



## Peptide Self-Assembled Polymers

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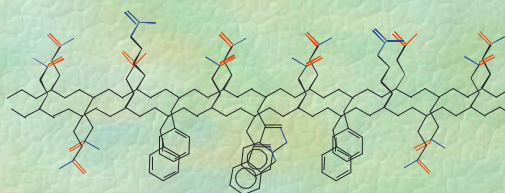
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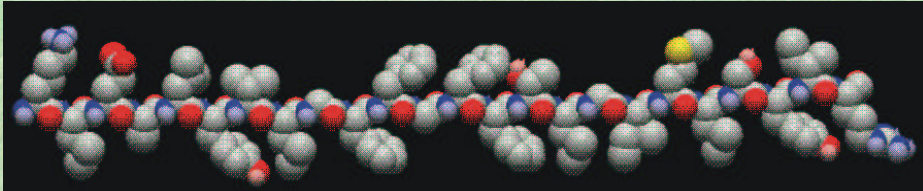
## Questions



- Why and when do peptides self-assemble?
- What is a good coarse-grained model for the energies of interaction?
- What limits fibre/bundle diameters?
- What are the slow kinetics?
- Do they constitute an example of tightly entangled stiff polymers?
- .....

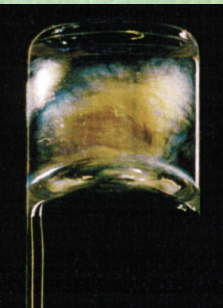
### Peptide 1: K24 - organic solvent

Lys-Leu-Glu-Ala-Leu-Tyr-Val-Leu-Gly-Phe-Phe-Gly-Phe-Phe-Thr-Leu-Gly-Ile-Met-Leu-Ser-Tyr-Ile-Arg  
- +



Hydrophobic

did this at only 1% in water




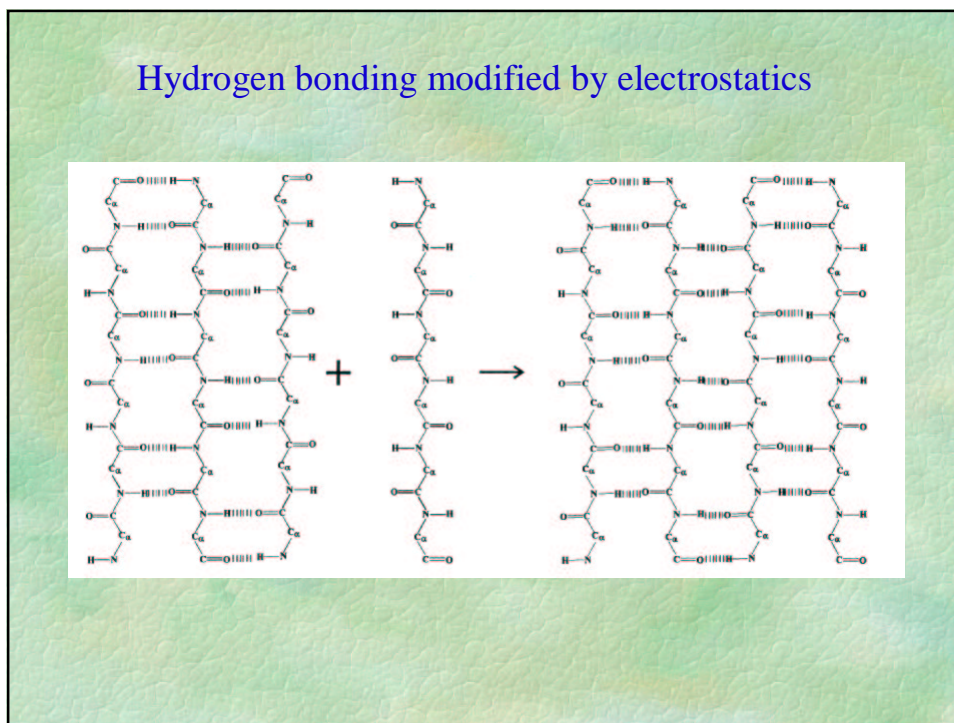
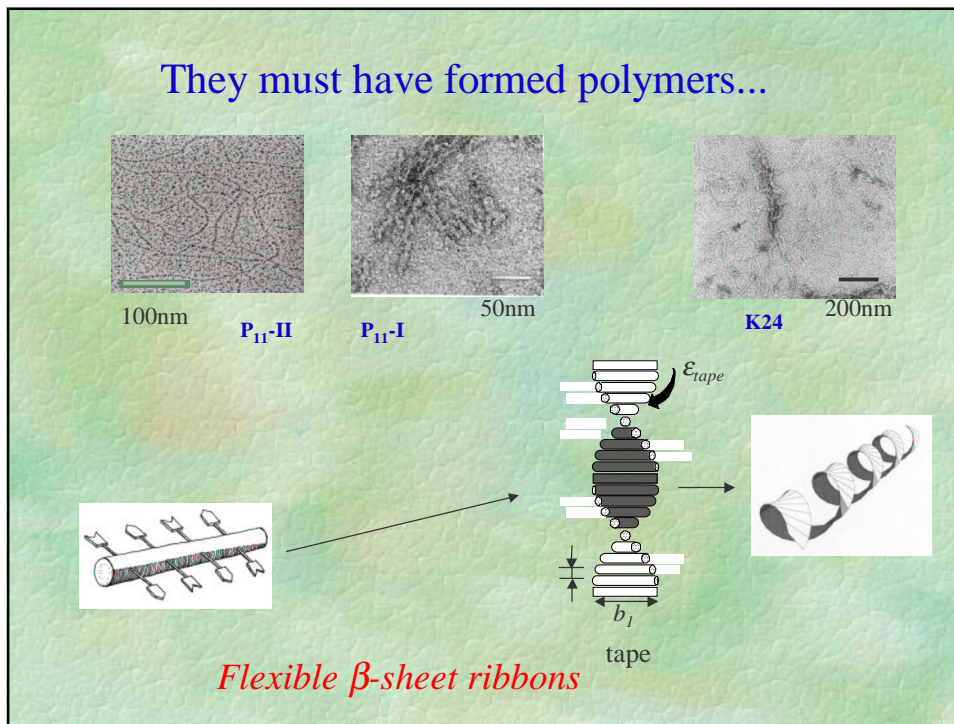
### Peptides 2 and 3: P<sub>11</sub>-I and P<sub>11</sub>-II ; aqueous

I CH<sub>3</sub>CO-Gln-Gln-Arg-Phe-Gln-Trp-Gln-Phe-Glu-Gln-Gln-NH<sub>2</sub>

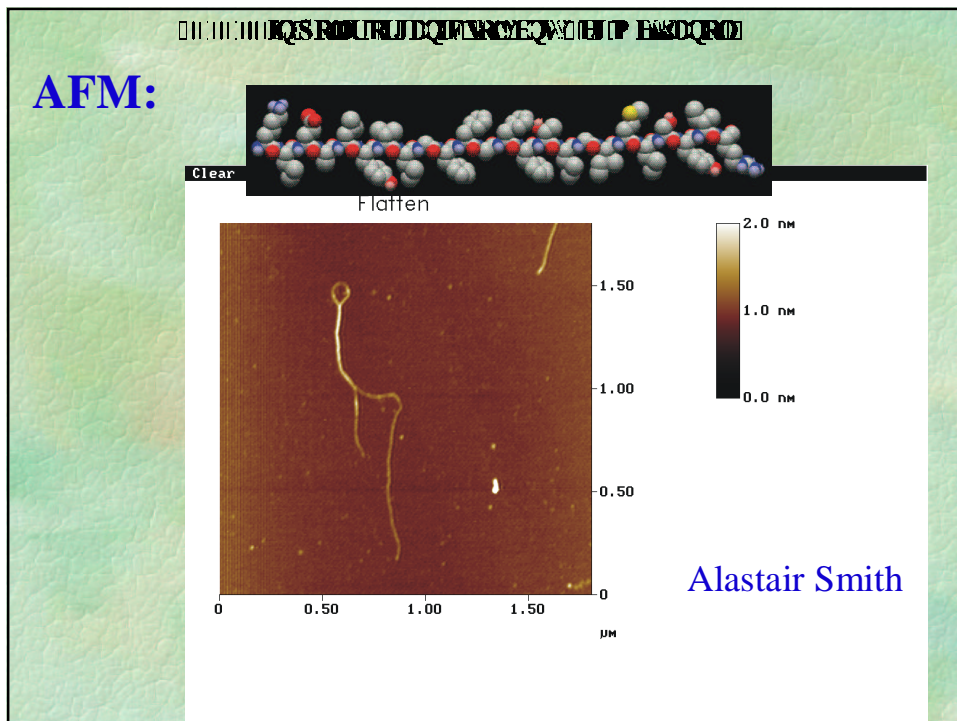
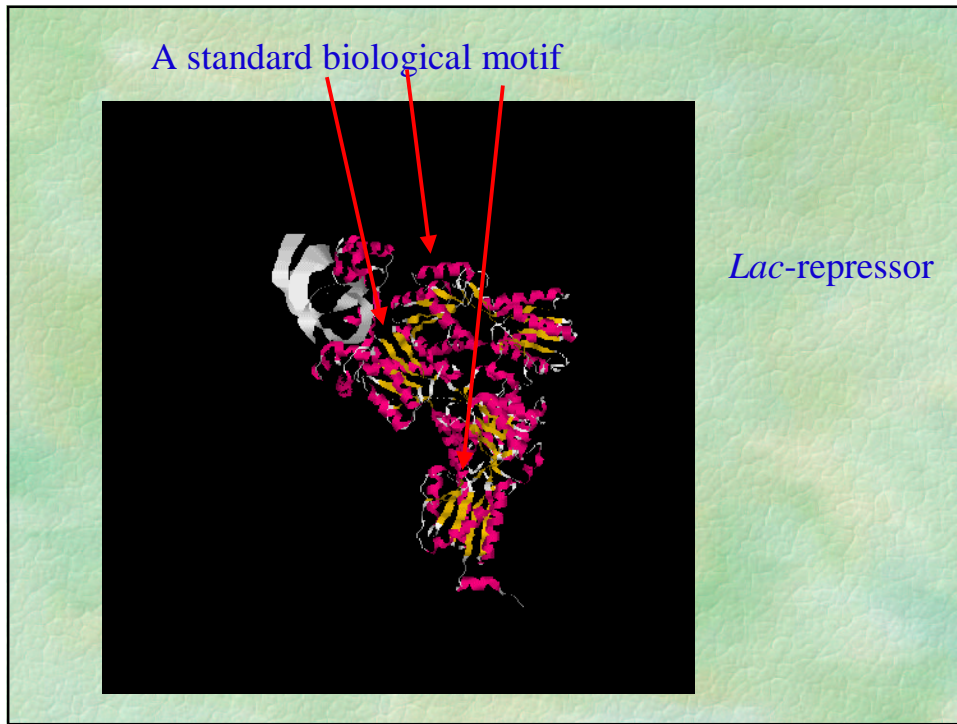
... the same plus a hydrophobic side..

II CH<sub>3</sub>CO-Gln-Gln-Arg-Phe-Gln-Trp-Gln-Phe-Glu-Gln-Gln-NH<sub>2</sub>

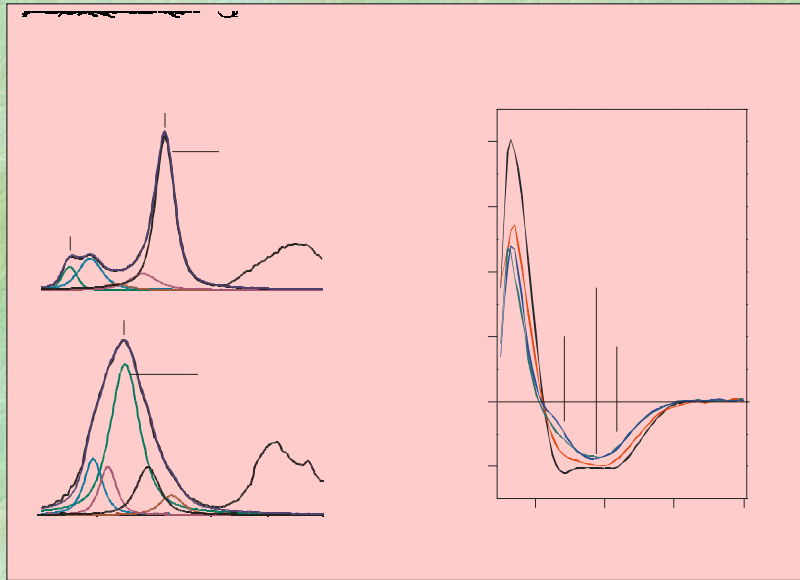




# Self-Assembled Peptide Tapes as Stiff Biopolymers



Check with spectroscopy



Surely an example of 1-d self-assembly:

$$\frac{F}{k_B T} = \sum_m N_m \ln \left( \frac{N_m v_0}{eV} \right) + \sum_m N_m \epsilon_m$$

with  $\sum_m N_m m = N$

So we need a model for

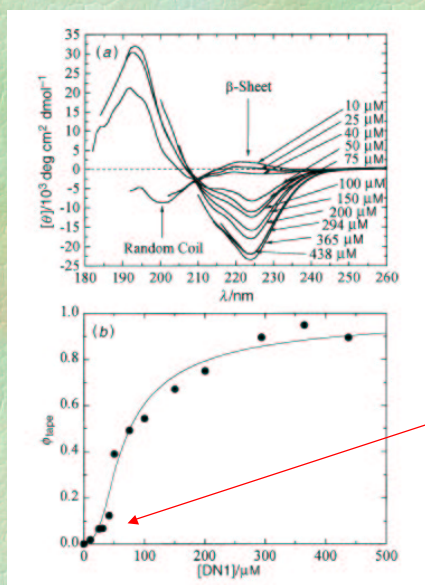
Famous example: wormlike micelles



$$\epsilon_m = 2\epsilon_{cap}$$

$$\Rightarrow \langle m \rangle = c^{1/2} e^{\epsilon_{cap}}$$

But the Spectroscopic self-assembly curves are S-shaped:



*Not  $\sim c^{1/2}$  !*

So modify the picture with a transition state...

*Pseudo-helix free state*

*Flexible  $\beta$ -sheet ribbons*

Now this gives:

$$\langle m_{tape} \rangle = \left( \frac{c - c_{tape}^*}{c_{tape}^*} \right)^{1/2} e^{\epsilon_{trans}/2} \quad \text{with} \quad c_{tape}^* \cong e^{-\epsilon_{tape} + \epsilon_{trans}}$$

With increased concentration they go on self-assembling..

tape

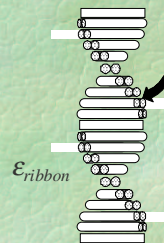
ribbon

fibril

fibre

So that, e.g.

$$\langle m_{\text{ribbon}} \rangle = \left( \frac{c - c_{\text{ribbon}}^*}{c_{\text{ribbon}}^*} \right)^{1/2} e^{(\epsilon_{\text{trans}} + \epsilon_{\text{tape}})/2}$$

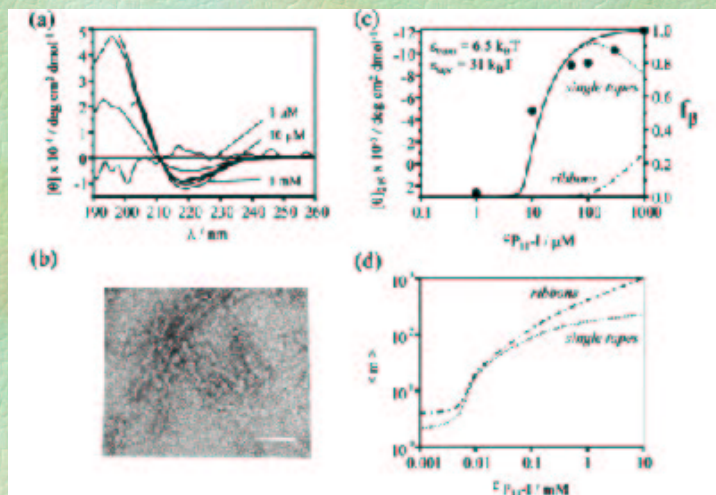


ribbon

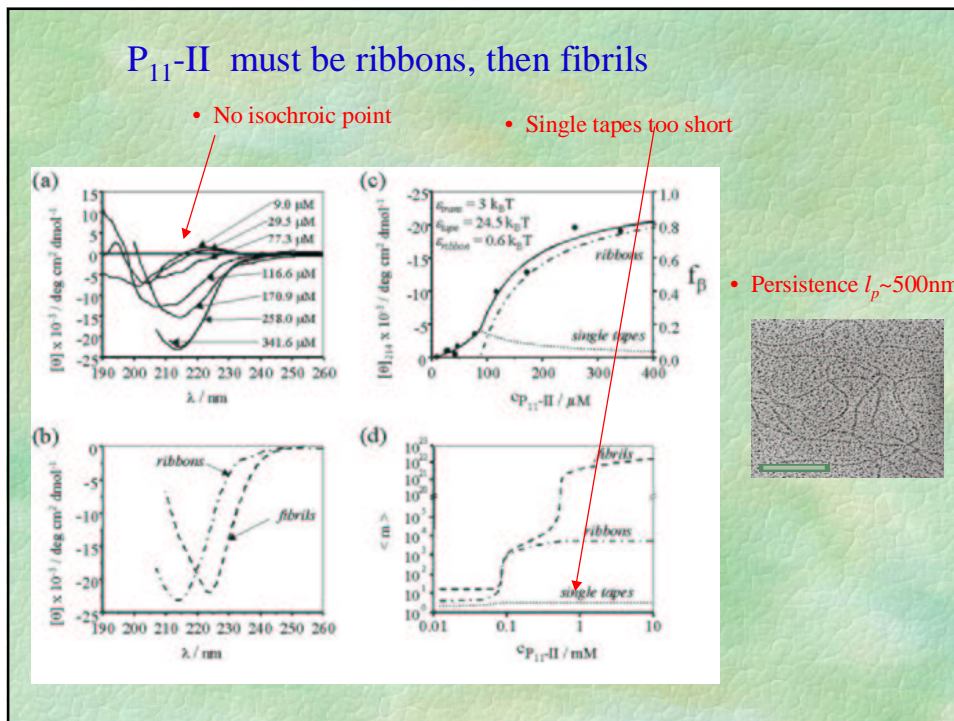
with

$$c_{\text{ribbon}}^* \cong c_{\text{tape}}^* + \epsilon_{\text{ribbon}}^{-2} e^{-\epsilon_{\text{tape}}}$$

P<sub>11</sub>-I looks like curly tapes



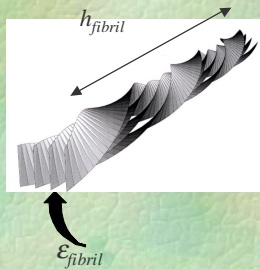




But what stabilises the fibrils?

$$\epsilon_{\text{elast}} = \frac{1}{2} k_{\text{bend}} (v - v_0)^2 + \frac{1}{2} k_{\text{twist}} (\theta - \theta_0)^2$$

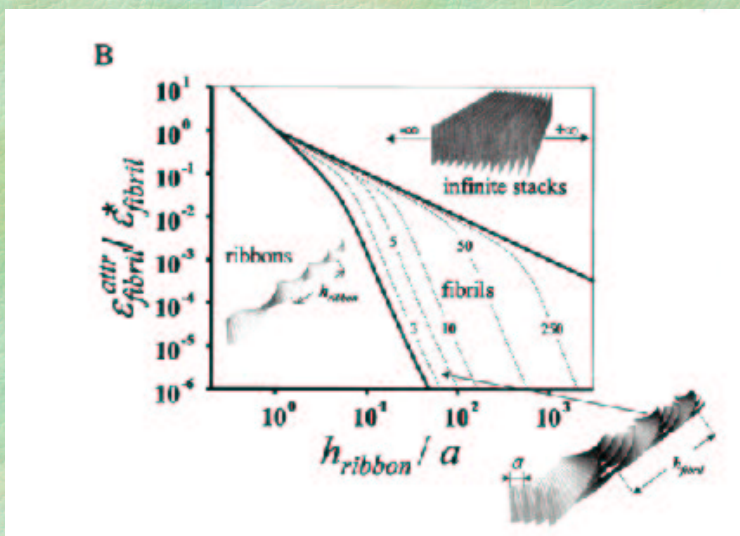
Twist-Stack Model



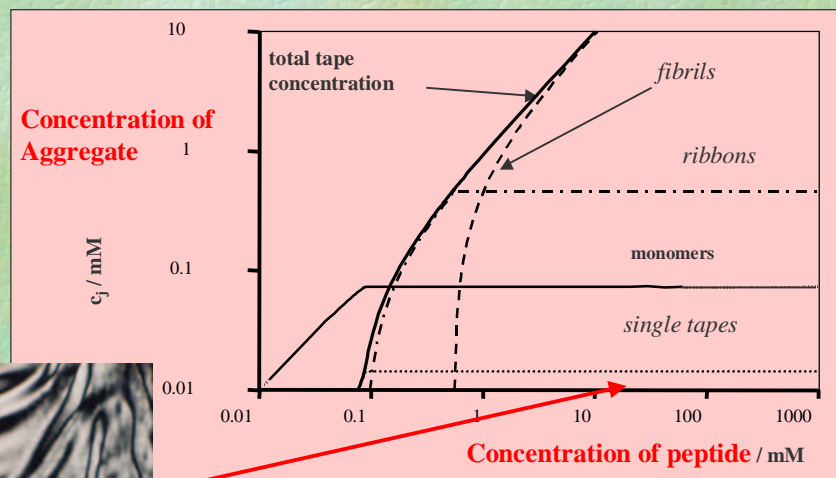
$$v = \gamma^2 \frac{\rho}{(1 + \gamma^2 \rho^2)}; \quad \theta = \gamma \frac{1}{(1 + \gamma^2 \rho^2)}$$

$$\epsilon_{\text{fibril}} = \frac{p-1}{2p} \epsilon_{\text{fibril}}^{\text{attr}} - \epsilon_{\text{elast}}^{\text{fibril}}$$

A structural phase diagram:

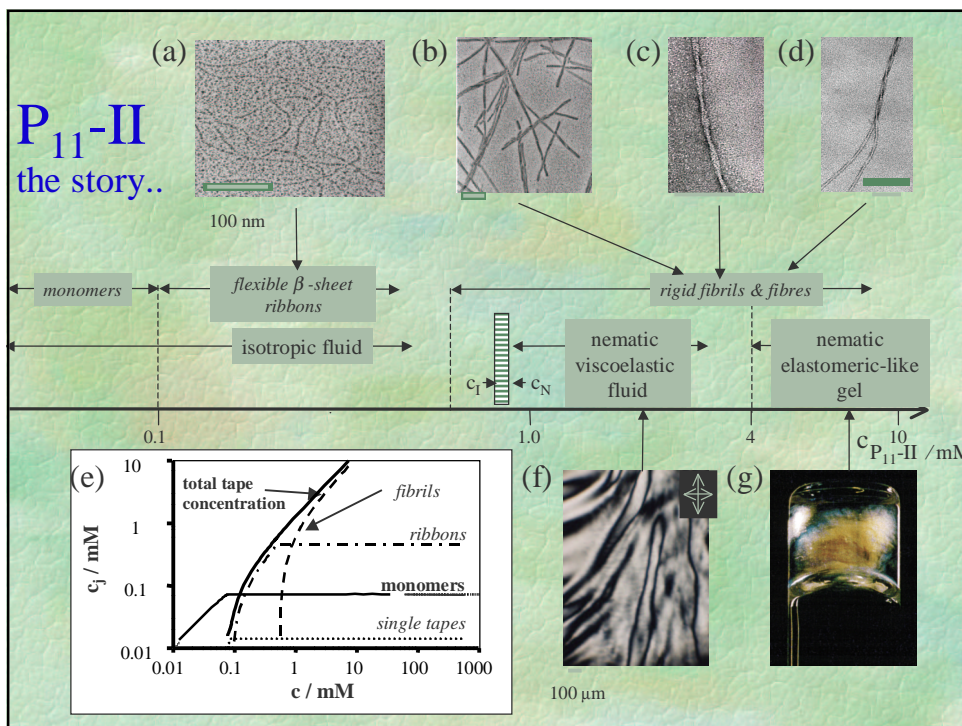


We can predict their formation quantitatively..



..and observe a nematic phase..

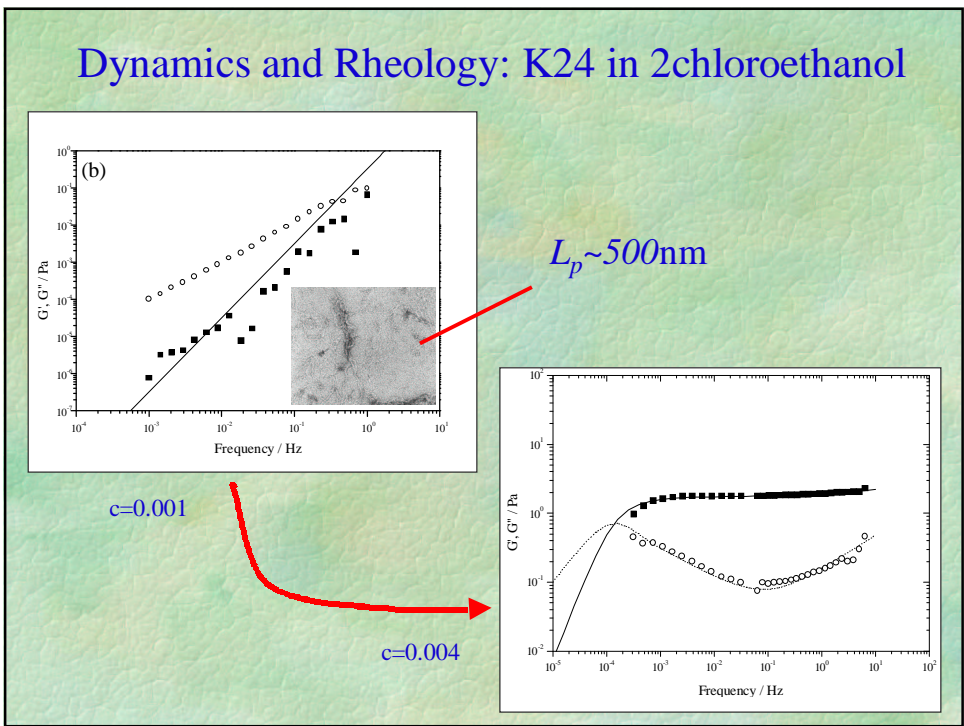
# Self-Assembled Peptide Tapes as Stiff Biopolymers



### Parameter Summary

	Peptide P <sub>11-I</sub>			Peptide P <sub>11-II</sub>		
	$\beta$ -Tapes	Ribbons	Fibrils	$\beta$ -Tapes	Ribbons	Fibrils
$c_{cr}$ / $\mu$ M	8*	1,000*	$c > 25,000^*$	$< 90^*$	90*	$700 \pm 200^*$
$\epsilon_{trans}$		$6.5 \pm 1.5$			$3 \pm 1$	
$\epsilon_{tape}$	$31.0 \pm 1.5$			$24.5 \pm 1.0$		
$\epsilon_{ribbon}$		$(3.5 \pm 1.5) 10^{-3}$			$0.6 \pm 0.3$	
$\epsilon_{fibril}$			$< 10^{-3}$			$(2.0 \pm 0.3) 10^{-4}$
Pitch $h$ / nm	$30 \pm 15^*$	$50 \pm 20^*$			$160 \pm 40$	$160 \pm 40^*$
Twist angle $\gamma_{\omega} / ^\circ$	3*	3*		1	1	1*
Bend angle $\gamma_{\nu} / ^\circ$	3*	0*			0*	0*
$\bar{l}$ / $\mu$ m	$< 0.3^*$	$0.6 \pm 0.2^*$			$1.0 \pm 0.3^*$	20–70*
$L$ / $\mu$ m ( $c = 6$ mM)	$10^{-1}$	$10^{-1} - 10^0$		$10^{-3}$	$10^0$	$10^{17}$
Properties of aq. solution	Isotropic fluid ( $c < 13$ mM) Nematic fluid / gel ( $c > 13$ mM)			Isotropic fluid ( $c < 0.9$ mM) Nematic fluid ( $c = 0.9 - 6$ mM) Nematic gel ( $c > 6$ mM)		

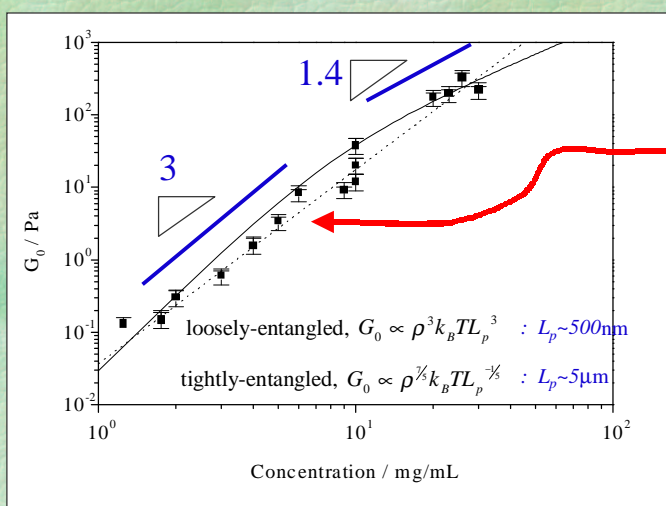
### Dynamics and Rheology: K24 in 2chloroethanol



### Plateau Modulus looks like stiff-entangled:

Estimate of  $L_e \sim 100\text{nm}$  gives

$$G_{curve} \cong \frac{\rho k_B T}{L_e} \cong 4\text{Pa}$$



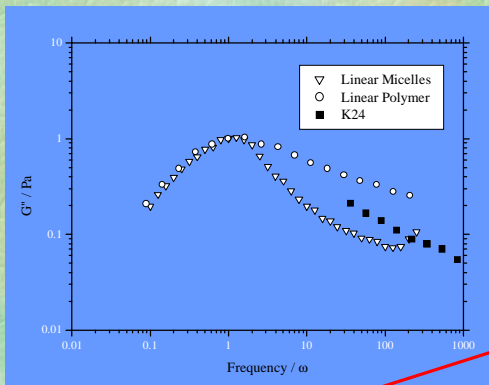
at

$$\phi = 5 \cdot 10^{-3}$$

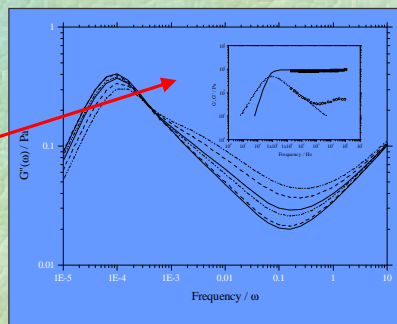
so

$$\rho = 10^{14} \text{m}^{-2}$$

Additional evidence from stiffness from DE-like spectrum

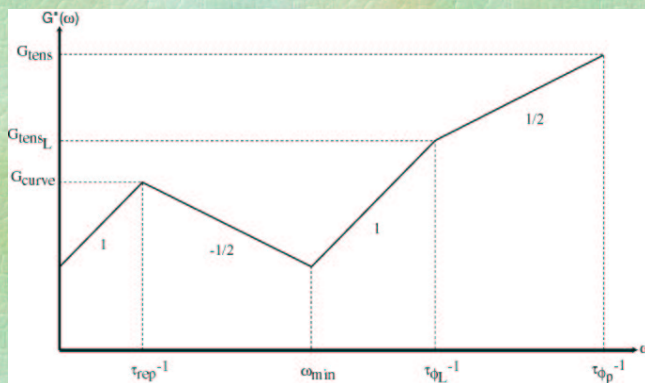


$$U_{eff}(s) = (B_{entropy} + B_{bend}) \left( \frac{s^2}{2} \right)$$



By fitting:  $L_p/L_e \sim 10$

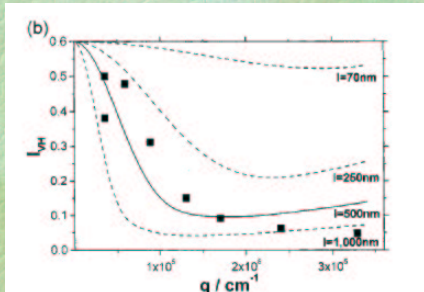
More from Morse, Maggs and more....



Useful relation:  $\ln\left(\frac{\omega_{min}}{\tau_d^{-1}}\right) = \frac{2}{3} \left[ 1 + \ln\left(\frac{L^2}{L_p L_e}\right) \right] \Rightarrow \frac{L}{L_e} \cong 250 \cong 100\mu$

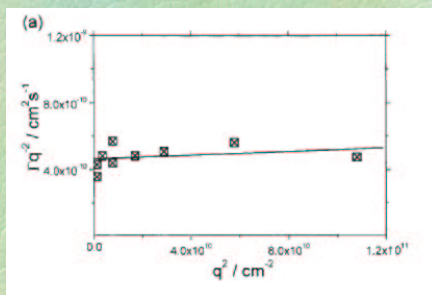
Depolarised Light Scattering

$I_{VH}$



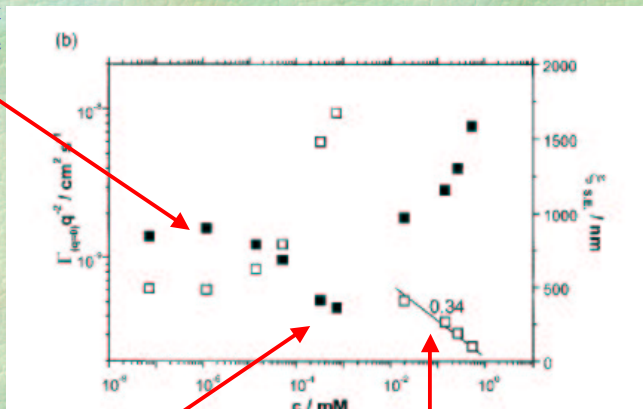
..looks like rods locally

...  $D(q) \sim q^0$



Relaxation rate with concentration

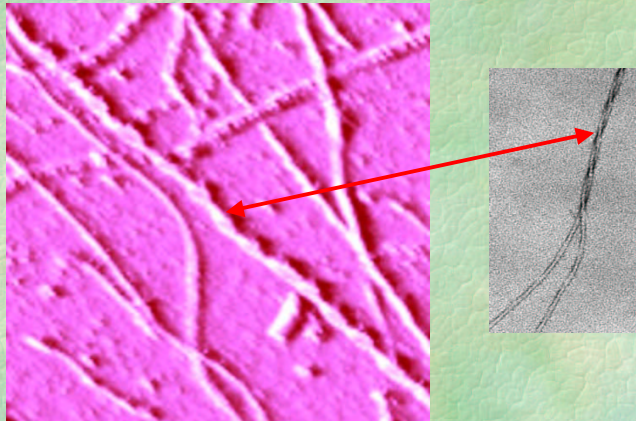
But  $L$  should only be at most 100nm down here



Strange slowing down

Anomalous semi-dilute exponent with  $c$

Application: these structures resemble “amyloids”



C. Dobson and A. Hill (Oxford)

- Next step is to understand kinetics (months!)
- We may have a cleanish model system
- Physics may have more to say about biology when it goes

**Wrong!**