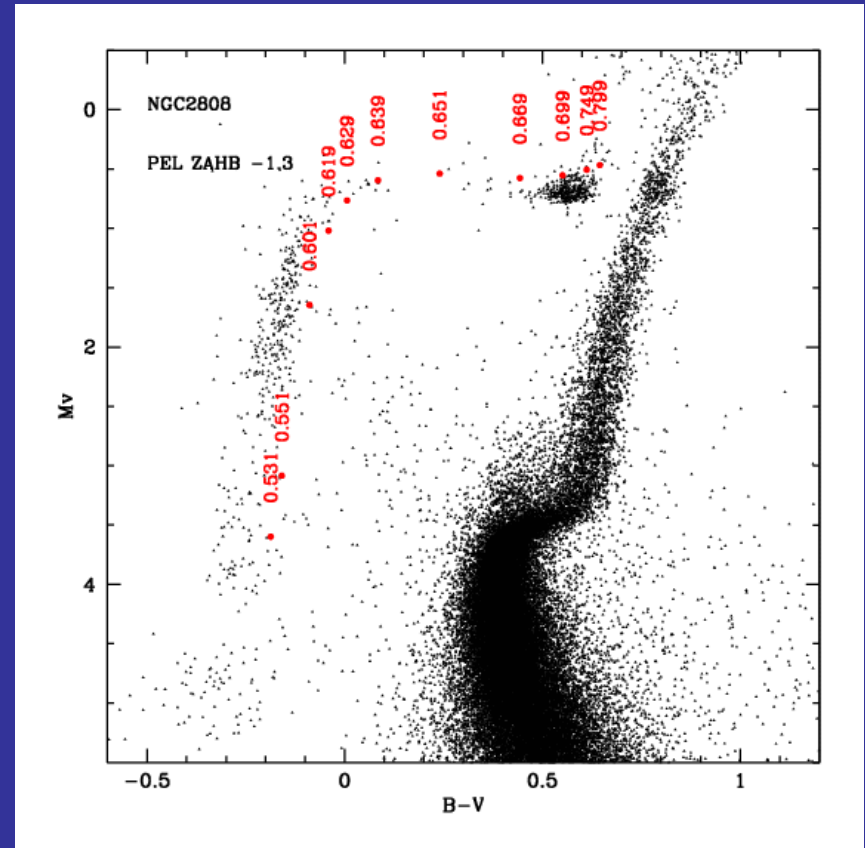
Age is the age parameter from De Angelis et al.,
or where missing from Rosenberg et al.

$[\text{Fe}/\text{H}]$ and from our determinations

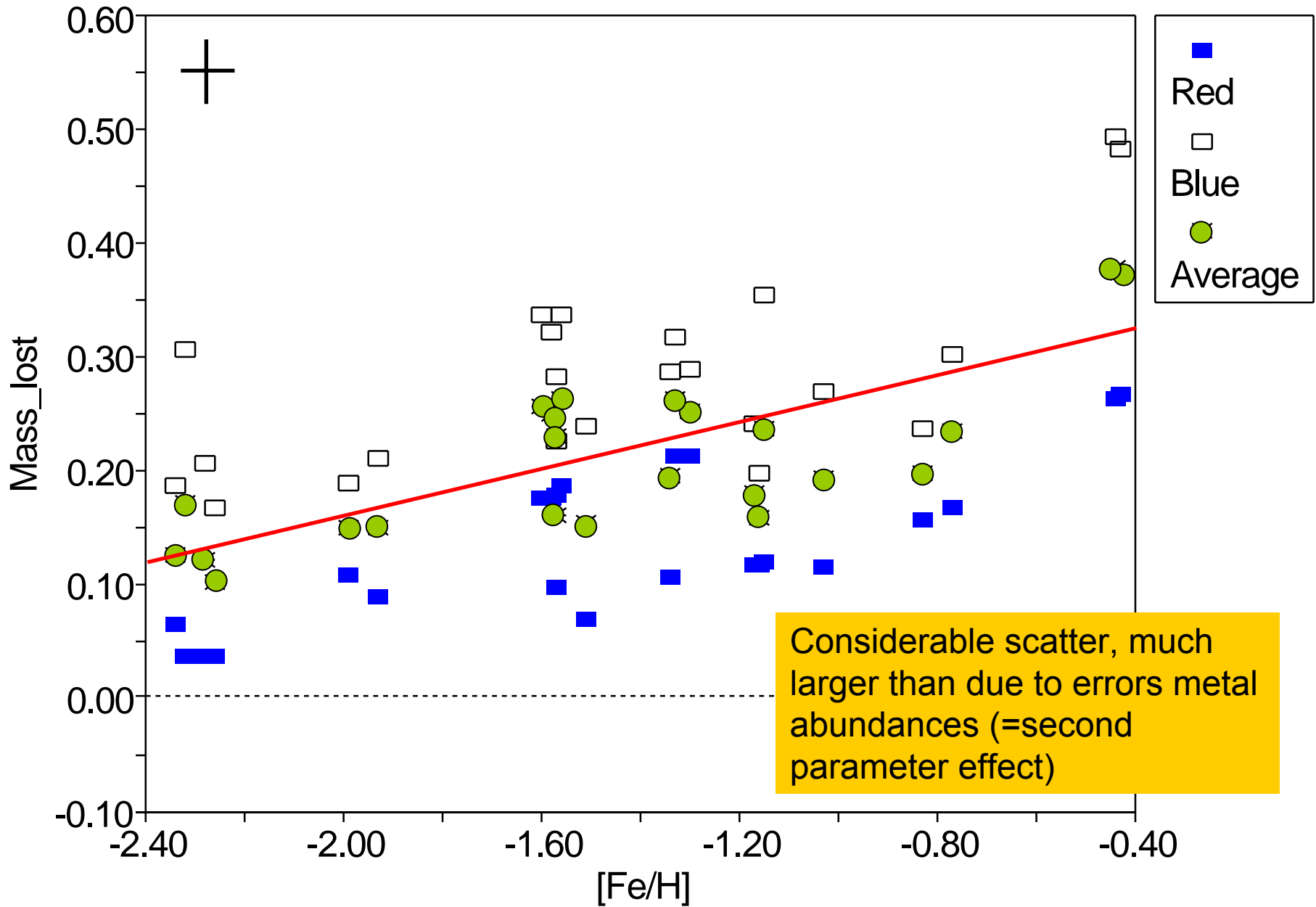
We assumed a similar overabundance of α -
elements in all stars ($[\alpha/\text{Fe}]=0.4$)

Masses of stars on HB

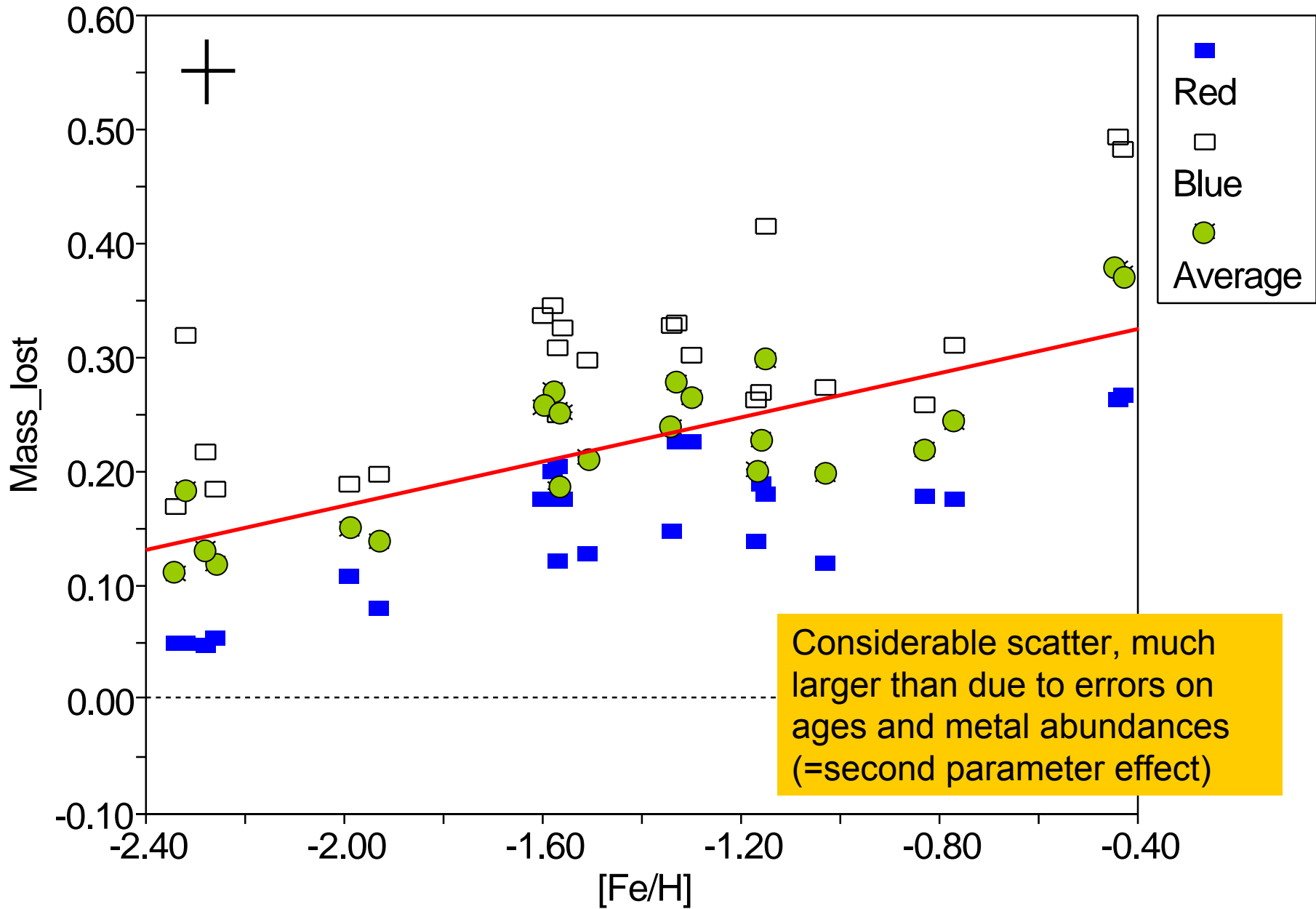
- Masses of stars on the HB from eye comparison between observed c-m diagrams and HB models by the Pisa Evolutionary Library
- Interpolations in a grid of ZAHB models of different metallicity
- The red edge (=larger mass) is uncertain in metal-rich clusters due to saturation



WITHOUT HE-PRODUCTION AND NO AGE DIFFERENCE



WITHOUT HE-PRODUCTION BUT WITH AGE DIFFERENCES



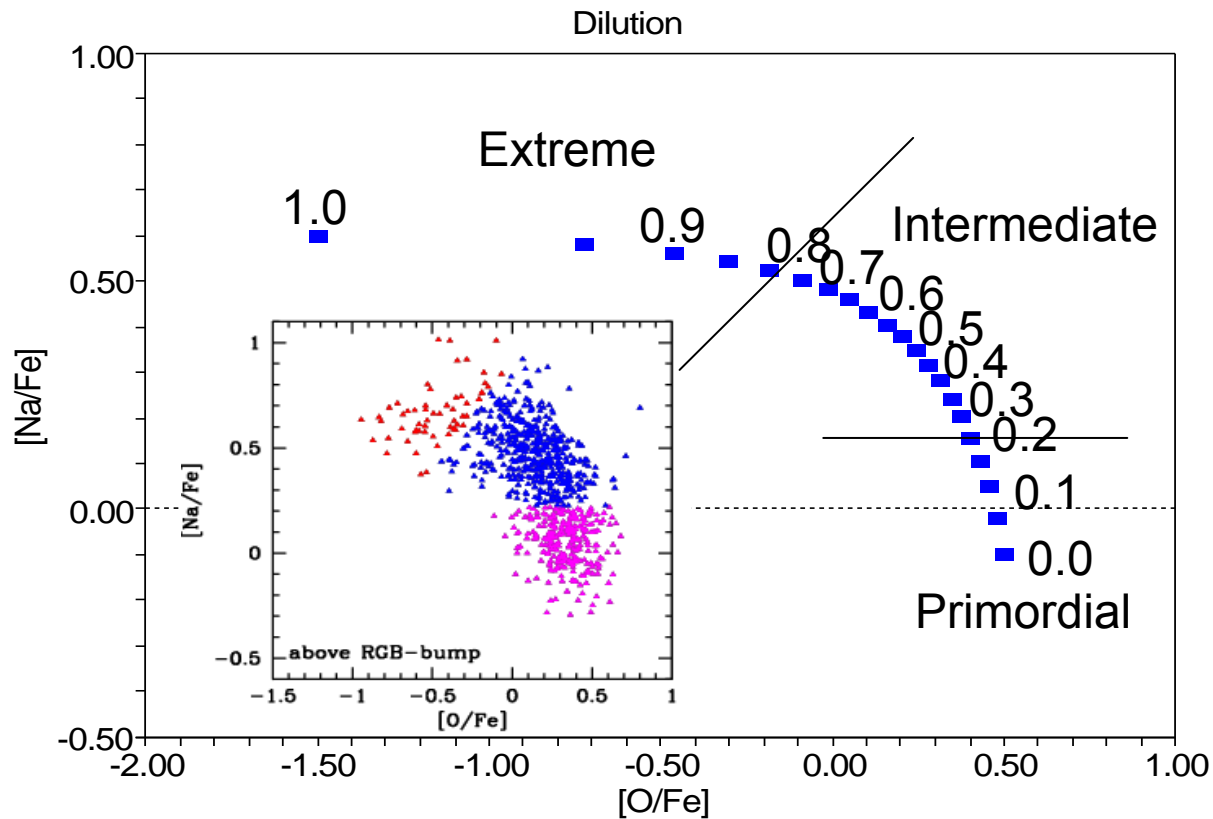
He abundance as a second parameter

- Let us assume that the He abundance is a second parameter
- He abundance has two effects:
 - A different (generally smaller) mass for stars at TO
 - A different color and luminosity of stars on the HB. Due to these effects, a different mass is obtained for stars on the HB
- How to obtain the He abundances: from the distribution of the O-Na anticorrelation
- However, we lack of reliable nucleosynthesis predictions
- For this reason we will adopt a model (based on dilution) with at least one free parameter, that will be obtained by fitting data.

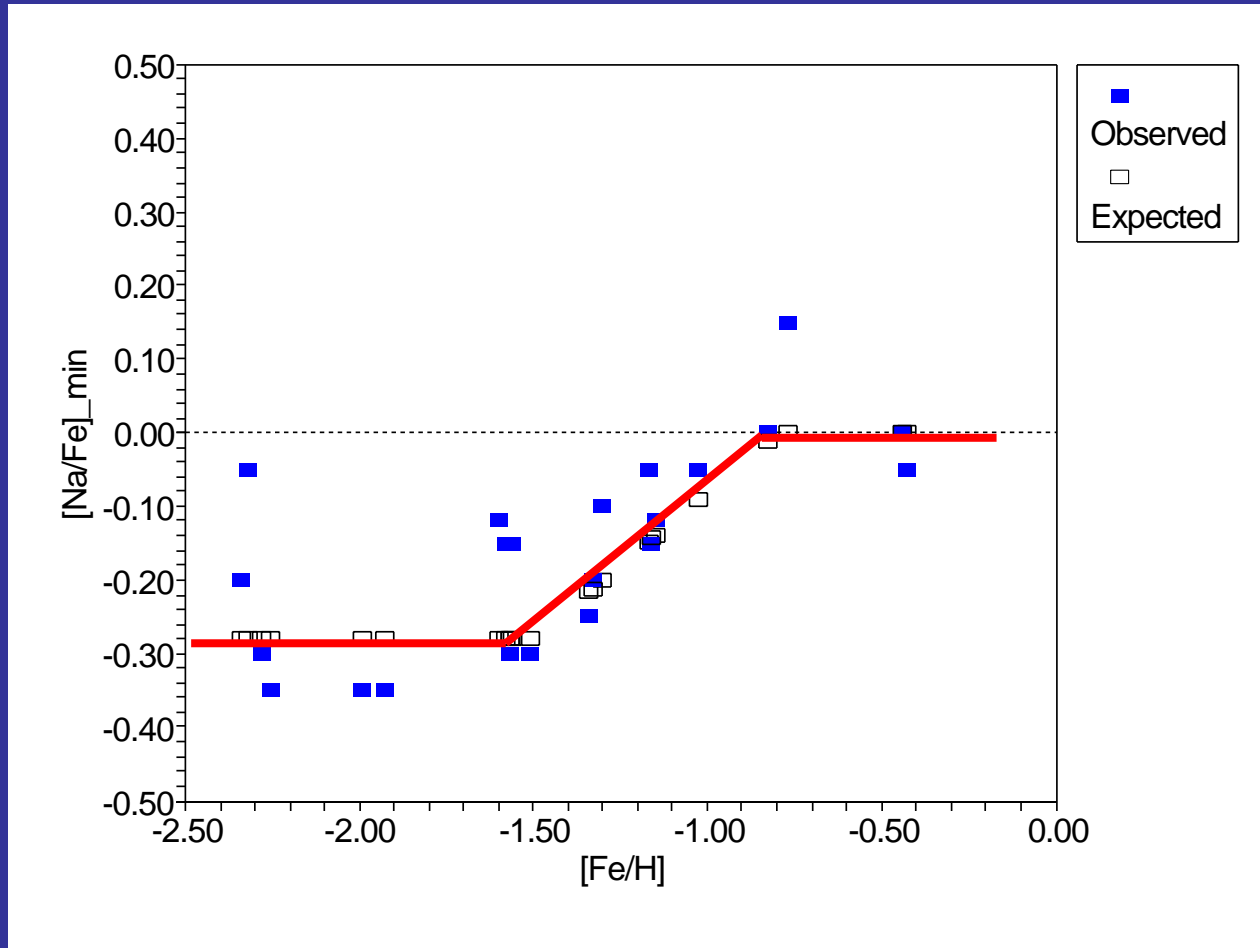
Dilution Model

- A model where polluted Na-rich, O-poor material is diluted into pristine Na-poor, O-rich material reproduces very well the expected O-Na anticorrelation (see Prantzos & Charbonnel 2006)
- It also reproduces Li abundances (Li is not null in the O-poor stars of NGC6752!)
- It is very interesting to use such a simple model in order to predict the distribution of stars on the HB starting from the observed distribution of stars along the Na-O anticorrelation
- In this model the logarithmic abundance of an element [X] for a given dilution factor dil is given by:
$$[X] = \log\{(1-dil) 10^{[X_o]} + dil 10^{[X_p]}\},$$
where [X_o] and [X_p] are the logarithmic abundance of the element in the original and polluted material

	[Na/Fe]	[O/Fe]
$[X_o]$	Na expected	0.5
$[X_p]$	0.6	-1.5

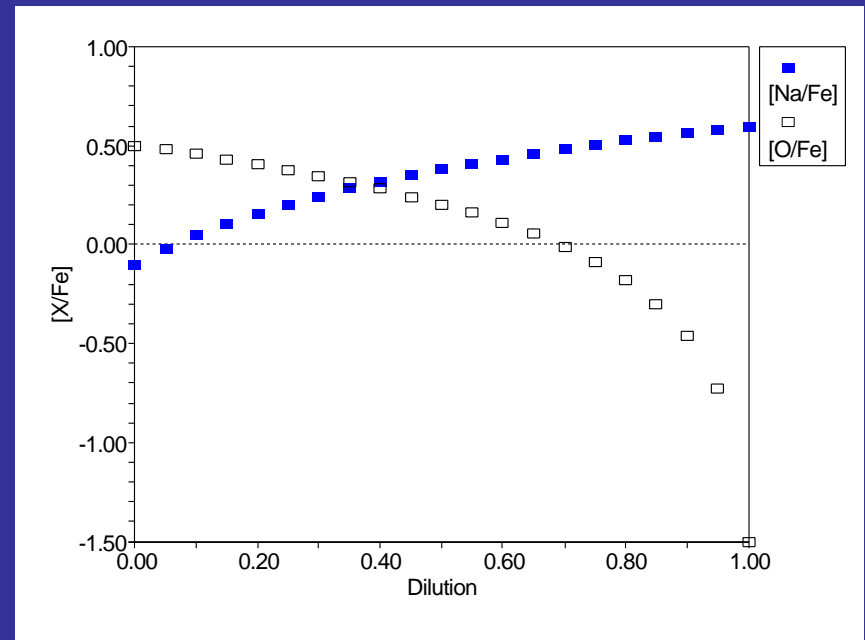


Expected original Na abundance



Estimate of minimum and maximum dilution

- In principle, minimum and maximum dilution can be derived from both O and Na abundances
- However, Na abundances is much better suited for minimum dilution and O for maximum dilution because of saturation



He and dilution

- Once the minimum and maximum dilution are determined, the minimum and maximum He content can be derived:

$$Y_{\min} = Y_{\text{BB}} + x \text{Dil}_{\min}$$

$$Y_{\max} = Y_{\text{BB}} + x \text{Dil}_{\max}$$

- In this model x is a free parameter, which represents the (average) He enrichment of the polluting material

TO mass in stars of different He

- The minimum and maximum mass of TO stars are then derived using the relation:
 - $M_{\max}(\text{TO}) = M_{\text{ref}}^{-1.3} \text{dil}_{\min} x$
 - $M_{\min}(\text{TO}) = M_{\text{ref}}^{-1.3} \text{dil}_{\max} x$
- The value of x is adjusted in order to have on average the same mass loss for stars at the blue and red edge of the HB

HB mass in stars of different He

- Before making this comparison, we should note that the masses derived for stars on the HB depend on the assumed He abundance
- The effect is important only for the minimum mass (i.e. stars at the blue edge)
- We corrected the mass previously derived (where $Y=0.25$) using the formula:

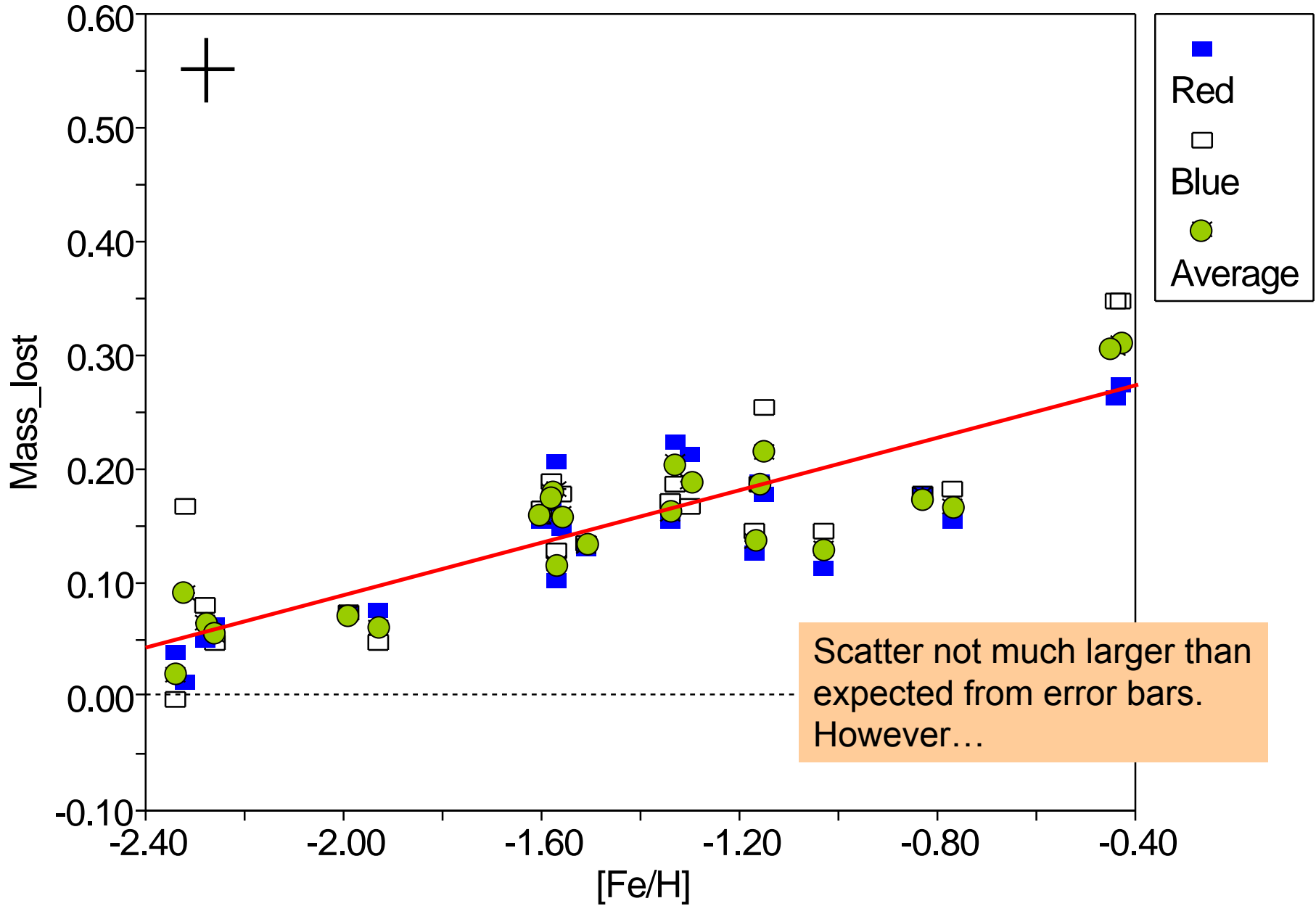
$$M_{\min}(\text{HB}) = M_{\min}(\text{HB})_{Y=0.25} + \Delta M$$

Where:

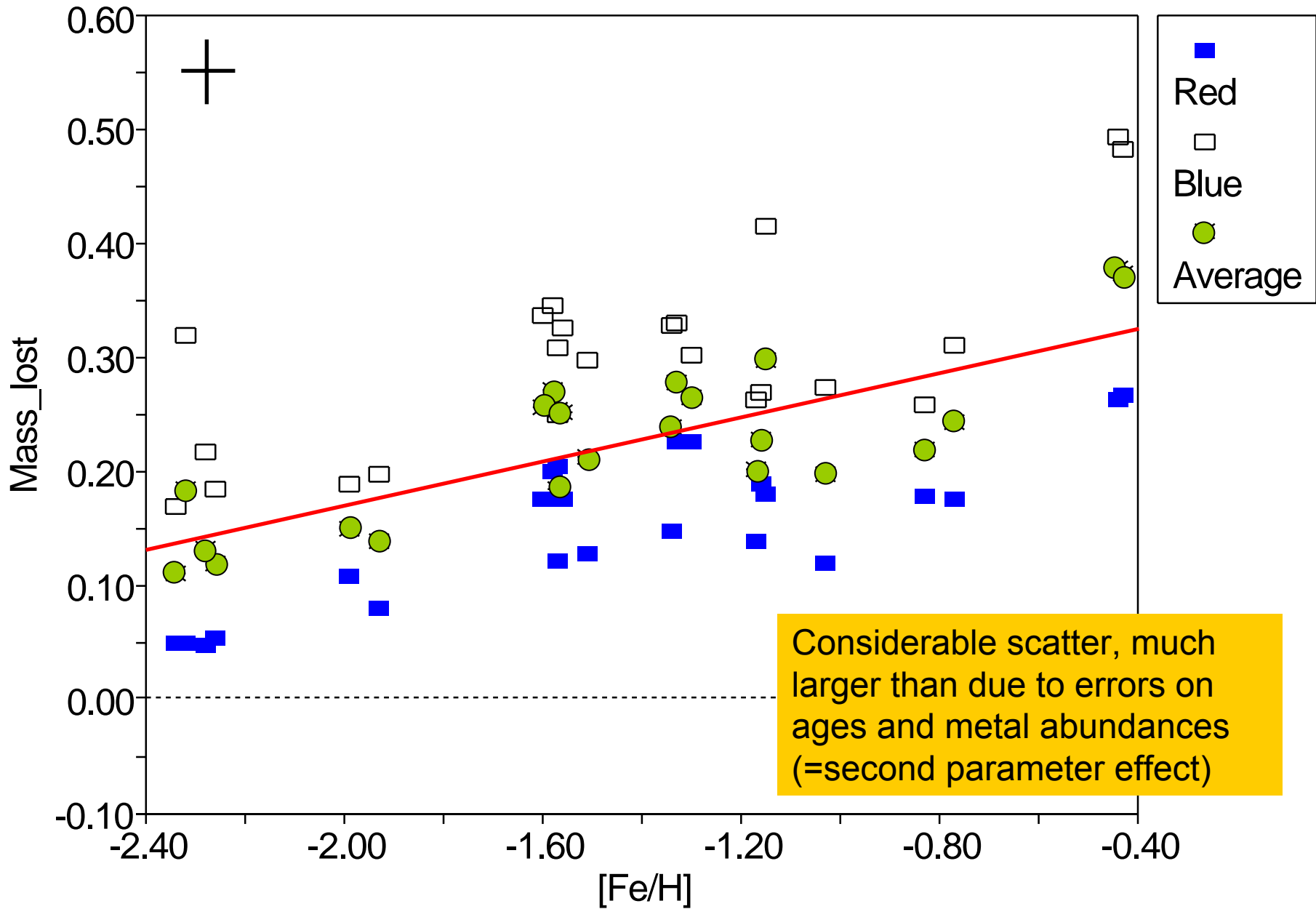
$$\Delta M = \max\{0, [-0.27 ([\text{Fe}/\text{H}] + 1.5) + 0.12] [Y_{\max} - 0.25]\}$$

- Of course, this procedure should be solved iteratively, because the value of Y_{\max} depends on x , which in turn is determined by assuming a given value for $M_{\min}(\text{HB})$
- The best value for x is $x=0.12$

WITH HE-PRODUCTION

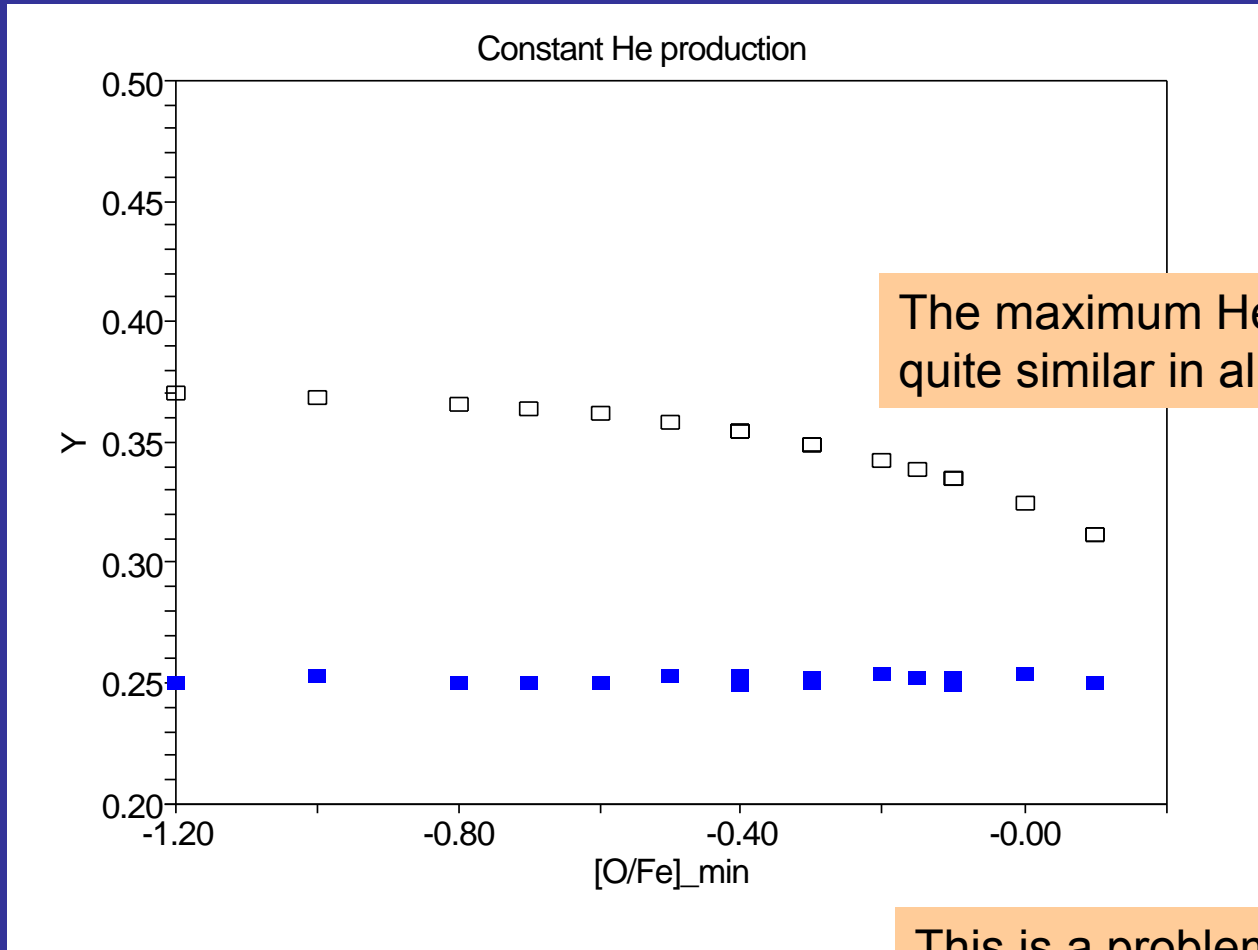
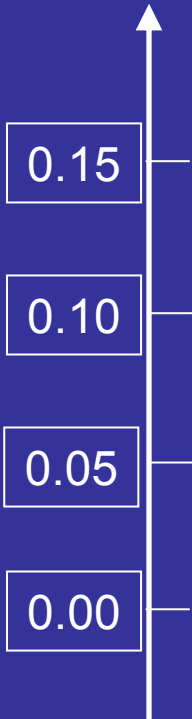


WITHOUT HE-PRODUCTION BUT WITH AGE DIFFERENCES



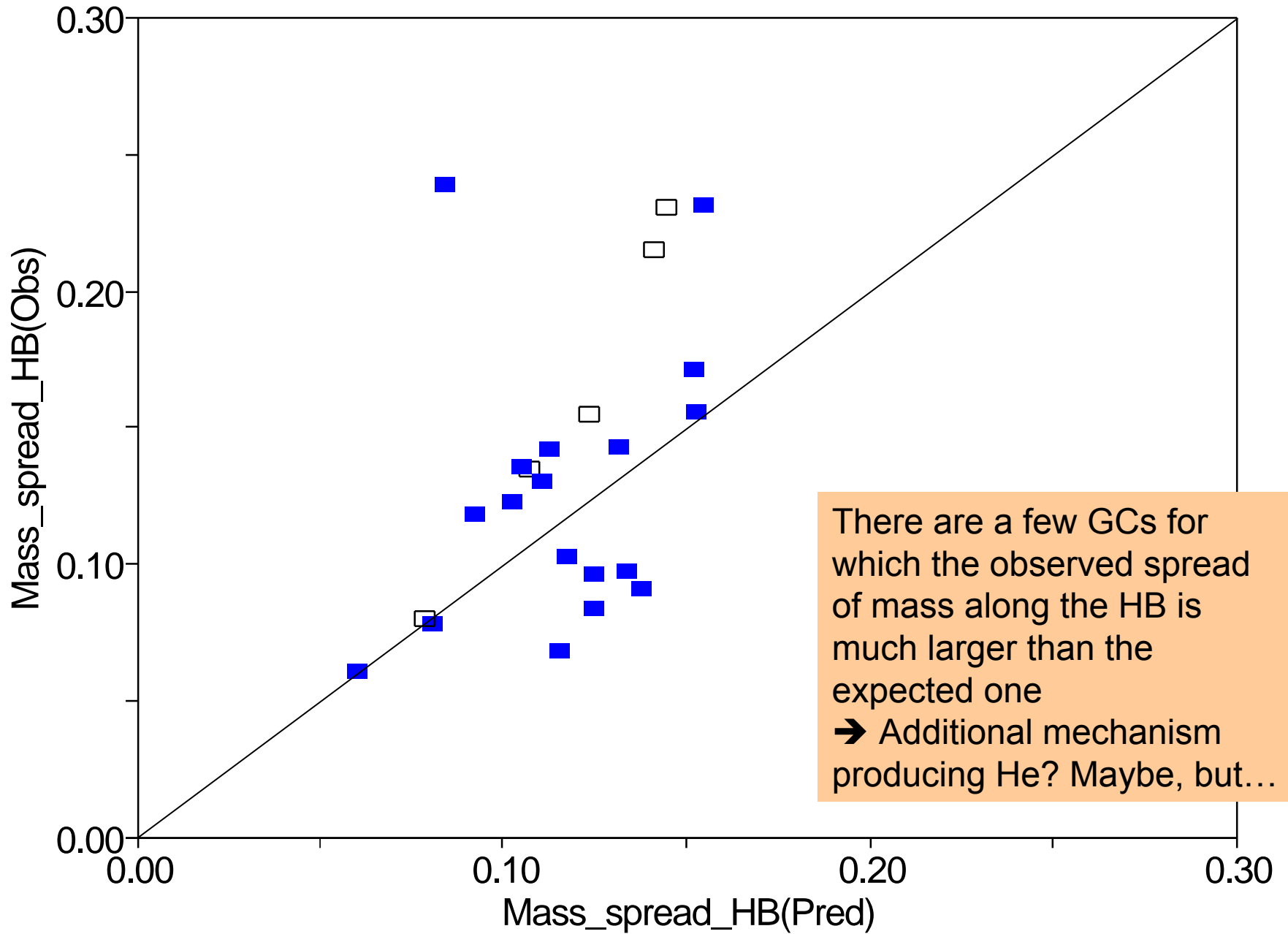
How much He is needed?

$\Delta(m_{F475W} - m_{F814W})$

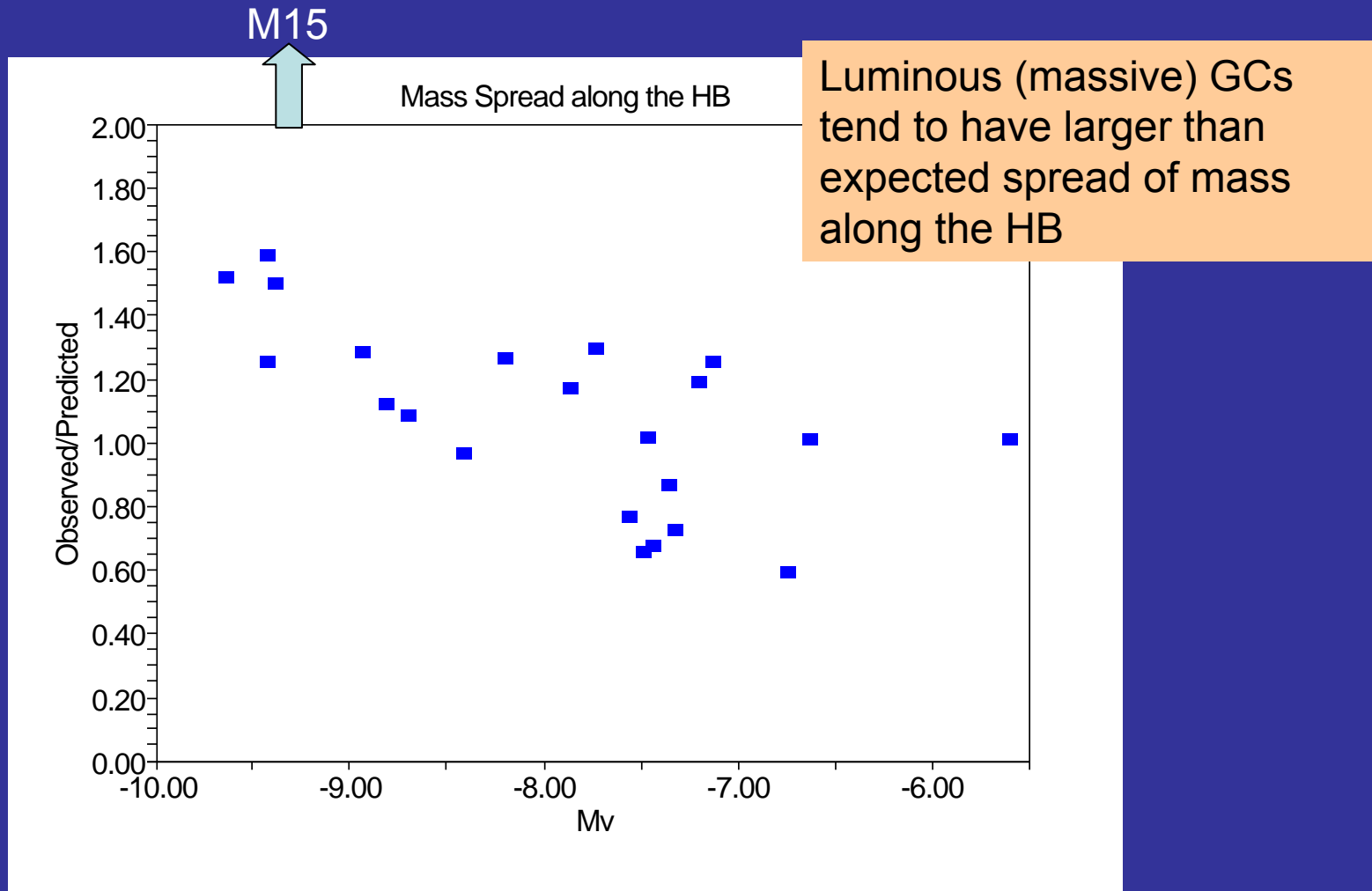


The maximum He value is quite similar in all clusters

This is a problem, because multiple MS's are rare



Correlation with M_V



He production $f(M_V)$

Let us assume that the He production is not constant, but rather depends on M_V :

$$x = -0.034 - 0.14 M_V$$

Or:

$$\Delta Y = (-0.034 - 0.14 M_V) \text{ Dil}$$

Does a variable Y at a given dilution have a reasonable explanation?

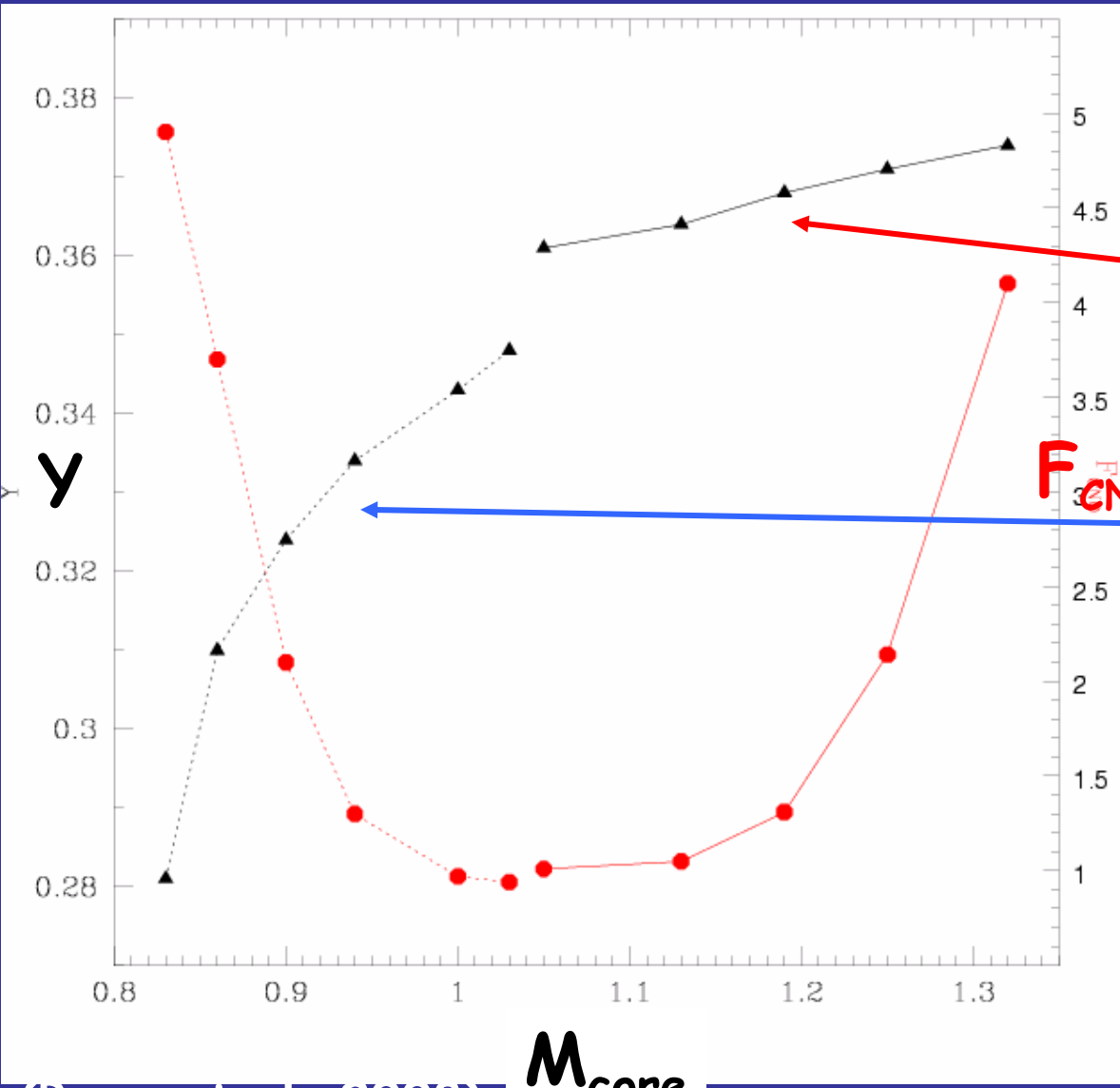
- Maximum depletion of O corresponds to the CNO burning equilibrium abundances
- Maximum production of Na corresponds to complete transformations of ^{22}Ne into ^{23}Na
- These are saturation values!
- Hence different polluters may produce different He while producing the same Na and destroying the same O

Does a variable Y at a given dilution have a reasonable explanation?

- Let us then assume that the amount of He produced is a function of the mass of the polluters
- For instance, suppose that more massive stars produce more He (super-massive AGB stars: see Pumo et al. 2008; Renzini 2008)



Helium yields from super-AGBs can!



(Pumo et al. 2008)

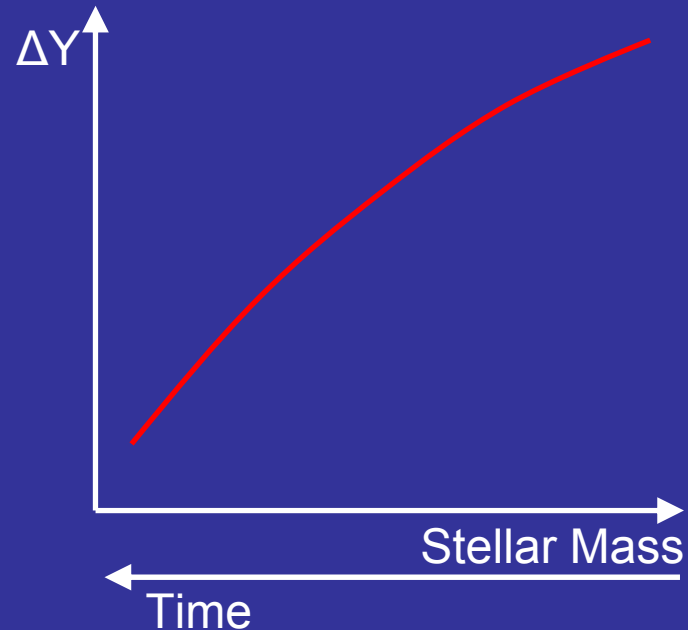
superAGB models (Siess 2007) at 2nd dredge up

AGB $M < 6.3 M_{\text{sun}}$ (VD 2007)



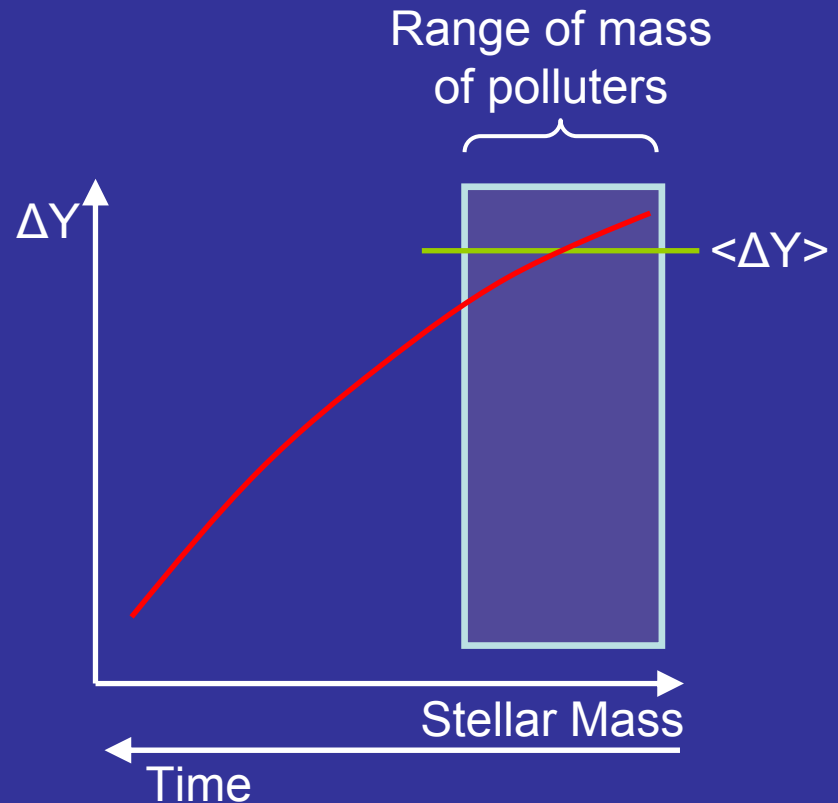
superAGBs reach the Y values needed to fit the blue MS in ω Cen and NGC 2808

- In this case the first polluting stars produce a lot of He (see also Renzini 2008)
- Let us also assume that the material lost by these stars does not form 2nd generation stars immediately, but rather goes into a pool from which 2nd generation stars form
- This is needed in order to have individual populations with different He (e.g. the case of NGC2808 and ω Cen; see Renzini 2008 and D'Ercole et al. 2008)



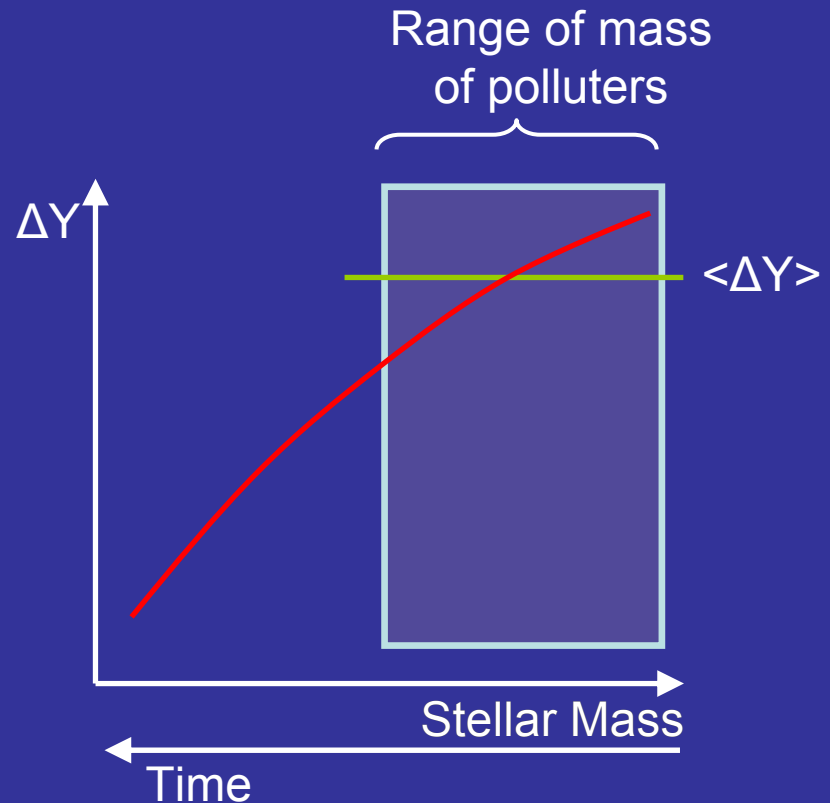
With time, the average Y of the pool decreases

- This pool will be initially very He-rich, but later its He content decreases, because the weight of the most massive stars progressively decreases



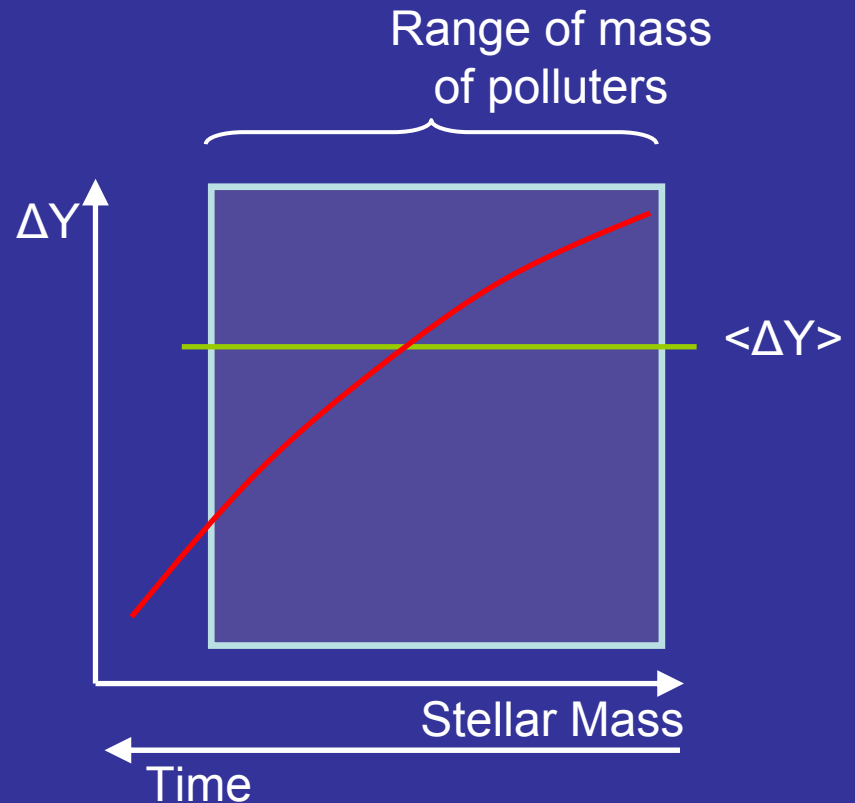
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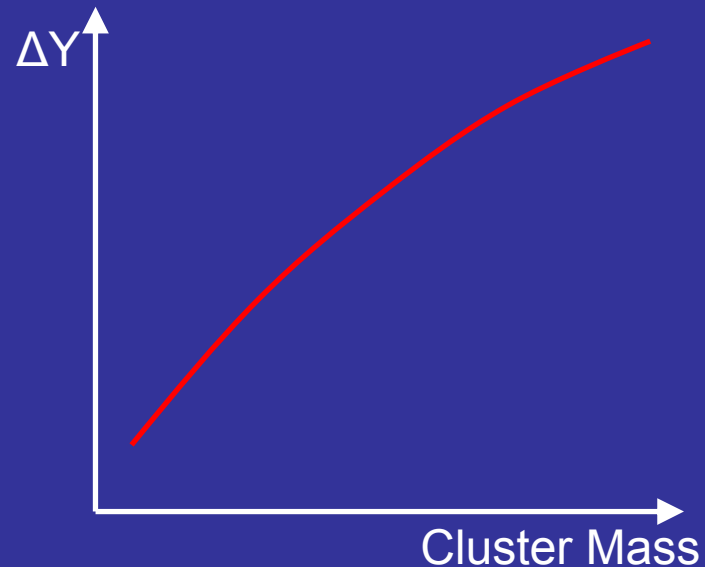
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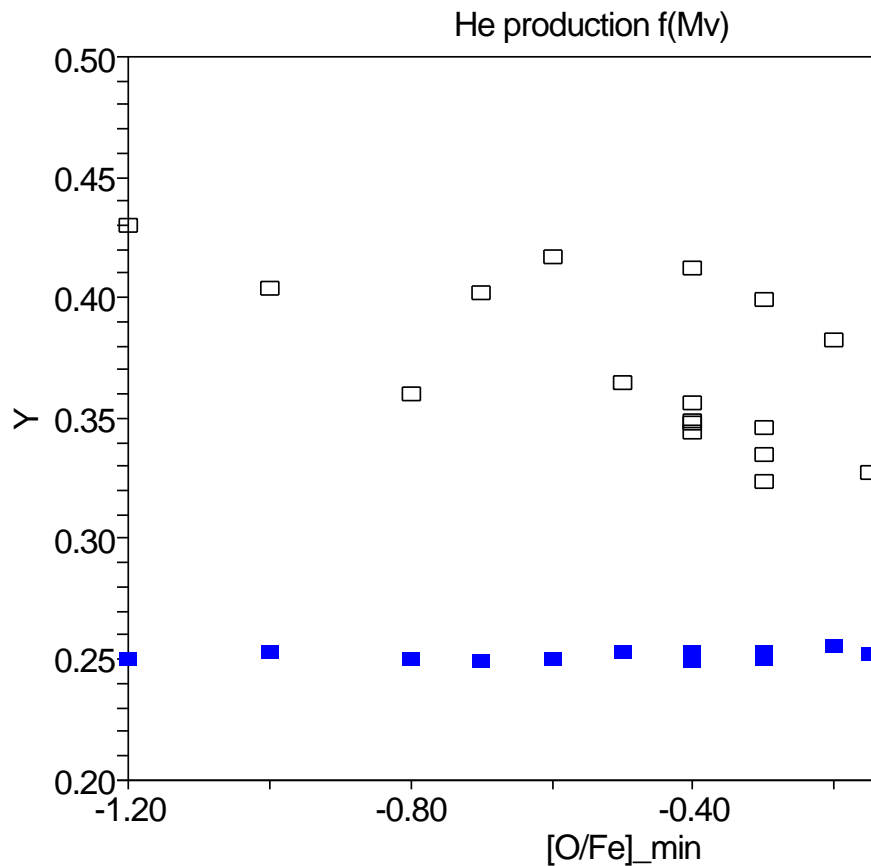
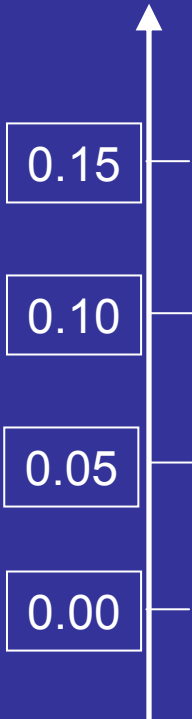
Dependence of He production on cluster mass

- It is reasonable to expect that formation of 2nd gen. stars only starts when a threshold mass is reached, and stops when first 2nd gen. SNe explode (see Renzini 2008)
- The whole process is then expected to be faster in more massive GCs
- In these clusters only the most massive stars contribute, while in less massive GCs less massive stars also participate
- In this way we may generate a dependence of x on cluster mass



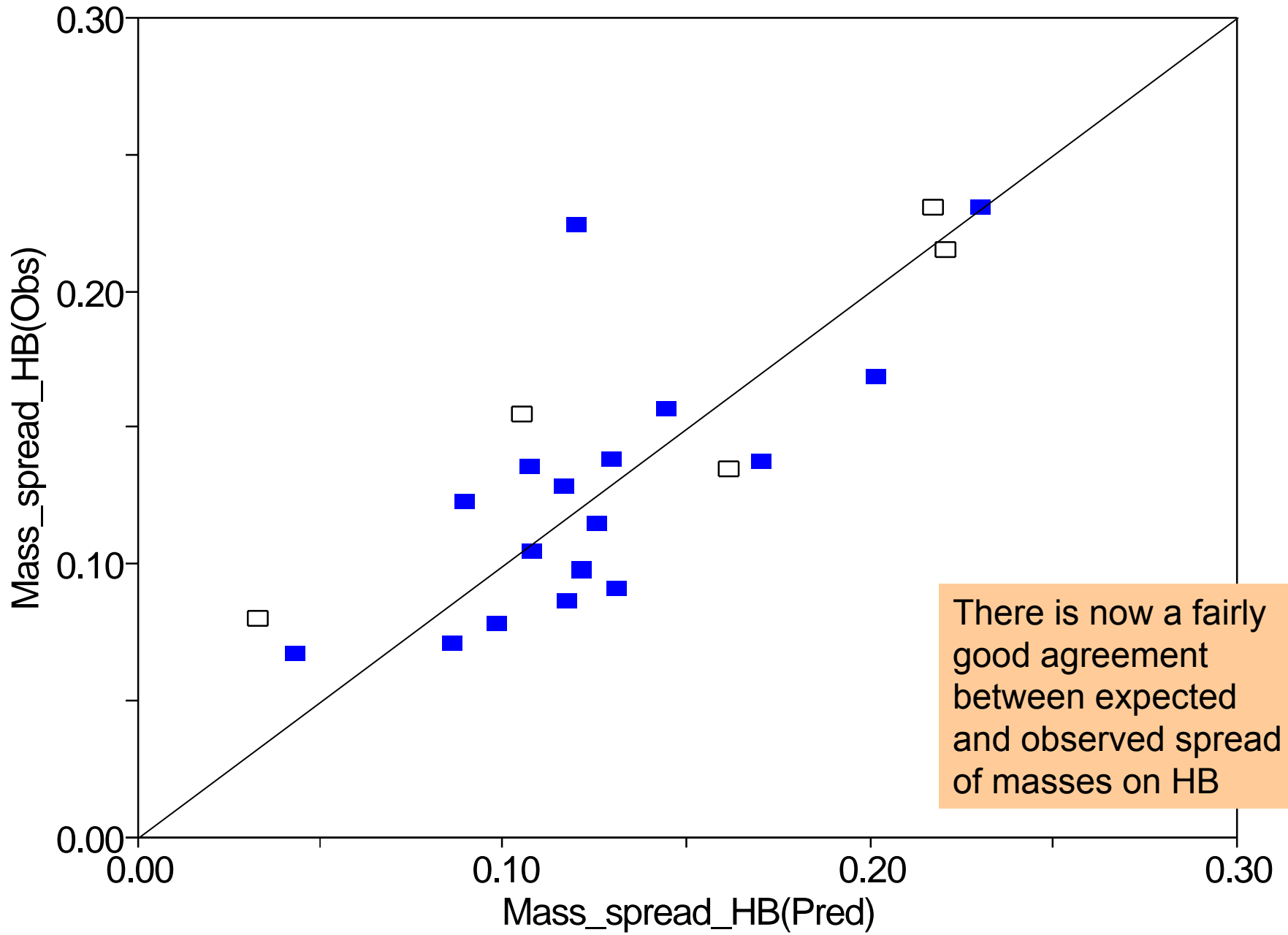
He production $f(M_V)$

$\Delta(m_{F475W} - m_{F814W})$

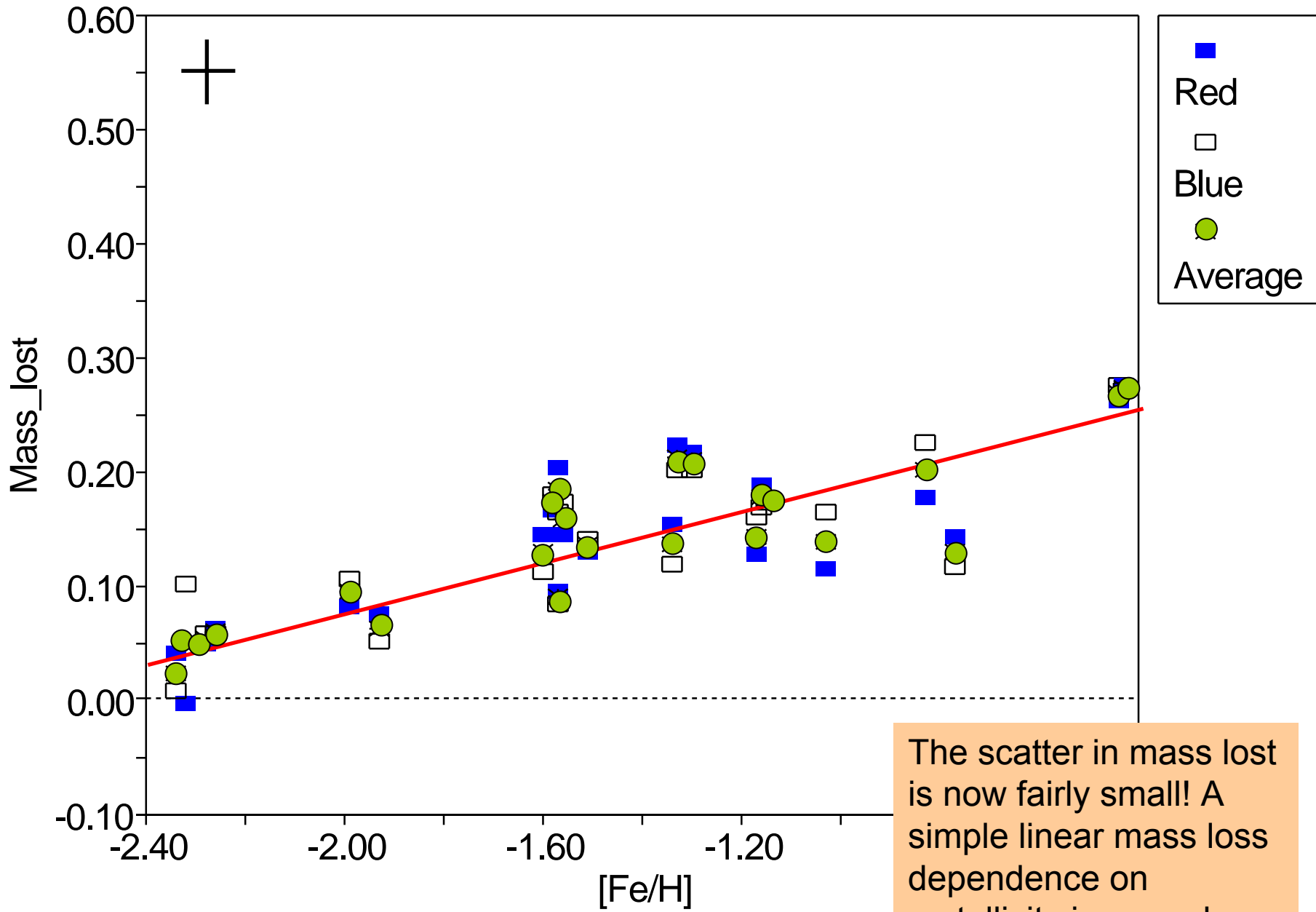


Maximum He is now quite different in different clusters

The values of Y in this diagram seems too large! To be repeated with a more accurate approach

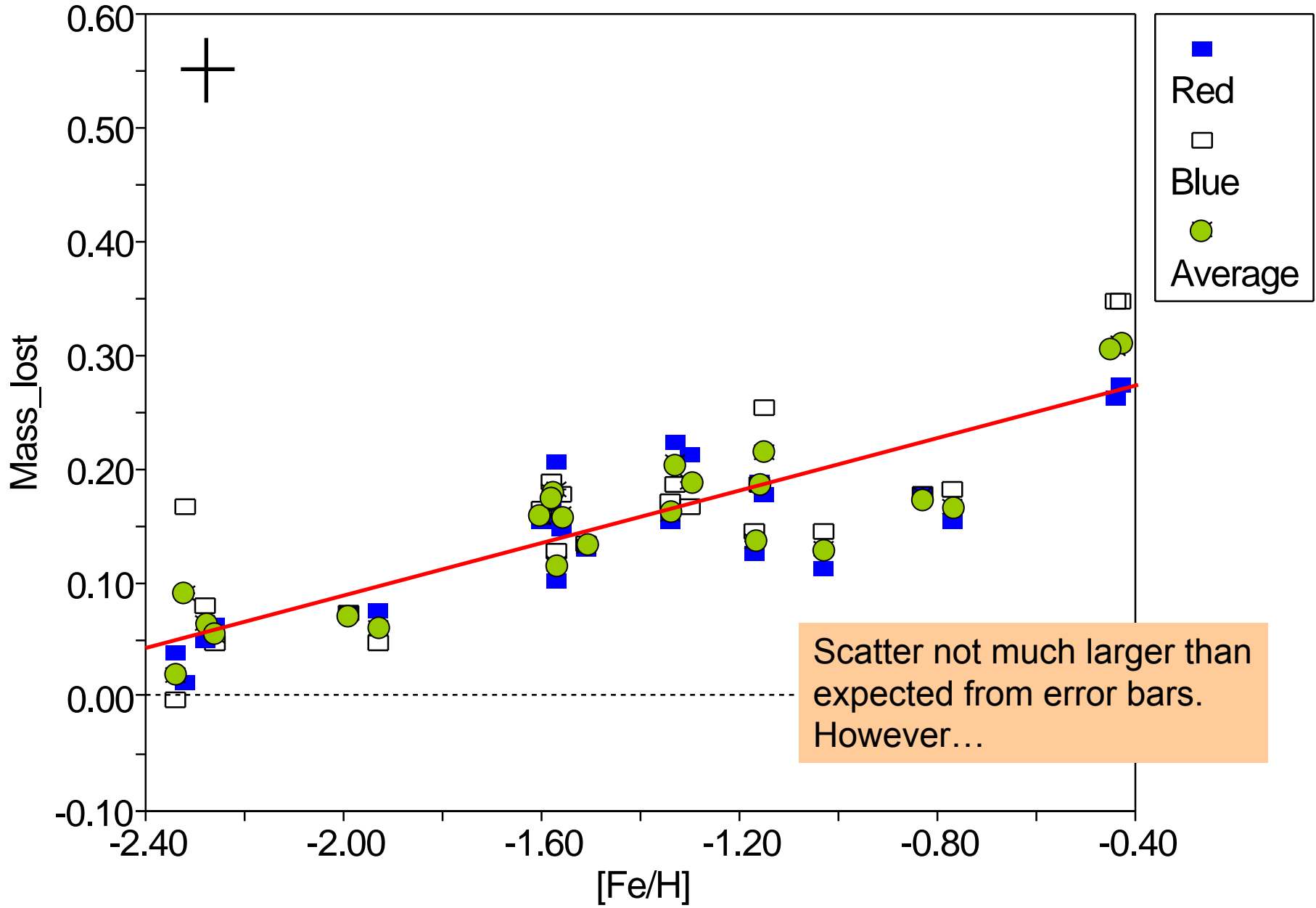


WITH HE-PRODUCTION

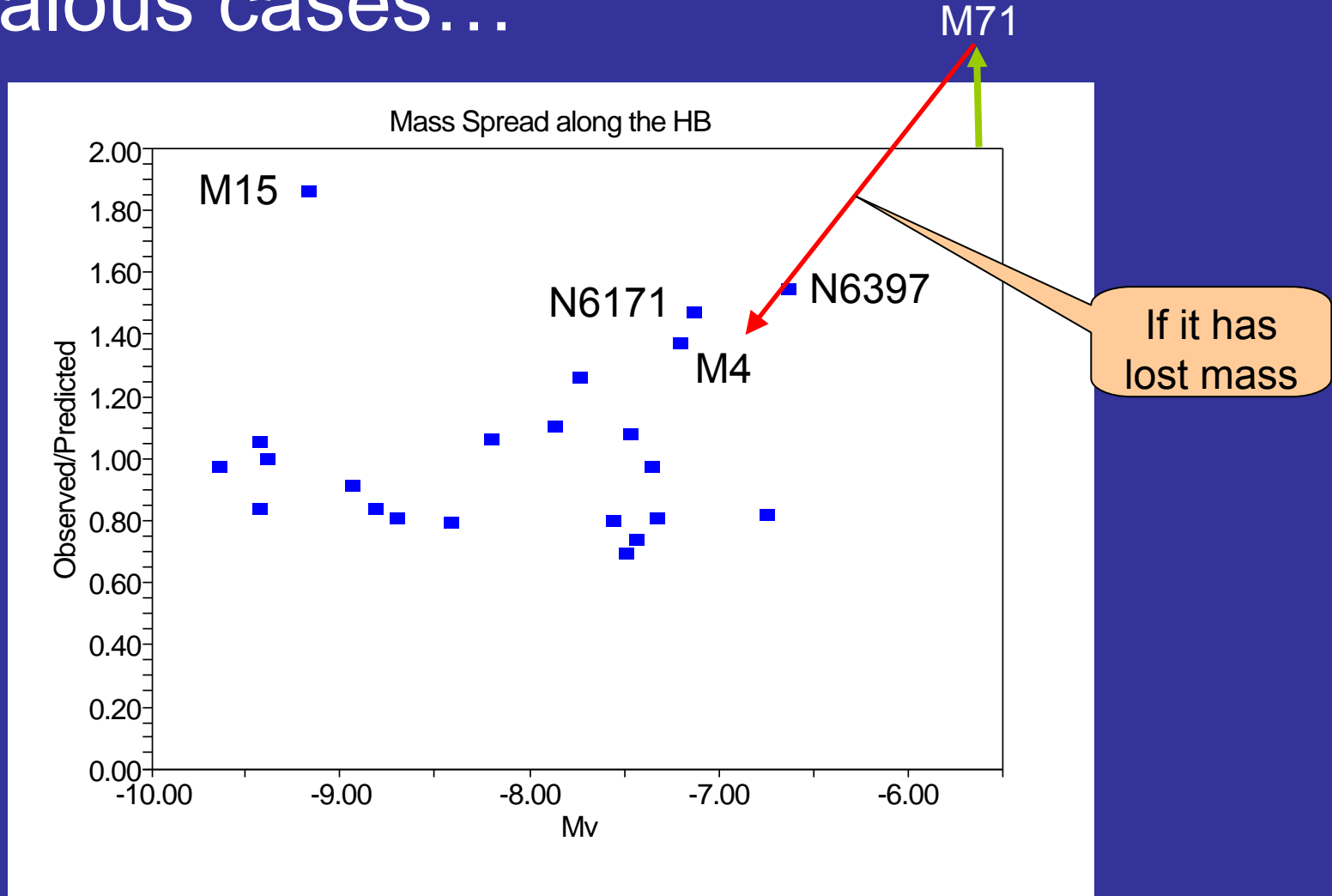


The scatter in mass lost is now fairly small! A simple linear mass loss dependence on metallicity is enough

WITH HE-PRODUCTION



Anomalous cases...



... might have an explanation

Conclusions

- Age is a second parameter, but it is not enough to justify HB morphologies
- Self pollution in globular clusters is most likely responsible for a large variety of the second parameter features
- Self pollution may be in part described using the O-Na anticorrelation, but modulation according to cluster luminosity is required

Many points remain to be done

- First and most important, what are the polluters?
 - Progresses in modeling AGB stars
 - Observations of young objects
 - Very young clusters (RSGC1 and RSGC2)
 - Intermediate age clusters in the LMC
 - Abundances of other elements
- A number of confirmation of this scenario are required
 - Direct determinations of He, Na and O in HB stars
 - The case of NGC 6752
 - New observations in both NGC6752 and M4
 - Do variables properties agree with expectations?
 - Are multiple sequences observed where they are expected?
 - Are anticorrelations found where expected (M54 and NGC1851)?
- Scenario refinements
 - Analytic dependences adopted throughout this discussion should be reviewed; updated age determinations should be used
 - Comparison of integrated mass lost along the RGB with mass loss laws (e.g. Reimers)
 - What is the lower mass limit for this scenario (NGC6791)
- Hydro-dynamical models