



# Type Ia Supernovae

Astrophysical Seminar

KITP Santa Barbara, 27 January 2005

Friedrich Röpke,

Max-Planck-Institut für Astrophysik, Garching

W. Hillebrandt, M. Gieseler, M. Reinecke, C. Travaglio,

L. Iapichino, M. Stehle





# The challenge

## 1. Cosmology

- ▶ new cosmological standard picture initiated by SN Ia measurements
- ▶ undone homework to SN Ia community: explain peak luminosity-light curve shape relation used to calibrate cosmological distance measurements
  
- ▶ next step: can dark energy equation of state be constrained by SN Ia observations?
- ▶ **No, unless we can control the systematics.**
- ▶ only way to get a handle on the systematics: modeling from "first principles" (→ 3d necessary) in conjunction with high quality observations of nearby objects



## 2. Observations of nearby objects

- ▶ over past years reached quality so that it is possible to constrain/discriminate between models  
(MPA contribution via European Research Training Network) → especially spectroscopic data
- ▶ **3 examples:**

Example 1: Late time (nebular) spectra (Kozma et al., in prep.)

- ▶ look into the center of the explosion products → hints for explosion mechanism

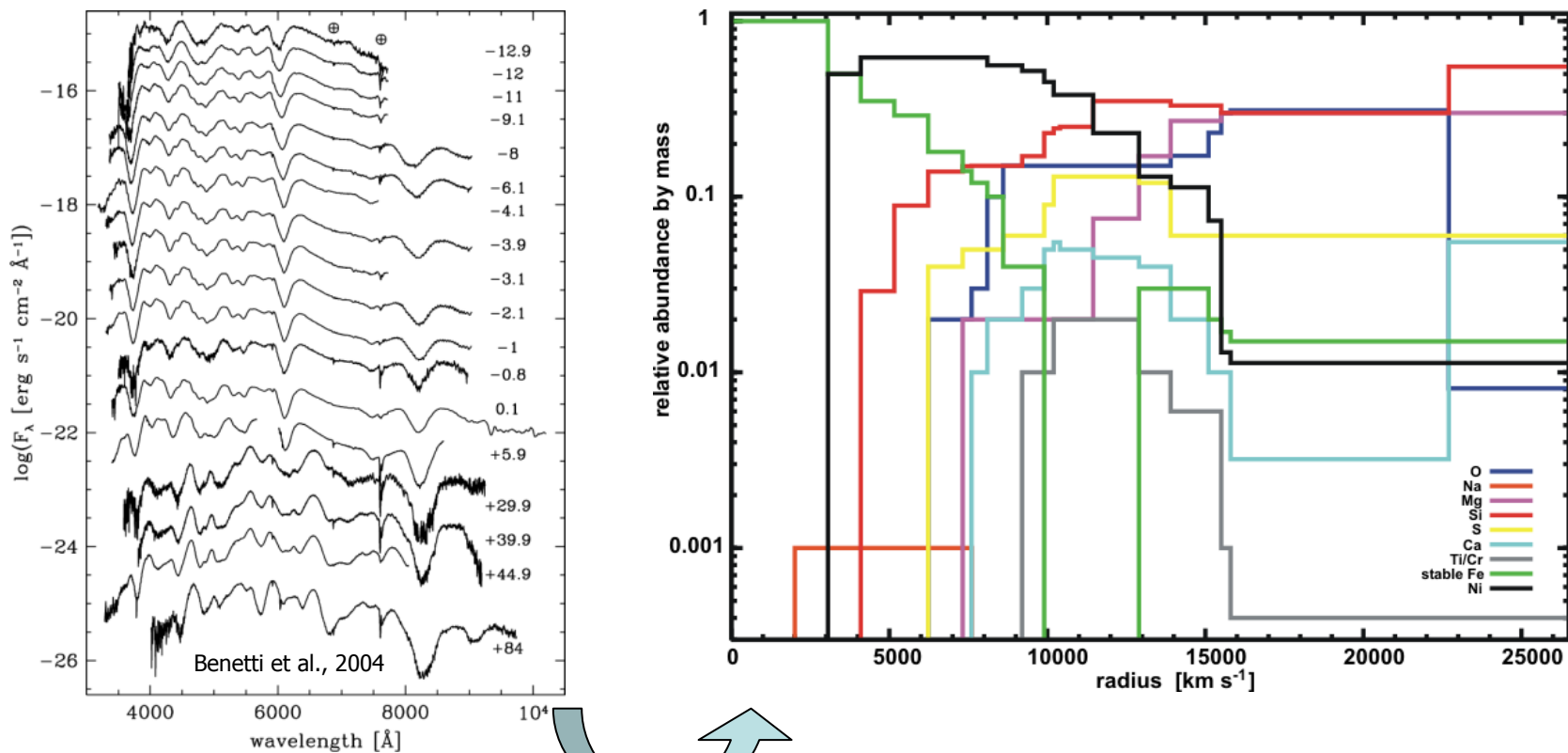
Example 2: Spectropolarimetry (e.g. Wang et al., 2004)

- ▶ provide information on multi-dimensional structure of explosion



# The challenge: nearby observations

Example 3: Abundance tomography of SN 2002bo (M. Stehle et al., 2004)



spectral modeling



# Astrophysical Scenario

- ▶ no hydrogen in the spectra
  - ▶ huge energy release ( $\sim 1$  foe)
  - ▶ uniform properties  $\rightarrow$  standard candles?
  - ▶ no compact remnant, occur in young and old populations
- $\rightarrow$  thermonuclear explosion of white dwarf star
- ▶ How can WD reach state to trigger thermonuclear explosion?

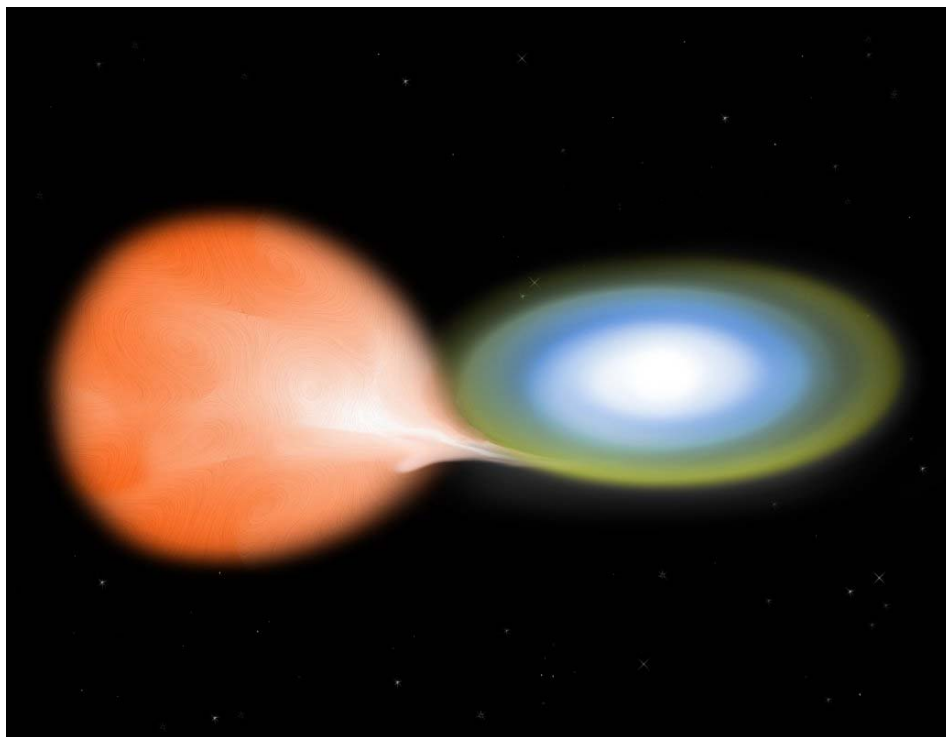
## scenarios:

- ▶ double degenerate (DD): 2 WDs merge, smaller is disrupted and accreted onto more massive companion, high rate expected, natural way to avoid hydrogen in spectra  
problem: too high accretion rate  $\rightarrow$  C-shell flash  $\rightarrow$  ONeMg WD  $\rightarrow$  collapse



# Astrophysical scenario

- ▶ single degenerate (SD): C/O WD accretes matter from non-degenerate binary companion (MS or AGB?)
  - ▶ sub-Chandrasekhar: WD composed of C/O center and He-shell, He-shell detonation converges in center, triggers detonation, high rate expected multi-d problem, nucleosynthesis not consistent with main channel
  - ▶ Chandrasekhar: accretion until WD reaches Chandrasekhar mass, candidates: supersoft sources (U Sco), cataclysmic binaries  
problem: too low rate

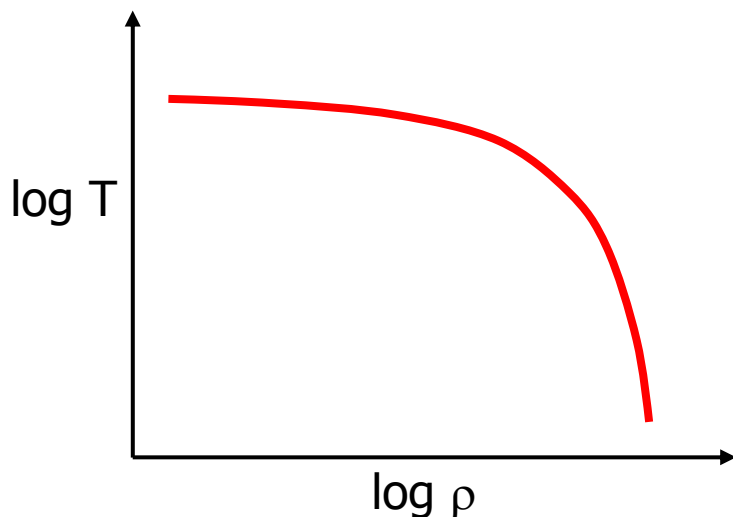




# Astrophysical scenario

## ignition

- ▶ accretion until close to  $M_{\text{Ch}}$
- ▶ densities reach values of carbon ignition



- ▶ convective burning until energy generation exceeds convective cooling
- ▶ thermonuclear runaway in small spatial region
- ▶ flame formation (central, multi-spot???)



# Astrophysical scenario

## flame propagation

- ▶ hydrodynamics: 2 modes:

### deflagration

subsonic

flame mediated by thermal  
conduction of  $e^-$

### detonation

(super)sonic

flame driven by shock waves

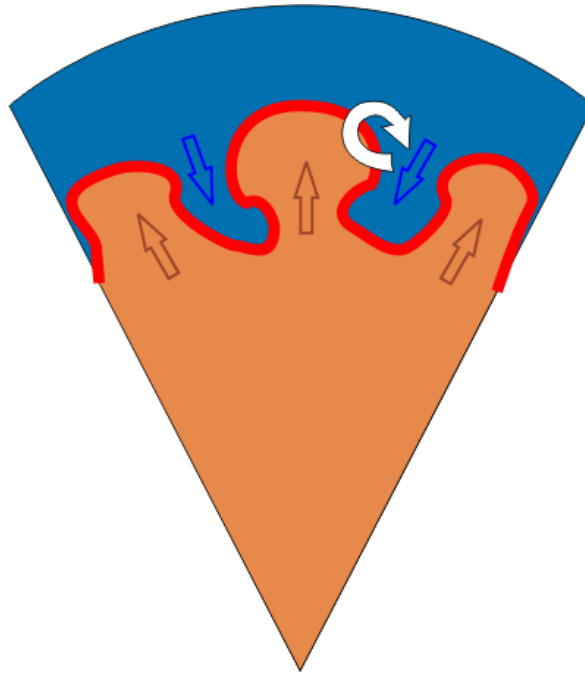
- ▶ pure detonation would produce wrong composition of explosion products (Arnett, 1969)
- ▶ flame starts out as deflagration
- ▶ problem: laminar deflagration flame too slow





# Astrophysical scenario

- ▶ interaction of flame with turbulence → **turbulent combustion**
- ▶  $Re \sim 10^{14}$  → instabilities generate turbulence

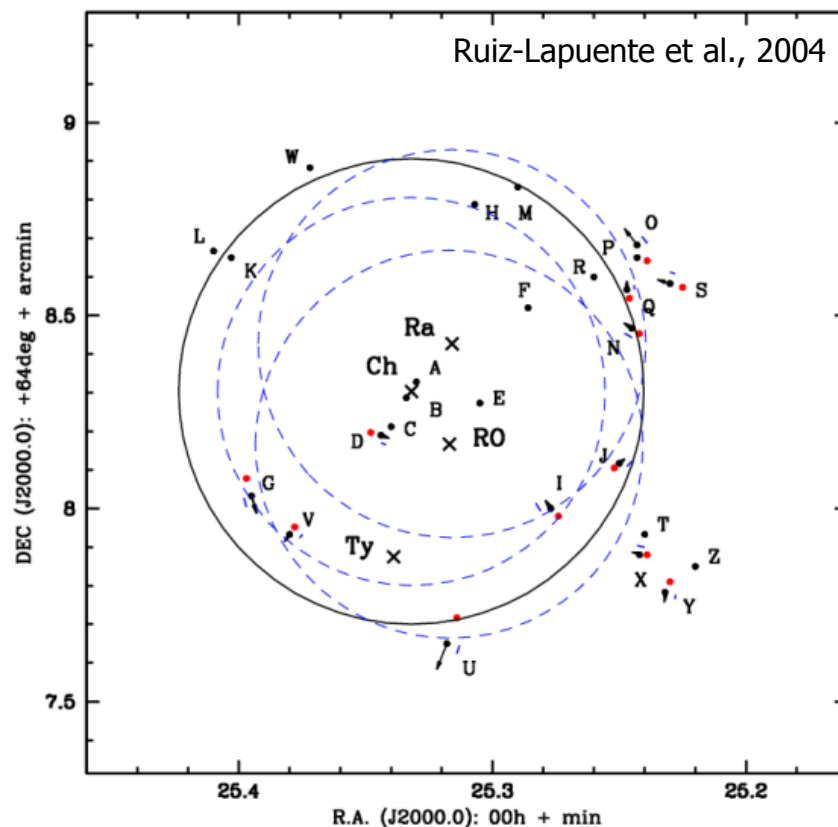
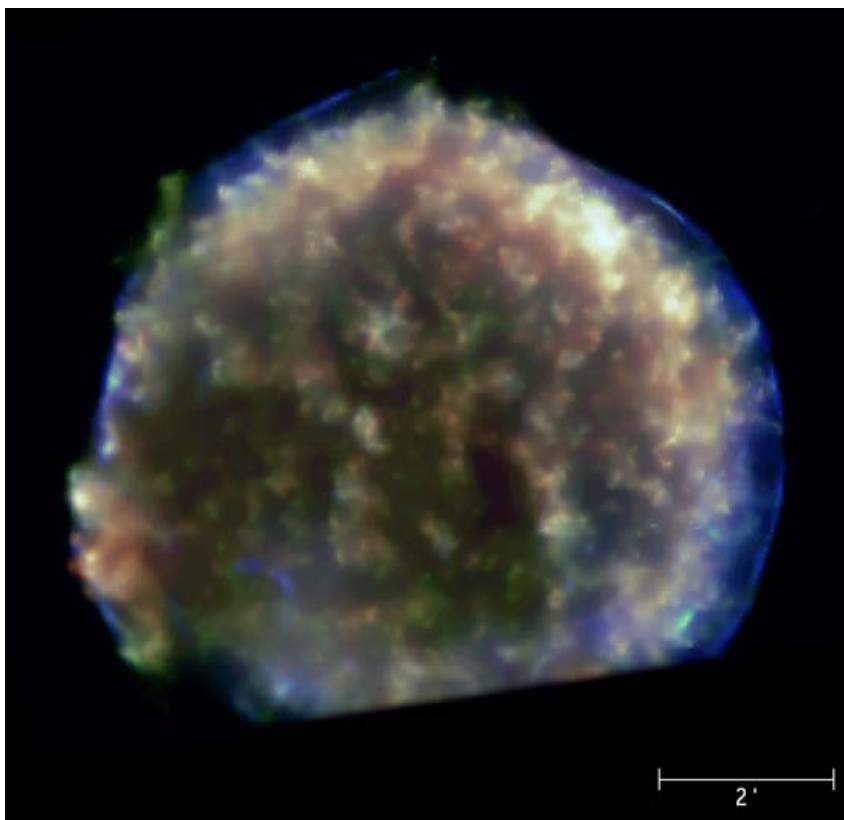


- ▶ wrinkling of the flame front → flame surface  $\uparrow$  → net burning rate  $\uparrow$  → flame propagation strongly accelerated
- ▶ later transition to (supersonic) detonation?



# Astrophysical scenario

- ▶ thermonuclear burning disrupts WD
- ▶ diffuse cloud of ejecta but no compact remnant → remnant of Tycho's supernova (1572)



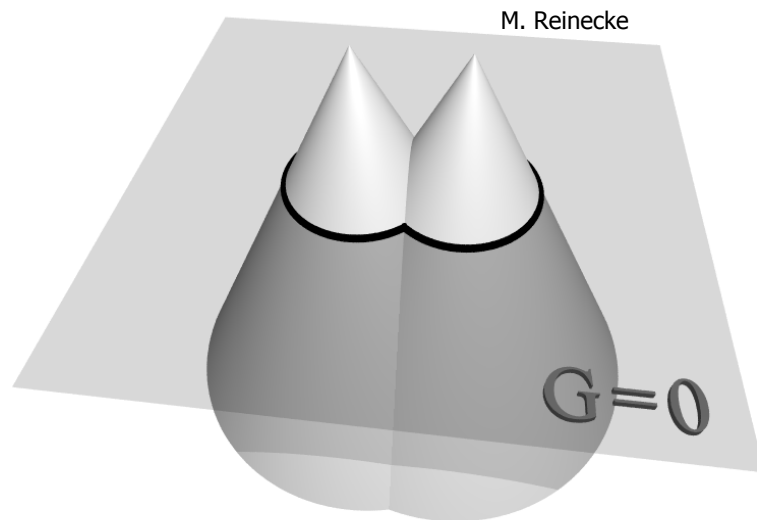


# Numerical techniques

**explosion model** (Reinecke et al., 1999, 2002)

- ▶ hydrodynamics: finite volume approach → PROMETHEUS (Fryxell et al., 1989) implementation of PPM (Colella & Woodward, 1984)
- ▶ turbulence on unresolved scales implemented via sub-grid scale model
- ▶ flame model: WD  $\sim 10^8$  cm structure of flame  $\sim 1$ mm → not resolvable → modeled as discontinuity between fuel and ashes
- ▶ level set method

- ▶ "flamelet regime" of combustion:  
turbulent flame propagation velocity  
determined from sub-grid scale model





# Numerical techniques

- ▶ simplified description of nuclear burning (Reinecke, 2002):
  - ▶ include 5 species:  $^{12}\text{C}$ ,  $^{16}\text{O}$ , "Mg"  $\rightarrow$  intermediate mass elements, "Ni"  $\rightarrow$  iron group elements,  $\alpha$ -particles
  - ▶ at high  $\rho_{\text{fuel}}$  burn to NSE consisting of "Ni" and  $\alpha$
  - ▶ for  $\rho_{\text{fuel}} < 5.25 \times 10^7 \text{ g cm}^{-3}$  burn to "Mg"
  - ▶ for  $\rho_{\text{fuel}} < 1 \times 10^7 \text{ g cm}^{-3}$  burning is no longer followed

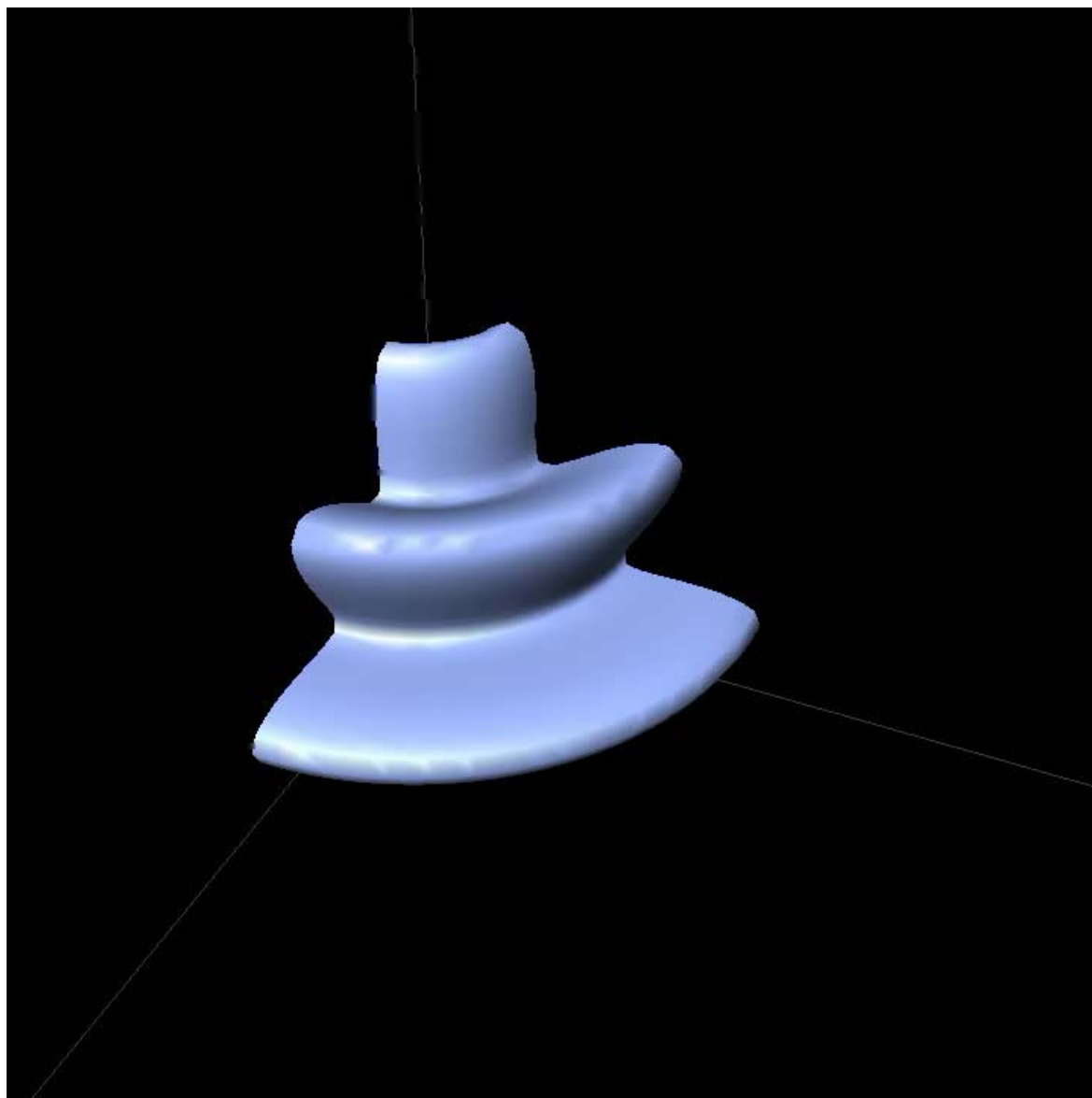
## nucleosynthesis postprocessing (C.Travaglio, 2004, M. Gieseler)

- ▶ record evolution of density, energy, temperature by tracer particles equally distributed in mass shells (Lagrangian component in Eulerian explosion code)
- ▶ use tracer information to perform nuclear postprocessing with nuclear reaction network (384 isotopes) provided by F.K. Thielemann



# Simulation

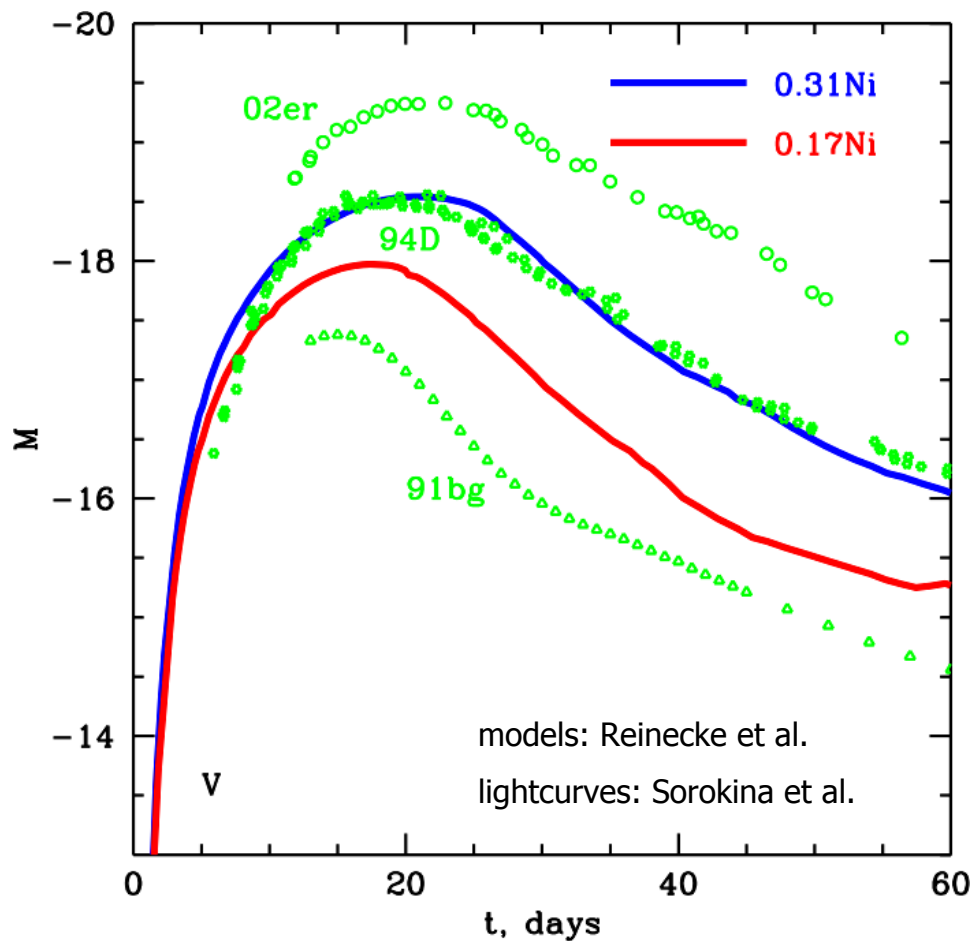
- ▶ isosurface represents flame front





# Status of modeling

- ▶ synthetic light curves:



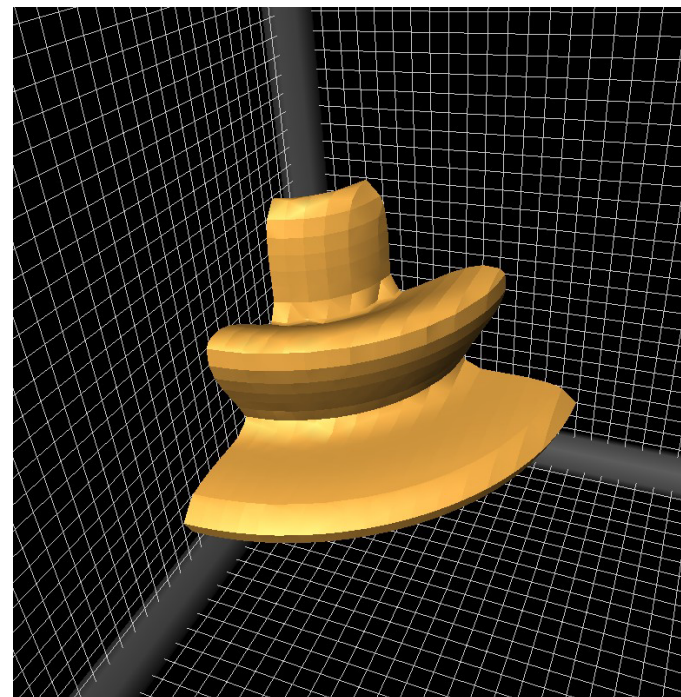
- ▶ "best model" (b30, M. Reinecke, 2003):  $0.4 M_{\odot}$  of  $^{56}\text{Ni}$ ,  $0.7 \text{foe}$



# Simulations

**parameter study with 3D models** (Röpke et al., 2004 and in prep.)

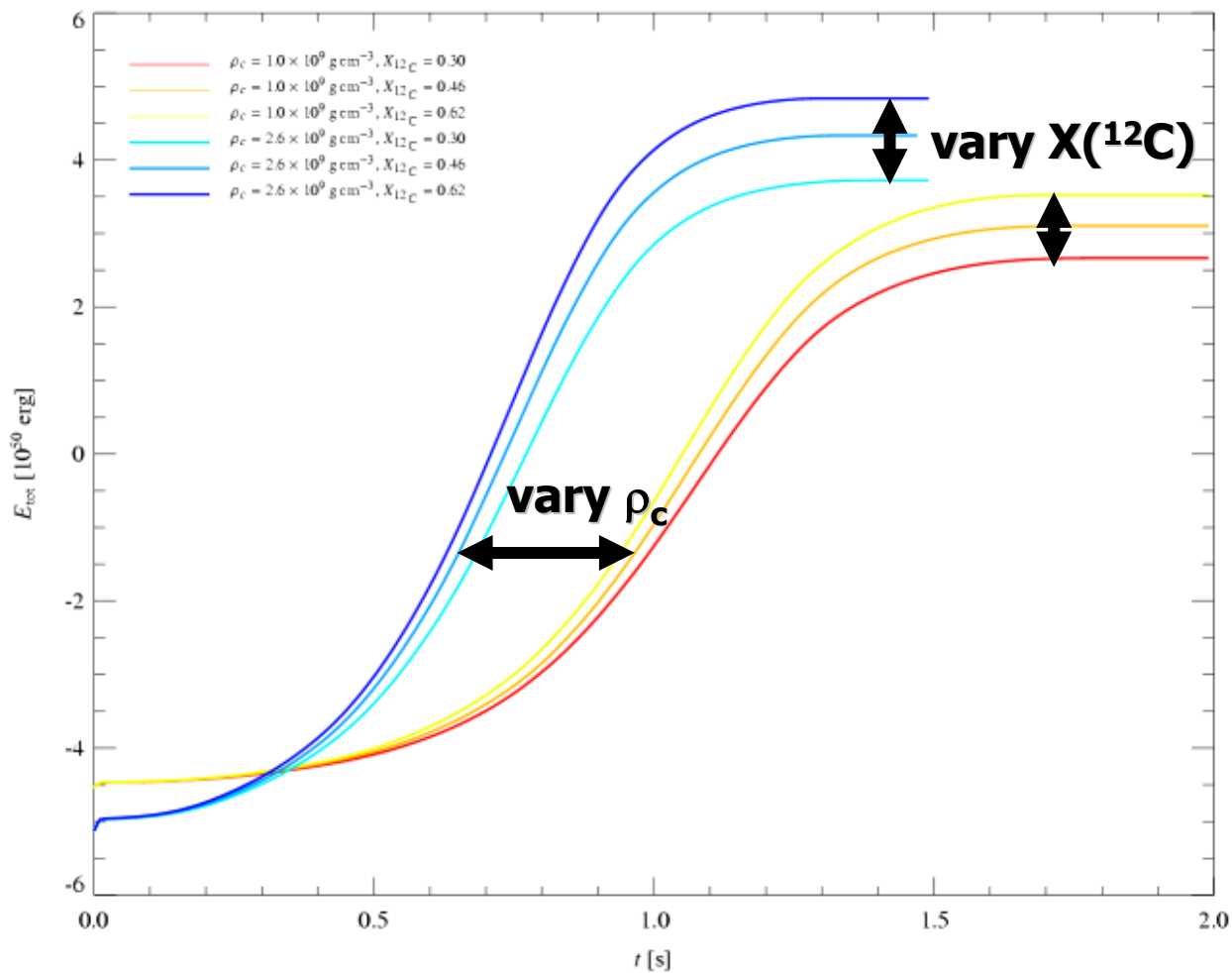
- ▶ Which parameters can account for SN Ia diversity?
  1. progenitor's carbon-to-oxygen ratio  $\rightarrow X(^{12}\text{C}) = 0.3, 0.46, 0.62$
  2. central density at ignition  $\rightarrow \rho_c = [1.0, 2.6] \times 10^9 \text{ g cm}^{-3}$
  3. progenitor's metallicity (Timmes et al. 2003)  $\rightarrow Z = 0.5, 1.0, 3.0 Z_\odot$   
 $\rightarrow ^{22}\text{Ne}$  fraction
  4. rotation
  5. flame ignition ...
- ▶ change parameters independently to study effects (but of course in a realistic scenario interrelated  $\rightarrow$  here: not based on stellar evolution of progenitor)
- ▶ simplified setup





# Results

- ▶ temporal evolution of explosion energy



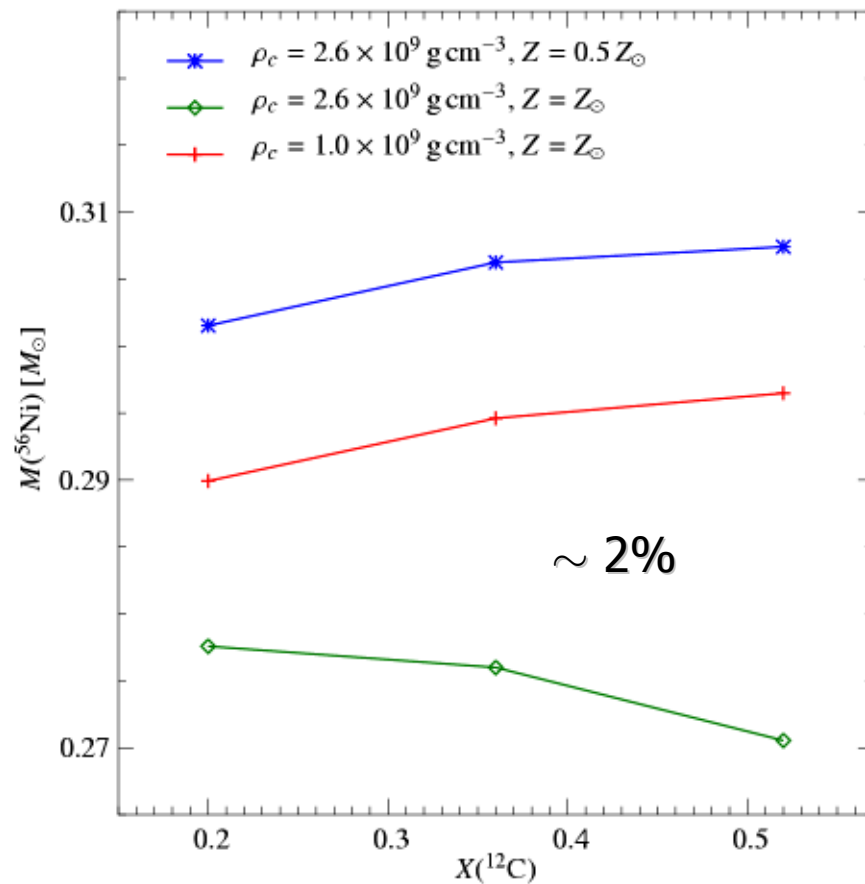
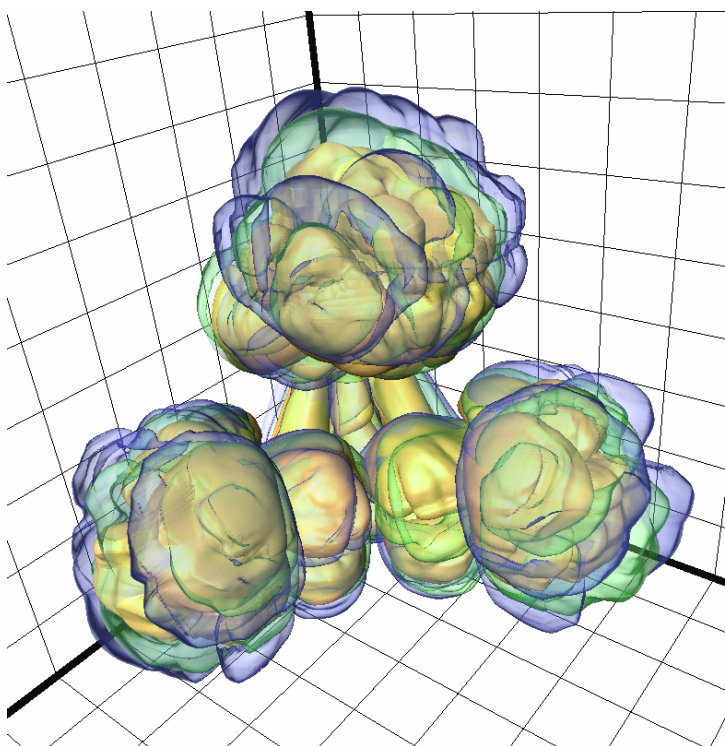




# Progenitor's C/O Ratio

▶ produced  $^{56}\text{Ni}$  mass

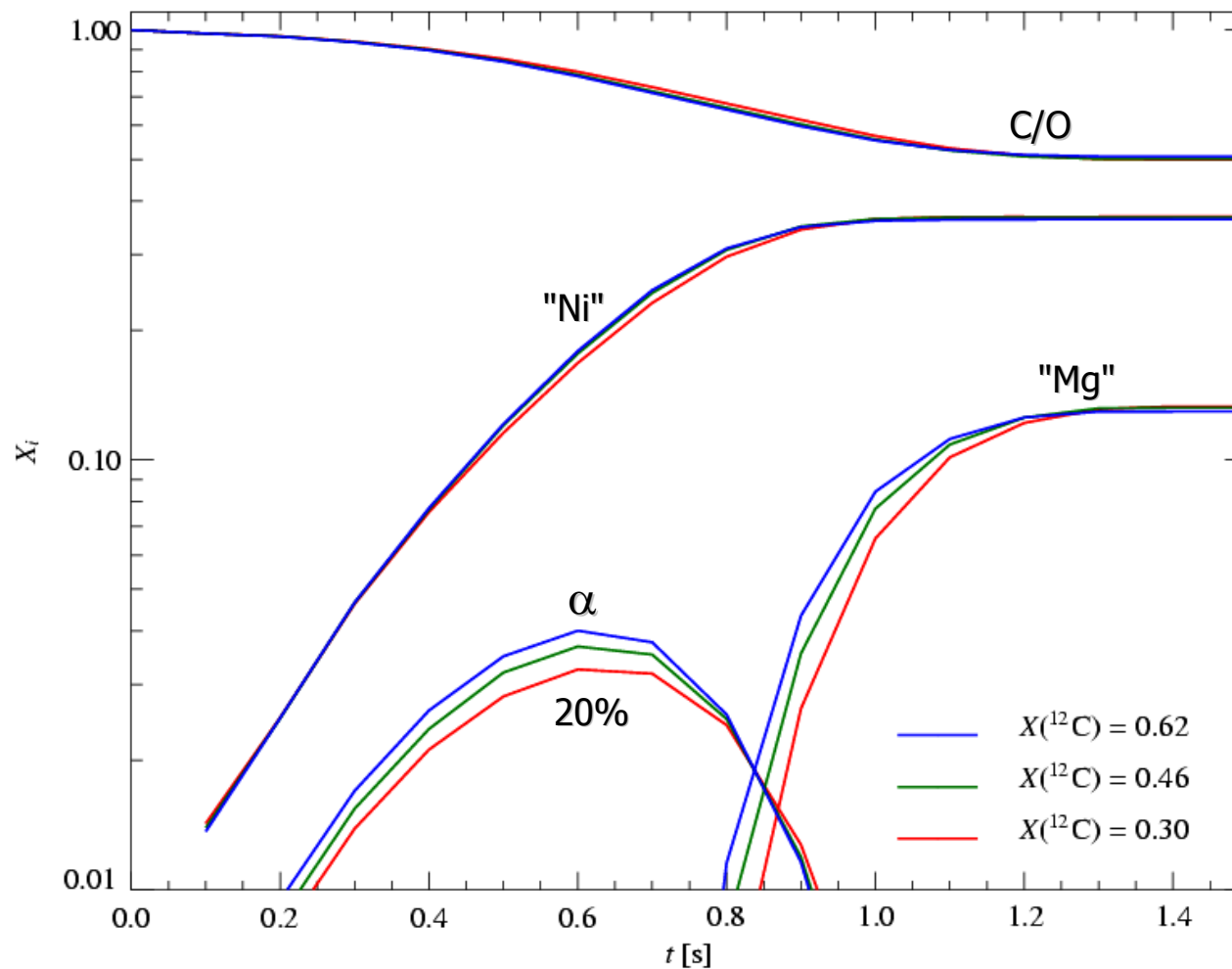
▶ flame front at  $t=1\text{s}$





# Progenitor's C/O Ratio

- ▶ chemical evolution of the explosion models

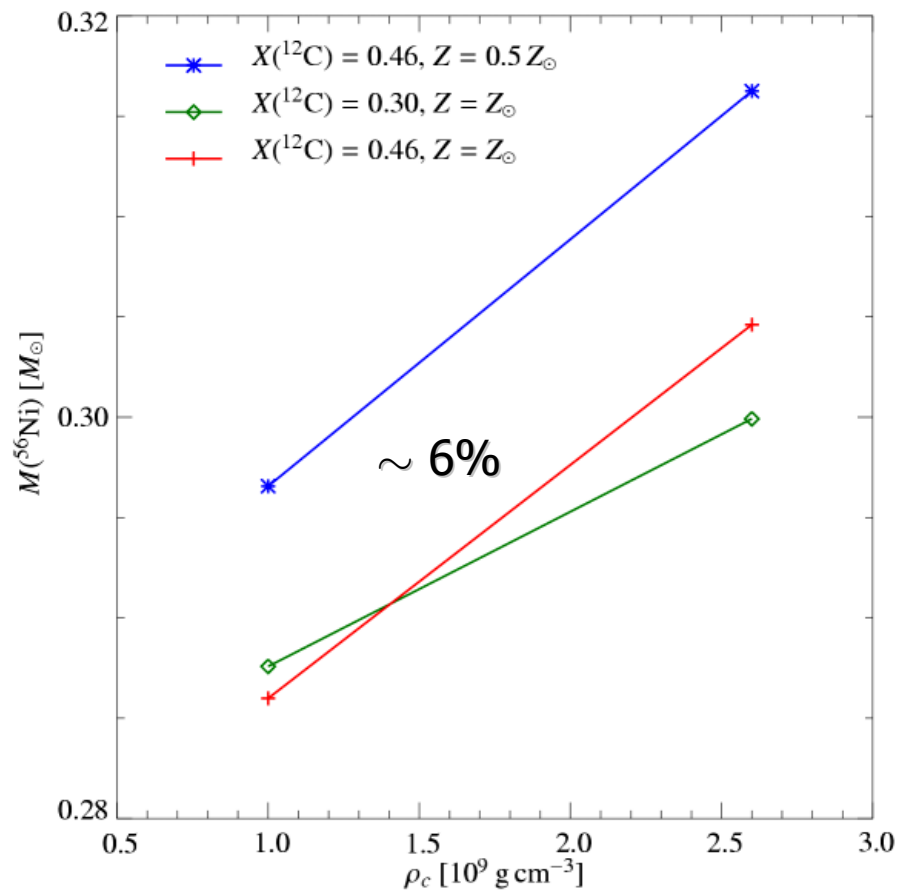
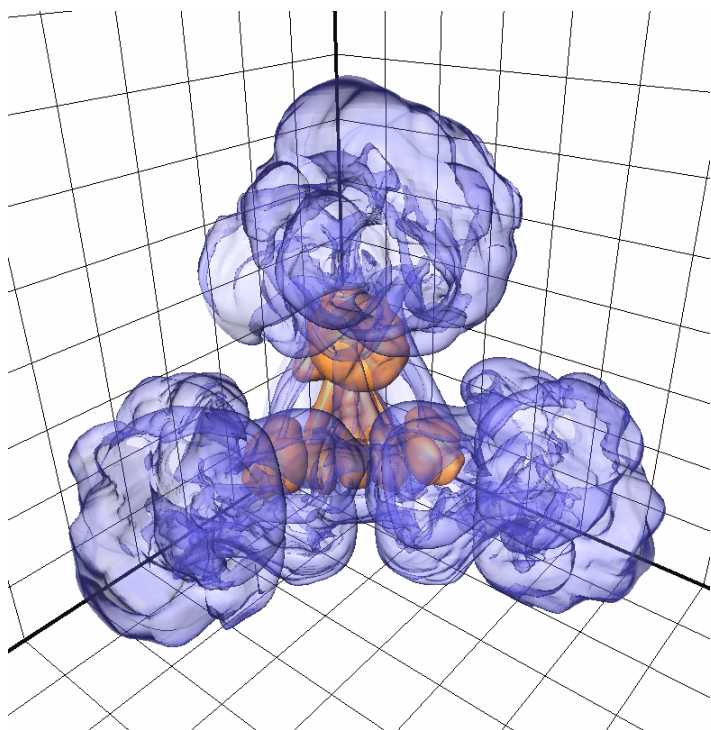




# Central Density

▶ produced  $^{56}\text{Ni}$  mass

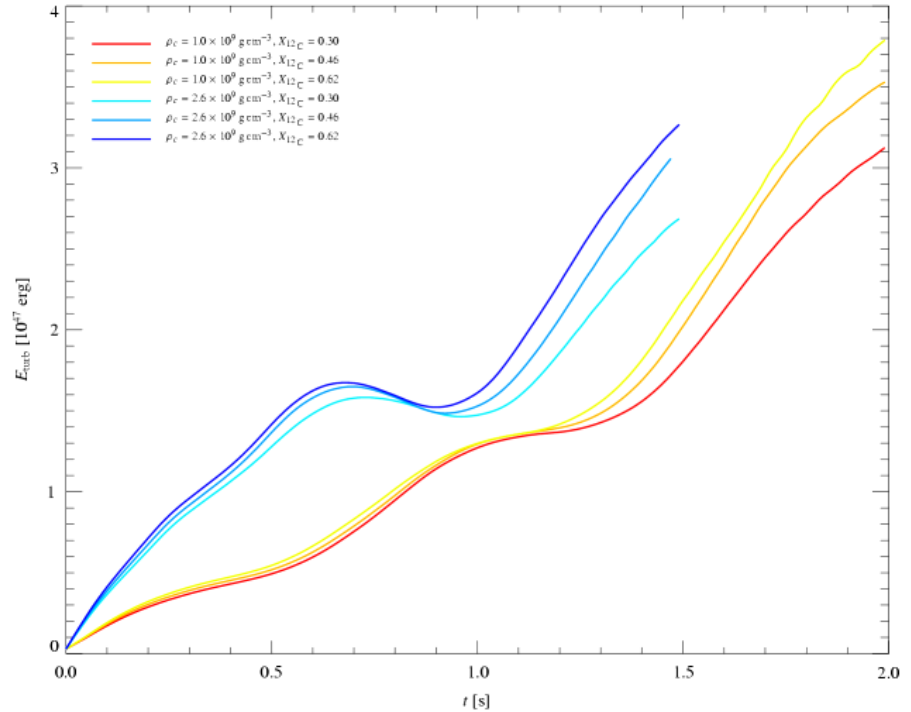
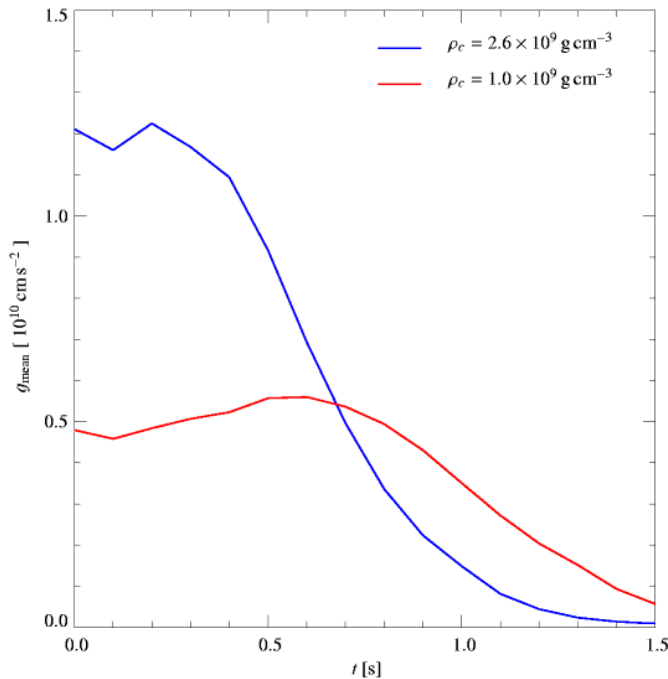
▶ flame fronts at  $t=1\text{s}$





# Central Density

- ▶ gravitational acceleration at mean flame position, turbulent energy

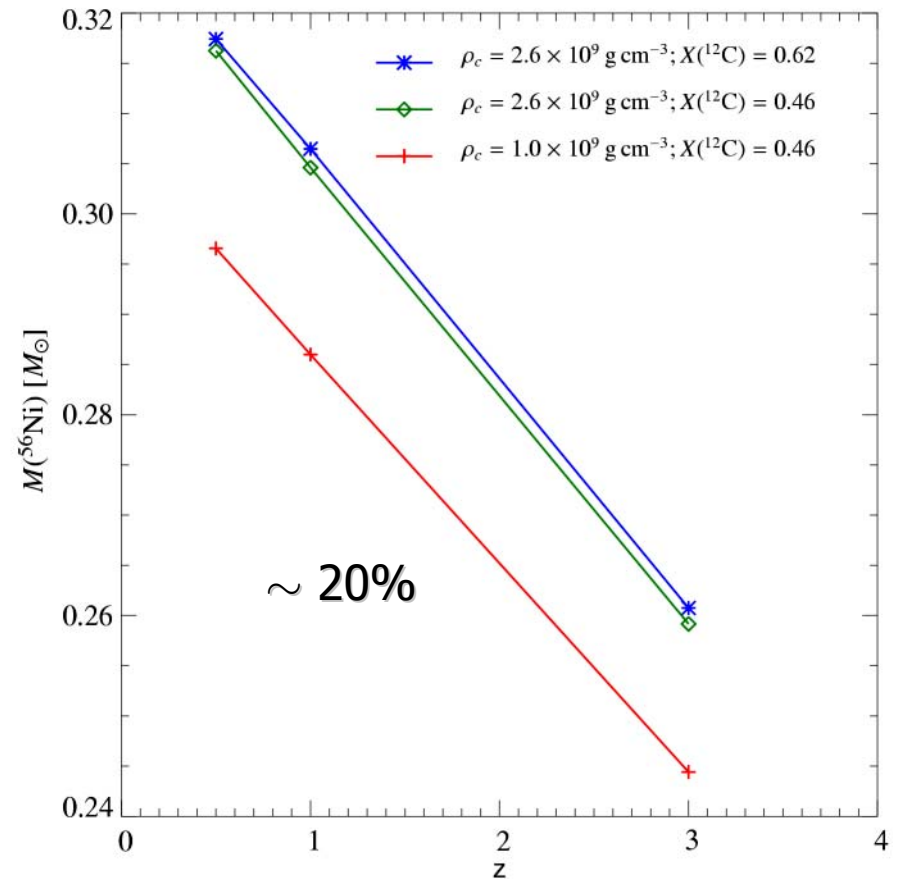


- ▶ two competing effects
  - ▶ with higher  $\rho_c$  increased flame propagation velocities  $\rightarrow$  more material burnt at high densities
  - ▶ at higher densities increased electron capture rates  $\rightarrow$  less  $^{56}\text{Ni}$



# Metallicity

- ▶ produced  $^{56}\text{Ni}$  mass



- ▶ linear relation as analytically predicted by Timmes et al. (2003)



# Results

- ▶ variations of the models due to initial parameters:

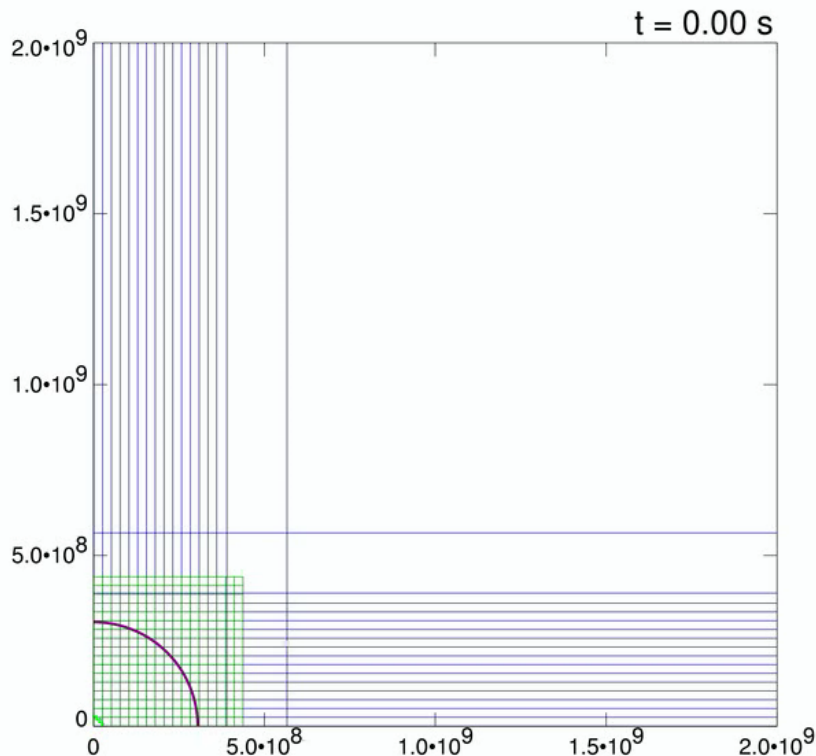
parameter	variation of $^{56}\text{Ni}$ mass ( $\rightarrow$ peak luminosity)	variation of explosion energy (light curve shape)
C/O ratio	a few percent	$\sim 14\%$
central density (preliminary result!)	$\sim 6\%$	$\sim 17\%$
metallicity	$\sim 20\%$	none

- ▶ can account partially for observed diversity
- ▶ no single parameter reproduces the empirically established peak luminosity-light curve shape relation
- ▶ probably combination of parameters (stellar evolution)
- ▶ **synthetic light curves from explosion models needed!**



# Homologous expansion

- ▶ for derivation of synthetic light curves, spectra models must be close to **homologous expansion**
- ▶ previous multi-dimensional explosion models reached to  $\sim 2$  s
- ▶ goal: evolve models to  $\sim 10$  s to reach homologous expansion (F.R., 2004)
- ▶ co-expanding computational grid, tracking outer mass shell of WD instead of static non-uniform grid used so far
- ▶ model meets criteria for homologous expansion after  $\sim 10$  s:
  - ▶  $v(r) \propto r$  (deviation below 5%)
  - ▶  $|\nabla p|, |\nabla \Phi|$  small
  - ▶  $E_{\text{kin}} \gg E_{\text{int}}, E_{\text{grav}}$



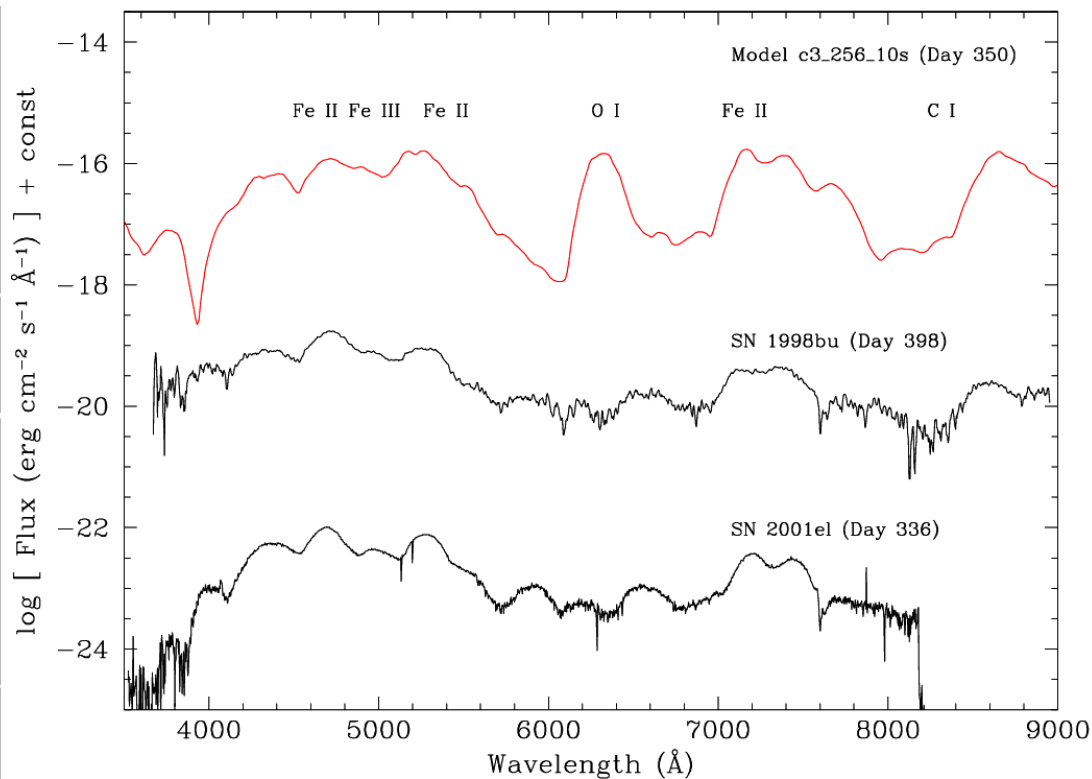
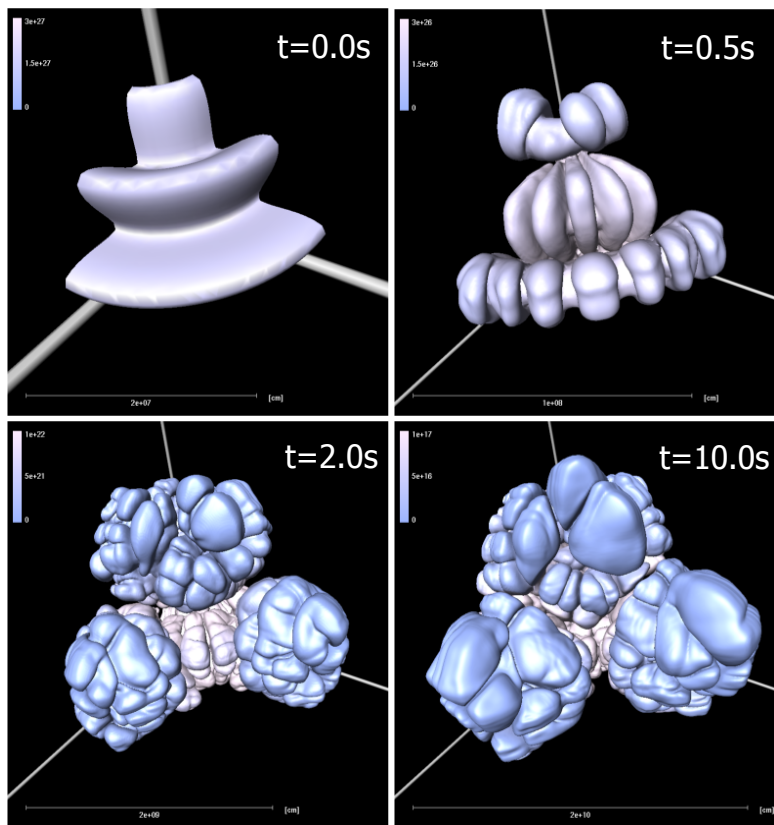


# Nebular spectra

▶ 3d example



spectrum at day  $\sim 350$  (Kozma et al., in prep.)

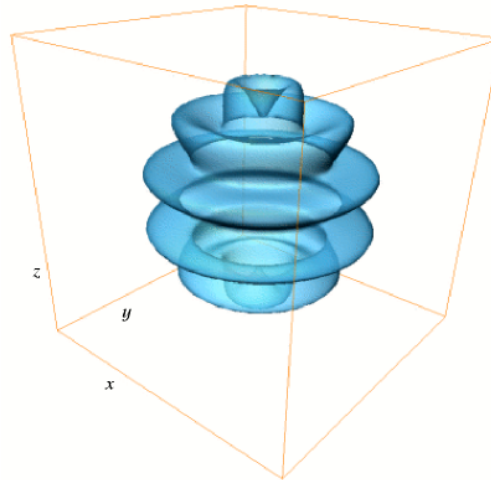
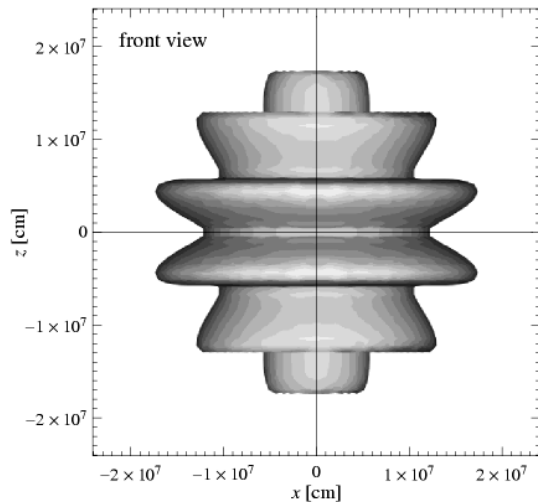




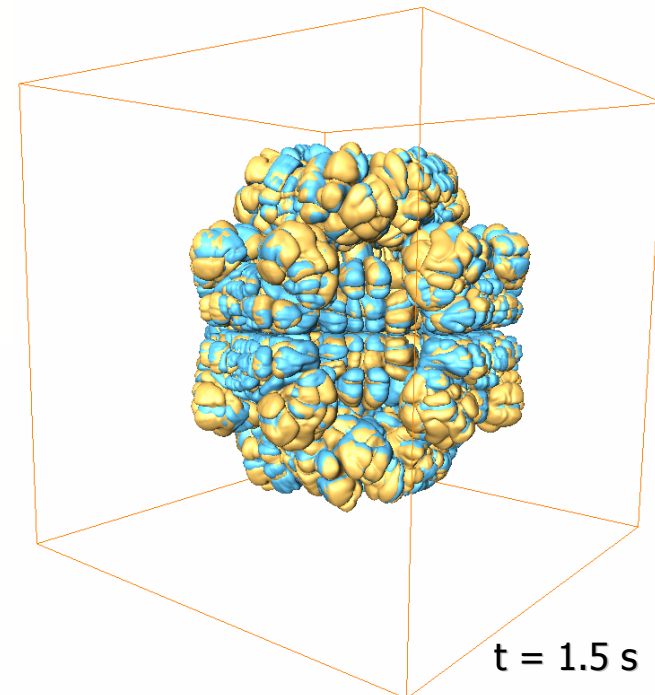


# Full-star models

- ▶ **purpose:** assess octant-symmetry in previous simulations by comparison with full-star model
- ▶ initial condition corresponds to mirrored c3-model (Reinecke, 1999,2002)



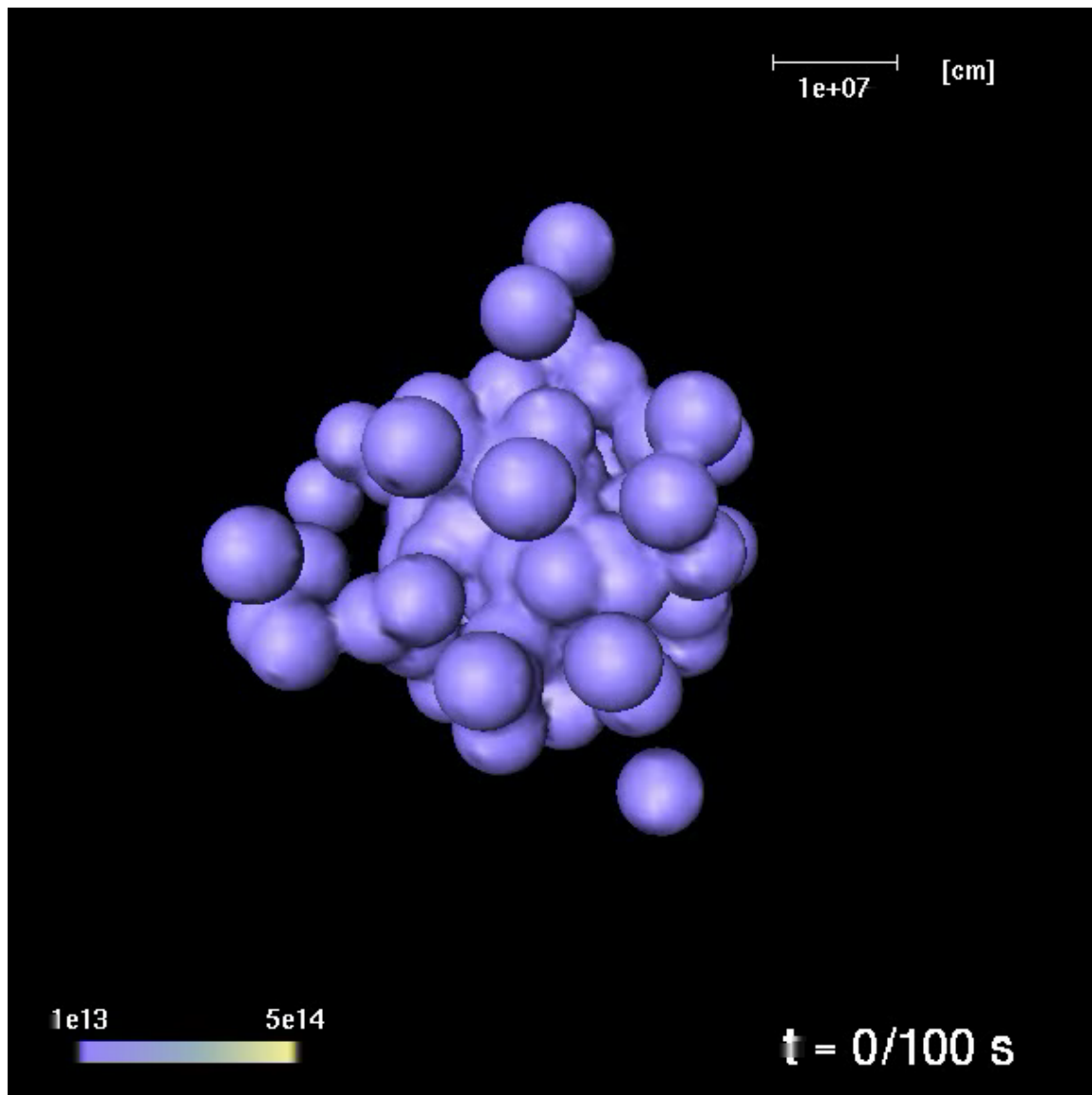
- ▶ only small differences between single-octant (yellow) and full-star (blue) model
- ▶ no surprising features by abolishing artificial mirror-symmetry





# Full star models

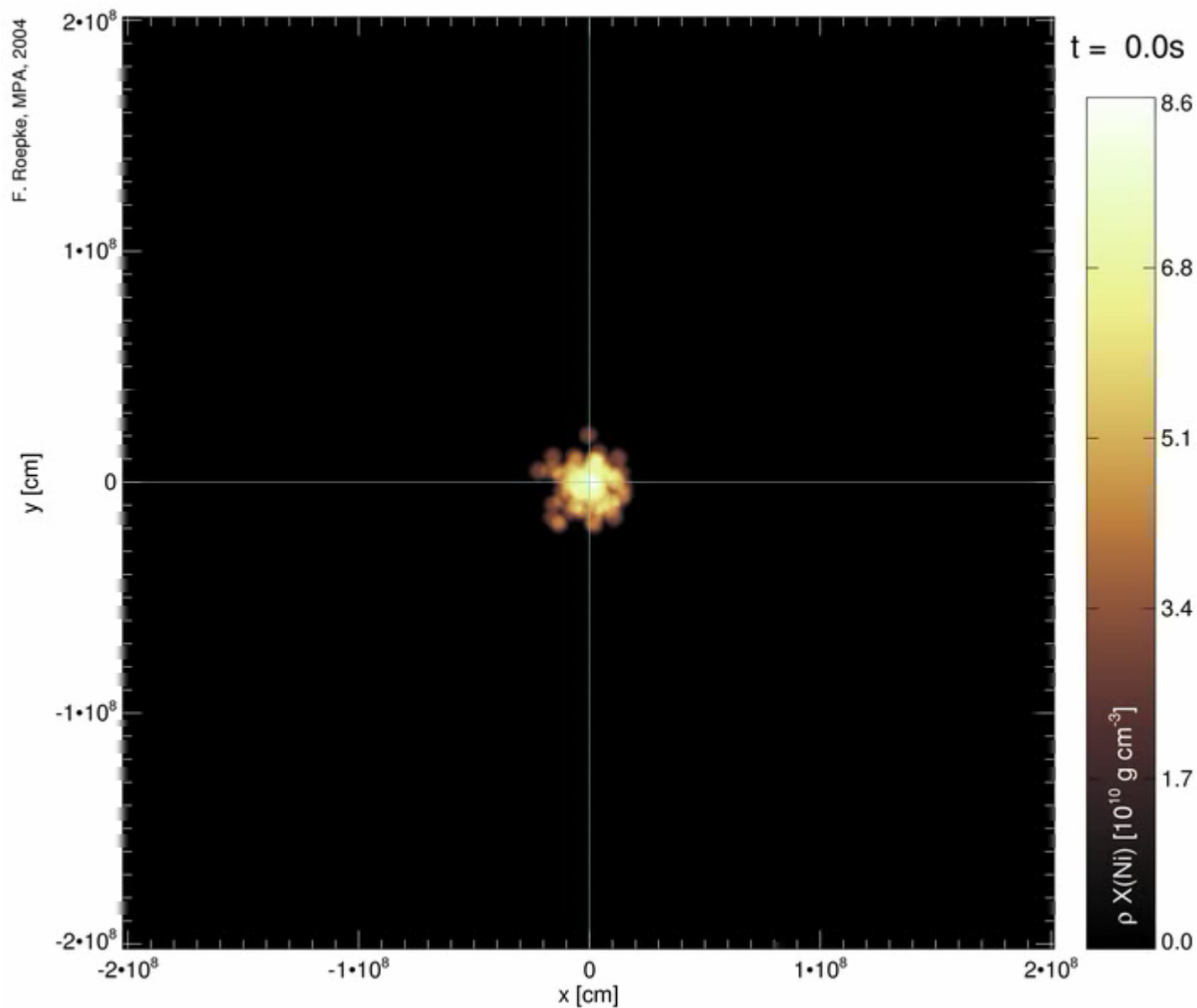
- ▶ "foamy" initial flame configuration
- ▶ anisotropic, asymmetric flame shape
- ▶ center of initial flame  $\sim 13$  km misaligned with WD center





# Asymmetries

- ▶ distribution of "nickel"





deflagration models can explain many observational features but need improvements

- ▶ large simulation in preparation
- ▶ cure low velocity unburnt material problem:
  - ▶ improve sub-grid scale model (W. Schmidt, U Würzburg)
  - ▶ test initial flame configurations
  - ▶ distributed burning in late phases
  - ▶ delayed detonation?
  - ▶ ...
- ▶ implement electron captures → study variation of central density
- ▶ improve initial models
- ▶ improve description of nuclear burning in explosion models
- ▶ (...)