

The cold dark matter model

Carlos S. Frenk
Institute for Computational Cosmology,
Durham University



The new Ogden Centre
at Durham

The Λ CDM model of cosmogony


Cosmological constant Cold dark matter

- *Ab initio*, **fully specified** model of cosmic evolution and the formation of cosmic structure
- Based on **known laws** of Physics (GR) which were formulated and tested **independently** of the Λ CDM model
- Has strong **predictive** power
- Has made a number of **predictions** that were subsequently **verified** empirically (e.g. CMB, LSS, galaxy formation)

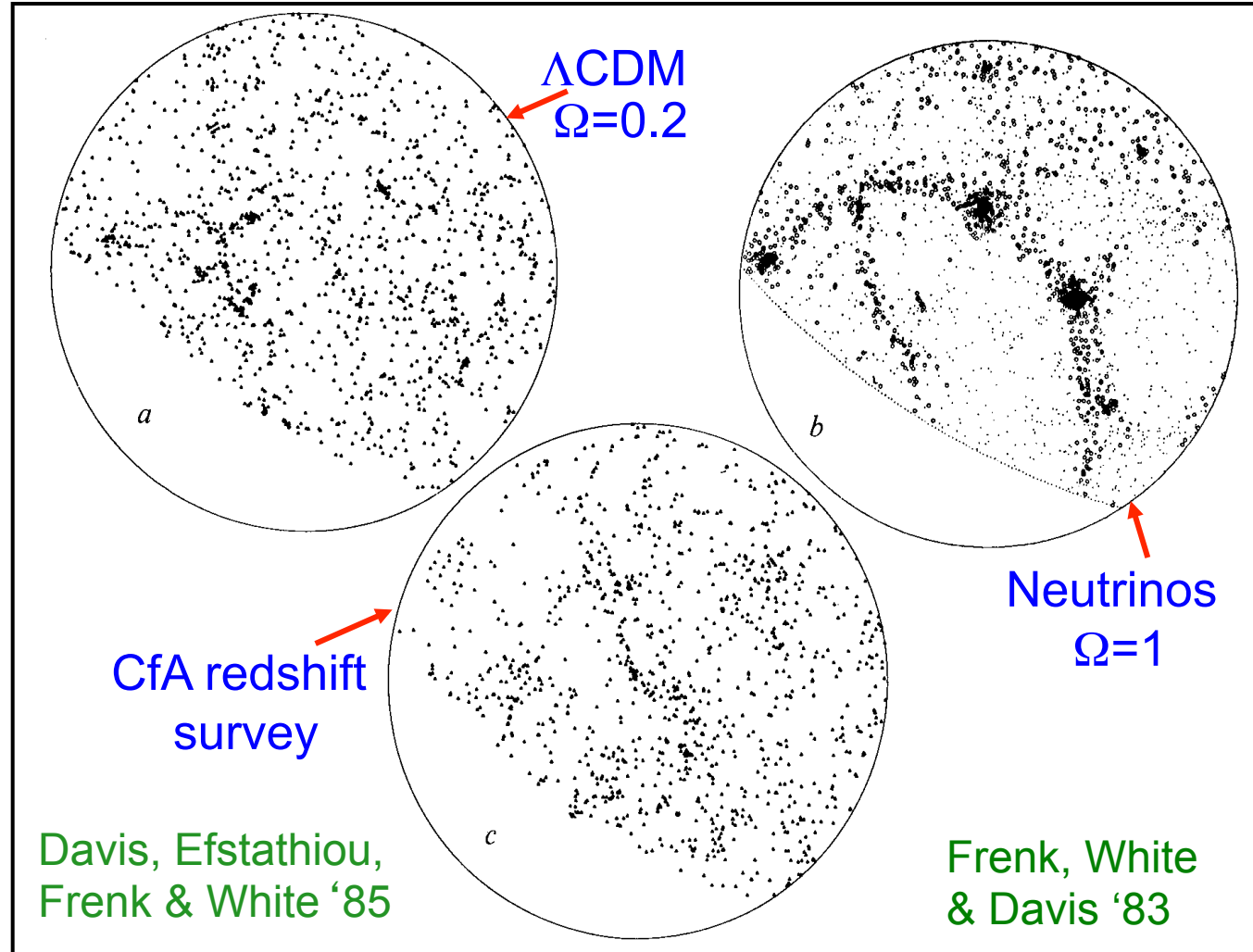
Non-baryonic dark matter cosmologies

Neutrino DM \rightarrow
wrong clustering

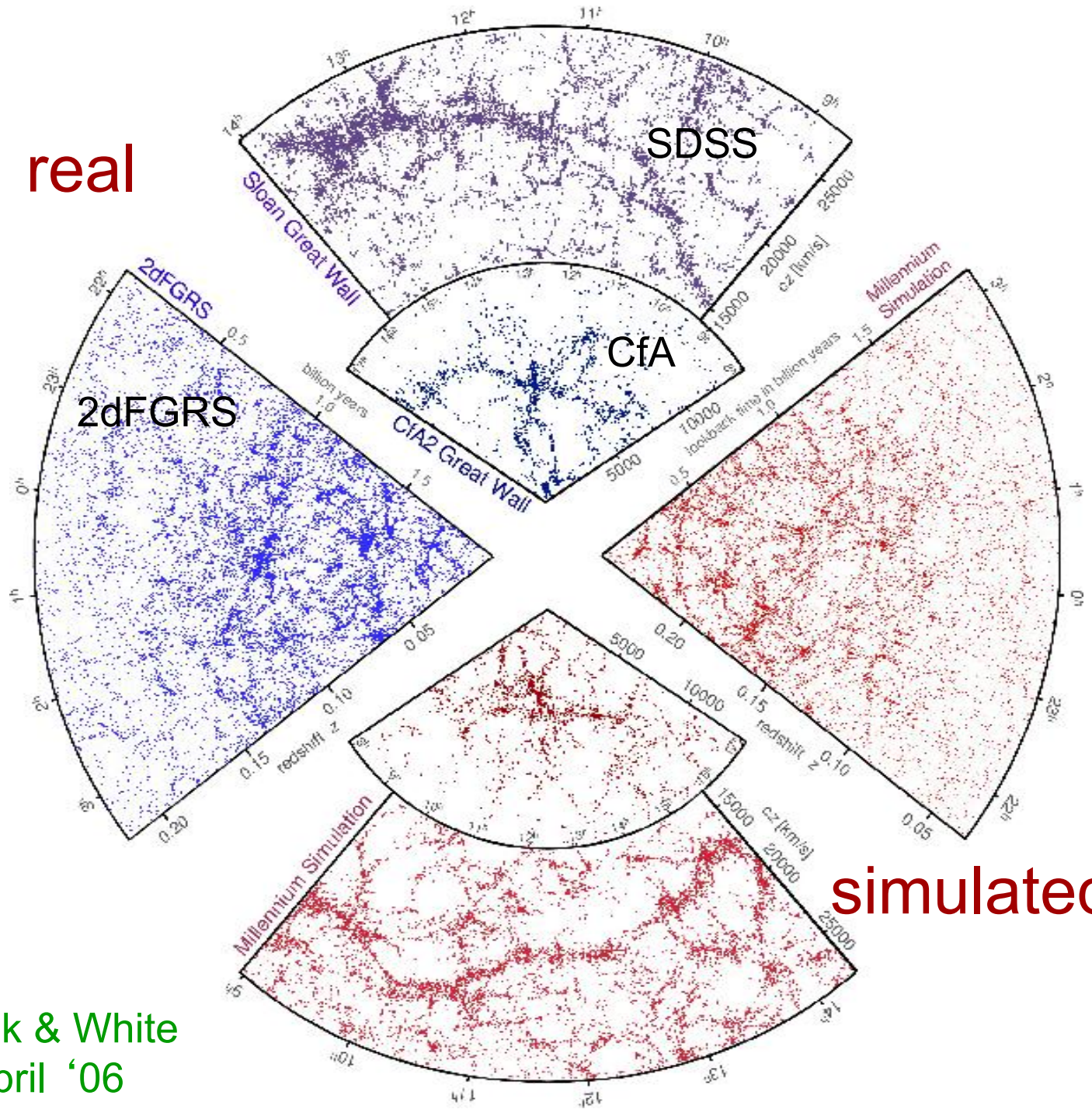
Neutrinos cannot
make appreciable
contribution to Ω
 $\rightarrow m_\nu \ll 30$ eV

Early CDM N-body
simulations gave
promising results

In CDM structure
forms hierarchically



real



simulated

The big Bang



300 tho

3 minutes

15 thousand million years

The temperature of this radiation should show small irregularities

Production of particle dark matter
($t \sim 10^{-10}$ s)

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degr

Linear growth

Cosmic inflation
(initial conditions)
($t \sim 10^{-35}$ s)

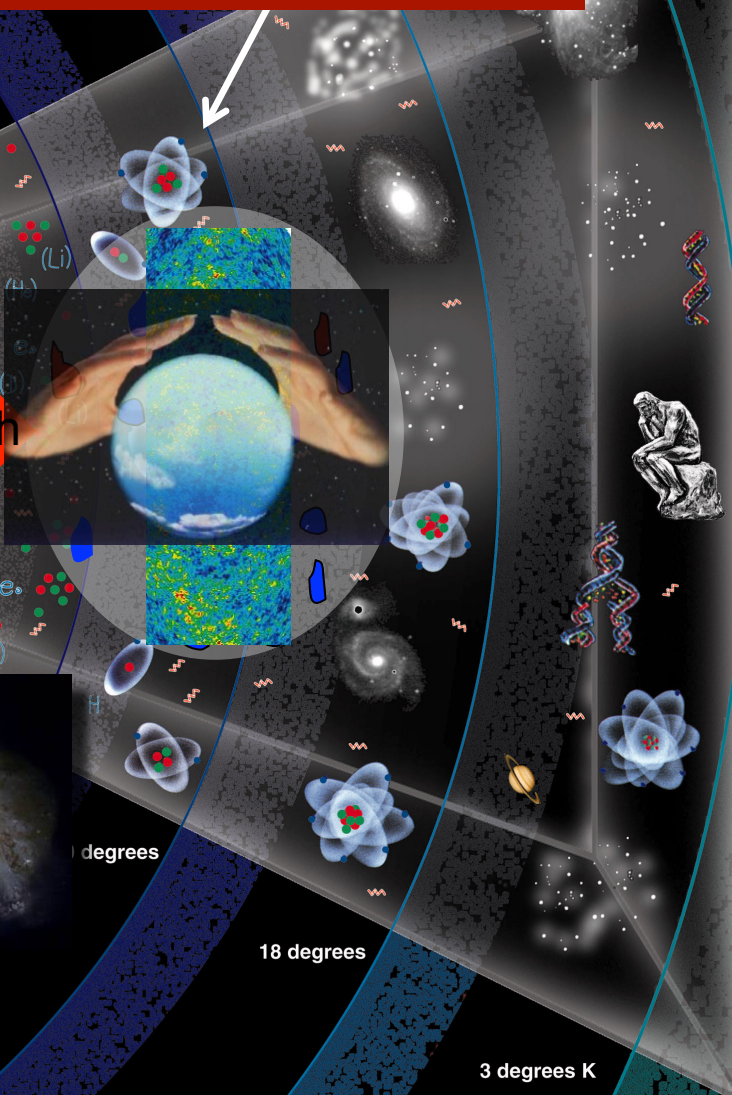
- radiation
- particles
- W^+ heavy particles carrying the weak force
- W^-
- Z
- quark
- anti-quark
- electron
- positron (anti-proton)
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium

degrees

18 degrees

3 degrees K

t = 13.7 billion yrs



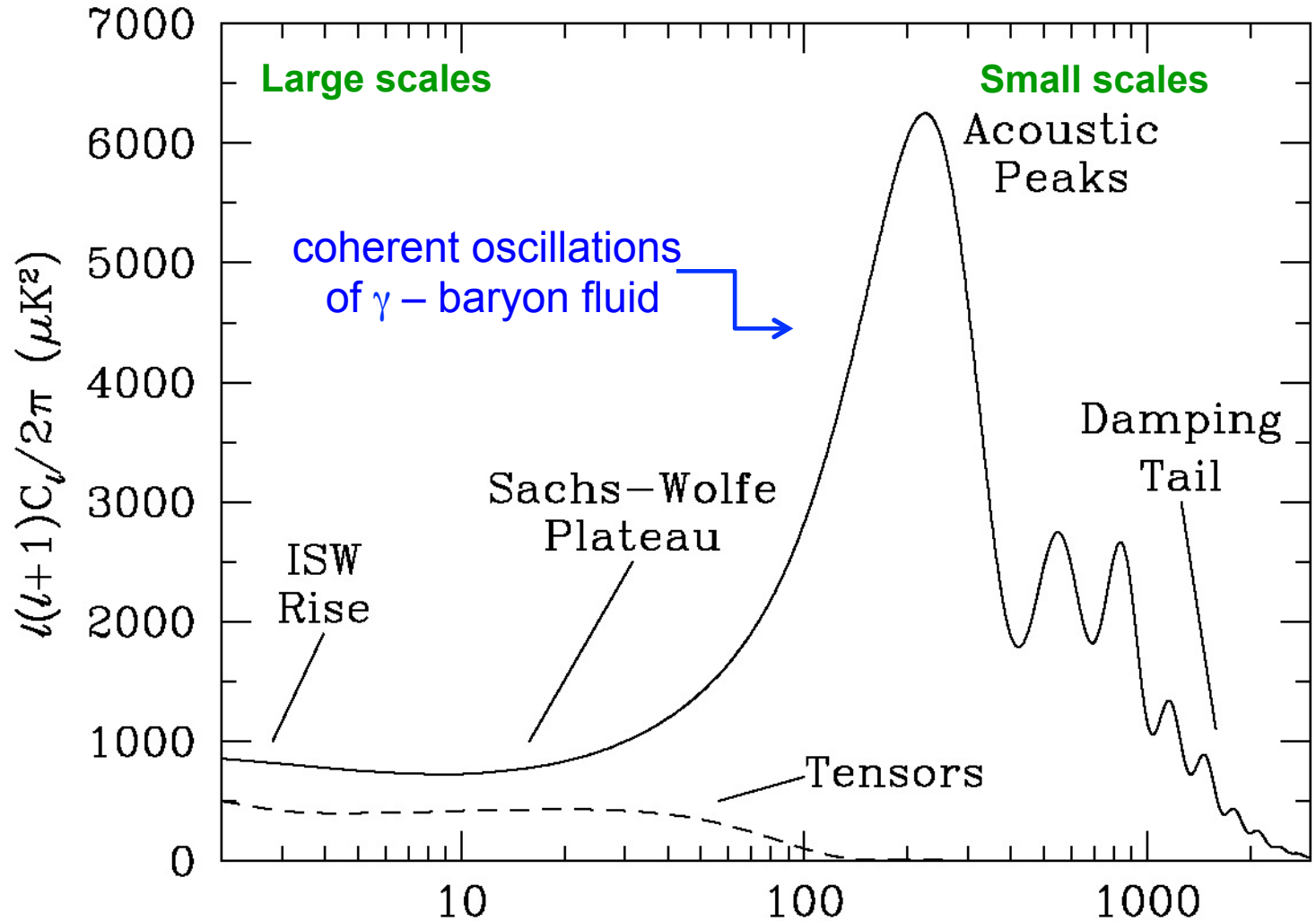
The initial conditions for galaxy formation



Quantum fluctuations from inflation

Temperature anisotropies in CMB

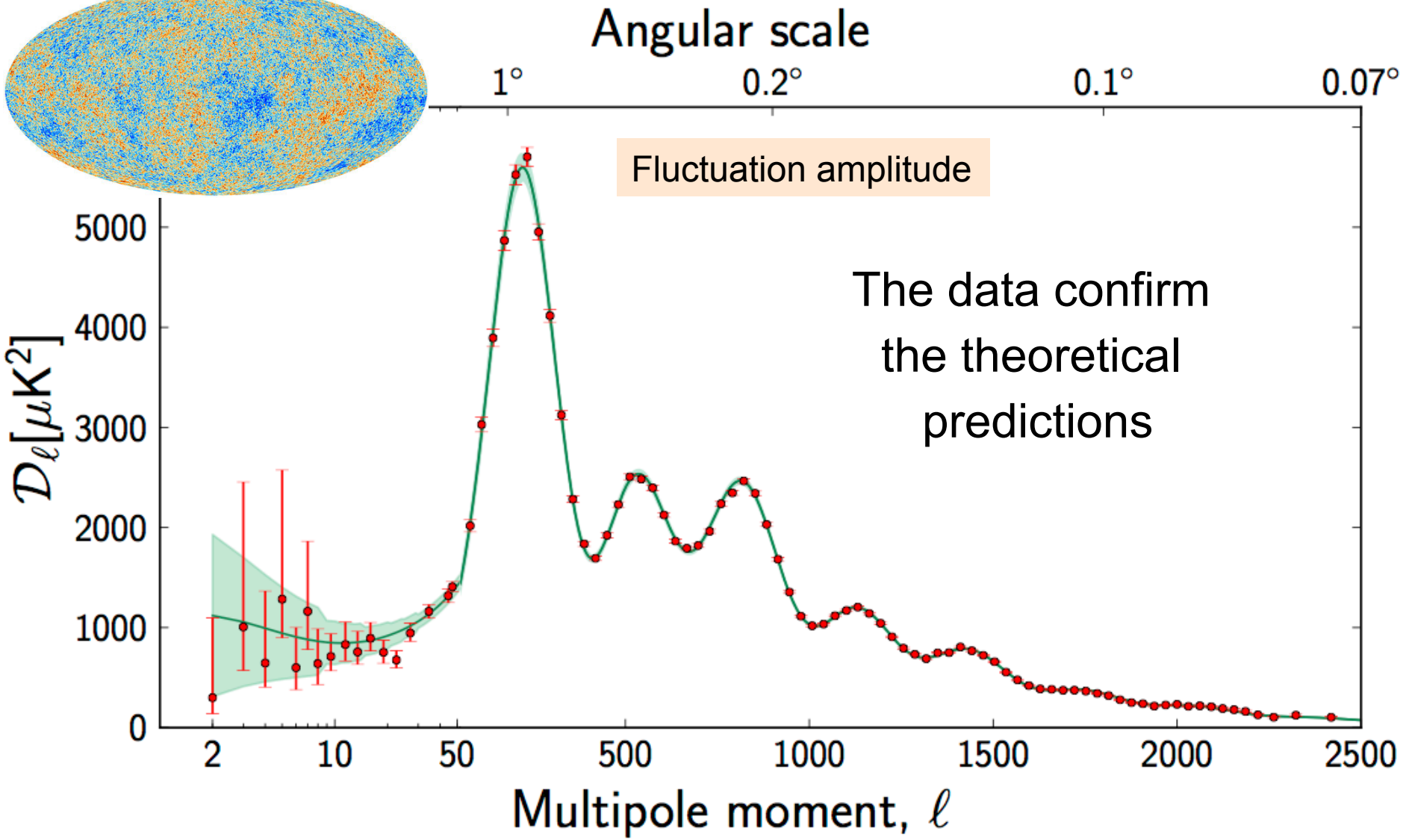
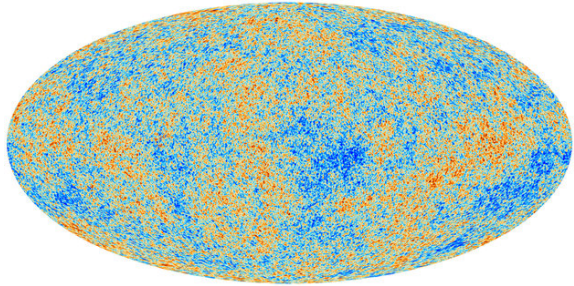
2D power spectrum



Peebles & Yu '70 Sunyev & Zel'dovich '70

For CDM: Peebles '82; Bond & Efstathiou '84

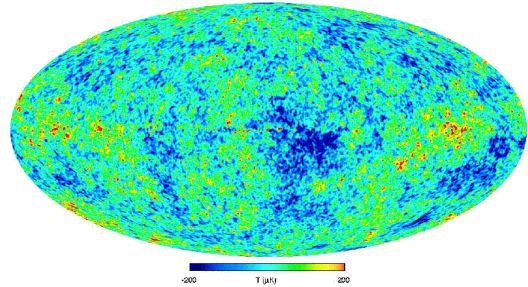
Planck: CMB temperature anisotropies



		<i>Planck</i> +WP	
Parameter		Best fit	68% limits
6 model parameters	$\Omega_b h^2$	0.022032	0.02205 ± 0.00028
	$\Omega_c h^2$	0.12038	0.1199 ± 0.0027
	$100\theta_{MC}$	1.04119	1.04131 ± 0.00063
	τ	0.0925	$0.089^{+0.012}_{-0.014}$
	n_s	0.9619	0.9603 ± 0.0073
	$\ln(10^{10} A_s)$	3.0980	$3.089^{+0.024}_{-0.027}$

A 40σ detection of non-baryonic dark matter using only $z=1000$ data!

The cosmic power spectrum: from the CMB to the 2dFGRS

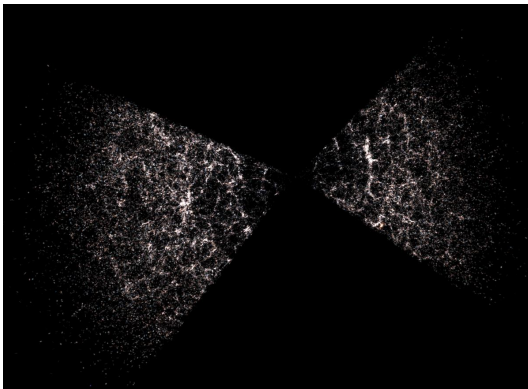


$z \sim 1000$

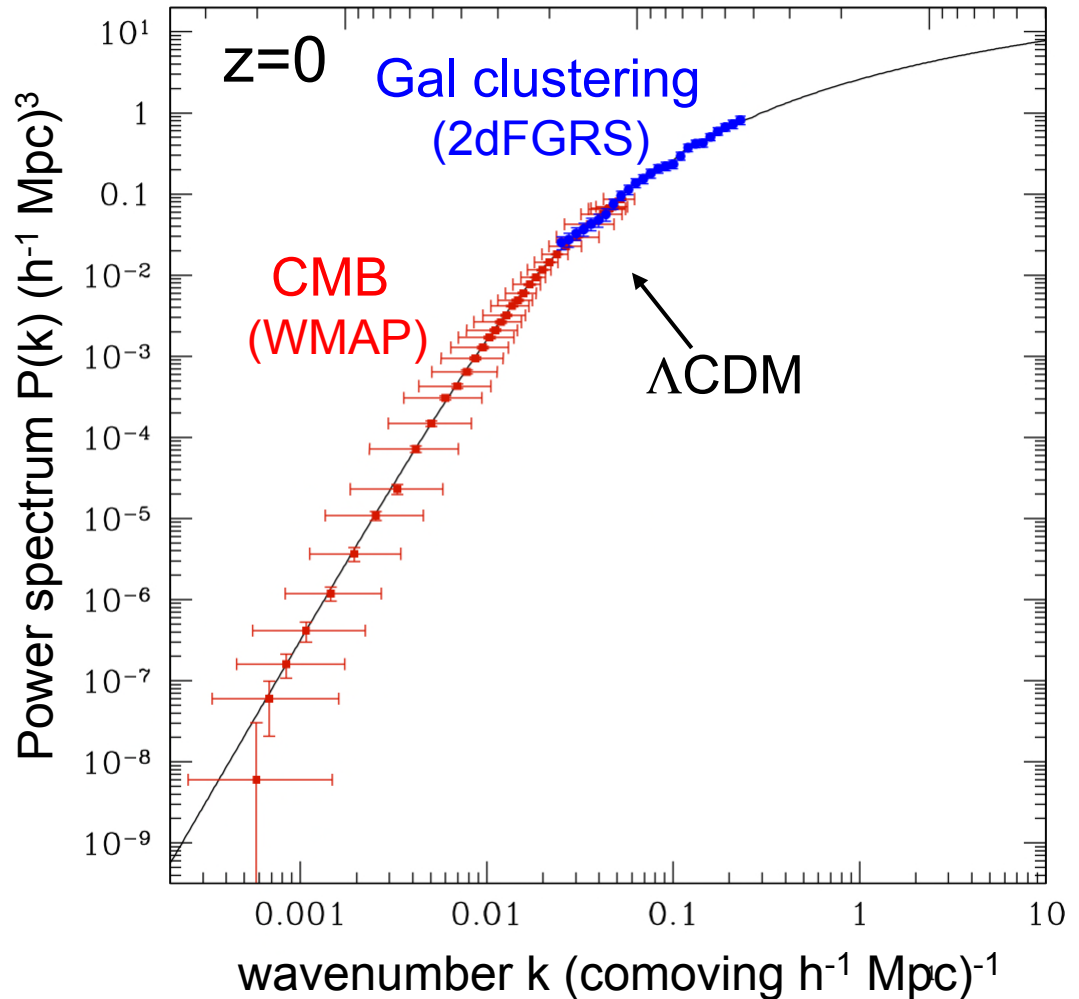
$\text{Log } k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)

1 000 100 10



$z \sim 0$



⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06

The big Bang



300 tho

3 minutes

The cosmic microwave background is emitted
($t \sim 350,000$ yrs)

15 thousand million years

Production of particle dark matter
($t \sim 10^{-10}$ s)

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degr

Linear growth

Non-linear growth

$t = 13.7$ billion yrs

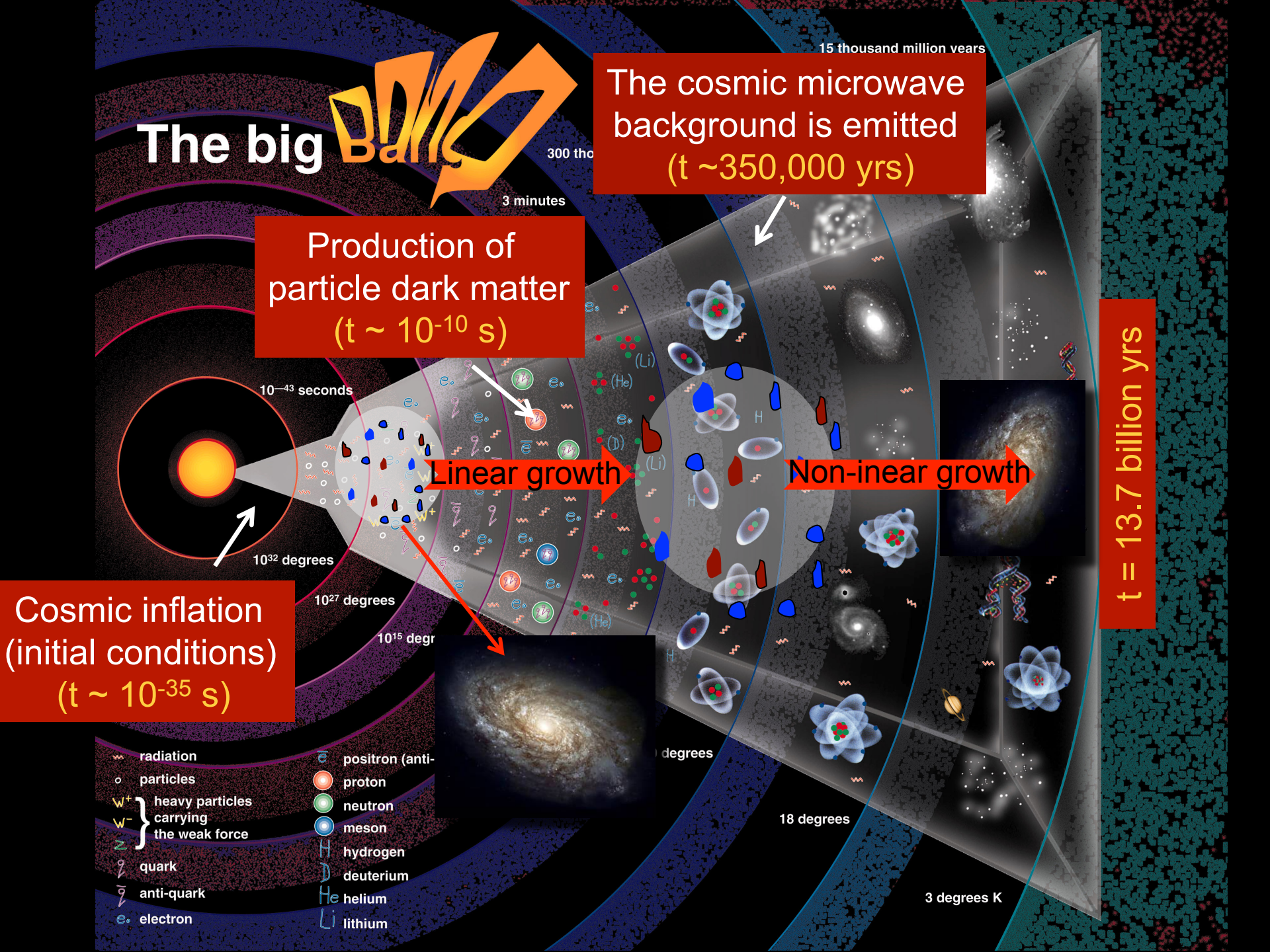
Cosmic inflation
(initial conditions)
($t \sim 10^{-35}$ s)

- ⌘ radiation
- particles
- W⁺ heavy particles carrying the weak force
- W⁻ heavy particles carrying the weak force
- Z heavy particles carrying the weak force
- q quark
- q̄ anti-quark
- e⁻ electron
- e⁺ positron (anti-proton)
- n neutron
- m meson
- H hydrogen
- D deuterium
- He helium
- Li lithium

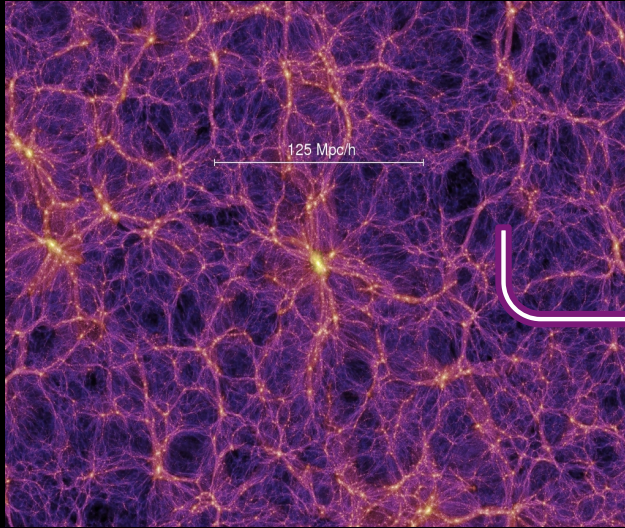
1 degrees

18 degrees

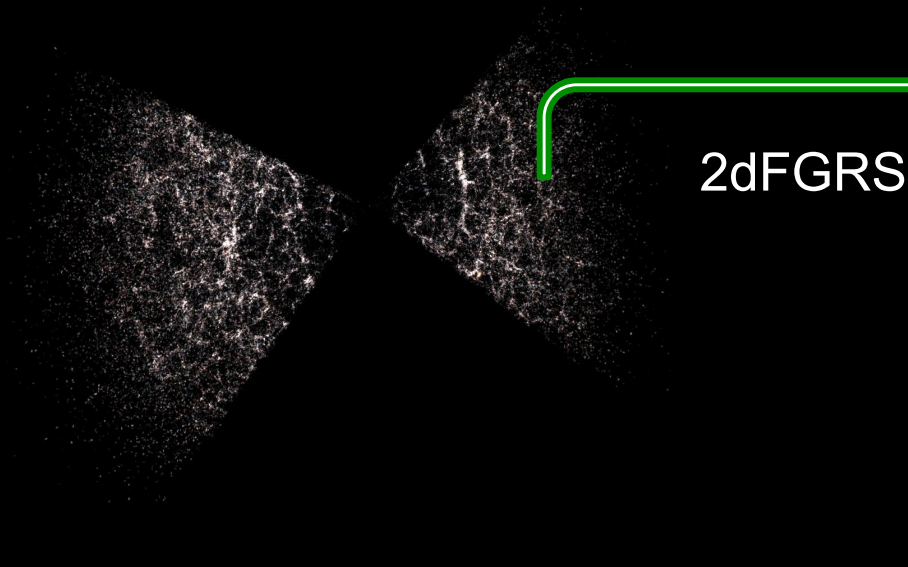
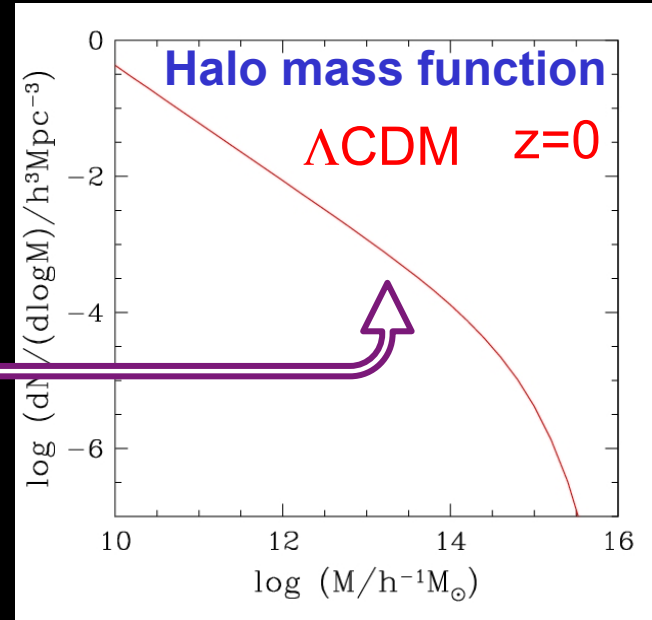
3 degrees K



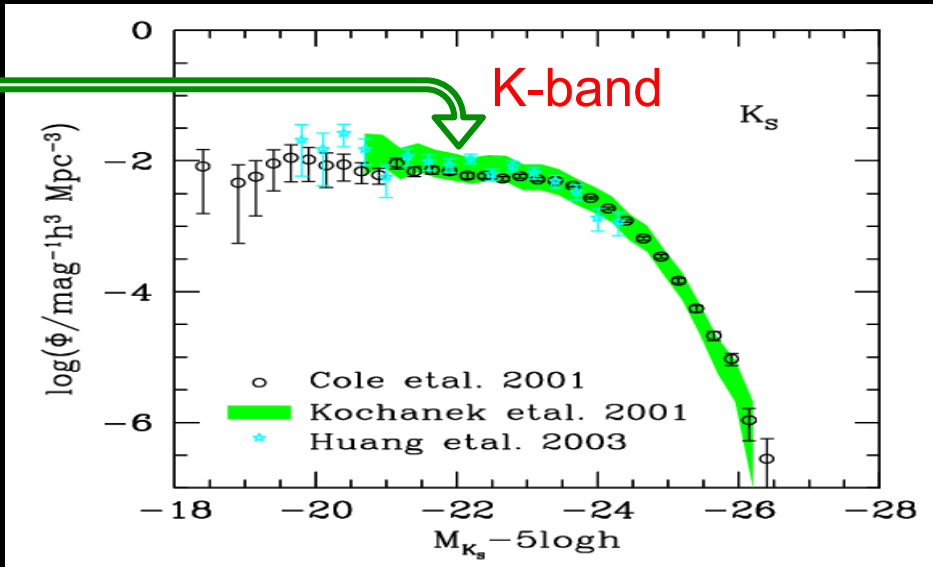
Abundance of gals & dark halos



Millennium simulation



2dFGRS

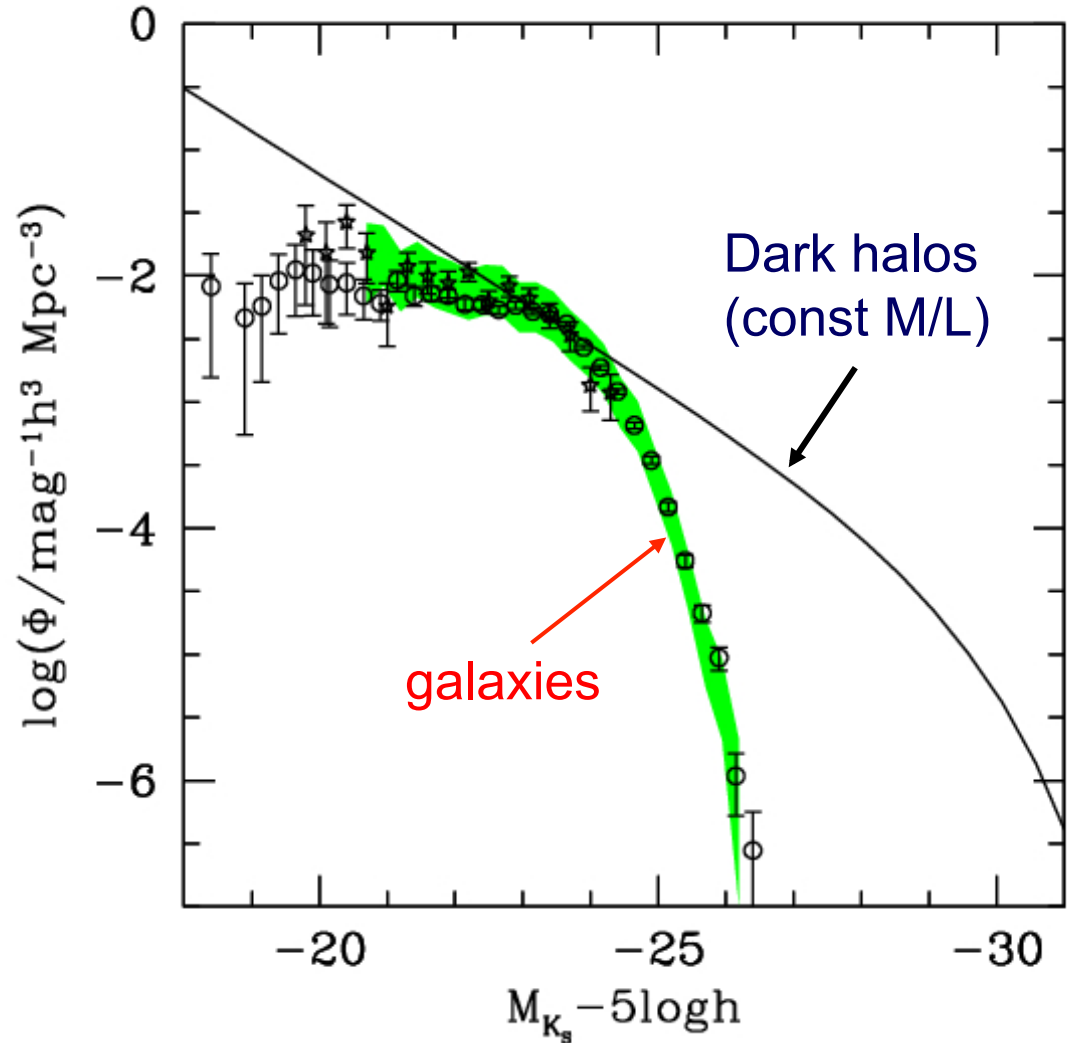


The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



Complicated variation of M/L with halo mass



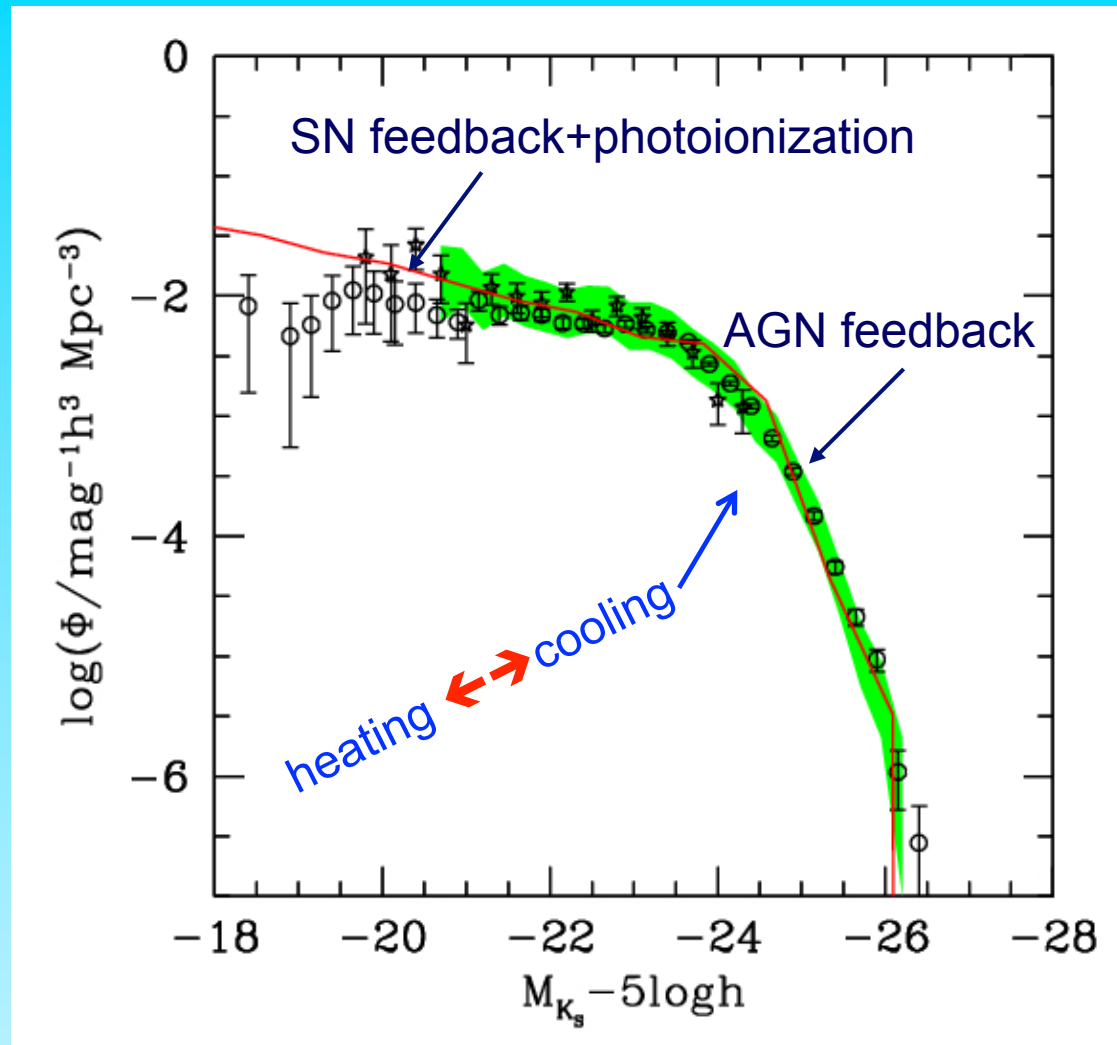
Deconstructing the galaxy LF

Faint end:

Photoionization + reheating of cold disk gas by SN

Bright end:

AGN feedback: energy transported by bubbles



VIRGO

icc.dur.ac.uk/Eagle

“Evolution and assembly of galaxies and
their environment”

THE EAGLE PROJECT

Virgo Consortium

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

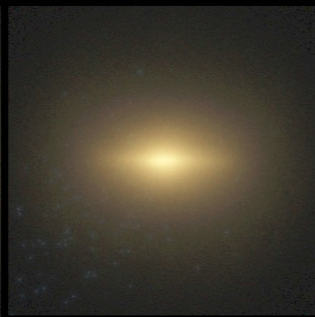
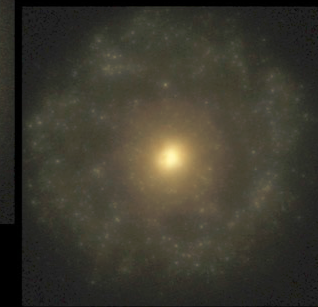
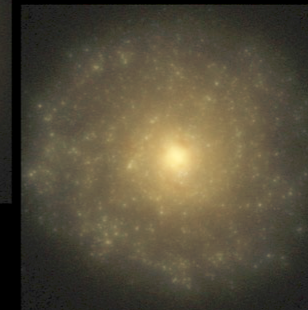
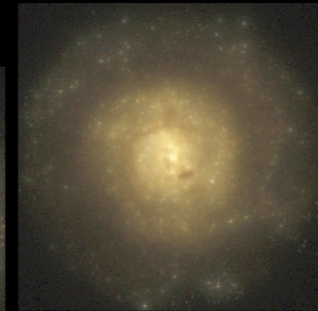
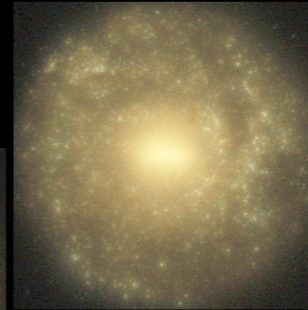
The Hubble Sequence realised in cosmological simulations

SB

E0

E7

S0



Irr

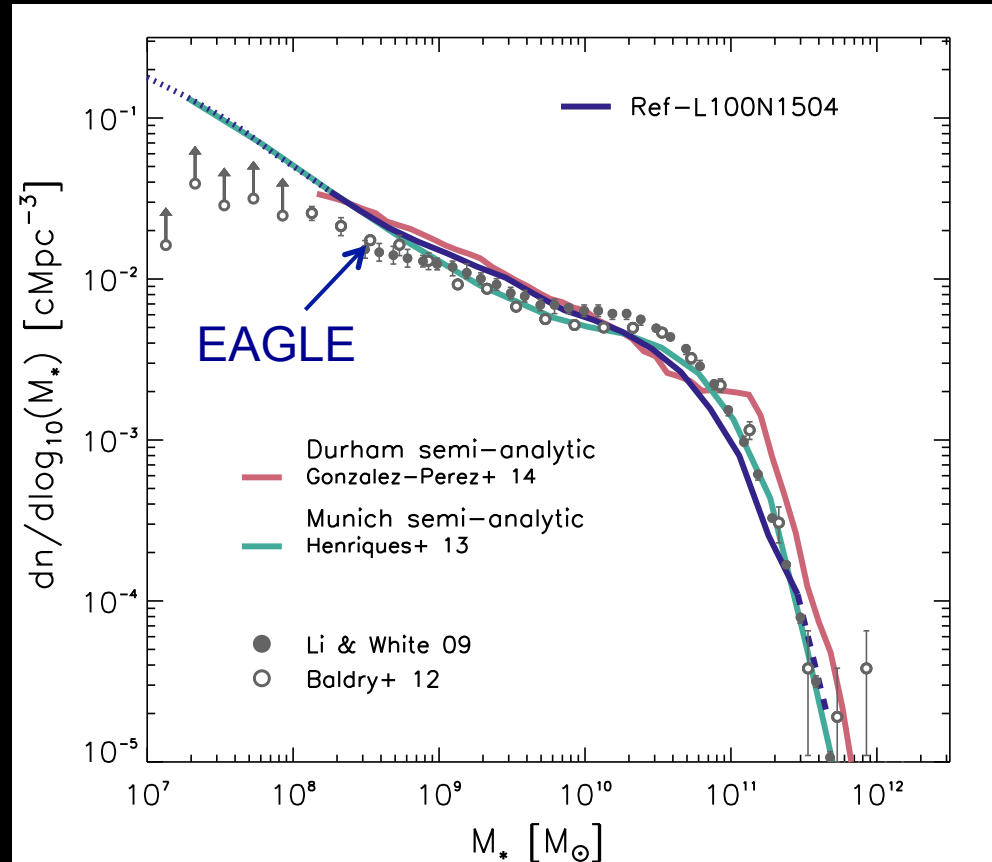
S

Trayford et al '15

Galaxy stellar mass function

Comparison to semi-analytic models

Λ CDM gives an excellent match to the galaxy stellar mass function



The CDM small-scale “crisis”

Three “problems:”

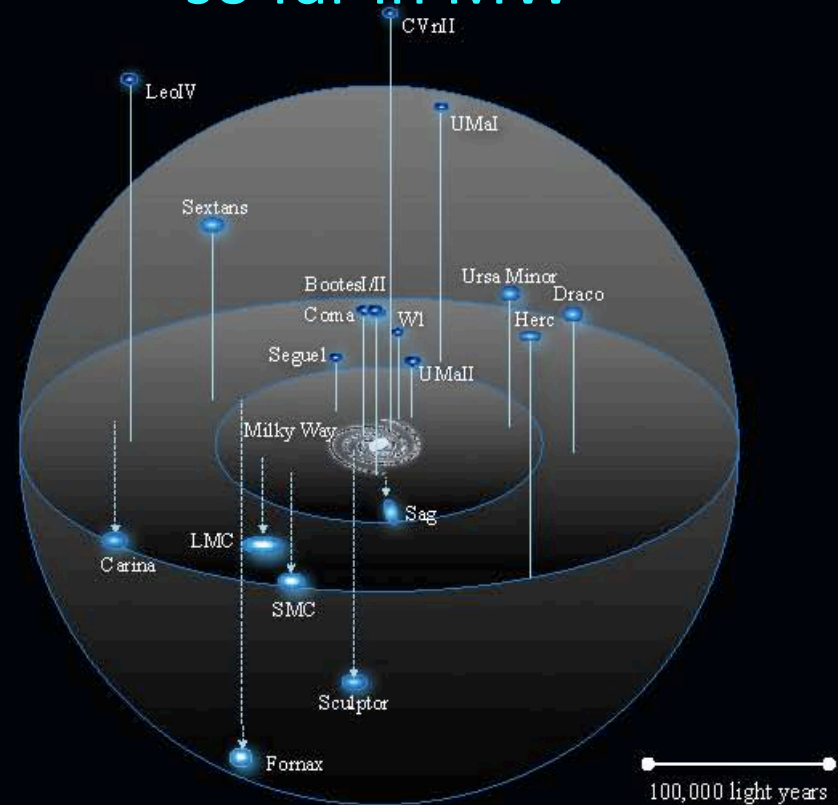
1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “core-cusp” problem

The satellites of the Milky Way

cold dark matter



~50 satellites discovered
so far in MW



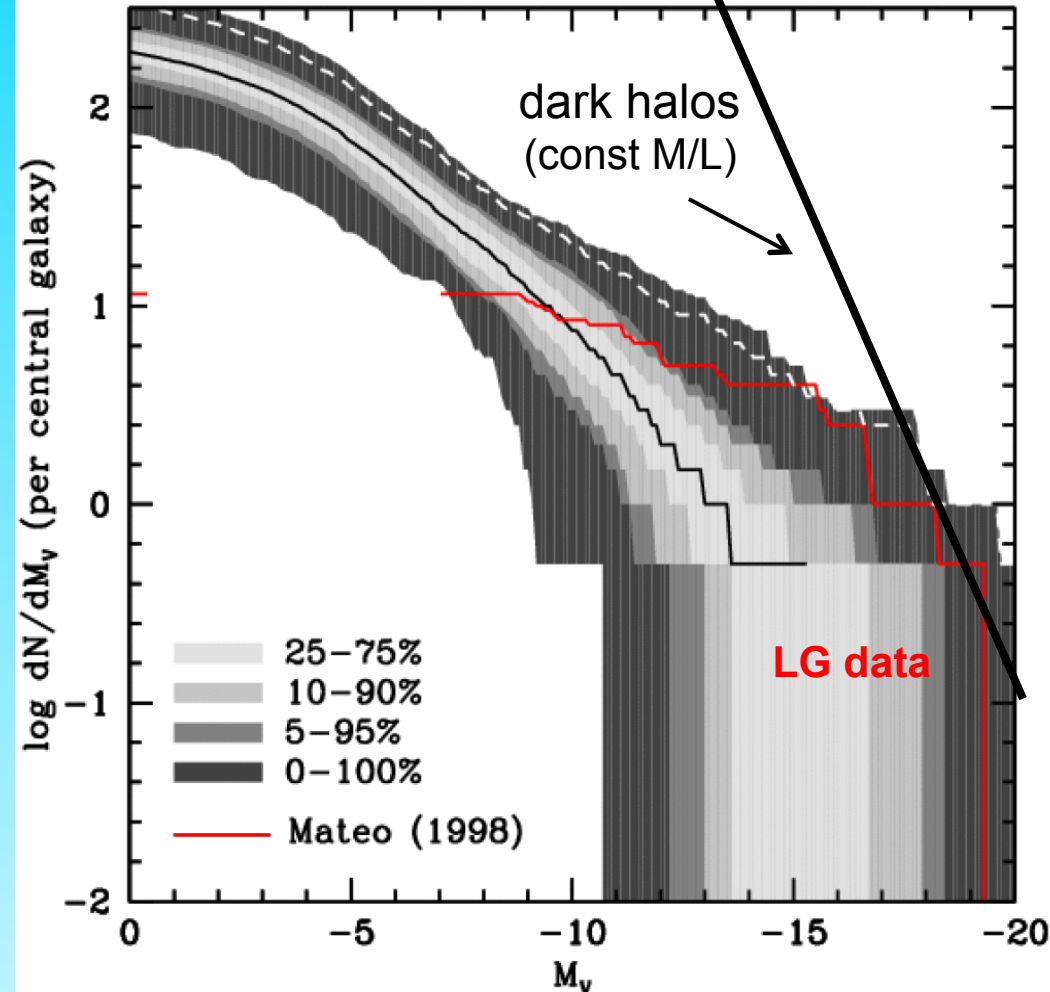
Most subhalos never make a galaxy!

Because:

- Reionization heats gas to 10^4K , preventing it from cooling and forming stars in small halos ($T_{\text{vir}} < 10^4\text{K}$)
- Supernovae feedback expels residual gas in slightly larger halos

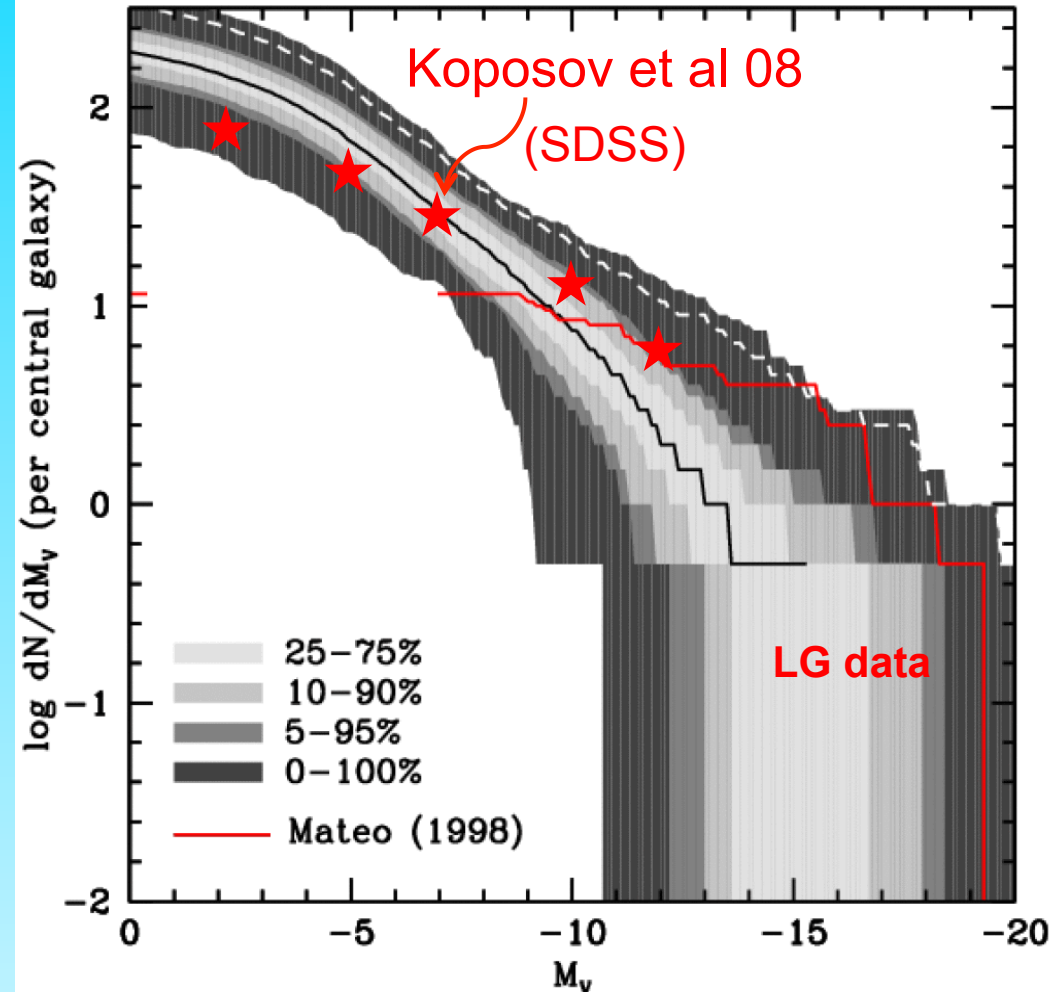
Luminosity Function of Local Group Satellites

- Median model \rightarrow correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare ($\sim 10\%$ of cases)



Luminosity Function of Local Group Satellites

- Median model \rightarrow correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare ($\sim 10\%$ of cases)



DARK MATTER SUBSTRUCTURE WITHIN GALACTIC HALOS

BEN MOORE, SEBASTIANO GHIGNA, AND FABIO GOVERNATO

Department of Physics, Science Laboratories, South Road, University of Durham, Durham, England, DH1 3LE, UK;
ben.moore@durham.ac.uk, ssg@durham.ac.uk, fabio@antares.merate.mi.astro.it

GEORGE LAKE, THOMAS QUINN, AND JOACHIM STADEL

Department of Astronomy, Box 351580, University of Washington, Seattle, WA 98195-1580;
lake@hermes.astro.washington.edu, trq@hermes.astro.washington.edu, stadel@hermes.astro.washington.edu

AND

PAOLO TOZZI

Osservatorio Astronomico di Roma, Via Frascati, 33, Monteporzio Catone, Rome, I-00040, Italy; paolo@pha.jhu.edu
Received 1999 April 16; accepted 1999 August 2; published 1999 September 13

ABSTRACT

We use numerical simulations to examine the substructure within galactic and cluster mass halos that form within a hierarchical universe. Clusters are easily reproduced with a steep mass spectrum of thousands of substructure clumps that closely matches the observations. However, the survival of dark matter substructure also occurs on galactic scales, leading to the remarkable result that galaxy halos appear as scaled versions of galaxy

2131 citations

637 citations

REIONIZATION AND THE ABUNDANCE OF GALACTIC SATELLITES

JAMES S. BULLOCK, ANDREY V. KRAVTSOV,¹ AND DAVID H. WEINBERG

Department of Astronomy, The Ohio State University, 140 W. 18th Avenue, Columbus, OH 43210-1173; james@astronomy.ohio-state.edu,
andrey@astronomy.ohio-state.edu, dhw@astronomy.ohio-state.edu

Received 2000 February 9; accepted 2000 March 24

ABSTRACT

Mon. Not. R. Astron. Soc. **333**, 177–190 (2002)

The effects of photoionization on galaxy formation – II. Satellite galaxies in the Local Group

A. J. Benson,^{1★} C. S. Frenk,² C. G. Lacey,³ C. M. Baugh² and S. Cole²

¹California Institute of Technology, MC 105-24, Pasadena, CA 91125, USA

²Physics Department, University of Durham, Durham DH1 3LE

³SISSA, Astrophysics Sector, via Beirut 2-4, 34014 Trieste, Italy

Accepted 2002 February 2. Received 2002 January 30; in original form 2001 August 13

282 citations

ABSTRACT

We use a self-consistent model of galaxy formation and the evolution of the intergalactic medium to study the effects of the reionization of the Universe at high redshift on the

Dark matter

VIRG

APOSTLE
EAGLE full
hydro
simulations

Local Group

CDM

Sawala et al '16



Stars

VIRG

APOSTLE
EAGLE full
hydro
simulations

Local Group

Stars

Far fewer satellite galaxies than CDM halos

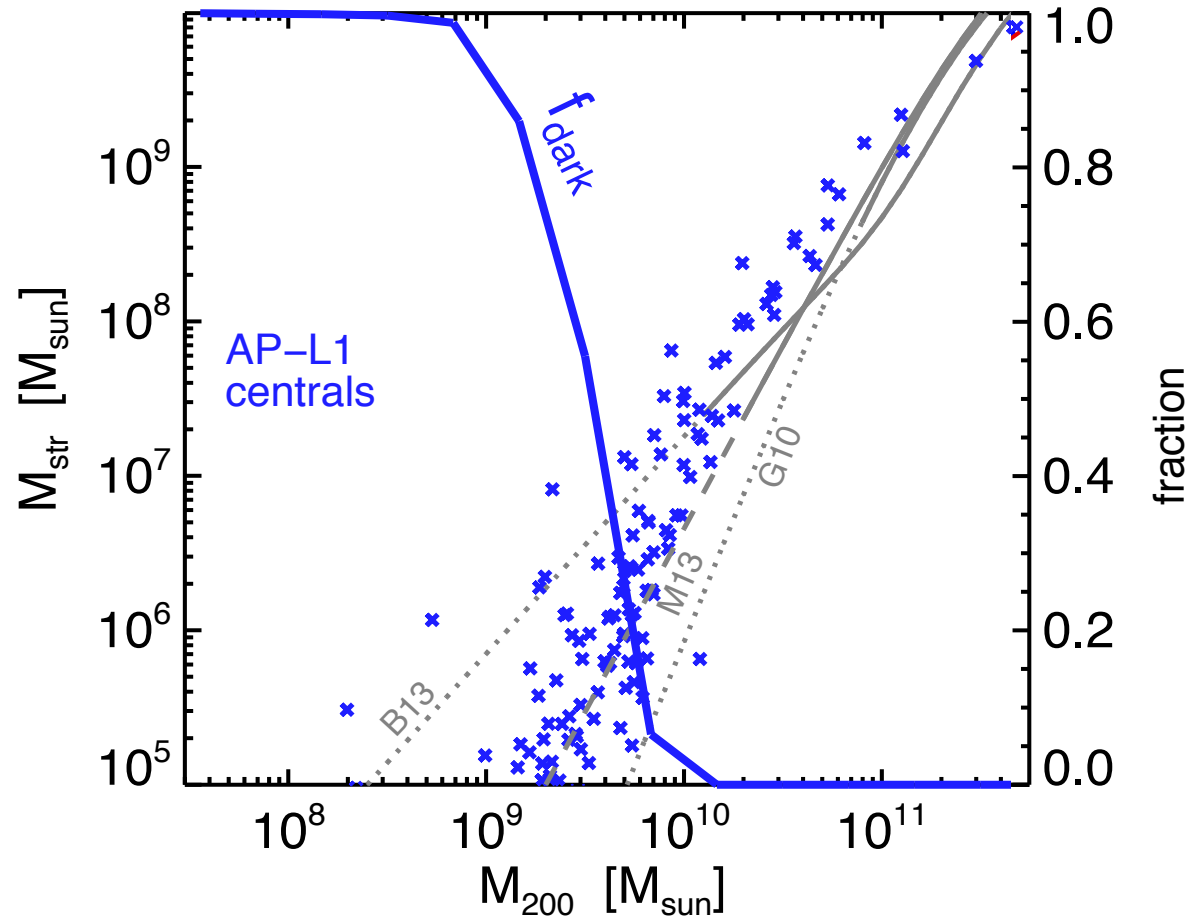
Sawala et al '16



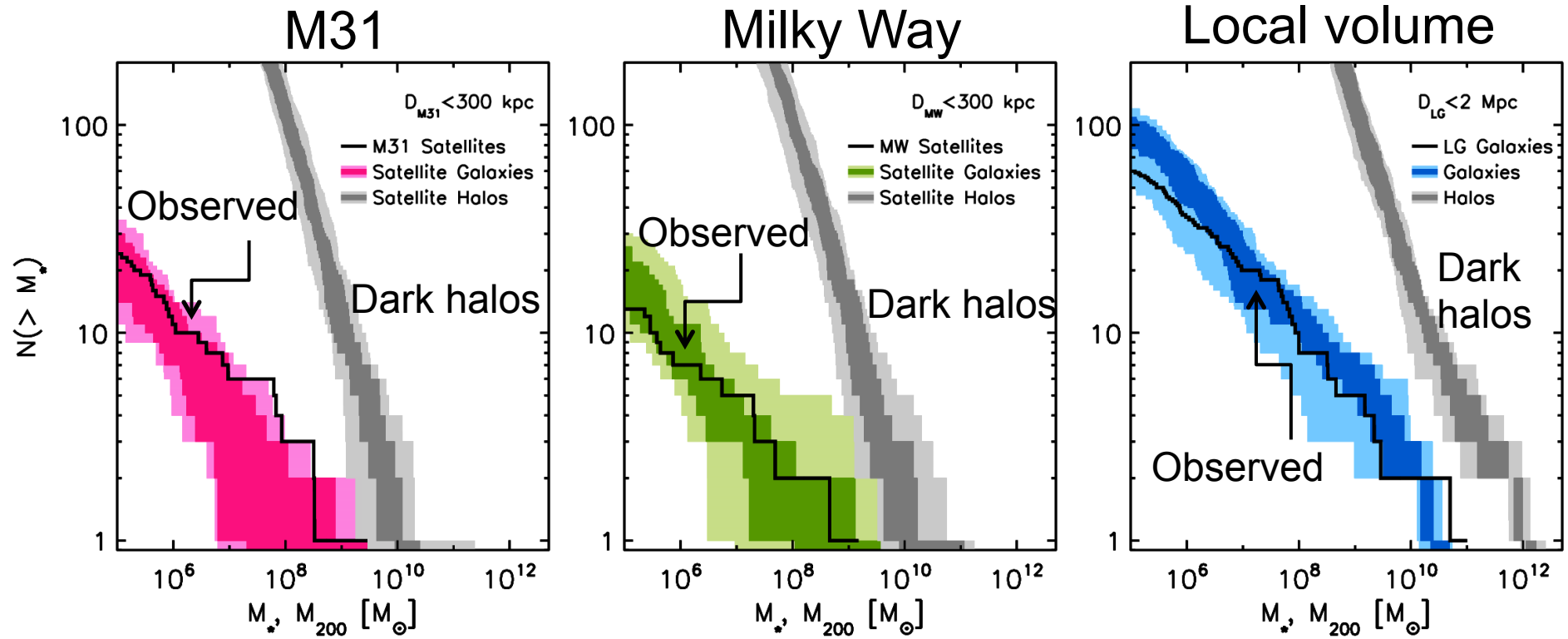
Fraction of dark subhalos

$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$



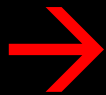
All halos of mass $< 5 \times 10^8 M_\odot$ or $V_{\max} < 7 \text{ km/s}$ are dark ($m_* < 10^4 M_\odot$)



When “baryon effects” are
taken into account



Observed abundance of satellites
is compatible with CDM



There is **no** such thing as the
“satellite problem” in CDM!

The CDM small-scale “crisis”

Three “problems:”

- ~~1. The “missing satellites” problem~~
2. The “too-big-to-fail” problem
3. The “core-cusp” problem

$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$

“Too-big-to-fail” problem in CDM:

N-body CDM sims produce too many massive subhalos
(e.g. >10 with $V_{\max} > 30$ km/s)

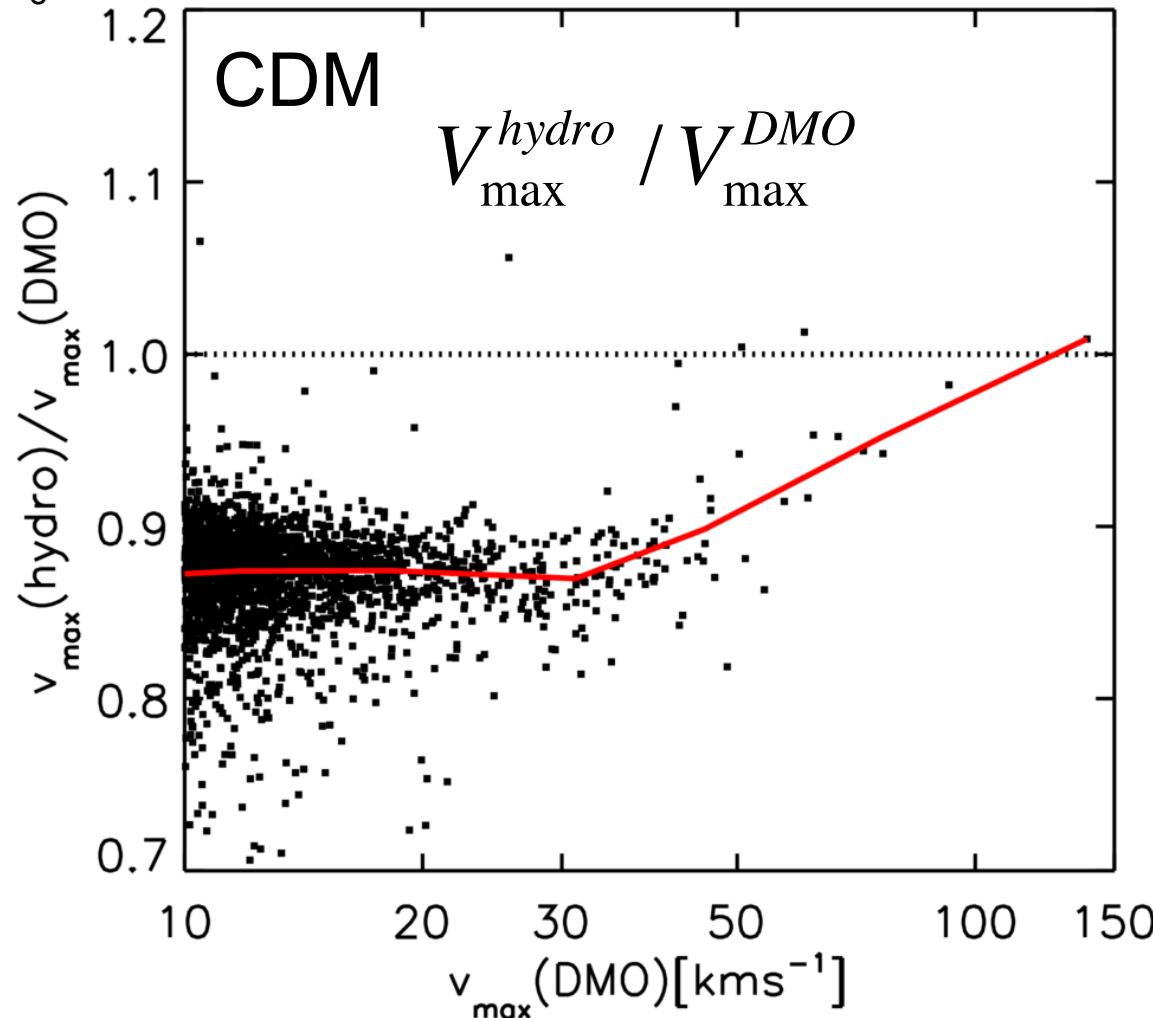
BUT: Milky Way has only 3 sats with $V_{\max} > 30$ km/s

Why did the big subhalos
not make a galaxy?

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

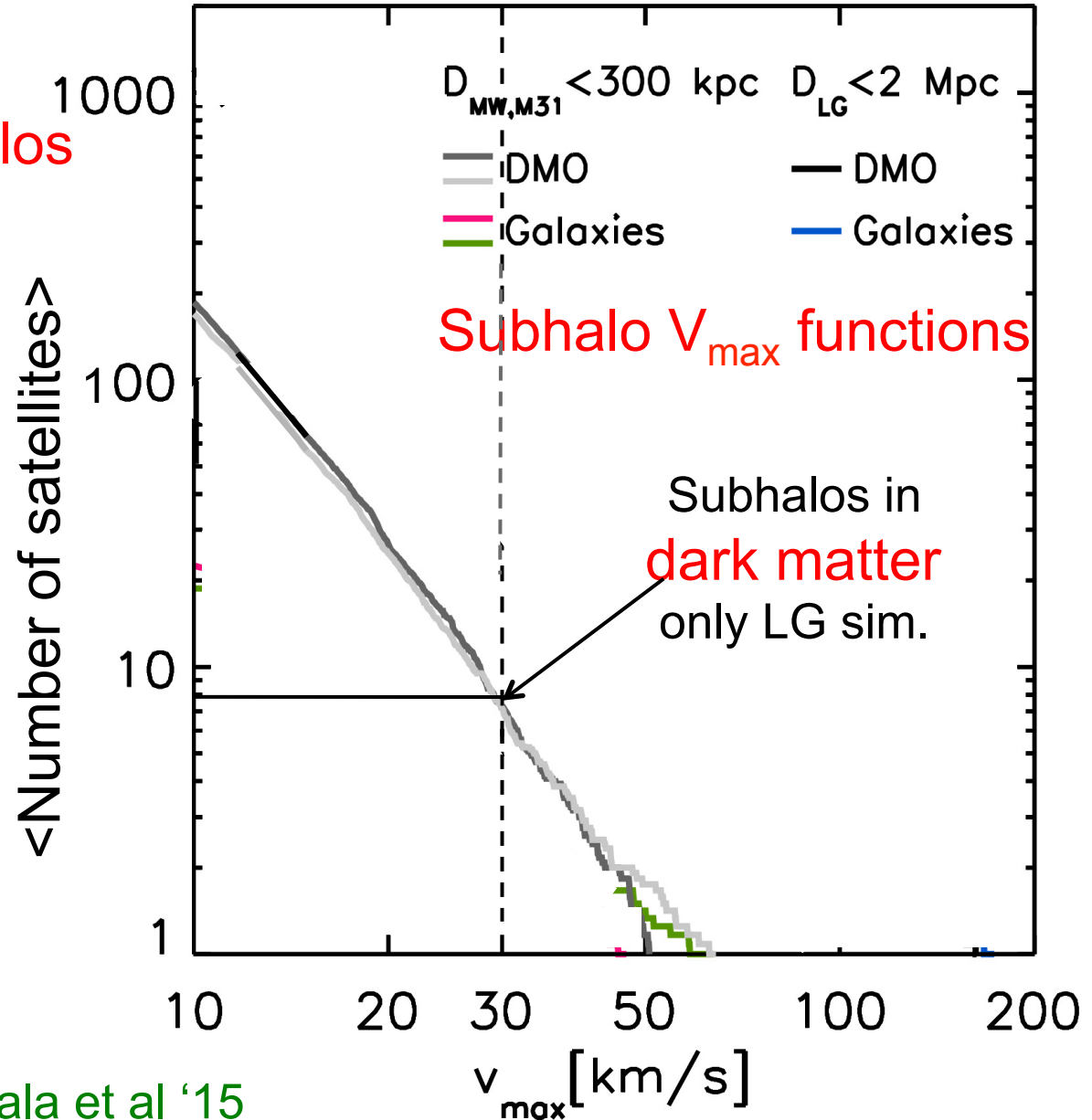
Reduction in V_{\max} due to SN feedback:

→ Lowers halo mass & thus halo growth rate



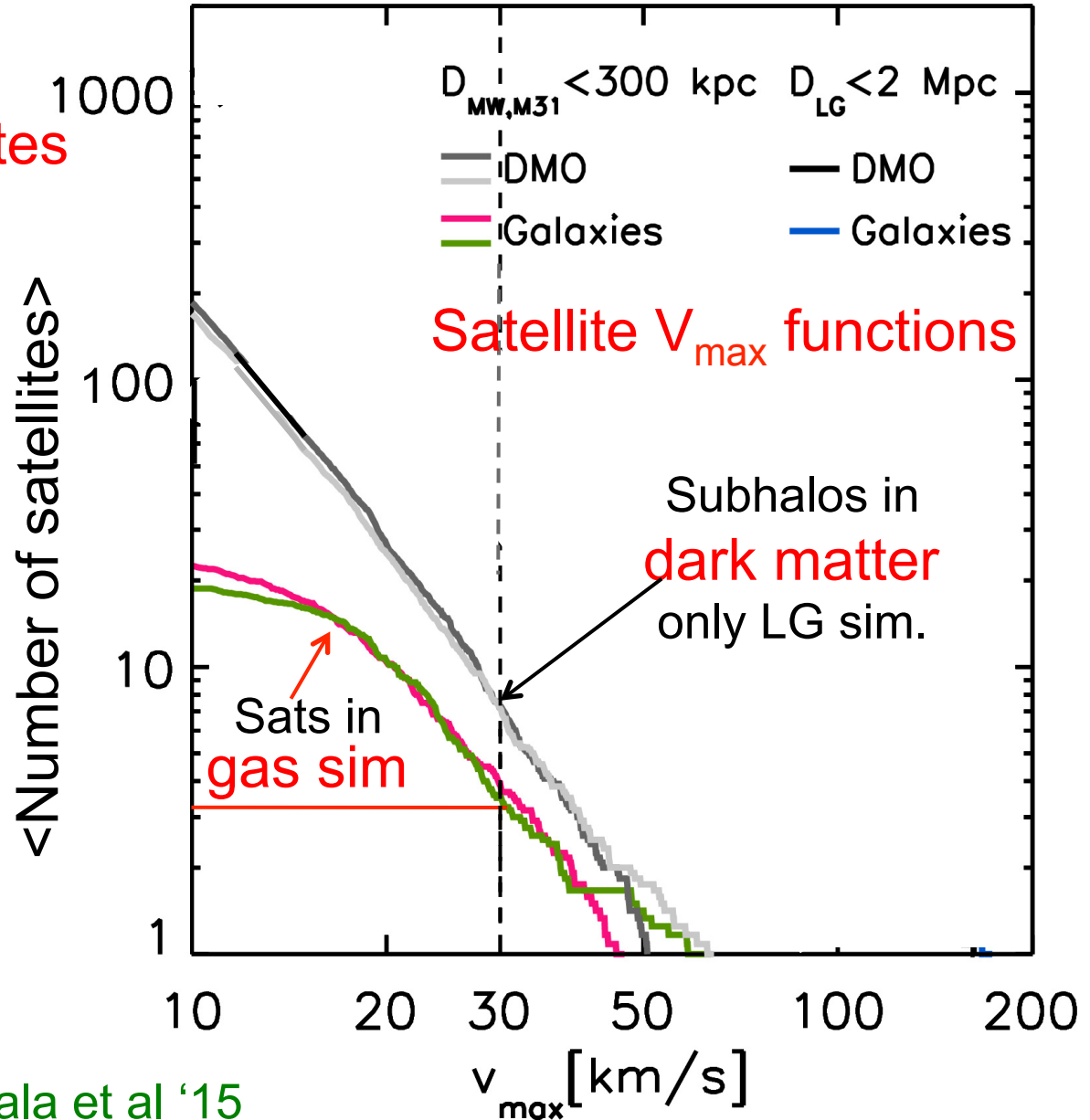
Too-big-to-fail: the baryon bailout

DM only sims \rightarrow **~ 10 halos**
 with $V_{\max} > 30$ km/s



Too-big-to-fail: the baryon bailout

Hydro sims \rightarrow **~ 3 satellites**
with $V_{\max} > 30$ km/s





When “baryon effects” are
taken into account



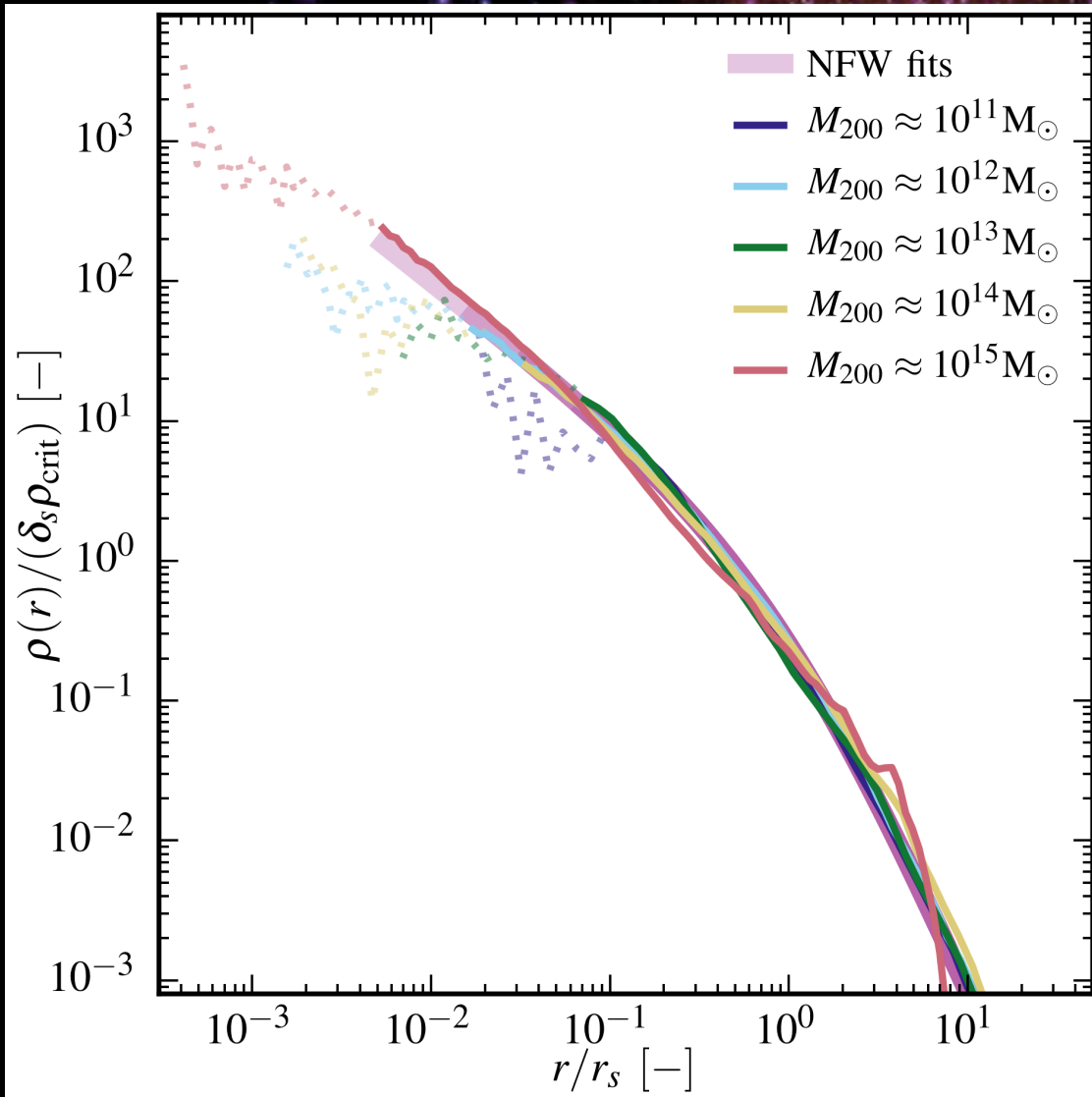
No too-big-to-fail **problem** in CDM

The CDM small-scale “crisis”

Three “problems:”

- ~~1. The “missing satellites” problem~~
- ~~2. The “too-big-to fail” problem~~
3. The “core-cusp” problem

The Density Profile of Cold Dark Matter Halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

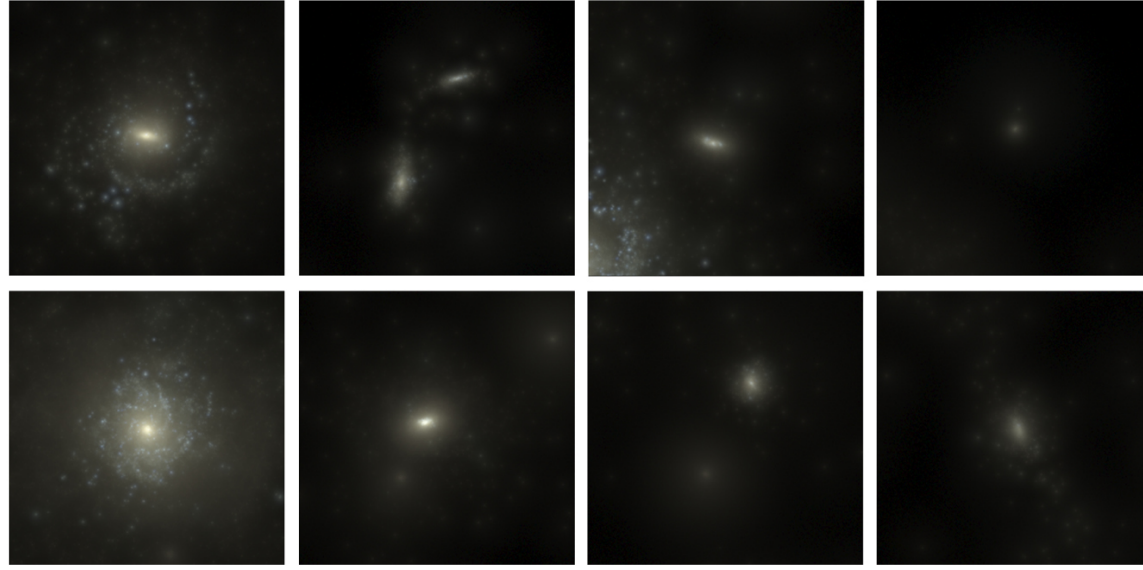
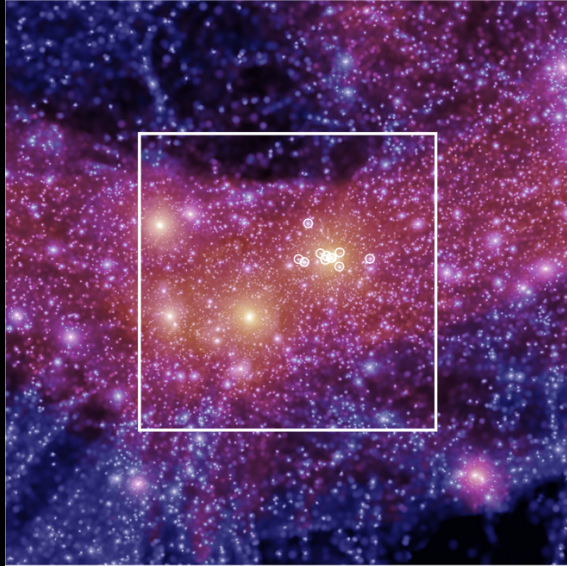
Density profiles are “cuspy” -
no ‘core’ near the centre

Fitted by simple formula:

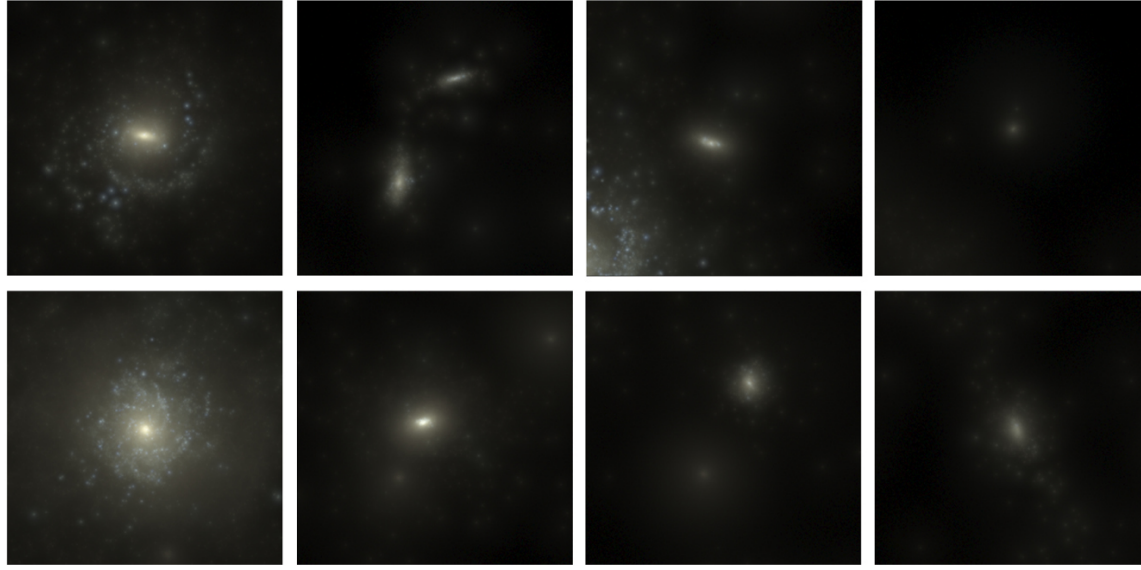
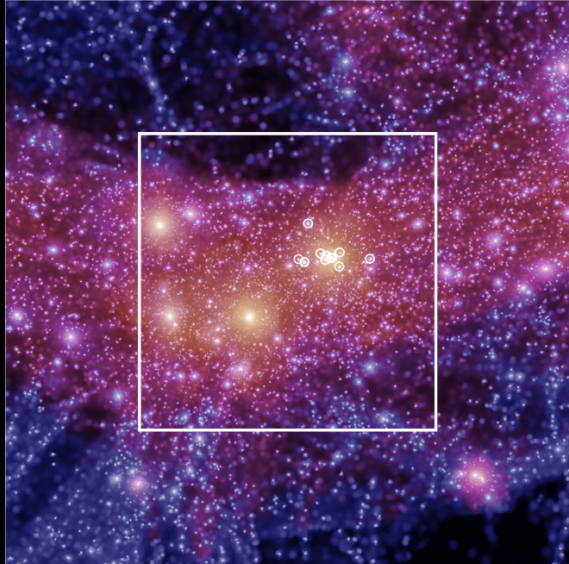
$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

More massive halos and
halos that form earlier have
higher densities (bigger δ)



EAGLE/Apostle/
Auriga galaxies have
NFW cusps



Does Nature have them?





But if cores were found in halos, would
this rule out CDM ?

The physics of core formation

Cusps → cores

Perturb central halo region
by growing a galaxy
adiabatically and removing
it **suddenly** (Navarro, Eke
& Frenk '96)

Cores may also form by
repeated fluctuations in
central potential (e.g. by
SN explosions) (Read &
Gilmore '05; Pontzen &
Governato '12,'14; Bullock &
Boylan-Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

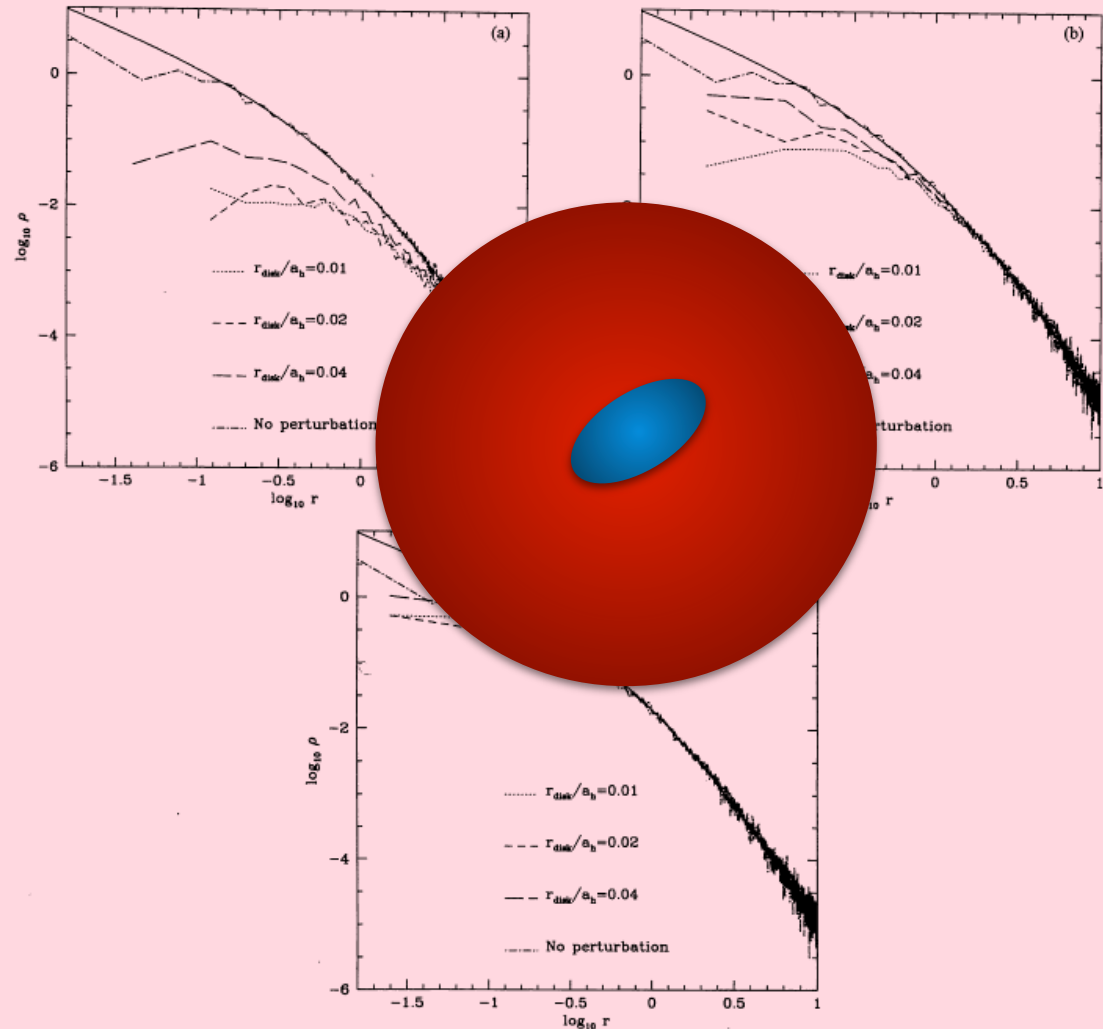


Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at $t = 200$. (a) $M_{\text{disc}} = 0.2$. (b) $M_{\text{disc}} = 0.1$. (c) $M_{\text{disc}} = 0.05$.

In the absence of a treatment of the (multi-phase) interstellar medium, need a “subgrid” model for star formation

In Eagle stars form from (cooling) gas that reaches a density higher than ρ_{th} (and $T \sim 10^4$ K)

In Eagle $\rho_{\text{th}} \sim 0.1 \text{ cm}^{-3}$

For each resimulated dwarf, vary ρ_{th} from $0.1 - 10^4 \text{ cm}^{-3}$

Physically meaningless

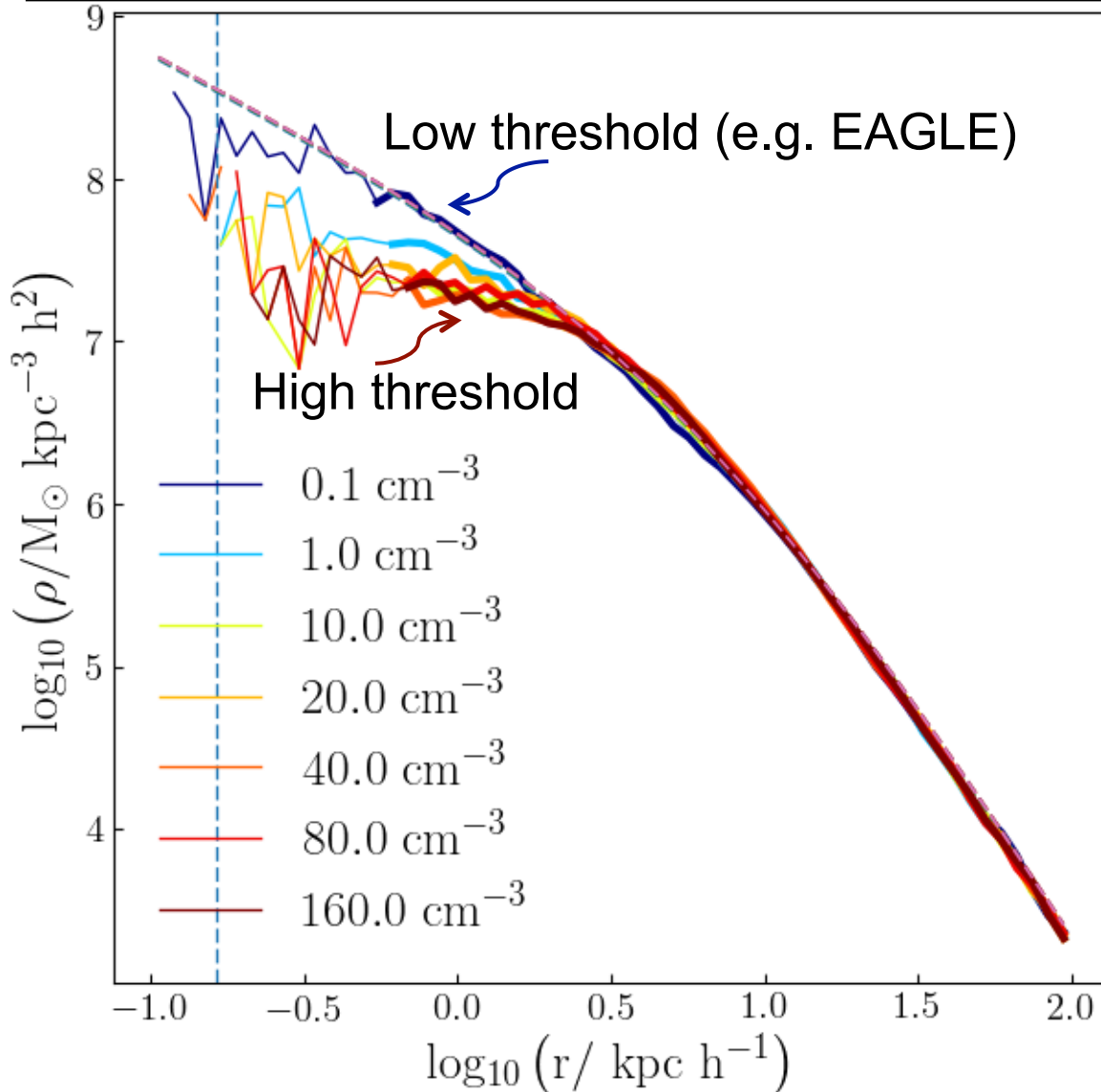
Cores or cusps in simulations?

Key parameter: gas density threshold for star formation

High density → NEF mechanism

Low density → not enough central gas density to perturb DM

Cores or cusps in simulations?



The CDM small-scale “crisis”

Three “problems:”

- ~~1. The “missing satellites” problem~~
- ~~2. The “too-big-to fail” problem~~
- ~~3. The “core-cusp” problem~~

The mass discrepancy-acceleration relation (MDAR)

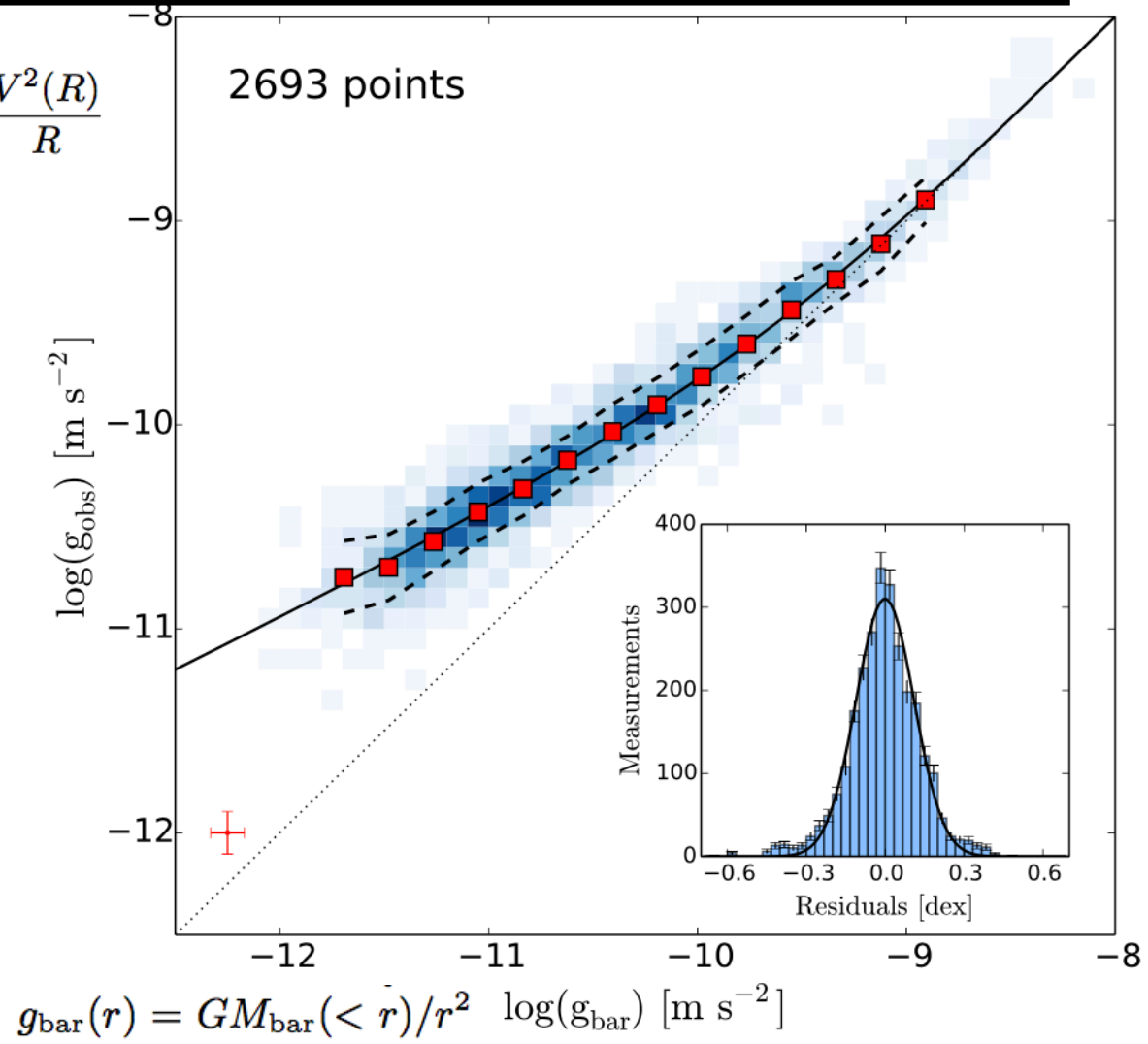
Relatively small scatter

Two characteristic accelerations:

$a_0 \sim 10^{-10} \text{ m/s}^2$: above which there is little need for dark matter, and

$a_{\text{min}} \sim 10^{-11} \text{ m/s}^2$: a “minimum” acceleration probed by galaxies

$$g_{\text{obs}} = \frac{V^2(R)}{R}$$



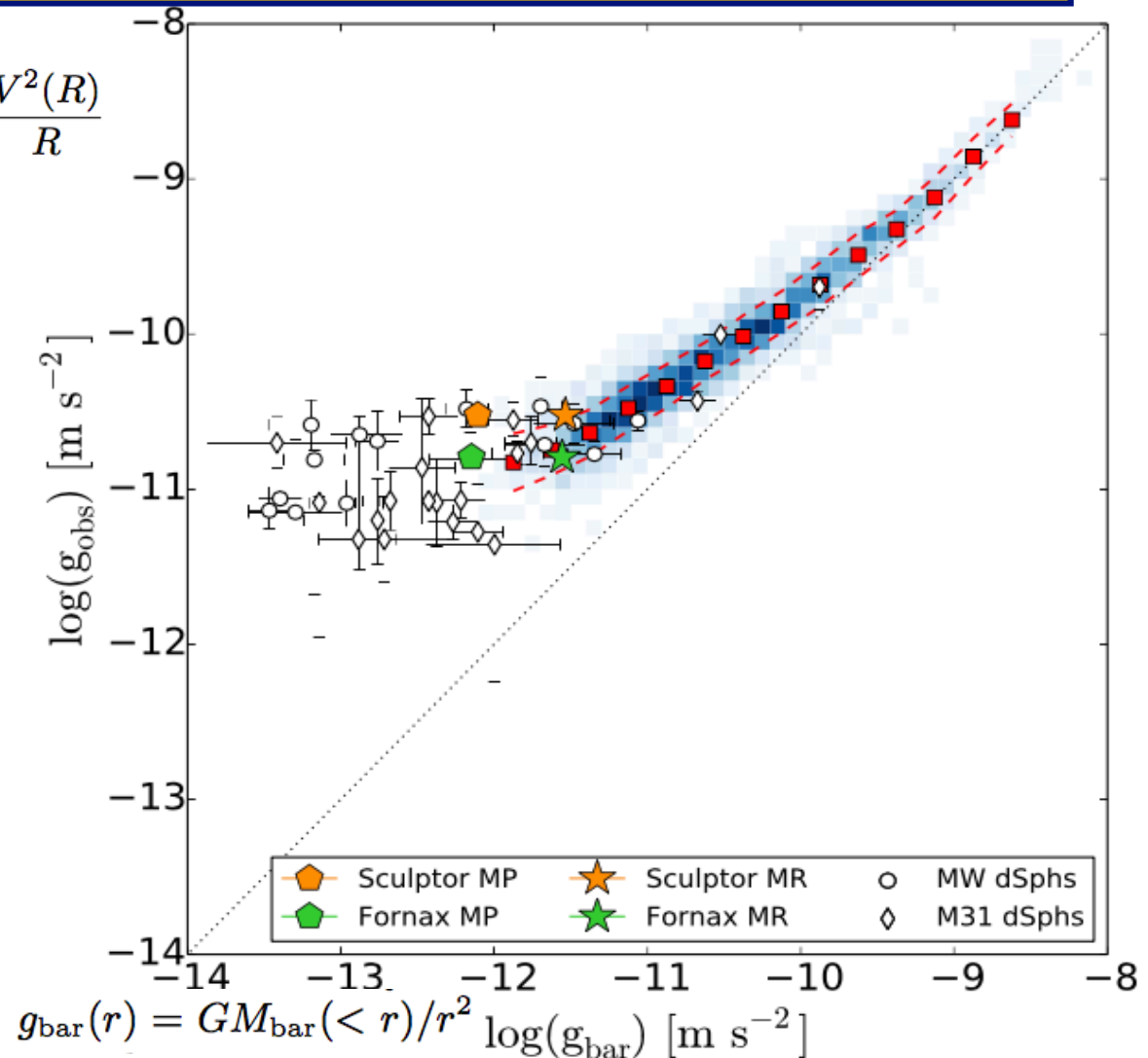
The mass discrepancy-acceleration relation (MDAR)

$$g_{\text{obs}} = \frac{V^2(R)}{R}$$

Two characteristic accelerations:

$a_0 \sim 10^{-10} \text{ m/s}^2$: above which there is little need for dark matter, and

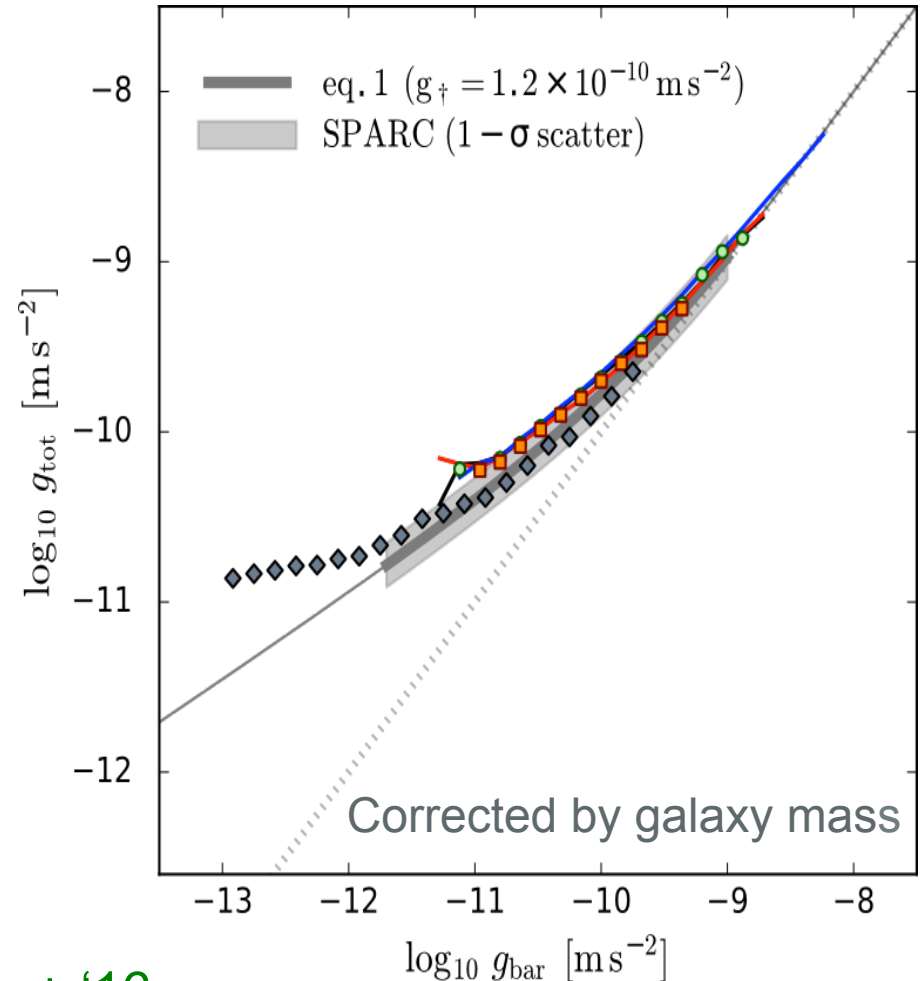
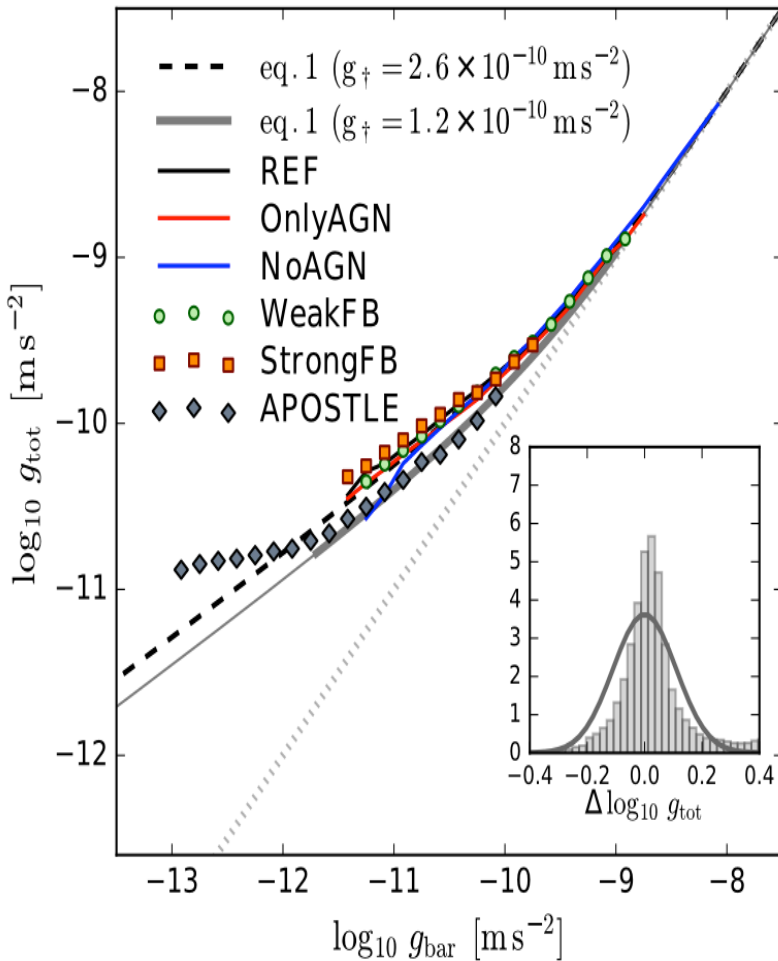
$a_{\text{min}} \sim 10^{-11} \text{ m/s}^2$: a “minimum” acceleration probed by galaxies



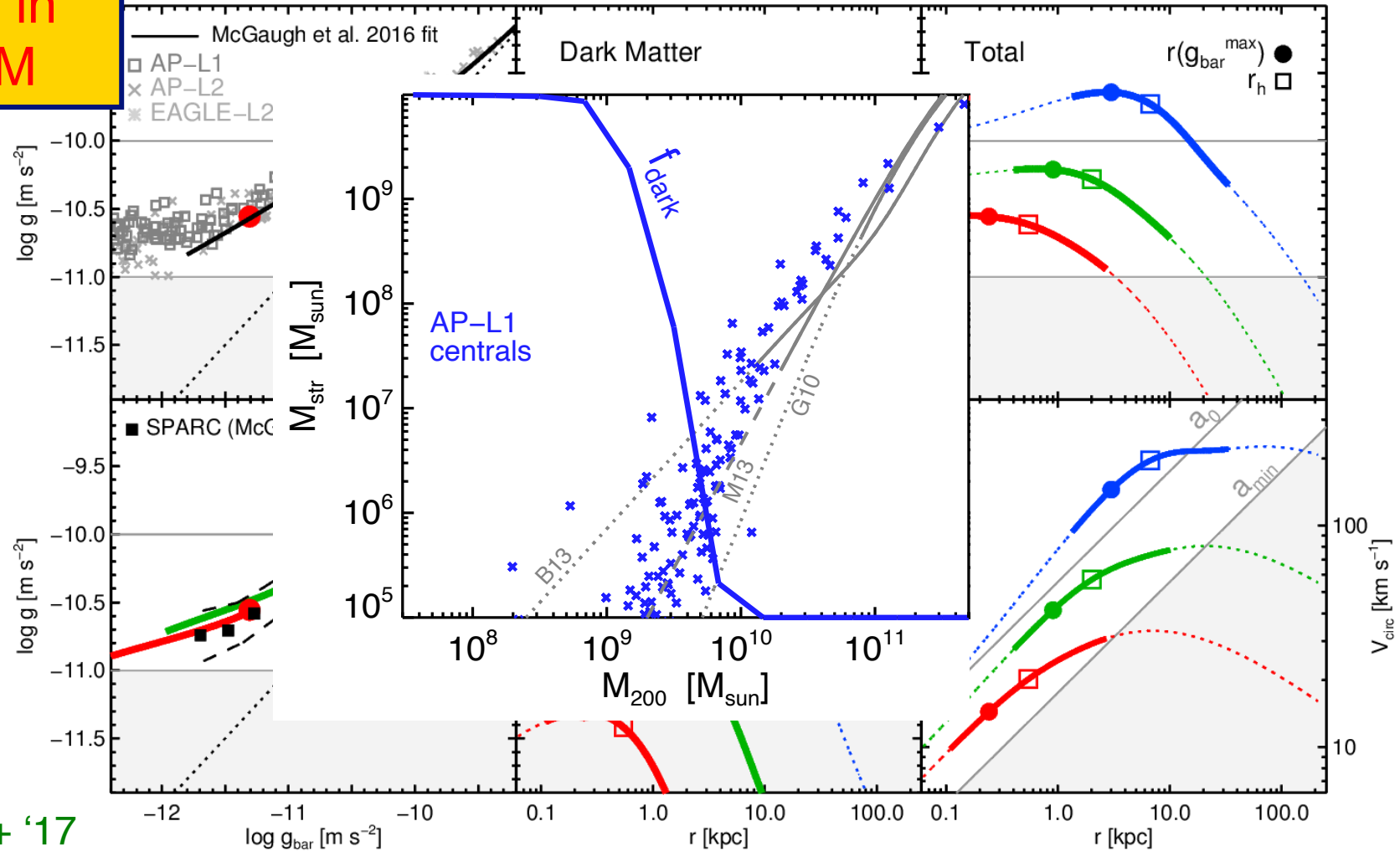
Lelli+17

MDAR in Eagle

Different subgrid physics models: M_* varies by x4 in same halo, but MDAR hardly changes



MDAR in Λ CDM



Navarro + '17

Λ CDM halos have a well-defined maximum central acceleration
 $a_0 \sim 10^{-10} \text{ m/s}^2$ is the central acceleration of the most massive halo that may host a disk galaxy ($V_{\text{max}} \sim 200\text{-}300 \text{ km/s}$)
 $a_{\text{min}} \sim 10^{-11} \text{ m/s}^2$ is the acceleration of the least massive halo able to host a luminous galaxy ($V_{\text{max}} \sim 20\text{-}30 \text{ km/s}$)

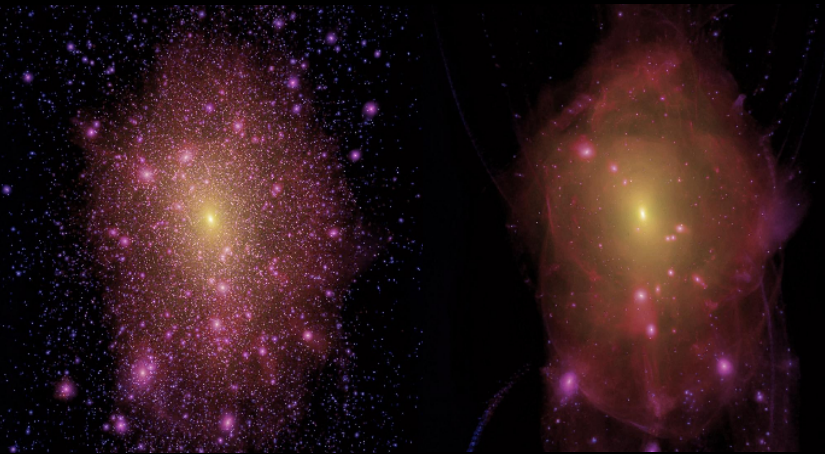


Can CDM be ruled out?

Yes !



The subhalo mass function

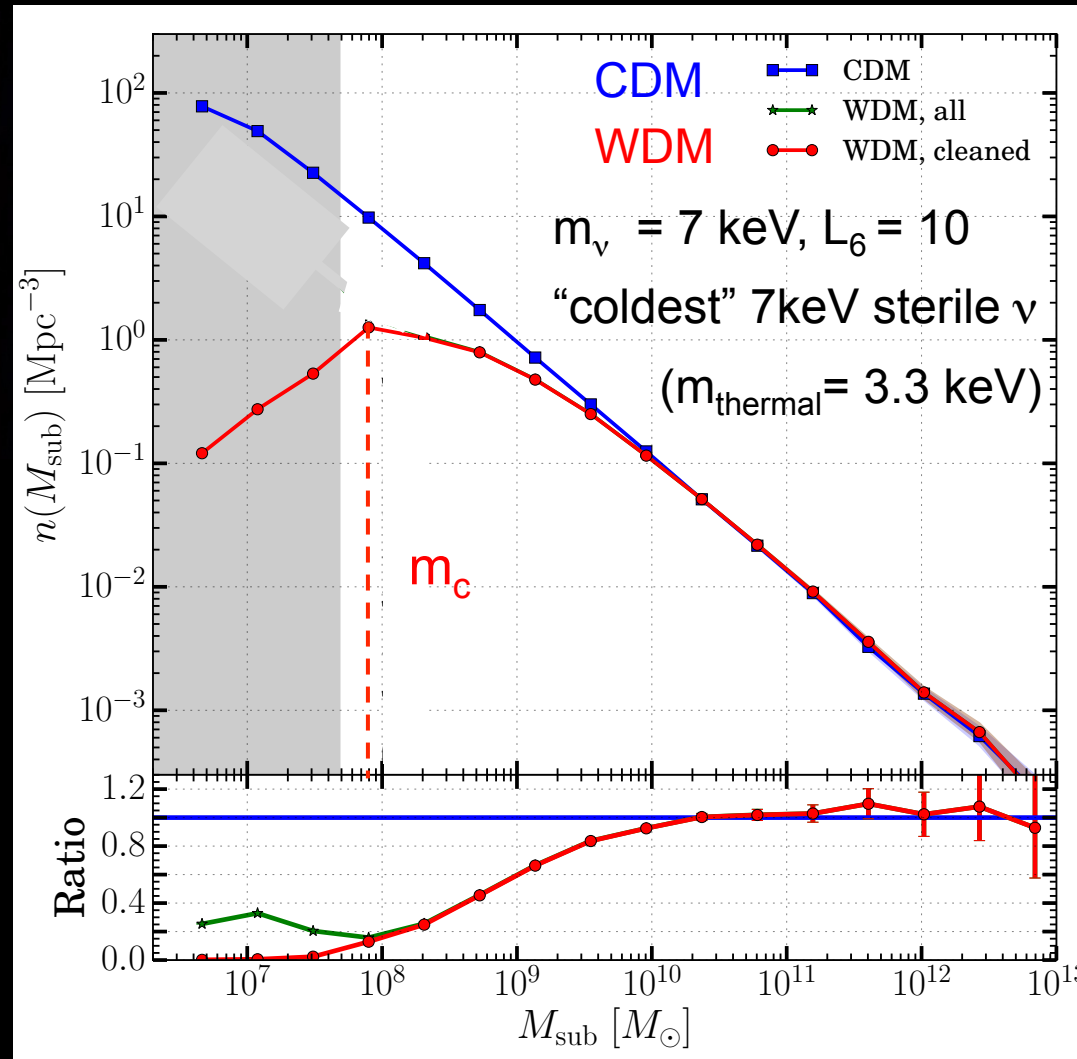


CDM

WDM

3 x fewer WDM subhalos at $3 \times 10^9 M_\odot$

10 x fewer at $10^8 M_\odot$





Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

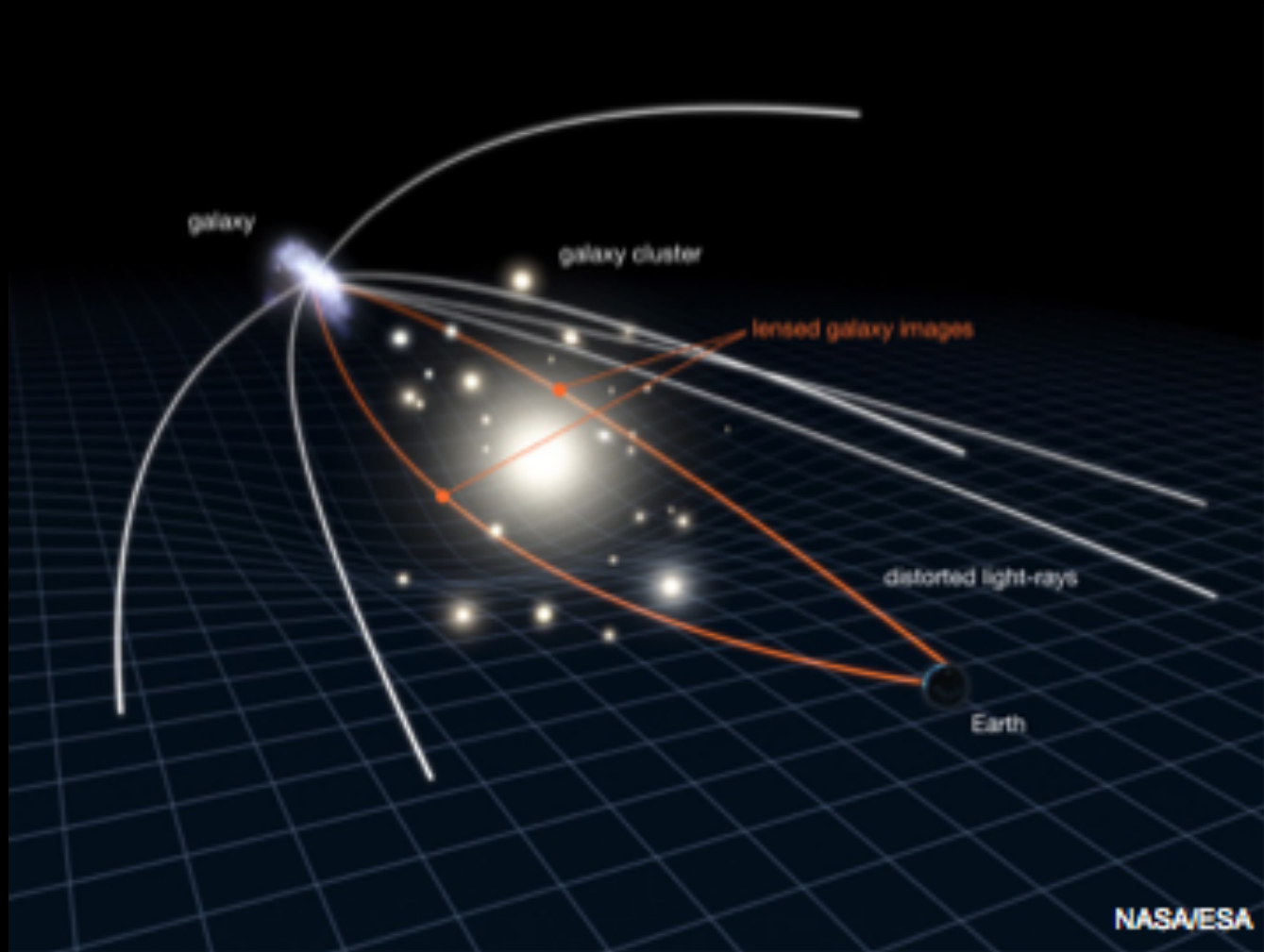
Dark halos can be detected through
gravitational lensing



Gravitational lensing: Einstein rings

How to rule out CDM

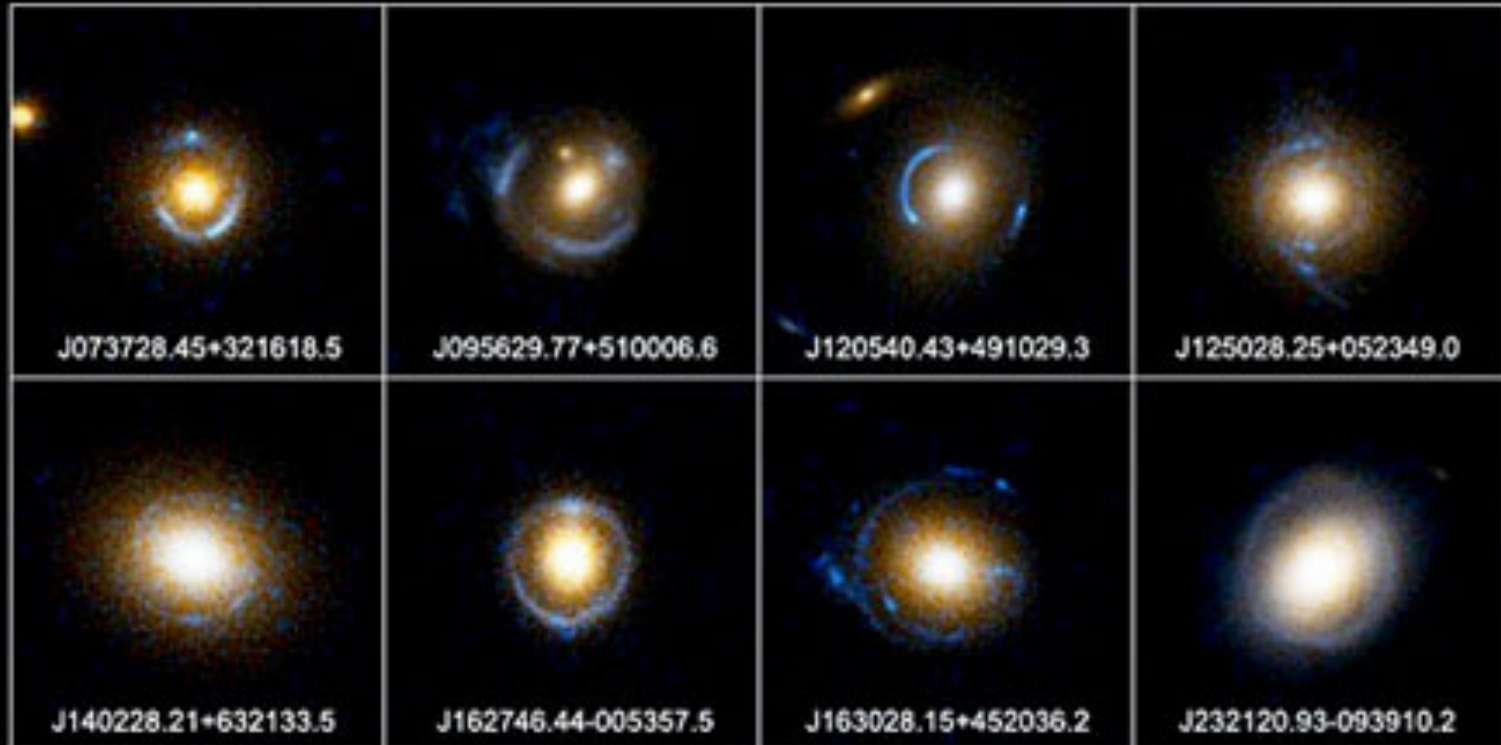
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Einstein Ring Gravitational Lenses

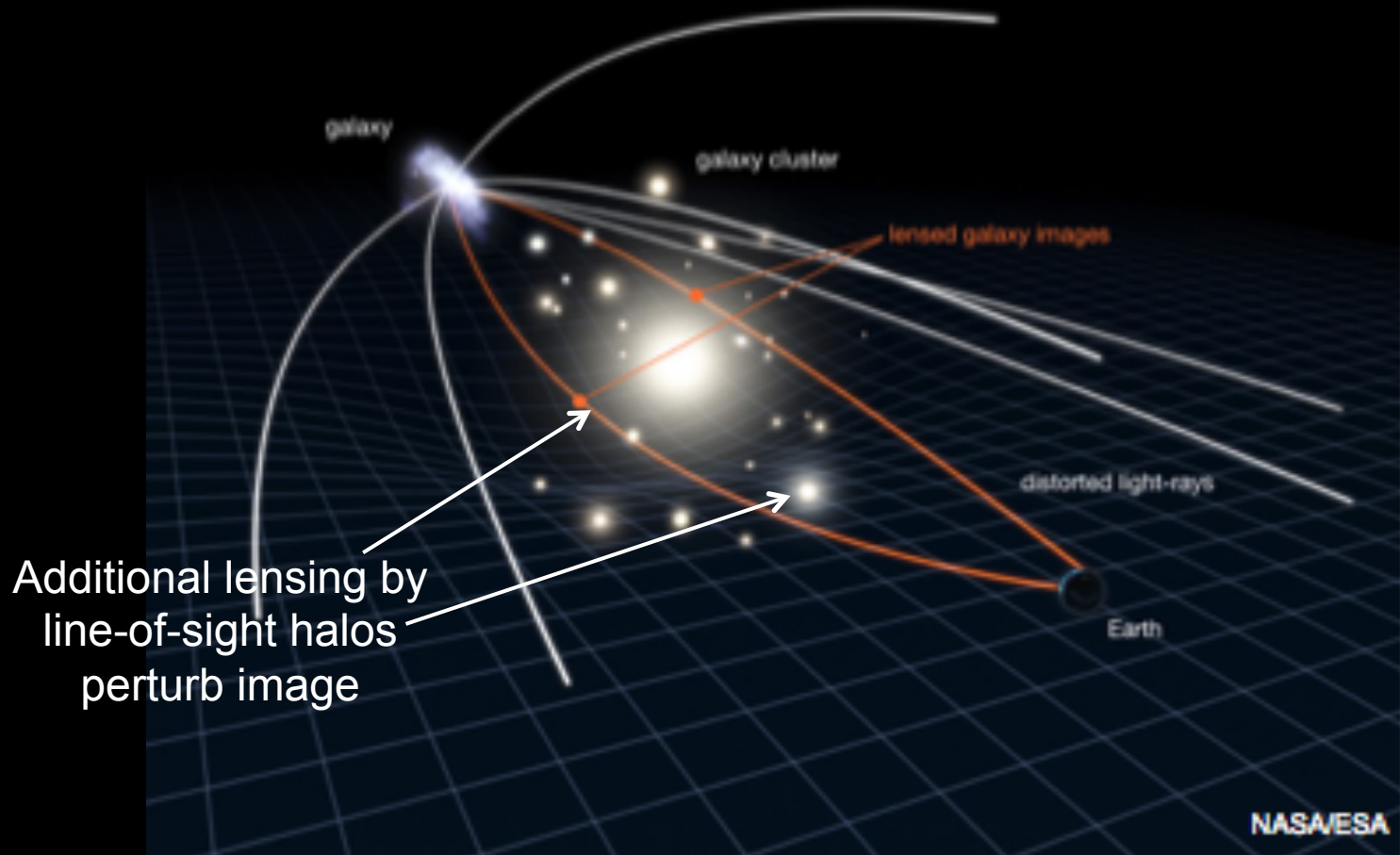
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

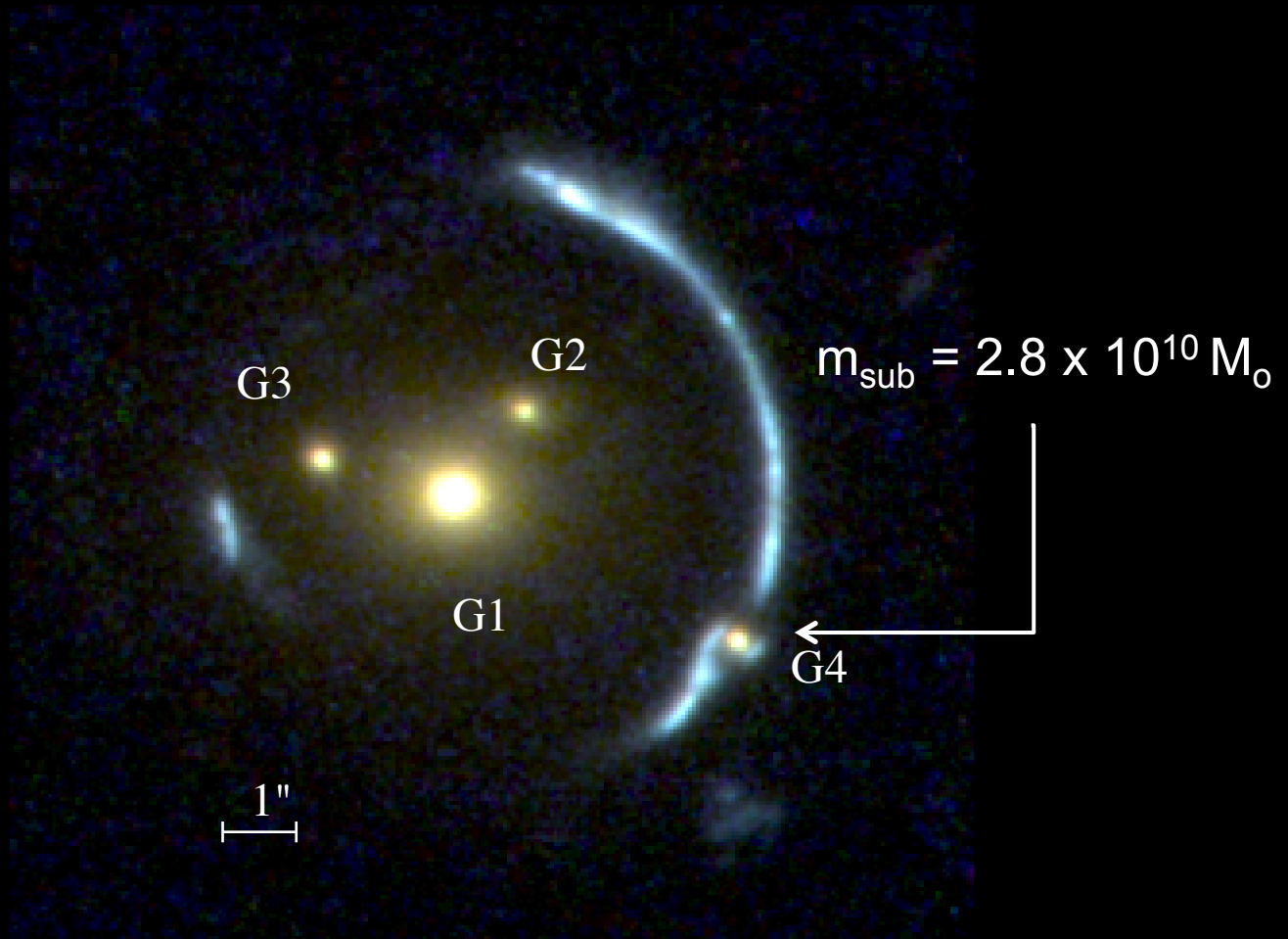
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image

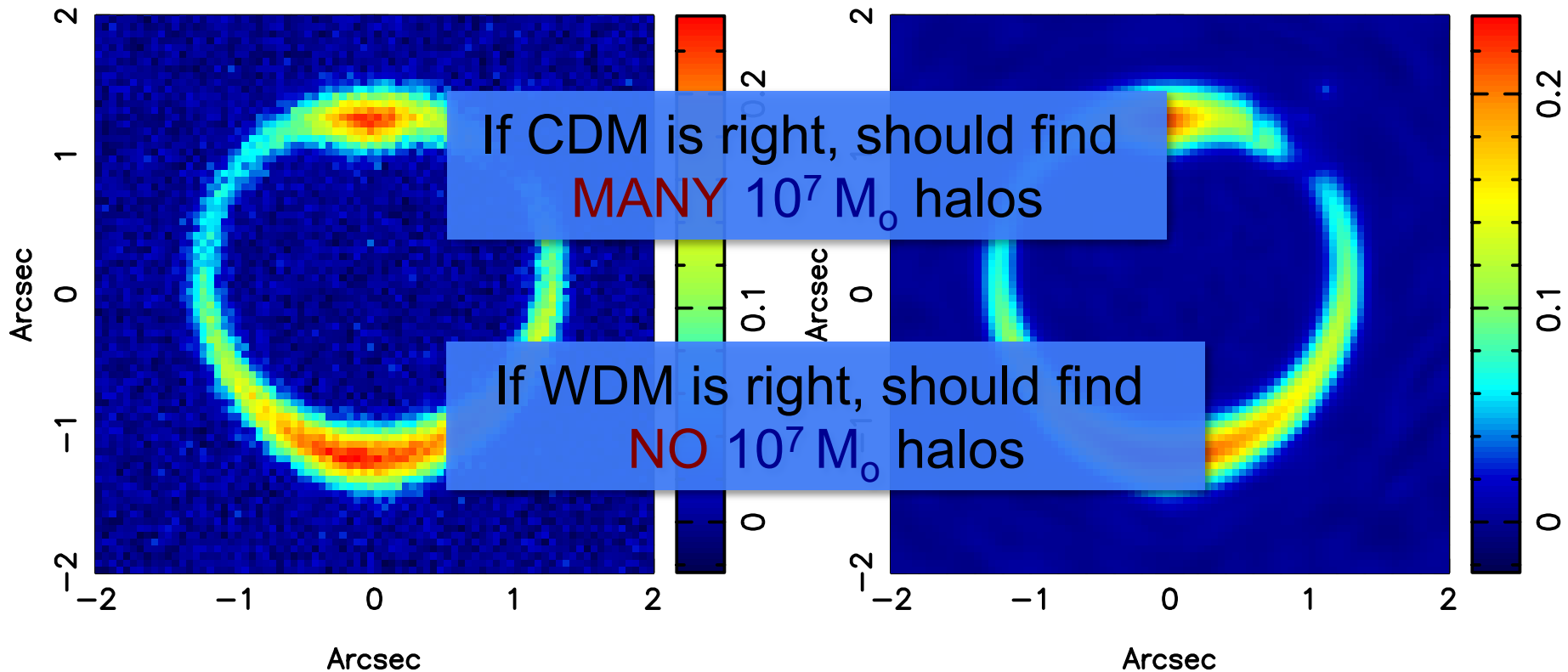


Detecting substructures with strong lensing

Can detect subhalos as small as $10^7 - 10^8 M_\odot$

Data

Model



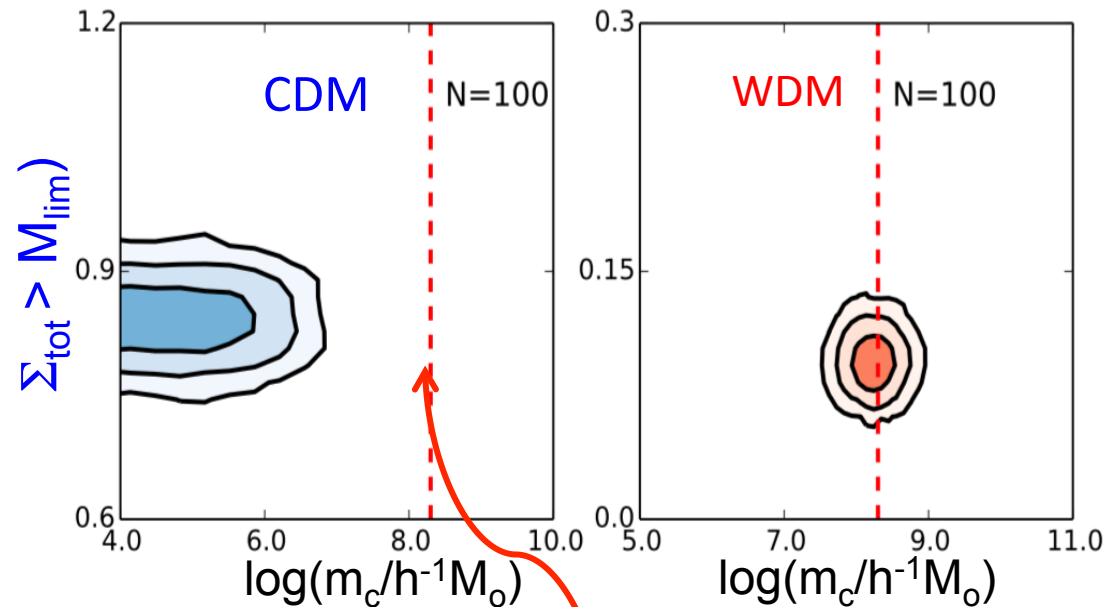
Detecting substructures with strong lensing

Σ_{tot} = projected halo number density within Einstein ring

m_c = halo cutoff mass

100 Einstein ring systems and detection limit: $m_{\text{low}} = 10^7 h^{-1} M_\odot$

Detection limit = $10^7 h^{-1} M_\odot$



m_c = halo cutoff mass

$m_c = 1.3 \times 10^8 h^{-1} M_\odot$ for coldest 7 keV sterile neutrino

- If DM is 7 keV sterile $\nu \rightarrow$ **exclude** CDM at $\gg \sigma$!
- If DM is CDM \rightarrow **exclude** 7 keV sterile ν at $\gg \sigma$



Conclusions

- Λ CDM:
- Fully-specified **physical** model with **predictive** power
- Important predictions (CMB, LSS, gal form) **verified** empirically
- One of the great **successes** of physics of past 30 years

CDM small-scale “crisis”:

- Halos $< \sim 5 \cdot 10^8 M_0$ are dark; halos $> 10^{10} M_0$ are bright
- When **baryons** taken into account \rightarrow **No satellite, too-big-to-fail, plane of sats, core/cusp** problems in CDM
- Distortions of **strong** gravitational **lenses** offer **clean test** of CDM
 \rightarrow and can potentially **rule it out!**