

Hole-doped HTSCs: band structure trend,  
 contact field and correlation with  $T_c$  max

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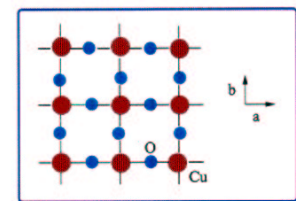
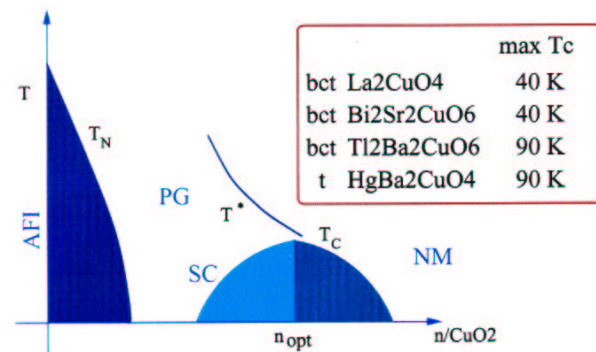
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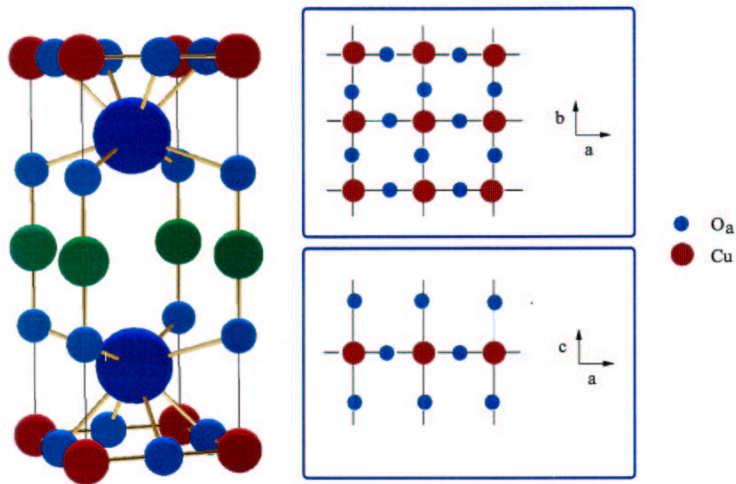


Motivation



Electronic structure  $\rightarrow H = \sum t_{ij} c_i^\dagger c_j$

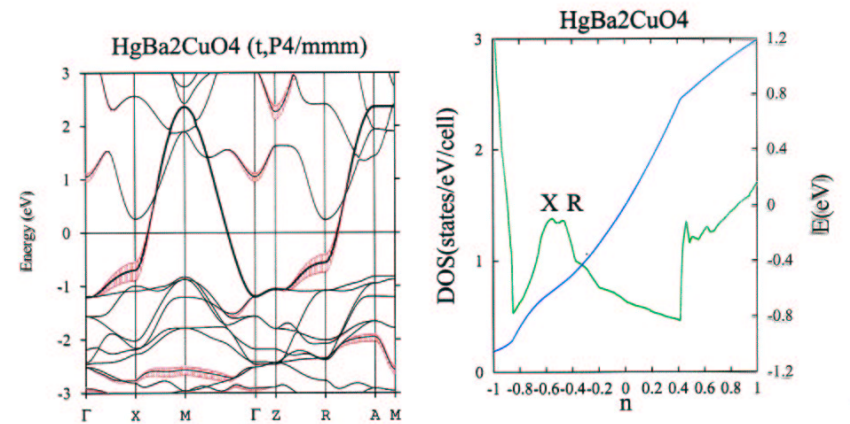
## HTSC: $\text{HgBa}_2\text{CuO}_4$



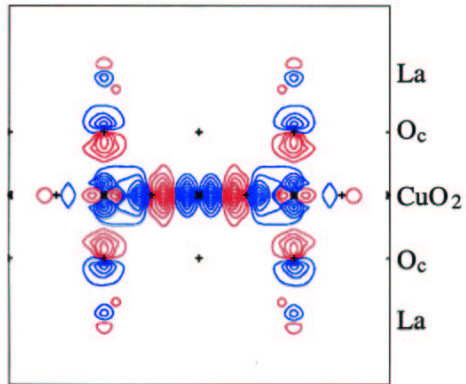
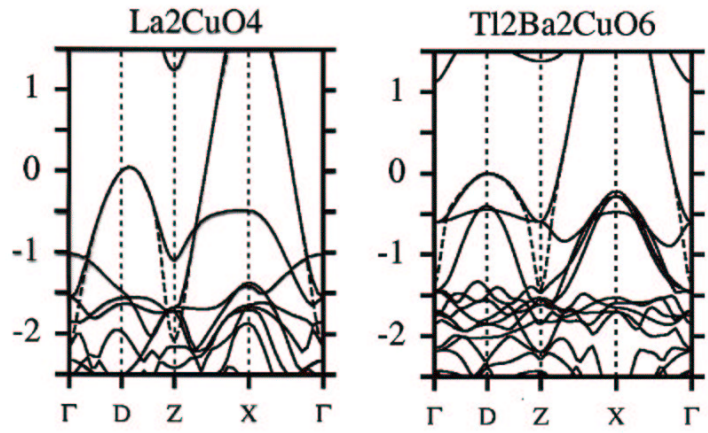
$\text{Cu} - \text{O}_a : 1.93 \text{ \AA}$   
 $\text{Cu} - \text{O}_c : 2.79 \text{ \AA}$   
 $\text{Hg} - \text{O}_c : 1.95 \text{ \AA}$

## Electronic structure

DFT(LDA), TB LMTO method.

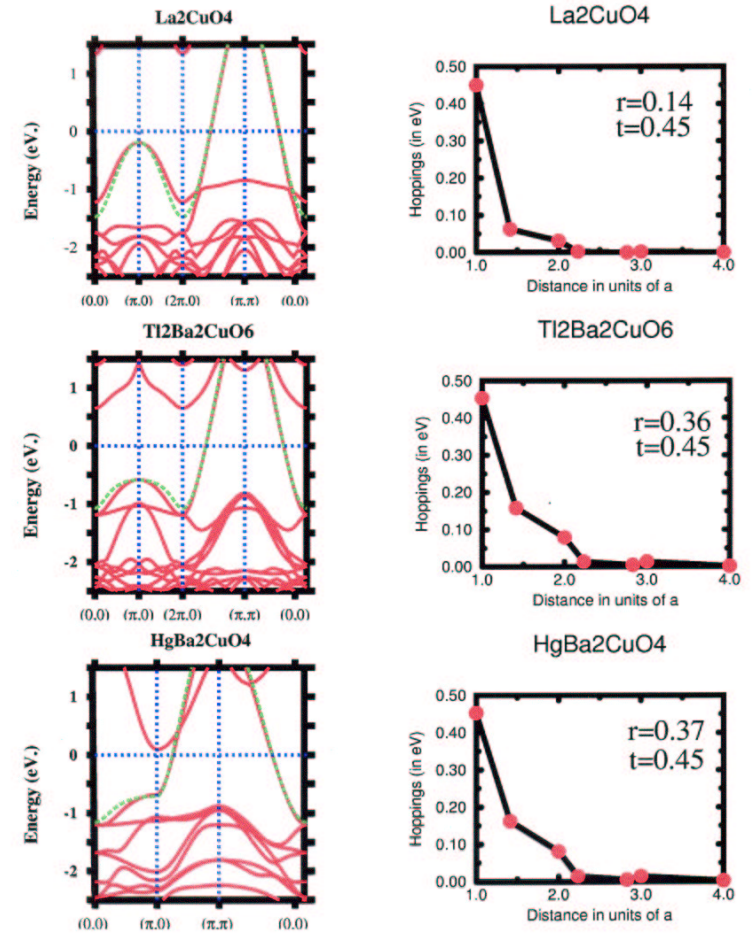


LDA bands → one-band model

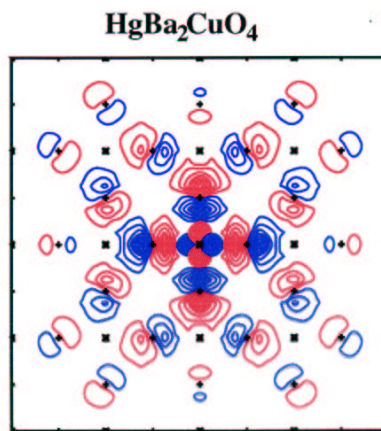
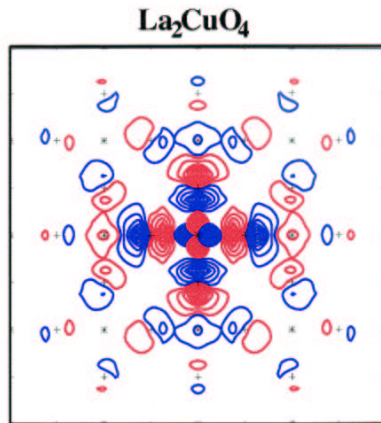


method: O.K. Andersen et al, Phys Rev B **62**, R16218 (2000)

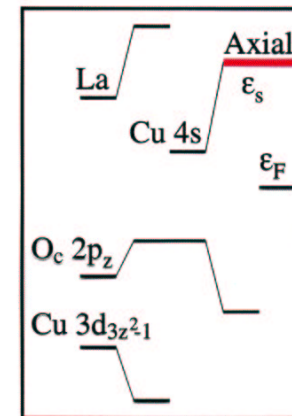
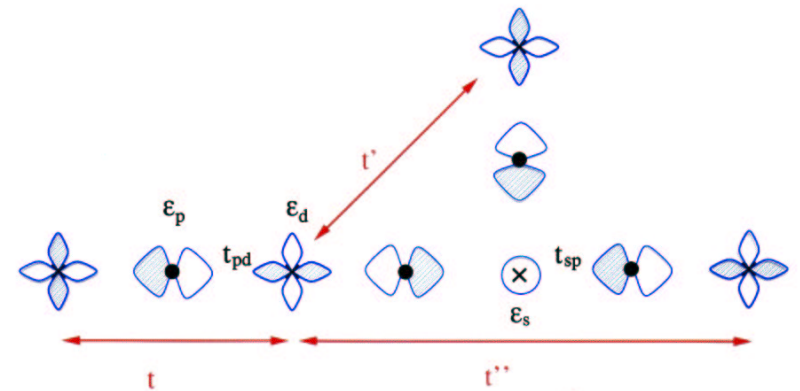
LDA bands, low energy conduction band and hopping integrals



ZMTO conduction-band orbital in the  $\text{CuO}_2$ -layer for  $\text{La}_2\text{CuO}_4$  and  $\text{HgBa}_2\text{CuO}_4$



From one- to four-band model



### One-band model

$$\epsilon(\mathbf{k}) \equiv -2t(\cos k_x + \cos k_y) + 4t'\cos k_x \cos k_y - 2t''(\cos 2k_x + \cos 2k_y) + \dots$$

with  $t'/t = r + o(r)$

### Four-band model

$$\epsilon(\mathbf{k}) = \frac{2t_{pd}^2}{\epsilon_F - (\epsilon_p + \epsilon_d)/2} \left( u + \frac{2rv^2}{1 - 2ru} \right)$$

with  $\begin{Bmatrix} u \\ v \end{Bmatrix} = (\cos k_x \pm \cos k_y)$

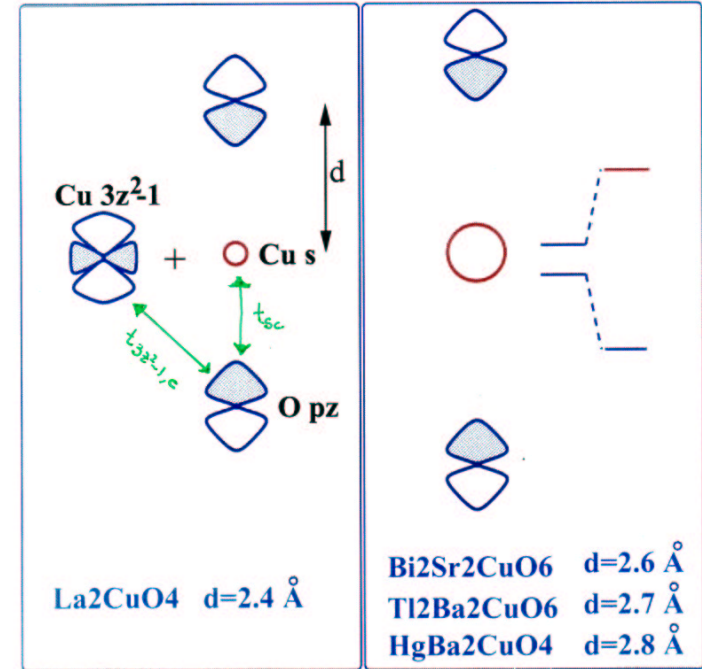
$r = [2(1 + s)]^{-1}$ , and  $s = (\epsilon_s - \epsilon_F)(\epsilon_F - \epsilon_p)/(2t_{sp}^2)$

The range-parameter is essentially the Cu *s* character

$$|c_s|^2 \propto v^2 r^2 |c_d|^2$$

### The axial orbital

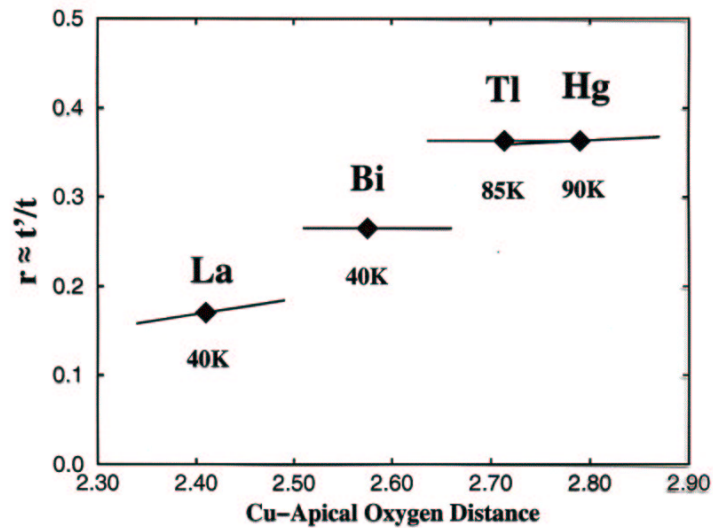
Effective Cu *s*: Cu *s* + apical O<sub>c</sub> *p<sub>z</sub>* + Cu *d<sub>3z<sup>2</sup>-1</sub>*



$$t_{3z^2-1,c} \propto d^{-4} \quad t_{sc} \propto d^{-2}$$

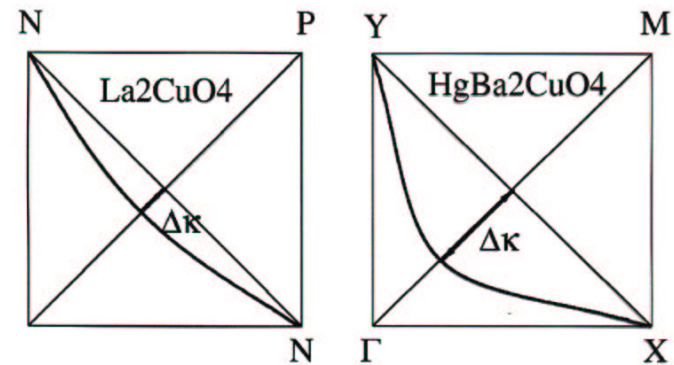
### Parameters of one-band model

single-layer materials



$r$  is controlled by the distance from Cu to apical O and the bonding of apical O to La, Bi, Tl or Hg.

### Constant energy contours passing through the $(\pi, 0)$ saddle point



Materials-dependence contained in a single parameter

$$r = \frac{1}{2} \sin \left( \frac{\Delta k}{\Gamma - M} \right) \sim \frac{t'}{t}$$

## Interpretation and Trends

- The only material dependent parameter is the energy  $\epsilon_s$  of the **effective Cu 4s** orbital (axial orbital). This energy is  $\epsilon_s - \epsilon_{x^2-y^2} \sim 6-9$  eV.

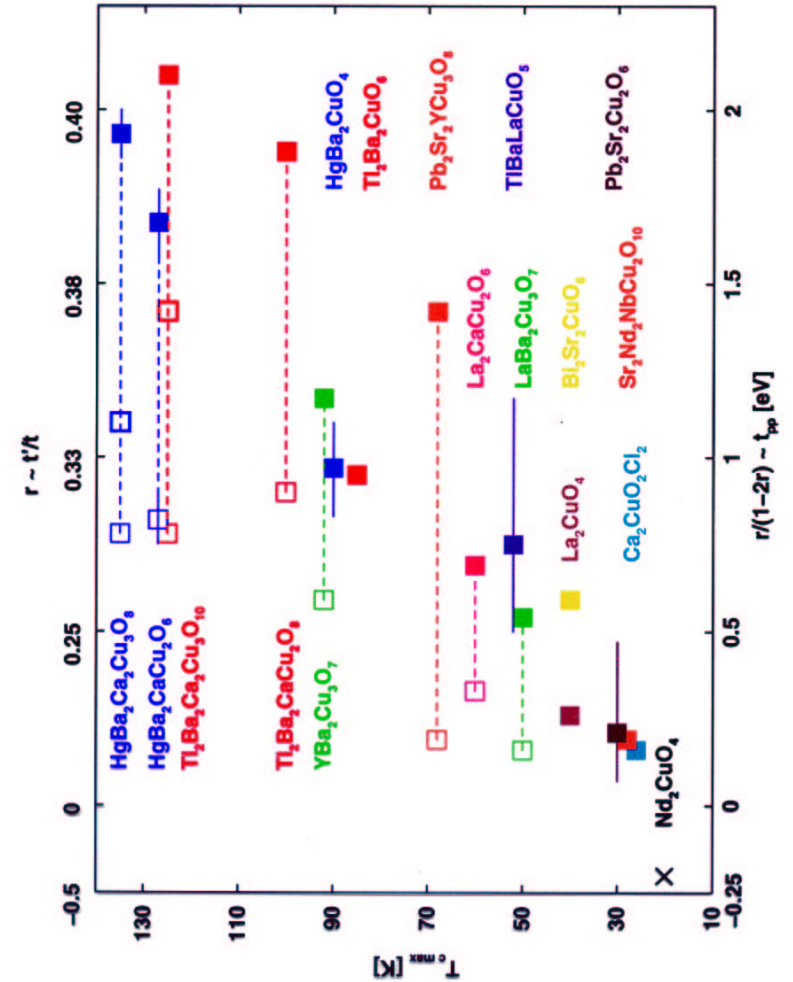
- The hopping integrals  $t', t'' \dots$ , as well as  $t_{\perp}$  proceed via this effective Cu 4s orbital

$$t'/t \sim r \quad t''/t' \sim 1/2 \quad r \equiv r(\epsilon_s)$$

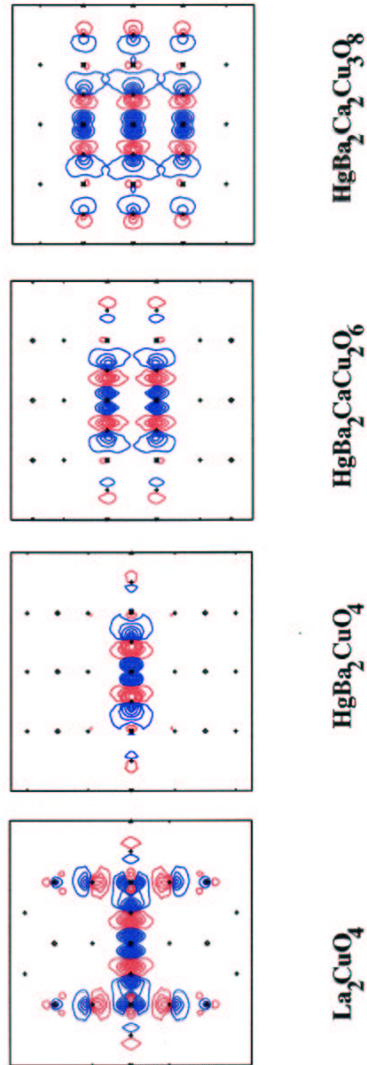
$$t_{\perp} \sim r^2 v^2 \cos ck_z \quad v \equiv \frac{1}{2}(\cos k_x - \cos k_y) \quad \text{tetragonal}$$

$$t_{\perp} \sim r^2 v^2 \cos \frac{1}{2}k_x \cos \frac{1}{2}k_y \cos \frac{1}{2}ck_z \quad \text{bct}$$

- One of the most important structural parameters determining the normal and superconducting properties for **single layer materials** is the **distance between the apical oxygen and the plane copper**.



Conduction-band orbital in the  $xz$ -plane



## Interpretation and Trends

- The essential material-dependence is contained in a single parameter,  $r$ , which expresses the range of the intra-layer hopping,  $t'/t \sim r + o(r)$ .
- This parameter is controlled by the **axial orbital**, the effective Cu 4s,  $\epsilon_s - \epsilon_{d_{x^2-y^2}} \sim 6 - 9eV$ .
- The axial orbital is a hybrid between Cu 4s, Cu  $3d_{3z^2-1}$ , apical oxygen  $2p_z$  and farther orbitals such as Hg or La.
- The ratio of axial-orbital to Cu  $d_{x^2-y^2}$  character is proportional to  $r^2(\cos k_x - \cos k_y)^2 = r^2v^2$
- The materials with larger  $r$  tend to be those with the higher observed value of  $\max T_c$ . For the materials with the highest observed  $\max T_c$ , the axial orbital is almost pure Cu 4s.
- The correlation between  $r$  and  $\max T_c$  holds also for multilayers with  $n \leq 3$ , if electrons are assumed to be coherent across the multilayer and if we use the  $r$ -value for the Cu 4s **bonding** subband.



- The axial orbital is also the main vehicle for perpendicular hopping. The axial character is maximum at "hot spots" and vanishes at cold "spots".
- $\text{CuO}_2$  layers stacked on top of each other:  $t_{\perp}(\mathbf{k}) \propto v^2 \cos k_z$ . bct stacked  $\text{CuO}_2$  layers: additional nodes along  $k_x = \pi \rightarrow k_z$ -dispersion killed in single-layer TI but not in single-layer Hg, nearly same max  $T_c$ . This argues against pair-tunnelling as a mechanism for boosting  $T_c$ .

#### Experiments consistent with our results

- Fermi surface shape: ARPES of  $\text{La}_2\text{CuO}_4$  (overdoped),  $\text{YBa}_2\text{CuO}_7$  and  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$
- $T_c$  in  $\text{La}_{1.9}\text{Sr}_{0.1}\text{CuO}_4$  films with different degrees of strain, J.-P. Locquet et al., Nature **394**, 453 (1998)