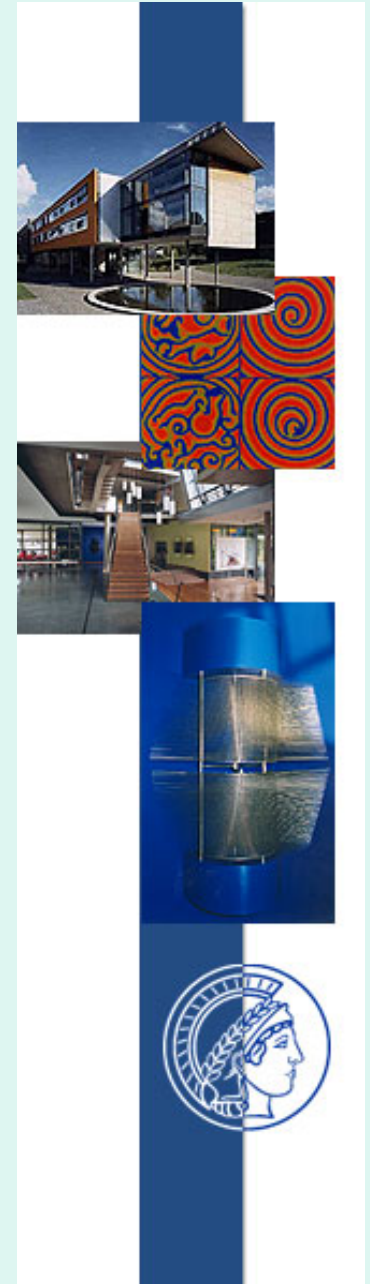


COFUS08 workshop

- Competing orders, Pairing Fluctuations, and Spin Orbit Effects in Novel Unconventional Superconductors
- 30 June -July 11 2008, MPI PKS, Dresden
- Organizers: JF Annett, D. Morr and I. Eremin





University of
BRISTOL

Spin Orbit Effects and Pairing Symmetry in Sr_2RuO_4

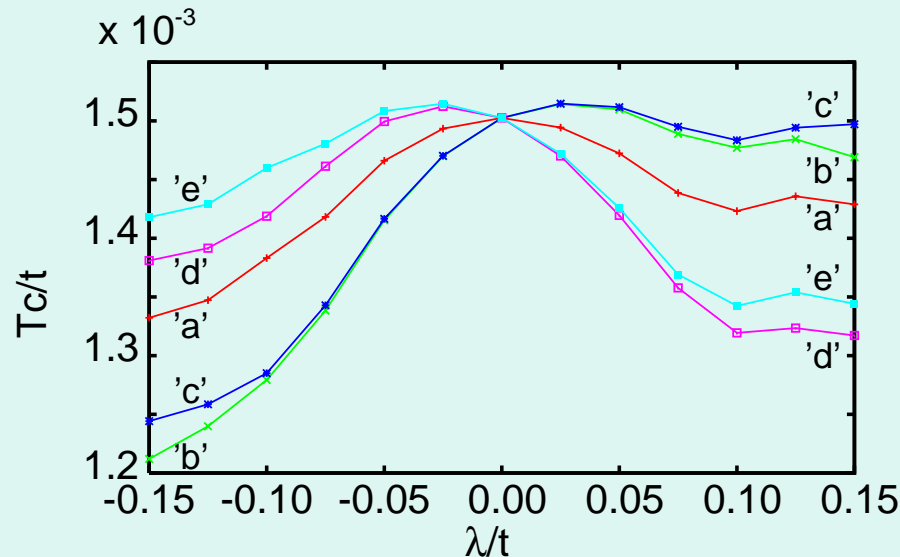
James Annett and
Balazs Gyorffy (Bristol)
Karol Wysokinski and
Grzegorz Litak(Lublin)



PRB 2006, Physica C 2007, + unpublished

We find a surprising result!

T_c as a function of spin-orbit parameter λ



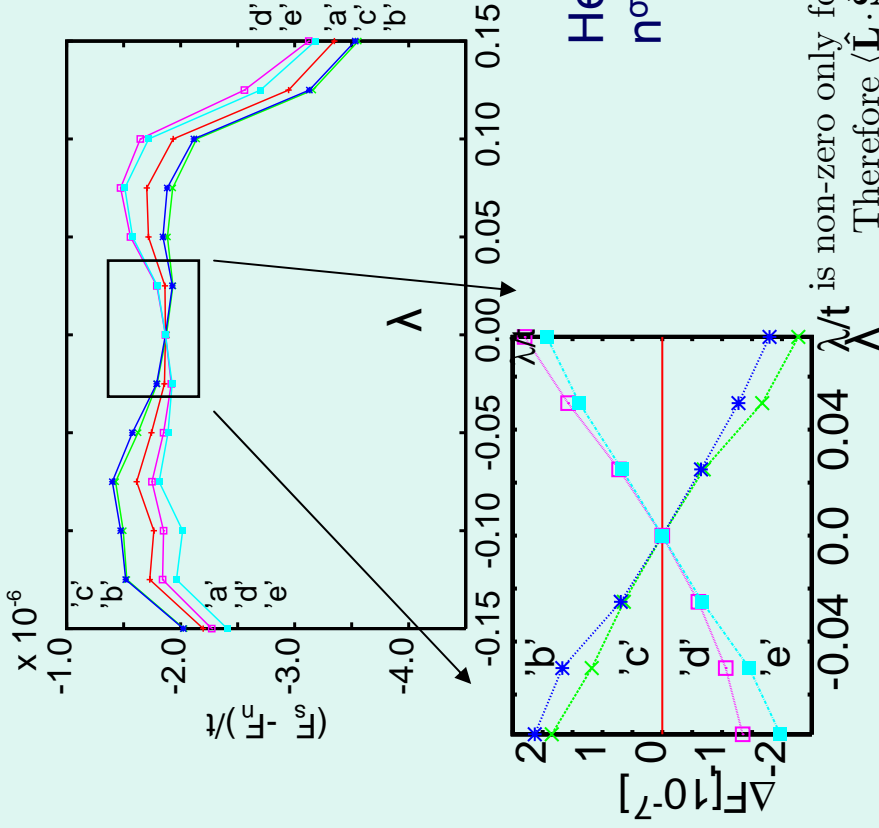
For $\lambda > 0$ b and c are most stable
For $\lambda < 0$ e and d are most stable

- (a) $\underline{\mathbf{d}}_{\mathbf{k}} \sim (0, 0, X + iY)$
- (b) $\underline{\mathbf{d}}_{\mathbf{k}} \sim (X, Y, 0)$
- (c) $\underline{\mathbf{d}}_{\mathbf{k}} \sim (Y, -X, 0)$
- (d) $\underline{\mathbf{d}}_{\mathbf{k}} \sim (X, -Y, 0)$
- (e) $\underline{\mathbf{d}}_{\mathbf{k}} \sim (Y, X, 0)$

$X(\mathbf{k}), Y(\mathbf{k})$ are basis functions in the 1st BZ transforming as k_x, k_y

Surprisingly the expected chiral (a) state is NEVER stable!

Simple perturbation theory in λ



$$\begin{aligned} \delta F &= \frac{\lambda}{2} \langle \hat{\mathbf{L}} \cdot \hat{\mathbf{S}} \rangle = \frac{\lambda}{2} \sum_{m,m'} \langle m | \hat{L}_z | m' \rangle n_{mm'}^{\uparrow\uparrow} \\ &\quad + \frac{\lambda}{2} \sum_{m,m'} \langle m | \hat{L}_x - i \hat{L}_y | m' \rangle n_{mm'}^{\uparrow\downarrow} \\ &\quad + \frac{\lambda}{2} \sum_{m,m'} \langle m | \hat{L}_x + i \hat{L}_y | m' \rangle n_{mm'}^{\downarrow\uparrow} \\ &\quad - \frac{\lambda}{2} \sum_{m,m'} \langle m | \hat{L}_z | m' \rangle n_{mm'}^{\downarrow\downarrow}, \end{aligned}$$

Here $|m\rangle = |d\ xz\rangle, |d\ yz\rangle, |d\ xy\rangle, |p\ ip\ BCS\rangle$
 $n_{mm'}^{\sigma\sigma'} = \langle c^+_{m\sigma} c_{m'\sigma'} \rangle$ relative to $|p+ip\ BCS\rangle$

$$\langle \hat{L}_z \rangle = n_{ab}^{\uparrow\uparrow} + n_{ab}^{\downarrow\downarrow} - (n_{ba}^{\uparrow\uparrow} + n_{ba}^{\downarrow\downarrow}),$$

is non-zero only for the chiral state.

Therefore $\langle \hat{\mathbf{L}} \cdot \hat{\mathbf{S}} \rangle$ is non-zero for four states (b)-(e) which have $\langle \hat{\mathbf{S}} \rangle = \langle \hat{\mathbf{L}} \rangle = 0$ while the (a) state has $\langle \hat{\mathbf{L}} \cdot \hat{\mathbf{S}} \rangle = 0, \langle \hat{L}_z \rangle \neq 0$.

Spin-dependent pairing interaction?

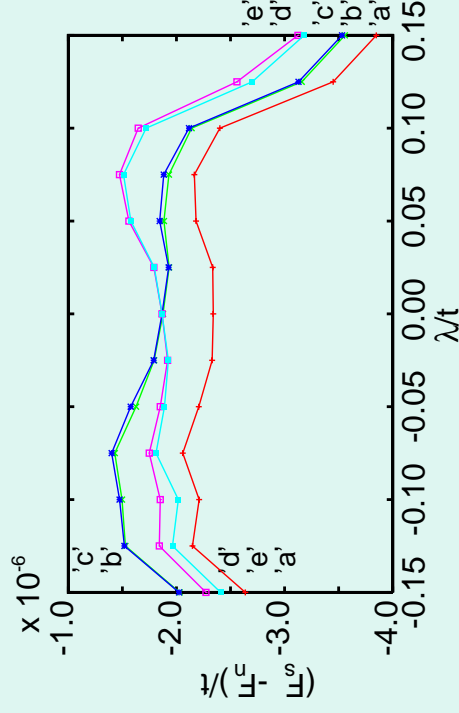
The chiral spin orientation of the Cooper pair must arise from another mechanism: such as **spin-dependent pairing interactions**.

We implicitly assumed $U_{mm'}^{\uparrow\uparrow}(ij) = U_{mm'}^{\downarrow\downarrow}(ij)$.

But in general: $U_{mm'}^{\uparrow\uparrow}(ij) \neq U_{mm'}^{\downarrow\downarrow}(ij)$,

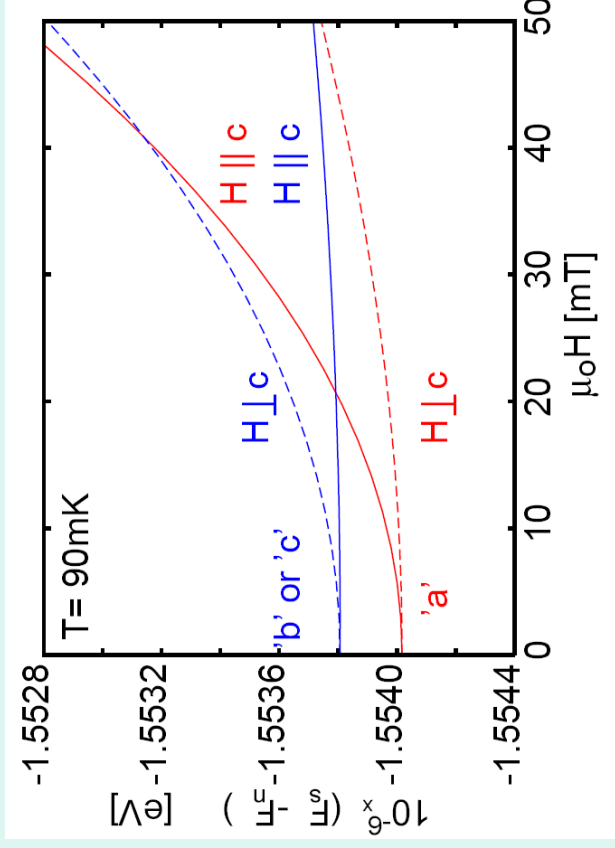
These can be different corresponding to the Fermi liquid parameters for parallel and opposite spin quasi-particles

Chiral state is $\uparrow\downarrow$ pairing only, while the others are $\uparrow\uparrow$ and $\downarrow\downarrow$ only



Effect of a c-axis magnetic field

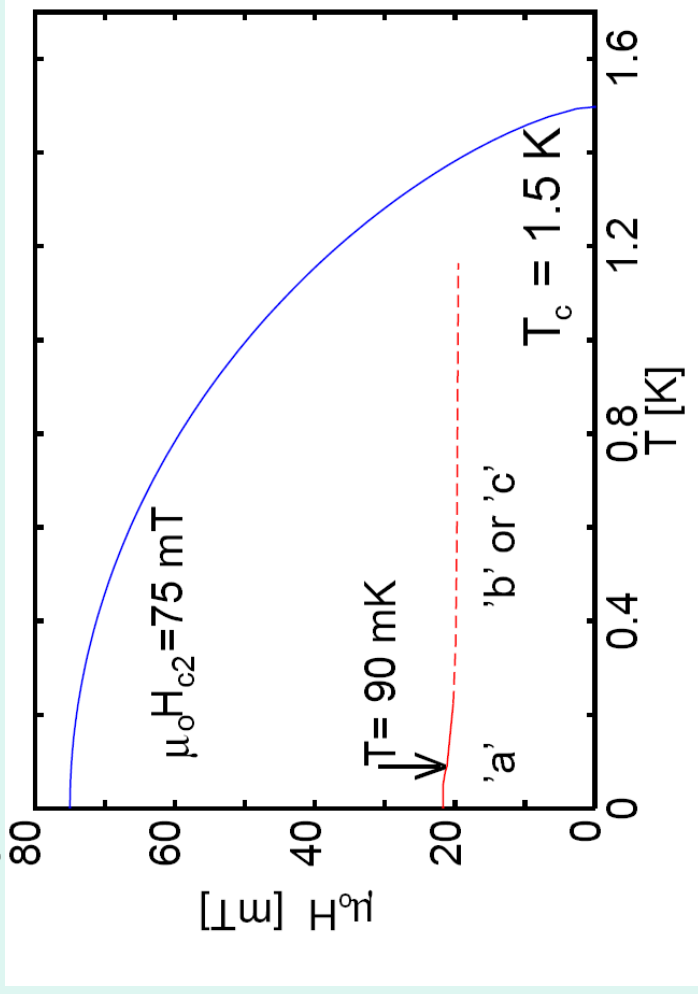
The d-vector cannot simply rotate. It must make a transition from (a) to one of the other phases b-e we saw earlier



This is what we find in our model. For c-axis fields (a) is stable for $H=0$, but there is a finite field transition to another phase, usually (b/c).

The parameters can be chosen to make the transition occur below 400G

Stability of phases in H-T plane



This transition has not been seen, but necessary to reconcile the Murukawa experiments with chiral pairing
-- 1st order but entropy change is tiny since $|d|^2$ identical in all phases

Location of boundary depends on combination of λ and U'/U

Size of the spin orbit term?

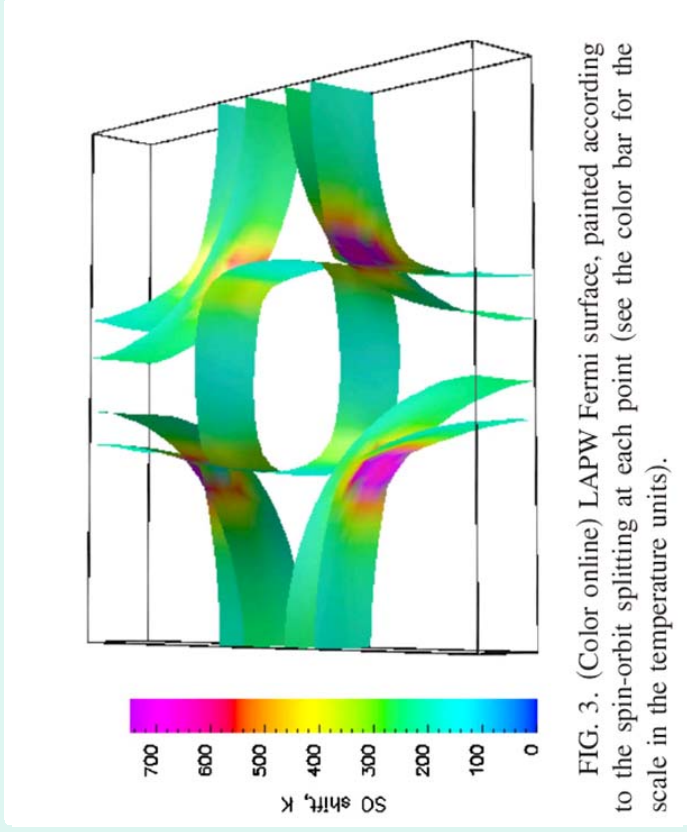
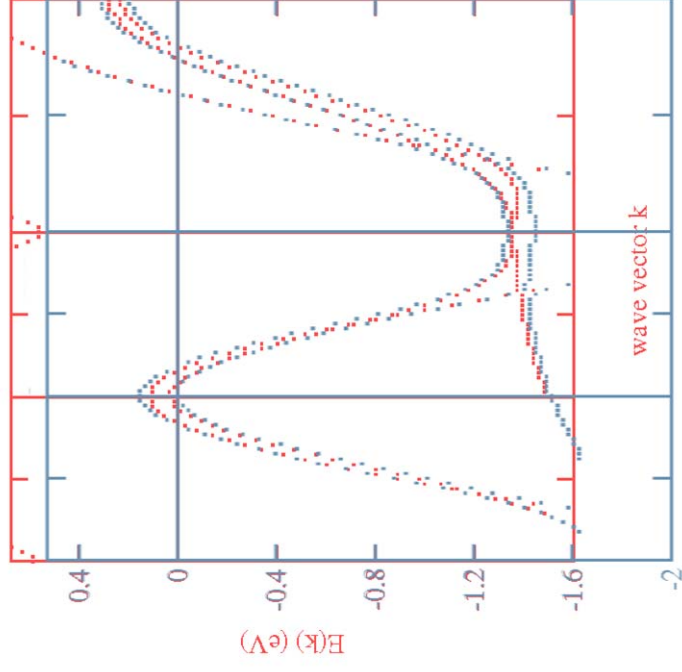


FIG. 3. (Color online) LAPW Fermi surface, painted according to the spin-orbit splitting at each point (see the color bar for the scale in the temperature units).

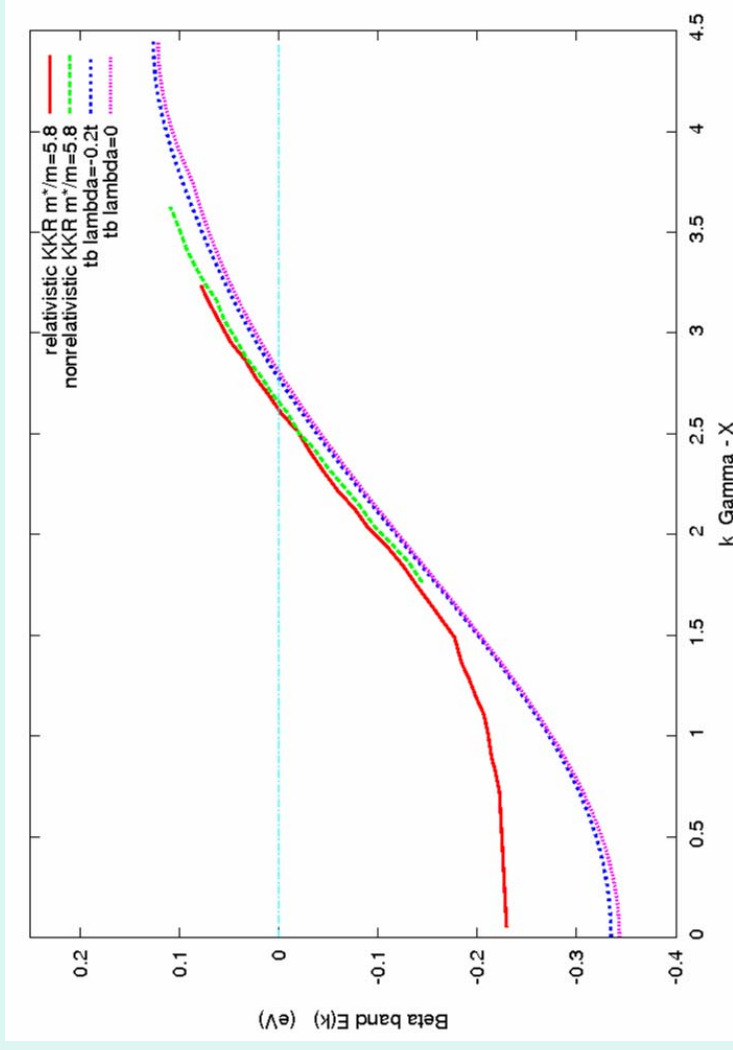
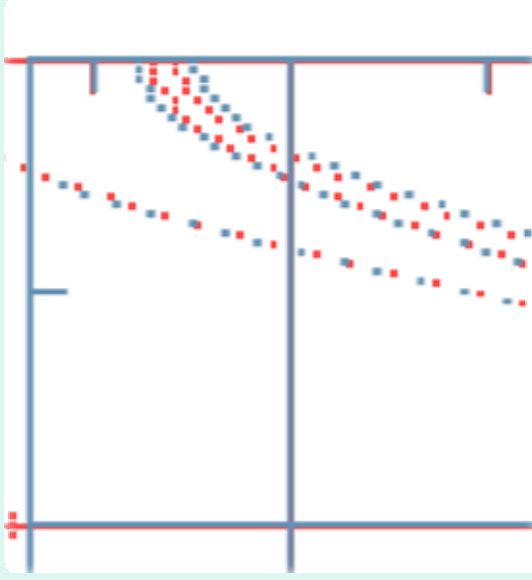
SPR-KKR-ASA calculation for Sr₂RuO₄
dispersion relation of Sr₂RuO₄



Mazin PRB2006, LAPW
bands coloured by relativistic
shift

Our KKR bands,
Blue $c=1x$ (fully relativistic)
Red $c=100x$ (non-relativistic)

Strength of spin-orbit term?



KKR-bands close up near (π, π)

Blue $c=1x$

Red $c=100x$

Our tight-binding β sheet
band from de Haas data,
with $\lambda=0$ or $-0.2t$ compared to
relativistic KKR bands (scaled
by $m^*/m \approx 5$)

Pairing in tetragonal symmetry: (JF Annett, Adv Phys 1990)

TABLE I: Irreducible representations of even and odd parity in a tetragonal crystal. The symbols X , Y , Z represent any functions transforming as x , y and z under crystal point group operations, while I represents any function which is invariant under all point group symmetries.

Rep.	symmetry	Rep.	symmetry
A_{1g}	I	A_{1u}	$XYZ(X^2 - Y^2)$
A_{2g}	$XY(X^2 - Y^2)$	A_{2u}	Z
B_{1g}	$X^2 - Y^2$	B_{1u}	XYZ
B_{2g}	XY	B_{2u}	$Z(X^2 - Y^2)$
E_g	$\{XZ, YZ\}$	E_u	$\{X, Y\}$

TABLE III: Basis functions $\gamma_i^T(\mathbf{k})$ for the odd parity irreducible representations of body-centred tetragonal crystals.

Rep.	in-plane	inter-plane
A_{1u}	-	-
A_{2u}	-	$\cos \frac{k_x}{2} \cos \frac{k_y}{2} \sin \frac{k_z}{2}$
B_{1u}	-	$\sin \frac{k_x}{2} \sin \frac{k_y}{2} \sin \frac{k_z}{2}$
B_{2u}	-	-
E_u	$\sin k_x$ $\sin k_y$	$\sin \frac{k_x}{2} \cos \frac{k_y}{2} \cos \frac{k_z}{2}$ $\cos \frac{k_x}{2} \sin \frac{k_y}{2} \cos \frac{k_z}{2}$

a

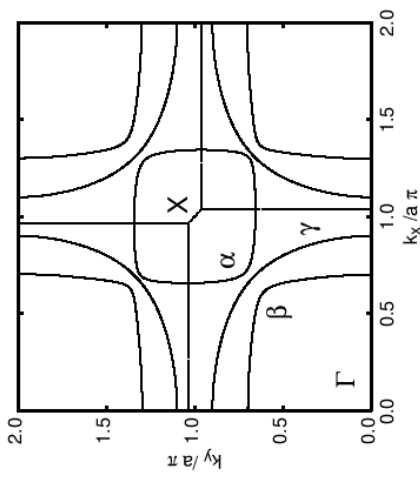
Here $X(\mathbf{k})$, $Y(\mathbf{k})$ and $Z(\mathbf{k})$ are any basis functions in the 1st BZ transforming as x, y, z under point group operations (analogues of cubic harmonics)

Note: even within the E_u ‘p-wave’ symmetry class there are basis functions with or without line nodes

Simple effective Hamiltonian model

$$\hat{H} = \sum_{ijmm',\sigma} ((\varepsilon_m - \mu)\delta_{ij}\delta_{mm'} - t_{mm'}(ij)) \hat{c}_{im\sigma}^+ \hat{c}_{jm'} - \frac{1}{2} \sum_{ijmm'} U_{\alpha\beta,\gamma\delta} \hat{c}_{im\alpha}^+ \hat{c}_{jm'\beta}^+ \hat{c}_{jm'\gamma} \hat{c}_{im\delta},$$

$$H^{SO} = i\frac{\lambda}{2} \sum_{i,\sigma\sigma'} \sum_{mm'} \varepsilon_{\kappa mm'} \sigma_{\sigma\sigma'}^{\kappa} \hat{c}_{im\sigma}^+ \hat{c}_{im'\sigma'}$$



**An effective 3 band Hamiltonian is constructed
Parameters fit to the 3d experimental Fermi surface**

**Hubbard interaction parameters U introduce attractive
Interactions between different sites (ij) and orbitals (mm')**